

# COMPASS results on the nucleon longitudinal spin structure

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**Introduction**

**Gluon polarisation**

**Proton spin structure function**

**Summary**



## Introduction

Gluon polarisation

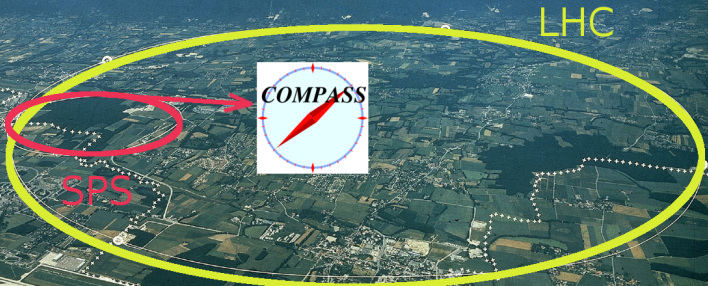
Proton spin structure function

Summary



# COMPASS

COMmon MUon PROton APPARATUS for STRUCTURE and SPECTROSCOPY



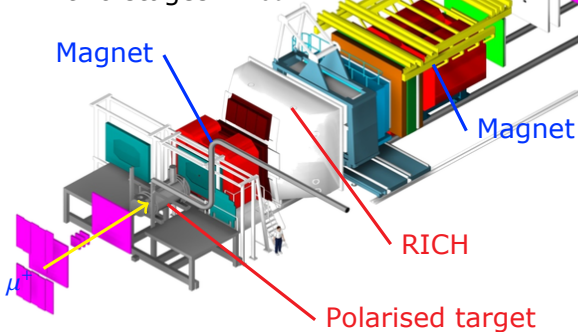
taken from <http://www.physics.ohio-state.edu/~smg/group/cern1.jpg>



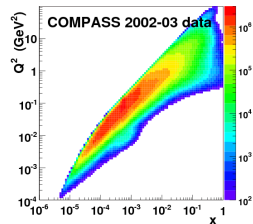
# COMPASS

## Setup

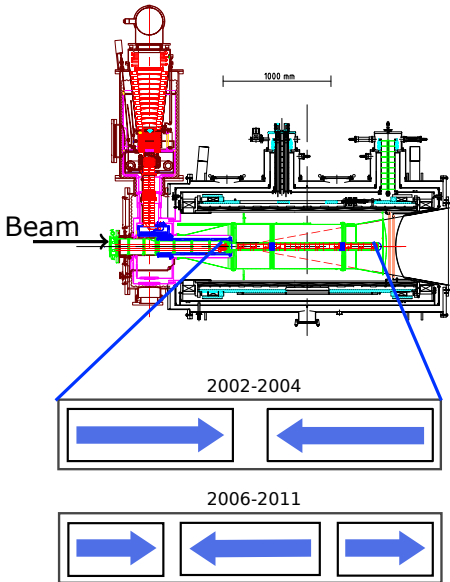
- ▶ Polarised  $\mu^+$  beam with 160/200 GeV energy
- ▶  $1 \times 10^8$  muons per spill
  - ▶ spill:  $\sim 10$  sec.
  - ▶ cycle time:  $\sim 50$  sec.
  - ▶ Beam polarisation:  $\sim 80\%$
- ▶ acceptance:  $\sim \pm 180$  mrad
- ▶ two stages:  $\sim 60$  m



$\mu$  filter



Kinematic acceptance



- ▶ Target cell
  - ▶ -2004: 2 cells
  - ▶ 2006-: 3 cells
- ▶ Target material
  - ▶ -2006:  ${}^6\text{LiD}$
  - ▶ 2007-:  $\text{NH}_3$
- ▶ Polarisation
  - ▶  ${}^6\text{LiD} \sim 50\%$
  - ▶  $\text{NH}_3 \sim 90\%$
- ▶ Rotate magnetic field to cancel acceptance difference
- ▶ Reverse microwave once in a while to cancel correlations



# COMPASS data taking



Year	Target	$E_{beam}$	Detail	
<b>2002</b>	<b>Deuteron</b>	160	Longitudinal mode (~20 % transverse mode)	
<b>2003</b>	<b>Deuteron</b>	160	Longitudinal mode (~20 % transverse mode)	
<b>2004</b>	<b>Deuteron</b>	160	Longitudinal mode (~20 % transverse mode)	
2005			Shutdown & upgrade	
<b>2006</b>	<b>Deuteron</b>	160	New setup, longitudinal mode	
<b>2007</b>	<b>Proton</b>	160	1/2 longitudinal, 1/2 transverse	
2008			Hadron physics	
2009			Hadron physics	
2010	Proton	160	Transverse	
<b>2011</b>	<b>Proton</b>	<b>200</b>	Longitudinal	
2012	Hydrogen		Hadron physics (Primakoff) + DVCS test run and SIDIS	
2013			Shutdown & upgrade	
2014	Proton		Drell-Yan	
2015	Proton		Drell-Yan	
2016	Hydrogen		DVCS	
2017	Hydrogen		DVCS	



# List of talks related to COMPASS

in PANIC2014



<b>Date</b>	<b>Title</b>
-------------	--------------

- 
- |        |  |
|--------|--|
| 25.Aug | Transverse structure of the nucleon at COMPASS   |
| 25.Aug | Polarised Drell-Yan measurement in the COMPASS experiment at CERN                          |
| 25.Aug | COMPASS polarized target for pion-induced Drell-Yan experiment                             |
| 25.Aug | COMPASS results on the nucleon longitudinal spin structure                                 |
| 26.Aug | The GPD physics program at COMPASS: present results and future perspectives                |
| 28.Aug | Studies of light mesons at COMPASS   |
| 28.Aug | Test of the OZI rule and spin alignment measurements with the COMPASS > experiment at CERN |





Introduction

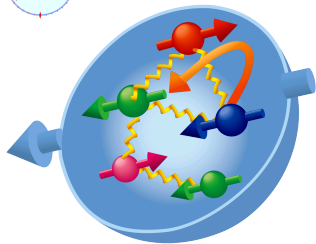
**Gluon polarisation**

Proton spin structure function

Summary



# Spin crisis



$$S_N = \frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_{q,g}$$

## Quarks

Well known

$$\Delta\Sigma = 0.30 \pm 0.01 \pm 0.02$$

*PLB 647 (2007) 8*

## Gluons

Poorly known

$$\Delta G = 0?, \neq 0?, > 0?, < 0?$$

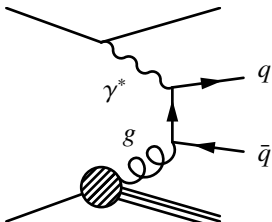
COMPASS, HERMES,  
CLAS, STAR, PHENIX  
give hints.

## Angular Orbital Moment

unknown

Future GPDs  
measurements give  
hints.

## Photon Gluon Fusion



$$A_{PGF} = \frac{N_{PGF}^{\leftarrow} - N_{PGF}^{\rightarrow}}{N_{PGF}^{\leftarrow} + N_{PGF}^{\rightarrow}}$$

$$\Rightarrow \Delta G/G$$

$N_{PGF}$ : the number of PGF events

## Methods

- ▶ High- $p_T$  hadron pair ( $Q^2 > 1$  and  $Q^2 < 1$ )
  - $\gamma^* g \rightarrow q\bar{q} \Rightarrow h^+h^-$  or 2 jets
  - ☺ High statistics
  - ☹ large physical backgrounds, strong MC dependence
- ▶ Open charm meson
  - $\gamma^* g \rightarrow c\bar{c} \Rightarrow D^0$  meson
  - ☺ Pure PGF events, weak MC dependence
  - ☹ Low statistics

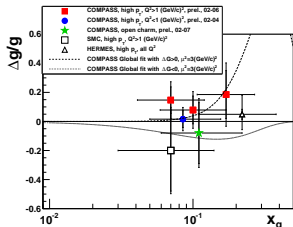


# $\Delta g/g$ results @ COMPASS

Recent published results

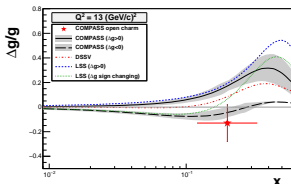


## LO @ high- $p_T$ hadron pair



PLB 718 (2013) 922

## NLO @ open charm



PRD 87 (2013) 052018

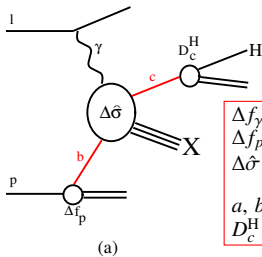
## $\Delta g/g$ @ COMPASS

- ▶  $+0.02 \pm 0.09 \pm 0.06$  @  $x_g = \langle 0.01 \rangle$  LO, high- $p_T$  pair,  $Q^2 < 1$ , PLB 633 (2006) 25
- ▶  $+0.13 \pm 0.06 \pm 0.06$  @  $x_g = \langle 0.09 \rangle$  LO, high- $p_T$  pair,  $Q^2 > 1$ , PLB 718 (2013) 922
- ▶  $-0.47 \pm 0.44 \pm 0.15$  @  $x_g = \langle 0.11 \rangle$  LO, open charm, arXiv:0802.3023
- ▶  $-0.49 \pm 0.27 \pm 0.11$  @  $x_g = \langle 0.11 \rangle$  LO, open charm, PLB 676 (2009) 31
- ▶  $-0.06 \pm 0.21 \pm 0.08$  @  $x_g = \langle 0.20 \rangle$  LO, open charm, PRD 87 (2013) 052018
- ▶  $-0.13 \pm 0.15 \pm 0.15$  @  $x_g = \langle 0.11 \rangle$  NLO, open charm, PRD 87 (2013) 052018

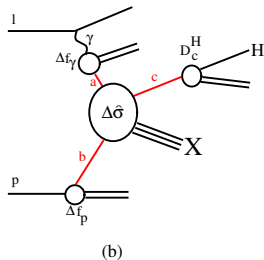
- ▶ based on JSV framework (EPJ C44 (2005) 533)
- ▶ collinear pQCD analysis at NLO
- ▶ photoproduction of single inclusive hadrons:  $l + N \rightarrow l' + H + X$   
 $Q^2 < 1 (\text{GeV}/c)^2$

## Direct $\gamma$ -contribution

## Resolved $\gamma$ -contribution



$\Delta f_\gamma$ : Photon's parton density  
 $\Delta f_p$ : Nucleon  $p$ 's parton density  
 $\Delta \hat{\sigma}$ : spin-dependent partonic  
 hard scattering cross section  
 $a, b, c = q, \bar{q}, g$   
 $D_c^H$ : fragmentation function

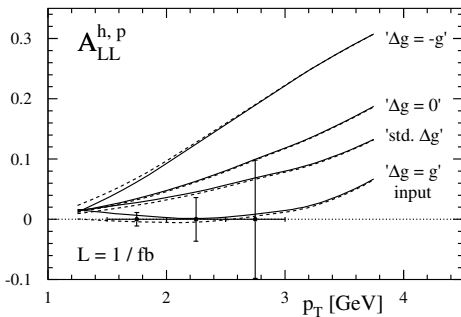
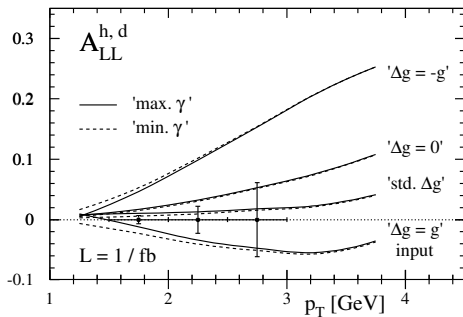




# Theoretical estimations of $A_{LL}$



Ref: EPJC 44 (2005) 533, Fig. 7



$$\blacktriangleright A_{LL} \equiv \frac{d\Delta\sigma}{d\sigma}$$

- ▶ Small impact of resolved photon PDF uncertainty at low- $p_T$
- ▶ Luminosity is estimated as  $4 \text{ fb}^{-1}$   
 $\Rightarrow$  error bars becomes half



# Comparison unpolarised cross section

COMPASS data v.s. theoretical calculation



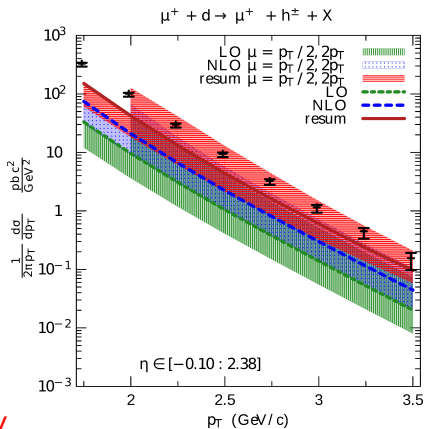
## COMPASS data in 2004

- ▶ C. Adolph, *et. al.*, PRD 88 (2013) 091101
- ▶  $\mu + d \rightarrow \mu' + h^\pm + X$  cross section at  $Q^2 < 0.1$  (GeV/c)<sup>2</sup>

## Theoretical calculations

- ▶ D. Florian, *et. al.*, PRD 88 (2013) 014024
- ▶ Higher-order QCD corrections to the cross section
- ▶ Large logarithmic "threshold" corrections  
→ improved the agreement between data and theory

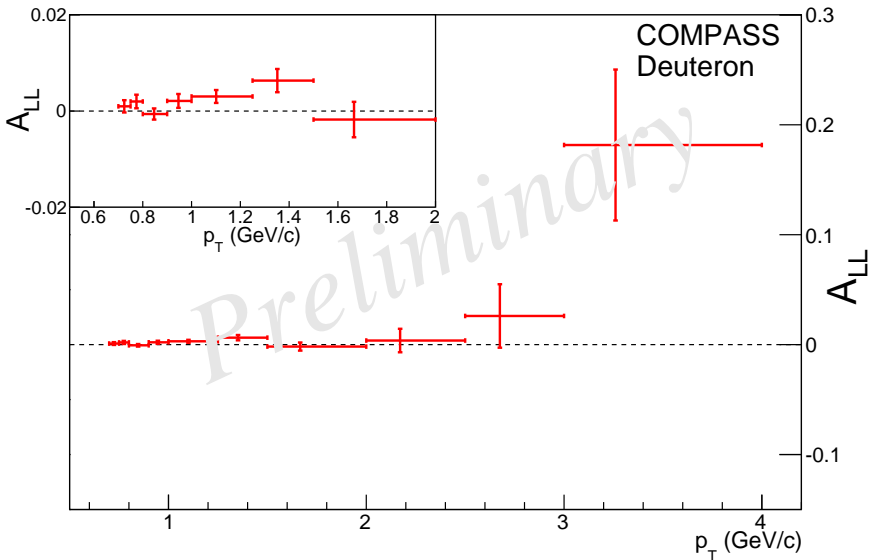
⇒ Valid within theoretical uncertainty





# Results: asymmetry

Deuteron

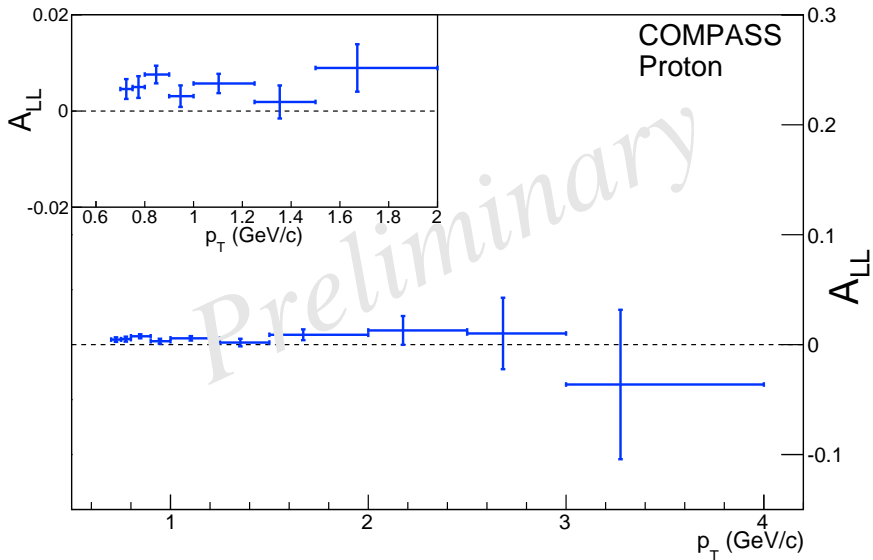


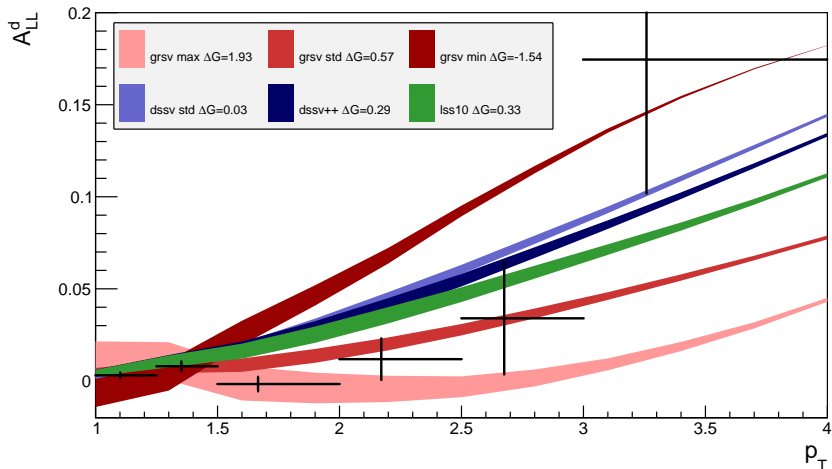




# Results: asymmetry

Proton



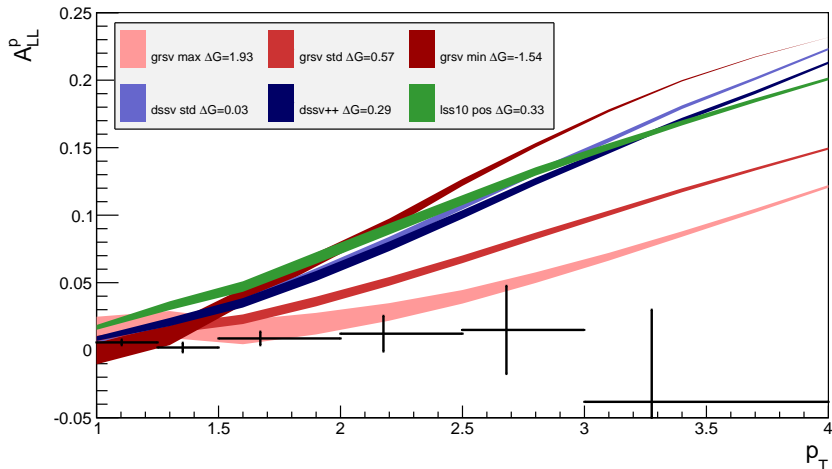


- ▶ Calculations suggest a high positive  $\Delta G$
- ▶ No calculations drawn with gluon resummation  
 → to be available in the very near future



# Comparison: Proton $A_{LL}^p$

NLO calculation from W. Vogelsang, M. Stratmann and B. Jäger codes



- ▶ no PDF can yet explain  $A_{LL}^p$  at quite high  $\Delta G$
- ▶ No calculations drawn with gluon resummation  
→ to be available in the very near future



Introduction

Gluon polarisation

**Proton spin structure function**

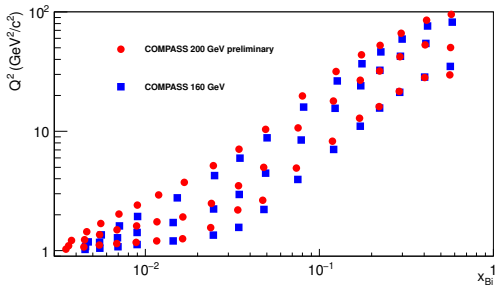
Summary



# $A_1, g_1$ extraction from double spin asymmetry

- ▶  $A_{LL} = \frac{1}{P_{beam} \cdot P_{target} \cdot f} \cdot \frac{N^{\leftarrow} - N^{\rightarrow}}{N^{\leftarrow} + N^{\rightarrow}} = D(A_1 + \eta A_2) \simeq DA_1$
- ▶  $A_1 = \frac{g_1 - \gamma^2 g_2}{F_1} \simeq \frac{g_1}{F_1}$
- ▶  $g_1 = \frac{F_2}{2x(1+R)} A_1, \quad R \equiv \frac{\sigma_L}{\sigma_T}$

- ▶ Data taken in 2007 with 160 GeV/c and 2011 with 200 GeV/c

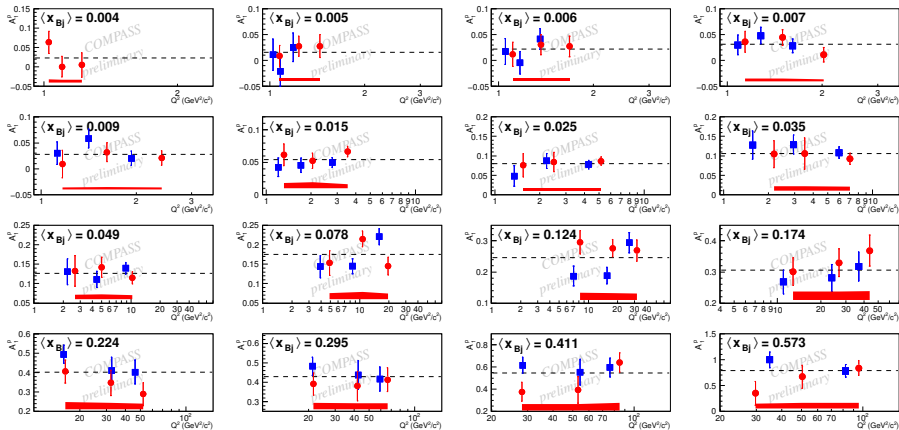




# A<sub>1</sub> results



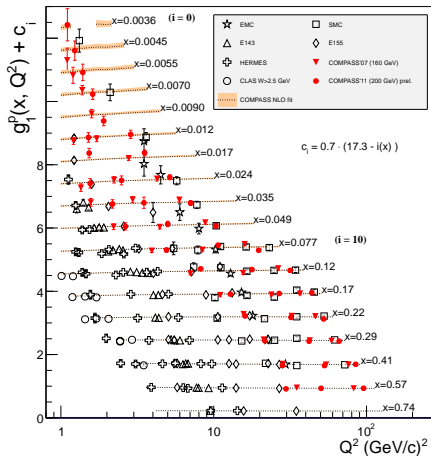
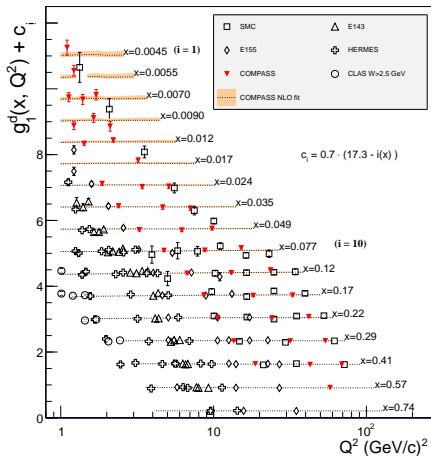
COMPASS 200 GeV prel.      COMPASS 160 GeV      --- const fit



- ▶ New asymmetries at low  $x$
- ▶ No  $Q^2$  dependencies



# World data of $g_1^d$ and $g_1^p$

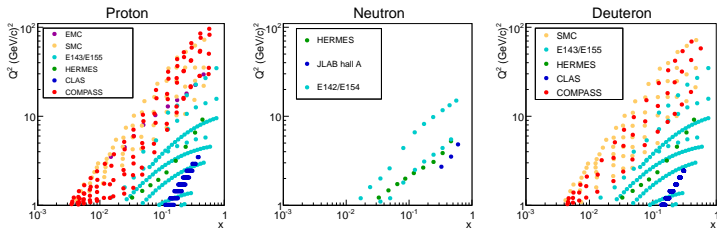


- ▶ New COMPASS point for the proton at low  $x$
- ▶ New COMPASS NLO QCD fit describes the data well



# NLO QCD fit

## Inputs and constrains



- ▶ 139 out of 679 data points

$$\text{▶ } g_1^{p(n)} = \frac{1}{9} \left( C_s \otimes \Delta q_s + C_{NS} \otimes \left[ \pm \frac{3}{4} \Delta q_3 + \frac{1}{4} \Delta q_8 \right] + C_g \otimes \Delta g \right)$$

- ▶  $\Delta q_s = \Delta u + \Delta d + \Delta s$
- ▶  $\Delta q_3 = \Delta u - \Delta d$
- ▶  $\Delta q_8 = \Delta u + \Delta d - 2\Delta s$
- ▶  $C_s, C_{NS}, C_g$ : Wilson coefficients

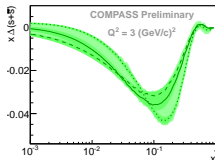
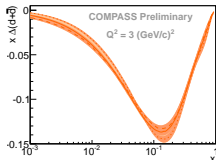
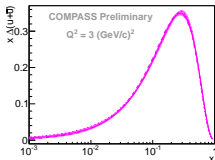
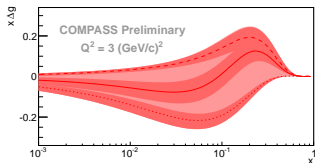
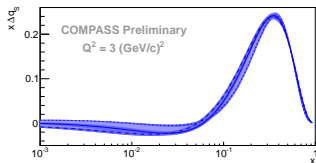
- ▶ Positivity constrains:  $|\Delta(s + \bar{s})| < (s + \bar{s}), |\Delta g| < g$





# NLO QCD fit

## Results



- ▶ Depending on  $\Delta G$  solutions:  $\Delta G > 0$ ,  $\Delta G \sim 0$ ,  $\Delta G < 0$
- ▶  $0.256 < \Delta\Sigma < 0.336$  at  $Q^2 = 3 \text{ (GeV/c)}^2$
- ▶ Uncertainty comes from the lack of
  - ▶ knowledge of functional form
  - ▶ data point to constrain gluon distribution



Introduction

Gluon polarisation

Proton spin structure function

**Summary**



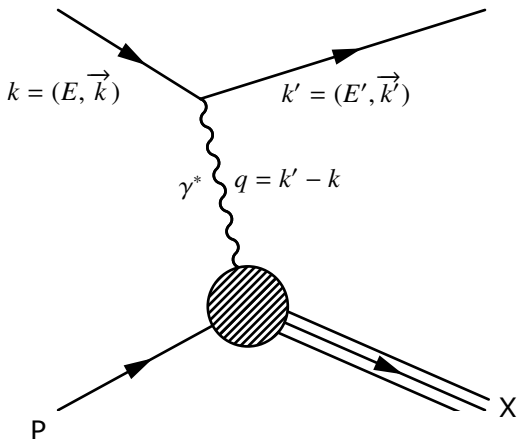
## Gluon polarisation

- ▶  $A_{LL}$  for single hadron photoproduction at high- $p_T$  on proton and deuteron targets
- ▶ Present NLO calculations do not agree simultaneously with deuteron and proton data
- ▶ Extraction of  $\Delta G$  from  $A_{LL}$  done after the inclusion of soft gluon resummation

## Proton spin structure function

- ▶ New measurements of  $A_1^P$  and  $g_1^P$  at 200 GeV/c
- ▶ Updated NLO QCD fit for  $g_1$  world data
- ▶ Extraction of polarised PDF for each flavour

# Backup

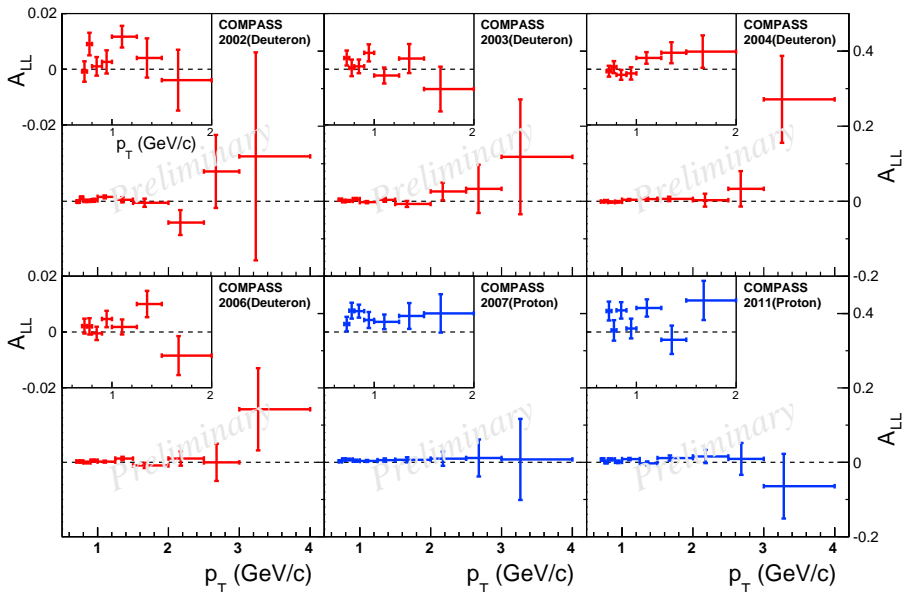


- ▶  $k = (E, \vec{k})$
- ▶  $k' = (E', \vec{k}')$
- ▶  $q = k' - k$
- ▶  $Q^2 = -q^2$
- ▶  $\nu = E - E'$
- ▶  $x_{Bj} = \frac{Q^2}{2M\nu}$
- ▶  $y = \frac{E-E'}{E}$



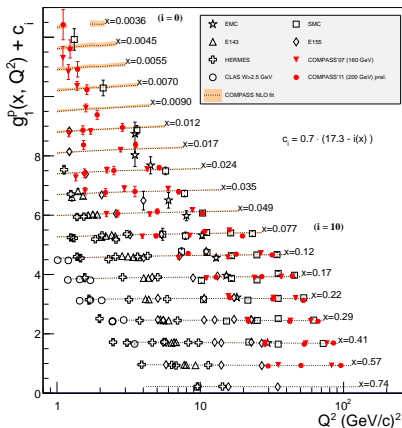
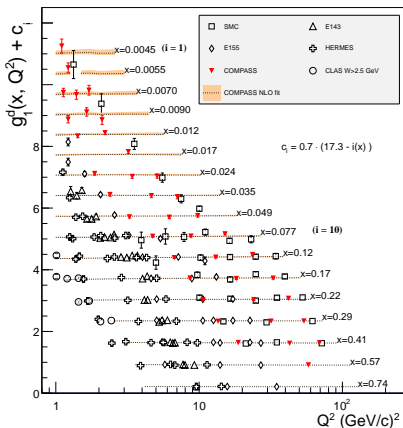
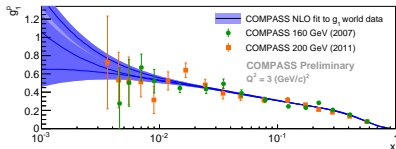
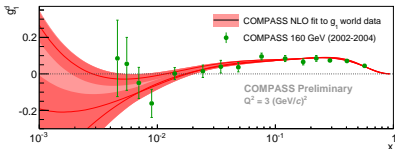
# Results: asymmetry

Year by year





# $g_1$ NLO fit results





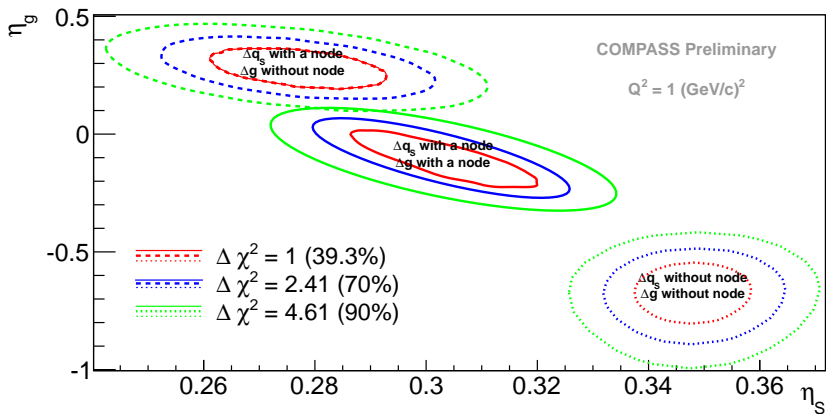
# $\Delta G$ v.s. $\Delta\Sigma$



$$\eta_g \rightarrow \Delta G$$

$$\eta_s \rightarrow \Delta\Sigma$$

$$Q^2 = 1 \text{ (GeV/c)}^2$$



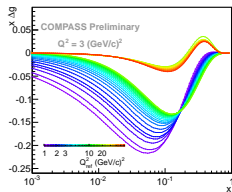
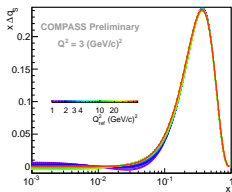




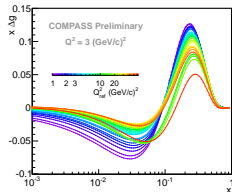
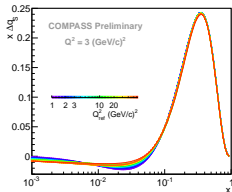
# $x\Delta g$ with difference $Q_0^2$ inputs



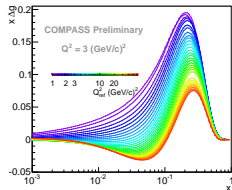
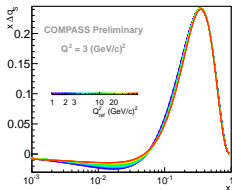
$\Delta G < 0$



$\Delta G = 0$



$\Delta G > 0$





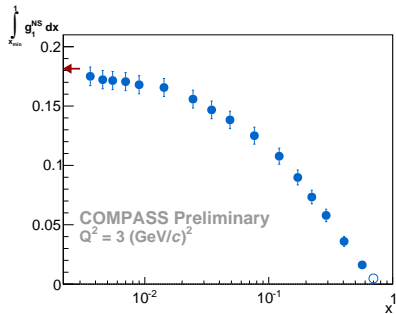
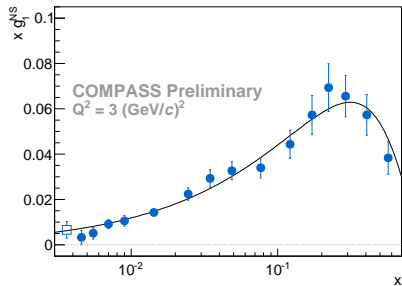
## Bjorken sum rule

$$\Gamma_1^{NS} = \int_0^1 g_1^{NS}(x, Q^2) dx = \frac{1}{6} \left| \frac{g_A}{g_V} \right| C_1^{NS}(Q^2)$$

- ▶ Fundamental QCD prediction connecting p and n
- ▶ Decorrelated from  $\Delta G$
- ▶  $g_1^{NS} = g_1^p - g_1^n = 2 \left[ g_1^p - \frac{g_1^d}{1 - 1.5\omega_D} \right], \omega_D = 0.05 \pm 0.01$
- ▶  $C_1^{NS} = 1 - \left( \frac{\alpha_s}{\pi} \right)$  @ NLO
- ▶  $C_1^{NS} = 1 - \left( \frac{\alpha_s}{\pi} \right) - p_1 \cdot \left( \frac{\alpha_s}{\pi} \right)^2$  @ NNLO



# Bjorken sum rule results



- ▶  $\left| \frac{g_A}{g_V} \right| = 1.2701 \pm 0.002$  from neutron  $\beta$  decay
- ▶  $\left| \frac{g_A}{g_V} \right| = 1.220 \pm 0.053(\text{stat.}) \pm 0.095(\text{syst.})$  with  $C_1$  at NLO
- ▶  $\left| \frac{g_A}{g_V} \right| = 1.256 \pm 0.054(\text{stat.}) \pm 0.098(\text{syst.})$  with  $C_1$  at NNLO
- ▶ Bjorken sum rule validated within 4%



# Bjorken sum rule



$$C_1^{NS} = 1 - \left(\frac{\alpha_s}{\pi}\right) - p_1 \cdot \left(\frac{\alpha_s}{\pi}\right)^2 - p_2 \cdot \left(\frac{\alpha_s}{\pi}\right)^3$$

$n_f$	$p_1$	$p_2$
3	3.58333	20.21527
<b>4</b>	<b>3.25000</b>	<b>14.85026</b>

mass of charm quark:  $m_c \sim 1.5 \text{ GeV}/c$