

Access to Generalized Parton Distributions at COMPASS

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on behalf of the  collaboration

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Outline

- The COMPASS experiment
- Deeply virtual Compton Scattering [DVCS]:
 - * Cross section -> Transverse size of the nucleon
 - * Asymmetries -> Generalized Parton Distributions [GPDs]
- Results: exclusive ρ^0 production: 2007 (${}^6\text{LiD}$) / 2010 (NH_3)
- Interpretation within phenomenological Goloskokov-Kroll model -> evidence for existence of transverse GPDs
- >2016/17: unpolarized LH target: DVCS and HEMP (hard exclusive meson production) -> constrain GPD H
- >2018: to constrain GPD E : need new transversely polarized target & recoil proton detection

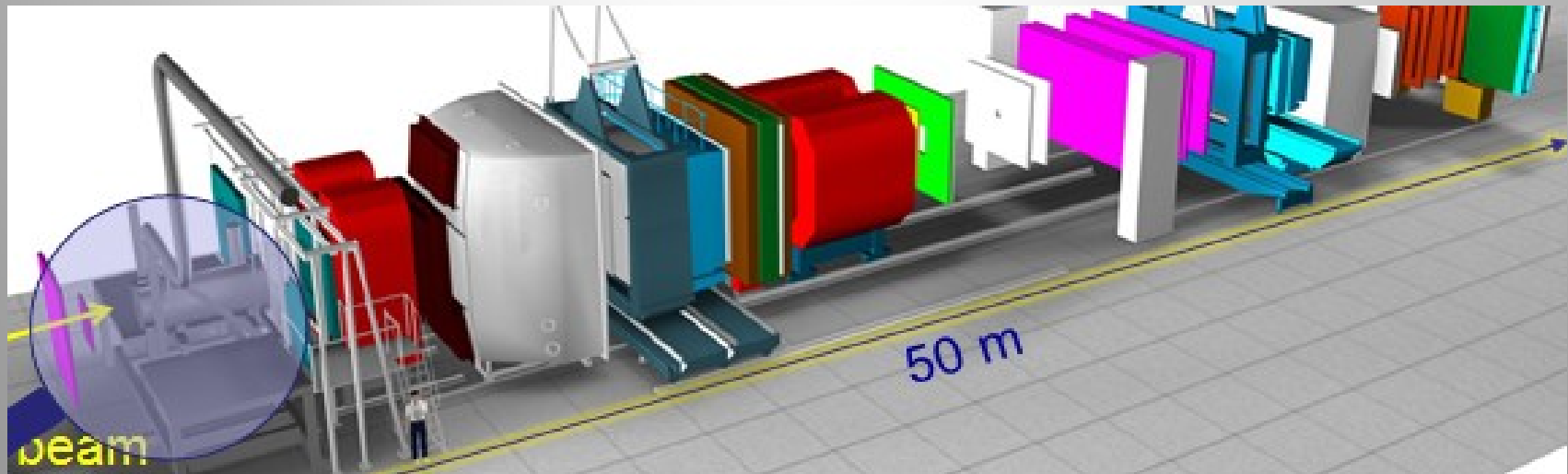
COMPASS experiment

240 physicists
28 institutions

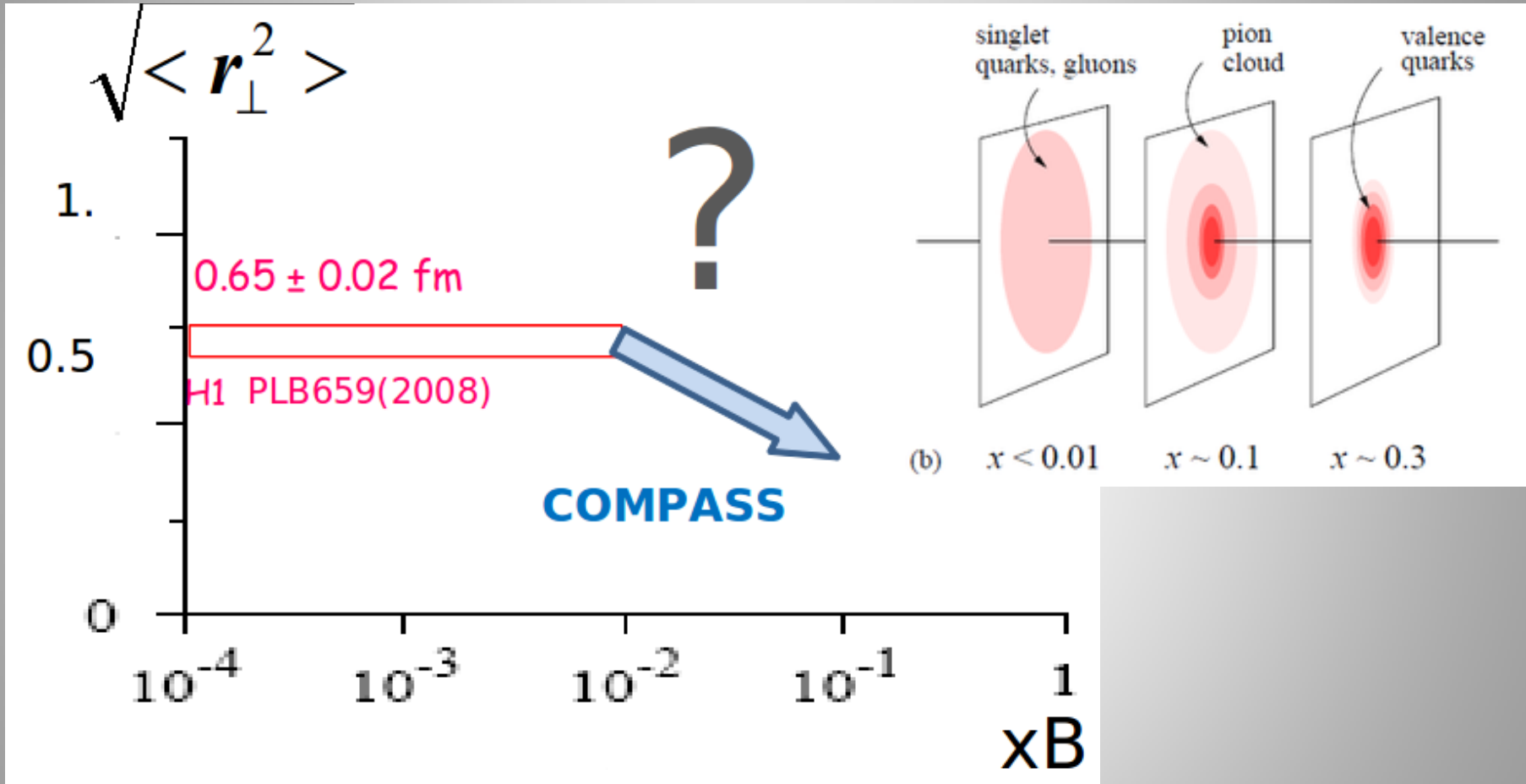


Unique Experimental Conditions at COMPASS

- High-energy 100-200 GeV/c (tertiary) muon beam (CERN)
- Natural high beam polarization: $O(0.8)$; pos.[neg.] for mu- [+]
- 2007(${}^6\text{LiD}$) & 2010(NH_3): transversely polarized d & p targets
- 2009 & 2012: DVCS test runs (LH target & small RPD)
- > 2015: unpolarized *liquid-hydrogen* (LH) target (no dilution)
- > 2015: large recoil-proton detector (RPD) around target
- Large acceptance; 2-stage tracking and calorimetry, PID

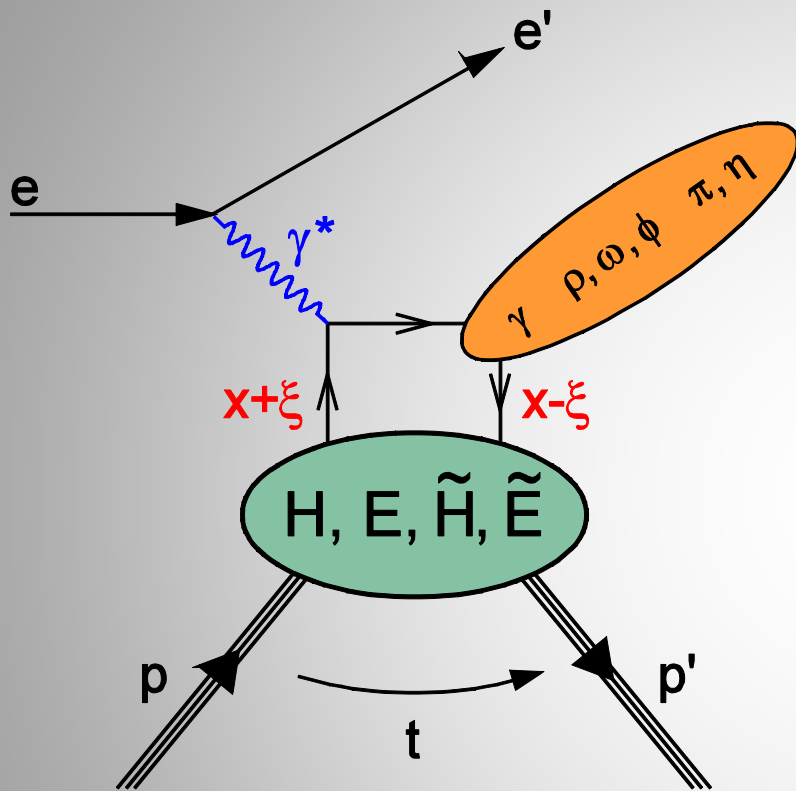


Transverse size of the nucleon vs. Bjorken-x



→ Compass covers low-x to medium-x region

Exclusive Processes: Access to GPDs



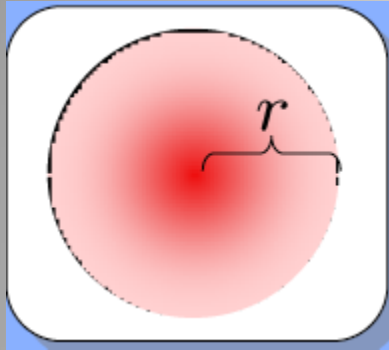
- For spin-1/2 target 4 chiral-even (= parton-helicity conserving) leading-twist parton GPDs: $H, E, \tilde{H}, \tilde{E}$
 - > H, \tilde{H} conserve nucleon helicity,
 - > E, \tilde{E} involve nucleon helicity flip
- Different final states are sensitive to different (combinations of) GPDs:
 - > DVCS (γ) $\rightarrow H, E, \tilde{H}, \tilde{E}$
 - > Vector mesons (ρ, ω, ϕ) $\rightarrow H, E$
 - > Pseudoscalar mesons (π, η) $\rightarrow \tilde{H}, \tilde{E}$
- Also: chiral-odd (transverse') (= parton-helicity flip) GPDs:

$$\underline{H_T} \quad \bar{E}_T = 2\tilde{H}_T + E_T$$

 - > accessible e.g. in ρ production

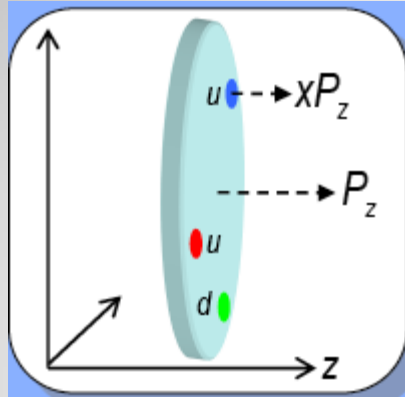
Interpretation of GPDs

Elastic Form Factors

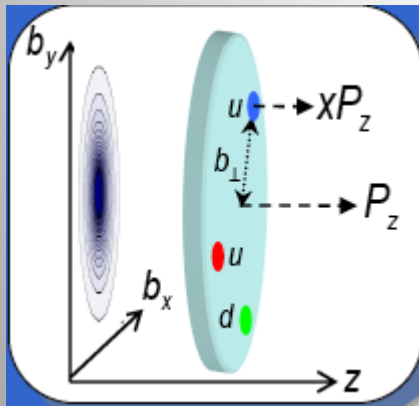


transverse position of partons

Parton Distribution Functions (PDFs)



longitudinal momentum of partons



Correlation between longitudinal momentum and transverse position

- GPDs include Form Factors and Parton Distribution Functions as moments and forward limits, resp.

- GPDs yield a multidimensional description of nucleon structure (longitudinal momentum vs. transverse position)

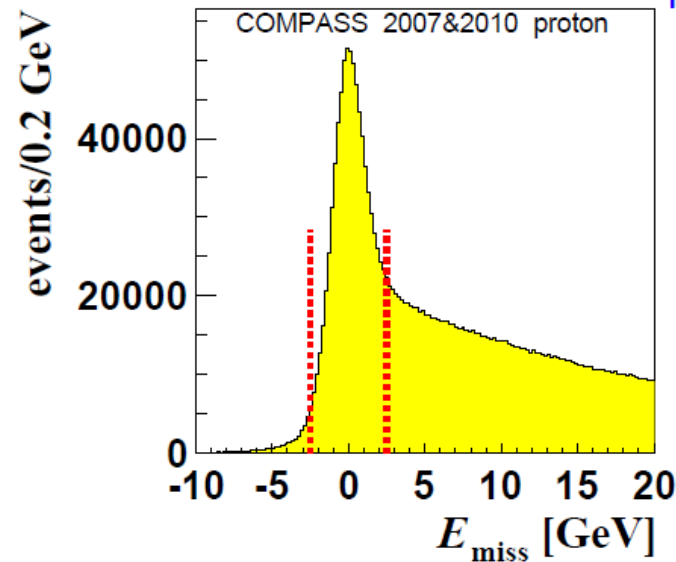
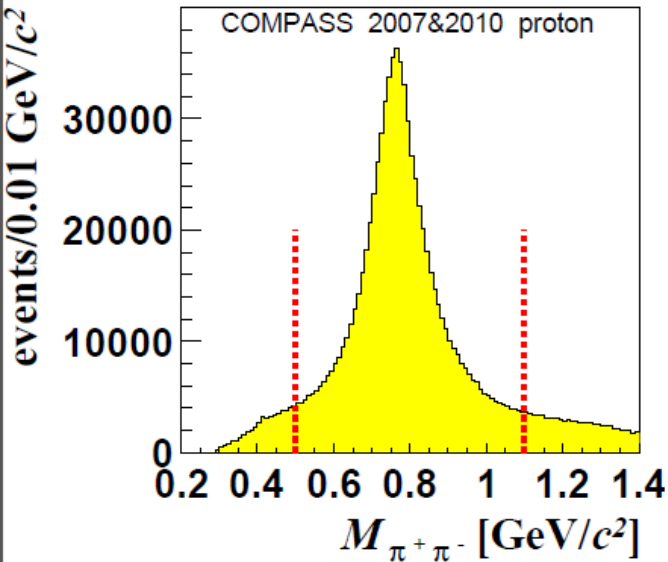
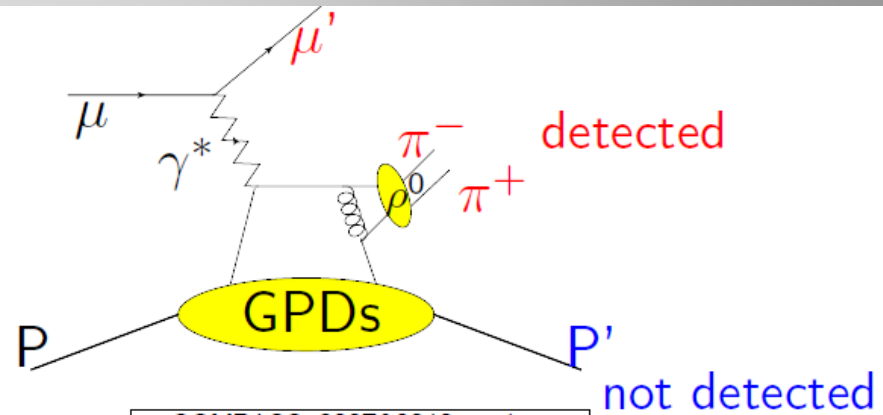
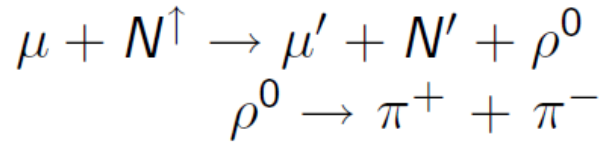
→ **NUCLEON TOMOGRAPHY**

- GPDs offer access to quark total angular momentum through the Ji relation (in principle also for gluons):

$$J_q = \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H_q(x, \xi, \xi) + E_q(x, \xi, \xi)]$$

[X. Ji, *Phys. Rev. Lett.* 78 (1997) 610]

2010: Exclusive ρ^0 production: event selection



- ▶ Peak at ρ^0 mass $\sim 0.775 \text{ GeV}/c^2$
- ▶ Signature for exclusivity $E_{\text{miss}} \sim 0$

$$E_{\text{miss}} = \frac{(p + q - \rho)^2 - p^2}{2 \cdot M_p} = \frac{M_X^2 - M_p^2}{2 \cdot M_p}$$

Hard exclusive ρ^0 production

- ▶ Factorisation valid for σ_L
- ▶ Leading twist term σ_{00}^{+-} sensitive to

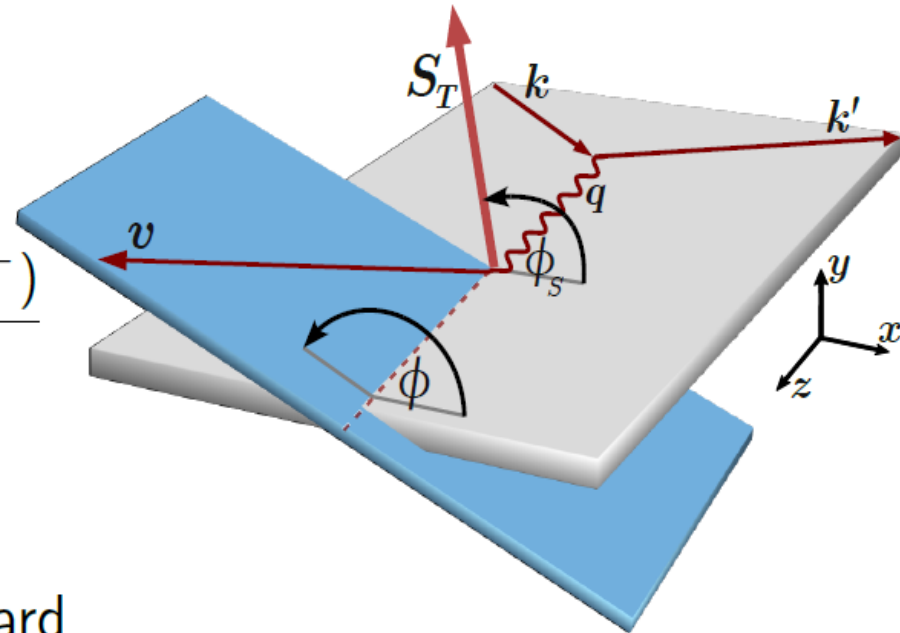
$$A_{\text{UT}}^{\sin(\phi-\phi_s)} = -\frac{\text{Im}(\sigma_{++}^{+-} + \varepsilon \sigma_{00}^{+-})}{\sigma_0}$$

$$\text{Im} \frac{d\sigma_{00}^{+-}}{dt} \sim \text{Im}(\mathcal{E}^* \mathcal{H})$$

- ▶ \mathcal{E} & \mathcal{H} are convolution integrals of hard scattering kernels and the ρ^0 distribution amplitude with GPDs E & H where:

$$E_{\rho^0} = \frac{1}{\sqrt{2}} \left(\frac{2}{3} E^u + \frac{1}{3} E^d + \frac{3}{8} E^g \right)$$

→ Constrain GPD E



- ▶ Additional asymmetries contain higher twist terms

Cross section of hard exclusive ρ^0 production

$$\left[\frac{\alpha_{\text{em}}}{8\pi^3} \frac{y^2}{1-\varepsilon} \frac{1-x_B}{x_B} \frac{1}{Q^2} \right]^{-1} \frac{d\sigma}{dx_B dQ^2 d\phi d\psi} = \frac{1}{2} \left(\sigma_{++}^{++} + \sigma_{++}^{--} \right) + \varepsilon \sigma_{00}^{++} - \varepsilon \cos(2\phi) \text{Re} \sigma_{+-}^{++}$$

$$- \sqrt{\varepsilon(1+\varepsilon)} \cos \phi \text{Re} (\sigma_{+0}^{++} + \sigma_{+0}^{--}) - P_\ell \sqrt{\varepsilon(1-\varepsilon)} \sin \phi \text{Im} (\sigma_{+0}^{++} + \sigma_{+0}^{--})$$

$$- S_L \left[\varepsilon \sin(2\phi) \text{Im} \sigma_{+-}^{++} + \sqrt{\varepsilon(1+\varepsilon)} \sin \phi \text{Im} (\sigma_{+0}^{++} - \sigma_{+0}^{--}) \right]$$

$$+ S_L P_\ell \left[\sqrt{1-\varepsilon^2} \frac{1}{2} (\sigma_{++}^{++} - \sigma_{++}^{--}) - \sqrt{\varepsilon(1-\varepsilon)} \cos \phi \text{Re} (\sigma_{+0}^{++} - \sigma_{+0}^{--}) \right]$$

$$- S_T \left[\sin(\phi - \phi_S) \text{Im} (\sigma_{++}^{+-} + \varepsilon \sigma_{00}^{+-}) + \frac{\varepsilon}{2} \sin(\phi + \phi_S) \text{Im} \sigma_{+-}^{+-} + \frac{\varepsilon}{2} \sin(3\phi - \phi_S) \text{Im} \sigma_{+-}^{-+}$$

$$+ \sqrt{\varepsilon(1+\varepsilon)} \sin \phi_S \text{Im} \sigma_{+0}^{+-} + \sqrt{\varepsilon(1+\varepsilon)} \sin(2\phi - \phi_S) \text{Im} \sigma_{+0}^{-+} \right]$$

$$+ S_T P_\ell \left[\sqrt{1-\varepsilon^2} \cos(\phi - \phi_S) \text{Re} \sigma_{++}^{+-} - \sqrt{\varepsilon(1-\varepsilon)} \cos \phi_S \text{Re} \sigma_{+0}^{+-}$$

$$- \sqrt{\varepsilon(1-\varepsilon)} \cos(2\phi - \phi_S) \text{Re} \sigma_{+0}^{-+} \right]$$

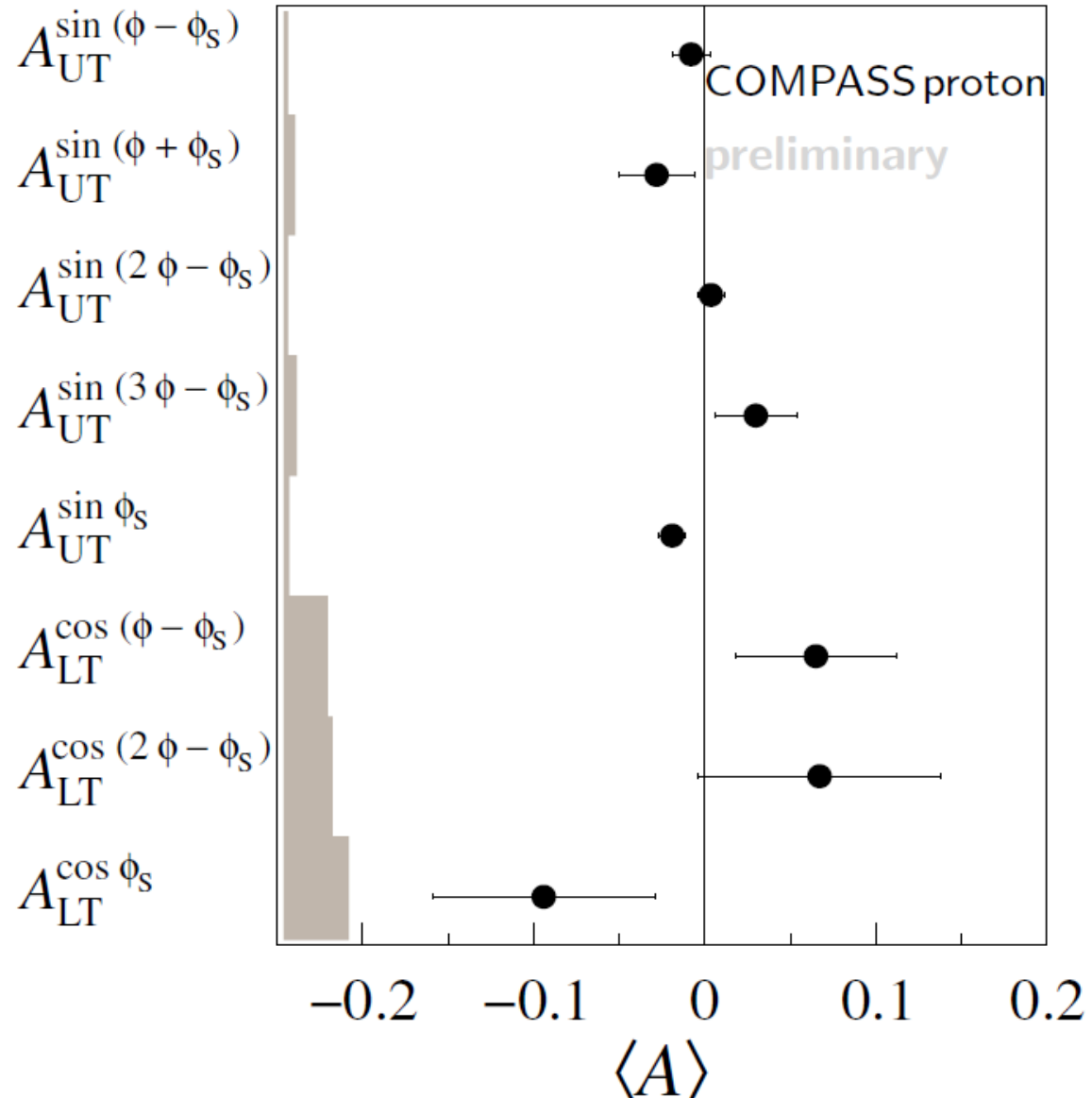
transversely
polarized
target

transversely
polarized
target +
longitudinally
polarized beam

ε = virtual photon polarization parameter
 σ_{mn}^{ij} = spin dependent photoabsorption cross sections,
interference terms
 m, n = virtual-photon helicity
 i, j = target nucleon helicity

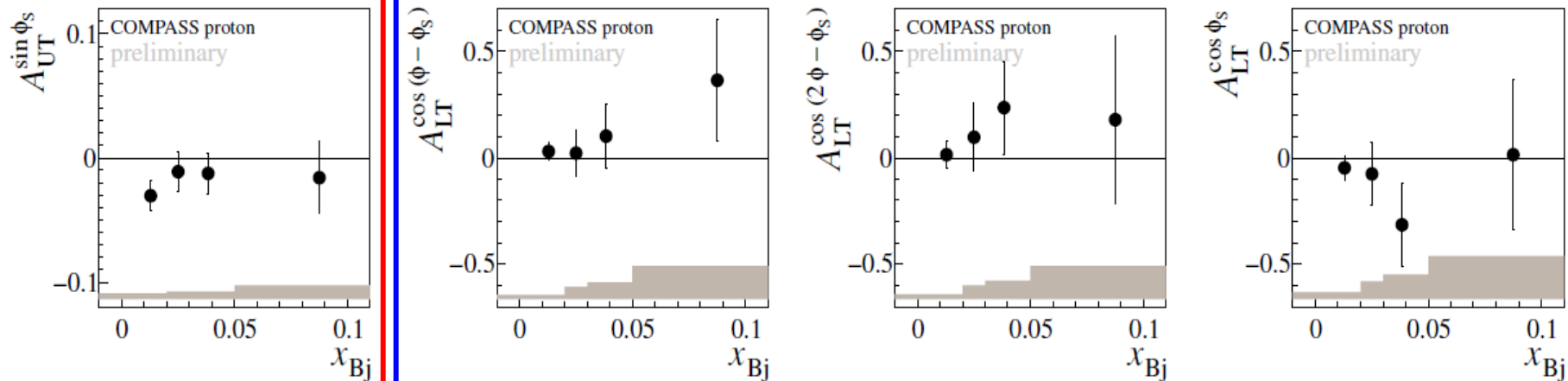
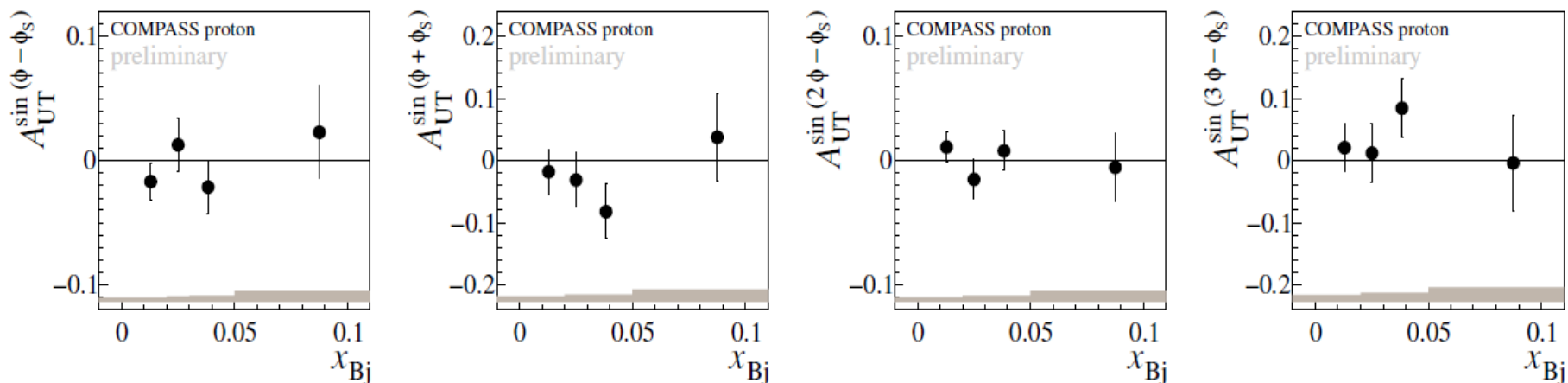
Diehl & Sapeta
Eur.Phys.J.C 41 (2005)

Mean asymmetries - NH₃ target (2007&2010)



Asymmetry $A_{UT,LT}$ - NH_3 target (2007&2010)

as a function of x_{Bj}



- ▶ Asymmetry extraction using a 2D binned maximum likelihood fit after subtracting the SIDIS background

Comparison with a phenomenological GPD-based model

- ▶ phenomenological 'handbag' approach
- ▶ based on k_{\perp} factorisation
- ▶ includes twist-3 meson wave functions
- ▶ includes contributions from γ_L^* and γ_T^*

Goloskokov & Kroll
Eur.Phys.J.C 59 (2009)

$$\sigma_{\mu\sigma}^{\nu\lambda} = \sum \mathcal{M}_{\mu'\nu',\mu\nu}^* \mathcal{M}_{\mu'\nu',\sigma\lambda}$$

$$A_{\text{UT}}^{\sin(\phi-\phi_s)} \sigma_0 = -2\text{Im} \left[\epsilon \mathcal{M}_{0-,0+}^* \mathcal{M}_{0+,0+} + \mathcal{M}_{+-,++}^* \mathcal{M}_{++,++} + \frac{1}{2} \mathcal{M}_{0-,++}^* \mathcal{M}_{0+,++} \right]$$

$$A_{\text{UT}}^{\sin(\phi_s)} \sigma_0 = -\text{Im} \left[\mathcal{M}_{0-,++}^* \mathcal{M}_{0+,0+} - \mathcal{M}_{0+,++}^* \mathcal{M}_{0-,0+} \right]$$

$$A_{\text{UT}}^{\sin(2\phi-\phi_s)} \sigma_0 = -\text{Im} \left[\mathcal{M}_{0+,++}^* \mathcal{M}_{0-,0+} \right]$$

$$A_{\text{LT}}^{\cos(\phi_s)} \sigma_0 = -\text{Re} \left[\mathcal{M}_{0-,++}^* \mathcal{M}_{0+,0+} - \mathcal{M}_{0+,++}^* \mathcal{M}_{0-,0+} \right]$$

$\mathcal{M}_{\delta\gamma,\beta\alpha}$ = helicity amplitudes
 α = initial-state proton helicity
 β = virtual-photon helicity
 γ = final-state proton helicity
 δ = meson helicity

Comparison with a phenomenological GPD-based model

Up to now mainly used to describe DVCS and HEMP:
chiral-even GPDs

$$\gamma_L^* \rightarrow \rho_L^0 \quad \mathcal{M}_{0+,0+} \sim H; \mathcal{M}_{0-,0+} \sim E \quad \text{dominant}$$

$$\gamma_T^* \rightarrow \rho_T^0 \quad \mathcal{M}_{++,++} \sim H; \mathcal{M}_{+-,++} \sim E \quad \text{suppressed}$$

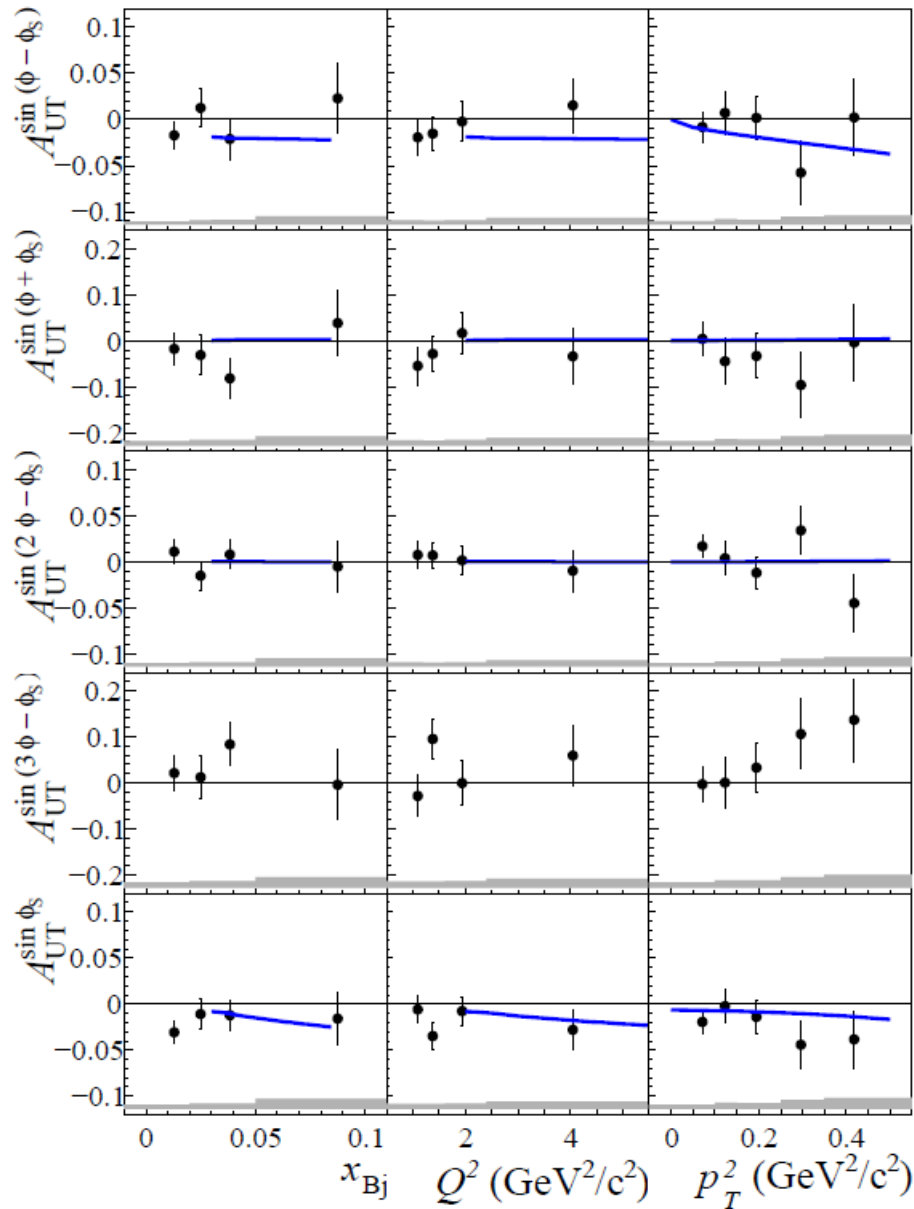
Recently introduced: chiral-odd (transverse) GPDs

$$\gamma_T^* \rightarrow \rho_L^0 \quad \mathcal{M}_{0-,++} \sim H_T; \mathcal{M}_{0+,++} \sim \bar{E}_T = 2\tilde{H}_T + E_T$$

$\gamma_L^* \rightarrow \rho_T^0, \gamma_T^* \rightarrow \rho_{-T}^0$ known to be suppressed, neglected in the model

$A_{\text{UT,p}}^{\sin(\phi_S)} = -0.019 \pm 0.008 \pm 0.003$ evidence for existence of
chiral-odd GPD H_T

Asymmetry $A_{UT,p} - \text{NH}_3$ target (2007&2010)



COMPASS proton
 Phys.Lett. B731 (2014) 96
 arXiv:1310.1454

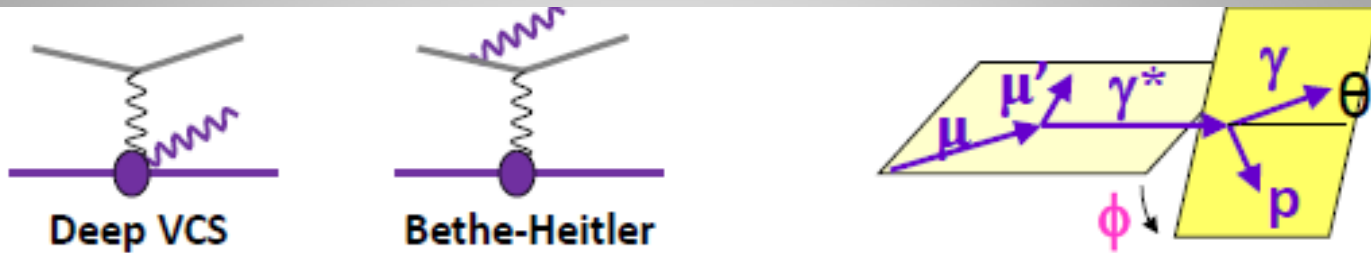
- ▶ Blue line: Model from Goloskokov and Kroll
- ▶ Predictions for COMPASS kinematic

$$W = 8.1 \text{ GeV}/c^2,$$

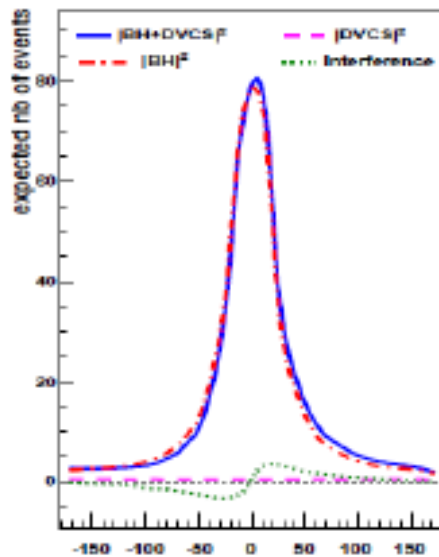
$$p_T^2 = 0.2 \text{ (GeV}/c)^2,$$

$$Q^2 = 2.2 \text{ (GeV}/c)^2$$

DVCS at COMPASS: Monte Carlo Simulation



$$d\sigma \propto |T^{BH}|^2 + \text{Interference Term} + |T^{DVCS}|^2$$

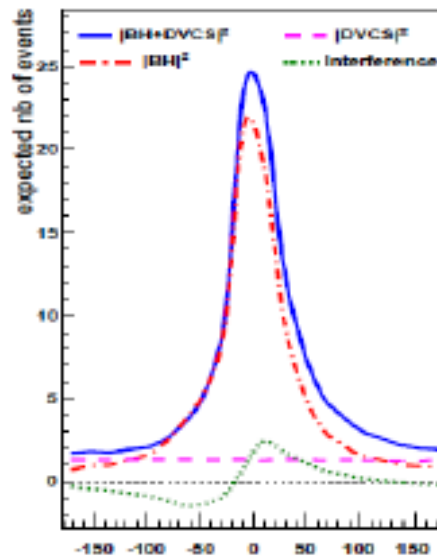


$0.005 < x_B < 0.01$

BH dominates

excellent

reference yield

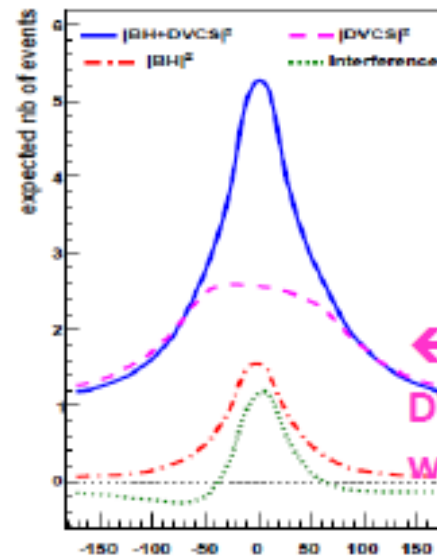


$0.01 < x_B < 0.03$

study of Interference

$\rightarrow \text{Re } T^{DVCS}$

or $\text{Im } T^{DVCS}$



$0.03 < x_B$

DVCS dominates

study of $d\sigma^{DVCS}/dt$

\rightarrow Transverse Imaging

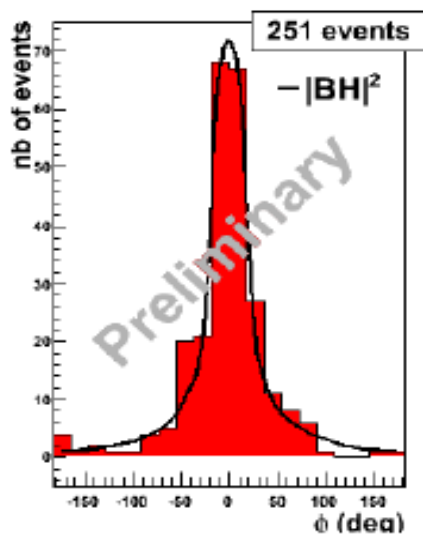
Monte-Carlo Simulation for COMPASS set-up with only ECAL1+2

← Missing DVCS acceptance without ECAL0

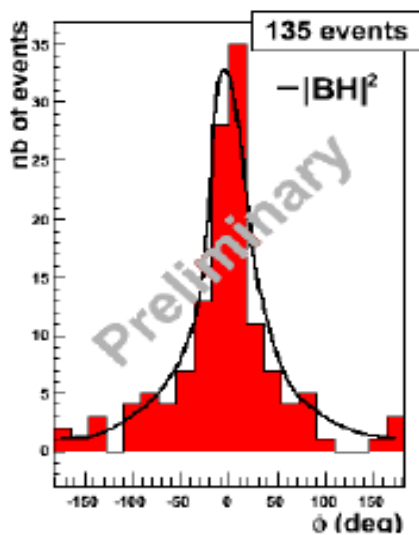
DVCS at COMPASS: 2009 test run data

Test runs in 2009 & 2012 with 40 cm long target & small recoil detector:

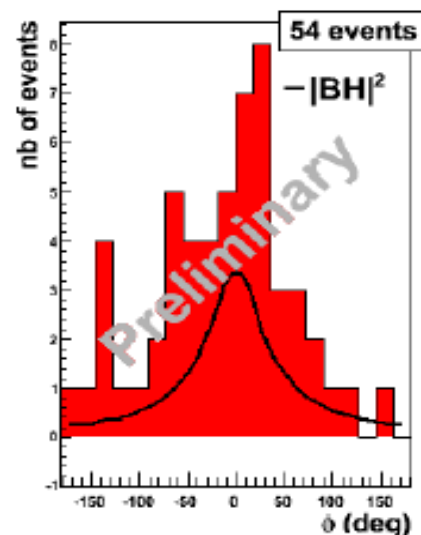
3 x-Bjorken regions -> indication for DVCS signal



$0.005 < x_B < 0.01$



$0.01 < x_B < 0.03$



$0.03 < x_B$

$$\epsilon_{\mu p \rightarrow \mu' \gamma p} \approx 35\%$$

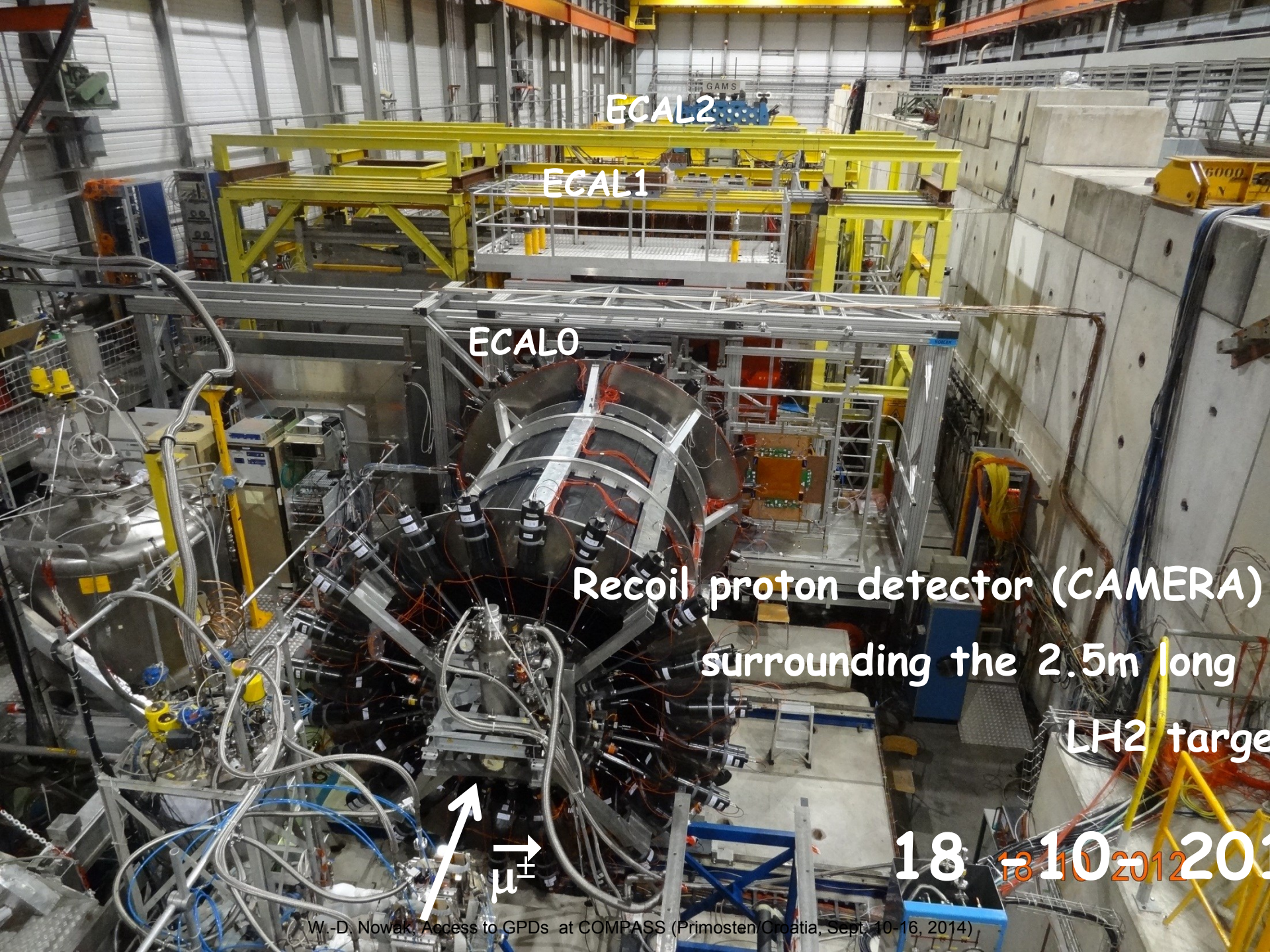
$\times (0.8)^4$ for SPS + COMPASS avail. + trigger eff + dead time

$$\epsilon_{\text{global}} \approx 0.14 \quad \text{confirmed} \quad \epsilon_{\text{global}} = 0.1$$

as assumed for COMPASS II predictions

$$54 \text{ evts} = 20 \text{ BH}$$

+ a significant DVCS contri.
which can be polluted
by γ from π^0 decay



ECAL2

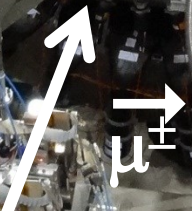
ECAL1

ECALO

Recoil proton detector (CAMERA)

surrounding the 2.5m long

LH2 target



18 ~~to 10~~ 2012-201

DVCS at COMPASS: How to constrain GPDs ?

● **U**n polarized beam: Constrain GPD H (2016-2017)

- **S**um of cross sections: **imaginary** part of Compton Form Factor
- **D**ifference of cross sections: **real** part of Compton Form Factor

$$\begin{aligned} \mathcal{D}_{CS,U} &\equiv d\sigma(\mu^{+\downarrow}) - d\sigma(\mu^{-\uparrow}) \propto c_0^{Int} + c_1^{Int} \cos \phi \quad \text{and} \quad c_{0,1}^{Int} \sim F_1 \operatorname{Re} \mathcal{H} \\ \mathcal{S}_{CS,U} &\equiv d\sigma(\mu^{+\downarrow}) + d\sigma(\mu^{-\uparrow}) \propto d\sigma^{BH} + c_0^{DVCS} + K \cdot s_1^{Int} \sin \phi \quad \text{and} \quad s_1^{Int} \sim F_1 \operatorname{Im} \mathcal{H} \end{aligned}$$

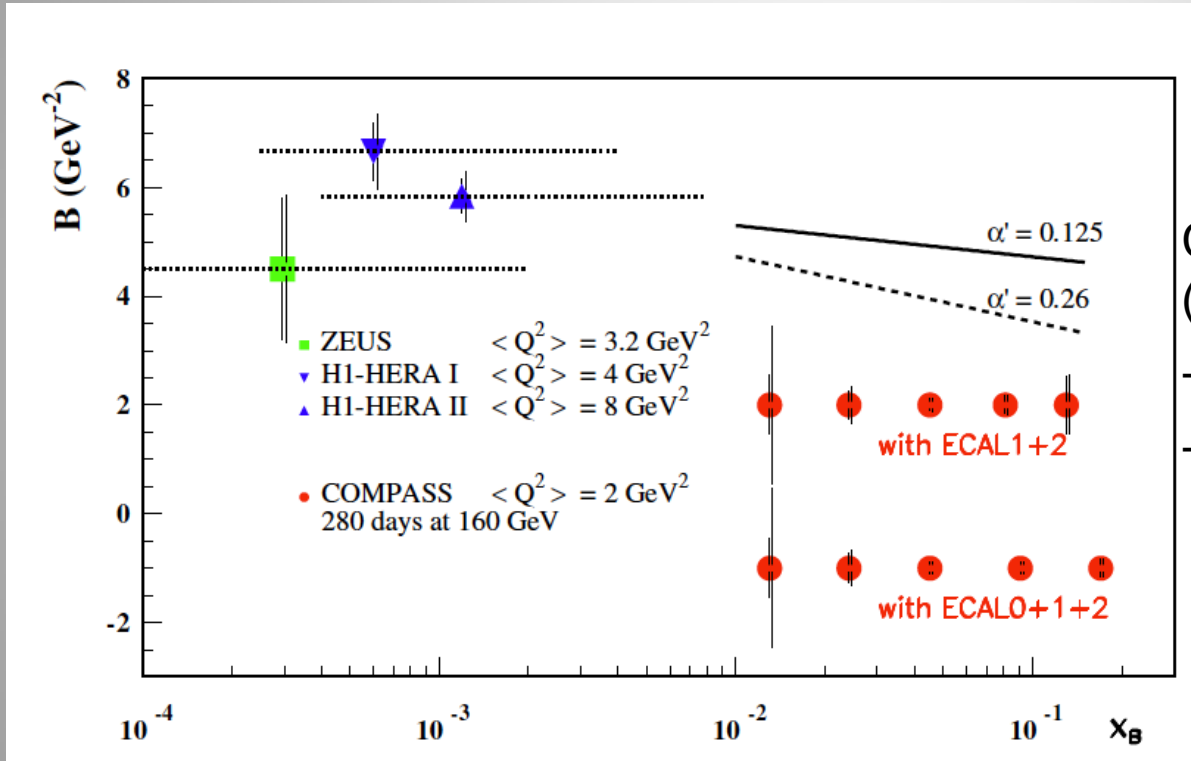
● **T**ransversely polarized target: Access GPD E (> 2018)

(addendum to proposal required)

$$\begin{aligned} \mathcal{D}_{CS,T} &\equiv d\sigma_T(\mu^{+\downarrow}) - d\sigma_T(\mu^{-\uparrow}) \\ &\propto \operatorname{Im}(F_2 \mathcal{H} - F_1 \mathcal{E}) \sin(\phi - \phi_S) \cos \phi \end{aligned}$$

DVCS cross section: transverse size of nucleon

$$\mathcal{S}_{CS,U} \equiv d\sigma^{\pm} + d\sigma^{\mp} = 2(d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + e_{\mu}P_{\mu}\text{Im } I),$$



$$\frac{d\sigma_{unpol}^{DVCS}}{dt} \propto \exp(-B|t|)$$

COMPASS expected results (2016+2017):

- 40 weeks of data,
- 2.5 m LH target

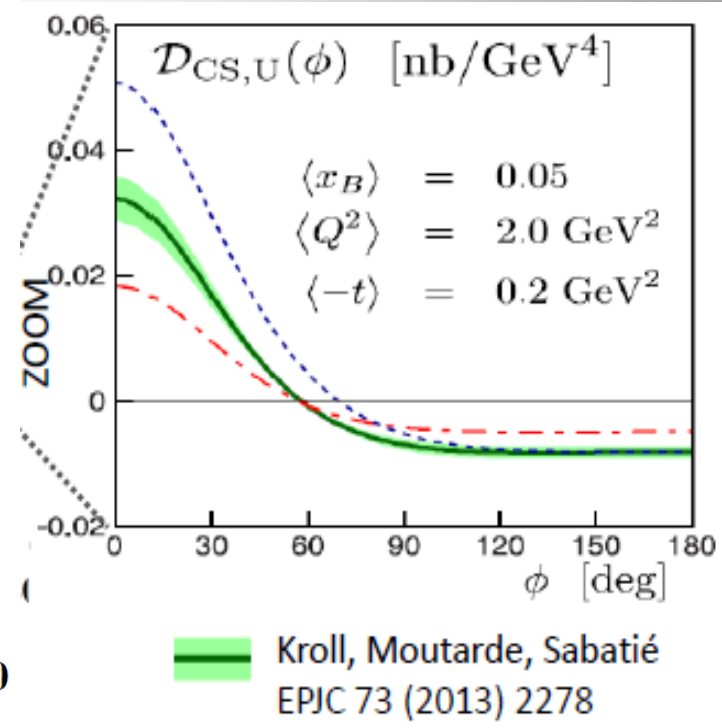
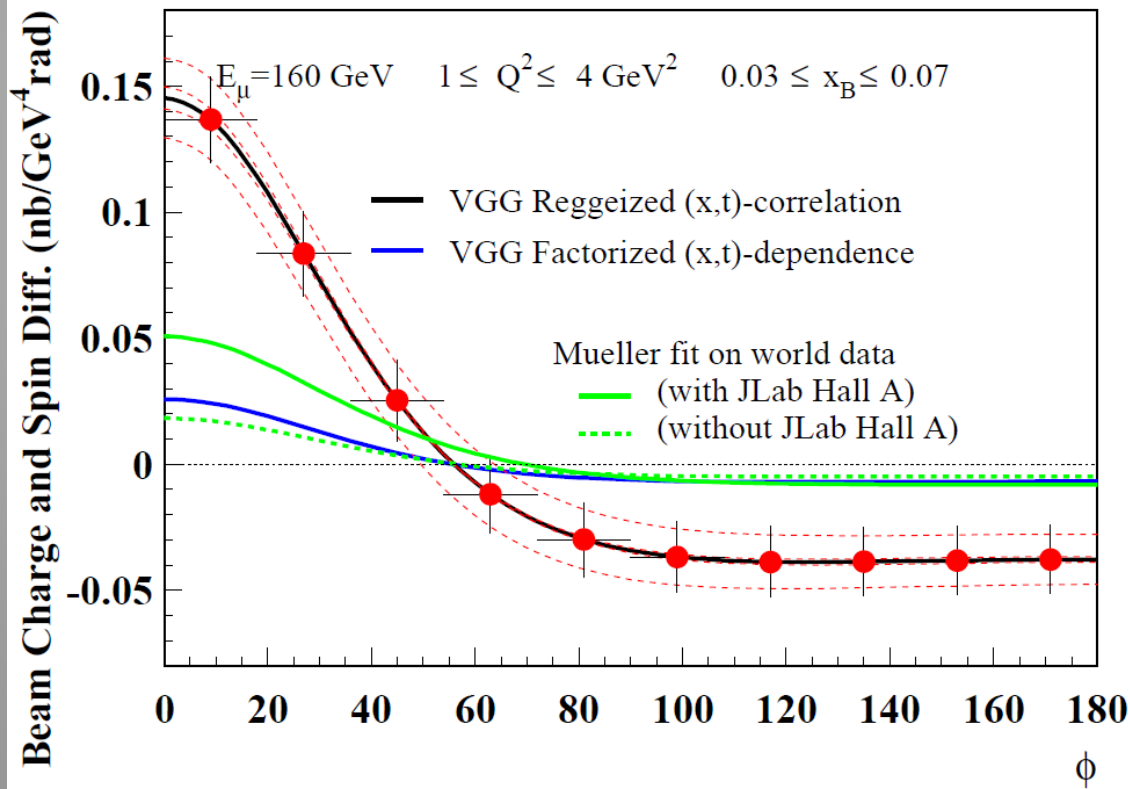
→ Transverse size of the nucleon as a function of Bjorken-x

Measure difference of DVCS cross sections

$$D_{CS,U} = d\sigma(\mu^{+\rightarrow}) - d\sigma(\mu^{-\leftarrow}) \propto P_\mu d\sigma_{pol}^{DVCS} + e_\mu \text{Re}(I) \propto c_0^{Int} + c_1^{Int} \cos\phi$$

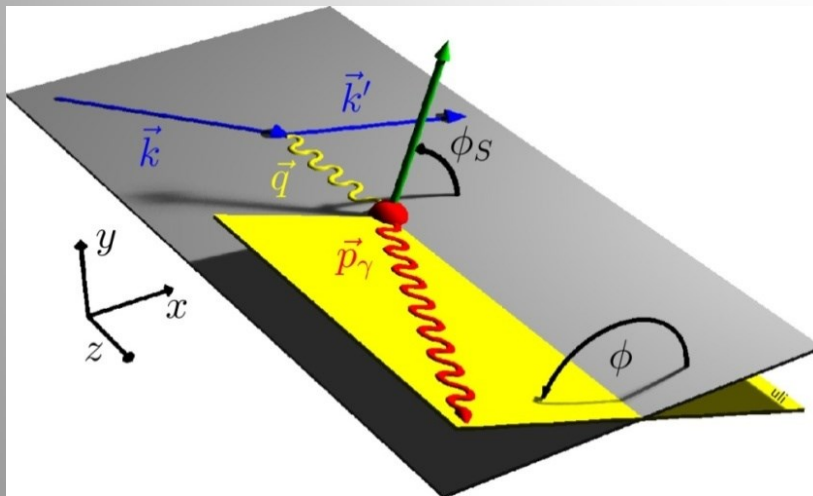
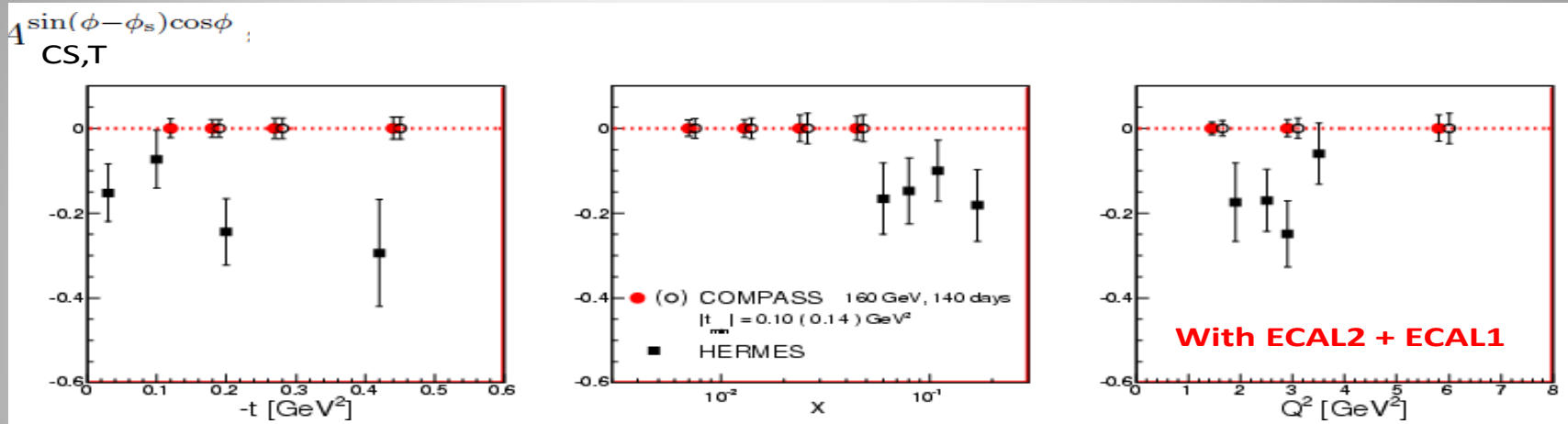
$$c_{0,1} \propto \text{Re}(F_1 H(\xi, t))$$

COMPASS expected results (2016+2017):
40 weeks of data, 2.5 m LH target, 10% global efficiency



DVCS with a transversely polarized Target

> 2018: 2 “years” data taking; $E=160$ GeV/c; 10% efficiency;
(new transversely polarized target & recoil proton detection)



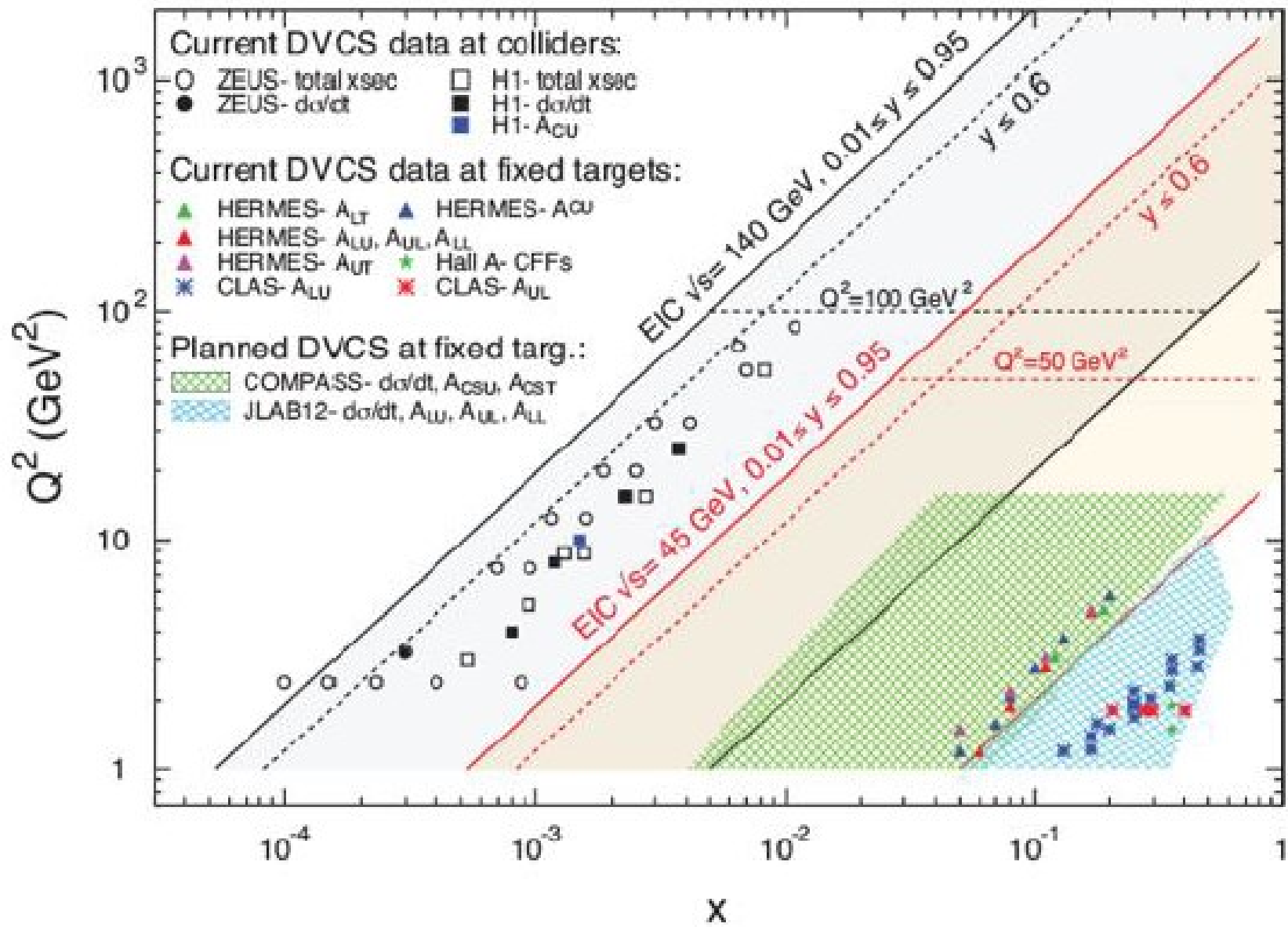
ϕ - angle between the lepton scattering and hadron production planes
 ϕ_s - angle between the target spin direction and the lepton scattering plane

Conclusions and Outlook

- ❶ **Generalized Parton Distributions** are a well-suited tool to explore the **structure of the nucleon (nucleon tomography)**
- ❷ COMPASS is a unique place to study **DVCS and HEMP in the medium-x region**
- ❸ COMPASS results on 2010 exclusive ρ^0 production show **indications for transverse GPDs**, when interpreted in terms of phenomenological Goloskokov-Kroll model
- ❹ 2016/17 data will deliver **COMPASS DVCS results** to help **constraining GPD H** and to better understand the **transverse size of the nucleon**
- ❺ Further ideas exist for >2018 to **constrain GPD E**

For a detailed discussion of 2009/2012 DVCS test run results: **see talk by O. Kouznetsov)**

SPARE SLIDES



Semi-inclusive background estimation

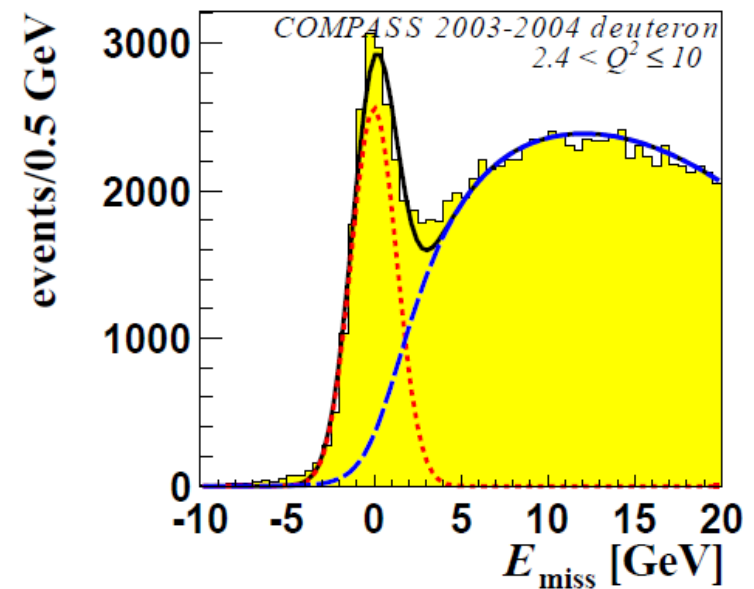
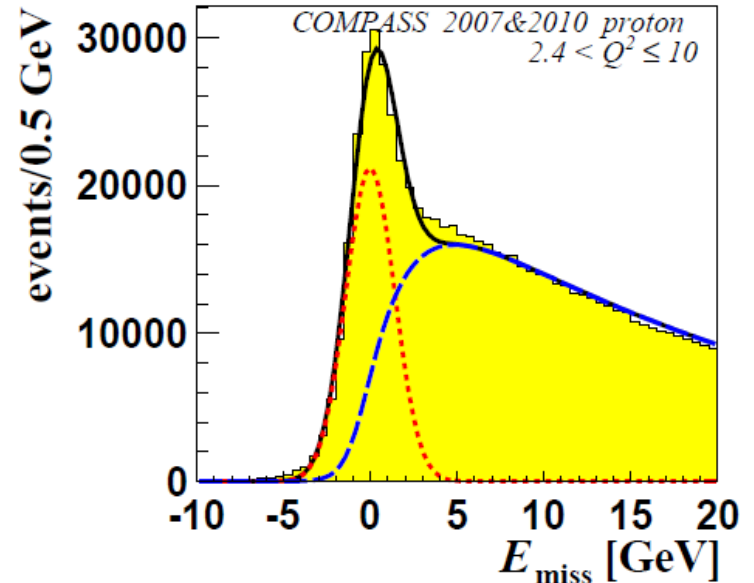
- ▶ LEPTO MC (COMPASS tuning)

1.) Parameterization of MC:

- ▶ MC weighted with the like sign sample

$$w = \frac{N_{\text{data}}^{h^+h^+}(E_{\text{miss}}) + N_{\text{data}}^{h^-h^-}(E_{\text{miss}})}{N_{\text{MC}}^{h^+h^+}(E_{\text{miss}}) + N_{\text{MC}}^{h^-h^-}(E_{\text{miss}})}$$

- ▶ Parameterize the E_{miss} shape of weighted MC
- ▶ Binning appropriate for asymmetry extraction (x_{Bj} , Q^2 or p_T^2 , target cell)

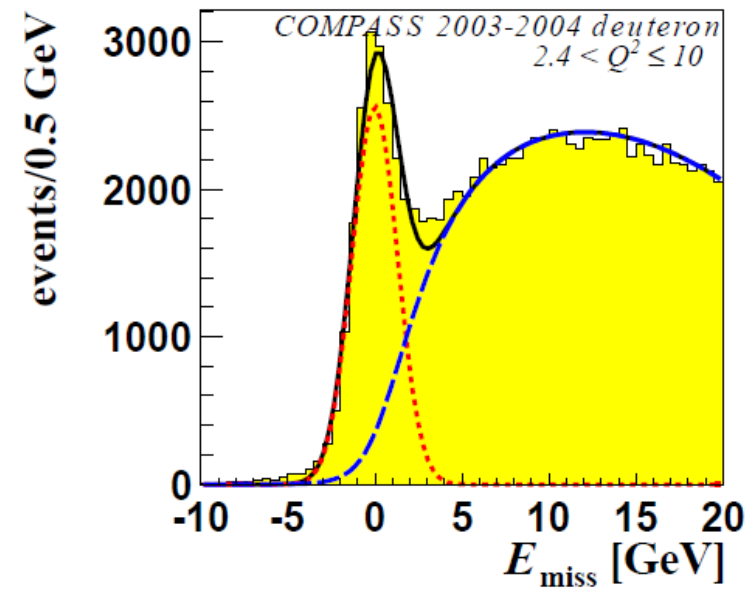
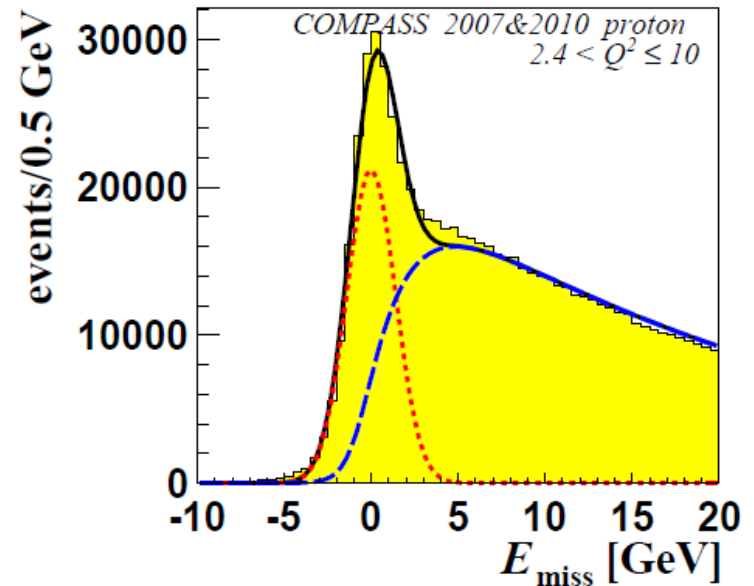


Semi-inclusive background estimation

- ▶ LEPTO MC (COMPASS tuning)

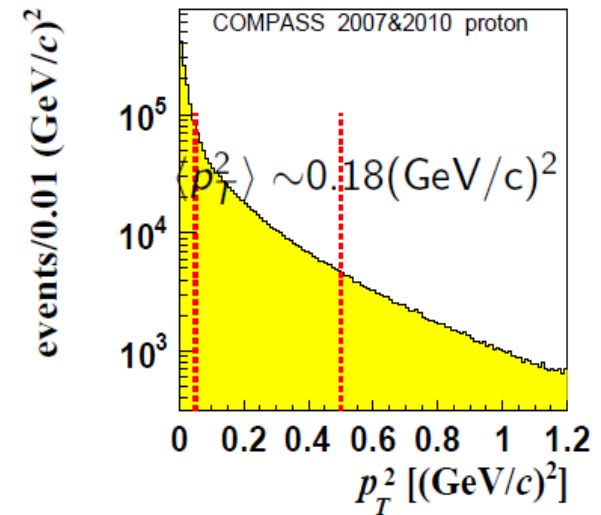
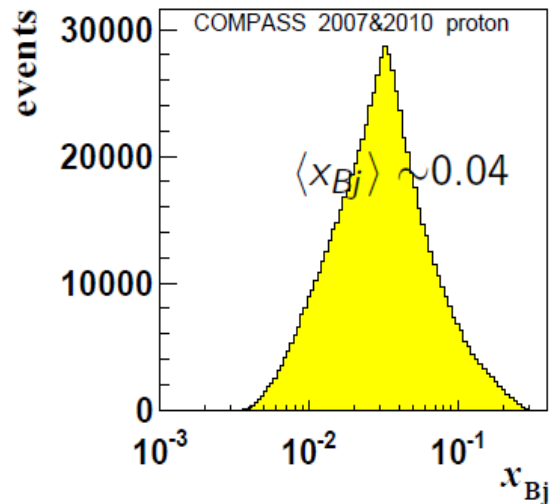
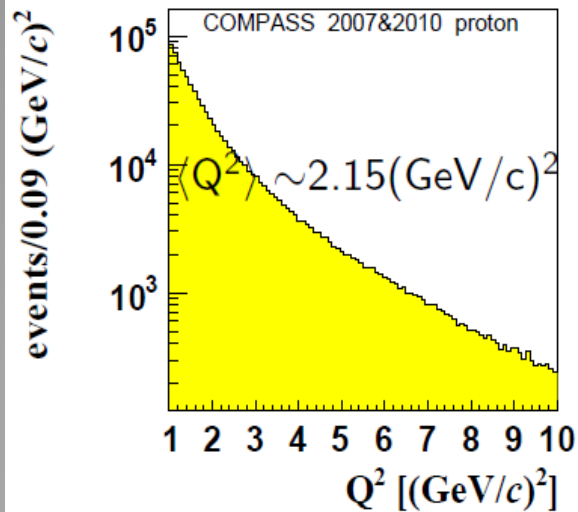
2.) Fit to data:

- ▶ Normalize MC E_{miss} shape to data by performing a two component **signal (gauss)** + **background** fit
 - ▶ ϕ , ϕ_S distribution for $7 < E_{\text{miss}} < 20$ GeV scaled with the number of background events and subtracted from ϕ , ϕ_S distribution in signal range $-2.5 < E_{\text{miss}} < 2.5$ GeV
 - ▶ Asymmetry extraction with corrected ϕ , ϕ_S distribution
- Total amount of SIDIS background:
18% (${}^6\text{LiD}$), 22% (NH_3)

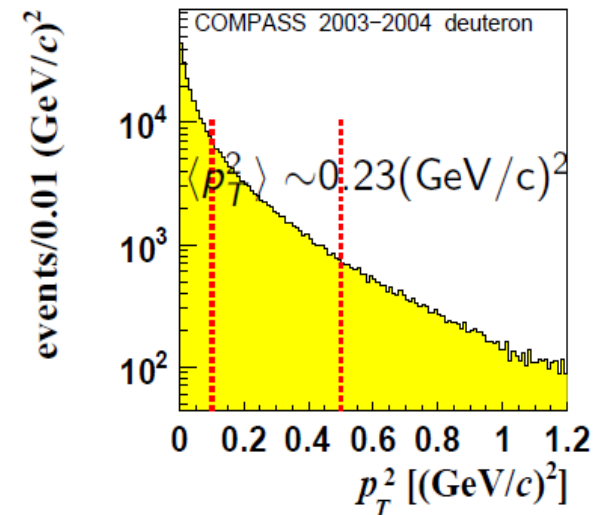
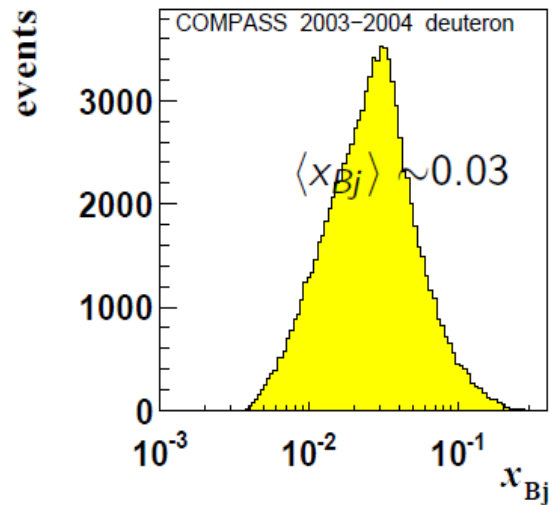
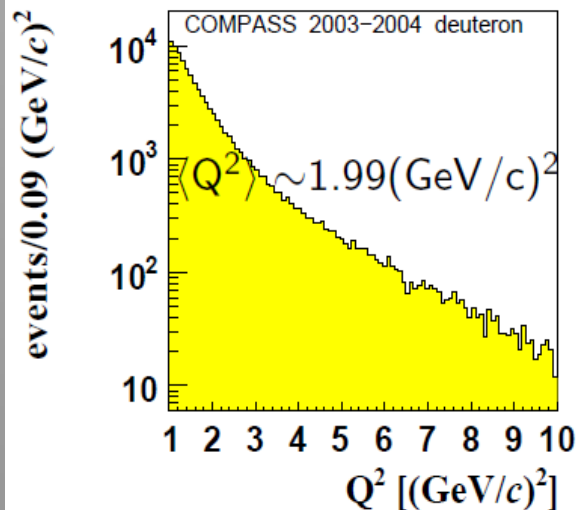


Exclusive ρ^0 production - kinematical distributions

protons

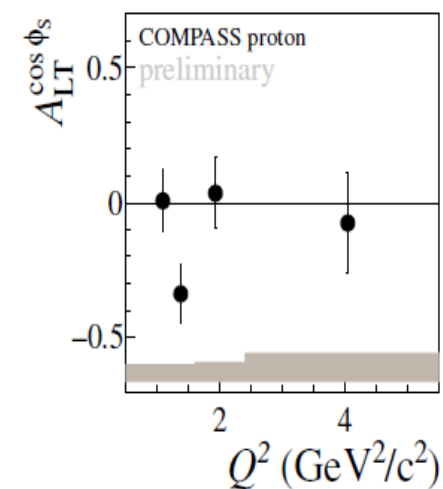
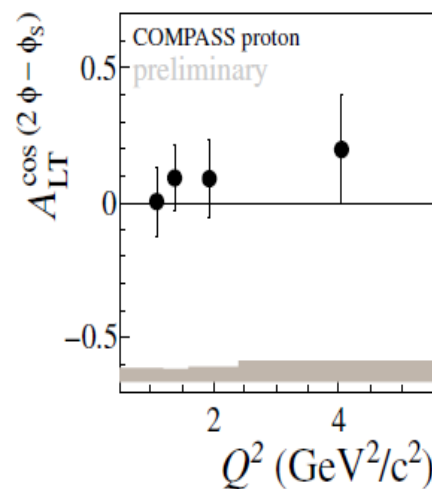
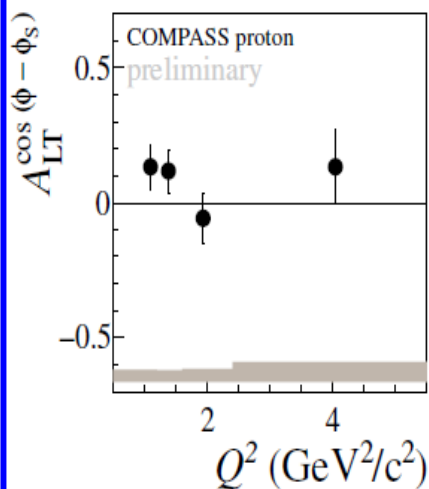
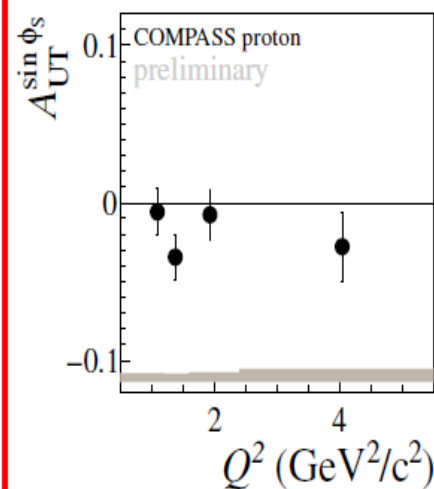
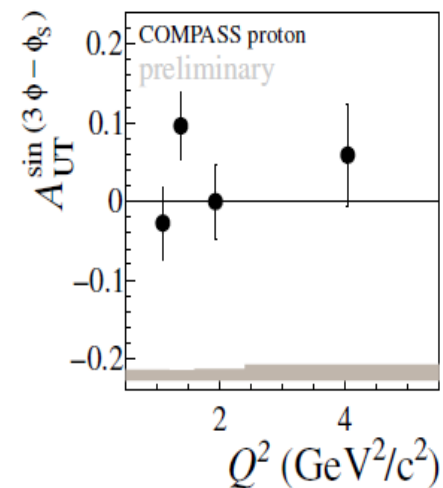
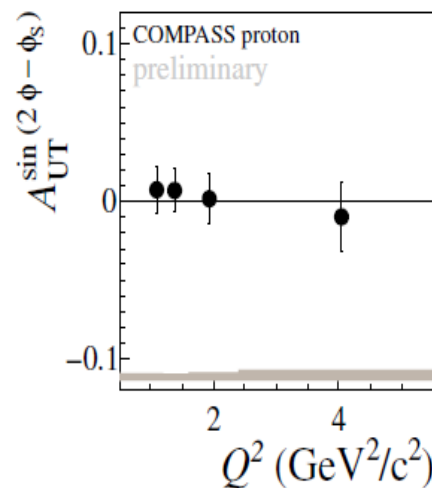
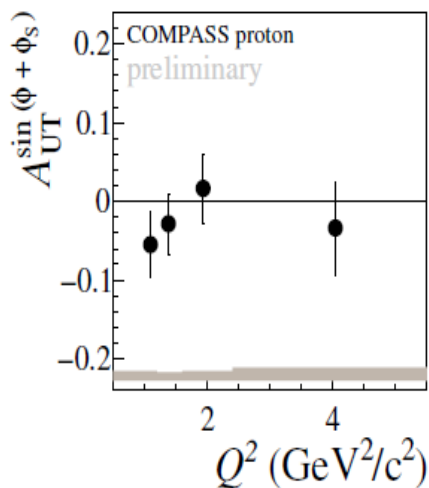
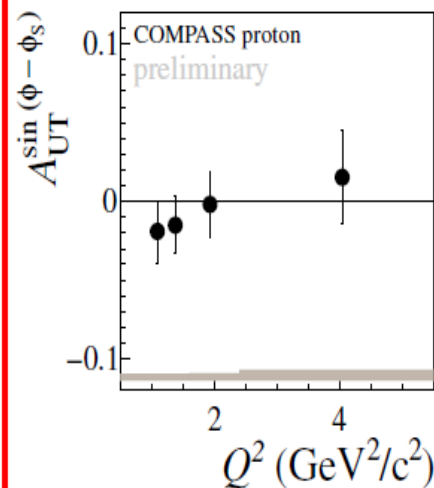


deuterons



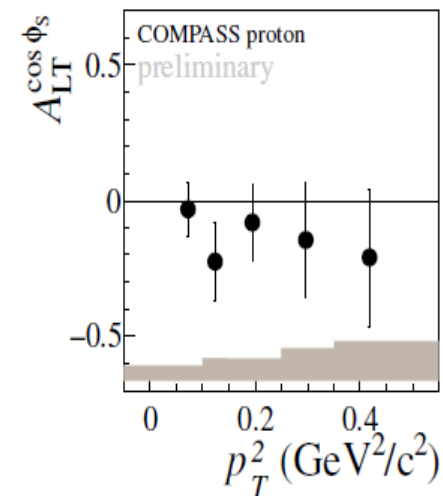
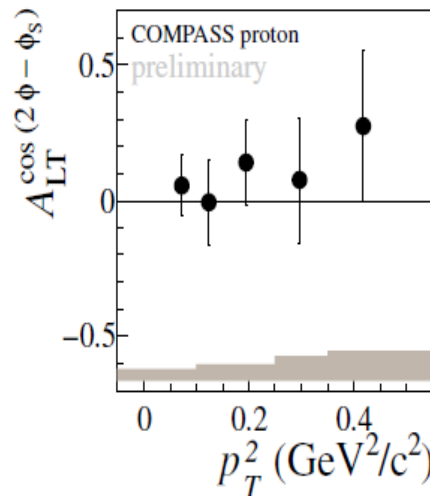
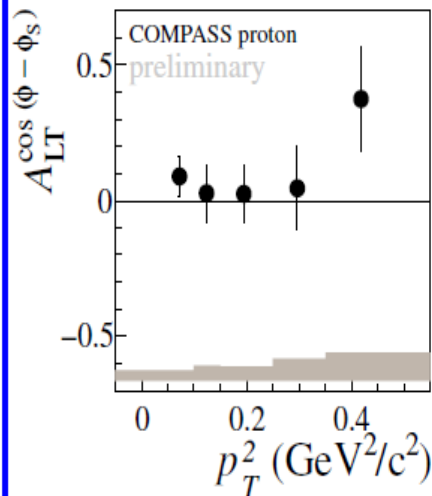
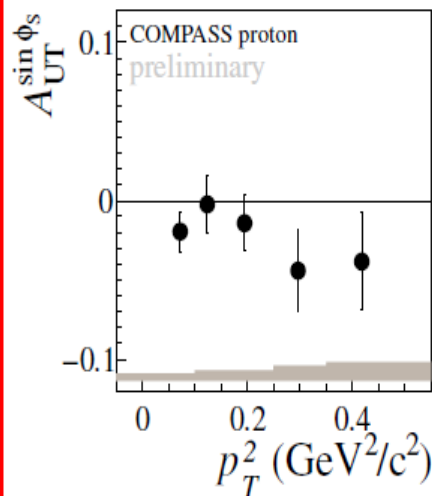
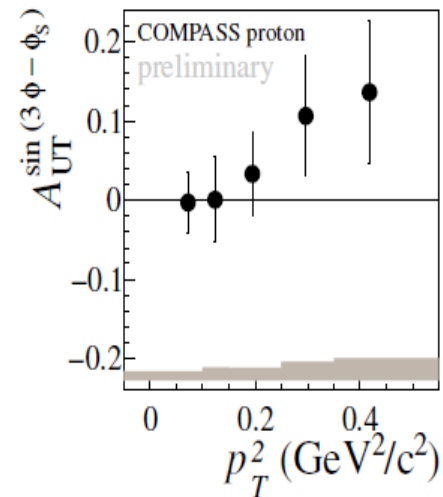
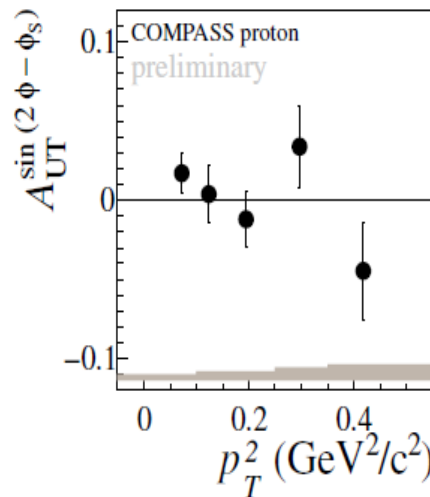
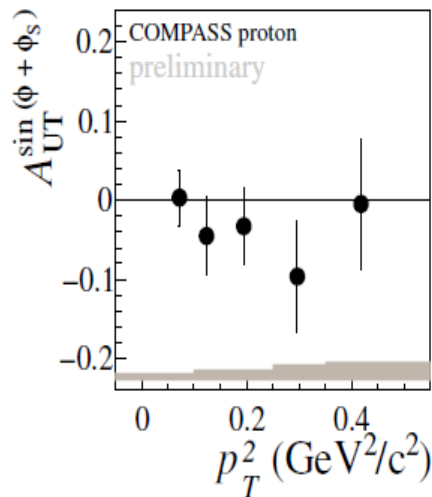
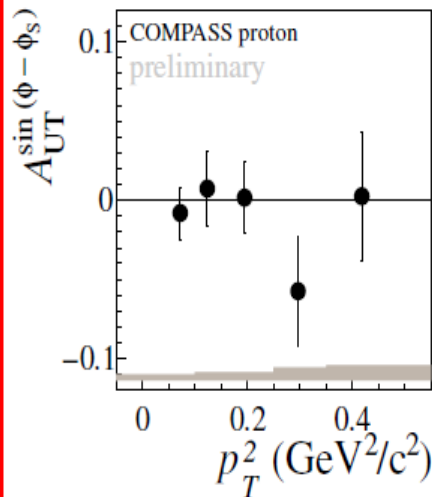
Asymmetry $A_{UT,LT}$ - NH_3 target (2007&2010)

as a function of Q^2

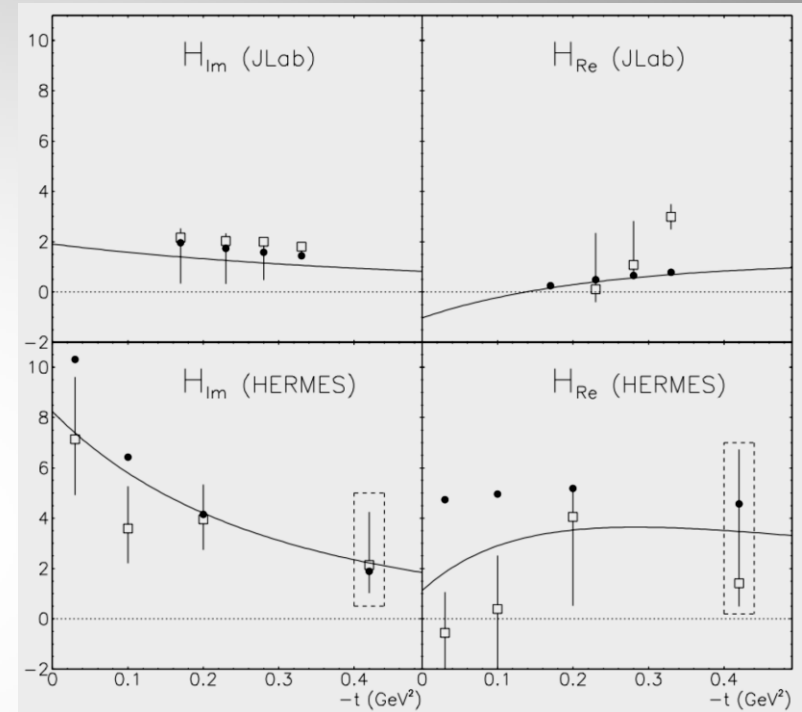
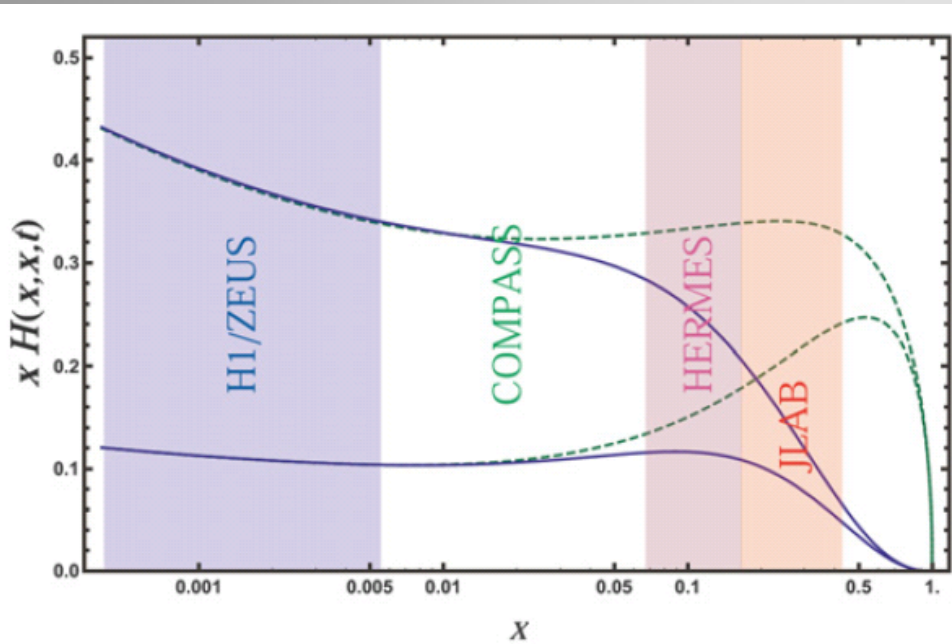


Asymmetry $A_{UT,LT}$ - NH_3 target (2007&2010)

as a function of p_T^2



Extraction of GPDs



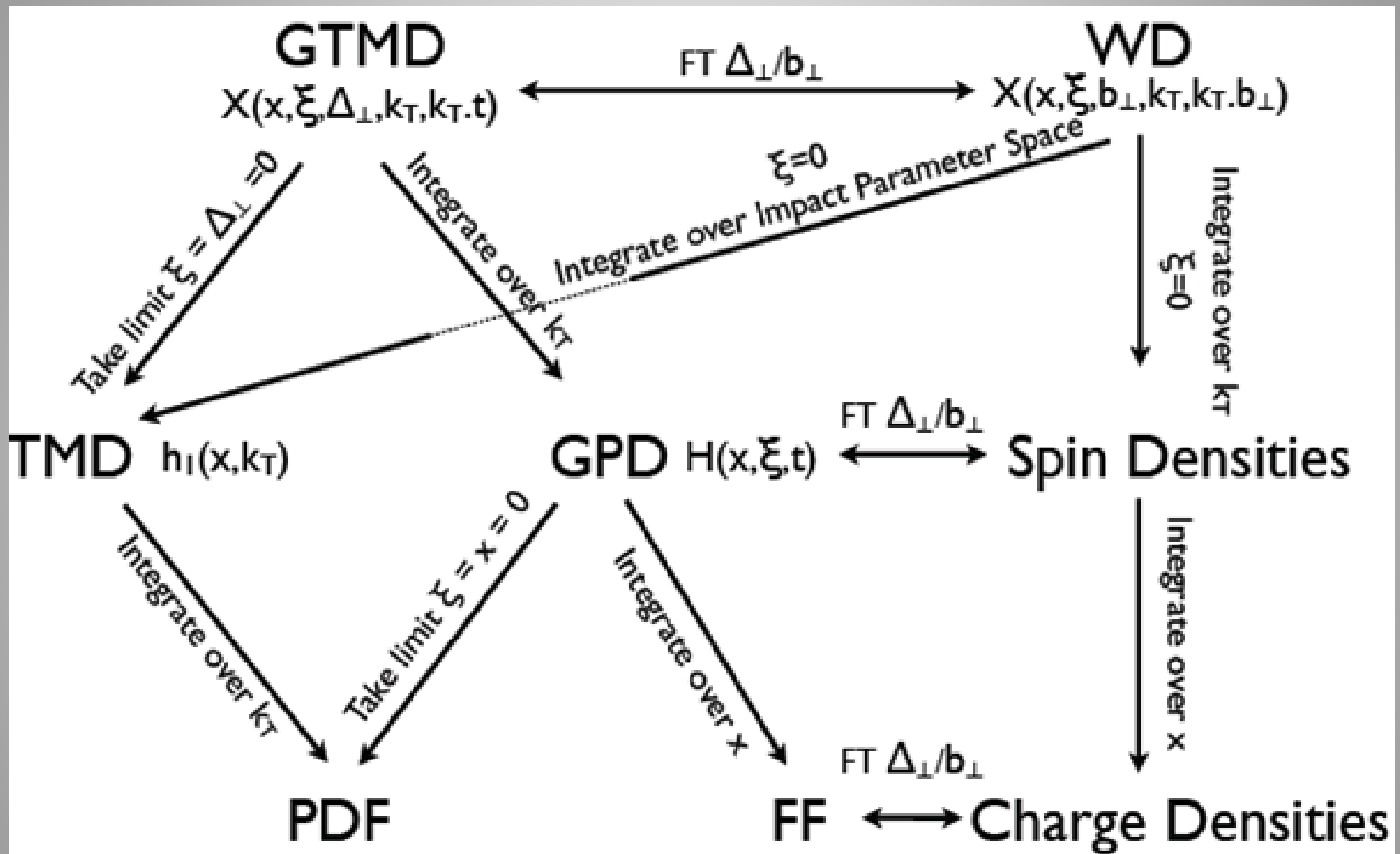
- Postulate GPDs from first principle models

*K. Kumerički and D. Müller,
Nucl. Phys. B 841, (2010) 1*

- Fit Compton form factors to asymmetry data

*M. Guidal and H. Moutarde,
Eur.Phys.J. A 42 (2009) 71*

Contemporary hierarchy of parton distributions



Courtesy M. Murray, Glasgow

Fourier Amplitudes

$$\left| \tau_{BH} \right|^2 = \frac{K_{BH}}{P_1(\phi)P_2(\phi)} \left\{ \sum_{n=0}^2 c_n^{BH} \cos(n\phi) + s_1^{BH} \sin(\phi) \right\}$$

$$\left| \tau_{DVCS} \right|^2 = K_{DVCS} \left\{ \sum_{n=0}^2 c_n^{DVCS} \cos(n\phi) + \sum_{n=1}^2 s_n^{DVCS} \sin(n\phi) \right\}$$

$$I = - \frac{K_I e_I}{P_1(\phi)P_2(\phi)} K_{DVCS} \left\{ \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^3 s_n^I \sin(n\phi) \right\}$$

Azimuthal asymmetries in DVCS

• Cross section

$$\sigma_{LU}(\phi; P_B, C_B) = \sigma_{UU} [1 + \boxed{P_B} A_{LU}^{DVCS} + \boxed{C_B P_B} A'_{LU} + \boxed{C_B} A_C]$$

• Beam-charge asymmetry

$$A_C(\phi) = \frac{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) - (\sigma^{-\leftarrow} + \sigma^{-\rightarrow})}{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) + (\sigma^{-\leftarrow} + \sigma^{-\rightarrow})} = -\frac{1}{D(\phi)} \frac{x_B}{y} \sum_{n=0}^3 \boxed{c'_n} \cos(n\phi)$$

• Charge-difference beam-helicity asymmetry

$$A'_{LU}(\phi) = \frac{(\sigma^{+\rightarrow} - \sigma^{+\leftarrow}) - (\sigma^{-\rightarrow} - \sigma^{-\leftarrow})}{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} + \sigma^{-\leftarrow})} = -\frac{1}{D(\phi)} \frac{x_B}{y} \sum_{n=1}^2 \boxed{s'_n} \sin(n\phi)$$

• Charge-averaged beam-helicity asymmetry

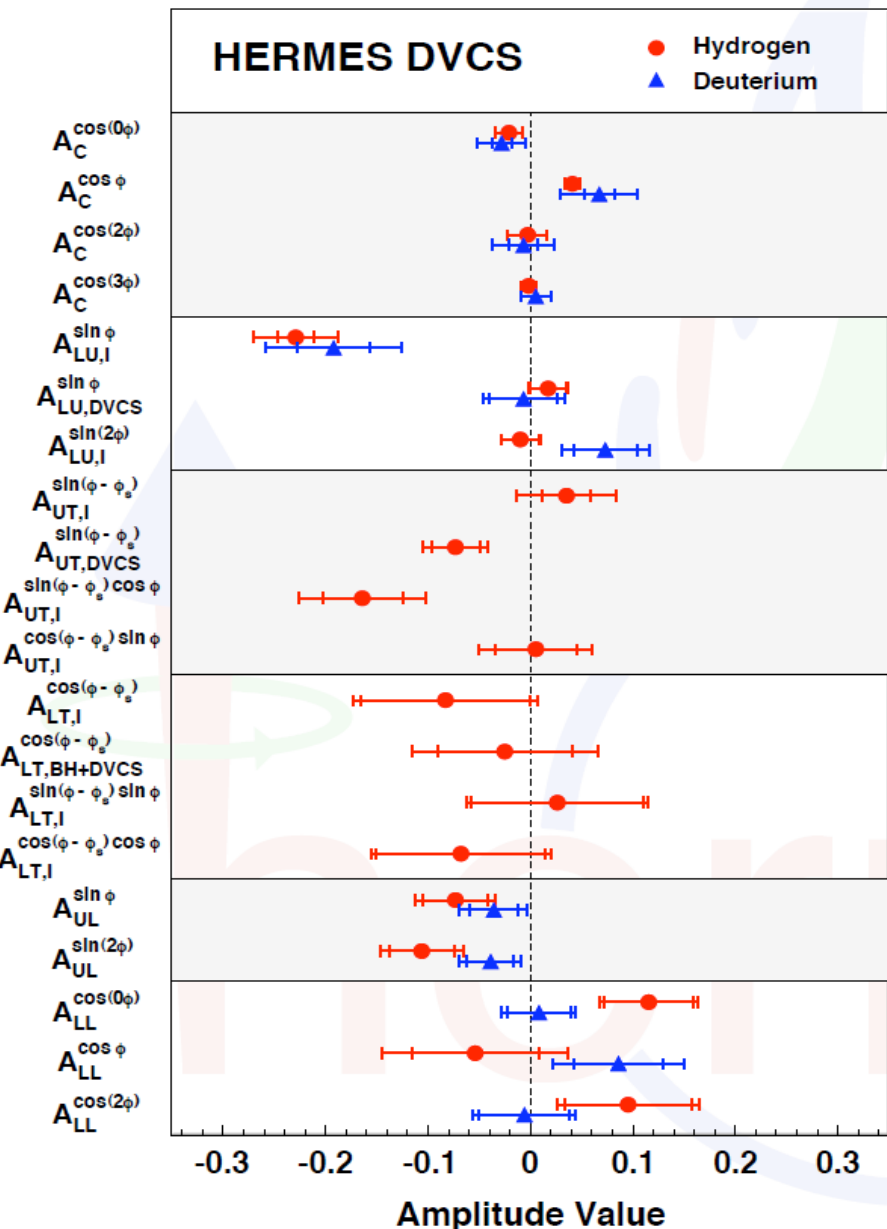
$$A_{LU}^{DVCS}(\phi) = \frac{(\sigma^{+\rightarrow} - \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} - \sigma^{-\leftarrow})}{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) + (\sigma^{-\leftarrow} + \sigma^{-\rightarrow})} = \frac{1}{D(\phi)} \cdot \frac{x_B^2 t \mathcal{P}_1(\phi) \mathcal{P}_2(\phi)}{Q^2} \boxed{s_1^{DVCS}} \sin(\phi)$$

• Separation of contributions from DVCS and interference term

• Impossible in case of single-charge beam-helicity asymmetry

$$A_{LU}(\phi) = \frac{\sigma^{\rightarrow} - \sigma^{\leftarrow}}{\sigma^{\rightarrow} + \sigma^{\leftarrow}}$$

HERMES measured a wealth of azimuthal amplitudes



Beam-charge asymmetry:

GPD H

PRD 75 (2007) 011103

NPB 829 (2010) 1

JHEP 11 (2009) 083

PRC 81 (2010) 035202

Beam-helicity asymmetry:

GPD H

PRL 87 (2001) 182001

JHEP 07 (2012) 032

Transverse target spin asymmetries:

GPD E from proton target

JHEP 06 (2008) 066

PLB 704 (2011) 15

Longitudinal target spin asymmetry:

GPD \tilde{H}

JHEP 06 (2010) 019

Double-spin asymmetry:

GPD \tilde{H}

NPB 842 (2011) 265