

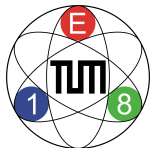
The virtue of precision spectroscopy :
A **new axial-vector meson**
and
The structure of the **$(\pi\pi)$ S-wave-isobar**

Stephan Paul

TUM

on behalf of the COMPASS Collaboration

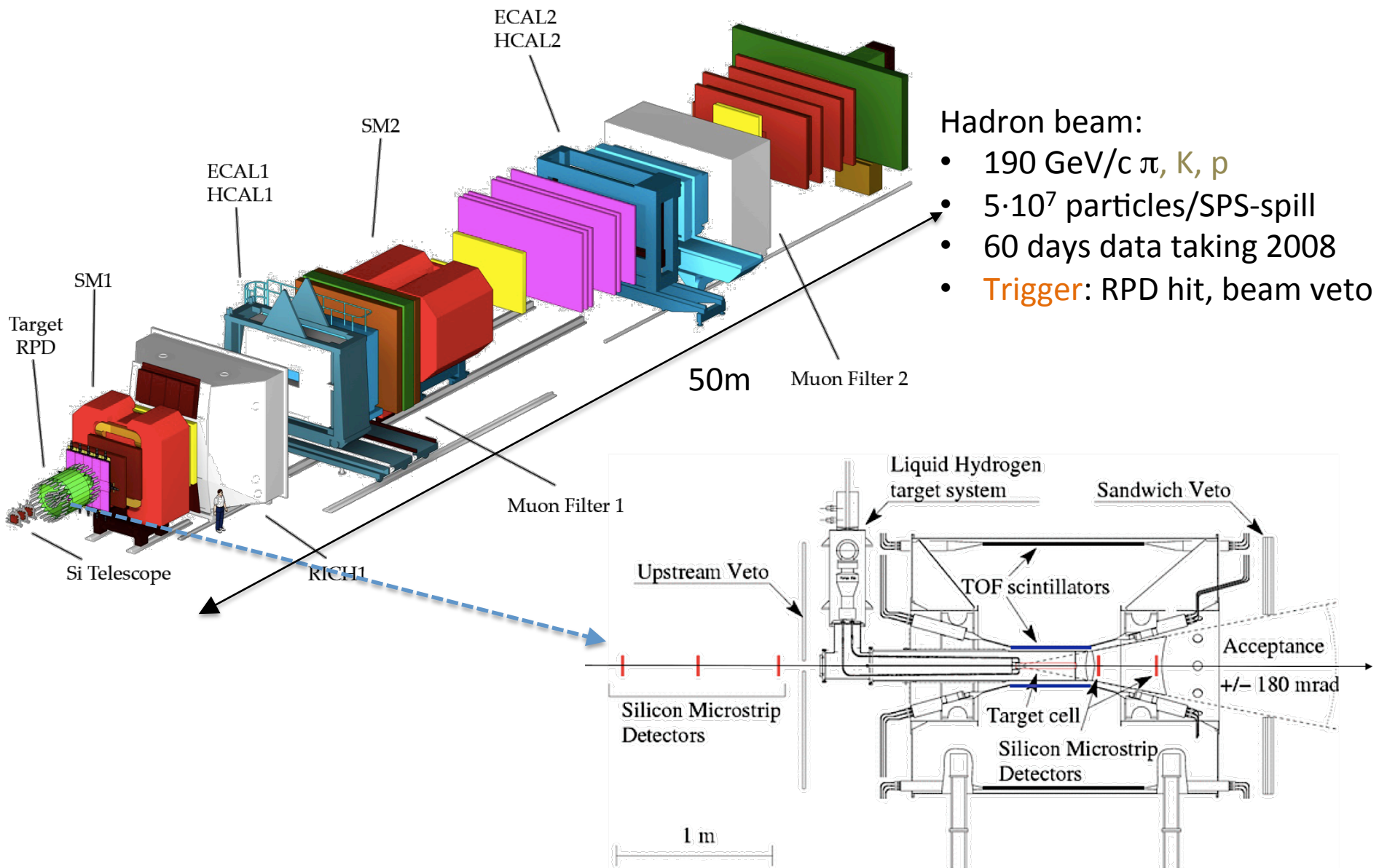




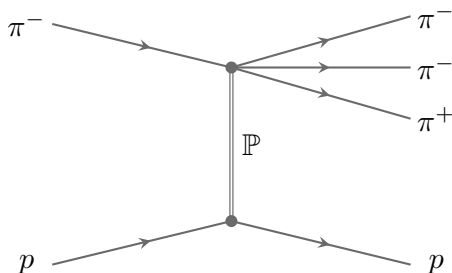
Today's presentation



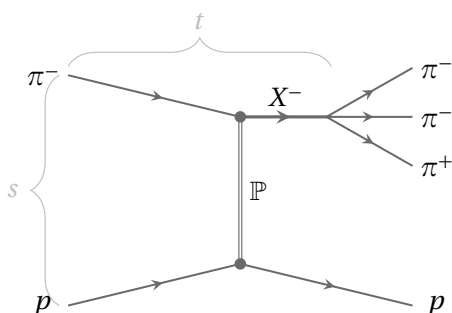
- **Concentrate talk** on
 - Data-set
 - mass-independent fit
 - mass-dependent fit
 - results for resonance parameters
 - A **new axial vector meson: $a_1(1420)$**
 - $\pi\pi$ S-wave extraction
 - results for 0^{-+} , 1^{++} , 2^{-+}
 - Role of $f_0(980)$
 - Conclusions



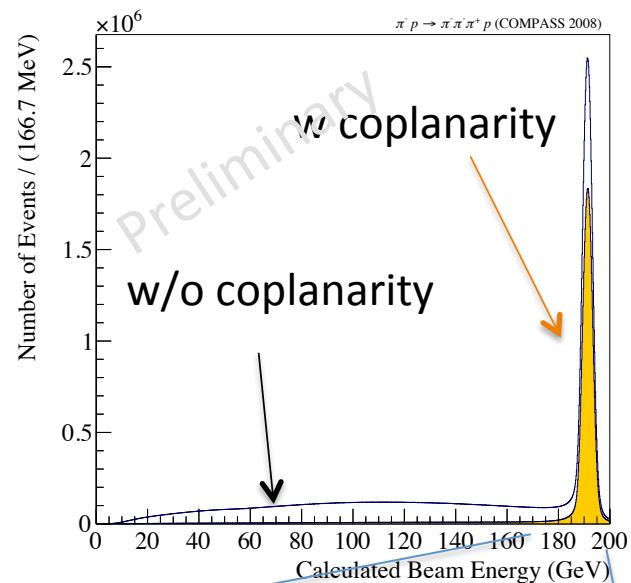
generic process



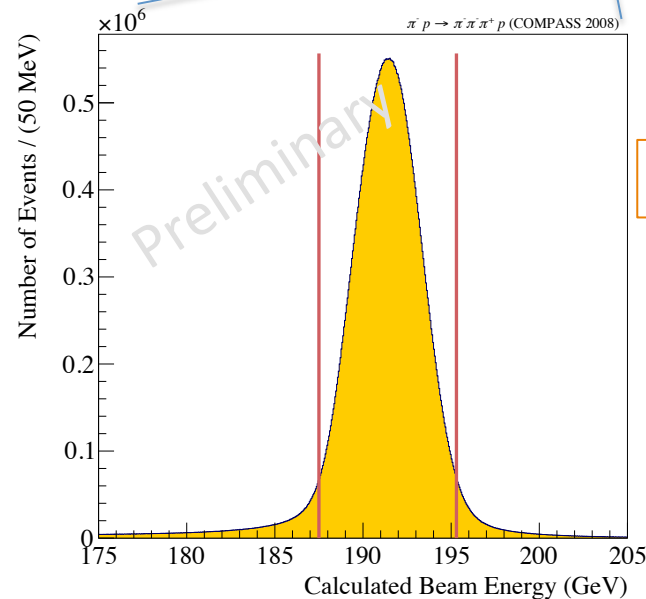
what we are after



exclusive reaction



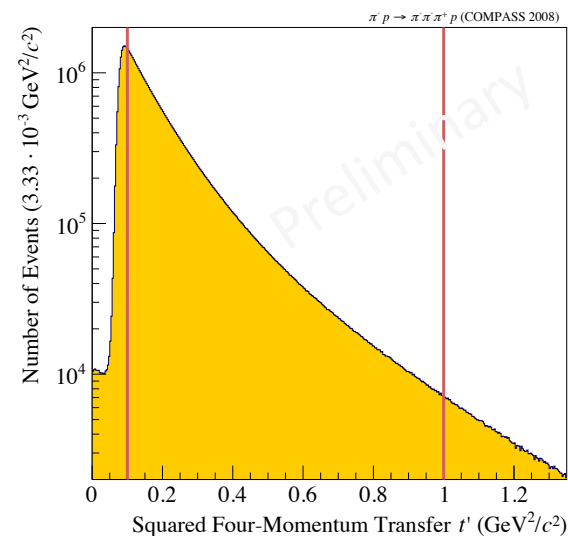
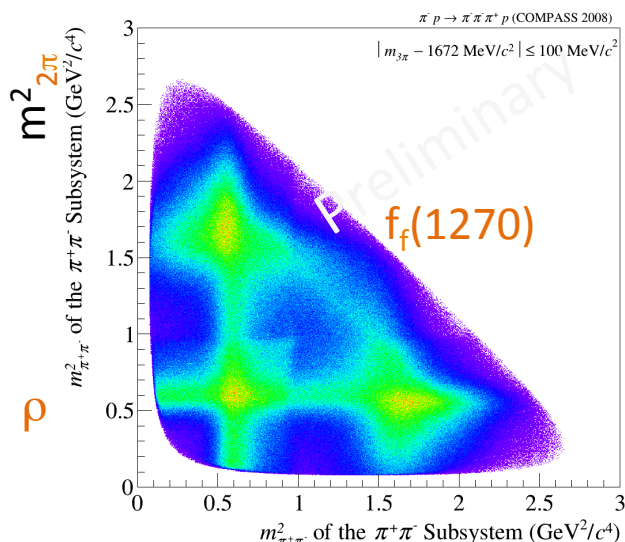
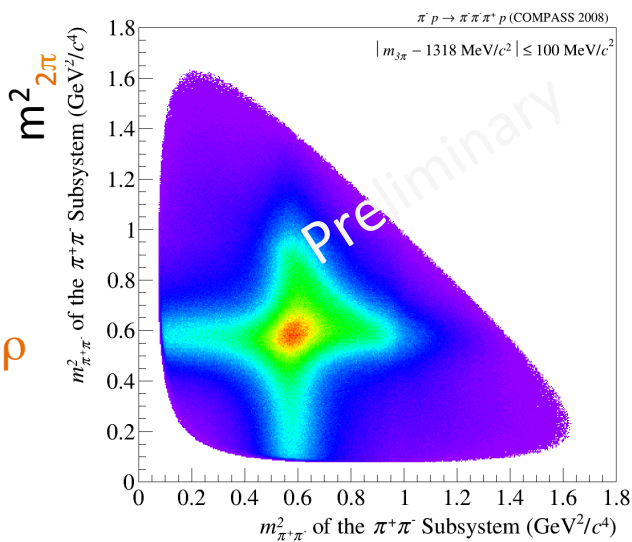
zoom



5 · 10⁷ evts

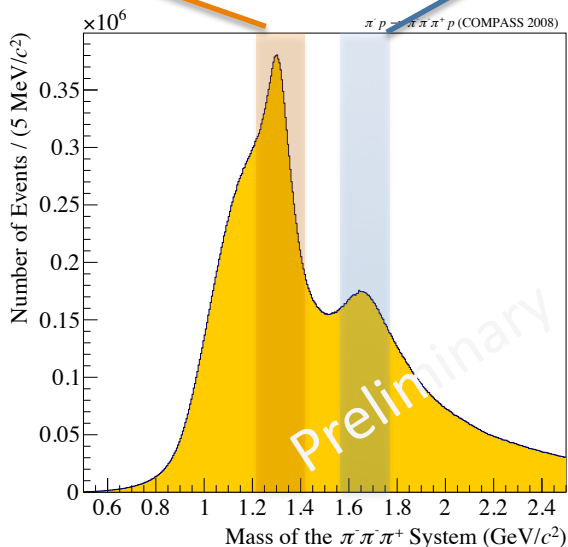
First Impressions

Motivation for Isobar Model

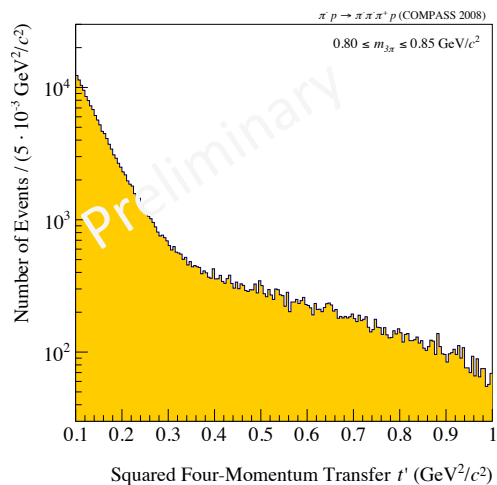
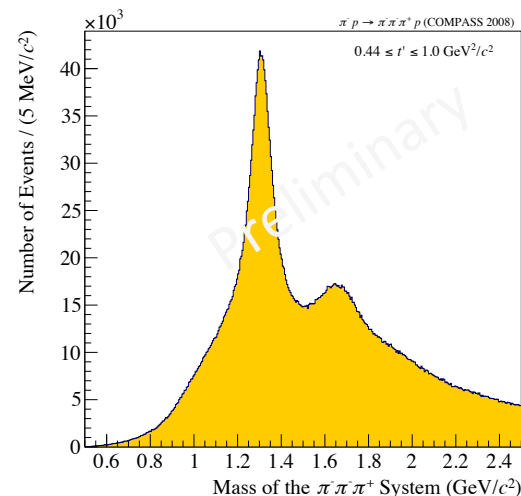
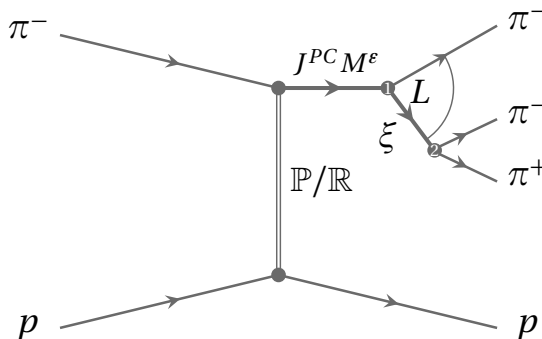
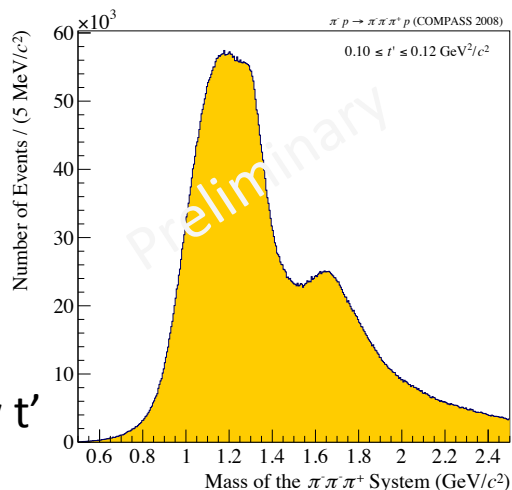


$m^2_{2\pi}$

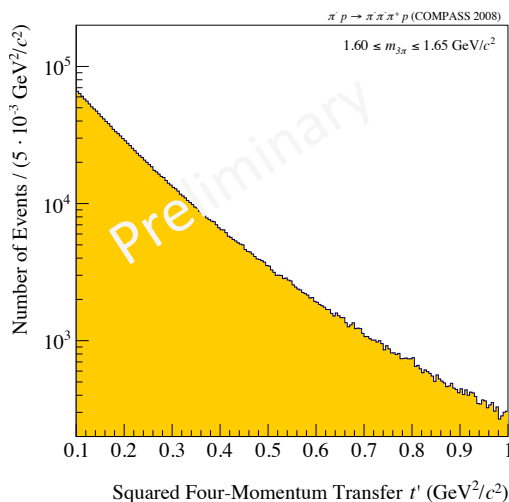
$m^2_{2\pi}$



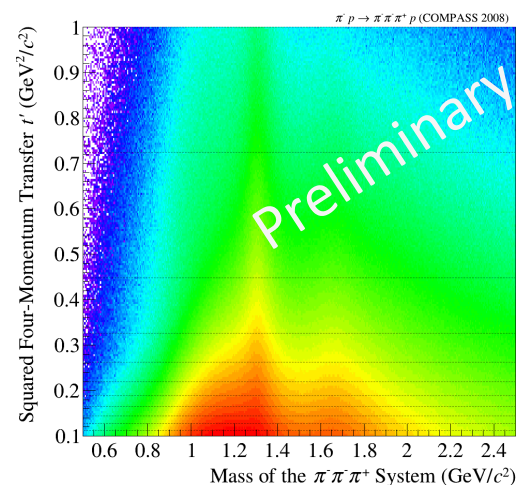
used in analysis



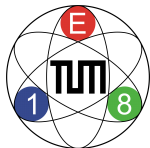
$0.8 < m_{3\pi} < 0.85$



$1.6 < m_{3\pi} < 1.65$



grid of t' used (11 bins)
 $\Delta m: 20 \text{ MeV}/c^2$



Fit Model - Isobars



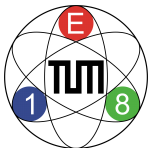
Use 88 waves:

- 80 waves with positive naturality
- 7 waves with negative naturality
- flat wave (garbage collection)

Particle	J^{PC}	Mass [MeV/ c^2]	Width [MeV/ c^2]
$f_0(500)$	0^{++}	400 to 550	400 to 700
$f_0(980)$	0^{++}	990 ± 20	40 to 100
$f_2(1270)$	2^{++}	1275.1 ± 1.2	$185.1^{+2.9}_{-2.4}$
$f_0(1370)$	0^{++}	1200 to 1500	200 to 500
$f_0(1500)$	0^{++}	1505 ± 6	109 ± 7
$f'_2(1525)$	2^{++}	1525 ± 5	73^{+6}_{-5}
$\rho(770)$	1^{--}	775.49 ± 0.34	149.1 ± 0.8
$\rho(1450)$	1^{--}	1465 ± 25	400 ± 60
$\rho_3(1690)$	3^{--}	1688.8 ± 2.1	161 ± 10
$\rho(1700)$	1^{--}	1720 ± 20	250 ± 100

$[\pi\pi]_S$

not used



Waves with Major Resonances



Major waves

$$1^{++} m^+ [\rho] \pi S$$

$$2^{++} m^+ [\rho] \pi D$$

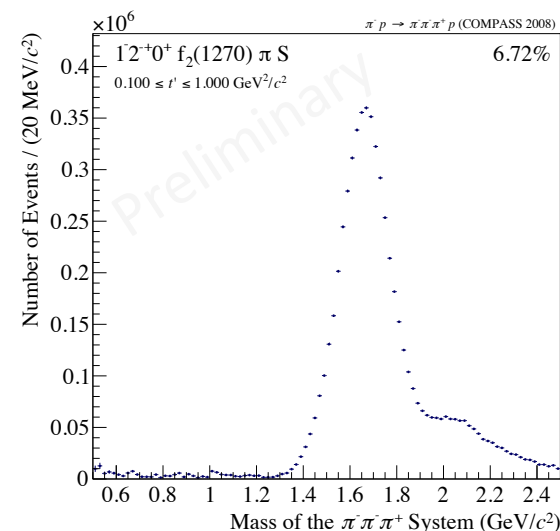
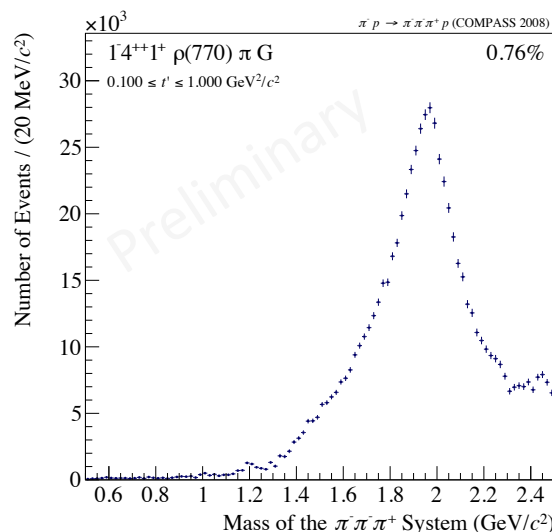
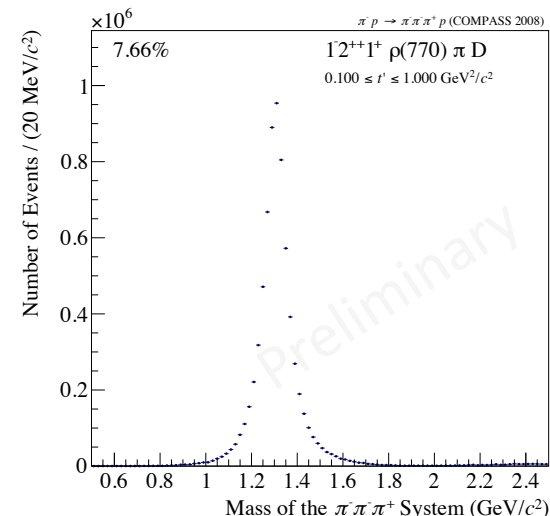
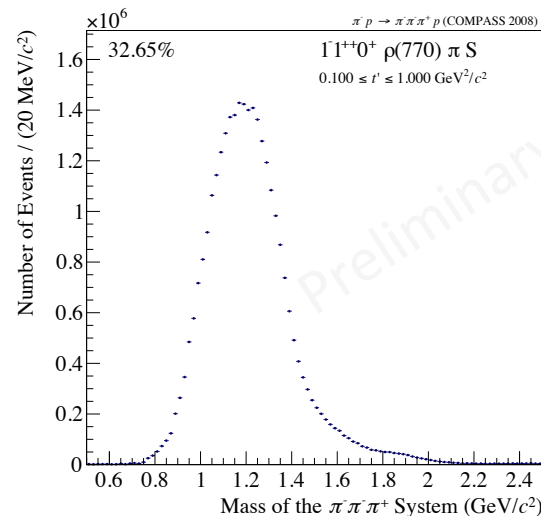
$$2^{-+} m^+ [f_2(1270)] \pi S$$

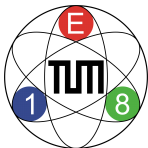
$$4^{++} m^+ [\rho] \pi G$$

$$1^{++} m^+ [f_0(980)] \pi P$$

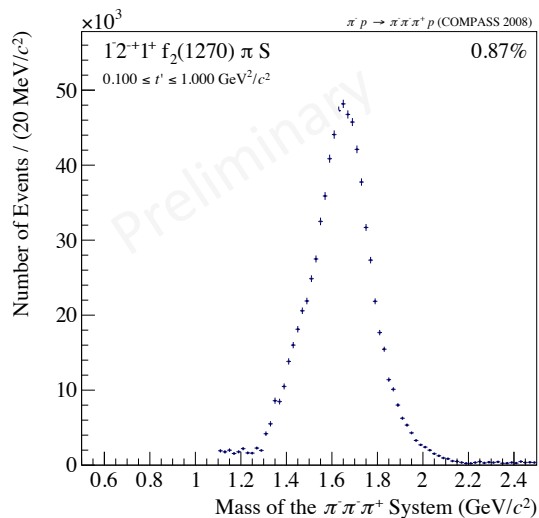
$$0^{-+} m^+ [f_0(980)] \pi S$$

mass independent fits
minimal $m = (0,1)$ waves

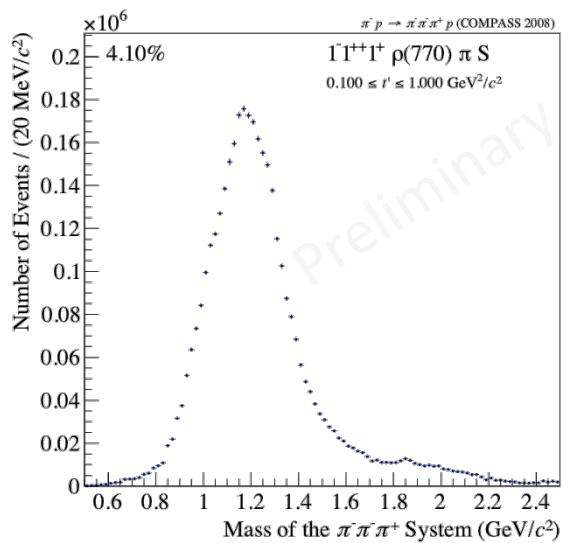


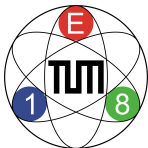


Major Waves $m = 1$



mass independent fits
 $m = 1 = m_{\text{min}} + 1$ waves

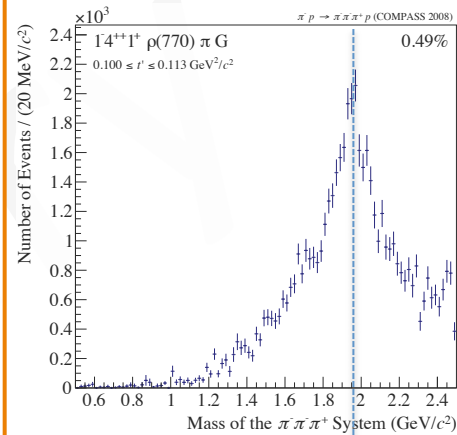
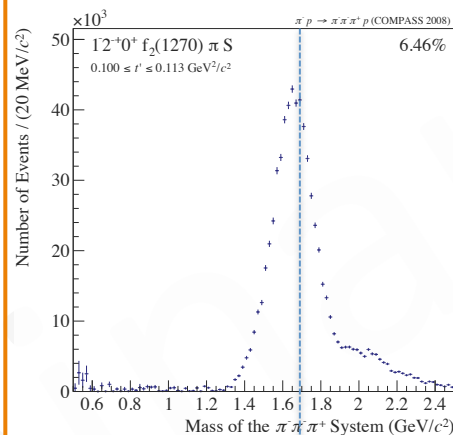
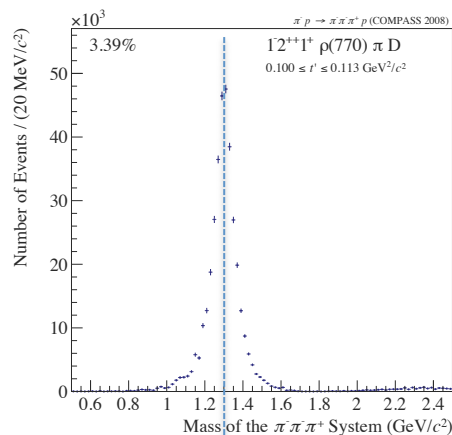
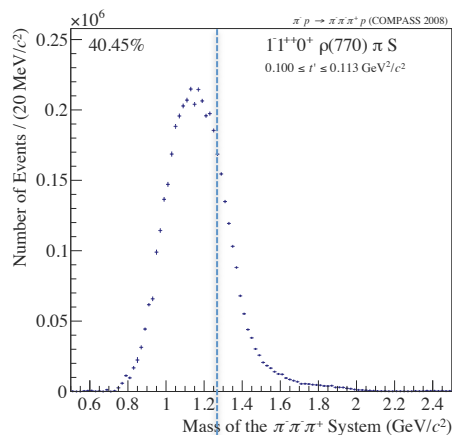




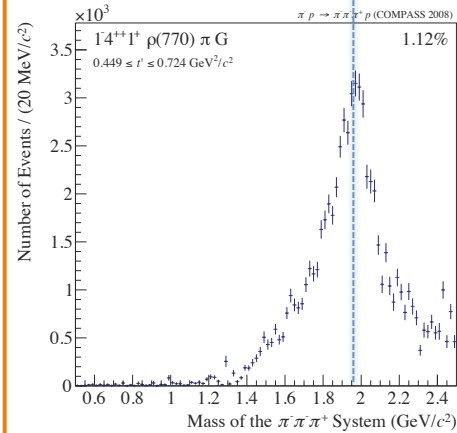
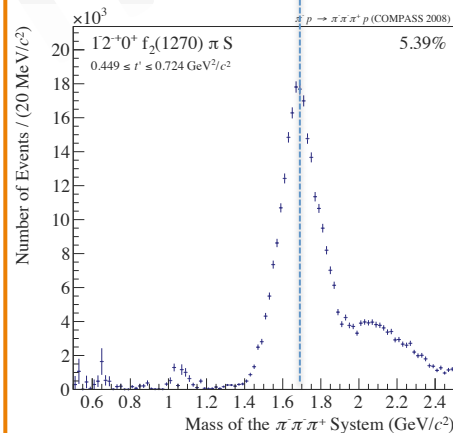
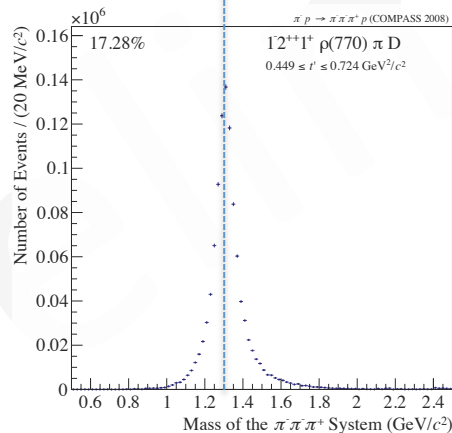
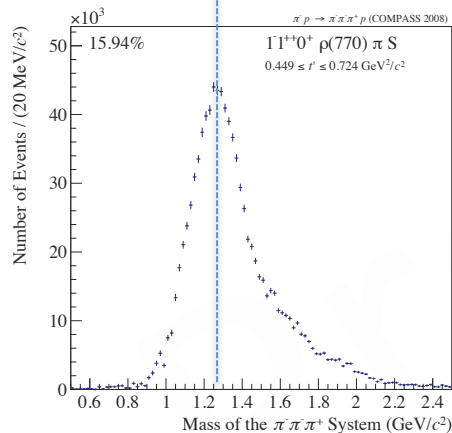
t' dependence of mass distributions



low t'



high t'



$1^{++}0^+ \rho \pi S$

$2^{++}1^+ \rho \pi D$

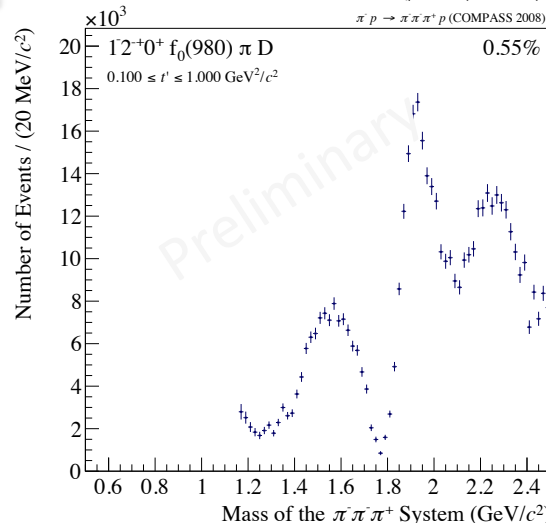
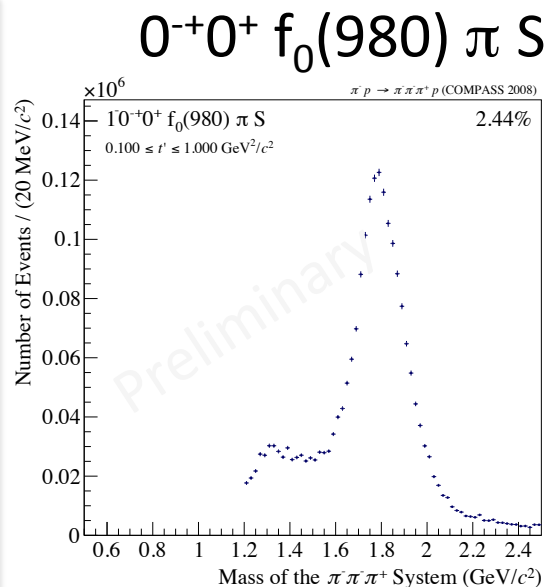
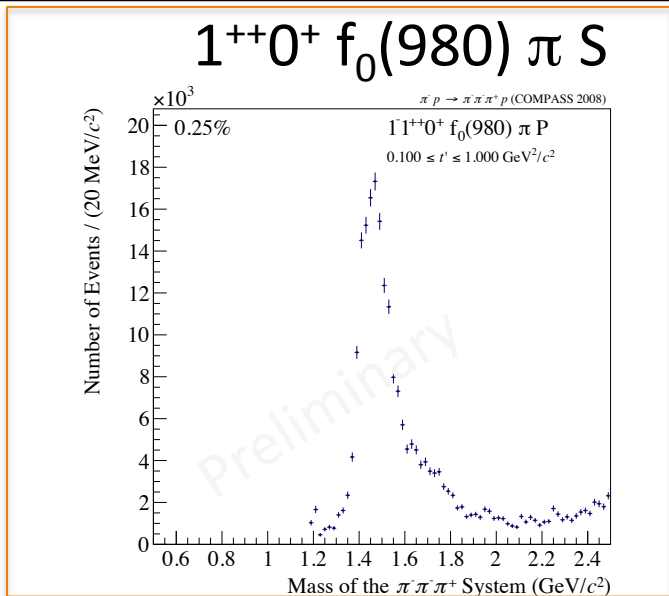
$2^{-}0^+ f_2 \pi S$

$4^{++}1^+ \rho \pi G$

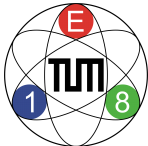
More exotic families



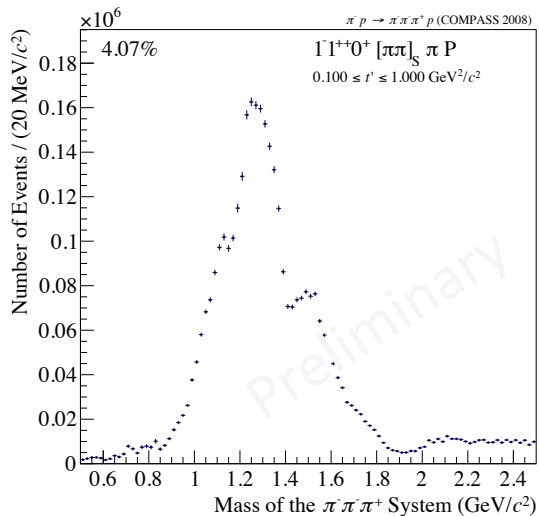
Waves involving $f_0(980)$



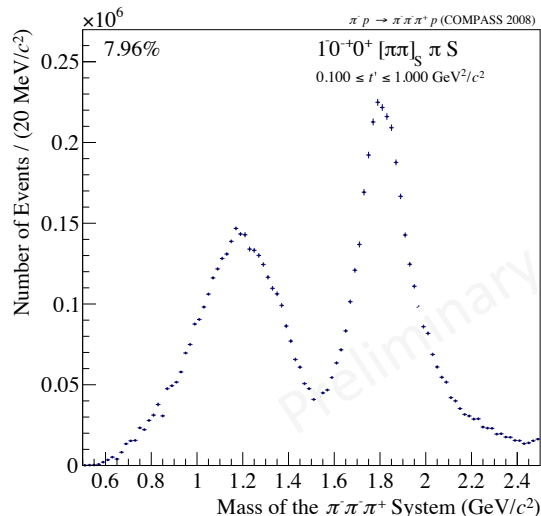
$2^{-+}0^+ f_0(980) \pi D$



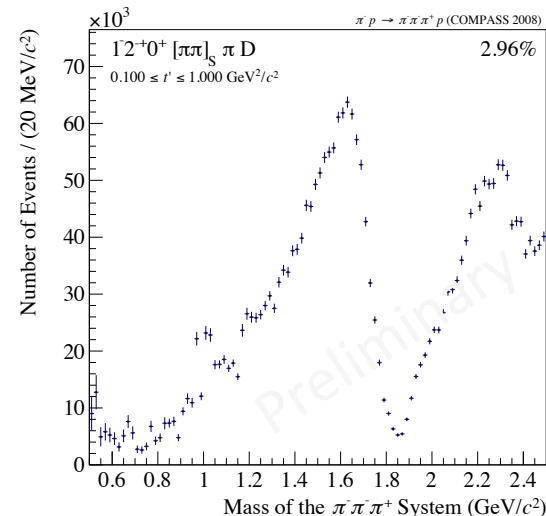
Waves involving $[\pi\pi]_S$



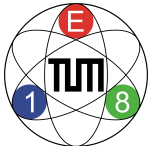
$1^{++}0^+ [\pi\pi]_S \pi P$



$1^+0^+ [\pi\pi]_S \pi S$



$2^{++}0^+ [\pi\pi]_S \pi D$



Mass-dependent fit



Use only lowest $m = 0, 1$ waves (so far)

This work: **6 waves**

+ non resonant term

Model:

$1^{++}1^+ \rho\pi$ S

2 resonances : $a_1(1260)$ and a_1' + non resonant term

$2^{++}0^+ \rho\pi$ D

2 resonances : $a_2(1320)$ and a_2' + non resonant term

$4^{++}1^+ \rho\pi$ G

1 resonance : $a_4(2040)$ + non resonant term

$2^{-+}0^+ f_2 \pi$ S

2 resonances : $\pi_2(1670)$ and π_2' + non resonant term

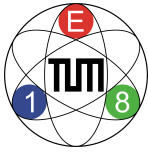
$1^{++}f_0(980) \pi$ P

1 resonance : $a_1(1420)$ + non resonant term

$0^{-+}f_0(980) \pi$ S

1 resonance : $\pi(1800)$ + non resonant term

- 231 mass distributions with 23100 data points
- **352 free parameters**
- systematic studies with 5 and 7 waves performed

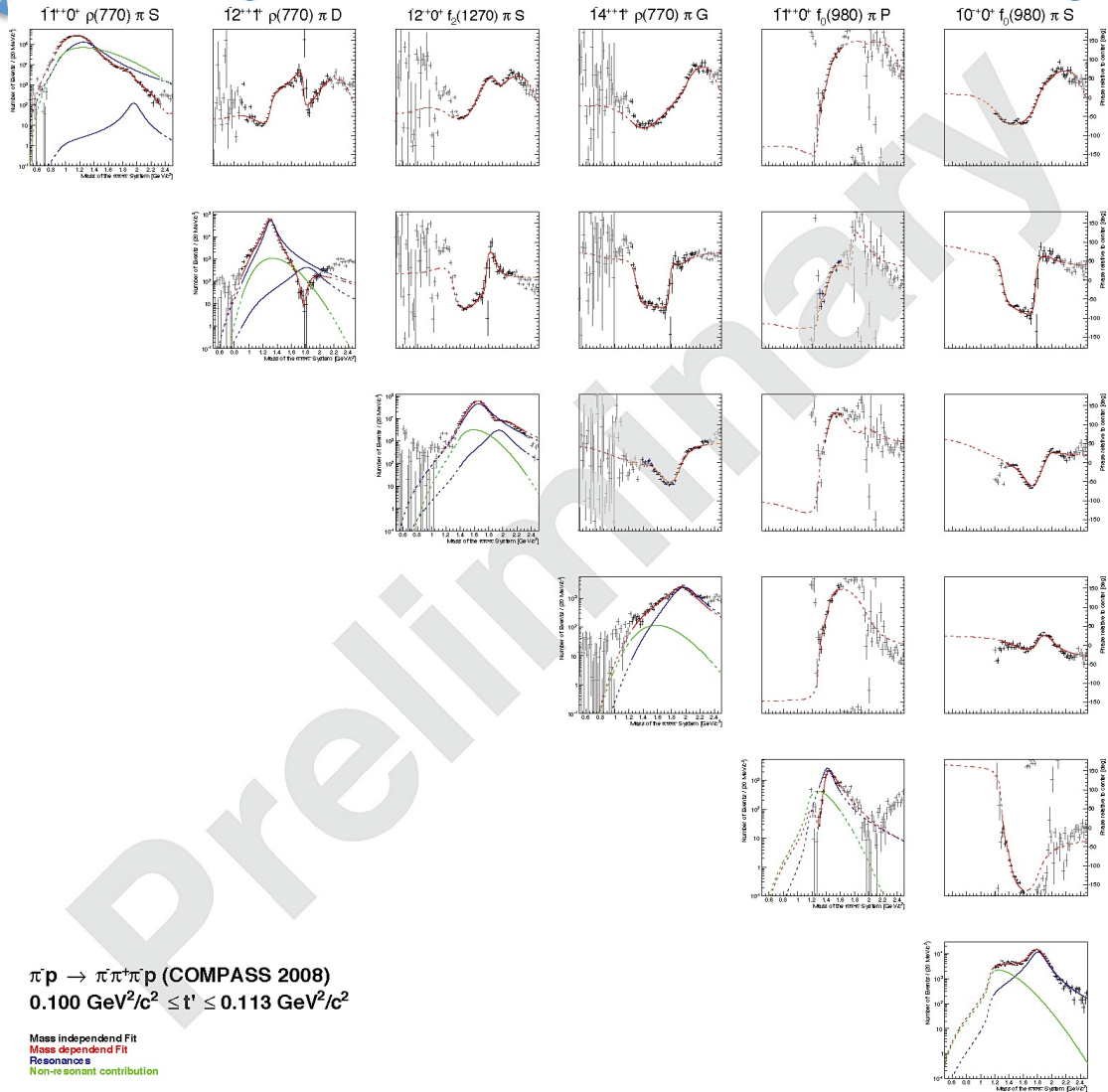


COMPASS Spin-Density Matrix



Reference waves

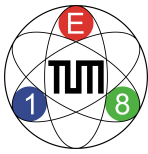
Interferometry



low t' -slice only

$\pi^+p \rightarrow \pi^+\pi^+\pi^-p$ (COMPASS 2008)
 $0.100 \text{ GeV}^2/c^2 \leq t' \leq 0.113 \text{ GeV}^2/c^2$

Mass independent Fit
Mass dependent Fit
Resonance S
Non-resonant contribution

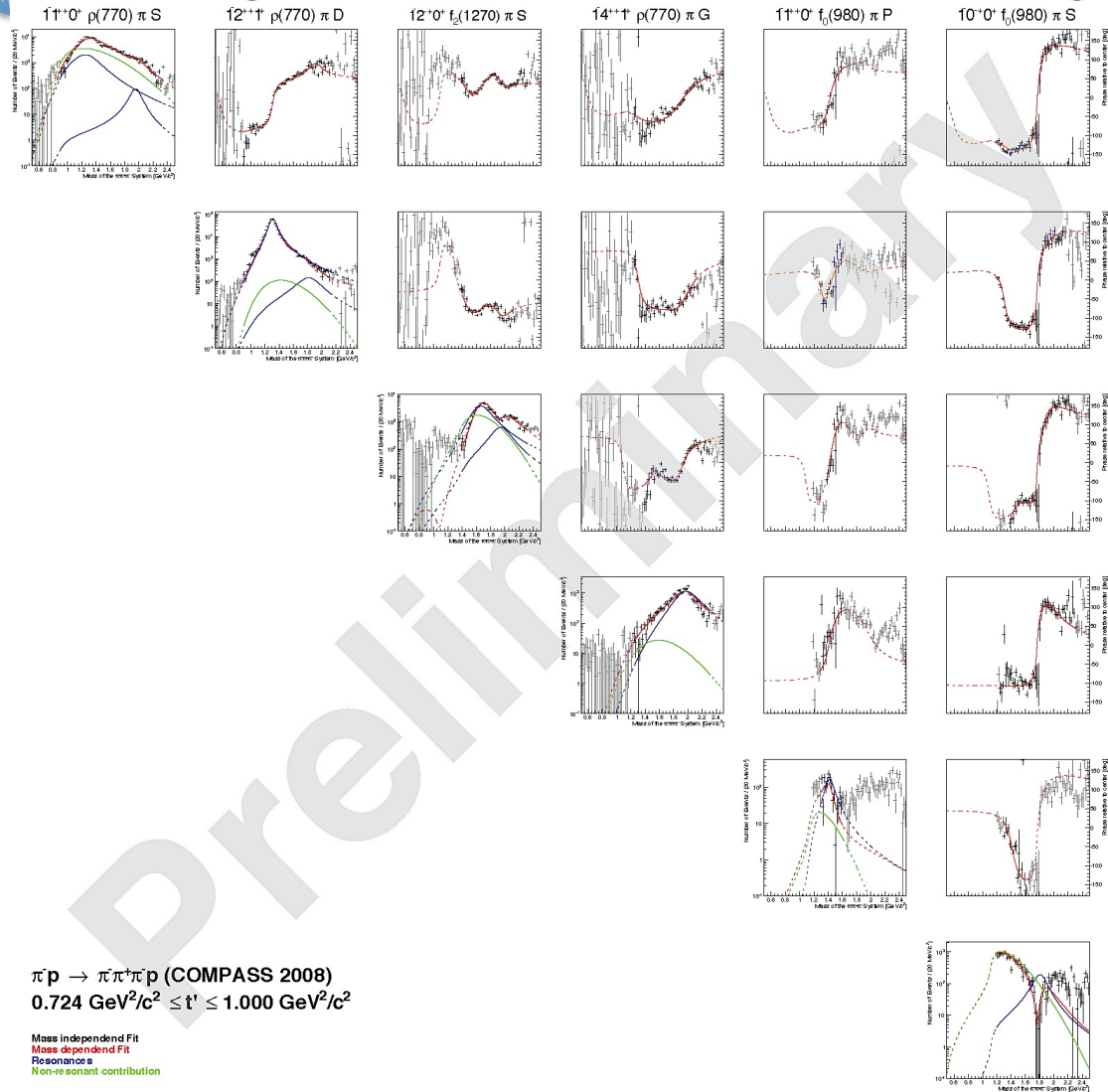


COMPASS Spin-Density Matrix



Reference waves

Interferometry

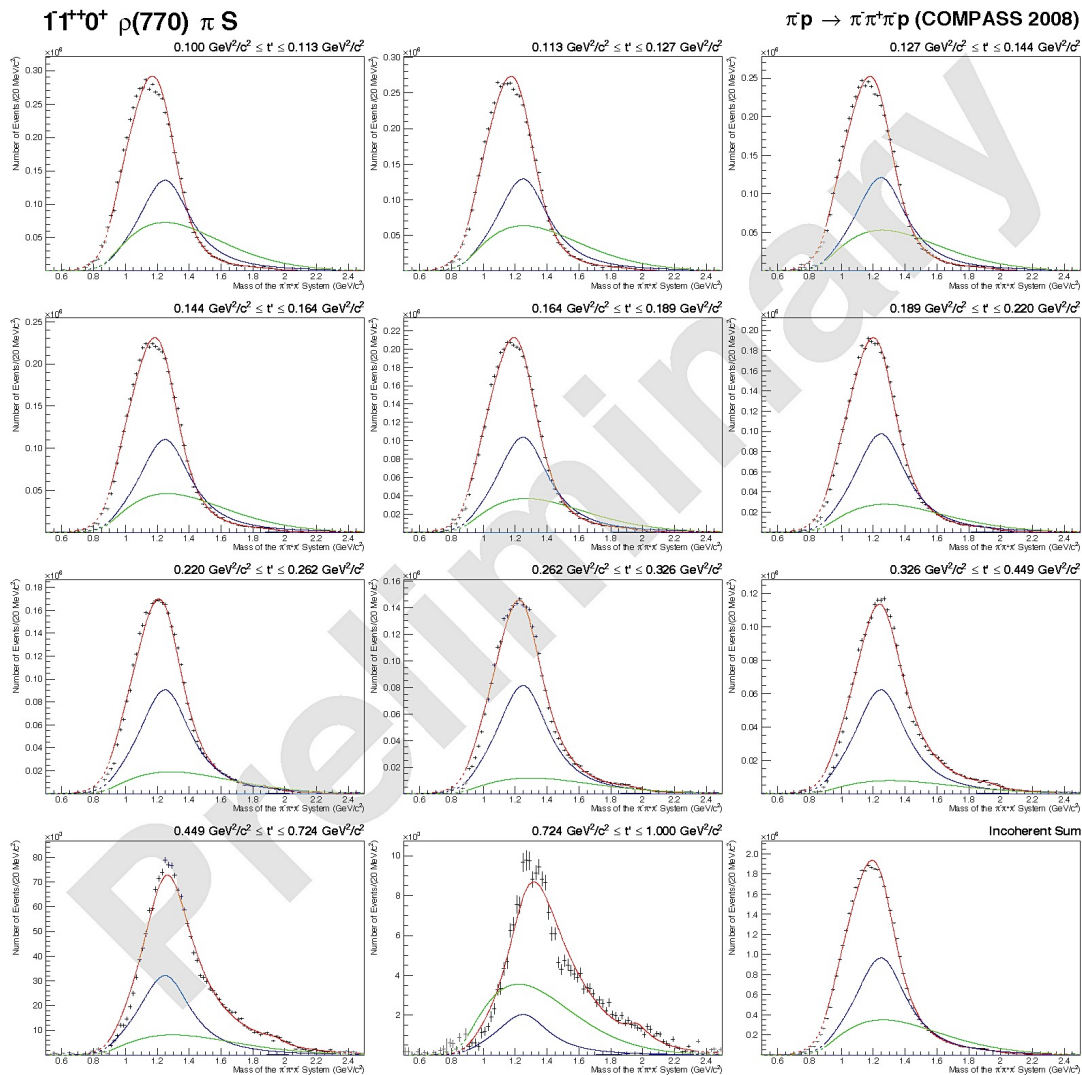


high t' -slice only

$\pi^+p \rightarrow \pi^+\pi^+\pi^-p$ (COMPASS 2008)
 $0.724 \text{ GeV}^2/c^2 \leq t' \leq 1.000 \text{ GeV}^2/c^2$

Mass independent Fit
 Mass dependent Fit
 Resonances S
 Non-resonant contribution

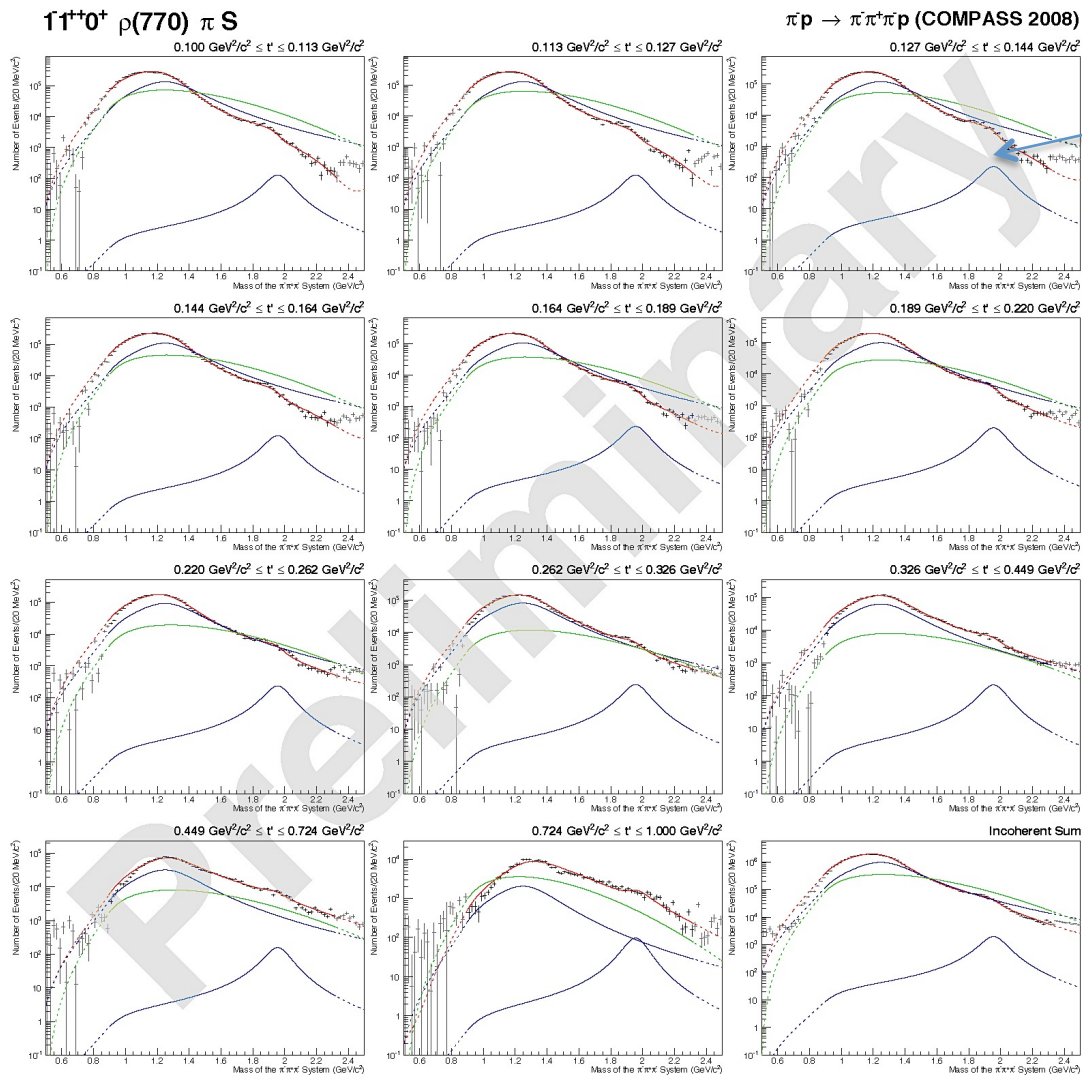
Fit in 11 t-bins



$1^{++}0^+ \rho \pi S$

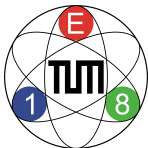
incoherent sum

Fit in 11 t-bins



$1^{++}0^+ \rho \pi S$

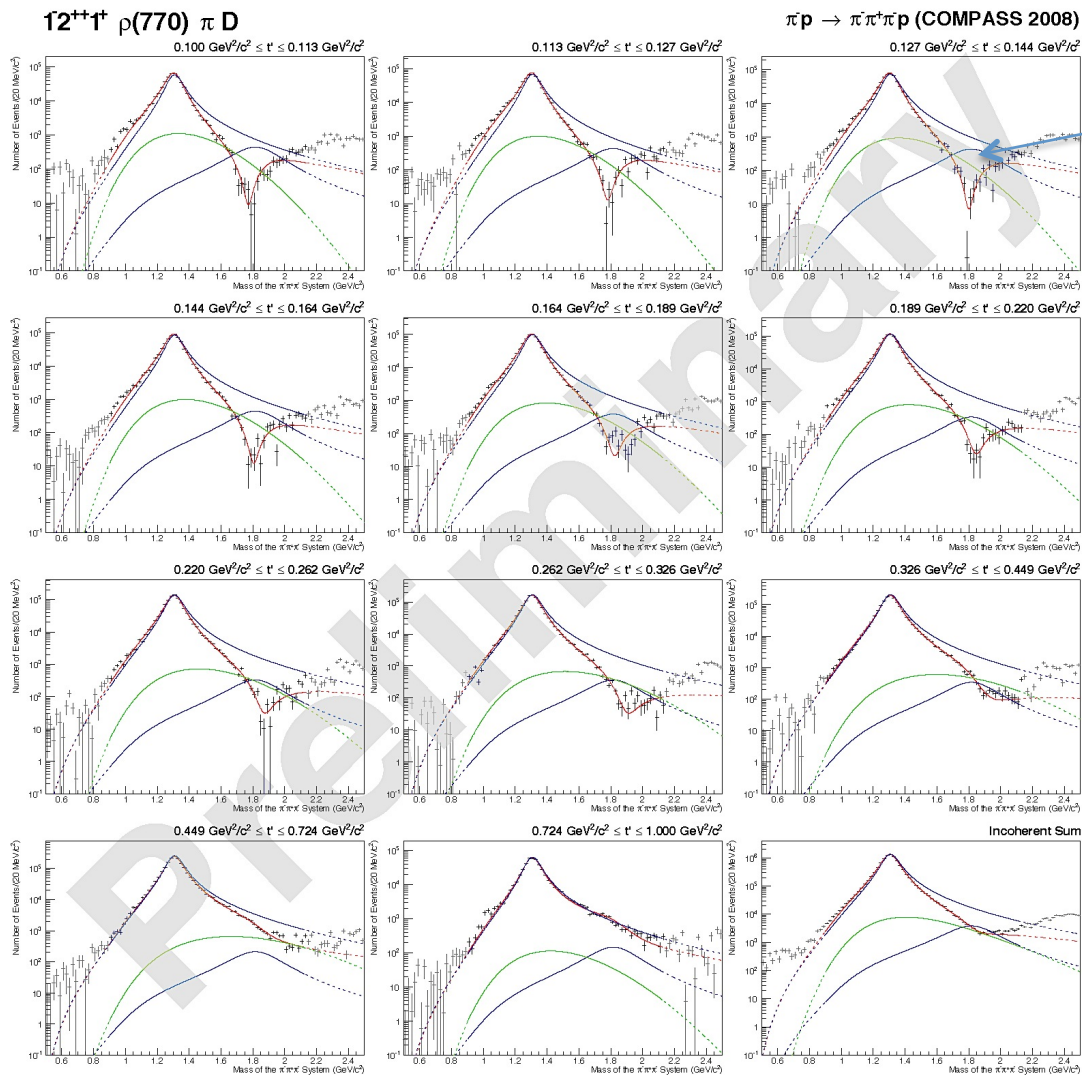
incoherent sum



Mass dependent fits

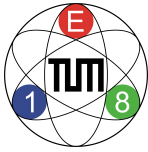


Fit in 11 t-bins



$2^{++}1^+ \rho\pi D$

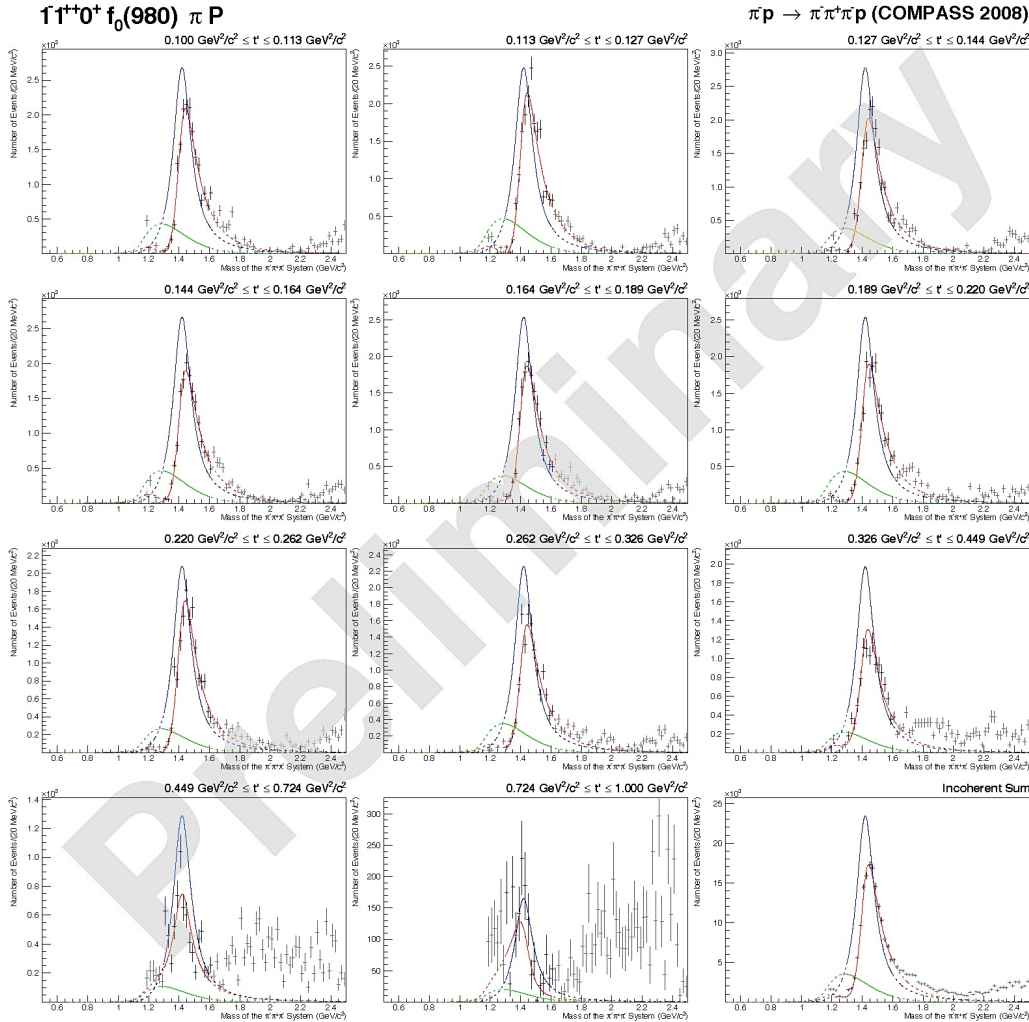
incoherent sum



Mass dependent fits $a_1(1420)$



Fit in 11 t-bins



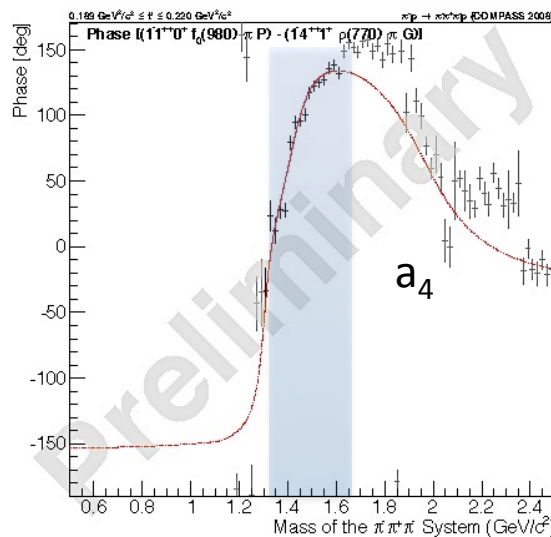
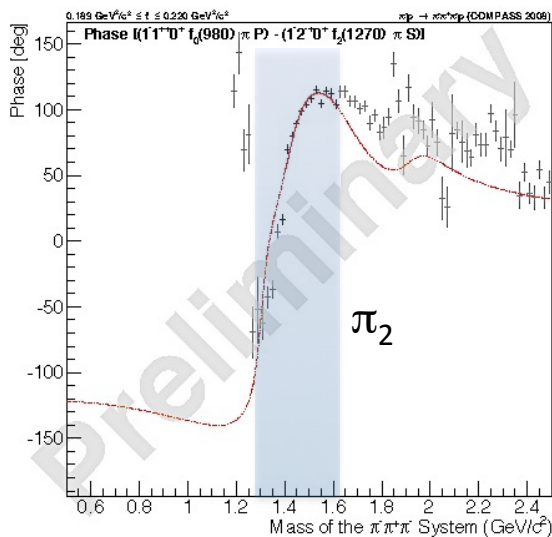
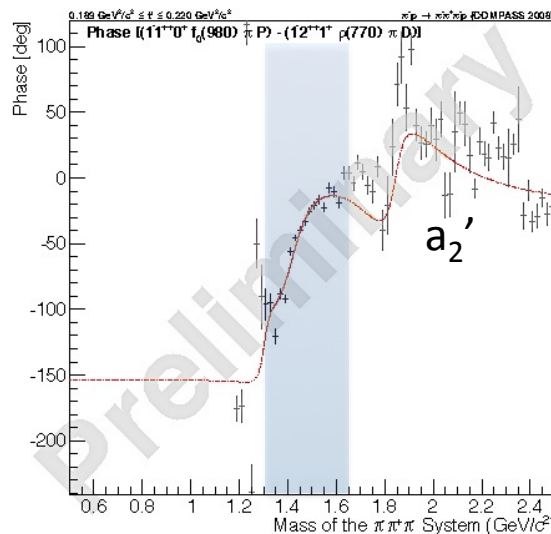
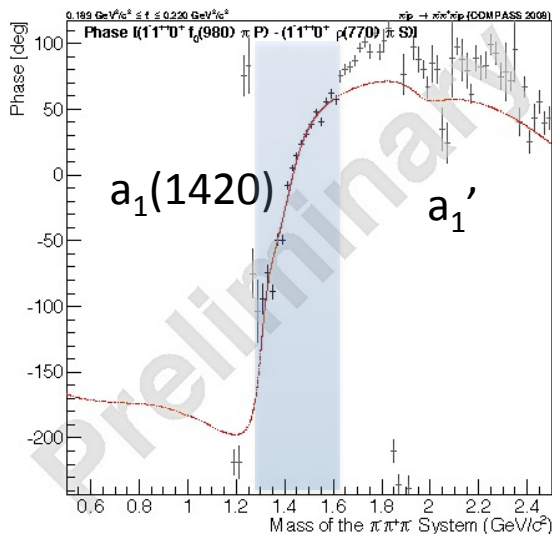
$1^{++}0^+ f_0(980) \pi P$

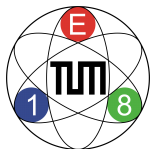
incoherent sum

Phase: $a_1(1420)$

Fit in 11 t-bins: medium t'

fit range



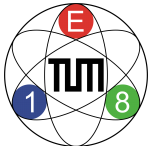


Results of Mass-Dependent Fit



Particle	J^{PC}	Mass Range [MeV/ c^2]	Width Range [MeV/ c^2]		PDG
“Established” states					
$a_1(1260)$	1^{++}	1260-1290	360-420	1230 ± 40	250 to 600
$a_2(1320)$	2^{++}	1312-1315	108-115	$1318.3^{+0.5}_{-0.6}$	107 ± 5
$a_4(2040)$	4^{++}	1928-1959	360-400	1996^{+10}_{-9}	255^{+28}_{-24}
$\pi_2(1670)$	2^{-+}	1635-1663	265-305	1672.2 ± 3.0	260 ± 9
$\pi(1800) \rightarrow f_0(980)\pi$	0^{-+}	1790-1807	212-230		
$\pi_2(1880)$	2^{-+}	1900-1990	210-390	1895 ± 16	235 ± 34
States not in PDG summary table					
$a_1(1420)$	1^{++}	1412-1422	130-150		
$a_1(1930)$	1^{++}	1920-2000	155-255	1930^{+30}_{-70}	155 ± 45
$a_2(1950)$	2^{++}	1740-1890	300-555	1950^{+30}_{-70}	180^{+30}_{-70}

Compass is a bit on the low side

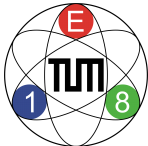


$(\pi\pi)_S$ -wave

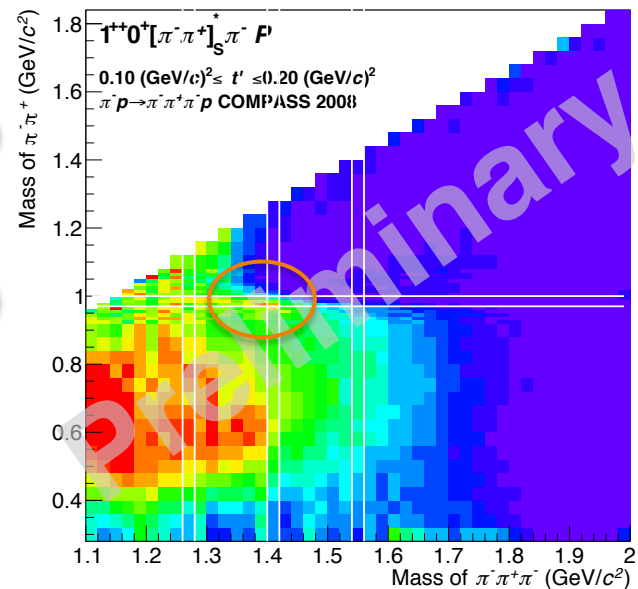
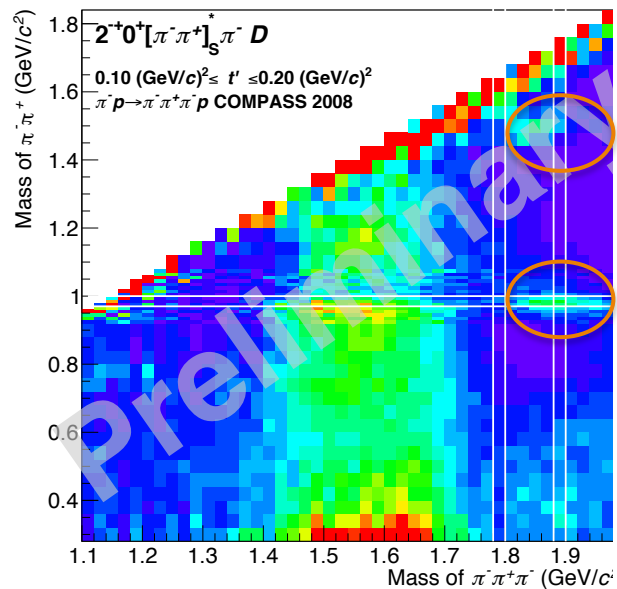
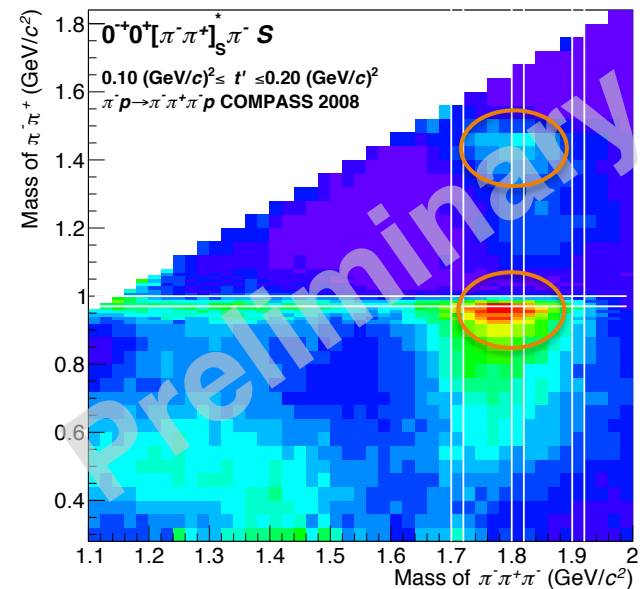


Method:

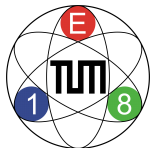
- Replace 2-body **fixed parametrisation**
e.g. Breit-Wigner/Flatté description of an isobar or $(\pi\pi)_S$
by **binned histogram**
- **Histogram-entries are free parameters**
 - instead of e.g. 3 isobars with $J^{PC} = 0^{++}$ use **n histogram bins** of two body mass $[m_{12}, m_{12} + \delta m]$ with these quantum numbers
 - $\delta m = 40 \text{ MeV}/c^2$
 - $\delta m = 10 \text{ MeV}/c^2$ around $f_0(980)$ ($\pm 80 \text{ MeV}/c^2$)
- obtain new phase information: $\phi_{\text{total}} = \phi_{\text{production}} + \phi_{\text{decay}}$



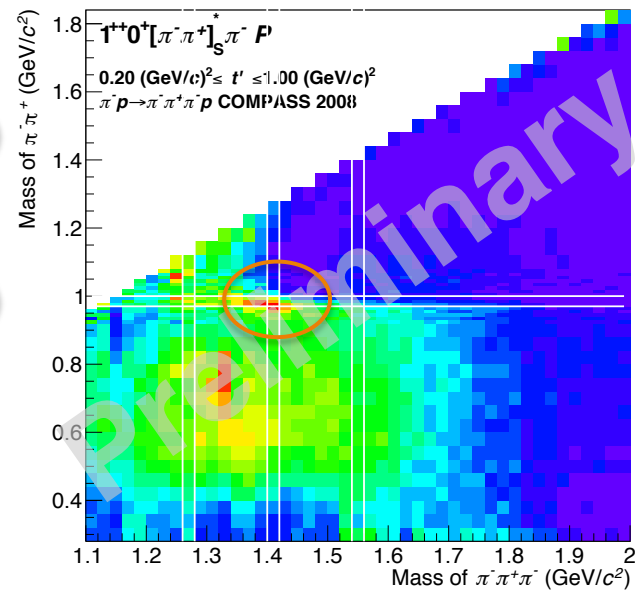
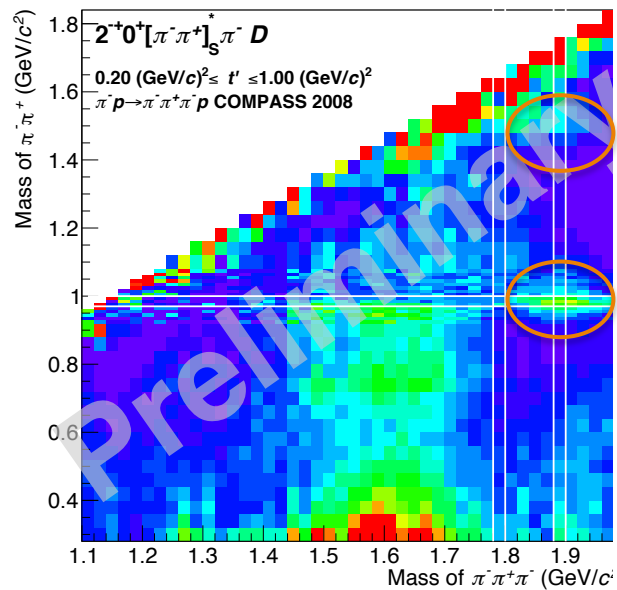
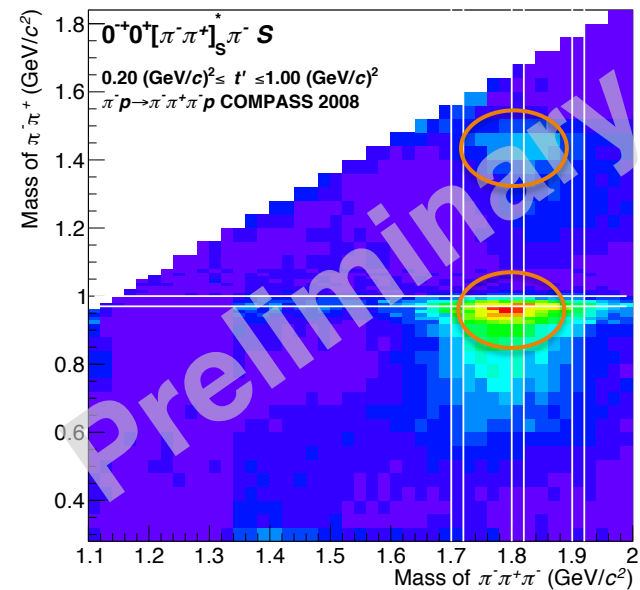
Correlation: $m_{2\pi} - m_{3\pi}$



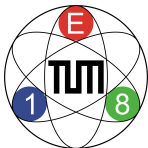
low t'



Correlation: $m_{2\pi} - m_{3\pi}$



high t'



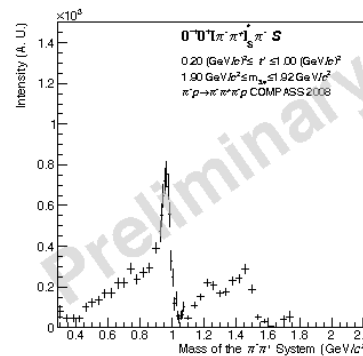
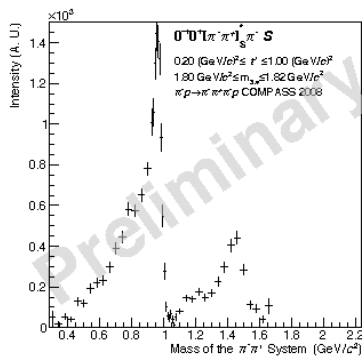
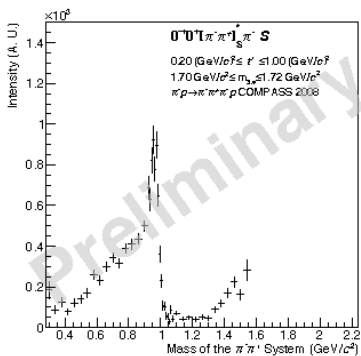
$(\pi\pi)^*_{S\text{-wave}} 0^{-+}$



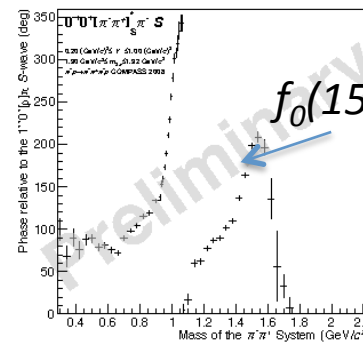
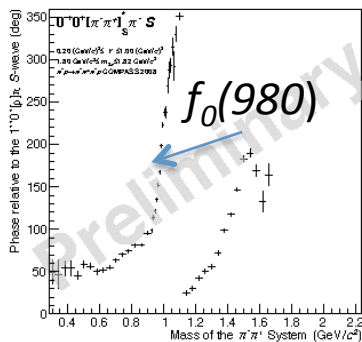
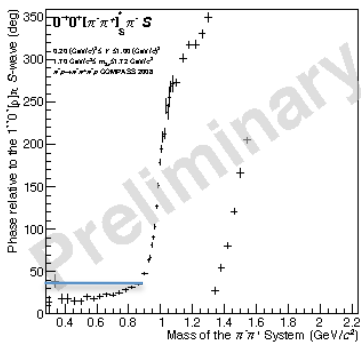
below resonance

at $\pi(1800)$

above resonance



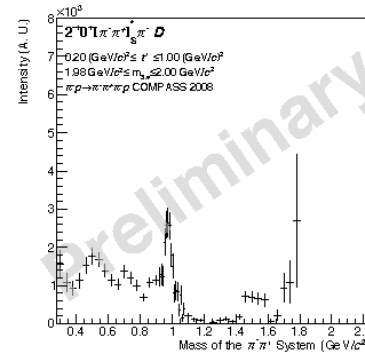
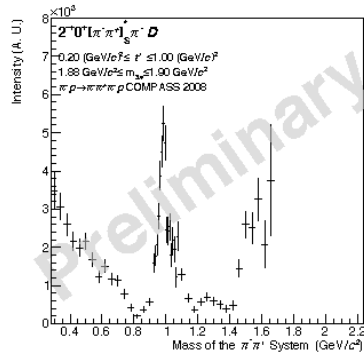
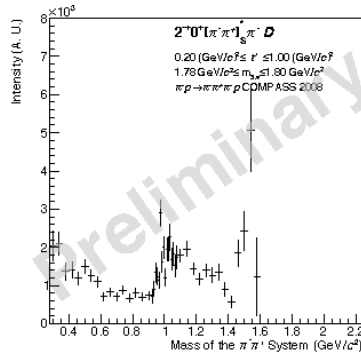
high t'



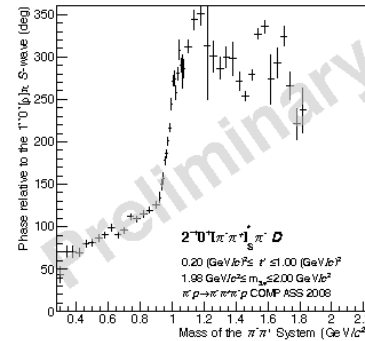
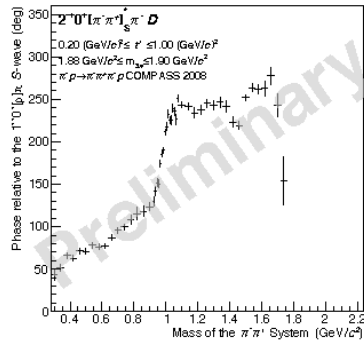
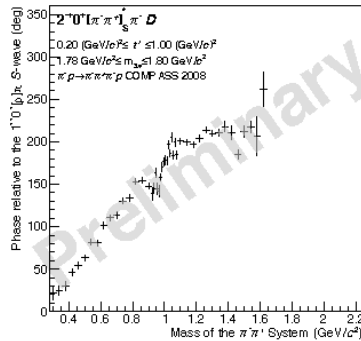
below resonance

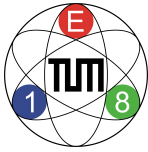
at $\pi_2(1880)$

above resonance



high t'

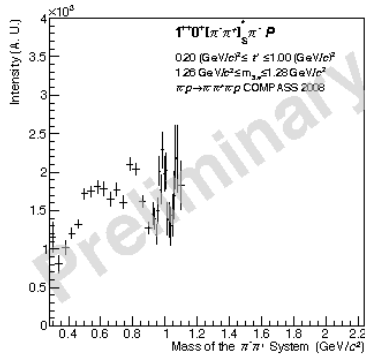




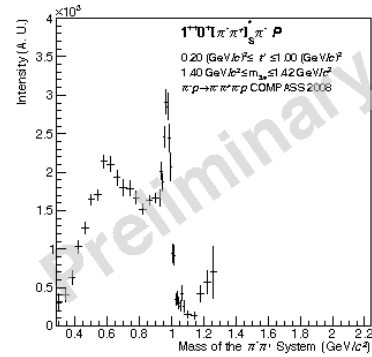
$(\pi\pi)^*_{S\text{-wave}} 1^{++}$



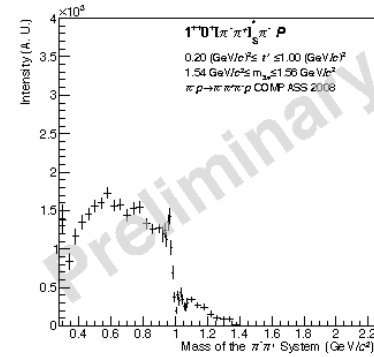
below resonance



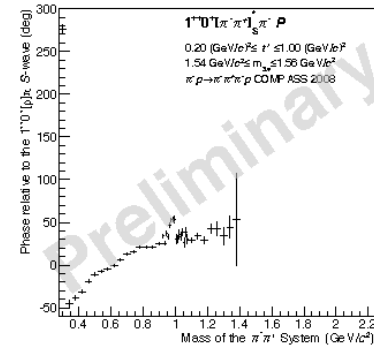
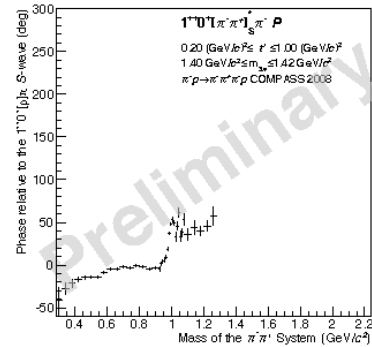
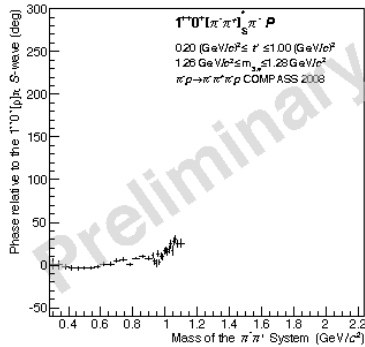
at $a_1(1420)$

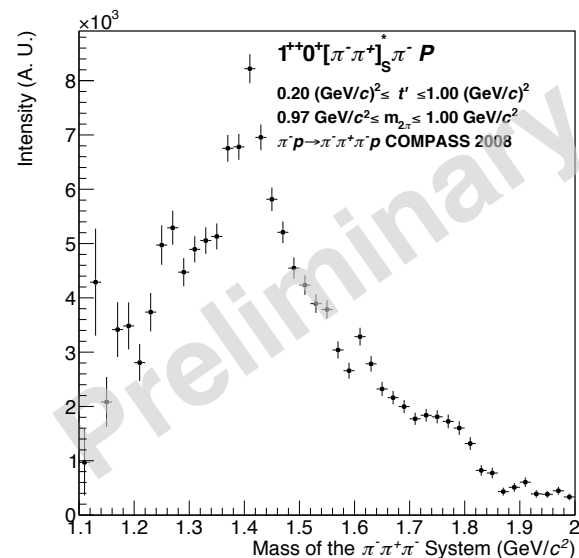
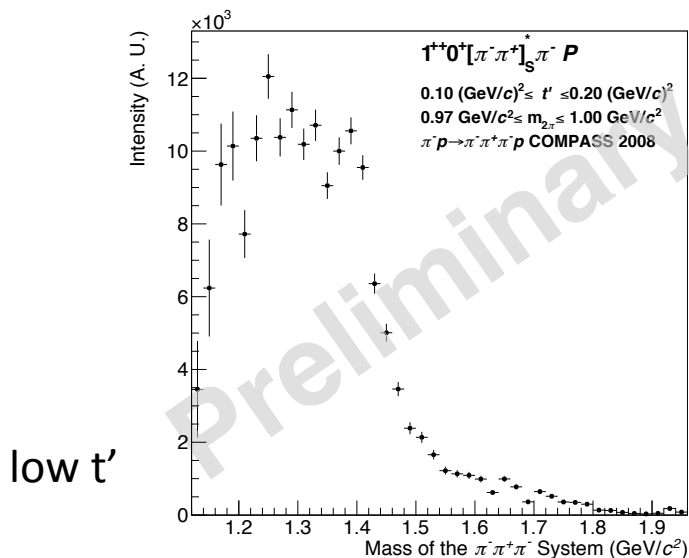


above resonance



high t'

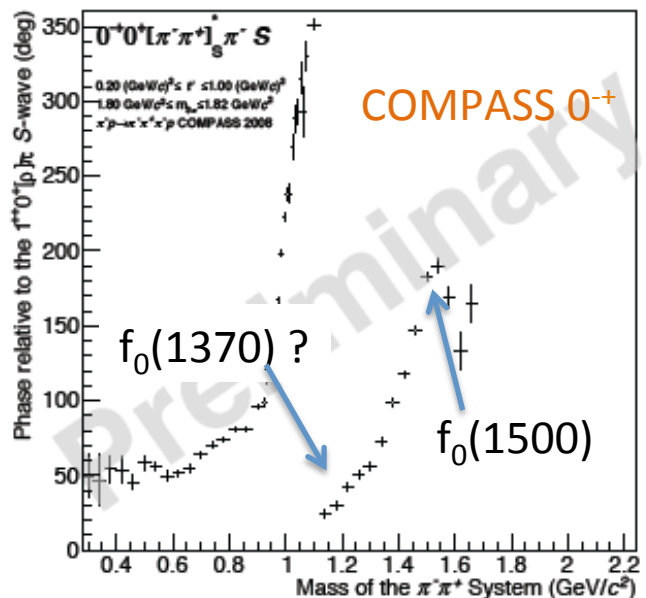
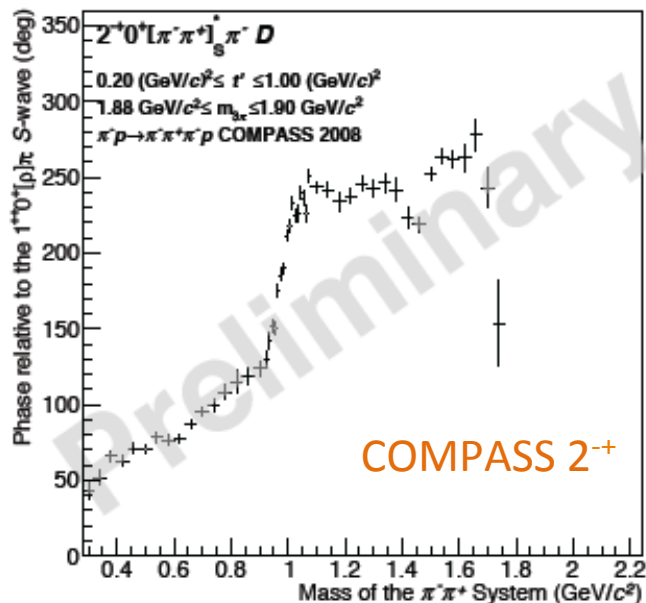
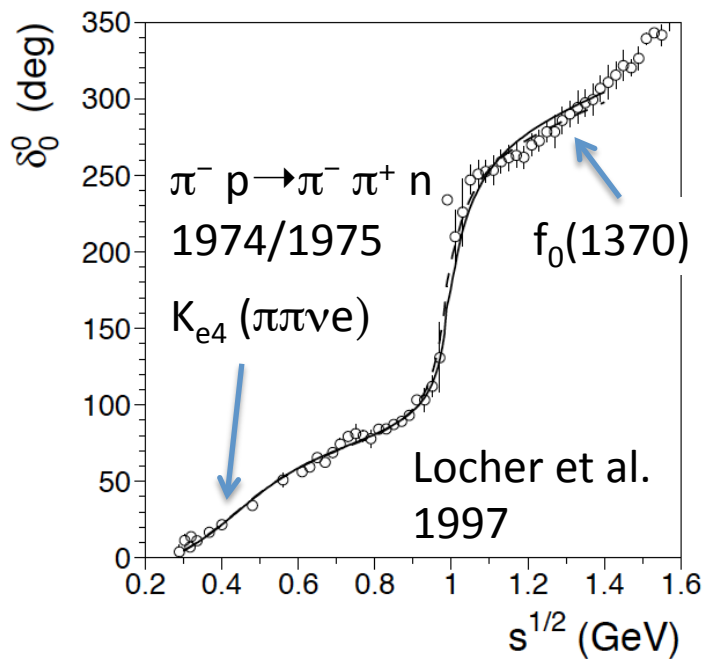




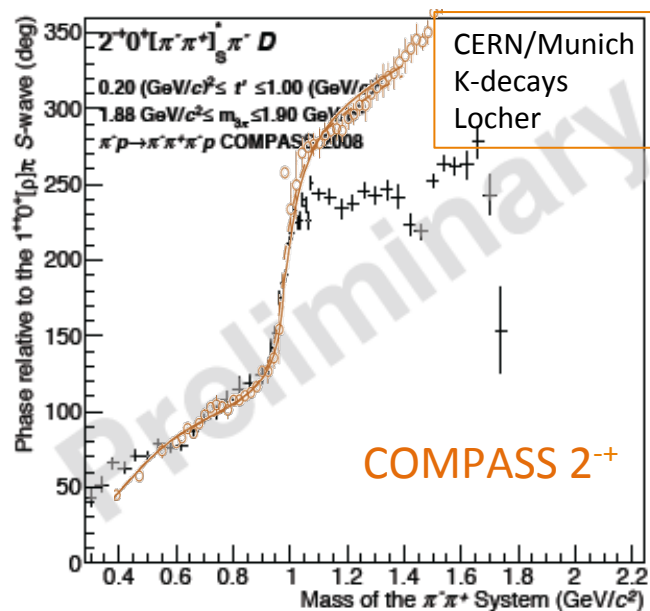
- $f_0(980)$ correlated with $a_1(1420)$
- non-resonant contributions at low t'
- **warning** !! just intensity cuts, amplitude selection

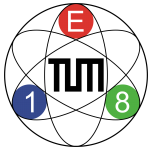
mass dependent fit

Further fun with $f_0(980)$



Further fun with $f_0(980)$





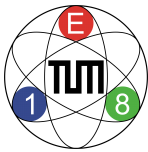
Conclusion



- Establish new “2D” fit method to perform PWA
 - mass independent: $m_{3\pi}$ bins and t' bins
 - Observe “various components” of resonances with different t' -dependencies:
 - extract resonance parameters
 - Identify non-resonant components
- Establish new method to establish shape of isobar-spectrum
 - first application: $[\pi\pi]_S^*$:
 - Shows strong dependence on mother wave
 - Shows strong dependence on $m_{3\pi}$
 - no unique parametrization yet
 - Reveals information on scalar isobars
 - Reveals different faces of $f_0(980)$
 - Allows to measure phases in decays

- Study of $a_1(1260)$
 - Observe “various components” of $a_1(1260)$ with different t' -dependencies:
Strong constraints on resonance parameters (w.r.t. PDG)
 - $M_{a_1(1260)} = 1260\text{-}1290 \text{ MeV}/c^2$, $\Gamma_{a_1(1260)} = 360 - 420 \text{ MeV}/c^2$
- Find **new iso-vector** state $a_1(1420)$
 - $M_{a_1(1420)} = 1412\text{-}1422 \text{ MeV}/c^2$, $\Gamma_{a_1(1420)} = 130\text{-}150 \text{ MeV}/c^2$
 - decay into $f_0(980)\pi$ in relative P-wave
 - observe full phase motion with respect to reference waves
 - coupling seems exclusively to $f_0(980)$
 - Phase-behavior of $(\pi\pi)_S$ hints to strong ss -component
 - Phase behavior **opposite** to $(\pi\pi)_S$ – coupling of $\pi(1800)$ and $\pi_2(1880)$
 - Nature of $a_1(1420)$? Isospin partner of $f_1(1420)$ (considered to be exotic) ?

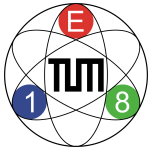




Conclusion II



- Sort out higher excitations of a_1 , a_2
States observed in reanalysis of CB-data
 - both states found at being at phase-space boundary by Bugg et al.
- COMPASS:
 - reasonable constraints on a_1'
$$M_{a_1(1930)} = 1920-2000 \text{ MeV}/c^2, \Gamma_{a_1(1930)} = 155 - 255 \text{ MeV}/c^2$$
 - poorer constraints on a_2'
$$M_{a_2(1950)} = 1740-1800 \text{ MeV}/c^2, \Gamma_{a_2(1950)} = 300 - 555 \text{ MeV}/c^2$$
- Radial excitation of π
 - $\pi(1800)$ well known: COMPASS observes decay into $f_0(980)$ and $f_0(1500)$ with two full circles from the Argand-diagram. Shape of $f_0(980)$ and $f_0(1500)$ to be investigated
 - $M_{\pi(1800)} = 1768-1807 \text{ MeV}/c^2, \Gamma_{\pi(1800)} = 215 - 280 \text{ MeV}/c^2$



Conclusion III



- Orbital-excitation of π
 - $\pi_2(1670)$ well known: **COMPASS** observes decay into $f_2(1270)$
 $M_{\pi_2(1670)} = 1635-1663 \text{ MeV}/c^2$, $\Gamma_{\pi_2(1670)} = 265-305 \text{ MeV}/c^2$
 - no evidence so far for coupling into $[\pi\pi]_S^*$
 - $\pi_2(1880)$: Clear signal observed in f_2 and f_0 . Strong coupling to iso-scalar sector
 - **COMPASS**: Decays observed into $f_0(980)$ and $f_2(1270)$
 $M_{\pi_2(1880) \rightarrow f_2(1270) \pi} = 1900-1990 \text{ MeV}/c^2$, $\Gamma_{\pi_2(1880) \rightarrow f_2(1270) \pi} = 210-390 \text{ MeV}/c^2$
- Other mesons:
 - $a_2(1320)$ clearly identified:
 $M_{a_2(1320)} = 1312-1315 \text{ MeV}/c^2$, $\Gamma_{a_2(1320)} = 108-115 \text{ MeV}/c^2$
 - $a_4(2040)$ clearly identified:
 $M_{a_4(2040)} = 1928-1959 \text{ MeV}/c^2$, $\Gamma_{a_4(2040)} = 360-400 \text{ MeV}/c^2$
comes our **lighter and broader than PDG** consistent with 2004 and $\eta(')\pi$