

Recent results from the COMPASS hadron program

Precision studies of light mesons

Sebastian Uhl
On Behalf of the COMPASS Collaboration

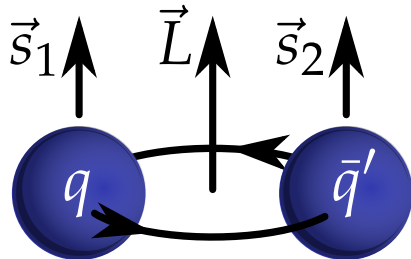


Physik Department E18
Technische Universität München



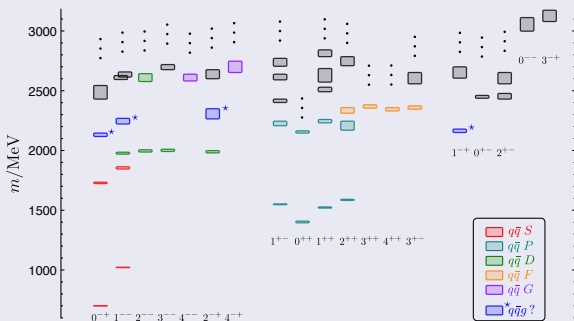
QCD@Work 2014 19.06.2014

- Quark spins couple to total intrinsic spin $S = 0$ (singlet) or 1 (triplet)
- Relative orbital angular momentum \vec{L} and total spin \vec{S} couple to meson spin $\vec{J} = \vec{L} + \vec{S}$
- parity $P = (-1)^{L+1}$
- charge conjugation $C = (-1)^{L+S}$
- forbidden J^{PC} :
 $0^{--}, 0^{+-}, 1^{-+}, 2^{+-}, 3^{-+}, \dots$



Naïve Constituent Quark Model

- Quark spins couple to total spin $S = 0$ (singlet) or 1 (triplet)
- Relative orbital angular momentum and total spin \vec{S} couple to meson spin $\vec{J} = \vec{L} + \vec{S}$
- parity $P = (-1)^{L+1}$
- charge conjugation $C = (-1)^{L+S}$
- forbidden J^{PC} : $0^{--}, 0^{+-}, 1^{-+}, 2^{+-}, 3^{--}$



J.Dudek, Phys.Rev.D84 (2011) 074023

Beyond the CQM: i.e. lattice QCD

isovector states

- prediction of states outside CQM
- hybrid candidate ($q\bar{q}g$)
- lightest candidate in 1^{-+}

in addition:

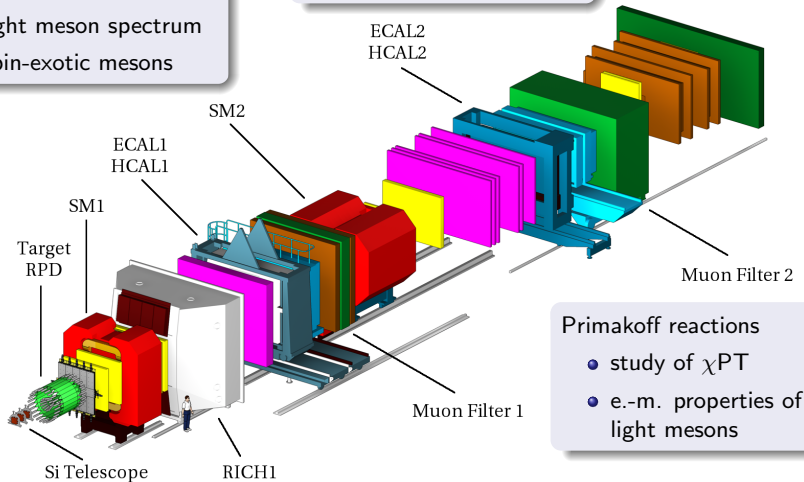
- (isoscalar) glueballs
- pure glue
- quantum numbers J^{PC} : $0^{++}, \dots$

diffractive dissociation

- light meson spectrum
- spin-exotic mesons

central production

- glue-rich environment
- scalar resonances



Primakoff reactions

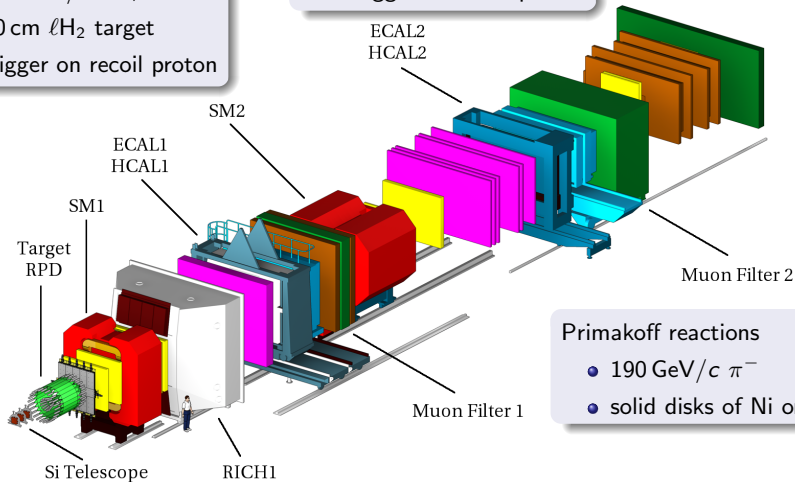
- study of χ PT
- e.-m. properties of light mesons

diffractive dissociation

- 190 GeV/c π^- , K^-
- 40 cm ℓH_2 target
- trigger on recoil proton

central production

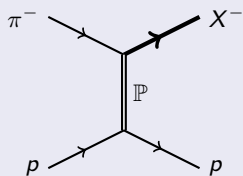
- 190 GeV/c p
- 40 cm ℓH_2 target
- trigger on recoil proton



Primakoff reactions

- 190 GeV/c π^-
- solid disks of Ni or Pb

diffractive dissociation

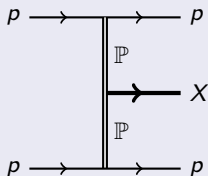


$$0.1 < t' < 1 \text{ GeV}^2/c^2$$

X^- :

- $\pi^- \pi^- \pi^+$
- $\pi^- \pi^0 \pi^0$
- $\pi^- \eta$
- $\pi^- \eta'$

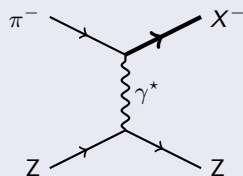
central production



X :

- $\pi^- \pi^+$
- $K^- K^+$

Primakoff reactions

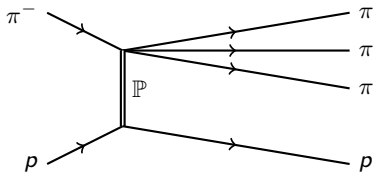


$$t' < 0.001 \text{ GeV}^2/c^2$$

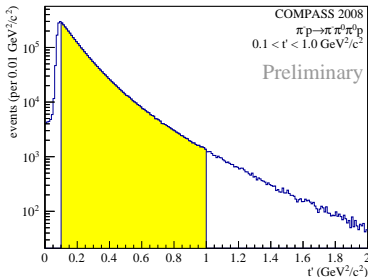
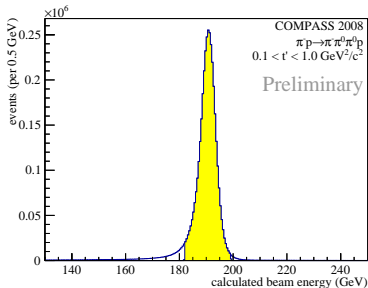
X^- :

- $\pi^- \pi^- \pi^+$
- $\pi^- \pi^0 \pi^0$
- $\pi^- \gamma$

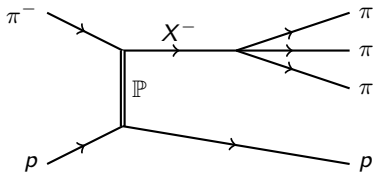
$$\pi^- p \rightarrow (3\pi)^- p$$



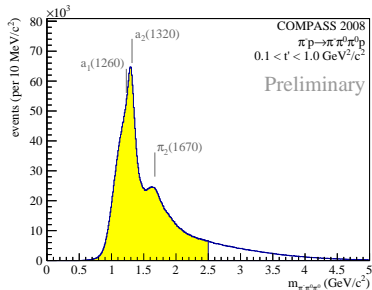
- exclusive $\pi^- p \rightarrow (3\pi)^- p$ reaction
- two channels in COMPASS
 - $\pi^- \pi^- \pi^+$
 - $\pi^- \pi^0 \pi^0$
- high- t' region: $0.1 < t' < 1.0 \text{ GeV}^2/c^2$



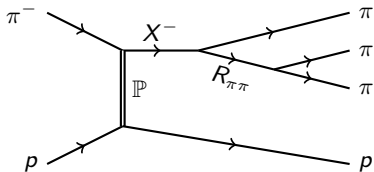
$$\pi^- p \rightarrow (3\pi)^- p$$



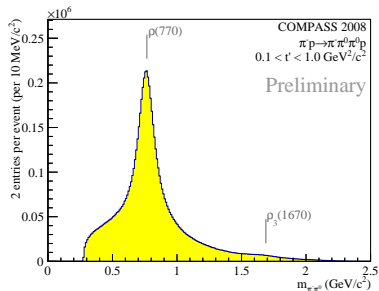
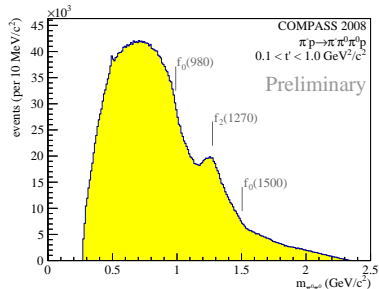
- exclusive $\pi^- p \rightarrow (3\pi)^- p$ reaction
- two channels in COMPASS
 - $\pi^- \pi^- \pi^+$
 - $\pi^- \pi^0 \pi^0$
- high- t' region: $0.1 < t' < 1.0 \text{ GeV}^2/c^2$
- huge dataset
 - 50 million $\pi^- \pi^- \pi^+$ events
 - 3.5 million $\pi^- \pi^0 \pi^0$ events

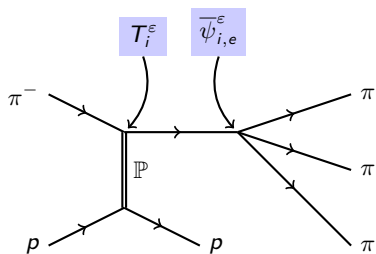


$$\pi^- p \rightarrow (3\pi)^- p$$

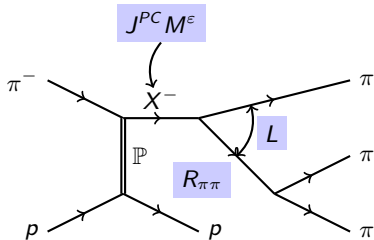


- exclusive $\pi^- p \rightarrow (3\pi)^- p$ reaction
- two channels in COMPASS
 - $\pi^- \pi^- \pi^+$
 - $\pi^- \pi^0 \pi^0$
- high- t' region: $0.1 < t' < 1.0 \text{ GeV}^2/c^2$
- huge dataset
 - 50 million $\pi^- \pi^- \pi^+$ events
 - 3.5 million $\pi^- \pi^0 \pi^0$ events
- partial-wave analysis using isobar model



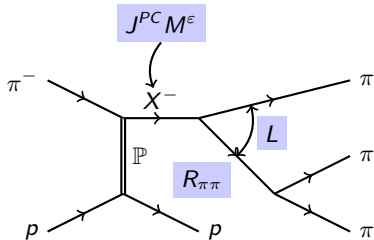


- process can be factorized
 - production T_i^ε
 - decay $\overline{\psi}_{i,e}^\varepsilon$



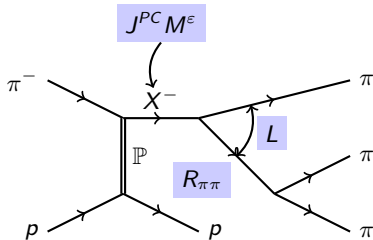
- process can be factorized
 - production T_i^ε
 - decay $\bar{\psi}_{i,e}^\varepsilon$

- 88 waves
 - 80 with positive reflectivity
 - 7 with negative reflectivity
 - flat wave
- spin J up to 6
- angular momentum L between bachelor π and isobar up to 6
- $(\pi\pi)_S$
- $f_0(980)$
- $f_2(1270)$
- $f_0(1500)$
- $\rho(770)$
- $\rho_3(1690)$
- for $\pi^- \pi^- \pi^+$ all isobars are $\pi^- \pi^+$
- for $\pi^- \pi^0 \pi^0$ split to
 - $\pi^- \pi^0$: ρ, ρ_3
 - $\pi^0 \pi^0$: $(\pi\pi)_S, 2 \times f_0, f_2$



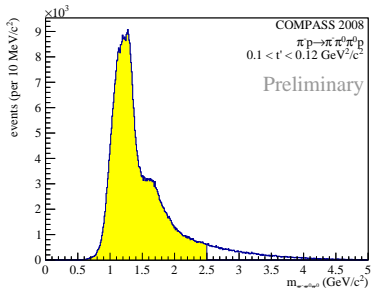
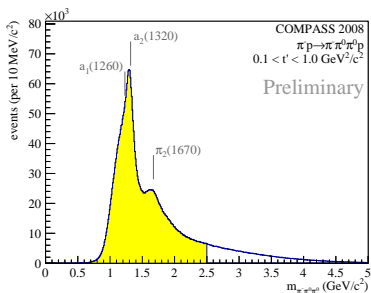
- process can be factorized
 - production T_i^ϵ
 - decay $\bar{\psi}_{i,e}^\epsilon$
- two-step approach
- ① fit in mass bins
 - extract production amplitudes T_i^ϵ

- 88 waves
 - 80 with positive reflectivity
 - 7 with negative reflectivity
 - flat wave
- spin J up to 6
- angular momentum L between bachelor π and isobar up to 6
- $(\pi\pi)_S$
- $f_0(980)$
- $f_2(1270)$
- $f_0(1500)$
- $\rho(770)$
- $\rho_3(1690)$
- for $\pi^-\pi^-\pi^+$ all isobars are $\pi^-\pi^+$
- for $\pi^-\pi^0\pi^0$ split to
 - $\pi^-\pi^0$: ρ, ρ_3
 - $\pi^0\pi^0$: $(\pi\pi)_S, 2 \times f_0, f_2$

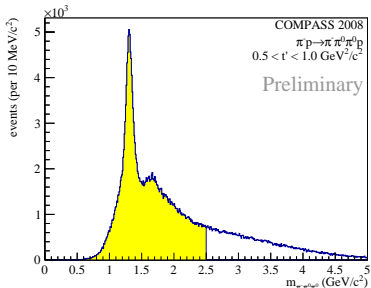


- process can be factorized
 - production T_i^ϵ
 - decay $\overline{\psi}_{i,e}^\epsilon$
- two-step approach
- ① fit in mass bins
 - extract production amplitudes T_i^ϵ
- ② fit of mass dependence of spin-density matrix

- 88 waves
 - 80 with positive reflectivity
 - 7 with negative reflectivity
 - flat wave
- spin J up to 6
- angular momentum L between bachelor π and isobar up to 6
- $(\pi\pi)_S$
- $f_0(980)$
- $f_2(1270)$
- $f_0(1500)$
- $\rho(770)$
- $\rho_3(1690)$
- for $\pi^-\pi^-\pi^+$ all isobars are $\pi^-\pi^+$
- for $\pi^-\pi^0\pi^0$ split to
 - $\pi^-\pi^0$: ρ, ρ_3
 - $\pi^0\pi^0$: $(\pi\pi)_S, 2 \times f_0, f_2$

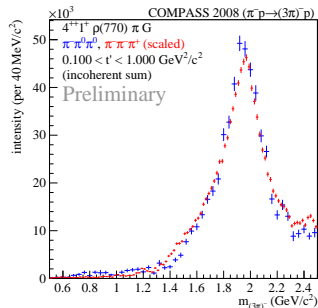
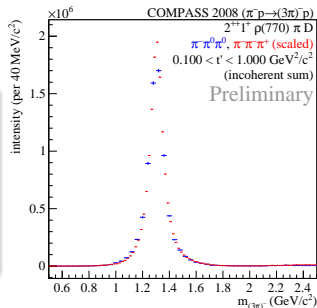
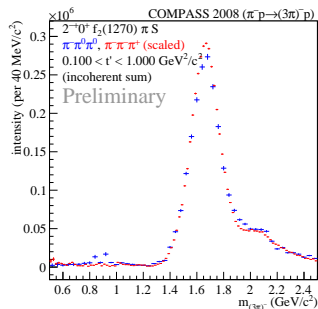
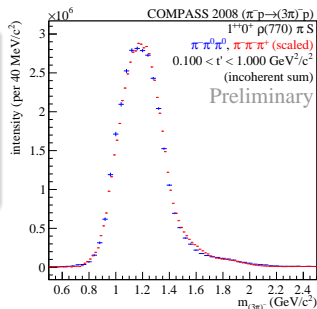


- mass spectrum depends on t'
- at low- t' ($0.1 < t' < 0.2 \text{ GeV}^2/c^2$)
 - a_1 (1260) dominates low-mass region
 - a_2 (1320) hardly visible
- at high- t' ($0.5 < t' < 1.0 \text{ GeV}^2/c^2$)
 - a_1 (1260) visible only as a shoulder
 - a_2 (1320) dominant
- no changes above π_2 (1670) region
- binning of data also in t'
 - 11 bins for $\pi^- \pi^- \pi^+$
 - 8 bins for $\pi^- \pi^0 \pi^0$



major waves

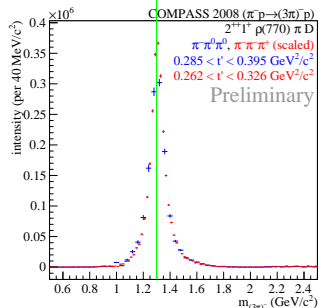
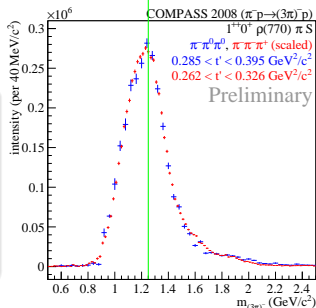
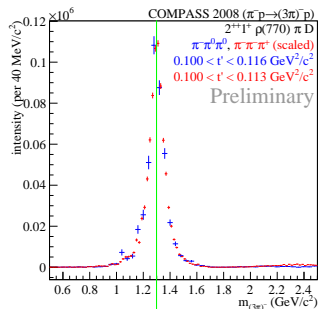
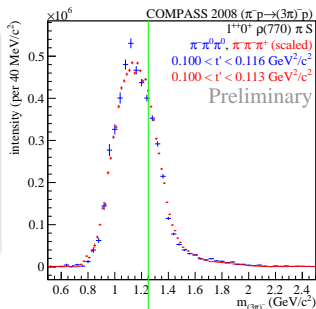
- $1^{++}0^+ \rho(770) \pi S$
- $2^{-+}0^+ f_2(1270) \pi S$
- $2^{++}1^+ \rho(770) \pi D$
- $4^{++}1^+ \rho(770) \pi G$



- $\pi^- \pi^0 \pi^0$
- $\pi^- \pi^- \pi^+$ (scaled)
- scaled for each plot
- agreement between channels

different t' bins

- $1^{++}0^+\rho(770)\pi S$
- $2^{++}1^+\rho(770)\pi D$
- position of peak in $1^{++}0^+$ changes
- a_2 not affected



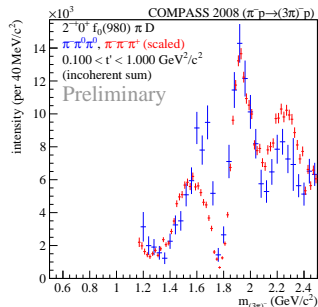
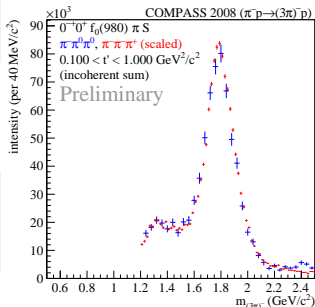
- $\pi^-\pi^0\pi^0$
- $\pi^-\pi^-\pi^+$ (scaled)
- scaled for each plot
- agreement between channels

$f_0(980)$ isobar

- $0^{-+}0^{+} f_0(980) \pi S$
- $2^{-+}0^{+} f_0(980) \pi D$

- stable fits also for non- ρ isobars

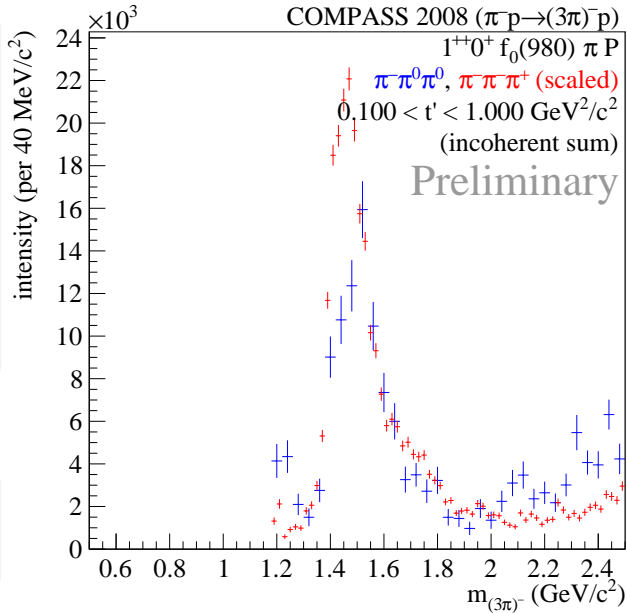
- $\pi^{-} \pi^{0} \pi^{0}$
- $\pi^{-} \pi^{-} \pi^{+}$ (scaled)
- scaled for each plot



$f_0(980)$ isobar

- $0^{-+}0^{+} f_0(980) \pi S$
- $2^{-+}0^{+} f_0(980) \pi D$
- $1^{++}0^{+} f_0(980) \pi P$
- stable fits also for non- ρ isobars
- **first observation of a signal in $1^{++}0^{+} f_0(980) \pi P$ around $1.4 \text{ GeV}/c^2$**

- $\pi^{-} \pi^0 \pi^0$
- $\pi^{-} \pi^{-} \pi^{+}$ (scaled)
- scaled for each plot



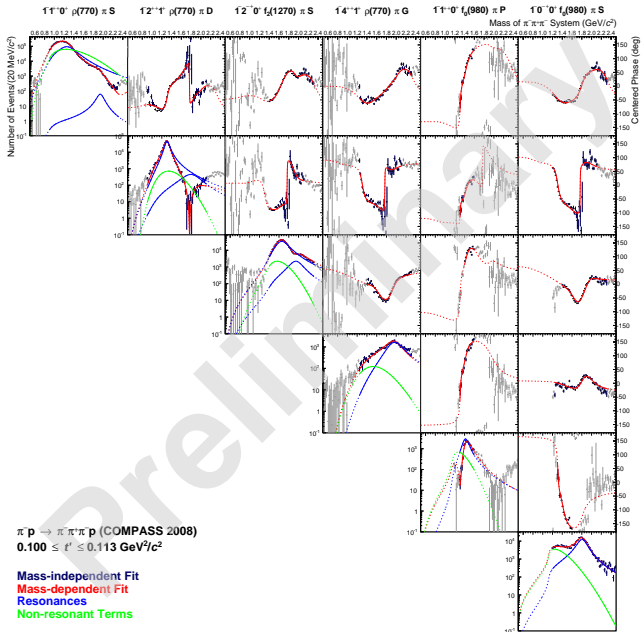
Model

- for the moment six waves
 - four major waves and two waves with $f_0(980)$ isobar
- describe spin-density sub-matrix with Breit-Wigner functions

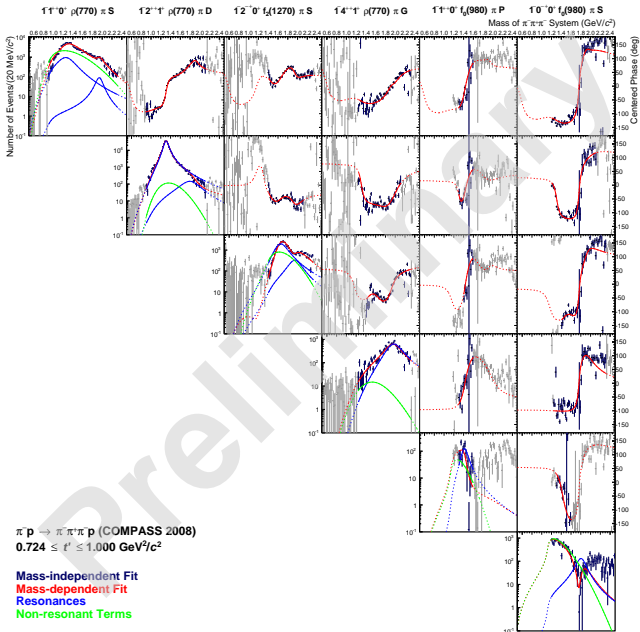
$1^{++}0^+ \rho(770) \pi S$	two BW:	$a_1(1260), a'_1$
$2^{-+}0^+ f_2(1270) \pi S$	two BW:	$\pi_2(1670), \pi_2(1880)$
$2^{++}1^+ \rho(770) \pi D$	two BW:	$a_2(1320), a'_2$
$4^{++}1^+ \rho(770) \pi G$	one BW:	$a_4(2040)$
$1^{++}0^+ f_0(980) \pi P$	one BW:	$a_1(1420)$
$0^{-+}0^+ f_0(980) \pi S$	one BW:	$\pi(1800)$

- non-resonant term for each wave
- 352 free parameters, around 15 000 data points

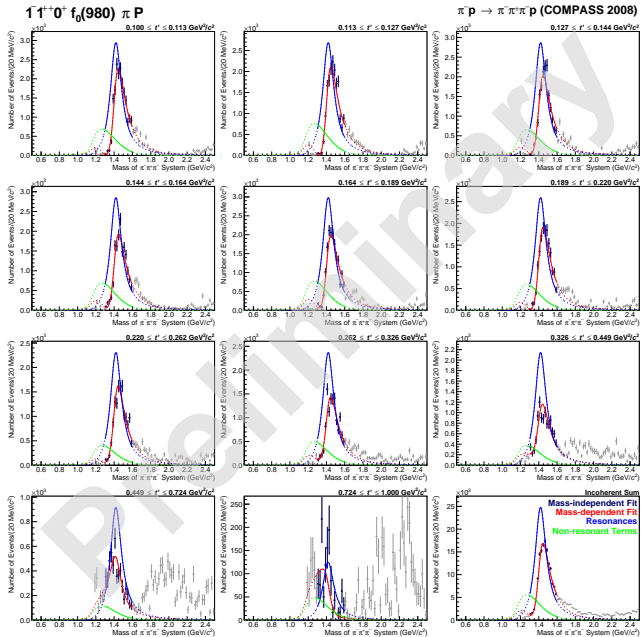
Mass-dependent fit for $\pi^- \pi^- \pi^+$



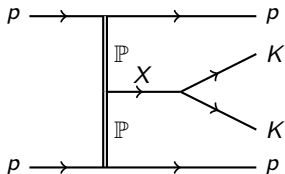
Mass-dependent fit for $\pi^- \pi^- \pi^+$



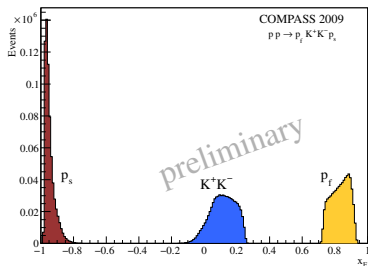
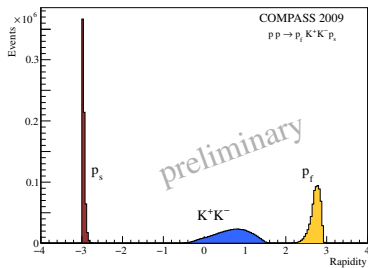
Mass-dependent fit of $1^{++}0^{+} f_0(980) \pi P$

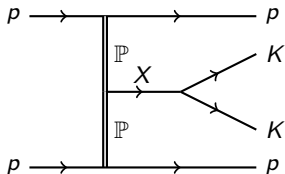


	J^{PC}	mass range (MeV/ c^2)	width range (MeV/ c^2)	PDG	
major waves					
a_1 (1260)	1^{++}	1260 – 1290	360 – 420	1230 ± 40	250 – 400
a_2 (1320)	2^{++}	1312 – 1315	108 – 115	$1318.3^{+0.5}_{-0.6}$	$105^{+1.6}_{-1.9}$
π_2 (1670)	2^{-+}	1635 – 1663	265 – 305	1672.2 ± 3.0	260 ± 9
a_4 (2040)	4^{++}	1928 – 1959	360 – 400	1996^{+10}_{-9}	255^{+28}_{-24}
π (1800)	0^{-+}	1790 – 1807	212 – 230	1812 ± 12	208 ± 12
π_2 (1880)	2^{-+}	1900 – 1990	210 – 390	1895 ± 16	235 ± 34
states not in PDG summary table					
a_1 (1930)	1^{++}	1920 – 2000	155 – 255	1930^{+30}_{-70}	155 ± 45
a_2 (1950)	2^{++}	1740 – 1890	300 – 555	1950^{+30}_{-70}	180^{+30}_{-70}
a_1 (1420)	1^{++}	1412 – 1422	130 – 150		

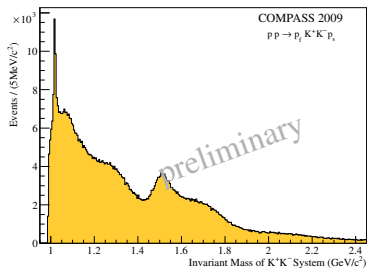


- exclusive $\pi^- p \rightarrow pK^-K^+p$ reaction
- rapidity gap to identify central system



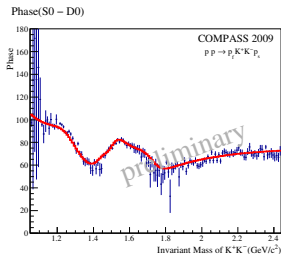
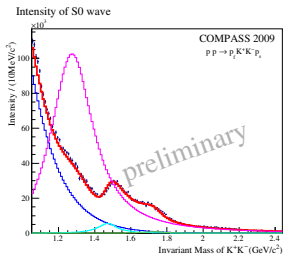


- exclusive $\pi^- p \rightarrow pK^-K^+p$ reaction
- rapidity gap to identify central system
- disentangle K^-K^+ mass spectrum
 - using PWA
 - identify isoscalar resonances
- further possible final states:
 $\pi^- \pi^+, \pi^0 \pi^0, \eta \eta, \dots$



Mass-dependent fit for K^-K^+

- focus on two most prominent waves
- resonances described by dynamic-width relativistic Breit-Wigner functions
- coherent background

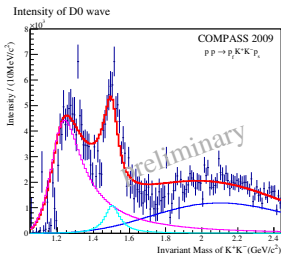


resonances in D_0^-

- f_2 (1270)
- f_2' (1525)

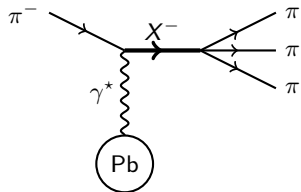
resonances in S_0^-

- f_0 (1500)
- f_0 (1710)
- f_0 (1370) as broad state
- required to account for phase wrt. D_0^-



- decay $X \rightarrow \pi\gamma$ allows access to electromagnetic transitions
 - $a_2(1320) \rightarrow \pi\gamma$ magnetic quadrupole moment
 - $\pi_2(1670) \rightarrow \pi\gamma$ electric quadrupole moment
- direct measurement of $\pi\gamma$ decay is experimentally challenging
- inverse process: scattering of a π off a Coulomb potential
 - quasi-real photons in the vicinity of heavy nuclei
- cross-section for Primakoff produced X

$$\sigma_{\text{Primakoff},X} \propto \Gamma_0(X \rightarrow \pi\gamma)$$



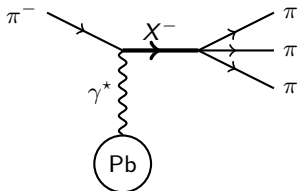
- decay $X \rightarrow \pi\gamma$ allows access to electromagnetic transitions
 - $a_2(1320) \rightarrow \pi\gamma$ magnetic quadrupole moment
 - $\pi_2(1670) \rightarrow \pi\gamma$ electric quadrupole moment
- direct measurement of $\pi\gamma$ decay is experimentally challenging
- inverse process: scattering of a π off a Coulomb potential
 - quasi-real photons in the vicinity of heavy nuclei
- cross-section for Primakoff produced X

$$\sigma_{\text{Primakoff},X} \propto \Gamma_0(X \rightarrow \pi\gamma)$$

identify Primakoff contribution

- Primakoff produced states have spin projection $M = 1$
- cross-section for diffractively produced states

$$\sigma \propto t'^M e^{-bt'}$$
- at small t' $M = 1$ states are predominantly Primakoff produced
- partial-wave analysis to identify the $M = 1$ final states
- count number of final states to get cross-section



measurements

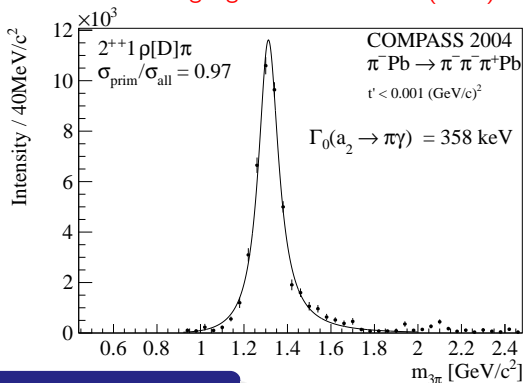
- SELEX (2001)
($284 \pm 25 \pm 25$) keV
- E272 (1982)
(295 ± 60) keV
- May et al. (1977)
(0.46 ± 0.11) MeV

- COMPASS
($358 \pm 6 \pm 42$) keV

theoretical predictions

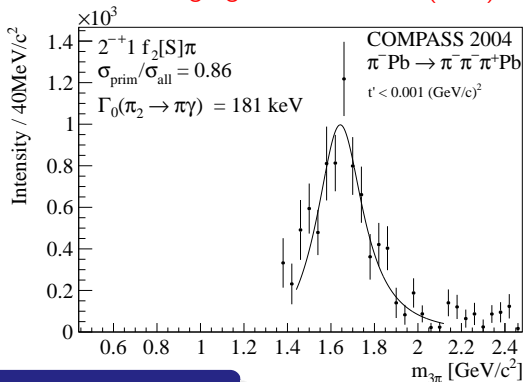
- Vector Meson Dominance Model
375 keV (Rosner, 1981)
- Relativistic Quark Mode
324 keV (Aznauryan and Oganesyan, 1988)
- Covariant Oscillator Quark Model
235 keV (Ishida et al., 1989)

EPJ A Highlight: EPJ A 50: 79 (2014)



first measurement

EPJ A Highlight: EPJ A 50: 79 (2014)

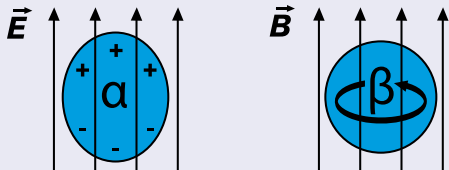


- COMPASS
($181 \pm 11 \pm 27$) keV

theoretical predictions

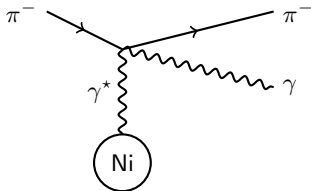
- Covariant Oscillator Quark Model
335 keV and
521 keV (both Maeda et al., 2013)

- π in strong electromagnetic field



- prediction by χ PT:

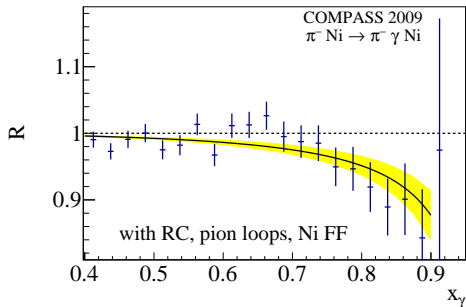
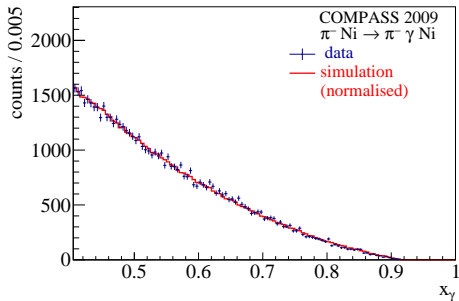
$$\alpha_\pi - \beta_\pi = (5.7 \pm 1.0) \times 10^{-4} \text{ fm}^3$$



- measure deviation of cross-section from expectation for point-like particle
- assumption

$$\alpha_\pi = -\beta_\pi$$

- use π and μ beams at COMPASS
- measure the fake-polarizability of the μ to verify simulation



submitted to PRL $\alpha_\pi = (2.0 \pm 0.6_{\text{stat.}} \pm 0.7_{\text{syst.}}) \times 10^{-4} \text{ fm}^3$

- in tension with previous experiments
- in agreement with χ PT predictions

Outlook

- more data taken in 2012
- separate measurement of α_π and β_π
- polarizability of K

COMPASS is a precision experiment to study light mesons

- unchallenged dataset for $\pi^- \pi^- \pi^+$
- charged and neutral particles with the same experimental setup

partial-wave analysis is a versatile tool for

- spectroscopy
 - various channels under study
 - t' resolved analysis, first mass-dependent fit in more than one t' bin
 - new resonance $a_1(1420)$:
 - $M_{a_1(1420)} = 1412 - 1422 \text{ MeV}/c^2$, $\Gamma_{a_1(1420)} = 130 - 150 \text{ MeV}/c^2$
 - full phase motion with respect to reference waves
- studies of light meson structure
 - measurement of radiative width of $a_2(1320)$ and $\pi_2(1670)$

tests of χ PT

- measurement of π polarizability

Backup

data binned

- in 50 mass bins of $40 \text{ MeV}/c^2$ width
- in 8 t' bins with equal amount of statistics

in each mass and t' bin optimize

$$\log \mathcal{L} = - \sum_e^{\text{RD evts.}} \log \left(\sum_{\varepsilon}^{\text{refl.}} \left| \sum_i^{\text{waves}} T_i^{\varepsilon} \cdot \overline{\psi}_{i,e}^{\varepsilon} \right|^2 \right) + \sum_{\varepsilon}^{\text{refl.}} \left(\sum_{i,j}^{\text{waves}} T_i^{\varepsilon} \cdot (T_j^{\varepsilon})^* \cdot \overline{\mathcal{A}}_{ij}^{\varepsilon} \right)$$

Spin-density matrix

$$\rho_{ij}^{\varepsilon} = T_i^{\varepsilon} \cdot (T_j^{\varepsilon})^*$$

intensity

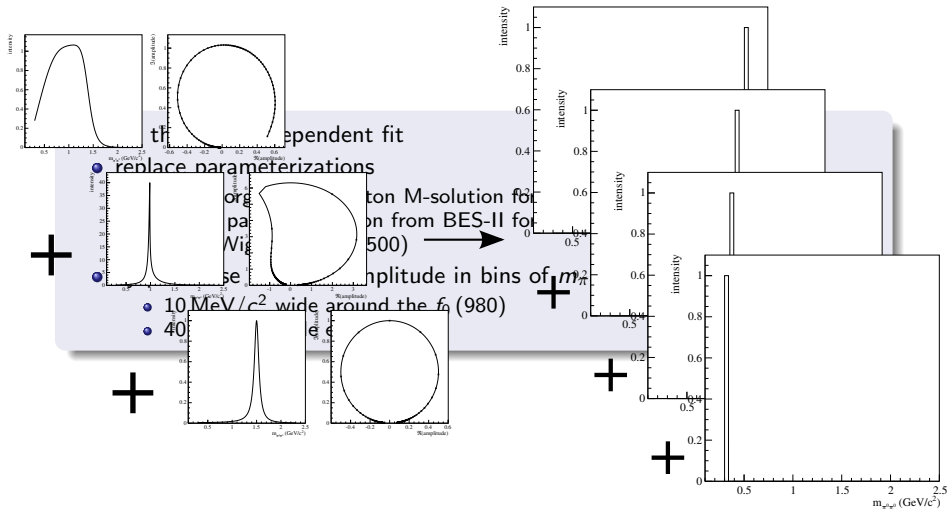
$$I_i^{\varepsilon} = \rho_{ii}^{\varepsilon}$$

absolute value and phase

$$\rho_{ij}^{\varepsilon} = r_{ij}^{\varepsilon} e^{i \cdot \varphi_{ij}^{\varepsilon}}$$

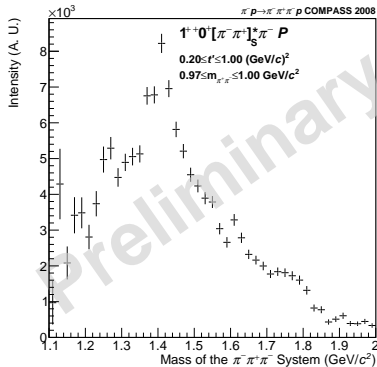
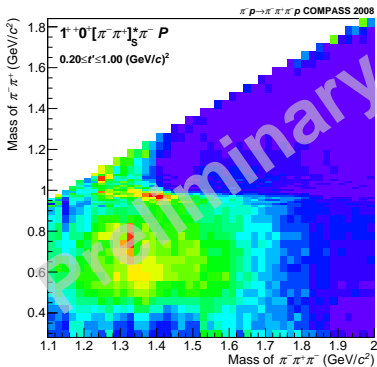
- for the mass-independent fit
- replace parameterizations
 - Au, Morgen, Pennington M-solution for $(\pi\pi)_S$ wave
 - Flatté parameterization from BES-II for $f_0(980)$
 - Breit-Wigner for $f_0(1500)$
- by piecewise constant amplitude in bins of $m_{\pi\pi}$
 - 10 MeV/ c^2 wide around the $f_0(980)$
 - 40 MeV/ c^2 wide elsewhere

Extraction of $(\pi\pi)_S$ wave from data



- for the mass-independent fit
- replace parameterizations
 - Au, Morgen, Pennington M-solution for $(\pi\pi)_S$ wave
 - Flatté parameterization from BES-II for $f_0(980)$
 - Breit-Wigner for $f_0(1500)$
- by piecewise constant amplitude in bins of $m_{\pi\pi}$
 - 10 MeV/ c^2 wide around the $f_0(980)$
 - 40 MeV/ c^2 wide elsewhere

- increase in number of fit parameters
- requires a lot of data
- only done for 0^{-+} , 1^{++} , 2^{-+}

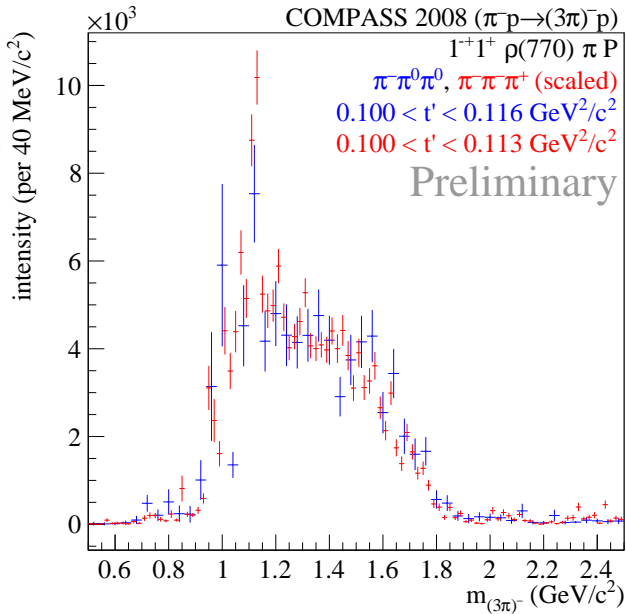


application to 1^{++}

- high- t' : $0.2 < t' < 1.0 \text{ GeV}^2/c^2$
- select $m_{2\pi}$ region around $f_0(980)$
- correlation of $a_1(1420)$ with $f_0(980)$

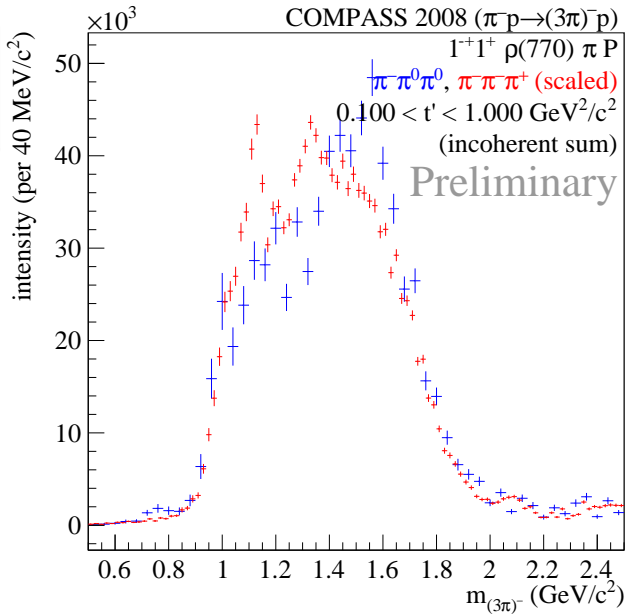
$1^{-+}1^{+}\rho(770)\pi P$

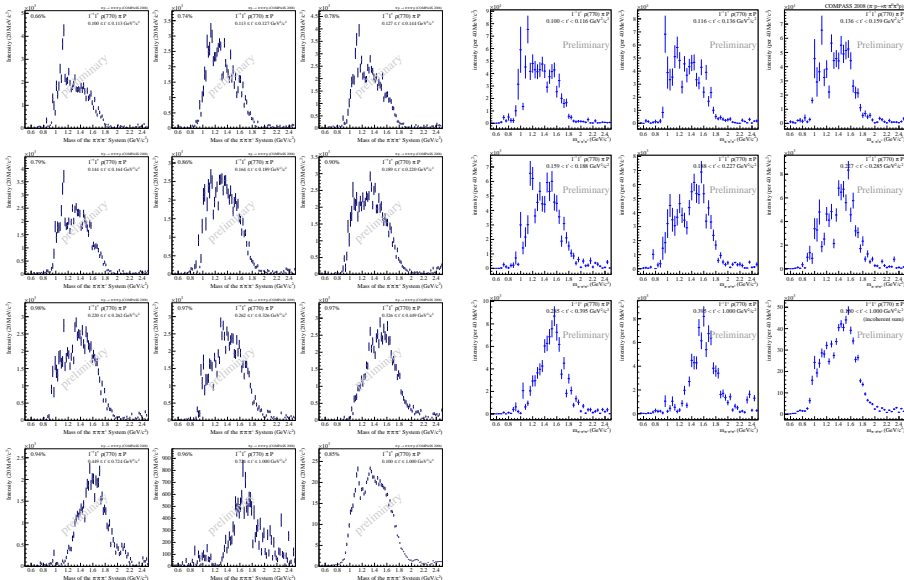
- agreement at low- t'



$1^{-+}1^{+}\rho(770)\pi P$

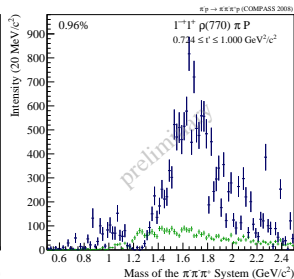
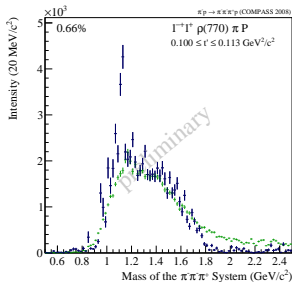
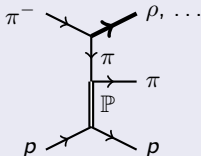
- agreement at low- t'
- differences for complete t' range

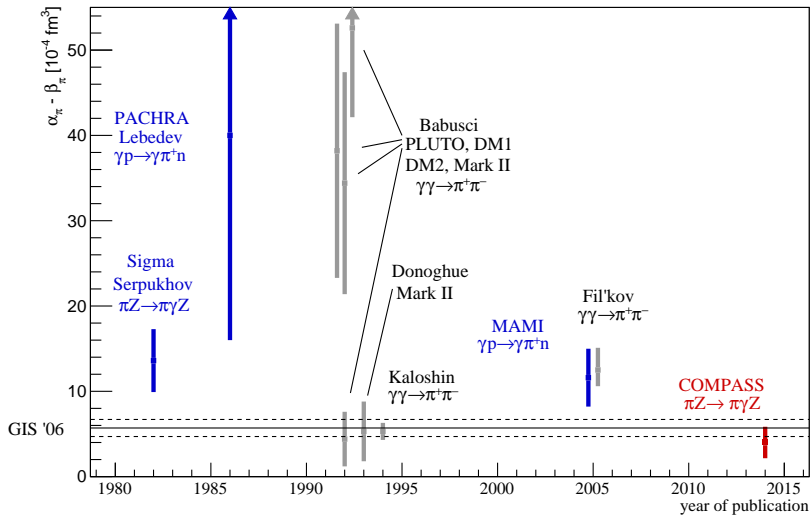


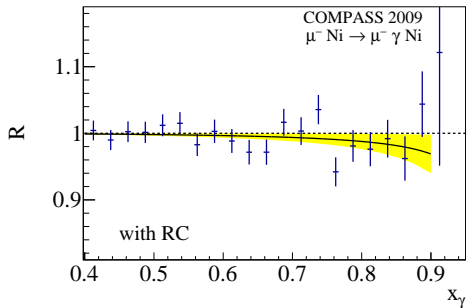
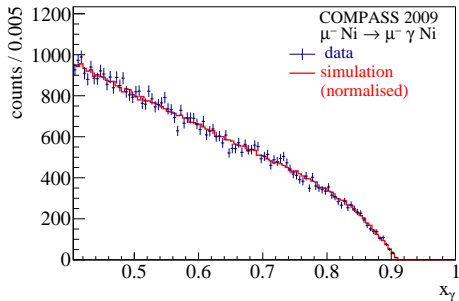


$1^{-+}1^{+}\rho(770)\pi P$

- agreement at low- t'
- differences for complete t' range
- non-resonant contribution
- especially at low- t'
- Deck-effect?







$$\alpha_\mu = (0.5 \pm 0.5) \times 10^{-4} \text{ fm}^3$$