

proton structure, spin, charge and QED expansion

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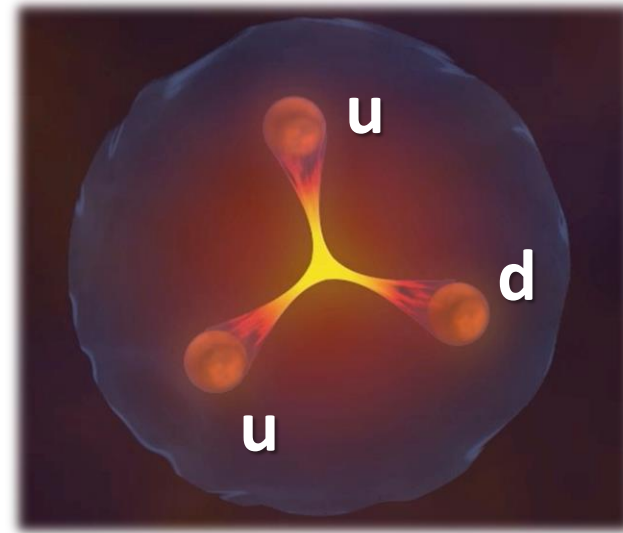
The proton: is it so well understood?

main constituent

- of our bodies
- of fuel of stellar furnaces
- of matter in the visible universe

$p + e^- : H_{\text{atom}} \rightarrow$ QED revolution 1920

$p+p \rightarrow$ Higgs boson discovery 2012



The nucleon is the best laboratory to study QCD

- PART I: Charge , Form Factors and proton charge radius
- PART II: Spin, quark and gluon distributions and 3D imaging of the nucleon

Only a selection of a few results

The electromagnetic probe

Lepton : electron or muon
of energy E_{beam}

QED: $\alpha=1/137$

one photon exchange dominates

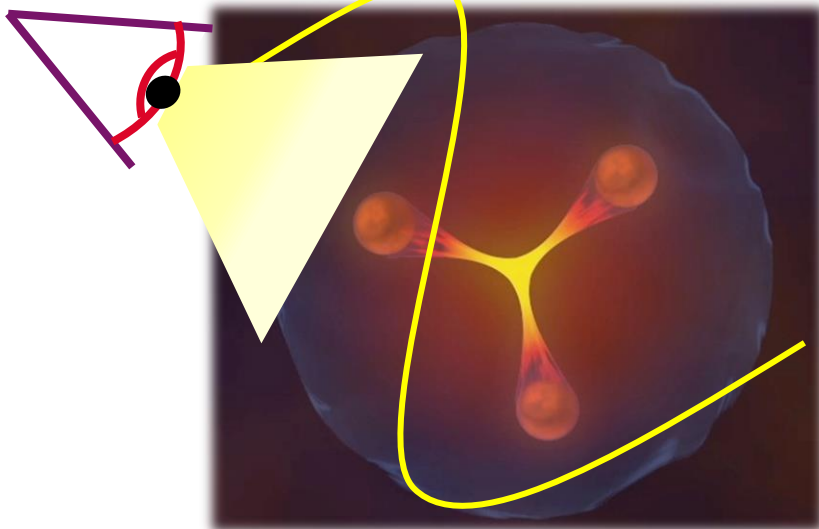
momentum \vec{q} and energy ν

$$Q^2 = \nu^2 - q^2 \text{ and } x_B^{\text{lab}} = Q^2/2m\nu$$

proton

$Q^2 \rightarrow 0$

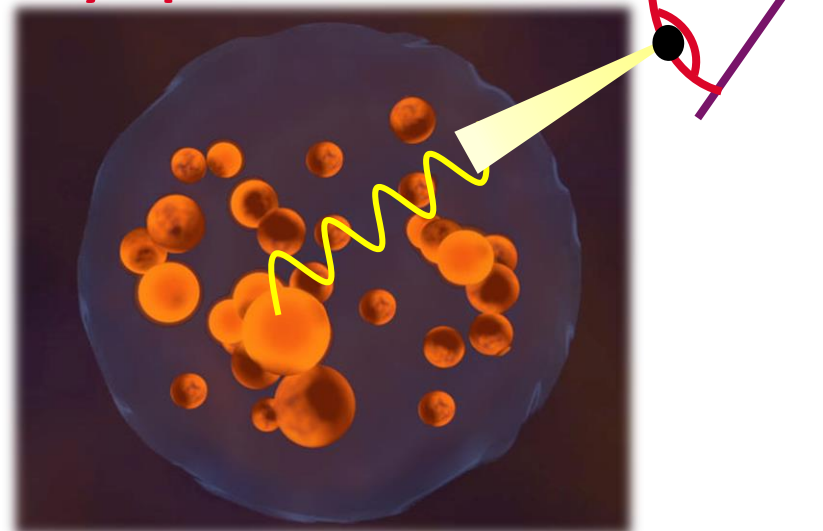
Confinement



Effective models based on chirality, pion cloud...
Lattice QCD calculations

$Q^2 \rightarrow \infty$

Asymptotic Freedom



Perturbative QCD

PART 1: Charge, Form Factors and proton radius

The elastic scattering: $ep \rightarrow ep$

$$\frac{d\sigma_{ep \rightarrow ep}}{d\Omega} = \frac{d\sigma_{Mott}}{d\Omega} \times \left[G_E^2(Q^2) + \frac{\tau}{\varepsilon} G_M^2(Q^2) \right]$$

$$\tau = \frac{Q^2}{4M^2}$$

$$\varepsilon = \left[1 + 2(1 + \tau) \tan^2 \frac{\theta_e}{2} \right]^{-1}$$

Point-like particle
Spin 1/2

Form factors (FFs)

Internal structure

Charge distribution

$$G_E^p(0) = 1 \quad G_E^n(0) = 0$$

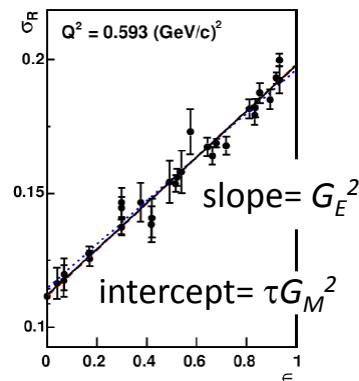
Distribution of magnetic moment

$$G_M^p = 2.793 \quad G_M^n = -1.91$$

The different techniques to extract FFs

1- Rosenbluth separation

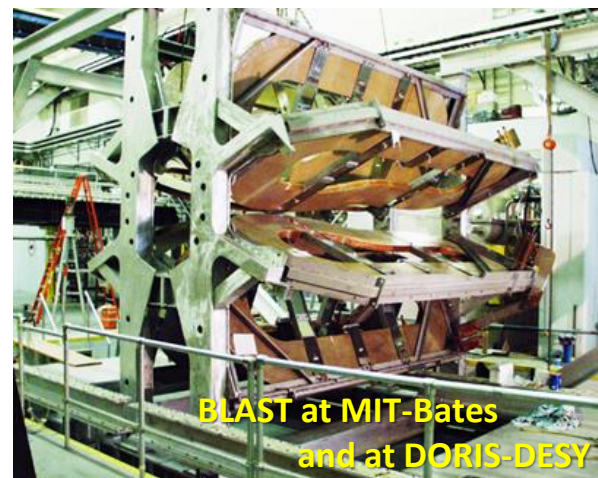
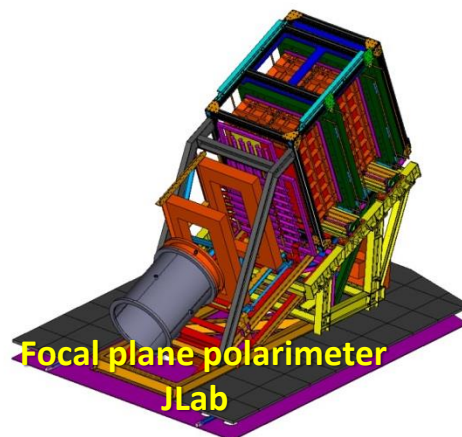
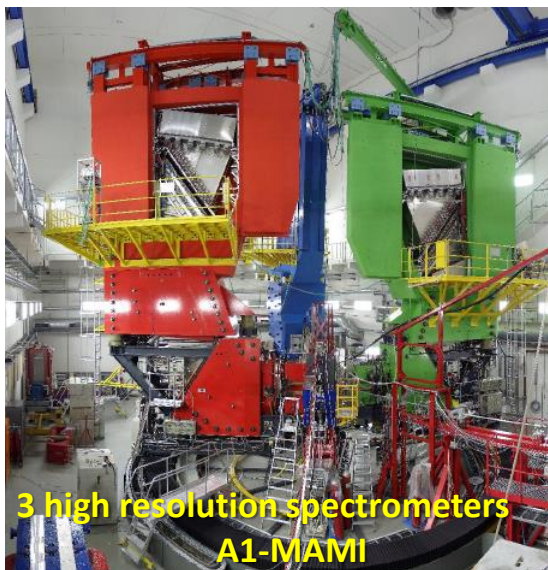
$$\sigma_R = (d\sigma/d\Omega)/(d\sigma/d\Omega)_{\text{Mott}} = \tau G_M^2 + \varepsilon G_E^2$$



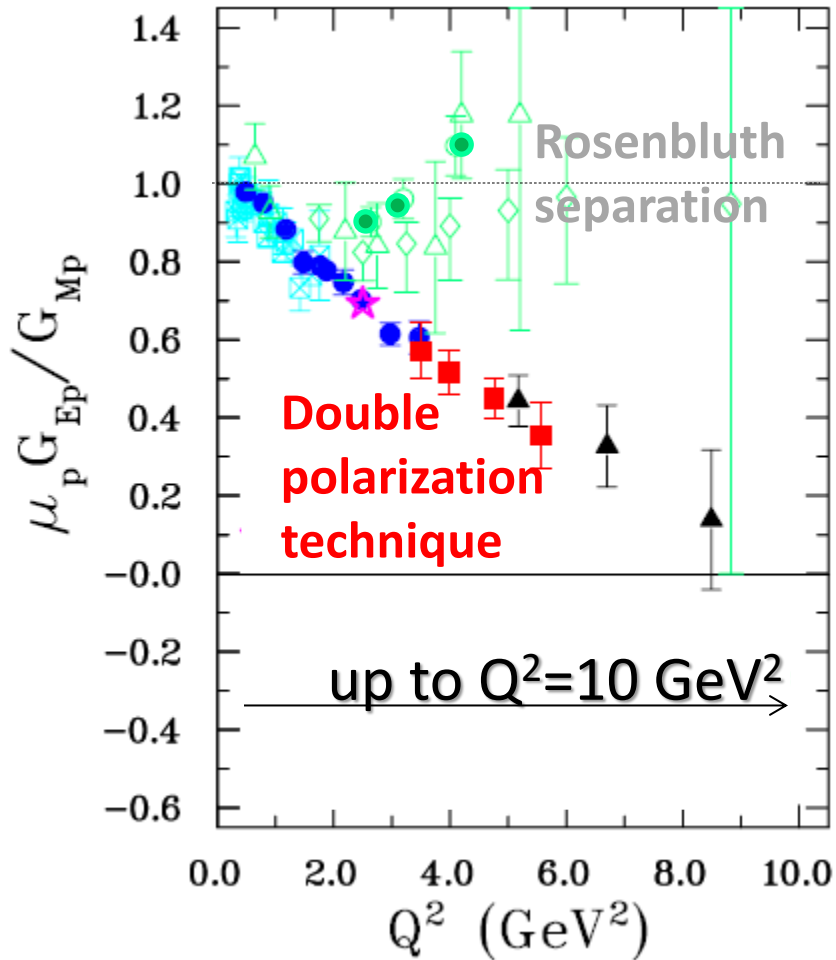
2- Double Polarization technique

Polarized beam and recoil proton polarization
or Polarized beam and polarized target

→ Direct measurement of the ratio G_E/G_M



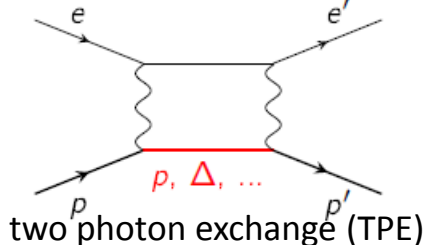
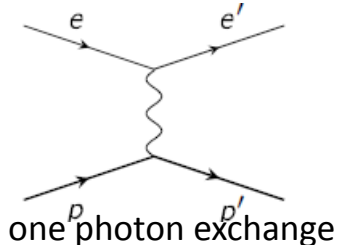
$\mu G_E / G_M$ by the 2 methods



- ◇ Andivahis PRD50 (1994) SLAC
- △ Christy PRC70 (2004) JLab
- ◎ Qattan PRL94 (2005) JLab
- Jones PRL84 (2000) JLab
- Punjabi PRC71 (2005) JLab
- ☆ Meziane PRL106 (2011) JLab
- Gayou PRL88 (2003) JLab
- Puckett PRC85 (2012) JLab
- ▲ Puckett PRL104 (2010) JLab
- ⊠ Other publications Mainz, Bates, JLab

Discrepancy between the 2 methods

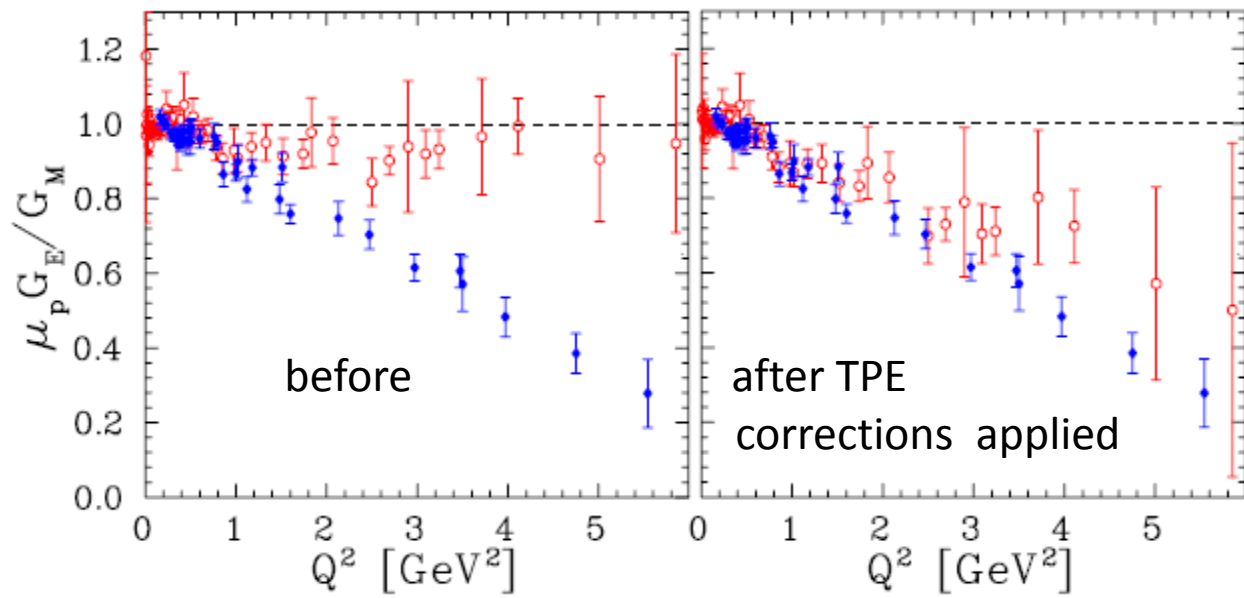
Two Photon exchange to solve the problem?



RADIATIVE CORRECTIONS:

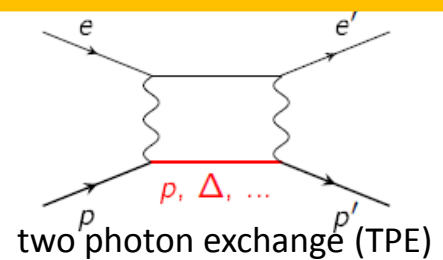
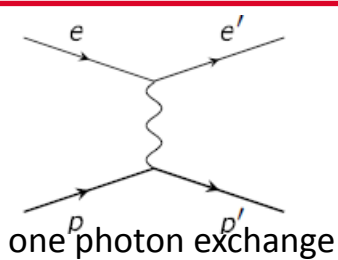
the hadron structure dependent part of the **two photon exchange (TPE)** was neglected

- ✓ large radiative corrections for σ
- ✓ negligible effect for G_E/G_M (similar effect for the numerator and denominator of the ratio)



Guichon, Vanderhaeghen, PRL91 (2003)
Blunden et al., PRC72 (2005)
Afanassev et al., PRC72 (2005)
Arrington et al., PPNP66 (2011)

Stringent comparison: e^+ and e^- scattering



$$\sigma(e^-p) = |M_{1\gamma}|^2 \alpha^2 - 2 |M_{1\gamma}| |M_{2\gamma}| \alpha^3 + \dots$$

$$\sigma(e^+p) = |M_{1\gamma}|^2 \alpha^2 + 2 |M_{1\gamma}| |M_{2\gamma}| \alpha^3 + \dots$$

$$R = \frac{\sigma(e^+p)}{\sigma(e^-p)} = 1 + \frac{4 \Re(M_{1\gamma}^\dagger M_{2\gamma})}{|M_{1\gamma}|^2}$$

3 experiments on going

✓ **Olympus: BLAST @ DORIS @ DESY**

DORIS e-/e+ storage ring

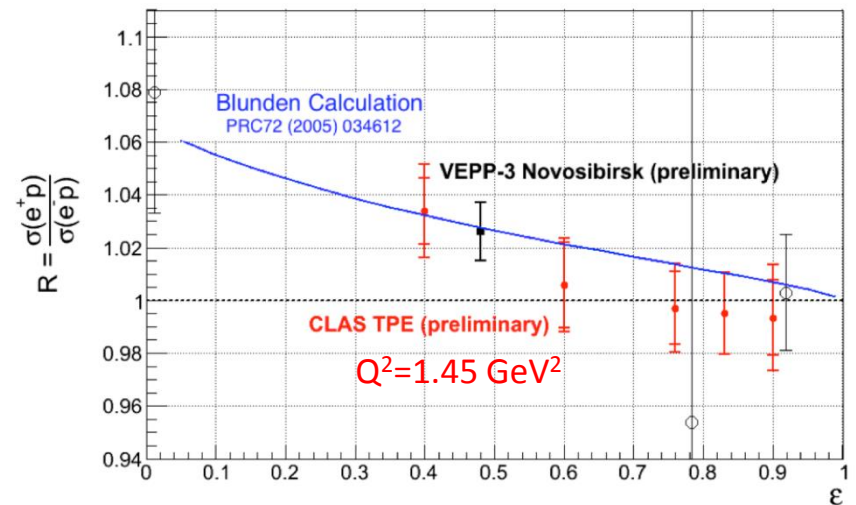
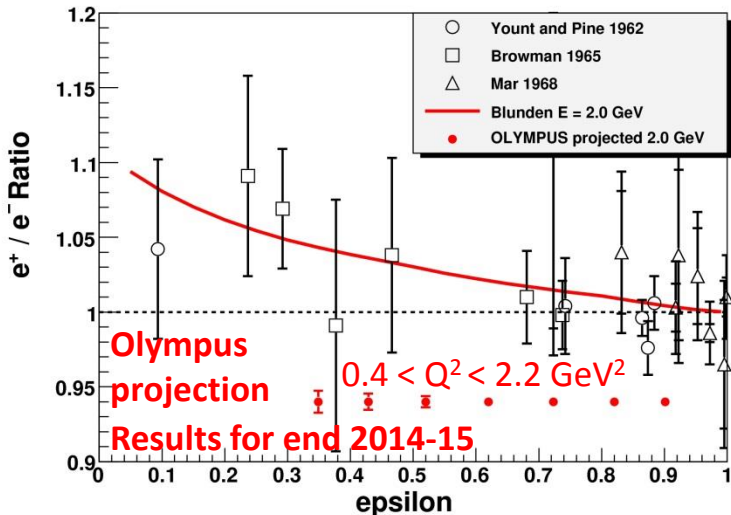
BLAST detector + internal target

✓ **VEPP-3 @ Novosibirsk**

e-/e+ storage ring, internal target

✓ **CLAS-PR04-116 @ Jlab**

e-/e+ pair production from photon beam



Shape of the nucleon

NON RELATIVISTIC INTERPRETATION

classical picture in the Breit frame ($q=Q$)
 the Form Factors are the Fourier Transform
 of the charge and magnetization distributions

$$\begin{aligned}
 F(\vec{q}) &= \int \rho(\vec{r}) e^{i\vec{q}\vec{r}} d^3\vec{r} \\
 &= \frac{4\pi}{q} \int_0^\infty \rho(r) \sin(qr) r dr \\
 &= 1 - \frac{\vec{q}^2}{6} \langle r^2 \rangle + \frac{\vec{q}^4}{120} \langle r^4 \rangle + \dots
 \end{aligned}$$

Taylor expans.

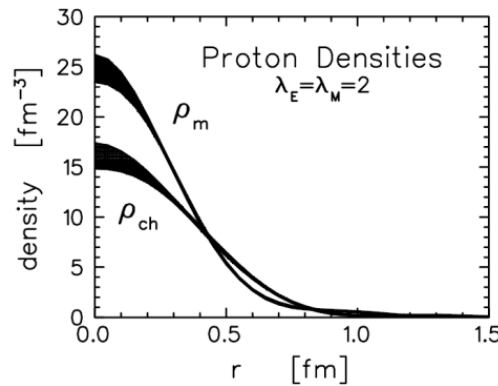
$$r_p^2 \equiv -6 \frac{dG_E}{dQ^2} \Big|_{Q^2=0}$$

This is a definition

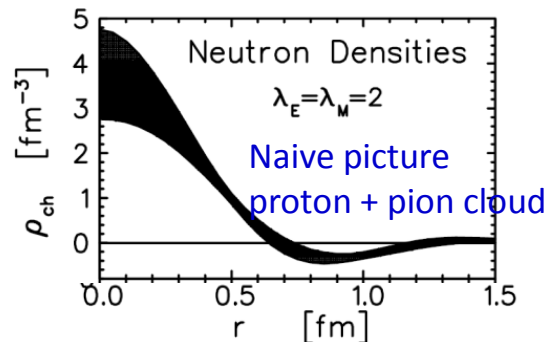
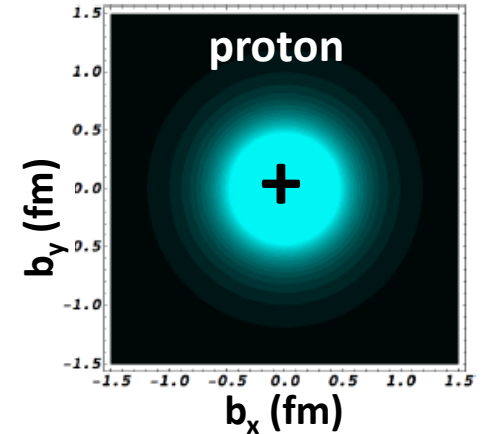
RELATIVISTIC INTERPRETATION

light front picture in the Infinite Momentum Frame

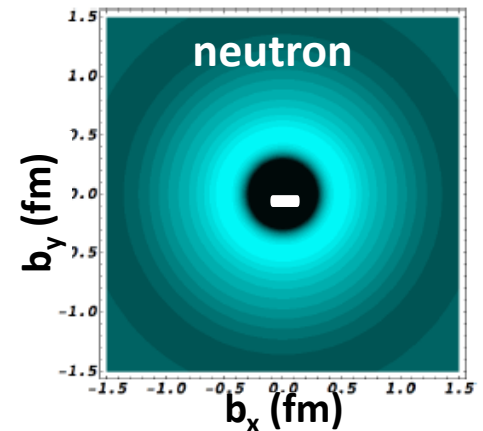
2D or **transverse** (\perp to boost) **spatial distrib**



\approx



\neq



Proton radius from ep scattering at low Q^2

MAMI – A1

High precision and redundancy

3 high resolution spectrometers

1400 measured cross sections (stat < 0.1%)

$$0.003 < Q^2 < 1 \text{ GeV}^2$$

Super-Rosenbluth technique

Fit of form factor models directly

Wide range of parametrizations

$$r_p = 0.879 \pm 0.008 \text{ fm}$$

Bernauer et al. , PRL105 (2010)
& PRC90 (2014) Including TPE and all world data

JLAB - HallA

using recoil polarimetry to get G_E/G_M

Exp E05-103: Ron et al. PRL99 (2007)

update PRC84 (2011)

Exp E08-107: Zhan et al. PLB 705 (2011)

$$Q^2 > 0.2 \text{ GeV}^2$$

In the near future

results from the 2nd part of E08-107

polarized beam - polarized NH3 target asymm.

$$0.01 < Q^2 < 0.16 \text{ GeV}^2$$

$$r_p = 0.875 \pm 0.010 \text{ fm}$$

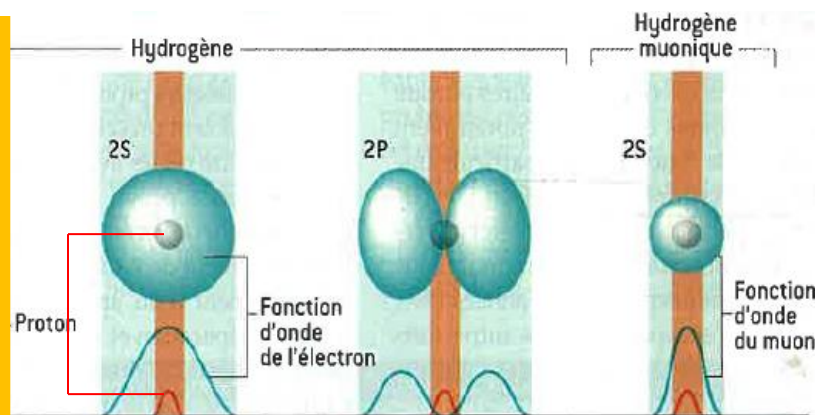
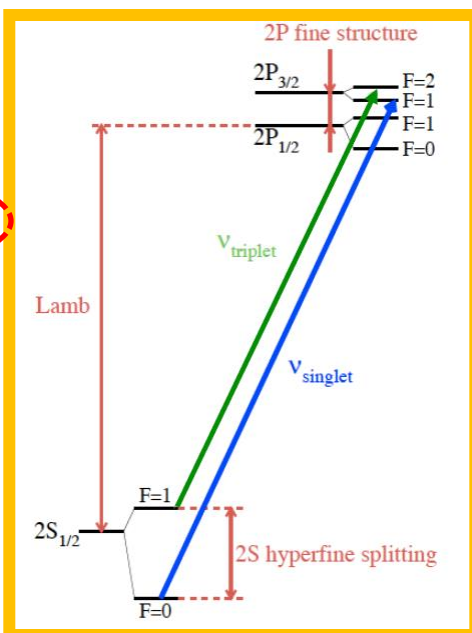
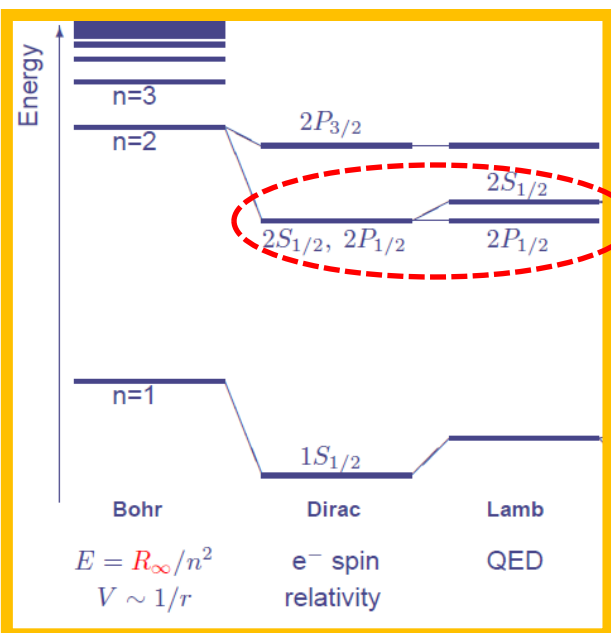
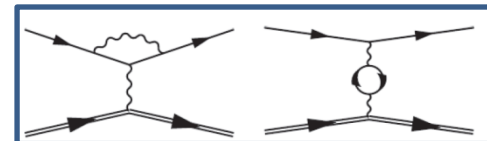
Zhan et al. PLB 705 (2011)

Proton radius from muonic hydrogen Lamb shift

Lamb shift (1947): pure radiative QED effects such as ‘self energy’ and ‘vacuum polarization’

The perturbation causes a fluctuation in the position of the electron (or muon).

→ subtle difference between the binding energies of the $2S_{1/2}$ and $2P_{1/2}$



Probability for the lepton to be within the volume of the proton

$$= (r_p/r_{\text{Bohr}})^3 \sim (\alpha m_{\text{lepton}} r_p)^3$$

→ $Proba(\mu) = 8 \times 10^6 Proba(e)$

With the new 5keV muon beam line at PSI:

• Pohl et al., Nature 466 (2010): **2S → 2P Lamb shift** → $r_p = 0.84184 \pm 0.00067 \text{ fm}$

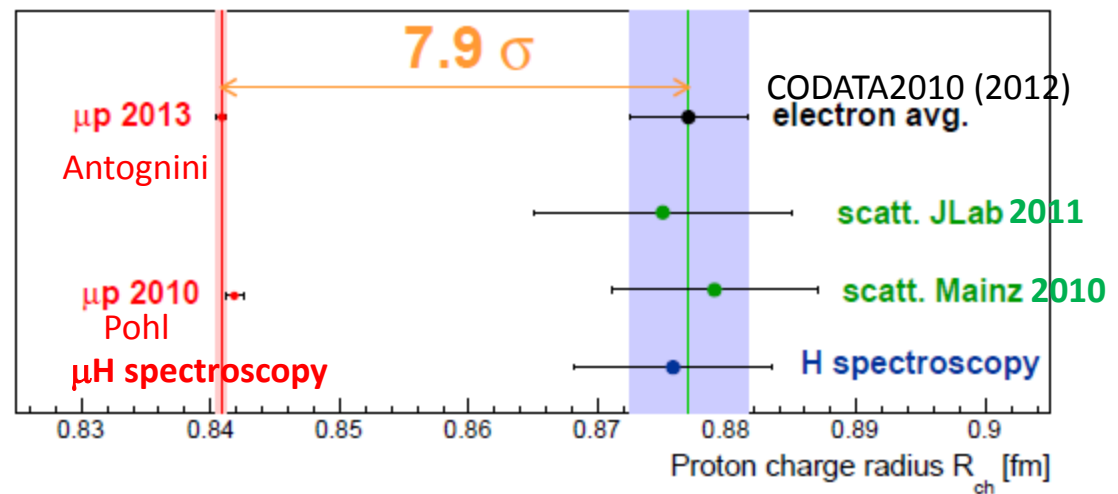
• Antognini et al., Science 339 (2013): **2S → 2P Lamb shift**

$$\Delta E(\text{meV}) = 206.0336(15) - 5.2275(10) r_p^2 + 0.0332(20)_{\text{TPE}} \rightarrow r_p = 0.84087 \pm 0.00039 \text{ fm}$$

Proton radius puzzle



Discrepancy between muonic and electronic measurements



Particle Data Group: “ Until the difference between the **ep** and **μp** values is understood, it does not make much sense to average all the values together. For the present, we stick with the less precise (and provisionally suspect) CODATA 2010 value. It is up to workers in this field to solve this puzzle.”

Possible origins of the disagreement

Pohl, Gilman, Miller, Pachuki, Annu. Rev. Nucl. Part. Sci. 63 (May 2013)

- The ep scattering experiments are not at enough low Q^2
→ 2 new experiments: Jlab ($Q^2=10^{-3}-10^{-4} \text{ GeV}^2$), MAMI (Initial State Radiation)
- QED calculations not enough accurate to compare ep and μp spectroscopy
Proton structure effect:
the TPE term (in m_{lepton}^4) depending on proton polarizability corrections could be not correct

- **Novel Beyond Standard Model Physics:**

Electron and muon really do have different interactions with the proton

Failure in the electron-muon Universality?

The muon anomalous magnetic moment $(g-2)_\mu$ exceeds the SM expectation by 3σ
Search for dark photon – light weakly coupled U(1) gauge boson

→ The MUSE experiment at PSI will use the world's most powerful low-energy separated $e/\pi/\mu$ beam for a direct comparison for $0.002 < Q^2 < 0.07 \text{ GeV}^2$

$e^+p, e^-p, \mu^+p, \mu^-p$

r_p (fm)	ep	μp
Spectroscopy	0.8758 ± 0.077	0.84087 ± 0.00039
Scattering	0.8770 ± 0.060	???

PART 2: The proton spin puzzle

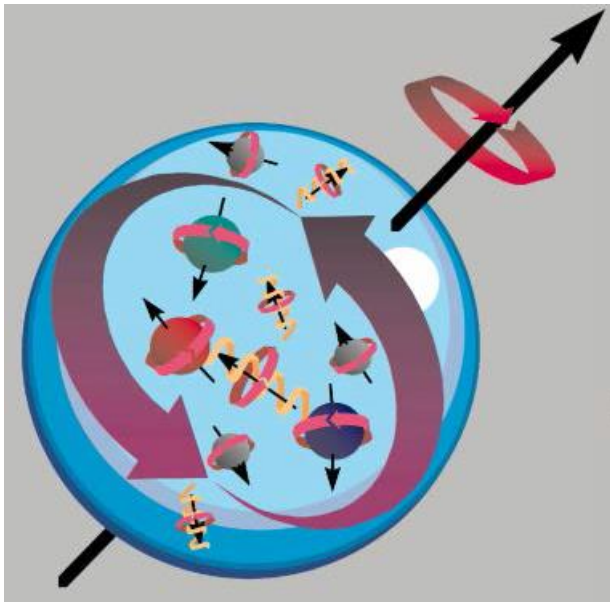
$$\frac{1}{2} = \frac{1}{2} \Delta \Sigma + L_q + \Delta G + L_g$$

Quark
spin

Quark
OAM

Gluon
spin

Gluon
OAM



$$\Delta \Sigma = \Delta u + \Delta d + \Delta s$$

Only **30%** of proton spin comes from spin of quarks and antiquarks. **?**
Where does the rest come from **!**

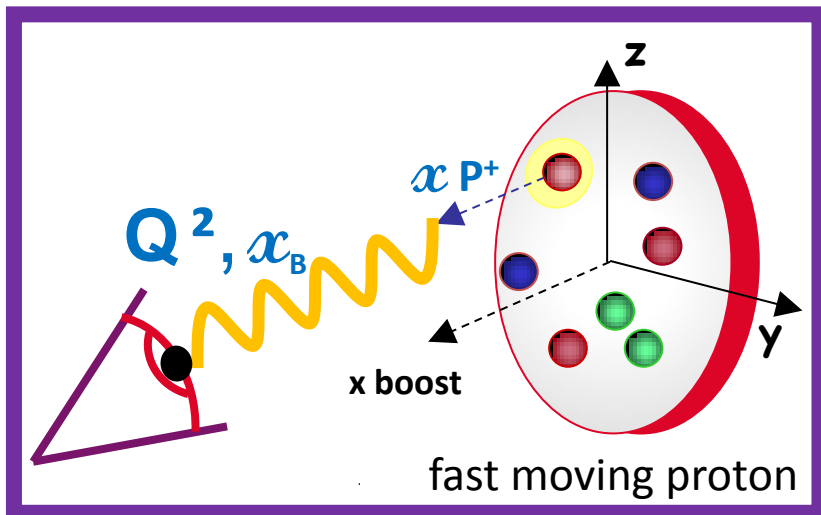
$$\Delta G = \int_0^1 \Delta g(x) dx$$

In $A^+=0$ light-cone gauge

Not unique decomposition (Jaffe / Ji)

and **Orbital Angular Momentum (OAM)**

Proton picture: 1D



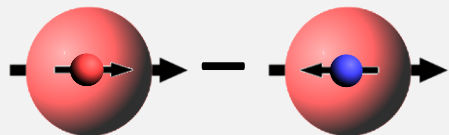
Longitudinal momentum

$$q(x) \text{ or } f_1^q(x)$$



Longitudinal spin

$$\Delta q(x) = \vec{q}(x) - \bar{q}(x)$$

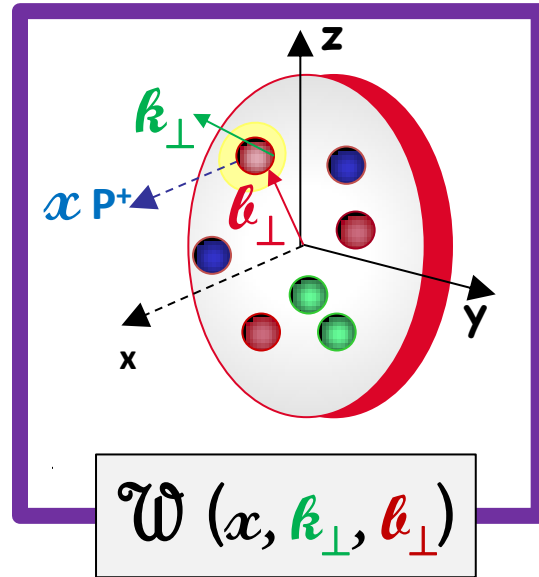
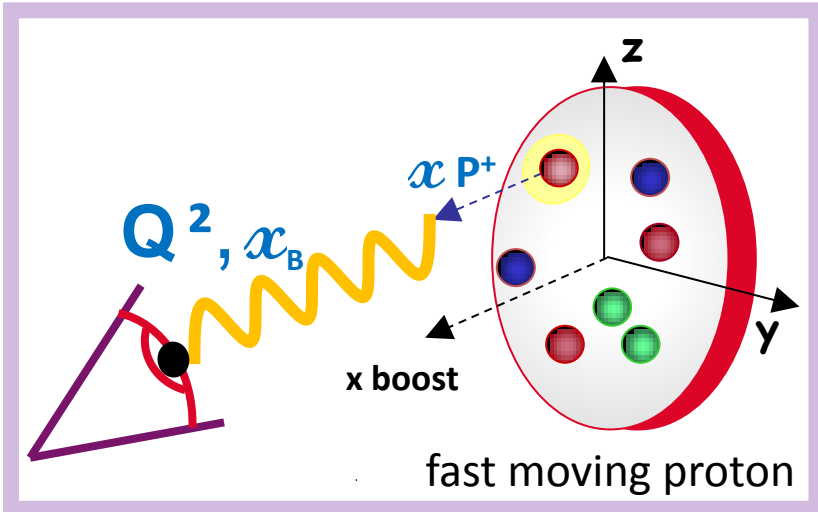


Transverse spin

$$\Delta_T q(x) \text{ or } h_1(x)$$



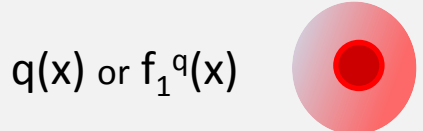
Proton picture: 1D \rightarrow 1+2D



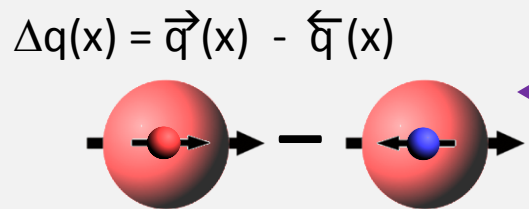
Quantum tomography of the nucleon

Meissner et al, PRD76 (2007)
Lorcé et al, JHEP1105 (2011)

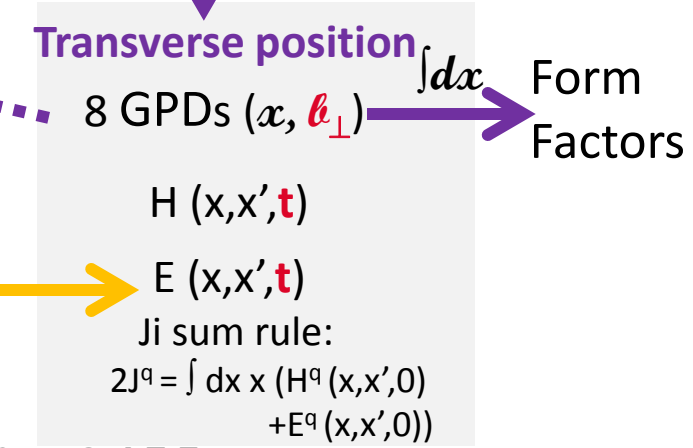
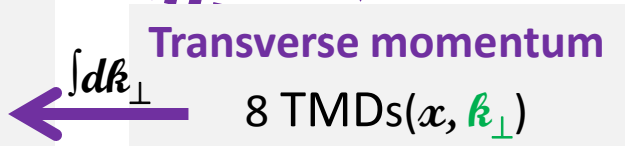
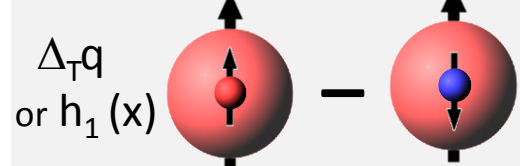
Longitudinal momentum



Longitudinal spin



Transverse spin

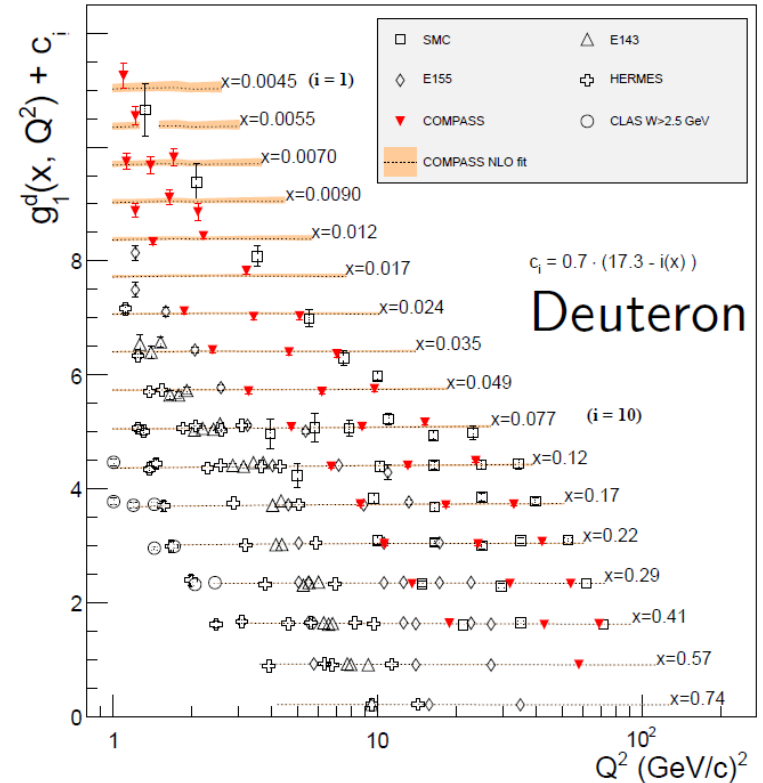
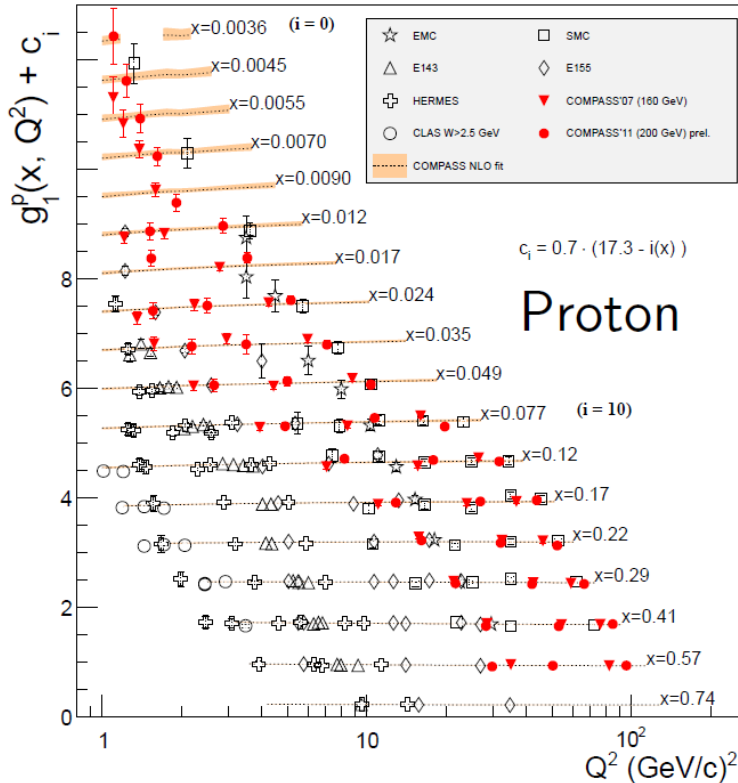
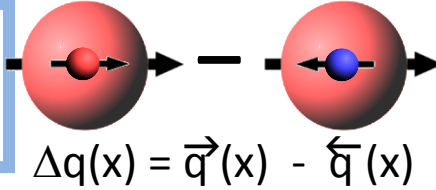


holy grail for OAM

The longitudinal spin structure, $\Delta\Sigma$ and ΔG

DIS: $\vec{\ell} \vec{p} \rightarrow \vec{\ell} X$

$$A_1(x, Q^2) = \frac{\sum_q e_q^2 \Delta q(x, Q^2)}{\sum_q e_q^2 q(x, Q^2)} = \frac{g_1(x, Q^2)}{F_1(x, Q^2)}$$



New **COMPASS-CERN** data with **polarized muon beams of 160 and 200 GeV** (for low x and high Q^2)

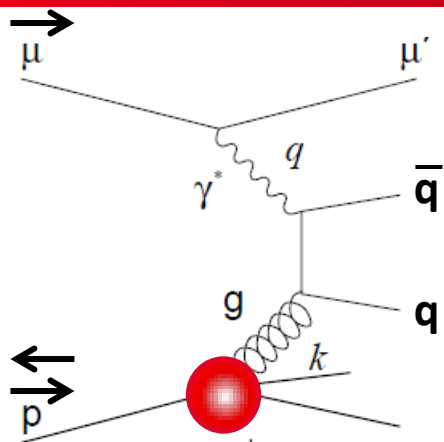
g_1 input to global NLO QCD fits for extraction of Δq and Δg

$$\int g_1 dx \rightarrow \mathbf{0.26 < \Delta\Sigma < 0.34}$$

$$\frac{d}{d \ln Q^2} g_1 \rightarrow \mathbf{\Delta G}$$

but x and Q^2 coverage
not yet sufficient
for precise ΔG

Glueon spin from photon-gluon fusion in SIDIS



Two channels: $A_{LL} = \Delta g/g + bg$

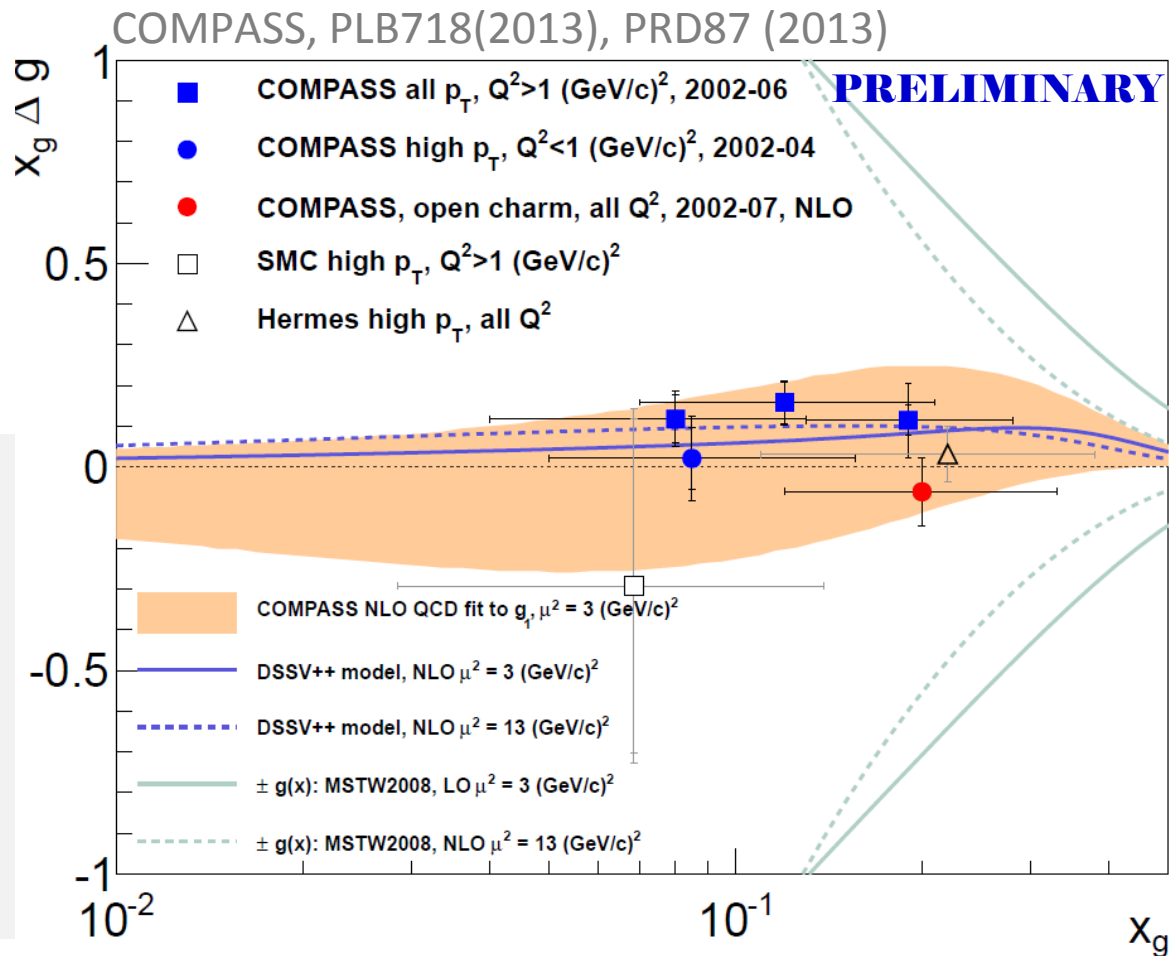
$q=c$ ● open charm (NLO)
scale = $\mu^2 \approx 13 \text{ GeV}^2$

$q=u,d,s$

● high- p_T (LO)

■ all p_T (LO) ← **NEW**

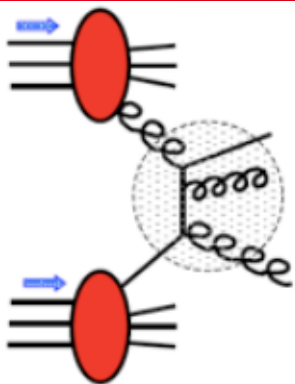
scale = $\mu^2 \approx 3 \text{ GeV}^2$



All direct measurements compatible $\int_{0.05}^{0.3} \Delta g(x) dx$ significantly positive

Note that these data are not included in the global fit DSSV++

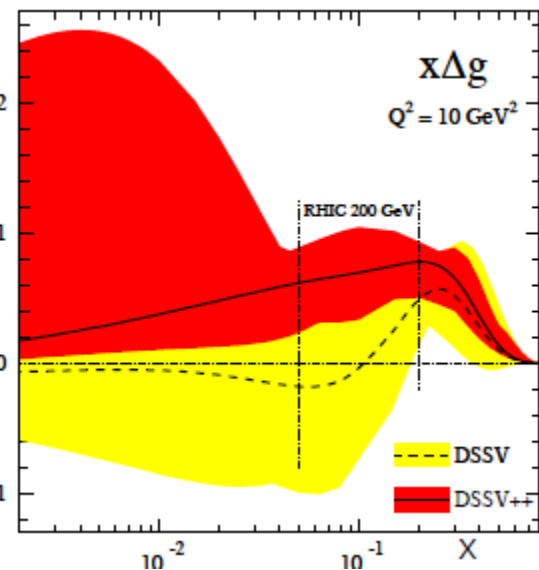
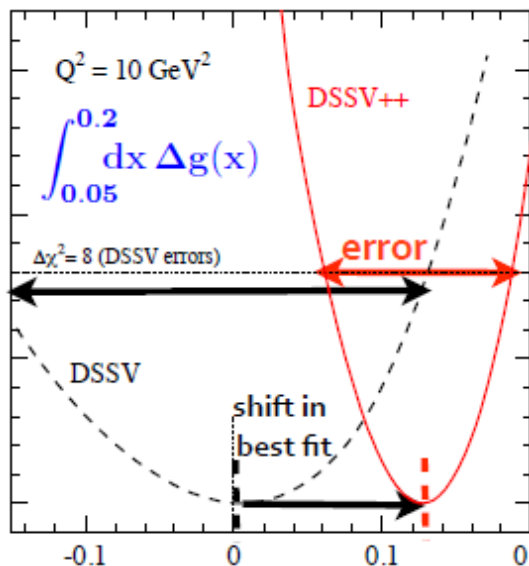
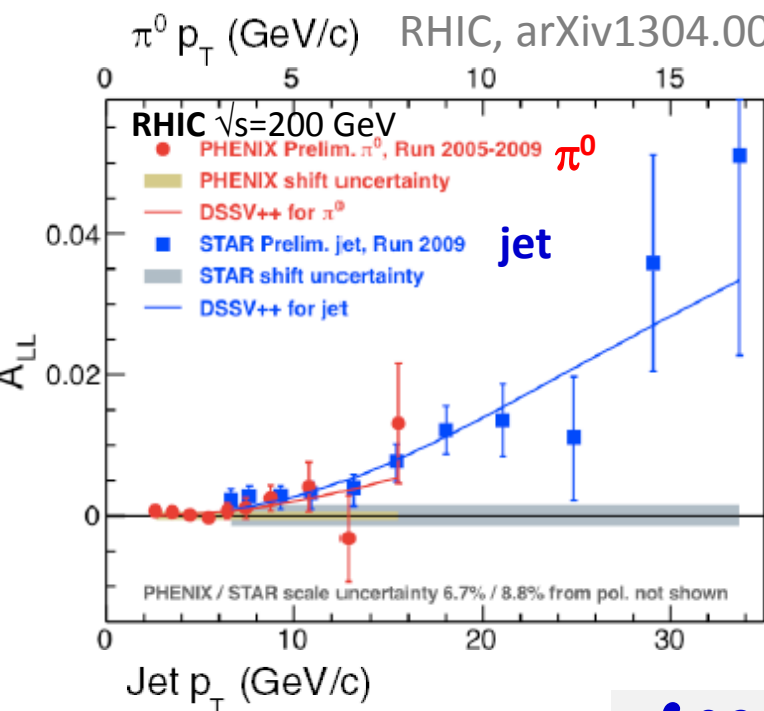
Gluon spin from $\vec{p} \vec{p}$ collisions at RHIC



$$A_{LL}(P_T) \propto \frac{\Delta g}{g} \frac{\Delta q}{q} + \frac{\Delta g}{g} \frac{\Delta g}{g} + \dots$$

Measure double spin asymmetry
Compare data to global fits

DSSV: De Florian, Sassot, Stratmann, Volgelsang, PRL113(2014)



$$\int_{0.05}^{0.2} \Delta g(x) dx = 0.1 \pm 0.06$$

Large uncertainties in the unmeasured small x domain

Transverse spin and transverse momentum in SIDIS

The **transversity** h_1 or $\Delta_T q$



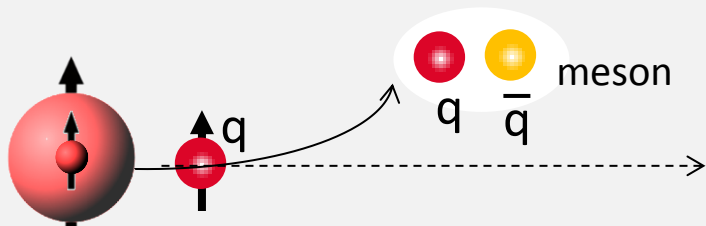
Measures the diff. of density of quarks with spin // and anti// to the transverse spin of the nucleon

The **Sivers** f_{1T}^\perp PDF

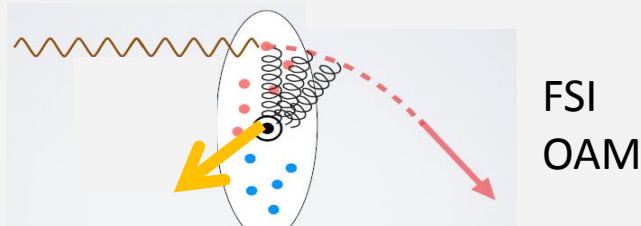


correlates the quark k_T and the nucleon transv. spin

Chiral-odd \rightarrow **Collins** odd FF



Chiral-even and T-odd

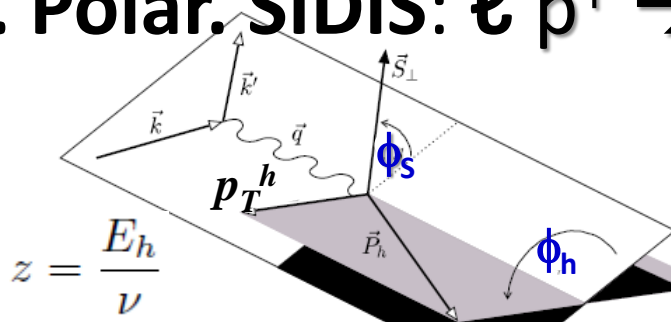


$$\mathbf{A}_{\text{Coll}} \approx \frac{\sum_q e_q^2 h_1^q(x) \otimes H_{1q}^{\perp h}(z, p_T^h)}{\sum_q e_q^2 f_1^q(x) \otimes D_{1q}^h(z, p_T^h)}$$

$$\mathbf{A}_{\text{Siv}} \approx \frac{\sum_q e_q^2 f_{1T}^{\perp q}(x) \otimes D_{1q}^h(z, p_T^h)}{\sum_q e_q^2 f_1^q(x) \otimes D_{1q}^h(z, p_T^h)}$$

Transv. Polar. SIDIS: $\ell p^\uparrow \rightarrow \ell h^\pm X$

Collins asymmetry
in $\sin(\phi_h + \phi_s - \pi)$

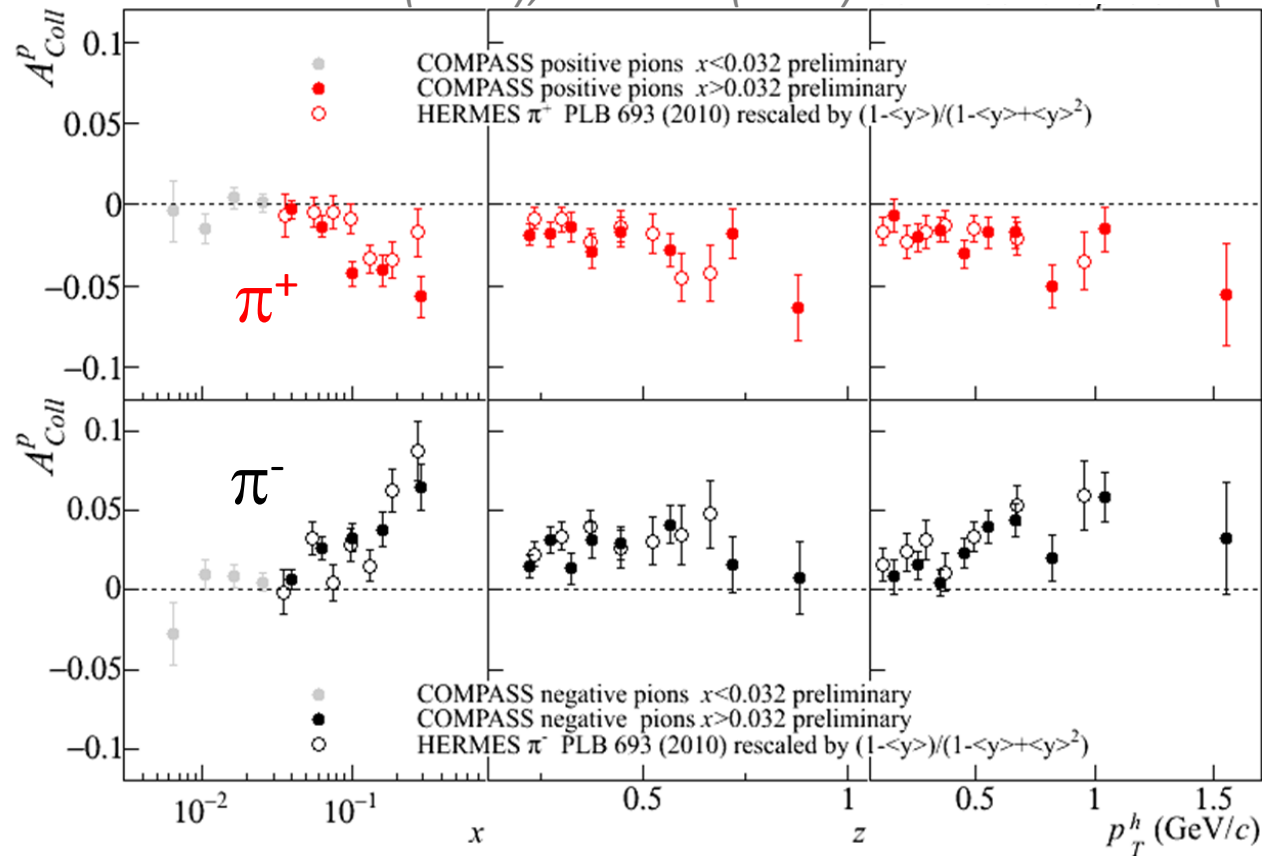


Sivers asymmetry
in $\sin(\phi_h - \phi_s)$

Transverse spin and Collins effect in SIDIS

Collins asymmetry

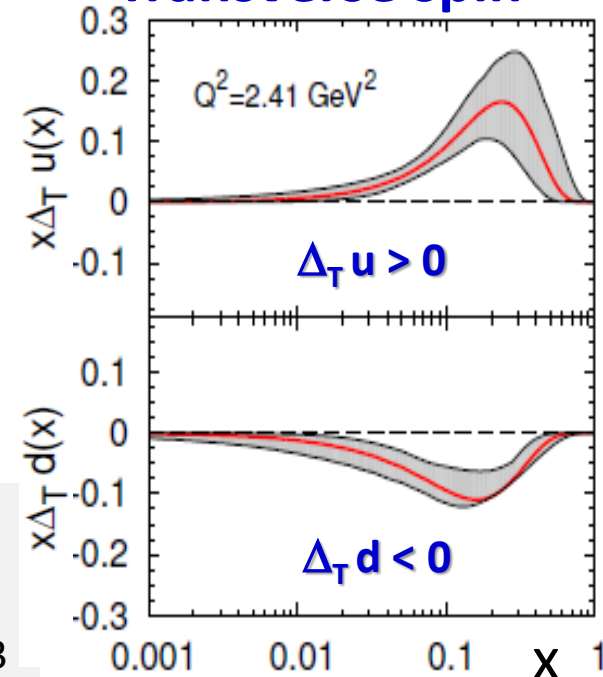
COMPASS: PLB 692 (2010), PLB 717 (2012) HERMES: PLB693(2010)



Global fit
 using data from
HERMES p,
COMPASS p and d,
Belle e+e- (\rightarrow FF)

Bacchetta et al., JHEP1303 (2013)
 Anselmino et al. PRD87 (2013)

Transverse spin



Large effect of opposite sign for π^+ and π^-

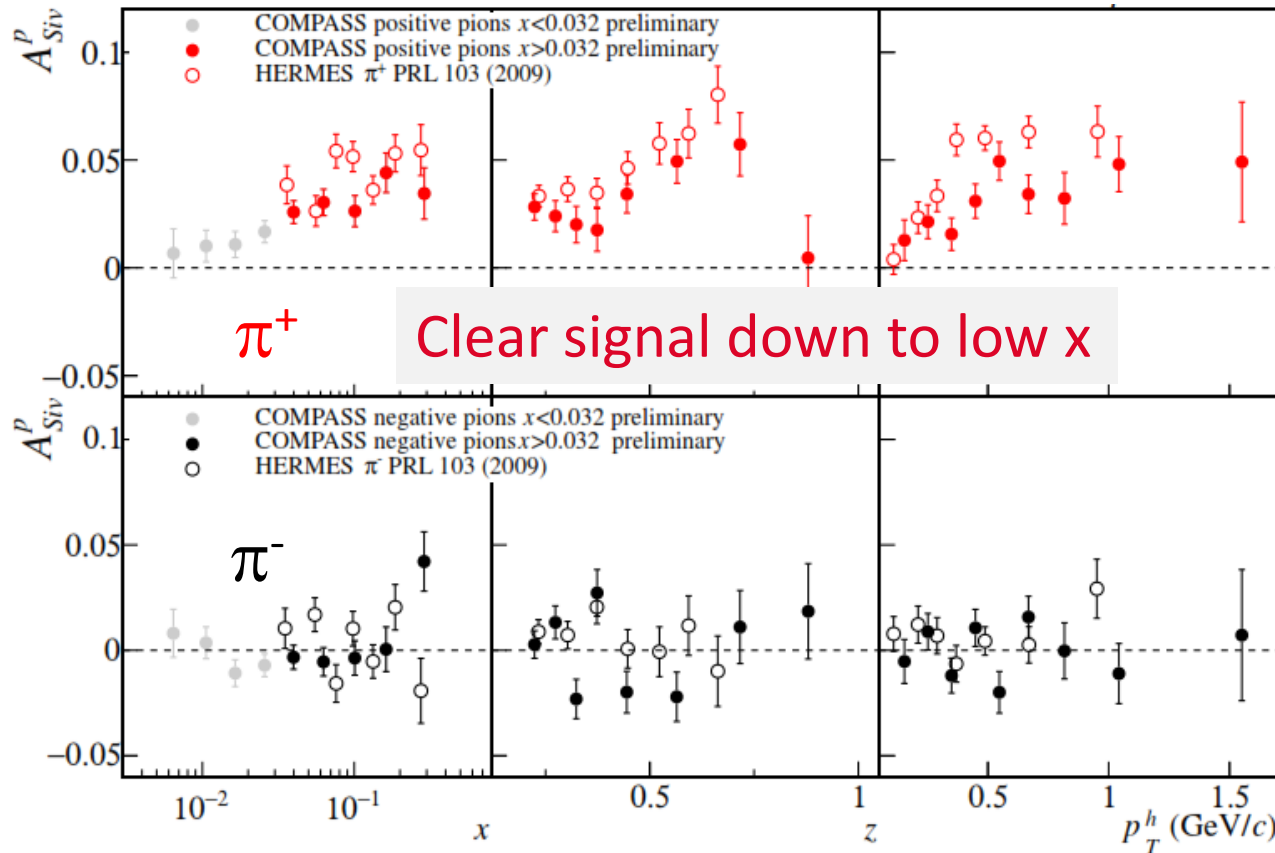
Good agreement between COMPASS and HERMES for $x > 0.032$

Not obvious as the COMPASS Q^2 domain is larger by a factor of about 2 or 3

Sivers in SIDIS

Sivers asymmetry

COMPASS: PLB 692 (2010), PLB 717 (2012) HERMES: PRL103(2009)

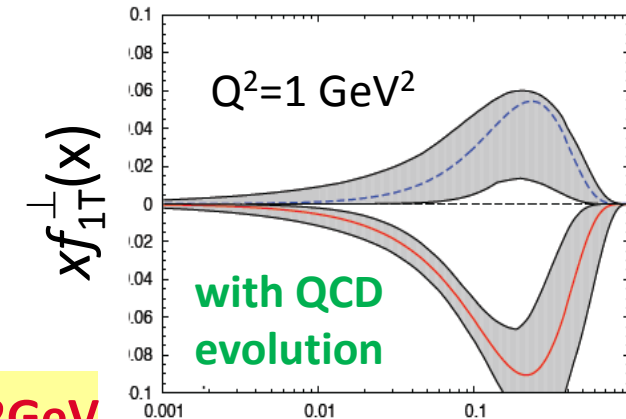
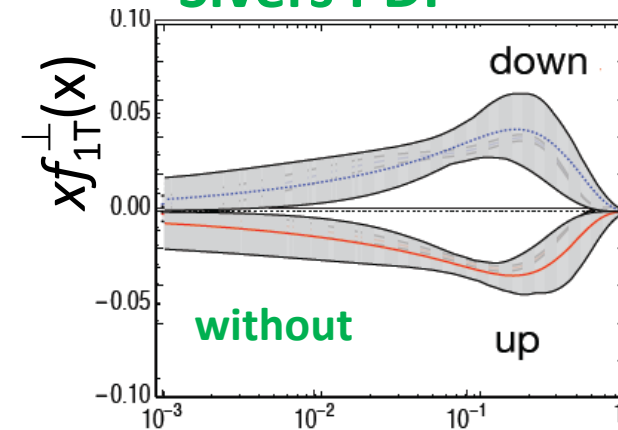


agreement between COMPASS and HERMES for $x > 0.032$
 but clear indication that the strength \searrow when $Q^2 \nearrow$

predictions

Aybat, Prokudin, Rogers,
 PRL108(2012) (2013)

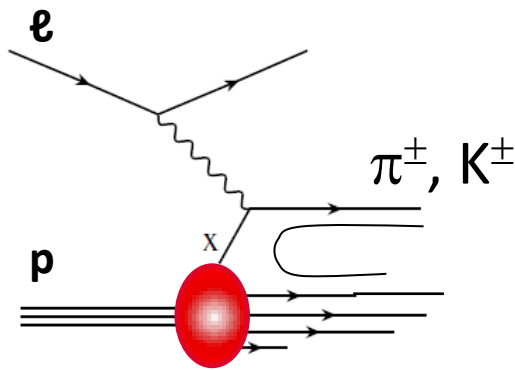
Sivers PDF



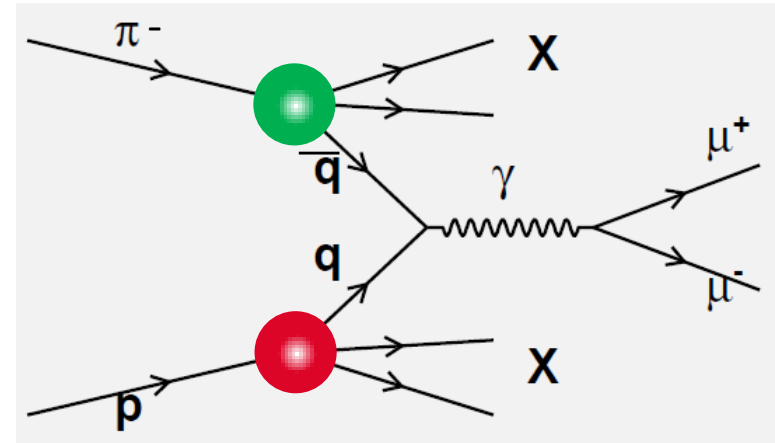
Extended TMD program in SIDIS at COMPASS and Jlab 12GeV

Test of Universality

SIDIS: $e p^\uparrow \rightarrow e h^\pm X$



Drell-Yan (DY)



Cross sections:

In SIDIS: convolution of a TMD with a fragmentation function

In DY: convolution of 2 TMDs

$$\sigma^{DY} \propto f_{\bar{u}|\pi^-} \otimes f'_{u|p}$$

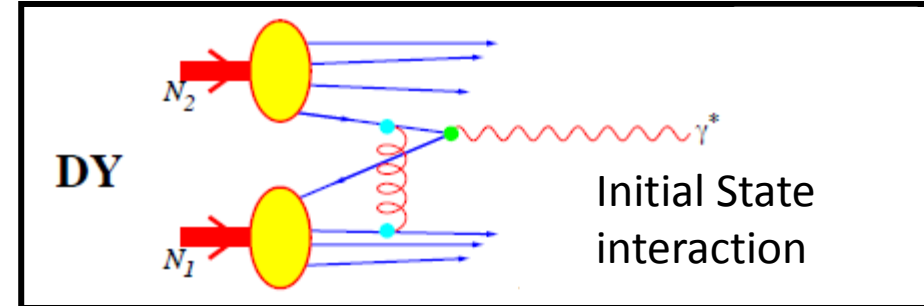
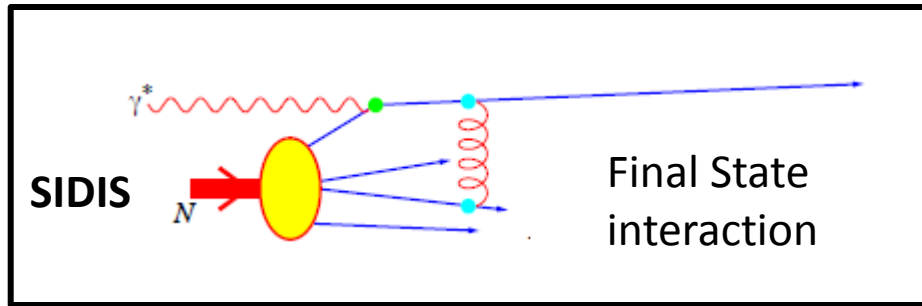
→ test of universality

Test of Universality

T-odd character of the Sivers functions

In order not to be forced to vanish by time-reversal invariance the SSA requires an interaction phase generated by a rescattering of the struck parton in the field of the hadron remnant

Time reversal

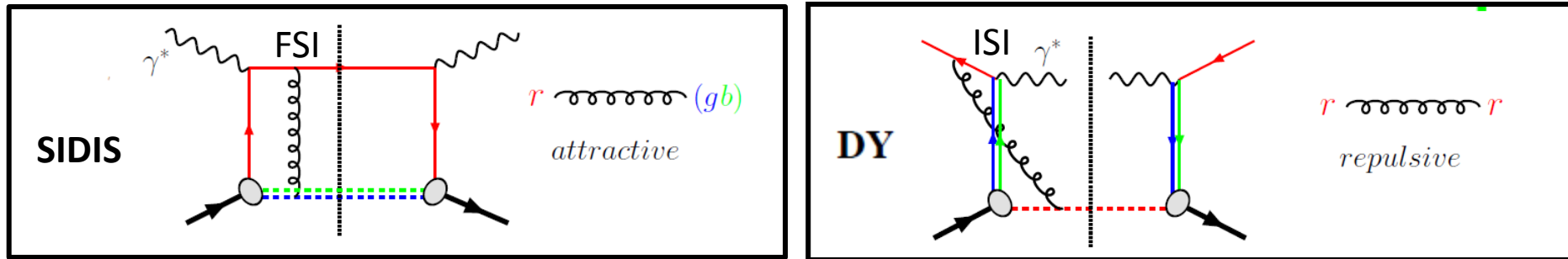


Test of Universality

T-odd character of the Sivers functions

In order not to be forced to vanish by time-reversal invariance the SSA requires an interaction phase generated by a rescattering of the struck parton in the field of the hadron remnant

Time reversal



The Sivers function is process dependent, it changes sign to provide the gauge invariance

$$f_{1T}^{\perp}(\text{SIDIS}) = -f_{1T}^{\perp}(\text{DY})$$

COMPASS end 2014 and 2015 with pion beam and polarized target:

1st ever experimental check of the change of sign of Sivers
confronting polarized Drell-Yan and SIDIS results

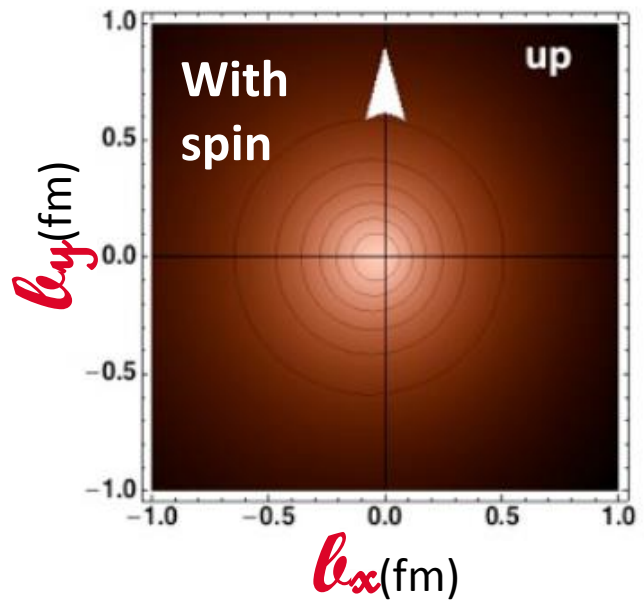
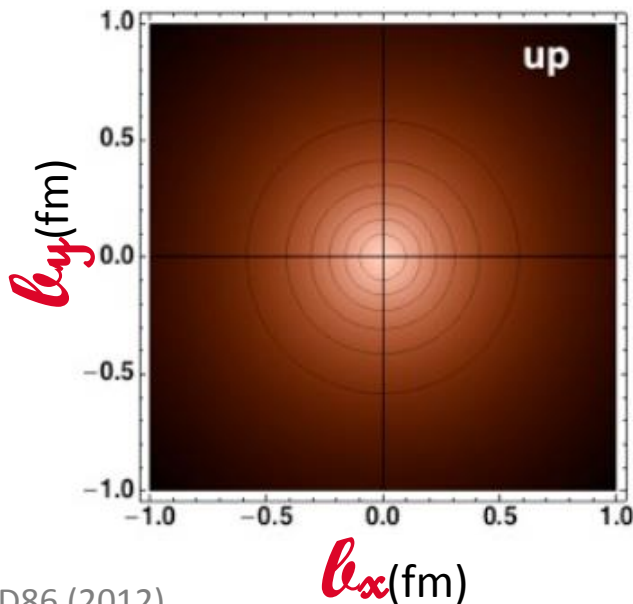
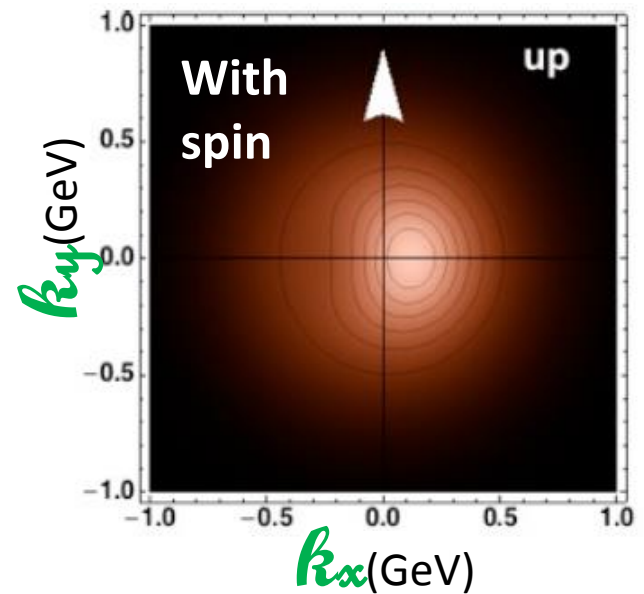
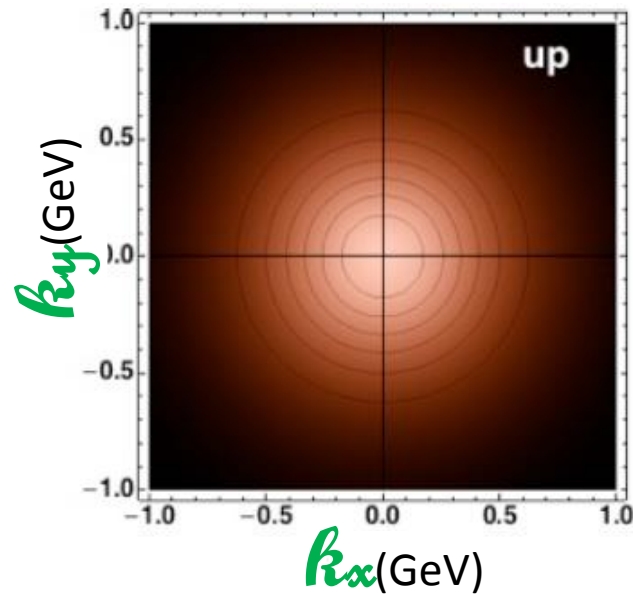
other DY programs in the world (Fermilab, RHIC, FAIR, NICA, JPARC)

3D imaging: mapping in the transverse plane

Proton
moving
towards us

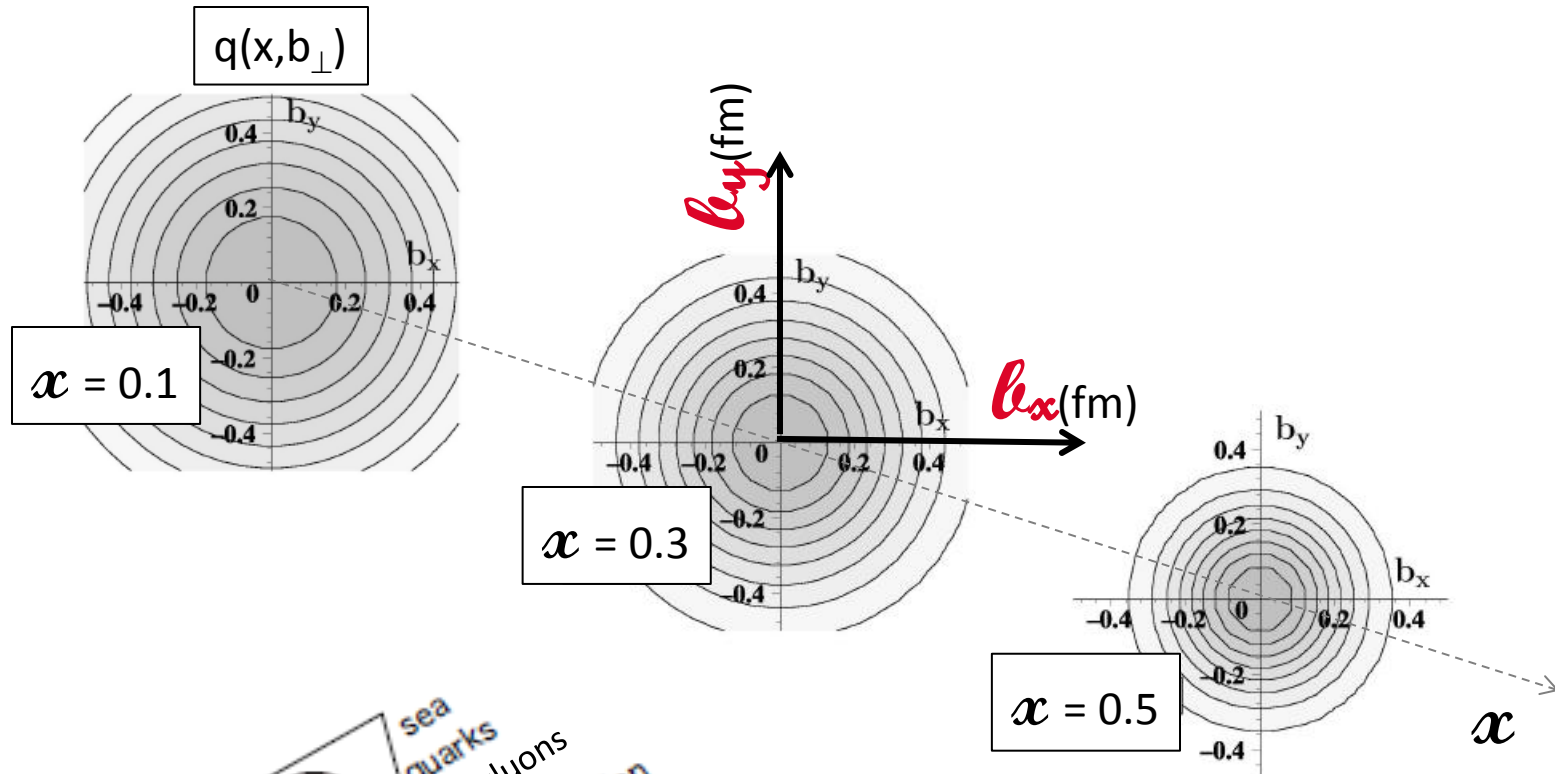
Transverse
momentum maps
with TMDs

Transverse
position maps
with GPDs

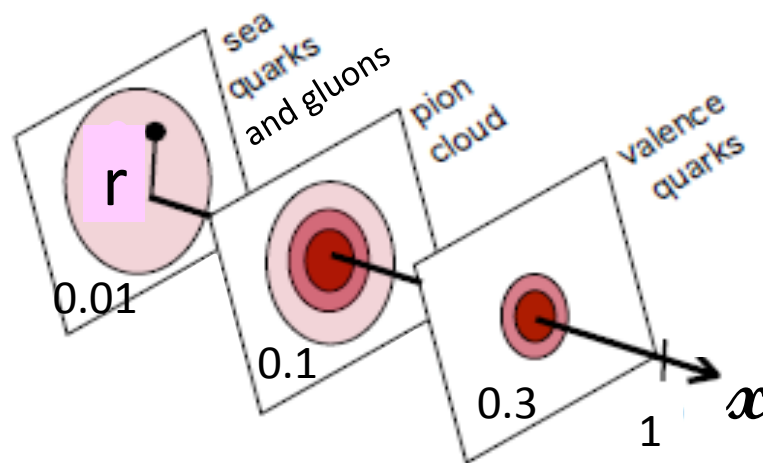


3D imaging: mapping in the transverse plane

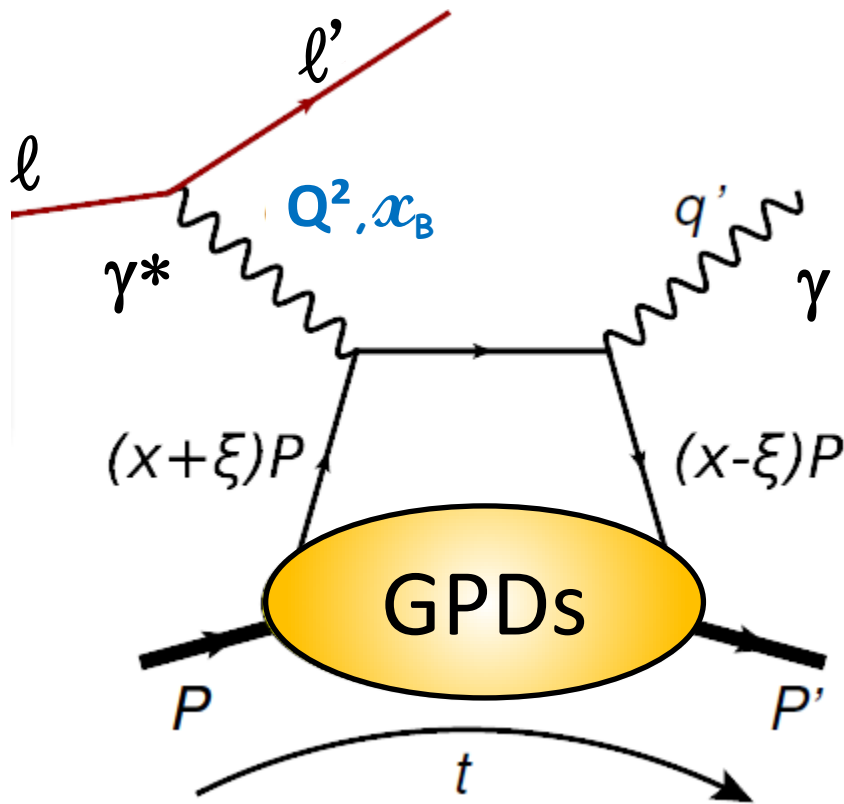
Proton
moving
towards us



Transverse
position maps
with GPDs



Deeply virtual Compton scattering (DVCS)



Definition of variables:

x : average long. momentum

ξ : long. mom. difference $\simeq x_B/(2 - x_B)$

t : four-momentum transfer
related to b_\perp via Fourier transform

D. Mueller *et al*, Fortsch. Phys. 42 (1994)

X.D. Ji, PRL 78 (1997), PRD 55 (1997)

A. V. Radyushkin, PLB 385 (1996), PRD 56 (1997)

DVCS: $l p \rightarrow l' p' \gamma$

the golden channel

because it interferes with
the Bethe-Heitler process

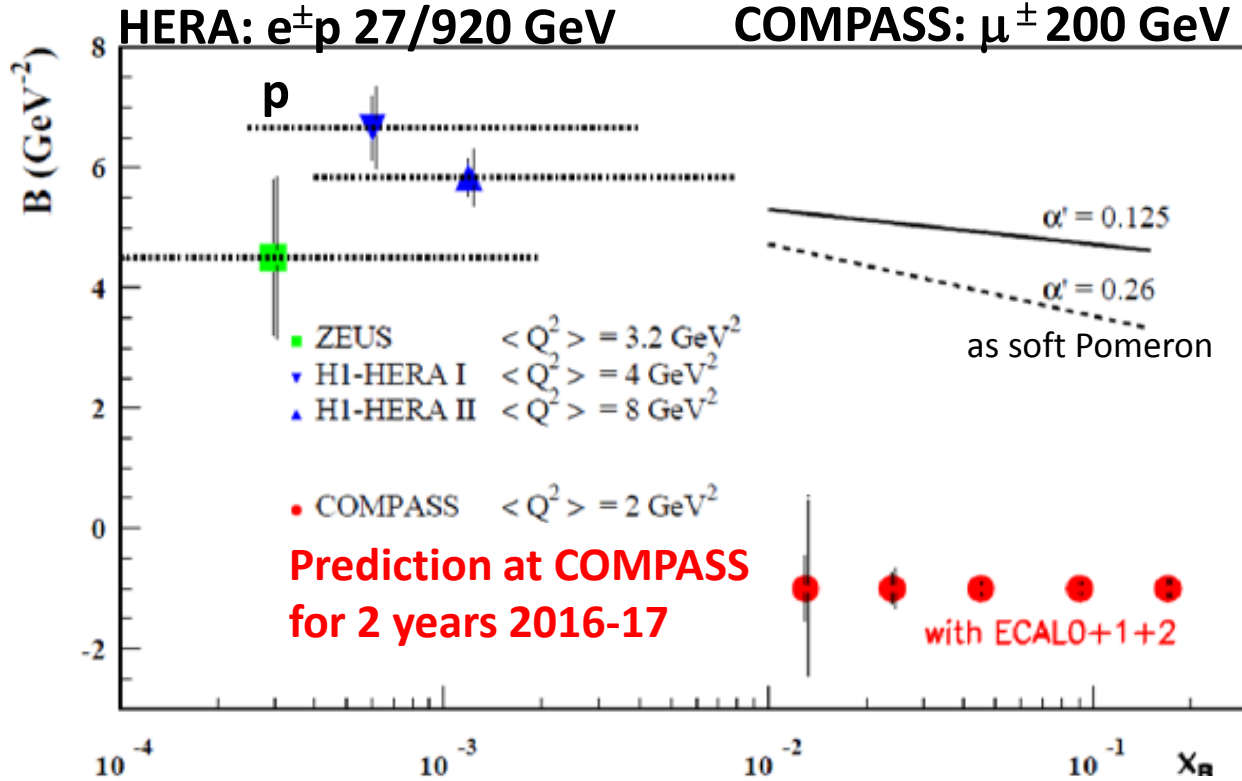
important parameters:

- high luminosity
- different beam energies
- polarized leptons
- positive and negative leptons

also meson production

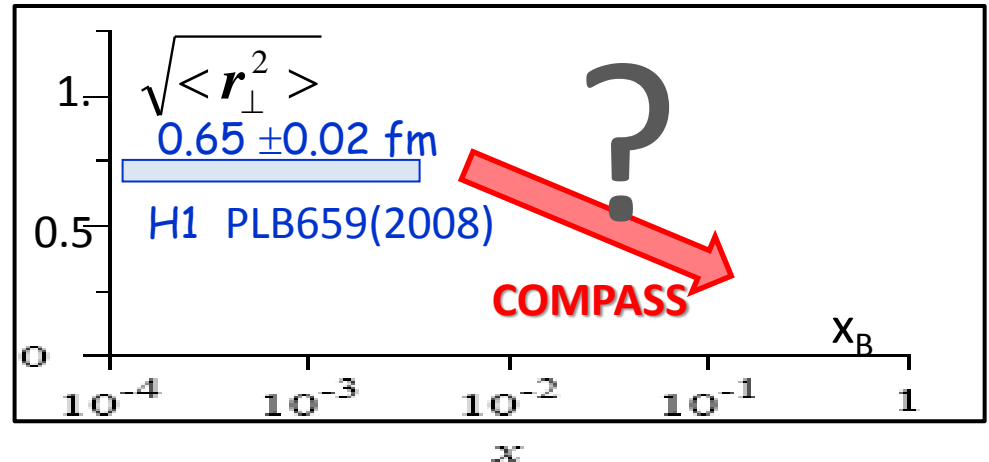
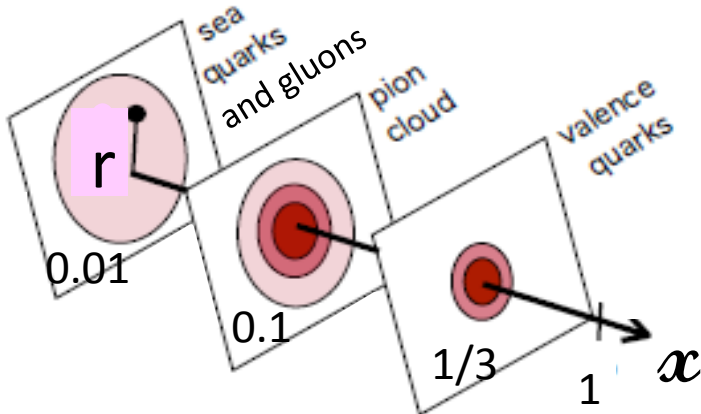
$l p \rightarrow l' p' \rho$ or ϕ or $J/\psi, \dots$

Gluon and sea quark imaging



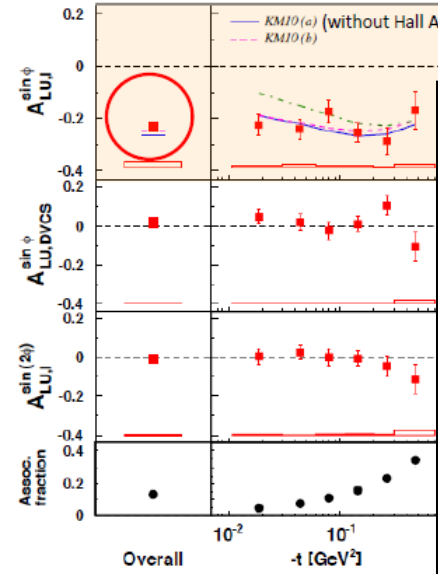
$$d\sigma^{\text{DVCS}}/dt = e^{-Bt}$$

$$\langle r_\perp^2(x_B) \rangle \approx 2B(x_B)$$



Beam Spin Asymmetry with HERMES

A. Airapetian et al, JHEP 07 (2012) 032



Beam Spin Diff and Sum – Jlab HallA

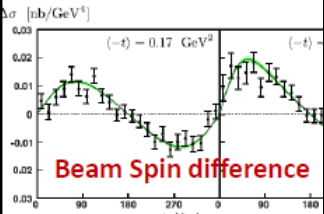
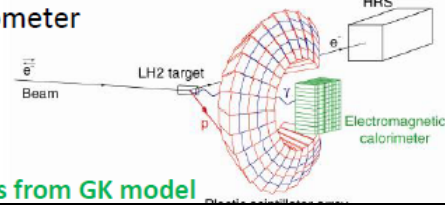
E00-110 pioneer experiment with magnetic spectrometer

3 measurements: $x_B=0.36$ $Q^2=1.5, 1.9, 2.3$ GeV²

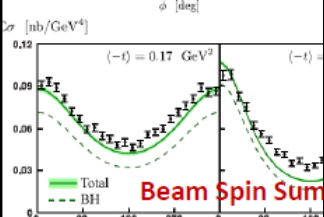
$$\vec{e}p \rightarrow e\gamma p$$

Data: Munoz et al. PRL97, 262002 (2006)

Model: Kroll, Moutarde, Sabatié, EPJ3 (2013) with GPDs from GK model



Beam Spin difference



Beam Spin Sum

Do we und

KM: Kumerički and Müller

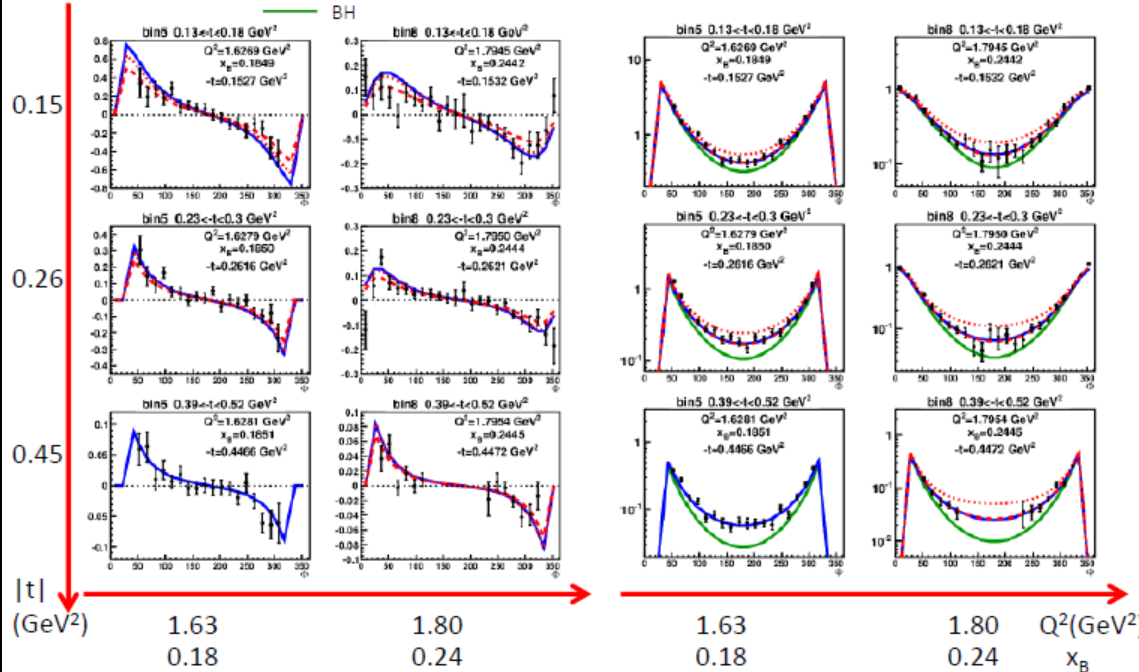
GHL11: G. Goldstein, J. Her

Beam Spin Diff and Sum – Jlab CLAS

PRELIMINARY

VGG: Guidal, Polyakov, Radyushkin, Vanderhaeghen, PRD72(2005)

KM10ab (fit) : Kumerički, Müller, Nucl.Phys. B841 1 (2010)



Important activities to get

Im DVCS and Re DVCS

✓ tricky data analyses

✓ models and fits

Valence quark imaging

the GPD H in Im DVCS

- Different local fits
- VGG model
- - - KM10 global fit on the world data ranging from H1, ZEUS to HERMES, JLab

e^- 6 GeV

Jlab Hall A

Beam Spin Diff
Beam Spin Sum

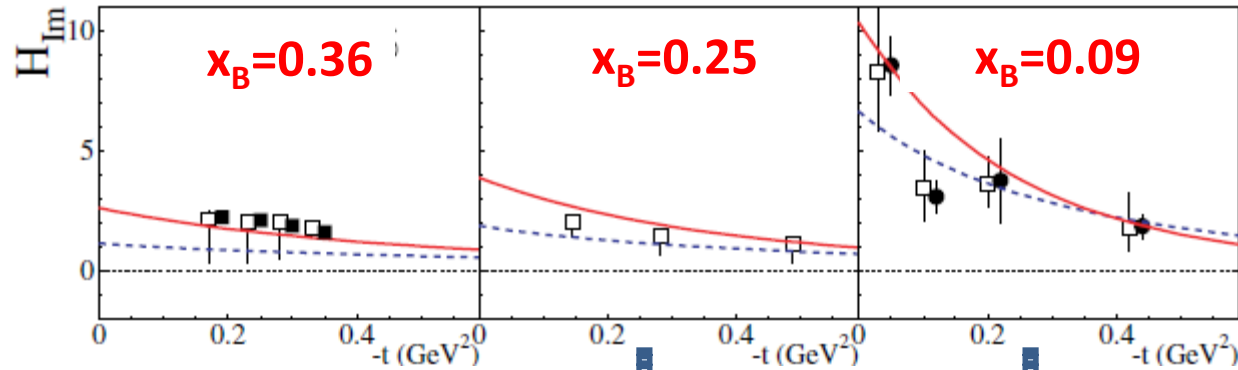
Jlab CLAS

Beam Spin Asym
Long Pol targ Asym

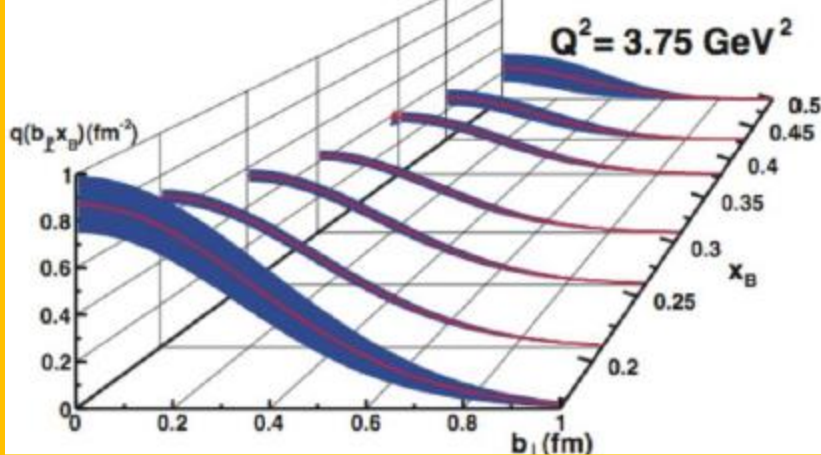
e^\pm 27 GeV

HERMES

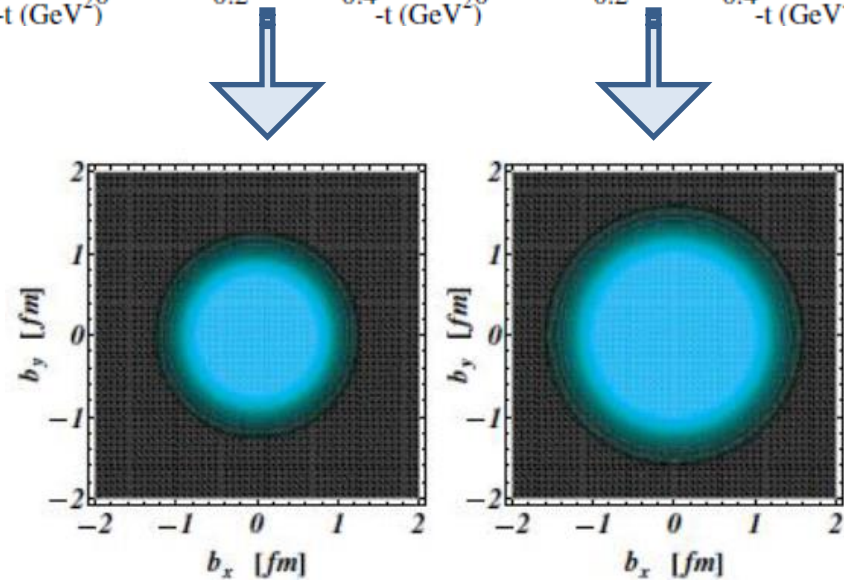
Beam Spin Asym
Beam Charge Asym



Projection for Jlab 12 GeV



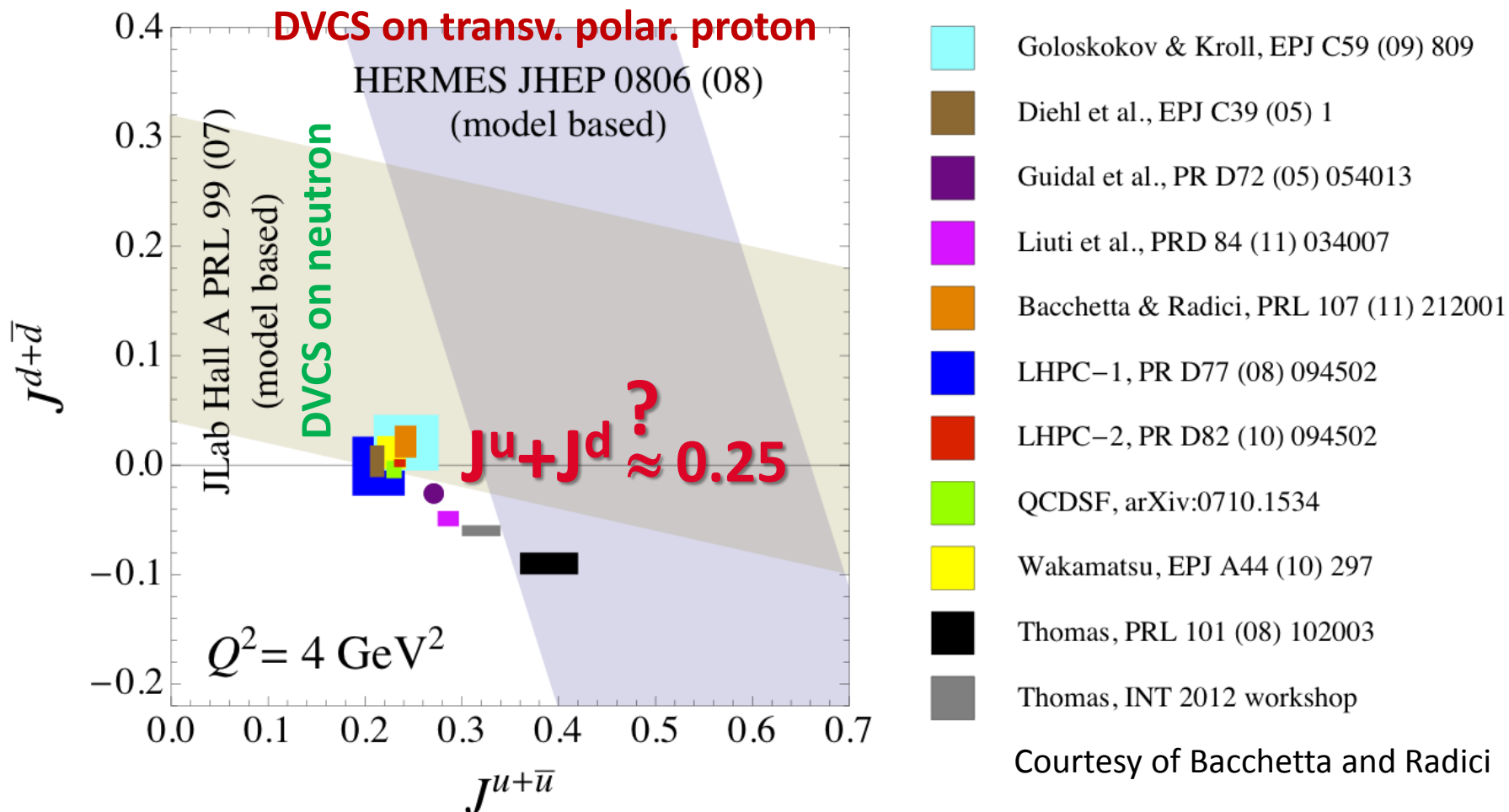
Dudek et al., EPJA48 (2012)



Guidal, Moutarde, Vanderhaeghen, Rept. Prog. Phys. 76 (2013)

Model dependent extraction of J^u and J^d

the GPD E, holy grail for OAM



GPD major program for JLab 12 GeV, COMPASS and for a future electron-proton collider

**Understanding the structure of the nucleon
is still an exciting and vibrant area of research**

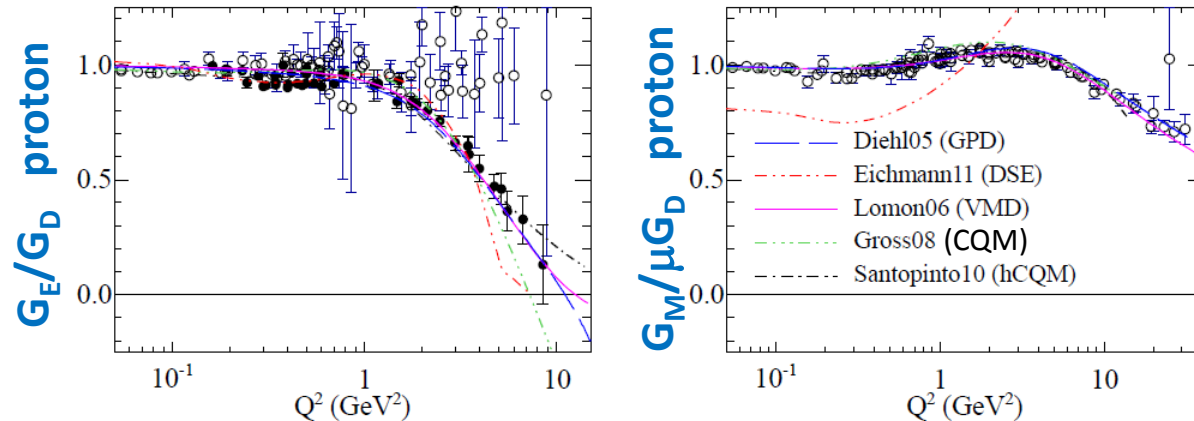
**Tremendous experimental effort
matched to theoretical progress**

Many details given in the parallel sessions
“Quarks and Gluons in hadrons, the hadron spectrum”

Many slides for a longer talk!

The proton Form Factors

From Puckett et al., PRC85 (2012)



The form factors deviate from a dipolar approximation

pQCD: G_E^p/G_M^p should be constant at very high Q^2 → No scaling before $Q^2 = 10 \text{ GeV}^2$

Lattice calculations QCDSF/UKQCD Collaboration, Collins et al., PRD84 (2011)

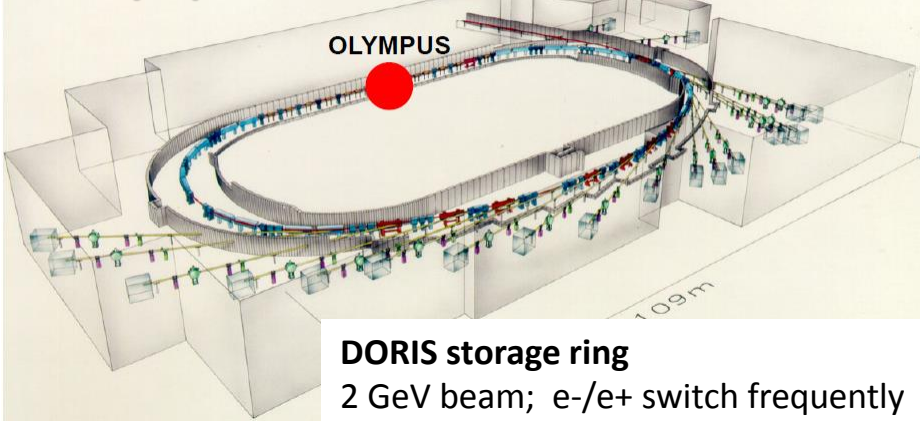
Progress with small lattice spacing, large V (>3.5fm), $m_\pi \sim 180\text{MeV}$ and chiral extrapolation

Many Models:

- Vector Meson Dominance (VMD)
- Dispersion Analysis
- Generalized Parton Distr. (GPD)
- Dyson-Schwinger Equations (DSE)
ab-initio calculation in npQCD
- Relativistic Constituent Quarks(CQM) with OAM
- Pion cloud
Chiral quark soliton

Stringent comparison: e^+ and e^- scattering

✓ **Olympus: BLAST @ DORIS @ DESY**



DORIS storage ring

2 GeV beam; e^-/e^+ switch frequently

Former BLAST experiment

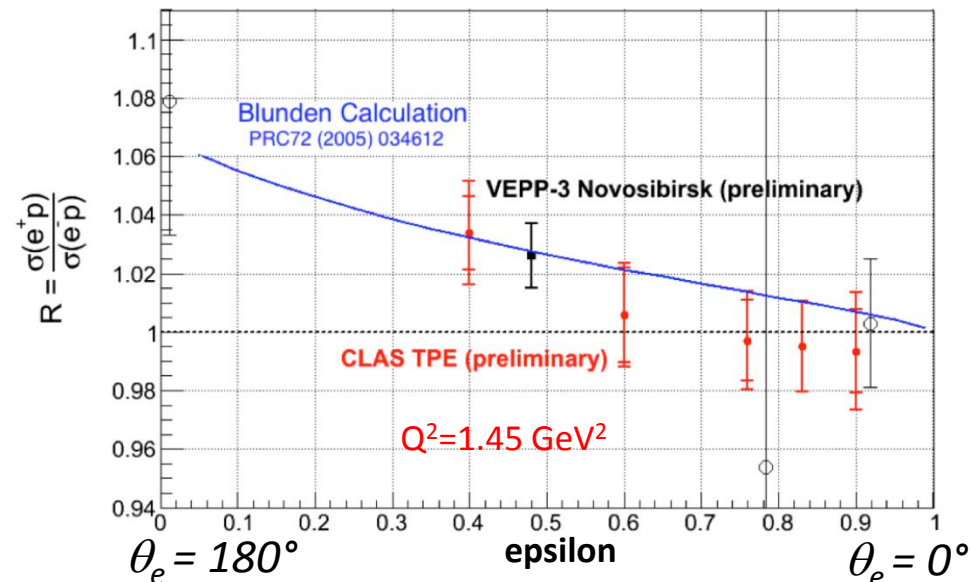
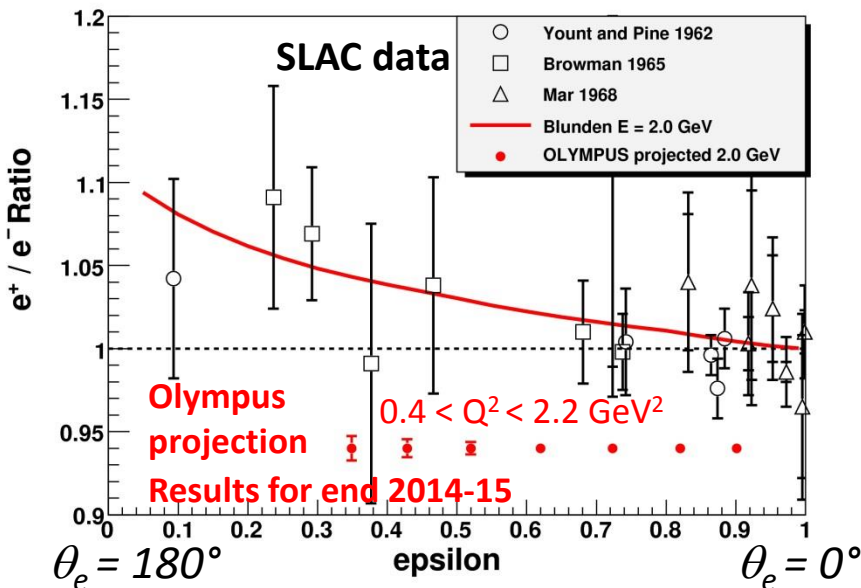
large acceptance left/right symmetric
internal target

✓ **VEPP-3 à Novosibirsk**

e^-/e^+ storage ring + internal target
 $Q^2 = 1.6 \text{ GeV}^2$ and $\epsilon = 0.47$

✓ **CLAS-PR04-116 @ Jlab**

e^-/e^+ pair production from photon beam
simultaneous measurements
several Q^2 measurements between 0.5 - 1.5 GeV^2
 $0.2 < \epsilon < 0.9$



Proton radius from MAMI ep scattering at low Q^2

High precision and redundancy

MAMI-A1 -3 high resolution spectrometers

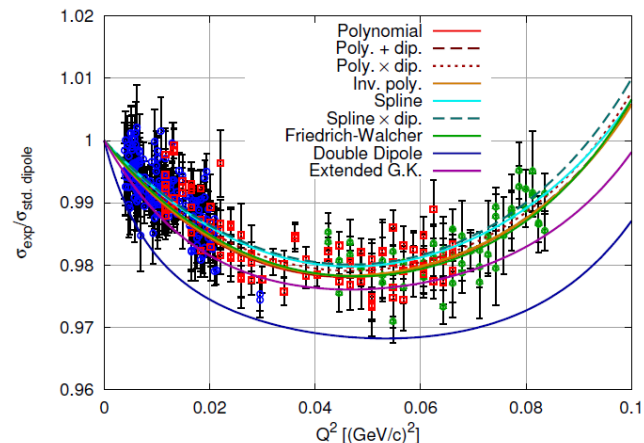
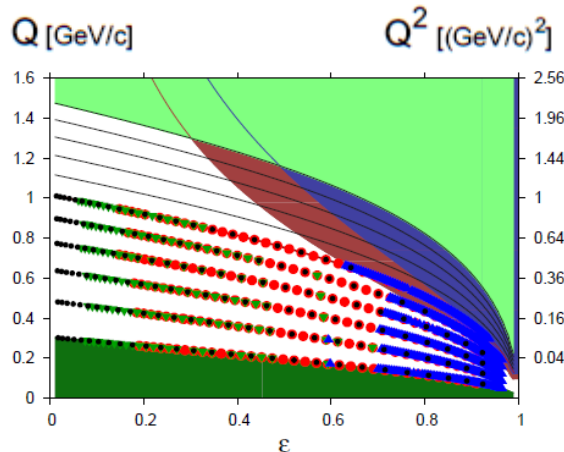
1400 settings $0.003 < Q^2 < 1 \text{ GeV}^2$

Statistics $< 0.1\%$

Control of Luminosity with the 3rd spectro

Measure at the same angle with 2 spectro

- spectrometer A
- ▲ spectrometer B
- ▼ spectrometer C



Super-Rosenbluth technique

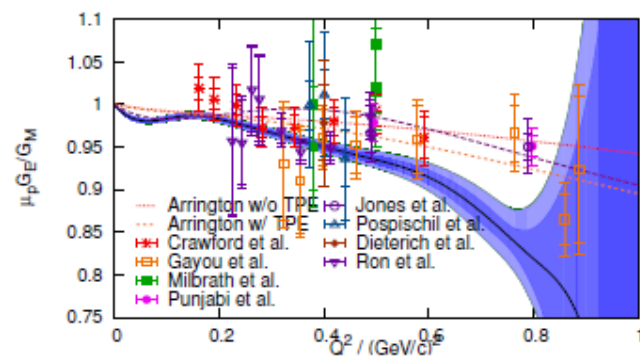
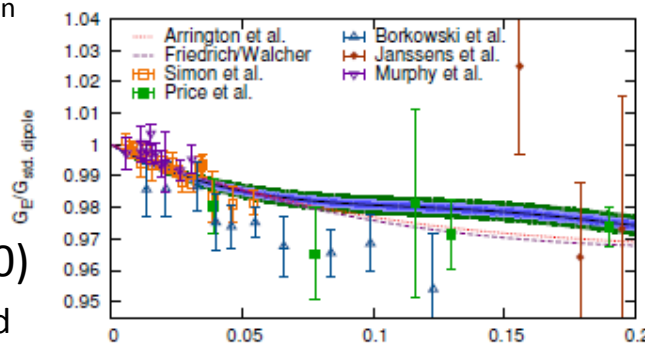
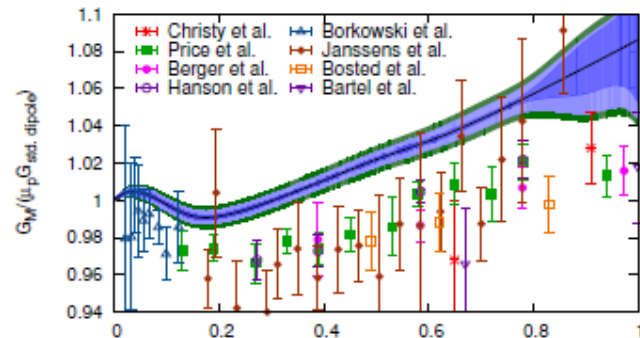
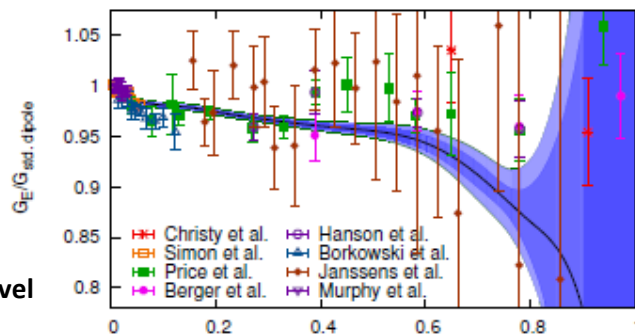
Fit of form factor models

Directly to cross section

All Q^2 and ϵ data used in one fit

Wide range of \neq parametrizations

- Best fit
- + stat. 68% confidence level
- + syst errors
- + 50% Coulomb correction



$$r_E^p = 0.879 \pm 0.008 \text{ fm}$$

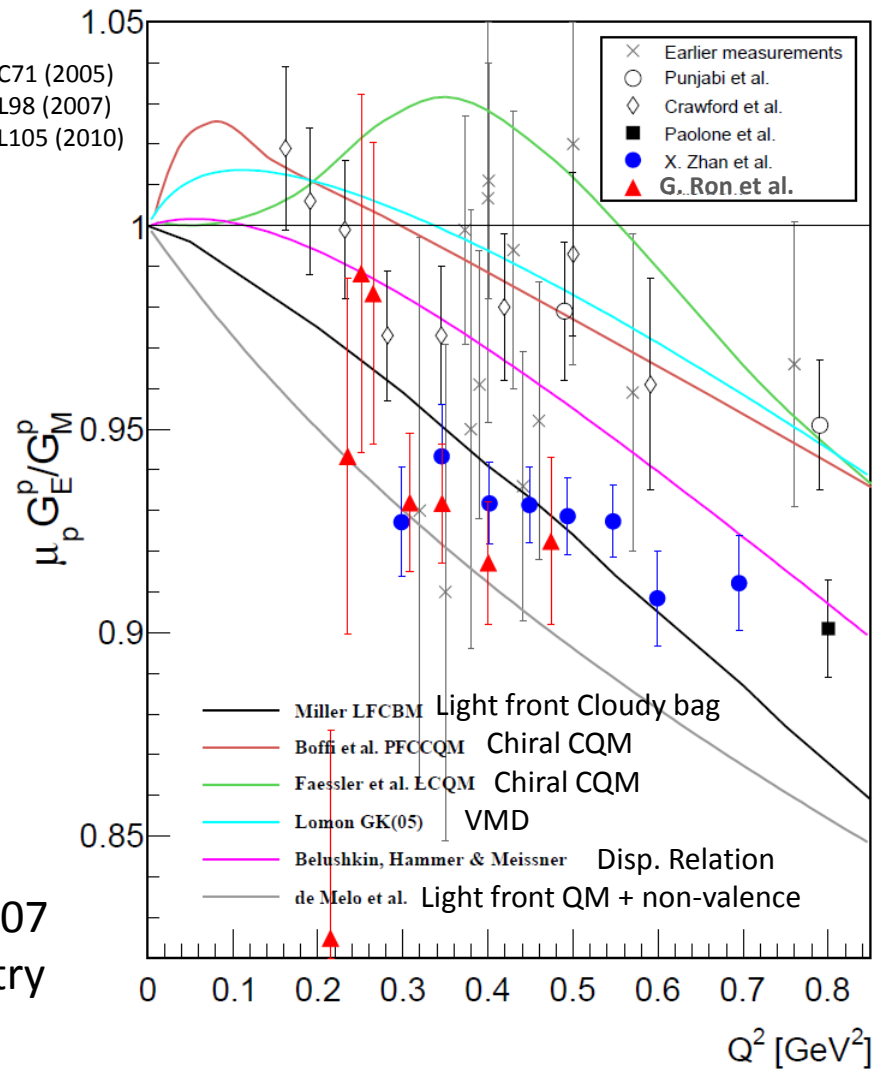
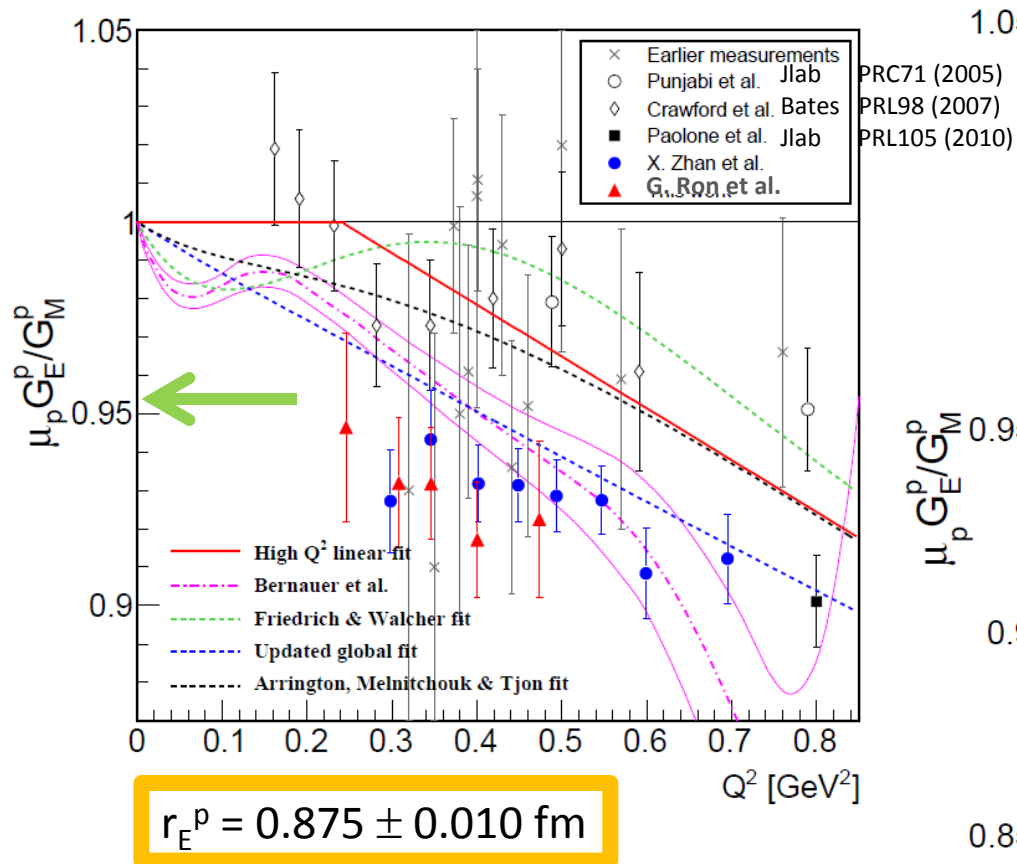
Bernauer et al. , PRL105 (2010)
& PRC90 (2014) Including TPE and
all world data

Proton radius from JLab ep scattering at low Q^2

JLab Hall A using recoil polarimetry:

Exp E05-103: Ron et al. PRL99 (2007), update PRC84 (2011)

Exp E08-107: Zhan et al. PLB 705 (2011)



in near future results from the 2nd part of E08-107
polarized beam - polarized NH₃ target asymmetry

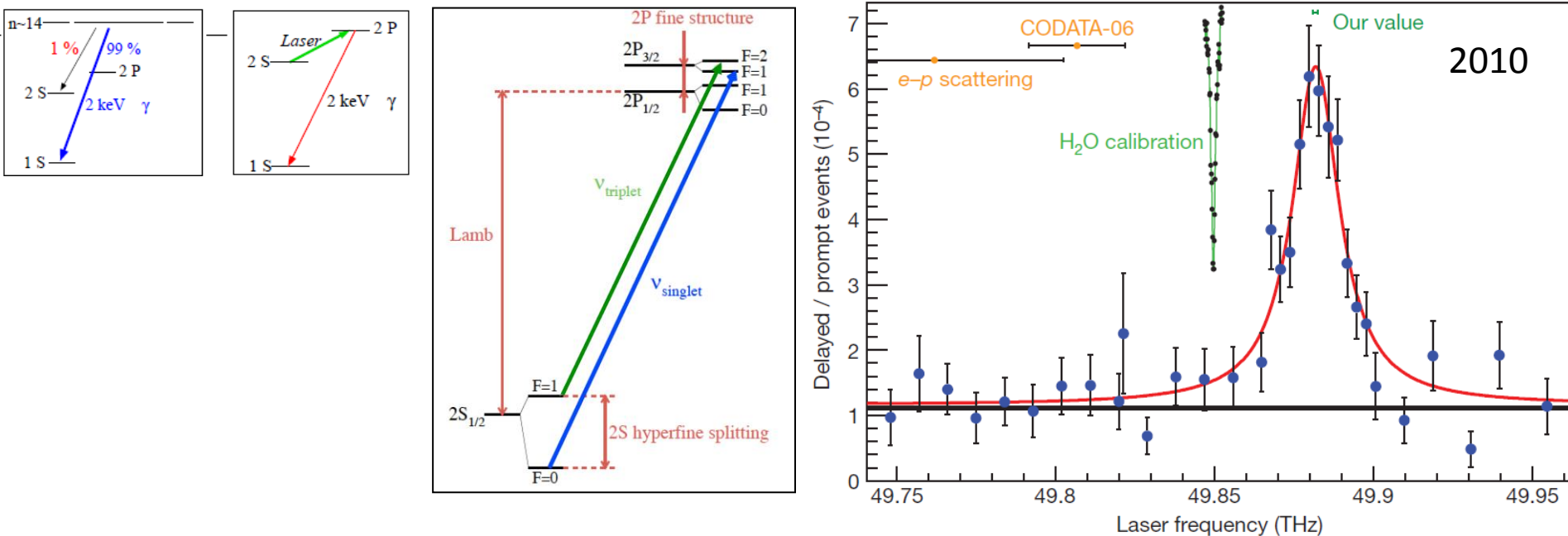
$0.01 < Q^2 < 0.16$ GeV²

Proton radius from muonic hydrogen Lamb shift

New 5keV muon beam line at PSI

Muons stopped in H₂ gas at low pressure → excited μp atoms (n=14) are formed

“prompt” (t ~ 0) “delayed” (t ~ 1 μs)



Pohl et al., Nature 466 (2010): **2S → 2P Lamb shift**

$$\Delta E_1(\text{meV}) = 209.9779(49) - 5.2262 r_p^2 + 0.0347 r_p^3 \Rightarrow r_p = 0.84184 \pm 0.00067 \text{ fm}$$

Antognini et al., Science 339 (2013): **2S → 2P Lamb shift + 2S-HFS**

$$\Delta E_2(\text{meV}) = 206.0336(15) - 5.2275(10) r_p^2 + 0.0332(20)_{\text{TPE}} \Rightarrow r_p = 0.84087 \pm 0.00039 \text{ fm}$$

Time evolution of the proton radius from H Lamb shift and ep scattering

PHYSICAL REVIEW

VOLUME 102, NUMBER 3

MAY 1, 1956

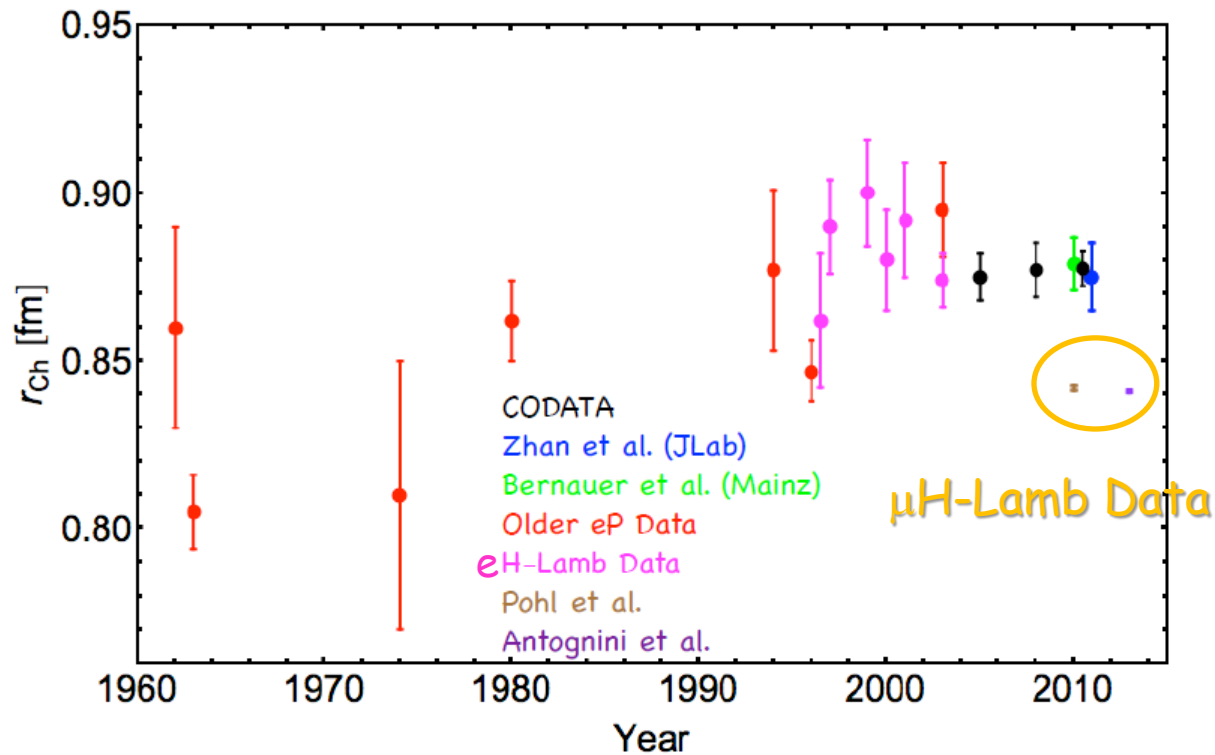
Elastic Scattering of 188-Mev Electrons from the Proton and the Alpha Particle*†‡§||¶

R. W. McALLISTER AND R. HOFSTADTER

Department of Physics and High-Energy Physics Laboratory, Stanford University, Stanford, California

(Received January 25, 1956)

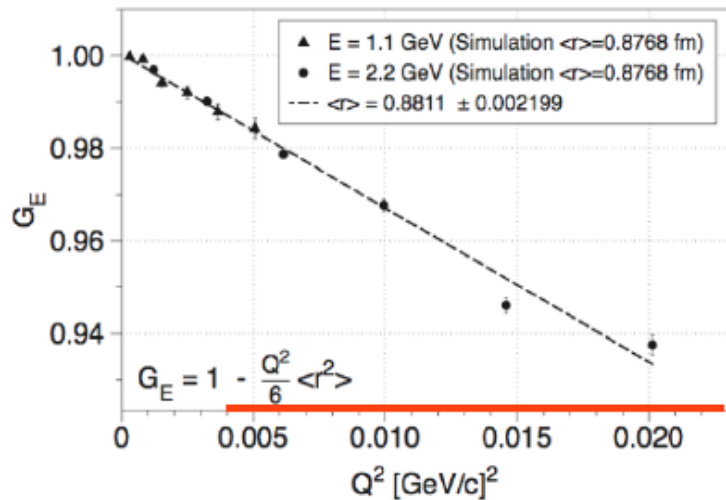
The root-mean-square radii of charge and magnetic moment are each $(0.74 \pm 0.24) \times 10^{-13}$ cm.



UNEXPECTED!

Experiments at very low Q^2

The PRAD proton radius proposal at JLab

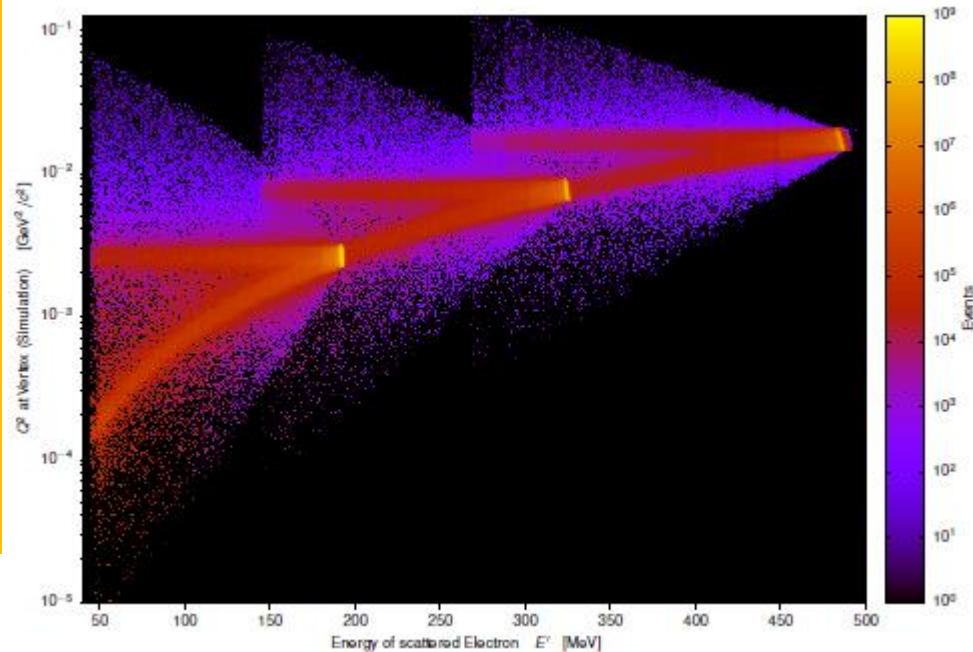
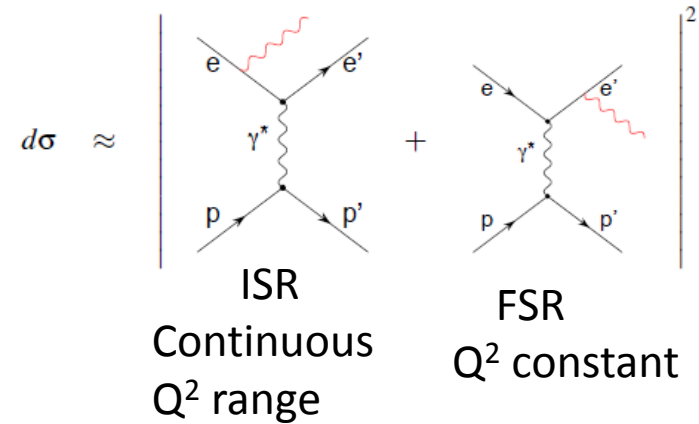


Lower $Q^2 = 2 \times 10^{-4}$ GeV^2

Low intensity beam in Hall B
into windowless target

Scattered ep and Moller electrons (for
normalisation) into an EM calorimeter at 0°

Initial State Radiations at MAMI



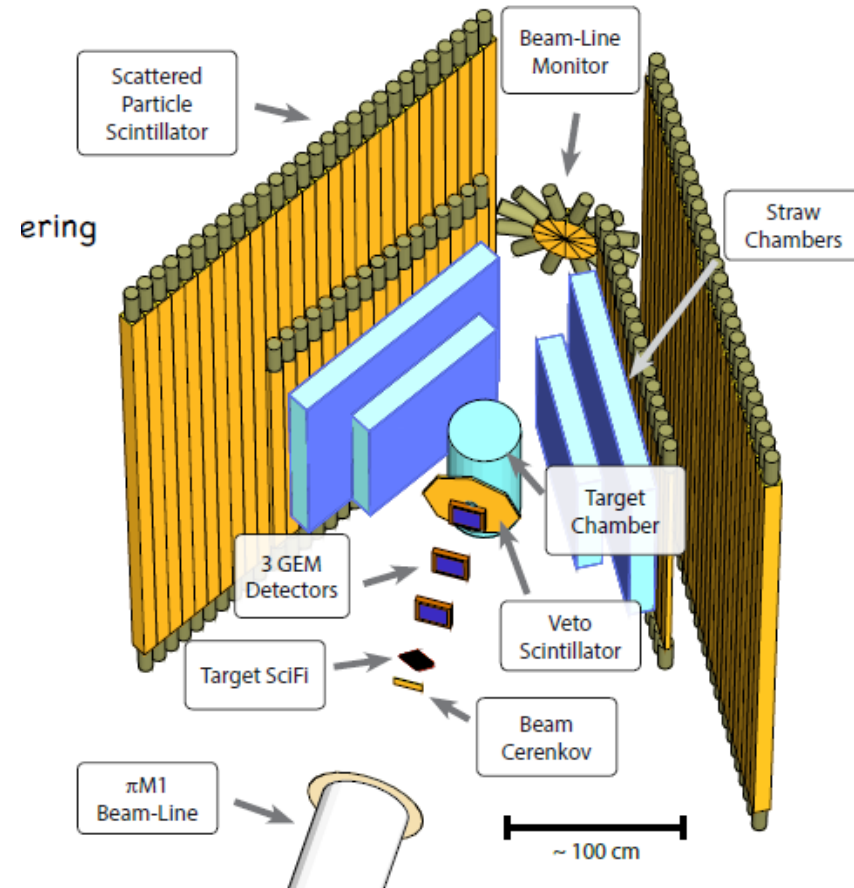
The MUSE experiment at PSI

r_p (fm)	ep	μp
Spectroscopy	0.8758 ± 0.077	0.84087 ± 0.00039
Scattering	0.8770 ± 0.060	???

use the world's most powerful low-energy separated $e/\pi/\mu$ beam

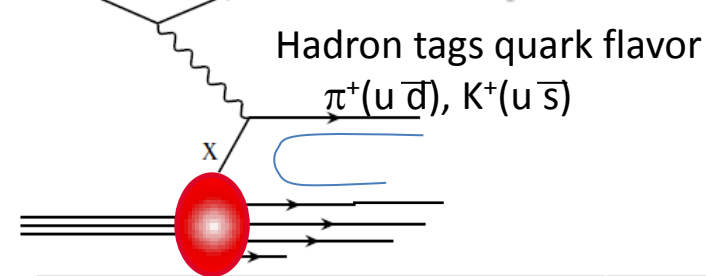
for a direct comparison

- if ep and μp scattering different?
- if TPE are different using $e^+ e^- \mu^+ \mu^-$ beams?



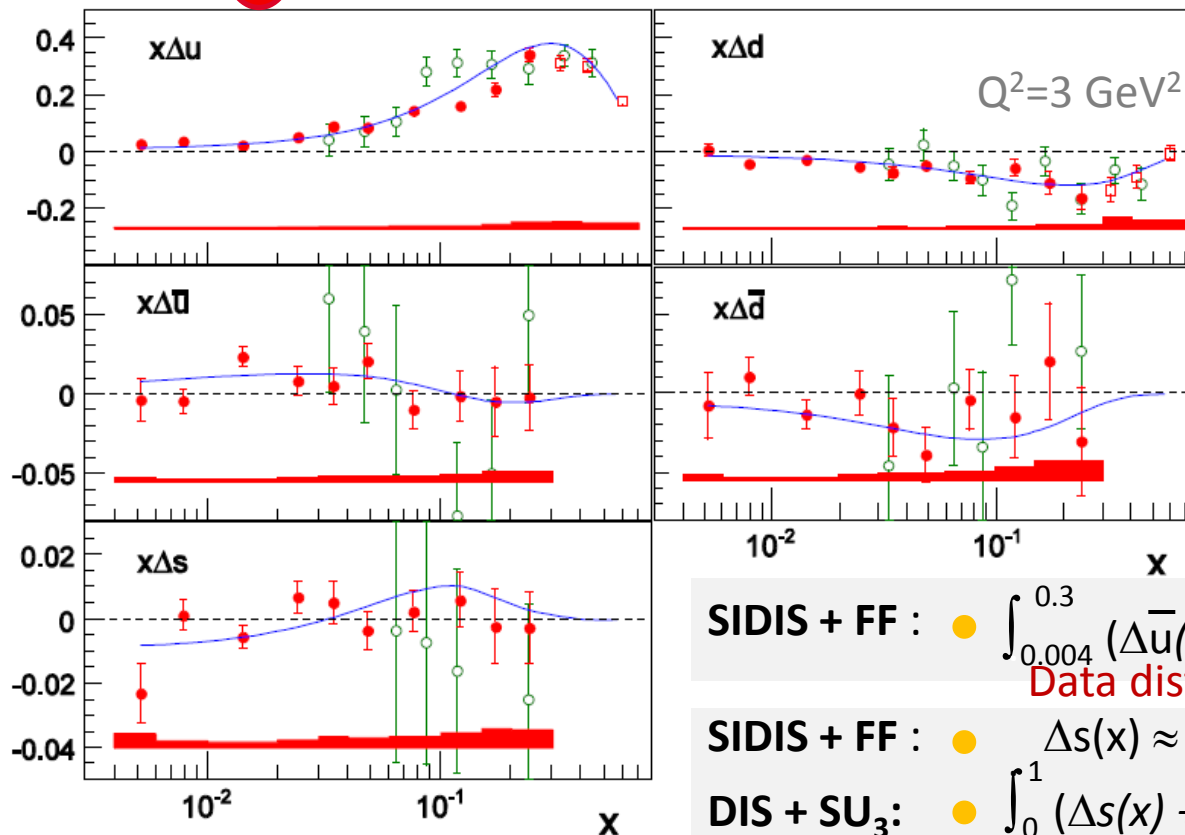
Quark spin from semi-inclusive DIS

SIDIS: $\vec{\ell} p \rightarrow \vec{\ell} h^\pm \chi$



$PDF \otimes$ Fragmentation Function FF

$$A_1^h = \frac{\sum_q e_q^2 \Delta q(x, Q^2) D_q^h(z, Q^2)}{\sum_q e_q^2 q(x, Q^2) D_q^h(z, Q^2)} \quad z = \frac{E_h}{\nu}$$



LO extraction from A_1^h

- **COMPASS μ 160 GeV**
using DSS FF

PLB693(2010)227

- **HERMES e 27 GeV**

PRD71(2005)012003

NLO QCD fit

— **DSSV prediction:** De Florian, Sassot, Stratmann, Volgelsang, PRL101(2008), PRD80(2009)

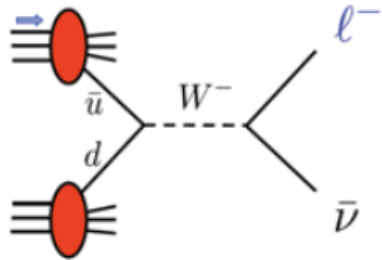
SIDIS + FF : ● $\int_{0.004}^{0.3} (\Delta \bar{u}(x) - \Delta \bar{d}(x)) dx = 0.06 \pm 0.04 \pm 0.02$
 Data disfavor a large unsymmetric sea

SIDIS + FF : ● $\Delta s(x) \approx 0$ in the range $x > 0.004$

DIS + SU_3 : ● $\int_0^1 (\Delta s(x) + \Delta \bar{s}(x)) dx = -0.08 \pm 0.01 \pm 0.02$?

→ a precise determination of FF @ COMPASS

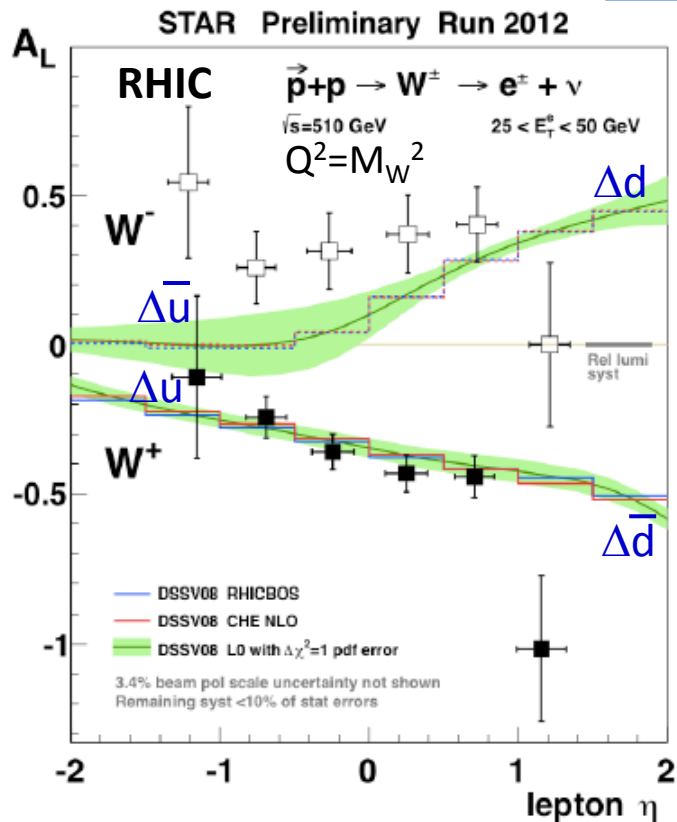
Sea quark spin from W production in $\vec{p} p$



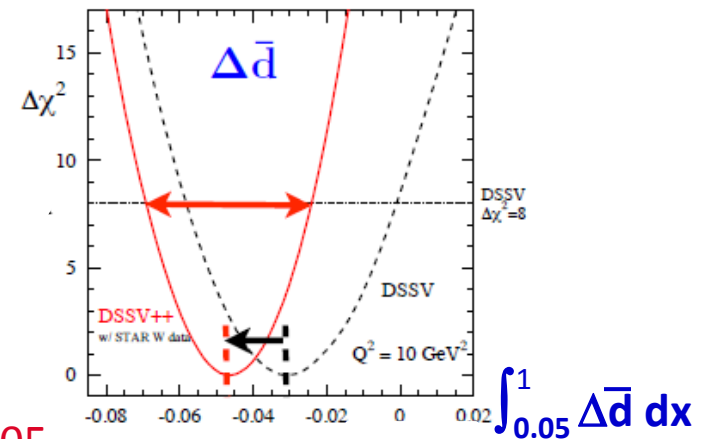
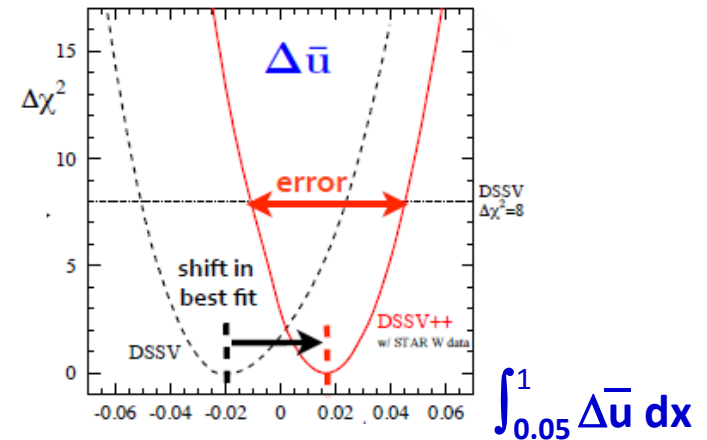
$$\vec{p} + p \rightarrow W^\pm + X \rightarrow l^\pm + X$$

Measure of the parity –violating single spin asymmetry

$$A_L^{W^-} \approx - \frac{\Delta d(x_1)\bar{u}(x_2) - \Delta\bar{u}(x_1)d(x_2)}{d(x_1)\bar{u}(x_2) + \bar{u}(x_1)d(x_2)}$$

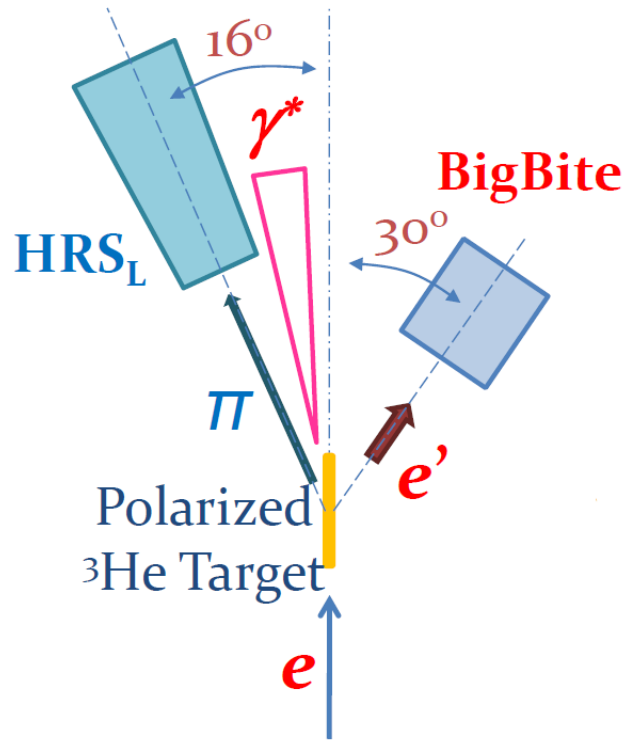


RHIC, arXiv1304.0079 (2013)

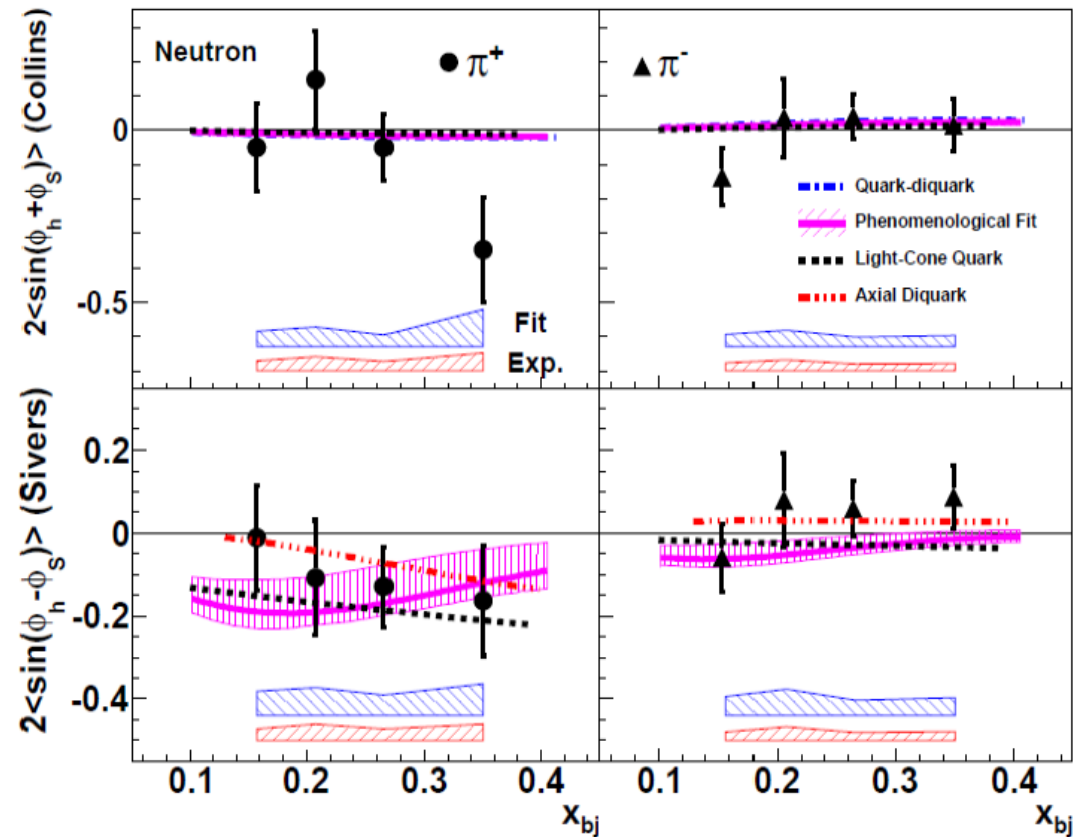


Preference for $\Delta\bar{u} > \Delta\bar{d}$ in the range $x > 0.05$

Collins and Sivers asymmetries on the neutron at Jlab

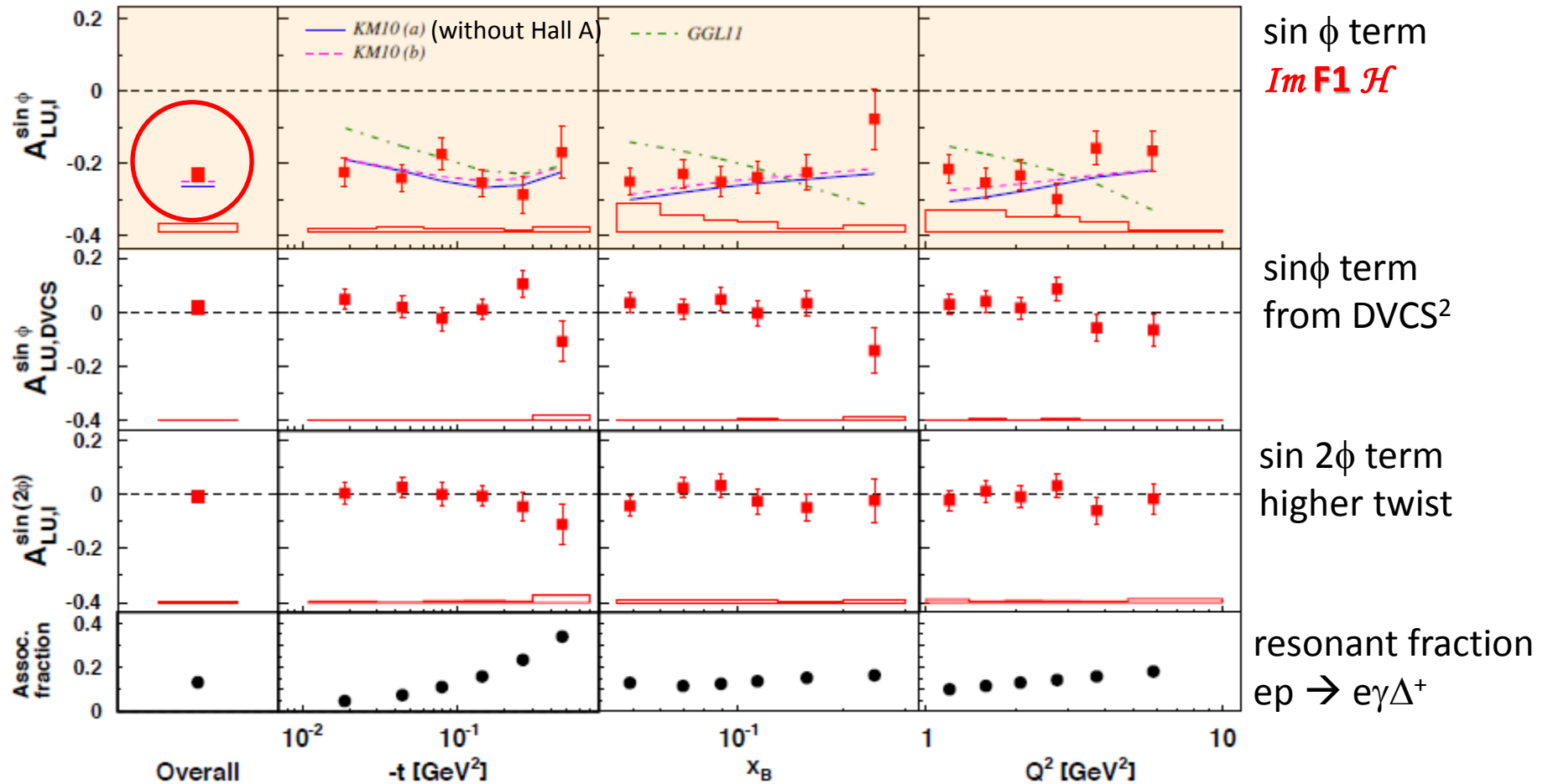


Qian et al., PRL107 (2011)



Beam Spin Asymmetry with HERMES

A. Airapetian et al, JHEP 07 (2012) 032



KM: *Kumerički and Müller, Nucl. Phys. B841 (2010)*

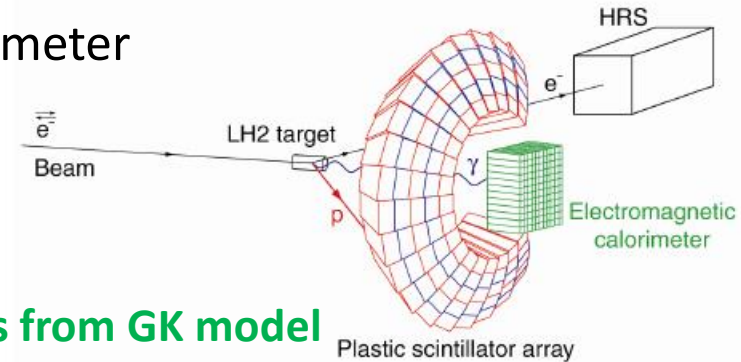
GHL11: *G. Goldstein, J. Hernandez and S. Liuti, Phys. Rev. D84 (2011)*

Beam Spin Diff and Sum – Jlab HallA

E00-110 pioneer experiment with magnetic spectrometer

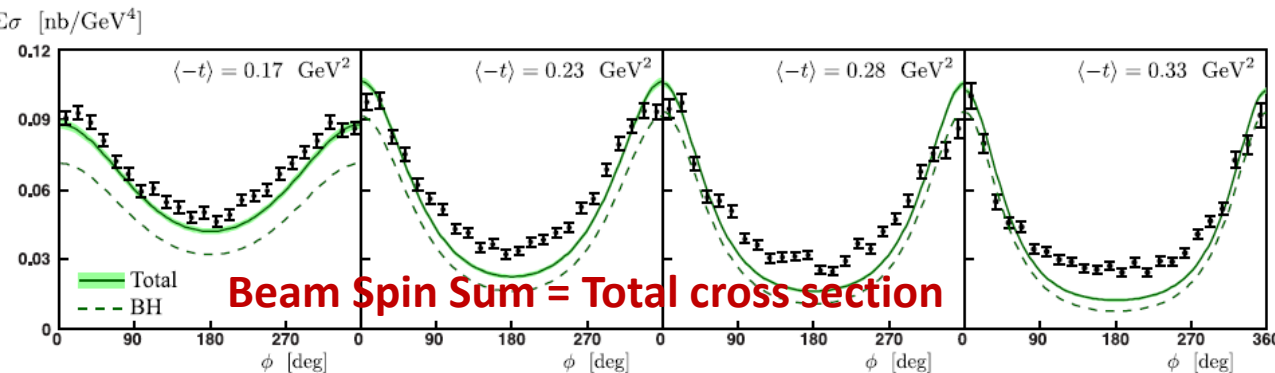
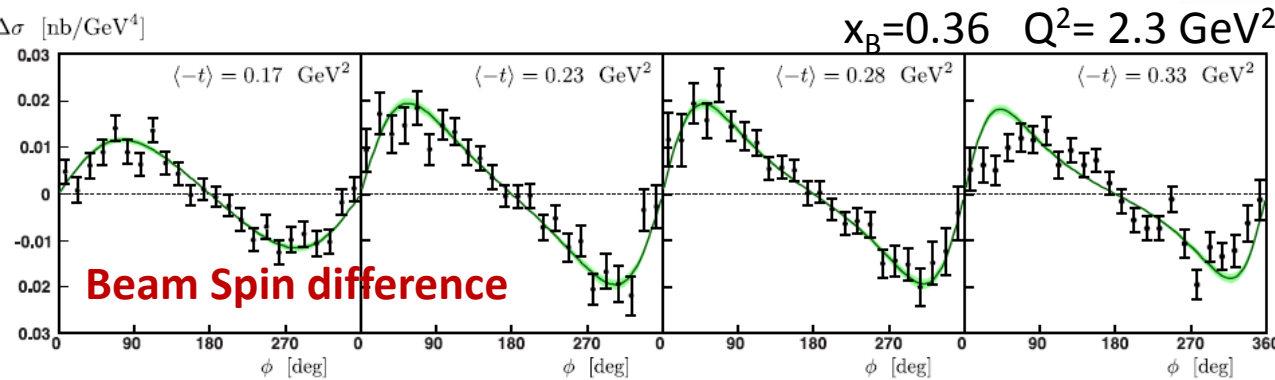
3 measurements: $x_B=0.36$ $Q^2= 1.5, 1.9, 2.3$ GeV²

$$\vec{e} p \rightarrow e \gamma p$$



Data: Munoz et al. PRL97, 262002 (2006)

Model: Kroll, Moutarde, Sabatié, EPJC73 (2013) with GPDs from GK model



News:

- Re-analysis of the data (MC, RC, normalisation/DIS)
- 2010: run E07-007 Rosenbluth-like DVCS²/Interpolation
- 2014: HallA with 11 GeV
- 2018: HallC with 11 GeV

Do we understand Hall A data?

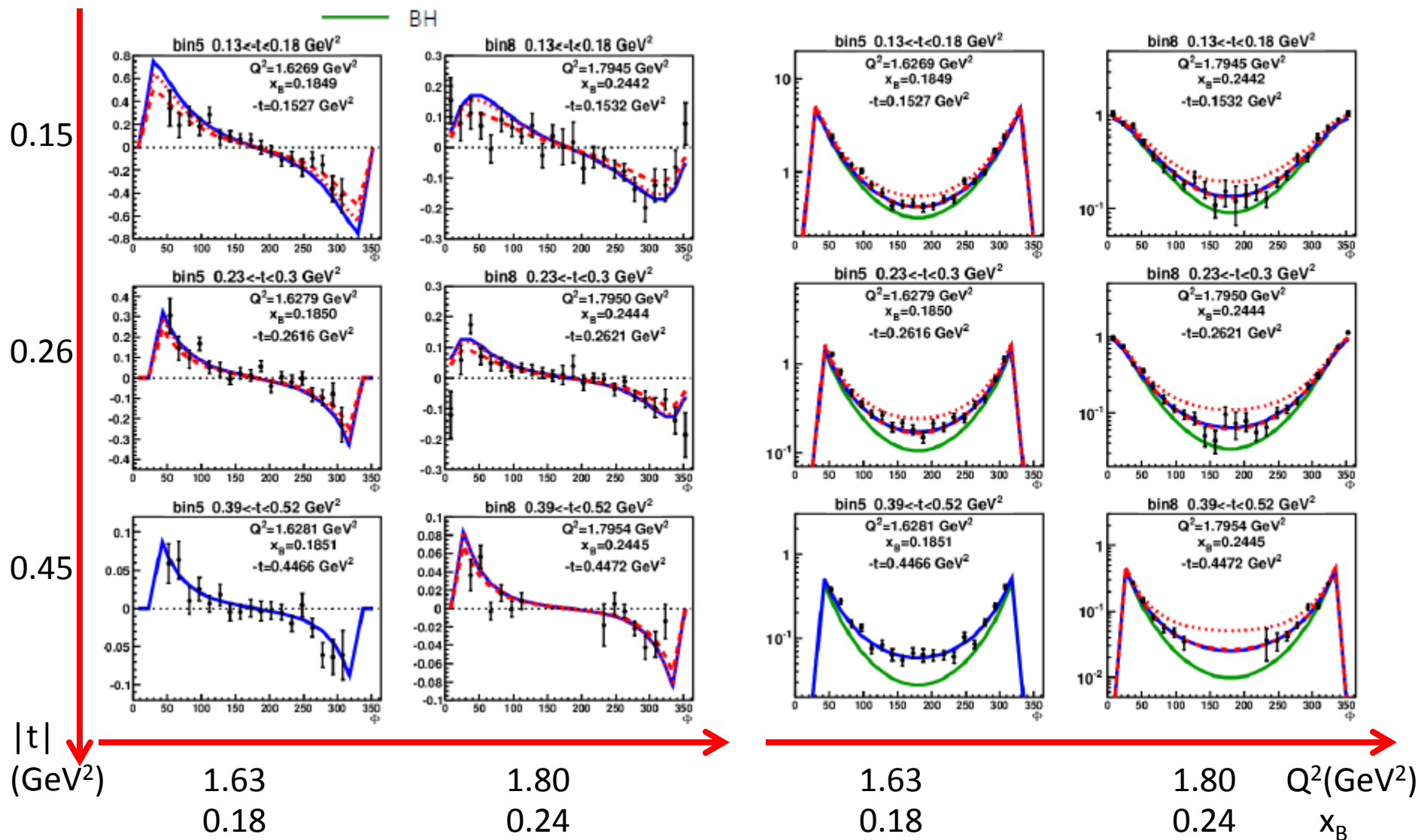
Beam Spin Diff and Sum – Jlab CLAS

PRELIMINARY

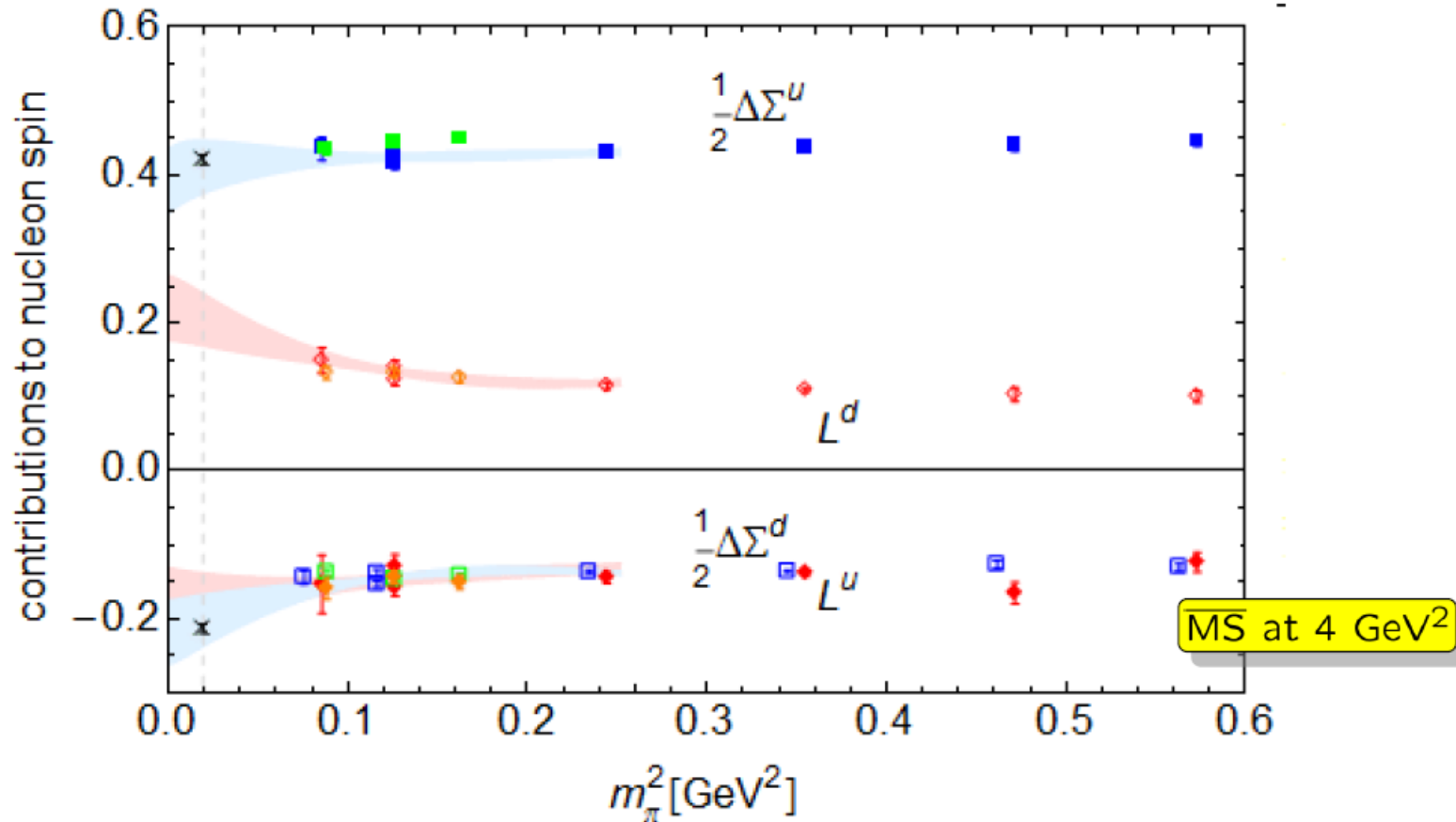
- VGG
- KM10a
- ⋯ KM10b
- BH

VGG: Guidal, Polyakov, Radyushkin, Vanderhaeghen, PRD72(2005)

KM10ab (fit) : Kumericki, Müller, Nucl.Phys. B841 1 (2010)



Spin prediction in Lattice Calculations



$$J^u \approx 0.236 \pm 0.006 \approx 48\% \text{ of } 1/2$$

$$J^d \approx 0.002 \pm 0.004$$

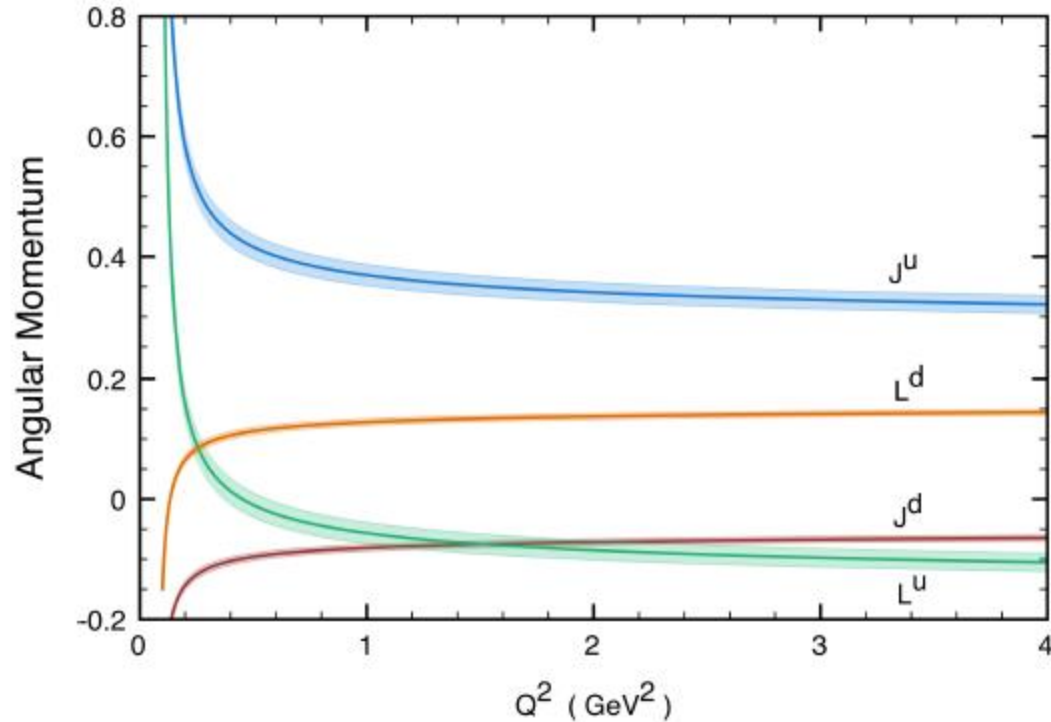
$$L^d \approx -L^u \approx 0.185 \pm 0.06 \approx 36\% \text{ of } 1/2$$

$$L^{u+d} \approx 0.030 \pm 0.012 \approx 6\% \text{ of } 1/2$$

pioneering lattice calculations by Gadiyak, Ji and Jung in 2001

$$\kappa^{u+d} = 3\kappa^{p+n} = -0.36$$

Spin prediction in Cloudy Bag Model

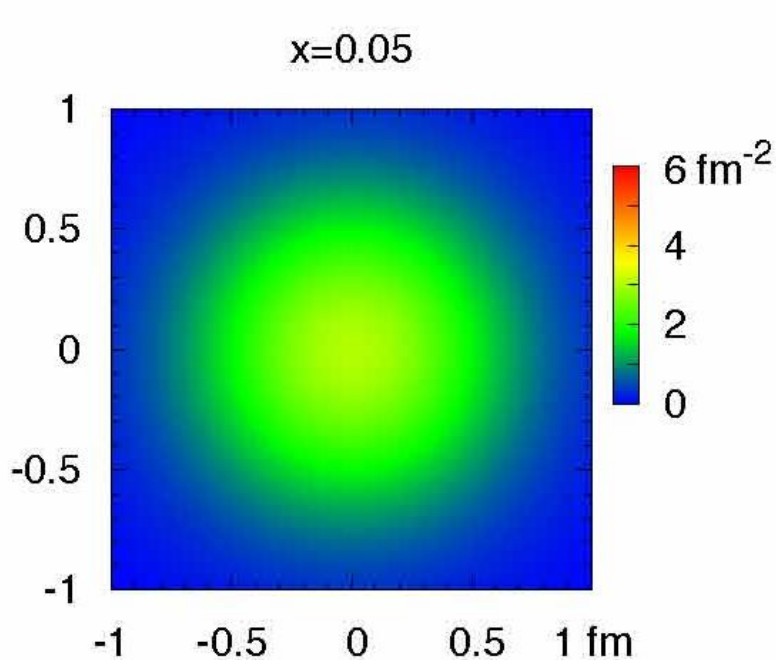


Calculation in NLO QCD evolution - Cloudy bag model
Thomas et al., Int. J. Mod. Phys A25 (2010)

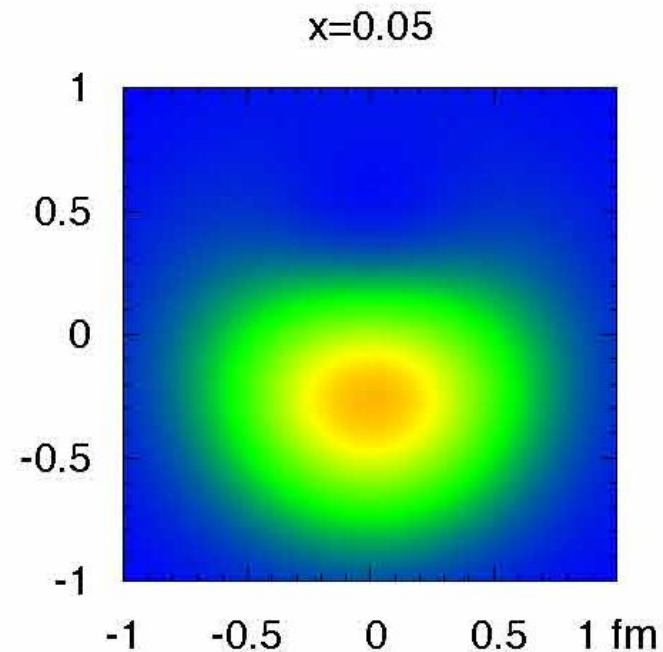
Spin prediction in GPD Model

evaluate parton angular momenta from Ji's sum rule

$$J^u = 0.25 \pm 0.03 \quad J^d = 0.02 \pm 0.03 \quad J^s = 0.02 \pm 0.03 \quad J^g = 0.21 \pm 0.06$$



unpolarized



polarized proton