

Pion-photon Reactions and Chiral Dynamics in Primakoff Processes at COMPASS

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for the COMPASS collaboration



**XIth Quark Confinement
and the Hadron Spectrum**

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St. Petersburg 8.-12.9.2014





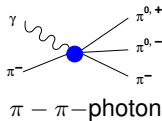
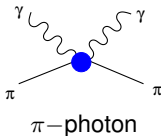
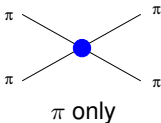
How to understand quark-gluon dynamics?



complicated system of
interacting quarks and gluons

ChPT
→

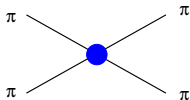
effective degrees of freedom
at low energy: mass, charge,
spin, effective (self-)coupling





- pion scattering lengths: 2-loop predictions

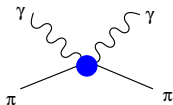
- $a_0^0 m_\pi = 0.220 \pm 0.005$ confirmed by E865 in $K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$
- $(a_0^0 - a_0^2) m_\pi = 0.264 \pm 0.006$ confirmed by NA48 in 0.268 ± 0.010 $K^+ \rightarrow \pi^+ \pi^0 \pi^0$



- pion polarisability: electric α_π , magnetic β_π

- contribution to Compton scattering
- ChPT prediction obtained by the relation to $\pi^+ \rightarrow e^+ \nu_e \gamma$ [Gasser, Ivanov, Sainio, Nucl. Phys. B745, 2006]

$$\begin{aligned}\alpha_\pi + \beta_\pi &= (0.2 \pm 0.1) \cdot 10^{-4} \text{fm}^3 \\ \alpha_\pi - \beta_\pi &= (5.7 \pm 1.0) \cdot 10^{-4} \text{fm}^3 \\ \alpha_\pi &= (2.9 \pm 0.5) \cdot 10^{-4} \text{fm}^3\end{aligned}$$



- ChPT prediction **contradicting** the experimental findings (prior to our analysis)



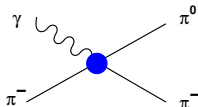
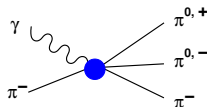
More pion-photon reactions

- Pion scattering including a real photon

- Leading-order prediction from ChPT
 \leftrightarrow pion scattering lengths
 combined with photon coupling
- **chiral loop contribution**
 theory prediction available, no measurement

- **Chiral anomaly $F_{3\pi}$**

- established on 10% level
- further development: inclusion of the ρ resonance
 theoretical work by Kubis, Hoferichter, Sakkas
 PRD86(2012)116009

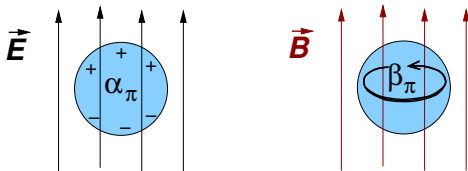




ChPT prediction for the pion polarisability

$$\pi + \gamma \rightarrow \pi + \gamma$$

Compton cross-section contains information about e.m. **polarisability**
(as deviation from the expectation for a pointlike particle)



polarisabilities α_π, β_π [10^{-4} fm^3]

ChPT (2-loop) prediction: $\alpha_\pi - \beta_\pi = 5.7 \pm 1.0$ $\alpha_\pi + \beta_\pi = 0.16$

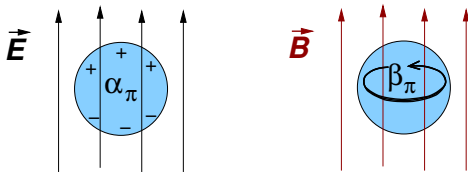
experiments: 4 — 14 ($\beta_\pi \approx -\alpha_\pi$ assumed)



ChPT prediction for the pion polarisability

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Compton cross-section contains information about e.m. **polarisability**
(as deviation from the expectation for a pointlike particle)



polarisabilities α_π, β_π [10^{-4} fm^3]

ChPT (2-loop) prediction: $\alpha_\pi = 2.93, \quad \beta_\pi = -2.77$

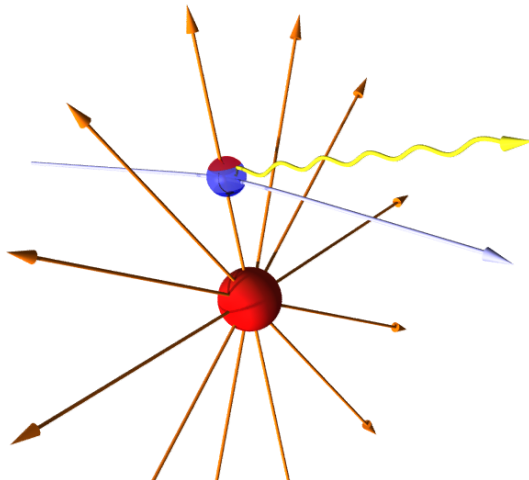
experiments: 2 – 7 ($\beta_\pi \approx -\alpha_\pi$ assumed)



Polarisability effect in Primakoff technique

Primakoff measurement technique

- Charged pion traversing the nuclear **electric field**
 - typical field strength at $r = 5R_{Ni}$: $E \sim 300 \text{ kV/fm}$
- **Bremsstrahlung emission**
 - particle scatters off **equivalent photons**
 - tiny momentum transfer $Q^2 \approx 10^{-5} \text{ GeV}^2/c^2$
 - pion/muon (quasi-)real Compton scattering
- Polarisability contribution
 - Compton cross-section typically diminished
 - expected charge separation $\sim 10^{-5} \text{ fm} \cdot e$

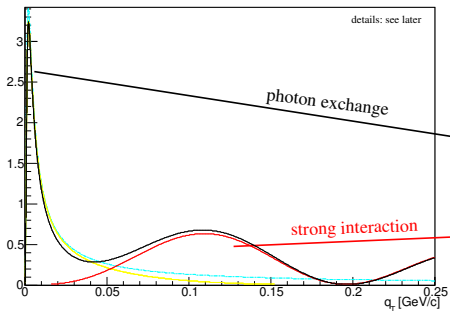




Polarisability effect in Primakoff technique

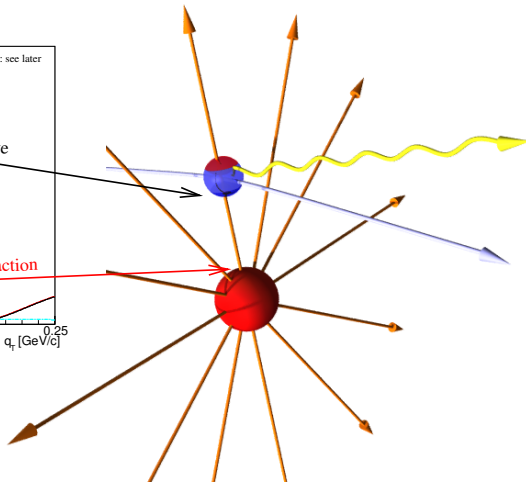
Primakoff measurement technique

- Charged pion traversing the nuclear **electric** field
 - typical field strength at



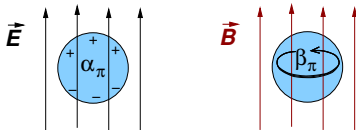
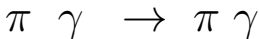
typically diminished

- expected charge separation
 $\sim 10^{-5} \text{ fm} \cdot e$





Pion Compton Scattering



- Two kinematic variables, in CM: total energy \sqrt{s} , scattering angle θ_{cm}

$$\frac{d\sigma_{\pi\gamma}}{d\Omega_{cm}} = \frac{\alpha^2 (s^2 z_+^2 + m_\pi^4 z_-^2)}{s (s z_+ + m_\pi^2 z_-)^2} - \frac{\alpha m_\pi^3 (s - m_\pi^2)^2}{4s^2 (s z_+ + m_\pi^2 z_-)} \cdot \mathcal{P}$$

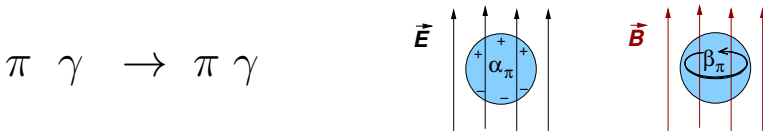
$$\mathcal{P} = z_-^2 (\alpha_\pi - \beta_\pi) + \frac{s^2}{m_\pi^4} z_+^2 (\alpha_\pi + \beta_\pi) - \frac{(s - m_\pi^2)^2}{24s} z_-^3 (\alpha_2 - \beta_2)$$

$$z_\pm = 1 \pm \cos \theta_{cm}$$

- $\sigma_{tot}(s)$ rather insensitive to pion's low-energy structure
- Up to 20% effect on *backward* angular distributions of $d\sigma/d\Omega_{cm}$



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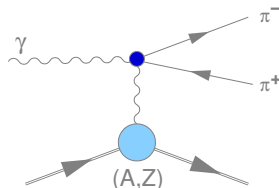
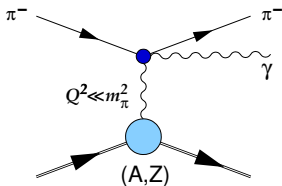
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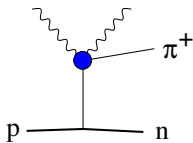
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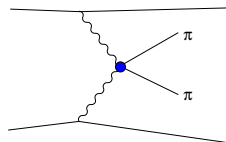
Pion Compton scattering: embedding the process



Primakoff processes



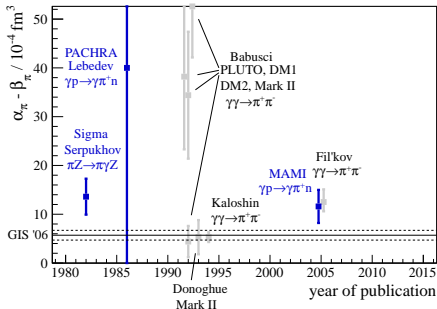
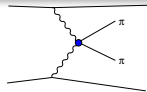
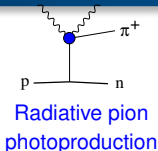
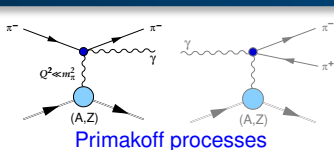
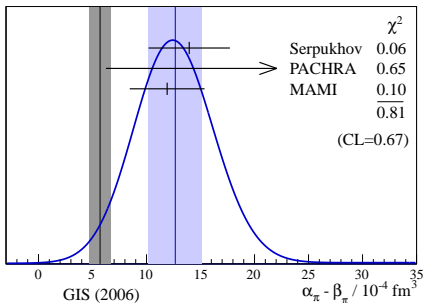
Radiative pion photoproduction



Photon-Photon fusion



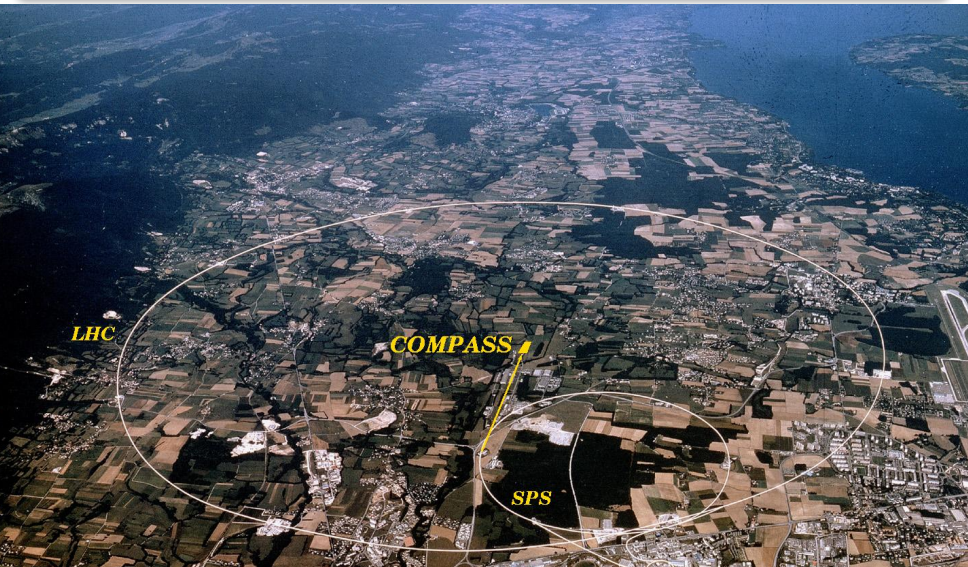
Pion polarisability: world data before COMPASS

world avg.: 12.7 ± 2.5 

GIS'06: ChPT prediction, Gasser, Ivanov, Sainio, NPB745 (2006), plots: T. Nagel, PhD
 Fil'kov analysis objected by Pasquini, Drechsel, Scherer PRC81, 029802 (2010)



Common Muon and Proton Apparatus for Structure and Spectroscopy





Common Muon and Proton Apparatus for Structure and Spectroscopy

CERN SPS: protons ~ 400 GeV (5 – 10 sec spills)

- secondary $\pi, K, (\bar{p})$: up to $2 \cdot 10^7 / \text{s}$
Nov. 2004, 2008-09, 2012:
hadron spec. & Primakoff reactions
- tertiary muons: $4 \cdot 10^7 / \text{s}$
2002-04, 2006-07, 2010-11: spin structure of the nucleon

LHC

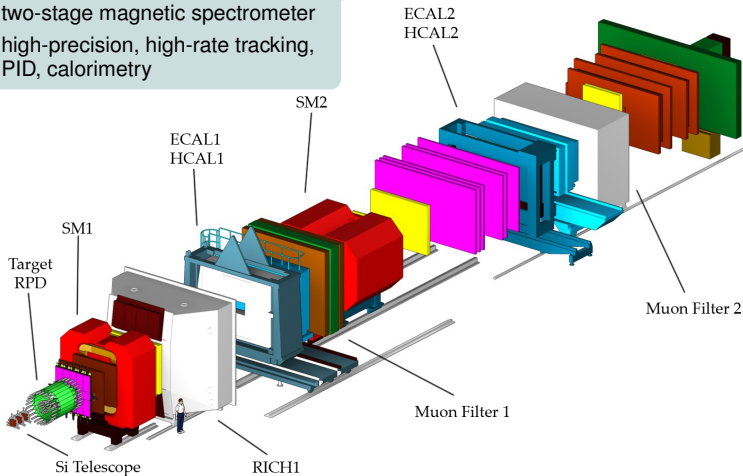
COMPASS

SPS



Fixed-target experiment

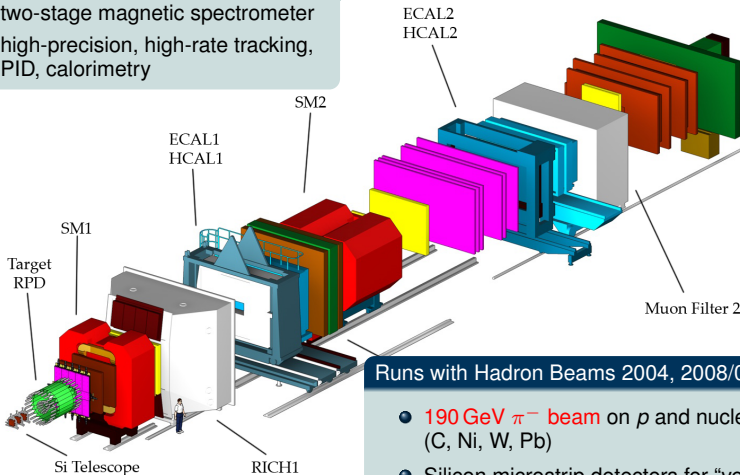
- two-stage magnetic spectrometer
- high-precision, high-rate tracking, PID, calorimetry





Fixed-target experiment

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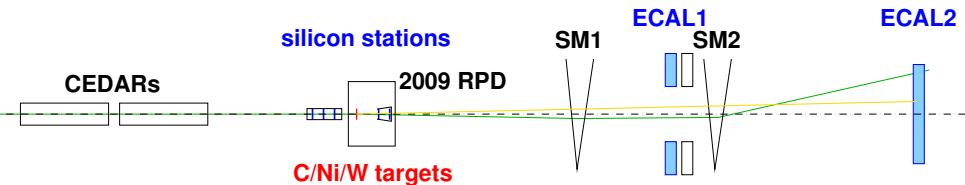


Runs with Hadron Beams 2004, 2008/09, 2012

- **190 GeV π^- beam** on p and nuclear targets (C, Ni, W, Pb)
- Silicon microstrip detectors for “vertexing”
- recoil and (digital) ECAL triggers



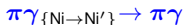
Principle of the measurement





Extraction of the pion polarisability

- Identify exclusive reactions



at smallest momentum transfer $< 0.001 \text{ GeV}^2/c^2$

- Assuming $\alpha_\pi + \beta_\pi = 0$, from the cross-section

$$R = \frac{\sigma(x_\gamma)}{\sigma_{\alpha_\pi=0}(x_\gamma)} = \frac{N_{meas}(x_\gamma)}{N_{sim}(x_\gamma)} = 1 - \frac{3}{2} \cdot \frac{m_\pi^3}{\alpha} \cdot \frac{x_\gamma^2}{1-x_\gamma} \alpha_\pi$$

is derived, depending on $x_\gamma = E_{\gamma(lab)}/E_{Beam}$.

Measuring R the polarisability α_π can be concluded.

- Control systematics by



and





Extraction of the pion polarisability

- Identify **exclusive reactions**



at smallest momentum transfer $< 0.001 \text{ GeV}^2/c^2$

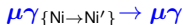
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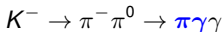
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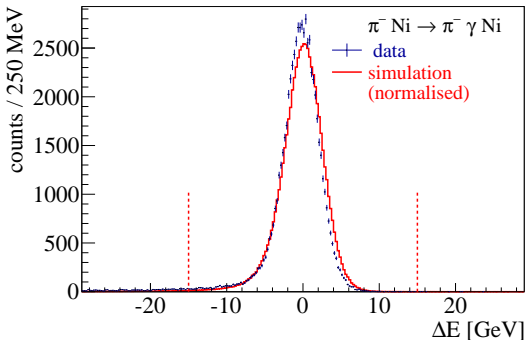
and





Identifying the $\pi\gamma \rightarrow \pi\gamma$ reaction

arxiv:1405.6377v1 subm. to PRL

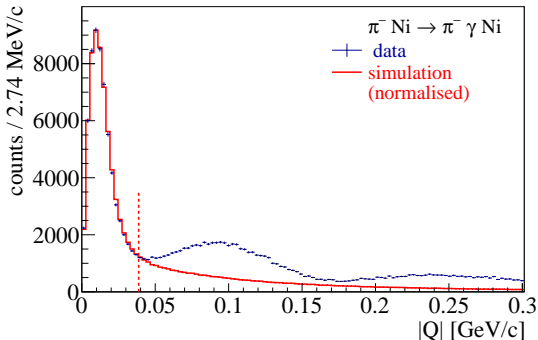


- Energy balance $\Delta E = E_\pi + E_\gamma - E_{\text{Beam}}$
- Exclusivity peak $\sigma \approx 2.6 \text{ GeV}$ (1.4%)
- ~ 63.000 exclusive events ($x_\gamma > 0.4$) (Serpukhov ~ 7000 for $x_\gamma > 0.5$)



Primakoff peak

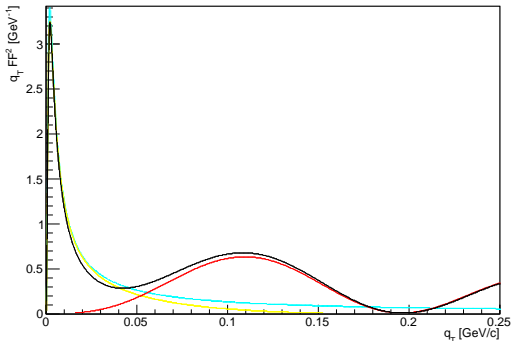
arxiv:1405.6377v1 subm. to PRL



- $\Delta Q_T \approx 12 \text{ MeV}/c$ (190 GeV/c beam \rightarrow requires few- μrad angular resolution)
- first diffractive minimum on Ni nucleus at $Q \approx 190 \text{ MeV}/c$



Photon density squared form factor

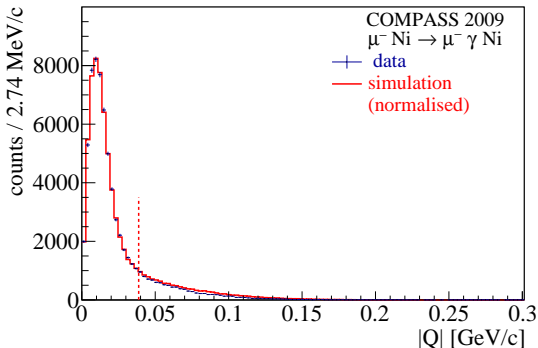


- calculation following G. Fäldt (Phys. Rev. C79, 014607)
- eikonal approximation: pions traverse Coulomb and strong-interaction potentials



Primakoff peak: muon data

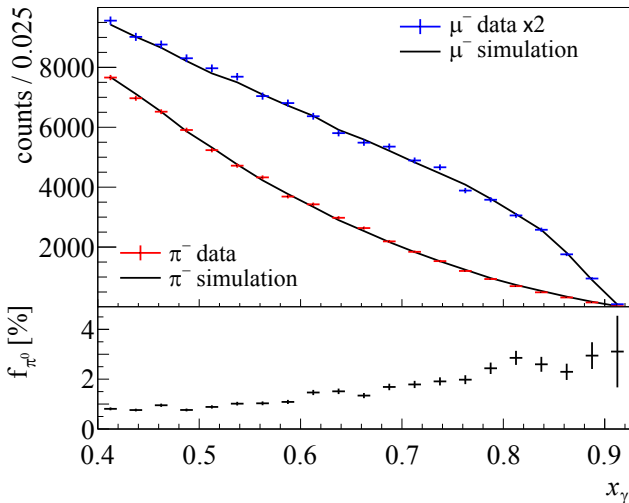
arxiv:1405.6377v1 subm. to PRL



- **muon control measurement:** pure electromagnetic interaction



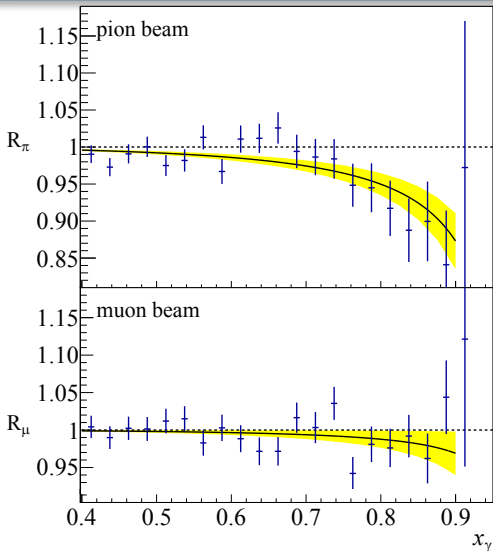
Photon energy spectra for muon and pion beam



arxiv:1405.6377v1 subm. to PRL



Pion polarisability: COMPASS result



$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}}) \times 10^{-4} \text{ fm}^3$$

(assuming $\alpha_\pi = -\beta_\pi$)

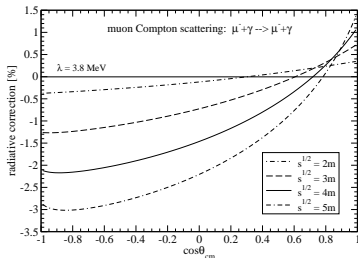
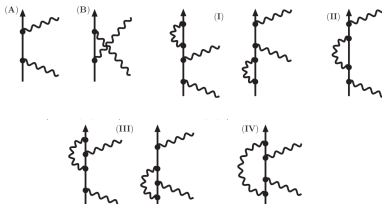
“false polarisability” from muon data:

$$(0.5 \pm 0.5_{\text{stat}}) \times 10^{-4} \text{ fm}^3$$

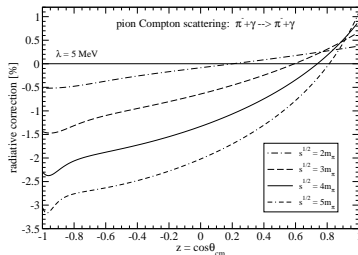
arxiv:1405.6377v1 subm. to PRL



Radiative corrections (Compton scattering part)



Nucl.Phys. A837 (2010)



Eur.Phys.J. A39 (2009) 71



source of systematic uncertainty	estimated magnitude	
	CL = 68 %	$[10^{-4} \text{ fm}^3]$
tracking		0.6
radiative corrections		0.3
background subtraction in Q		0.4
pion electron scattering		0.2
quadratic sum		0.8



source of systematic uncertainty	estimated magnitude CL = 68 % [10 ⁻⁴ fm ³]
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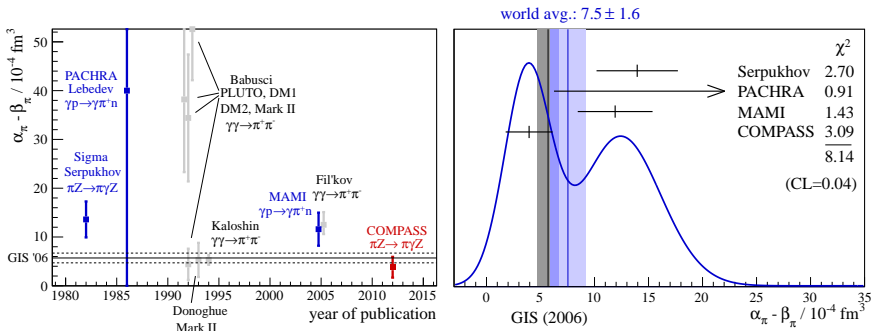
COMPASS result for the pion polarisability:

$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3$$

with $\alpha_\pi = -\beta_\pi$ assumed



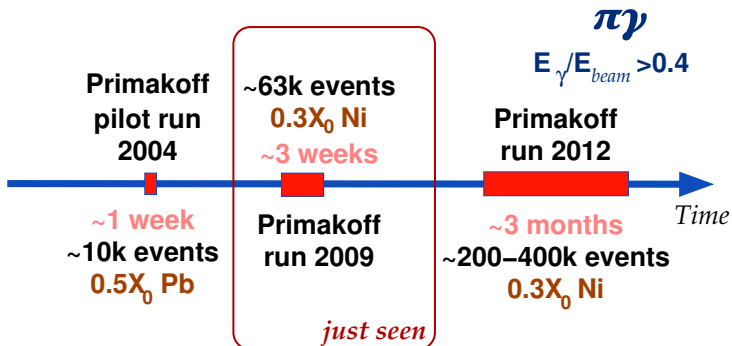
Pion polarisability: world data including COMPASS



- The new COMPASS result is in significant tension with the earlier measurements of the pion polarisability
- The expectation from ChPT is confirmed within the uncertainties



Pion polarisability measurements at COMPASS





Access to $\pi + \gamma$ reactions via the **Primakoff effect**:

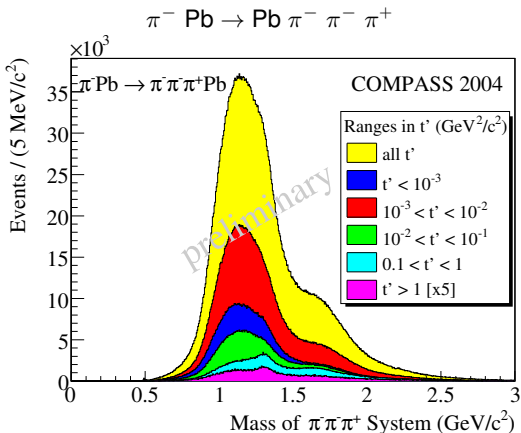
At smallest momentum transfers to the nucleus, high-energetic particles scatter predominantly off the **electromagnetic field** quanta ($\sim Z^2$)

$$\pi^- + \gamma \rightarrow \left\{ \begin{array}{l} \pi^- + \gamma \\ \pi^- + \pi^0 / \eta \\ \pi^- + \pi^0 + \pi^0 \\ \pi^- + \pi^- + \pi^+ \quad \leftarrow \leftarrow \\ \pi^- + \pi^- + \pi^+ + \pi^- + \pi^+ \\ \pi^- + \dots \end{array} \right.$$

analogously: Kaon-induced reactions $K^- + \gamma \rightarrow \dots$



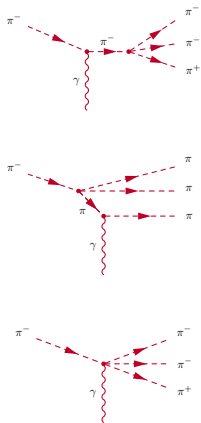
2004 Primakoff results



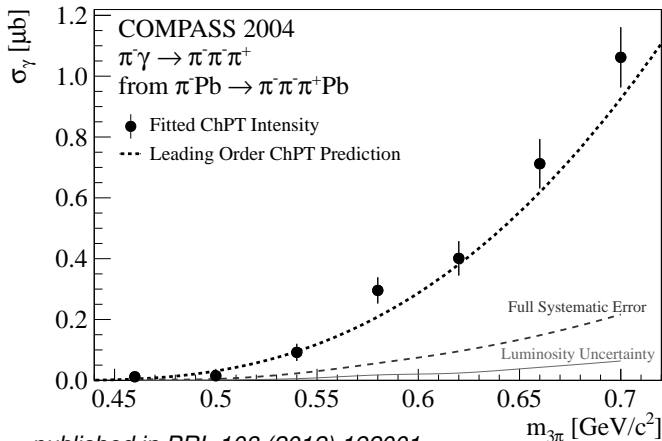
- "Low t' ": $10^{-3} \text{ (GeV/c)}^2 < t' < 10^{-2} \text{ (GeV/c)}^2 \sim 2\,000\,000$ events
- "Primakoff region": $t' < 10^{-3} \text{ (GeV/c)}^2 \sim 1\,000\,000$ events



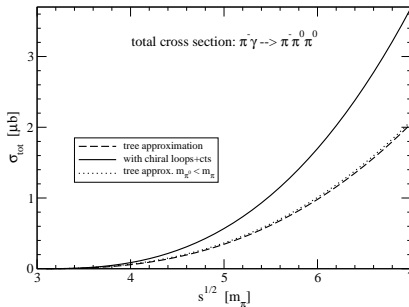
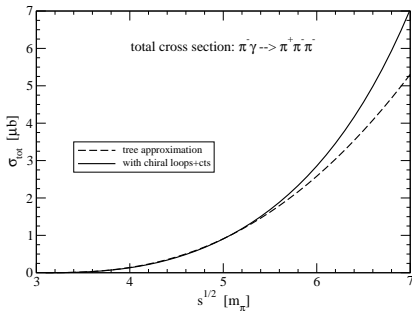
First Measurement of $\pi\gamma \rightarrow 3\pi$ Absolute Cross-Section



Measured absolute cross-section of $\pi^- \gamma \rightarrow \pi^- \pi^- \pi^+$

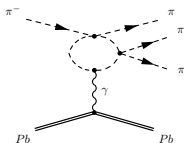
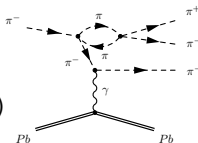


published in *PRL* 108 (2012) 192001

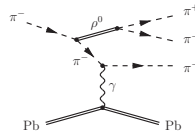


Chiral loops, e.g.

(N. Kaiser,
NPA848 (2010) 198)

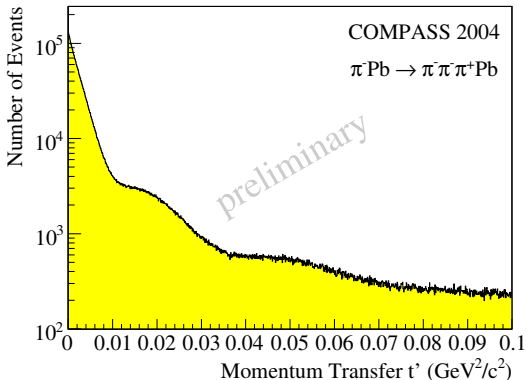


not (yet)
included:





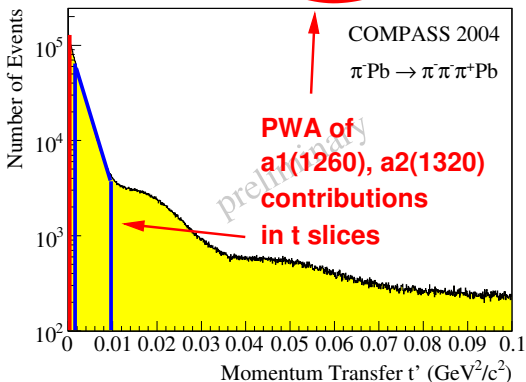
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- "Primakoff region": $t' < 10^{-3} \text{ (GeV/c)}^2 \quad \sim 1\,000\,000 \text{ events}$



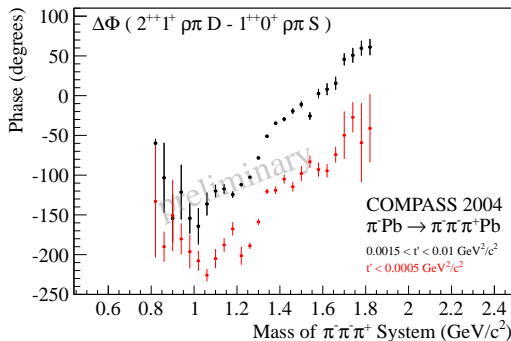
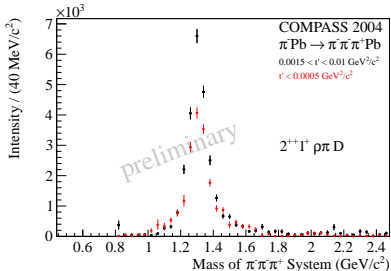
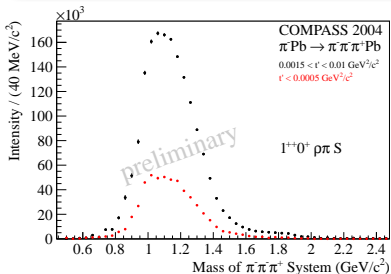
2004 Primakoff results

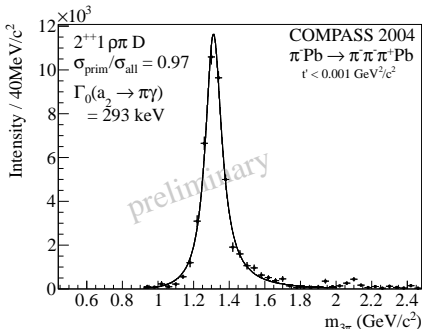


- "Low t' ": $10^{-3} (\text{GeV}/c)^2 < t' < 10^{-2} (\text{GeV}/c)^2$ $\sim 2\,000\,000$ events
- "Primakoff region": $t' < 10^{-3} (\text{GeV}/c)^2$ $\sim 1\,000\,000$ events

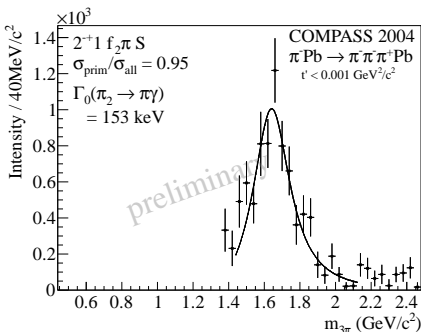


PWA: a_1 , a_2 and $\Delta\Phi$ in separated t' regions



Radiative Coupling of $a_2(1320)$ and $\pi_2(1670)$ 

$\Gamma_0(a_2(1320) \rightarrow \pi\gamma)$ **M2**



$\Gamma_0(\pi_2(1670) \rightarrow \pi\gamma)$ **E2**

\Leftrightarrow meson w.f.'s: $\Gamma_{i \rightarrow f} \propto |\langle \Psi_f | e^{-i\vec{q} \cdot \vec{r}} \hat{\epsilon} \cdot \vec{p} | \Psi_i \rangle|^2$, VMD

- normalization via beam kaon decays
- large Coulomb correction

published in EPJ A50 (2014) 79

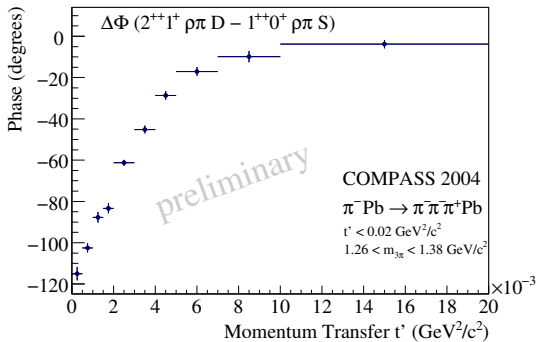
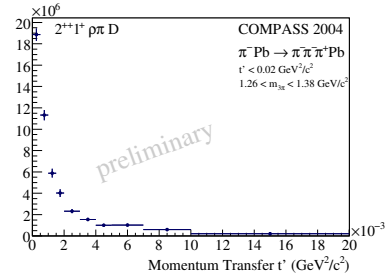
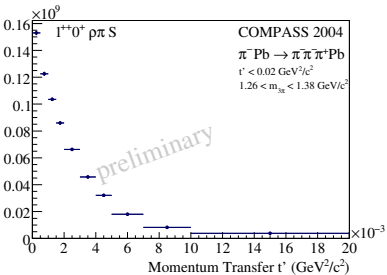


- Measurement of the **pion polarisability** at COMPASS
 - Via the Primakoff reaction, COMPASS has determined

$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3 \quad \text{assuming } \alpha_\pi + \beta_\pi = 0$$

- Most precise experimental determination
 - Systematic control: $\mu\gamma \rightarrow \mu\gamma$, $K^- \rightarrow \pi^- \pi^0$
- **Chiral dynamics** in $\pi^- \gamma \rightarrow \pi^- \pi^0$ and $\pi\gamma \rightarrow \pi\pi\pi$ reactions
 - Charged-channel $\pi\gamma \rightarrow \pi^- \pi^- \pi^+$ tree-level ChPT prediction confirmed
 - Neutral-channel $\pi\gamma \rightarrow \pi^- \pi^0 \pi^0$ analysis ongoing
 - Resonance properties, radiative couplings
- High-statistics run 2012
 - separate determination of α_π and β_π
 - s -dependent quadrupole polarisabilities
 - First measurement of the kaon polarisability

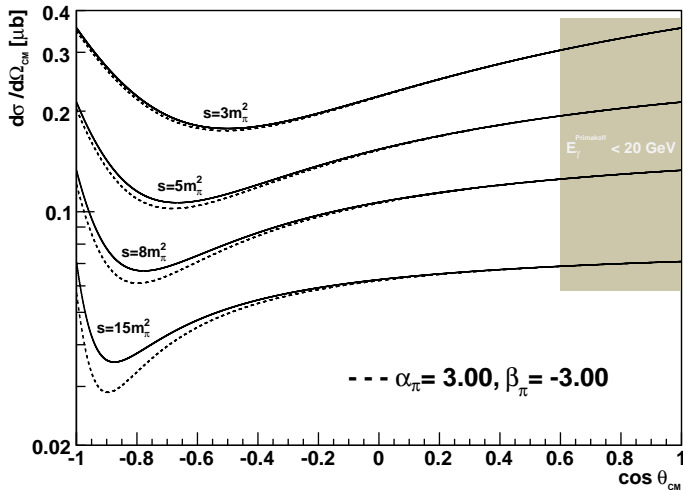




- transition of $\pi\gamma$ to $\pi IP \rightarrow a_2$ production
- work in progress
- interference can be used to map details of resonances and production mechanisms

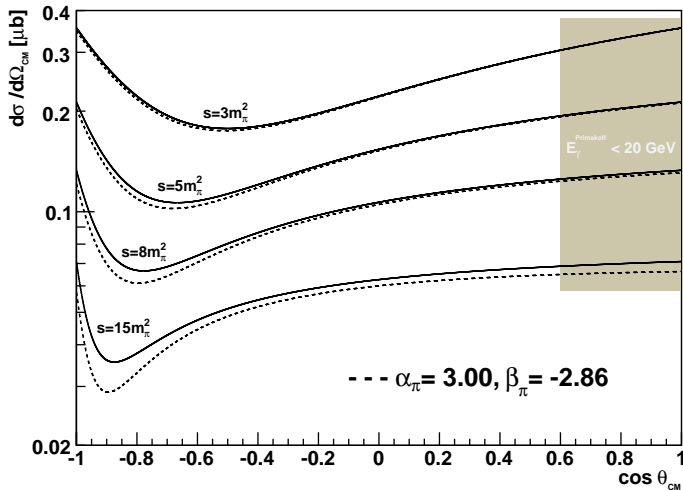


loop effects not shown



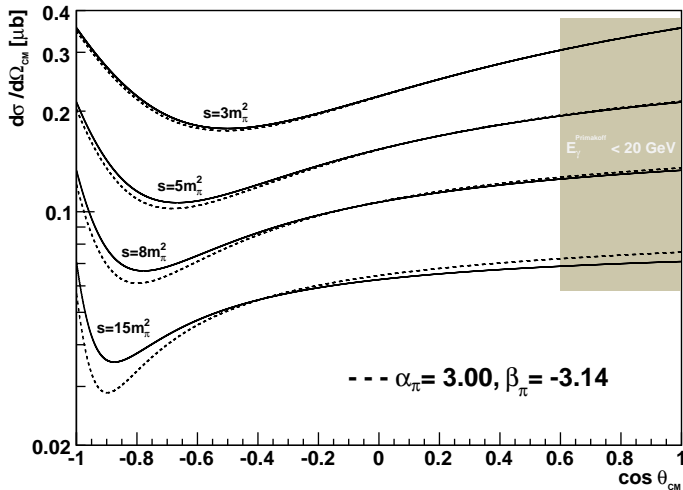


loop effects not shown



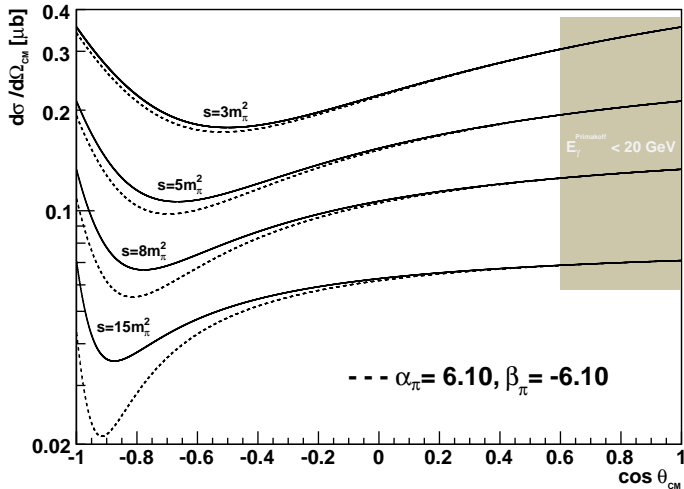


loop effects not shown





loop effects not shown





- Radiative π^+ production on the proton:

$$\gamma \pi^* \longrightarrow \pi \gamma \quad [\text{via } \gamma p \rightarrow n \pi^+ \gamma]$$

Mainz (2005) measurement: $\alpha_\pi - \beta_\pi = 11.6 \pm 1.5 \pm 3.0 \pm 0.5$

“ ± 0.5 ”: model error *only within the used ansatz*,

full systematics not under control

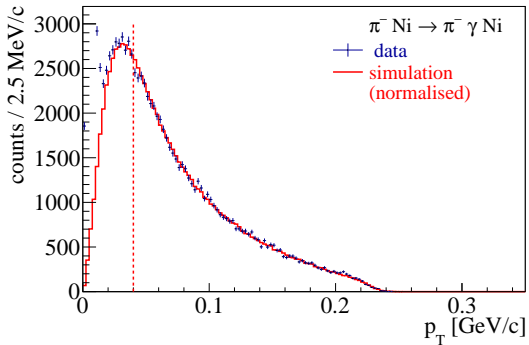
- Primakoff Compton reaction:

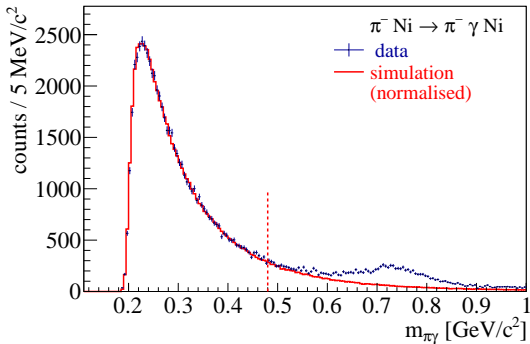
$$\gamma^* \pi \longrightarrow \pi \gamma \quad [\text{via } \pi Z \rightarrow Z \pi \gamma]$$

tiny extrapolation $\gamma^* \rightarrow \gamma$ $\mathcal{O}(10^{-3} m_\pi^2)$

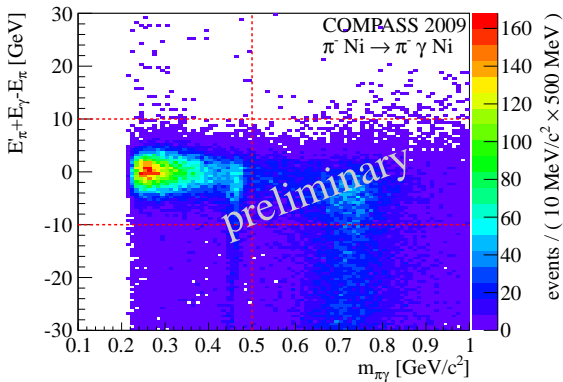
fully under theoretical control

[N. Kaiser, J.F., Nucl. Phys. A 812 (2008) 186]





- ρ contribution from $\pi\gamma \rightarrow \pi\pi^0$

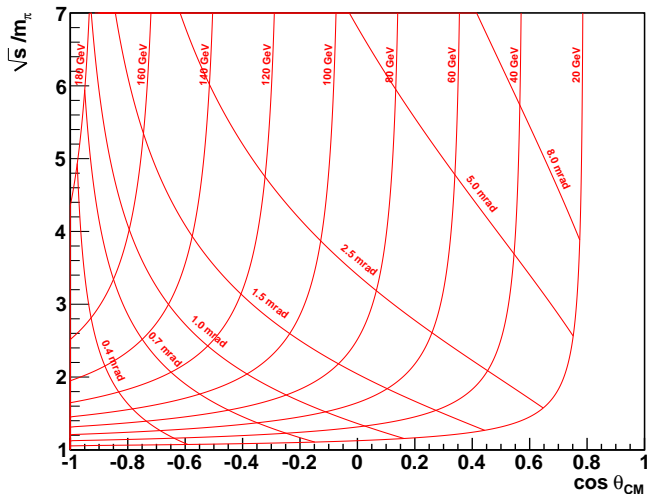


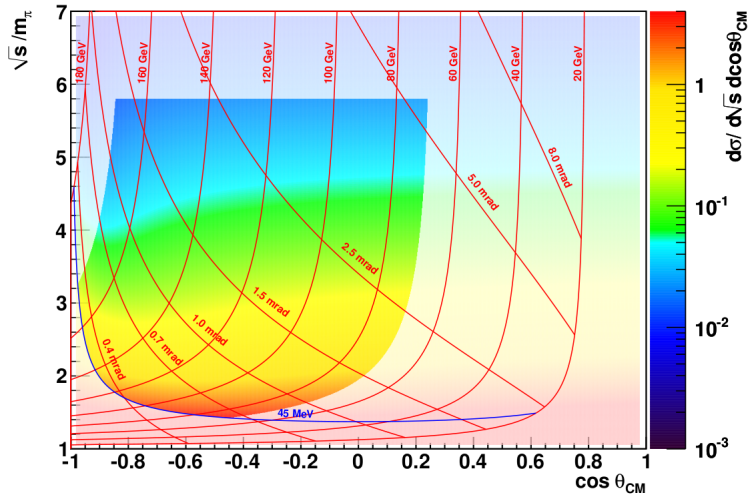
- ρ contribution from $\pi\gamma \rightarrow \pi\pi^0$



Mandelstam $\{s, t\} \leftrightarrow$ Laboratory $\{E_\gamma, \theta_\gamma\}$

for $\pi\gamma \rightarrow \pi\gamma$

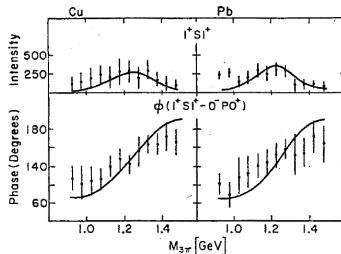
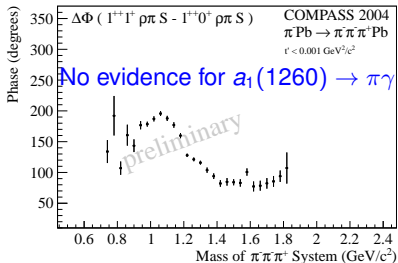
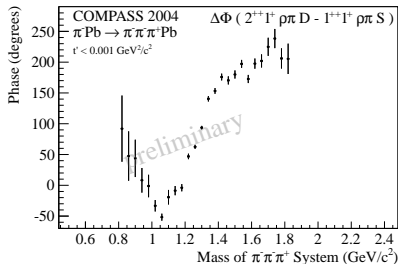
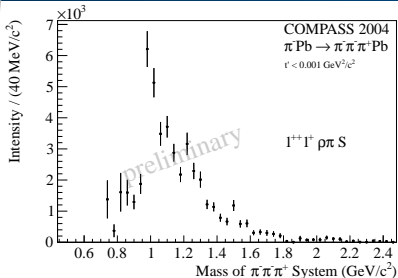






M.R. Pennington in the 2nd DAΦNE Physics Handbook,
“What we learn by measuring $\gamma\gamma \rightarrow \pi\pi$ at DAΦNE”:

All this means that the only way to measure the pion polarisabilities is in the Compton scattering process near threshold and not in $\gamma\gamma \rightarrow \pi\pi$. Though the low energy $\gamma\gamma \rightarrow \pi\pi$ scattering is seemingly close to the Compton threshold (...) and so the *extrapolation* not very far, the dominance of the pion pole (...) means that the energy scale for this continuation is m_π . Thus the polarisabilities cannot be determined accurately from $\gamma\gamma$ experiments in a model-independent way and must be measured in the Compton scattering region.



M. Zielinski et al, Phys. Rev. Lett 52 (1984) 1195



- **Mass-independent PWA** (narrow mass bins):

$$\sigma_{\text{indep}}(\tau, m, t') = \sum_{\epsilon=\pm 1} \sum_{r=1}^{N_r} \left| \sum_i T_{ir}^\epsilon f_i^\epsilon(t') \psi_i^\epsilon(\tau, m) / \sqrt{\int |f_i^\epsilon(t')|^2 dt'} \sqrt{\int |\psi_i^\epsilon(\tau', m)|^2 d\tau'} \right|^2$$

- Production strength assumed constant in single bins
 - Decay amplitudes $\psi_i^\epsilon(\tau, m)$, with t' dependence $f_i^\epsilon(t')$
 - Production amplitudes $T_{ir}^\epsilon \rightarrow$ Extended log-likelihood fit
 - Acceptance corrections included
- **Spin-density matrix:** $\rho_{ij}^\epsilon = \sum_r T_{ir}^\epsilon T_{jr}^{\epsilon*}$

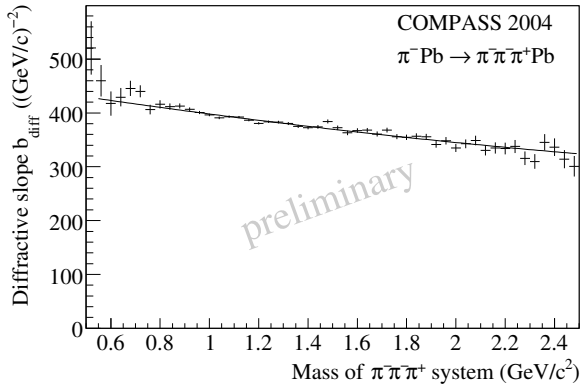
\rightarrow Physical parameters:

$$\text{Intens}_i^\epsilon = \rho_{ii}^\epsilon,$$

relative phase Φ_{ij}^e

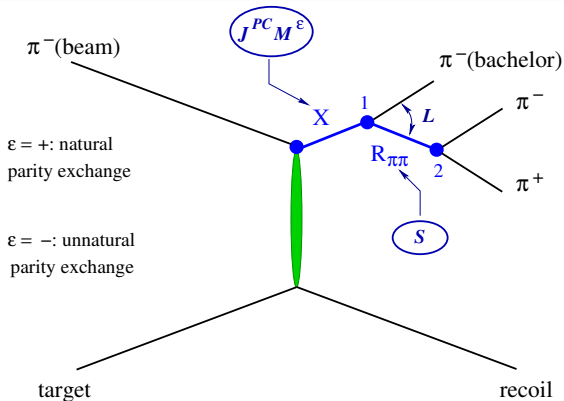
$$\text{Coh}_{i,j}^\epsilon = \sqrt{(\text{Re } \rho_{ij}^\epsilon)^2 + (\text{Im } \rho_{ij}^\epsilon)^2} / \sqrt{\rho_{ii}^\epsilon \rho_{jj}^\epsilon}$$

- **Mass-dependent χ^2 -fit** (not presented here):
 - X parameterized by Breit-Wigner (BW) functions
 - Background can be added





Isobar Model

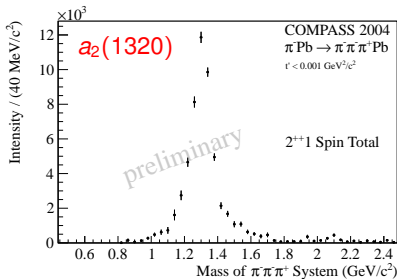
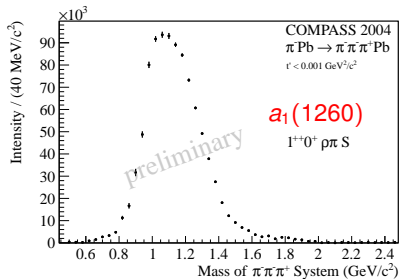
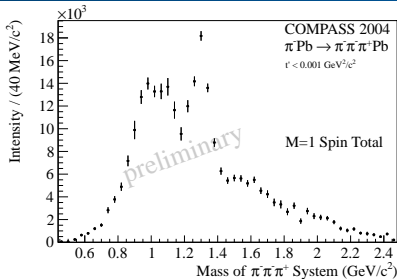
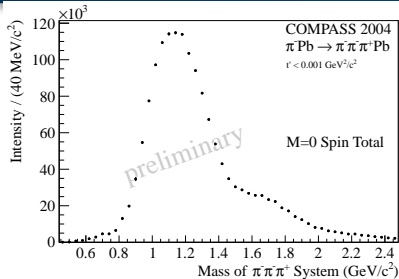


- Isobar model: Intermediate 2-particle decays
- Partial wave in reflectivity basis: $J^{PC} M^\epsilon [isobar] L$

- **Mass-independent** PWA ($40 \text{ MeV}/c^2$ mass bins): **38 waves**
Fit of angular dependence of partial waves, interferences
- **Mass-dependent** χ^2 -fit (Not presented here)



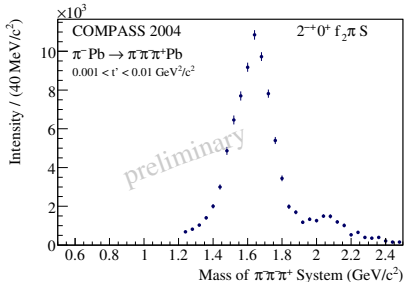
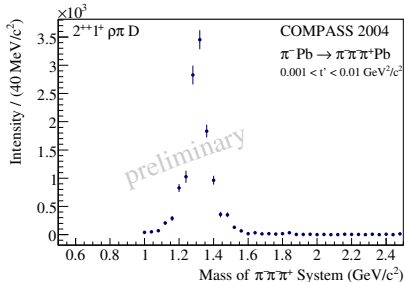
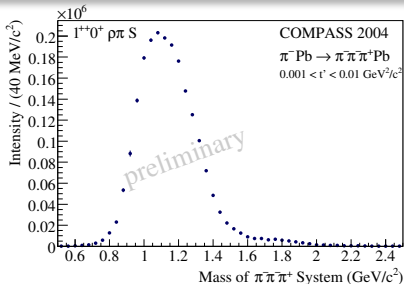
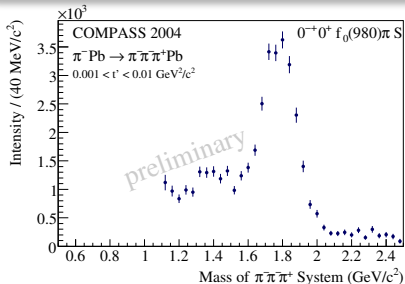
Major intensities in $m(3\pi)$ -bins (acceptance corrected)





PWA of data with low t'

Intensity of selected waves: $0^{-+}0^{+}f_0(980)\pi S$, $1^{++}0^{+}\rho\pi S$, $2^{++}1^{+}\rho\pi D$, $2^{-+}0^{+}f_2(1270)\pi S$





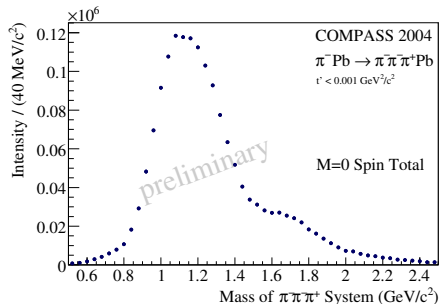
“Spin Totals”: Sum of all contributions for given M (i.e. z-projection of J)

t' -dependent amplitudes:

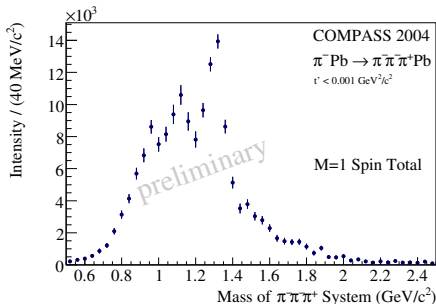
Primakoff production: $M=1: \sigma(t') \propto e^{-b_{\text{Prim}}t'} \rightarrow$ arises at $t' \approx 0$ (resolved shape!)

Diffractive production: $M=0: \sigma(t') \propto e^{-b_{\text{diff}}(m)t'}$

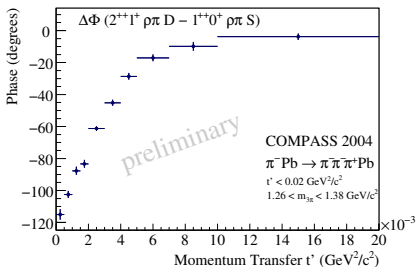
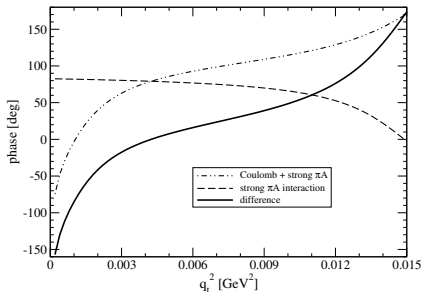
$M=1: \sigma(t') \propto t' e^{-b_{\text{diff}}(m)t'} \rightarrow$ vanishes for $t' \approx 0$



M=0



M=1



Glauber modell

G. Fäldt and U. Tengblad, Phys. Rev. C79, 014607 (2009)

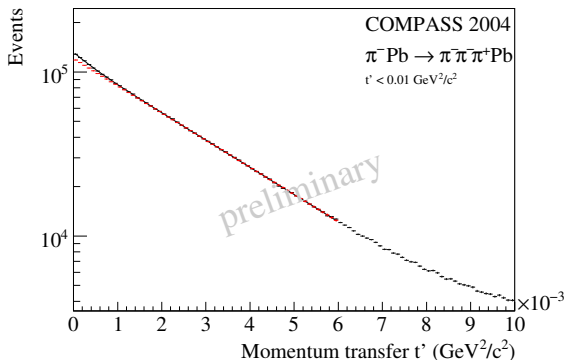
Plot: N. Kaiser (TU München)

- ⇒ indicates confirmation of interference Coulomb-interaction - strong interaction
- ⇒ detailed studies of the nature of resonances



Primakoff: $\sigma(t') \propto e^{-b_{\text{Prim}} t'}$, $b_{\text{Prim}} \approx 2000 \text{ (GeV}/c)^{-2}$ (mainly resolution)

Diffractive: $\sigma(t') \propto e^{-b_{\text{diff}} t'}$, $b_{\text{diff}} \approx 400 \text{ (GeV}/c)^{-2}$ for lead target



(Mass) spectrum of this Primakoff contribution?

⇒ Statistical subtraction of diffractive background (for bins of $m_{3\pi}$)