Azimuthal asymmetries in SIDIS with transversely polarized target at COMPASS

UNIVERSITÀ DEGLI STUDI DI TORINO

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on behalf of the COMPASS Collaboration

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Outline

- Introduction
- COMPASS experiment
- Measured asymmetries and theory expectations
  - Re-evaluation of $A_{LT}^{\cos\varphi_S}$ and $A_{LT}^{\cos(\varphi_h - \varphi_S)}$: from the lp to $\gamma^* p$ cross-section
  - Theory expectations
- Summary

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SIDIS x-section

A.Kotzinian, Nucl. Phys. B441, 234 (1995). Bacchetta, Diehl, Goeke, Metz, Mulders and Schlegel JHEP 0702:093 (2007).

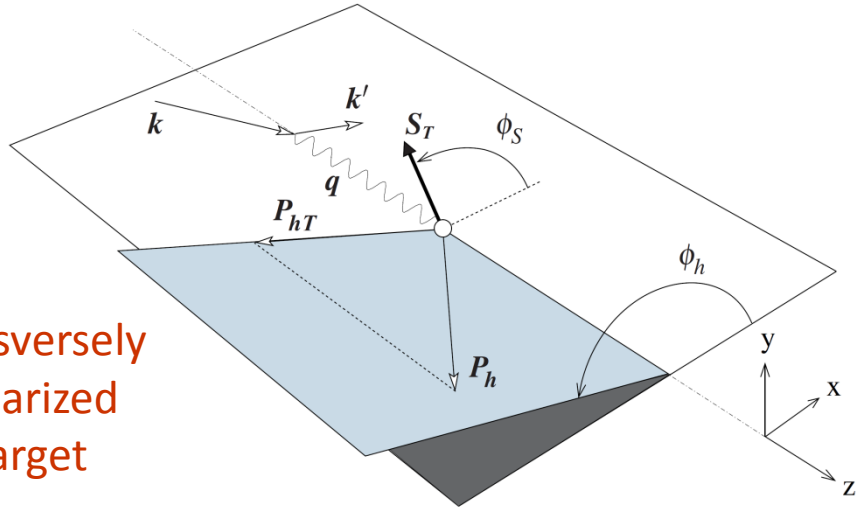
$$\frac{d\sigma}{dx dy dz dP_{hT}^2 d\varphi_h d\psi} = \left[\frac{\alpha}{xyQ^2}\frac{y^2}{2(1-\varepsilon)}\left(1+\frac{\gamma^2}{2x}\right)\right]\times\left(F_{UU,T}+\varepsilon F_{UU,L}\right)\times$$

$$\left\{\begin{array}{l}
1+\cos\varphi_h\times\sqrt{2\varepsilon(1+\varepsilon)}A_{UU}^{\cos\varphi_h}+\cos(2\varphi_h)\times\varepsilon A_{UU}^{\cos(2\varphi_h)}+\lambda\sin\varphi_h\times\sqrt{2\varepsilon(1-\varepsilon)}A_{LU}^{\sin\varphi_h}+ \\
S_L\left[\sqrt{2\varepsilon(1+\varepsilon)}\sin\phi_h A_{UL}^{\sin\phi_h}+\varepsilon\sin(2\phi_h)A_{UL}^{\sin(2\phi_h)}\right]+ \\
S_L\lambda\left[\sqrt{1-\varepsilon^2}A_{LL}+\sqrt{2\varepsilon(1-\varepsilon)}\cos\phi_h A_{LL}^{\cos\phi_h}\right]+ \\
S_T\left[\begin{array}{l}
\sin\varphi_S\times\left(\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin\varphi_S}\right)+ \\
\sin(\varphi_h-\varphi_S)\times\left(A_{UT}^{\sin(\varphi_h-\varphi_S)}\right)+ \\
\sin(\varphi_h+\varphi_S)\times\left(\varepsilon A_{UT}^{\sin(\varphi_h+\varphi_S)}\right)+ \\
\sin(2\varphi_h-\varphi_S)\times\left(\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin(2\varphi_h-\varphi_S)}\right)+ \\
\sin(3\varphi_h-\varphi_S)\times\left(\varepsilon A_{UT}^{\sin(3\varphi_h-\varphi_S)}\right)
\end{array}\right]+ \\
S_T\lambda\left[\begin{array}{l}
\cos\varphi_S\times\left(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos\varphi_S}\right)+ \\
\cos(\varphi_h-\varphi_S)\times\left(\sqrt{(1-\varepsilon^2)}A_{LT}^{\cos(\varphi_h-\varphi_S)}\right)+ \\
\cos(2\varphi_h-\varphi_S)\times\left(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos(2\varphi_h-\varphi_S)}\right)
\end{array}\right]
\end{array}\right\}$$

transversely polarized target

$$A_{U(L),T}^{w(\varphi_h,\varphi_s)} = \frac{F_{U(L),T}^{w(\varphi_h,\varphi_s)}}{F_{UU,T}+\varepsilon F_{UU,L}}$$

$$\varepsilon = \frac{1-y-\frac{1}{4}\gamma^2y^2}{1-y+\frac{1}{2}y^2+\frac{1}{4}\gamma^2y^2}, \quad \gamma = \frac{2Mx}{Q}$$



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$$1+\cos\varphi_h\times\sqrt{2\varepsilon(1+\varepsilon)}A_{UU}^{\cos\varphi_h}+\cos(2\varphi_h)\times\varepsilon A_{UU}^{\cos(2\varphi_h)}+\lambda\sin\varphi_h\times\sqrt{2\varepsilon(1-\varepsilon)}A_{LU}^{\sin\varphi_h}+$$

$$S_L\left[\sqrt{2\varepsilon(1+\varepsilon)}\sin\phi_h A_{UL}^{\sin\phi_h}+\varepsilon\sin(2\phi_h)A_{UL}^{\sin(2\phi_h)}\right]+$$

$$S_L\lambda\left[\sqrt{1-\varepsilon^2}A_{LL}+\sqrt{2\varepsilon(1-\varepsilon)}\cos\phi_h A_{LL}^{\cos\phi_h}\right]+$$

$$S_T\left[\sin\varphi_S\times\left(\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin\varphi_S}\right)+\sin(\varphi_h-\varphi_S)\times\left(A_{UT}^{\sin(\varphi_h-\varphi_S)}\right)+\sin(\varphi_h+\varphi_S)\times\left(\varepsilon A_{UT}^{\sin(\varphi_h+\varphi_S)}\right)+\sin(2\varphi_h-\varphi_S)\times\left(\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin(2\varphi_h-\varphi_S)}\right)+\sin(3\varphi_h-\varphi_S)\times\left(\varepsilon A_{UT}^{\sin(3\varphi_h-\varphi_S)}\right)\right]+$$

$$S_T\lambda\left[\cos\varphi_S\times\left(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos\varphi_S}\right)+\cos(\varphi_h-\varphi_S)\times\left(\sqrt{(1-\varepsilon^2)}A_{LT}^{\cos(\varphi_h-\varphi_S)}\right)+\cos(2\varphi_h-\varphi_S)\times\left(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos(2\varphi_h-\varphi_S)}\right)\right]$$

← Presented by A. Martin

Sivers & Collins

← Presented by A. Bressan

Twist-2

SSA

DSA

SIDIS x-section

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$$S_T\lambda\left[\cos\varphi_S\times\left(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos\varphi_S}\right)+\cos(\varphi_h-\varphi_S)\times\left(\sqrt{(1-\varepsilon^2)}A_{LT}^{\cos(\varphi_h-\varphi_S)}\right)+\cos(2\varphi_h-\varphi_S)\times\left(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos(2\varphi_h-\varphi_S)}\right)\right]$$

Sivers & Collins

Pretzelosity

Worm-gear

SSA

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$$S_T\lambda\left[\cos\varphi_S\times\left(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos\varphi_S}\right)+\cos(\varphi_h-\varphi_S)\times\left(\sqrt{(1-\varepsilon^2)}A_{LT}^{\cos(\varphi_h-\varphi_S)}\right)+\cos(2\varphi_h-\varphi_S)\times\left(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos(2\varphi_h-\varphi_S)}\right)\right]$$

Sivers & Collins

Pretzelosity

Worm-gear

Higher twists

SSA

DSA

Twist-2

Twist-3

SIDIS x-section

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$$S_T\lambda\left[\cos\varphi_S\times\left(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos\varphi_S}\right)+\cos(\varphi_h-\varphi_S)\times\left(\sqrt{(1-\varepsilon^2)}A_{LT}^{\cos(\varphi_h-\varphi_S)}\right)+\cos(2\varphi_h-\varphi_S)\times\left(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos(2\varphi_h-\varphi_S)}\right)\right]$$

Sivers & Collins

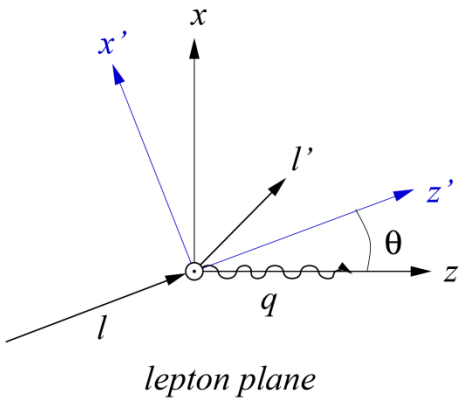
Pretzelosity

Worm-gear

Higher twists

SSA

DSA



lepton plane

Twist-2

Twist-3

SIDIS x-section

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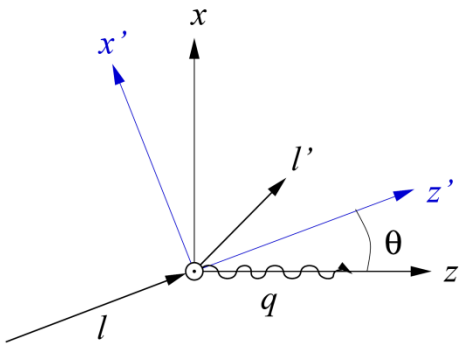
$$S_T\Big[\sin\varphi_S\times\Big(\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin\varphi_S}\Big)+\sin(\varphi_h-\varphi_S)\times\Big(A_{UT}^{\sin(\varphi_h-\varphi_S)}\Big)+\sin(\varphi_h+\varphi_S)\times\Big(\varepsilon A_{UT}^{\sin(\varphi_h+\varphi_S)}\Big)+\sin(2\varphi_h-\varphi_S)\times\Big(\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin(2\varphi_h-\varphi_S)}\Big)+\sin(3\varphi_h-\varphi_S)\times\Big(\varepsilon A_{UT}^{\sin(3\varphi_h-\varphi_S)}\Big)+\Big]+$$

$$S_T\lambda\Big[\cos\varphi_S\times\Big(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos\varphi_S}\Big)+\cos(\varphi_h-\varphi_S)\times\Big(\sqrt{(1-\varepsilon^2)}A_{LT}^{\cos(\varphi_h-\varphi_S)}\Big)+\cos(2\varphi_h-\varphi_S)\times\Big(\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos(2\varphi_h-\varphi_S)}\Big)+\Big]\Big]$$



lepton plane

$$\sin\theta=\gamma\sqrt{\frac{1-y-\frac{1}{4}\gamma^2y^2}{1+\gamma^2}},\ \gamma=\frac{2Mx}{Q};$$

$$\theta\xrightarrow[\text{Bjorken limit}]{}0\Rightarrow S_T\simeq P_T,\ S_L\simeq P_L$$

SIDIS x-section: from lp to $\gamma^* p$ (P_L=0)

Kotzinian et al.
hep-ph/9808368 (1998)
hep-ph/9908466 (1999)
M. Diehl and S. Sapeta,
Eur. Phys. J. C 41 (2005) 515

$$\frac{d\sigma}{dx dy dz dP_{hT}^2 d\varphi_h d\varphi_S} = \left[\frac{\cos\theta}{1-\sin^2\theta\sin^2\varphi_S}\right]\times\left[\frac{\alpha}{xyQ^2}\frac{y^2}{2(1-\varepsilon)}\left(1+\frac{\gamma^2}{2x}\right)\right]\times\left(F_{UU,T}+\varepsilon F_{UU,L}\right)\times$$

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$$\frac{P_T}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}}\left[\sin\varphi_S\times\left(\cos\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin\varphi_S}\right)+\right.$$

$$\sin(\varphi_h-\varphi_S)\times\left(\cos\theta A_{UT}^{\sin(\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UL}^{\sin\varphi_h}\right)+$$

$$\sin(\varphi_h+\varphi_S)\times\left(\cos\theta\varepsilon A_{UT}^{\sin(\varphi_h+\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UL}^{\sin\varphi_h}\right)+$$

$$\sin(2\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin(2\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\varepsilon A_{UL}^{\sin 2\varphi_h}\right)+$$

$$\sin(3\varphi_h-\varphi_S)\times\left(\cos\theta\varepsilon A_{UT}^{\sin(3\varphi_h-\varphi_S)}\right)+$$

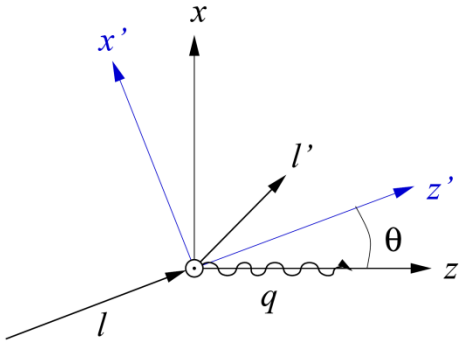
$$\left.\left.\sin(2\varphi_h+\varphi_S)\times\left(\frac{1}{2}\sin\theta\varepsilon A_{UL}^{\sin 2\varphi_h}\right)\right]+\right.$$

$$\frac{P_T\lambda}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}}\left[\cos\varphi_S\times\left(\cos\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos\varphi_S}+\sin\theta\sqrt{(1-\varepsilon^2)}A_{LL}\right)+\right.$$

$$\cos(\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{(1-\varepsilon^2)}A_{LT}^{\cos(\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LL}^{\cos\varphi_h}\right)+$$

$$\cos(2\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos(2\varphi_h-\varphi_S)}\right)+$$

$$\left.\left.\cos(\varphi_h+\varphi_S)\times\left(\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LL}^{\cos\varphi_h}\right)\right]\right]$$



lepton plane

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$$\left[1 + \cos\varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)}\, A_{UU}^{\cos\varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \lambda \sin\varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)}\, A_{LU}^{\sin\varphi_h} + \right.$$

$$\frac{P_T}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}} \left[\sin\varphi_S \times \left(\underline{\cos\theta} \sqrt{2\varepsilon(1+\varepsilon)}\, A_{UT}^{\sin\varphi_S} \right) + \right.$$

$$\sin(\varphi_h - \varphi_S) \times \left(\underline{\cos\theta} A_{UT}^{\sin(\varphi_h-\varphi_S)} + \underline{\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}\, A_{UL}^{\sin\varphi_h}} \right) +$$

$$\sin(\varphi_h + \varphi_S) \times \left(\underline{\cos\theta\varepsilon} A_{UT}^{\sin(\varphi_h+\varphi_S)} + \underline{\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}\, A_{UL}^{\sin\varphi_h}} \right) +$$

$$\sin(2\varphi_h - \varphi_S) \times \left(\underline{\cos\theta}\sqrt{2\varepsilon(1+\varepsilon)}\, A_{UT}^{\sin(2\varphi_h-\varphi_S)} + \underline{\frac{1}{2}\sin\theta\varepsilon} A_{UL}^{\sin 2\varphi_h} \right) +$$

$$\sin(3\varphi_h - \varphi_S) \times \left(\underline{\cos\theta\varepsilon} A_{UT}^{\sin(3\varphi_h-\varphi_S)} \right) +$$

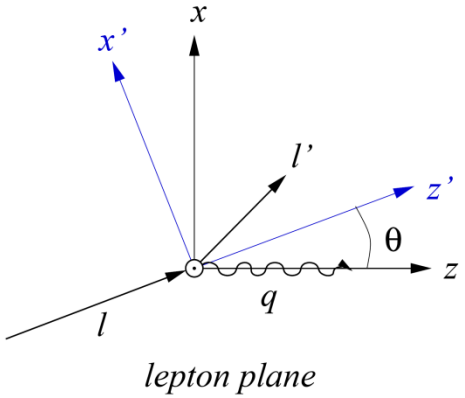
$$\left. \left. \sin(2\varphi_h + \varphi_S) \times \left(\underline{\frac{1}{2}\sin\theta\varepsilon} A_{UL}^{\sin 2\varphi_h} \right) \right] + \right.$$

$$\frac{P_T \lambda}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}} \left[\cos\varphi_S \times \left(\underline{\cos\theta}\sqrt{2\varepsilon(1-\varepsilon)}\, A_{LT}^{\cos\varphi_S} + \underline{\sin\theta}\sqrt{(1-\varepsilon^2)}\, A_{LL} \right) + \right.$$

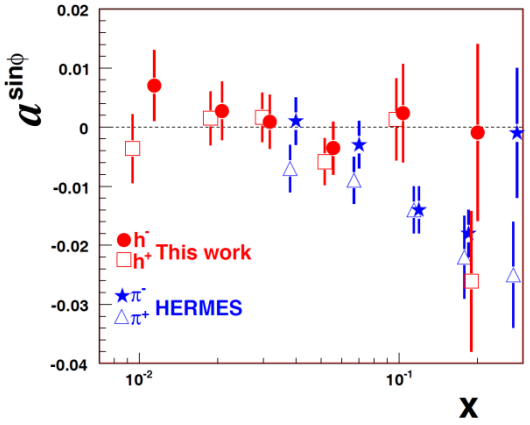
$$\cos(\varphi_h - \varphi_S) \times \left(\underline{\cos\theta}\sqrt{(1-\varepsilon^2)}\, A_{LT}^{\cos(\varphi_h-\varphi_S)} + \underline{\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1-\varepsilon)}\, A_{LL}^{\cos\varphi_h}} \right) +$$

$$\cos(2\varphi_h - \varphi_S) \times \left(\underline{\cos\theta}\sqrt{2\varepsilon(1-\varepsilon)}\, A_{LT}^{\cos(2\varphi_h-\varphi_S)} \right) +$$

$$\left. \left. \cos(\varphi_h + \varphi_S) \times \left(\underline{\frac{1}{2}\sin\theta}\sqrt{2\varepsilon(1-\varepsilon)}\, A_{LL}^{\cos\varphi_h} \right) \right] \right]$$



Eur.Phys.J.C70:39-49,2010



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hep-ph/9808368 (1998)
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$$\sin(\varphi_h-\varphi_S)\times\left(\cos\theta A_{UT}^{\sin(\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UL}^{\sin\varphi_h}\right)+$$

$$\sin(\varphi_h+\varphi_S)\times\left(\cos\theta\varepsilon A_{UT}^{\sin(\varphi_h+\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UL}^{\sin\varphi_h}\right)+$$

$$\sin(2\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin(2\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\varepsilon A_{UL}^{\sin 2\varphi_h}\right)+$$

$$\sin(3\varphi_h-\varphi_S)\times\left(\cos\theta\varepsilon A_{UT}^{\sin(3\varphi_h-\varphi_S)}\right)+$$

$$\left.\left.\sin(2\varphi_h+\varphi_S)\times\left(\frac{1}{2}\sin\theta\varepsilon A_{UL}^{\sin 2\varphi_h}\right)\right]+\right.$$

$$\frac{P_T\lambda}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}}\left[\cos\varphi_S\times\left(\cos\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos\varphi_S}+\sin\theta\sqrt{(1-\varepsilon^2)}A_{LL}\right)+\right.$$

$$\cos(\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{(1-\varepsilon^2)}A_{LT}^{\cos(\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LL}^{\cos\varphi_h}\right)+$$

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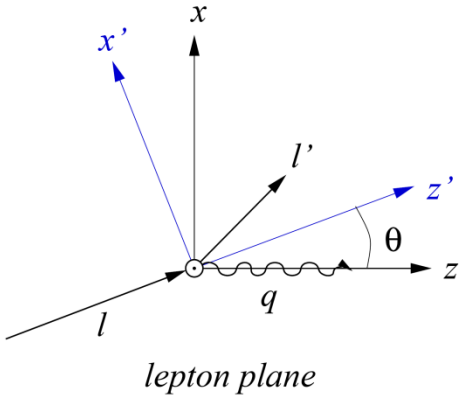

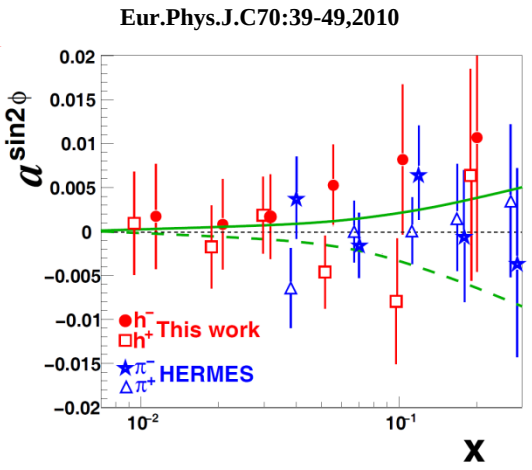

SIDIS x-section: from lp to $\gamma^* p$ (P_L=0)

Kotzinian et al.
hep-ph/9808368 (1998)
hep-ph/9908466 (1999)
M. Diehl and S. Sapeta,
Eur. Phys. J. C 41 (2005) 515

$$\frac{d\sigma}{dx dy dz dP_{hT}^2 d\varphi_h d\varphi_S} = \left[\frac{\cos\theta}{1-\sin^2\theta\sin^2\varphi_S}\right]\times\left[\frac{\alpha}{xyQ^2}\frac{y^2}{2(1-\varepsilon)}\left(1+\frac{\gamma^2}{2x}\right)\right]\times\left(F_{UU,T}+\varepsilon F_{UU,L}\right)\times$$

$$\left[1+\cos\varphi_h\times\sqrt{2\varepsilon(1+\varepsilon)}A_{UU}^{\cos\varphi_h}+\cos(2\varphi_h)\times\varepsilon A_{UU}^{\cos(2\varphi_h)}+\lambda\sin\varphi_h\times\sqrt{2\varepsilon(1-\varepsilon)}A_{LU}^{\sin\varphi_h}+\right.$$

$$\frac{P_T}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}}\left[\sin\varphi_S\times\left(\cos\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin\varphi_S}\right)+\right.$$

$$\sin(\varphi_h-\varphi_S)\times\left(\cos\theta A_{UT}^{\sin(\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UL}^{\sin\varphi_h}\right)+$$

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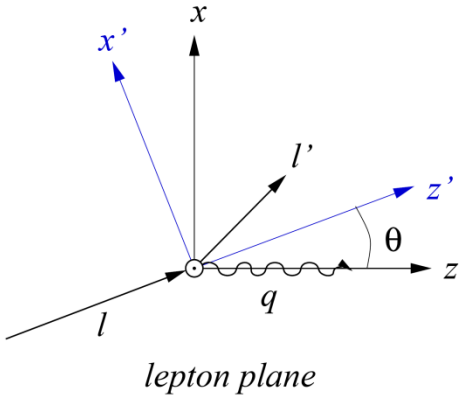
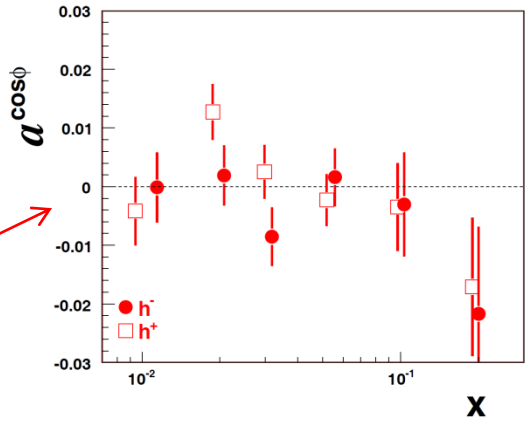


lepton plane

Eur.Phys.J.C70:39-49,2010



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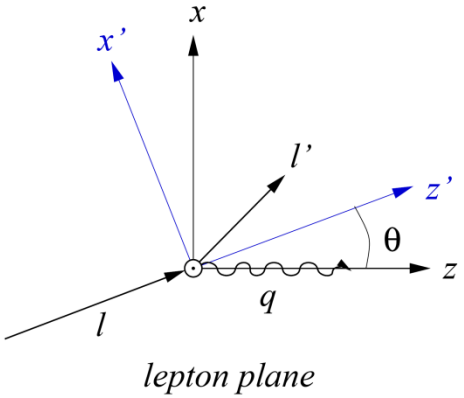

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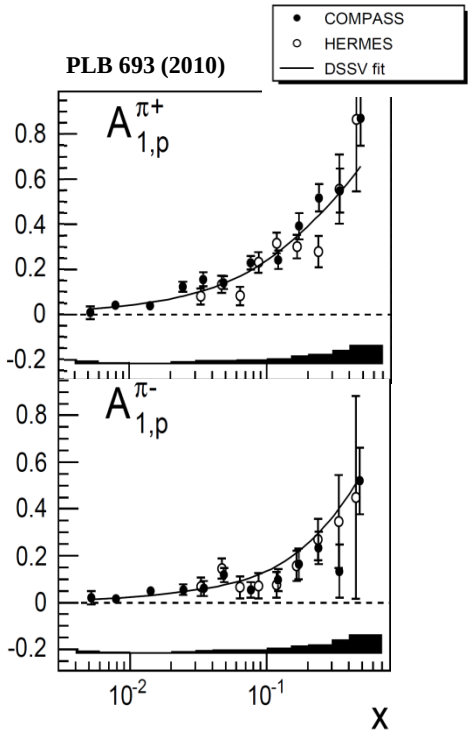
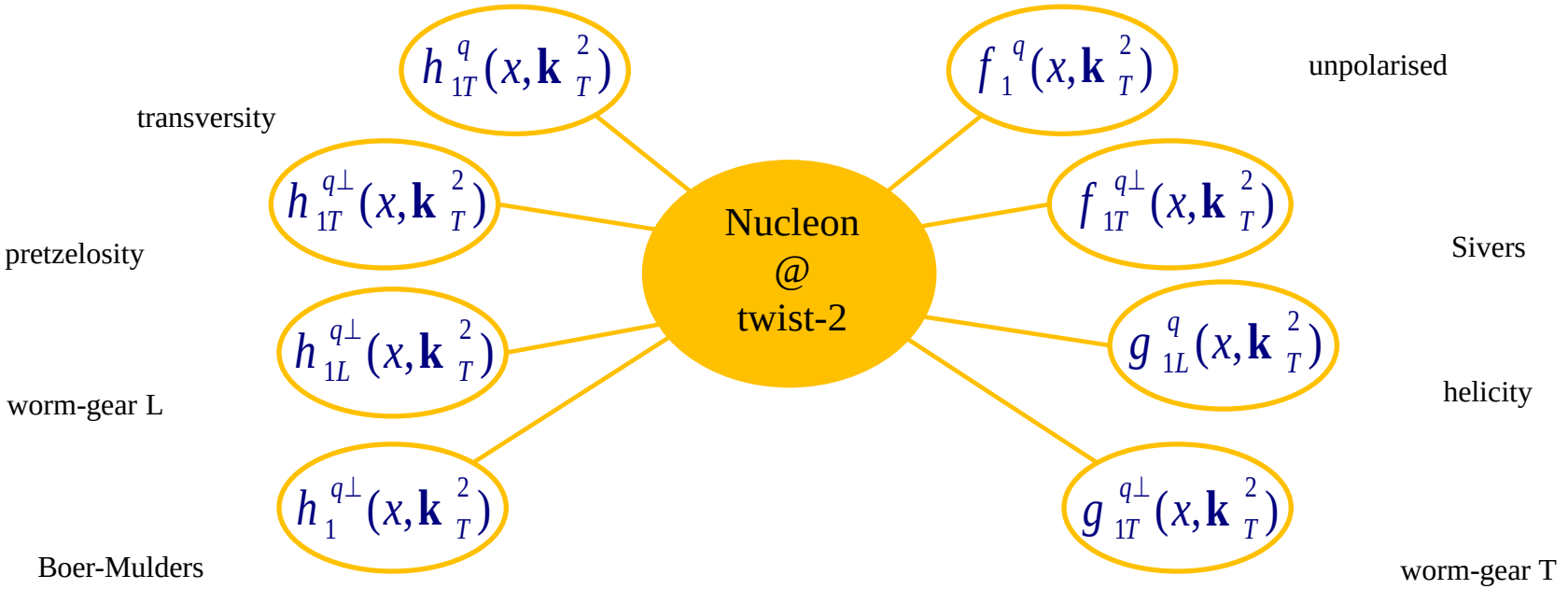
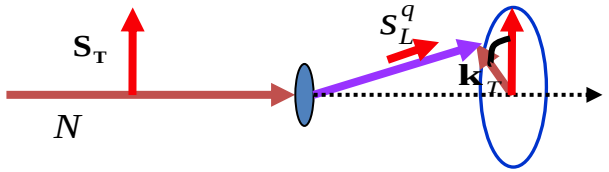


TMD parton distribution functions

Collins, Soper (81,82); Ji, Ma, Yuan (03, 04); Collins, Metz (04) – Definition of TMD DF's and FF's & QCD factorization of SIDIS.

LO QCD = Simple parton model + Factorized twist-2 PDF & FF





$\mathbf{k}_T$ – intrinsic transverse momentum of the quark

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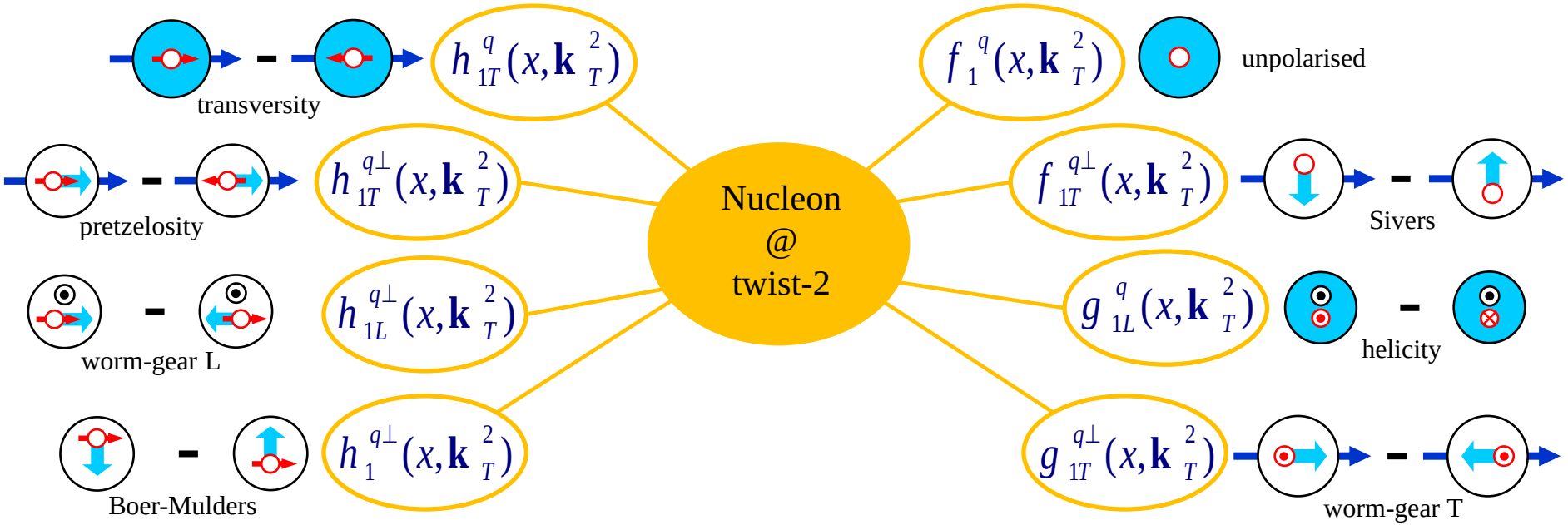
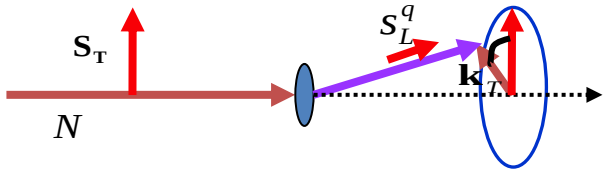


nucleon with transverse or longitudinal spin

parton with transverse or longitudinal spin

parton transverse momentum

Proton goes out of the screen. Photon goes into the screen



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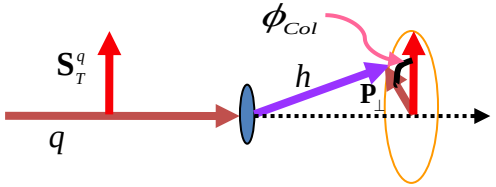
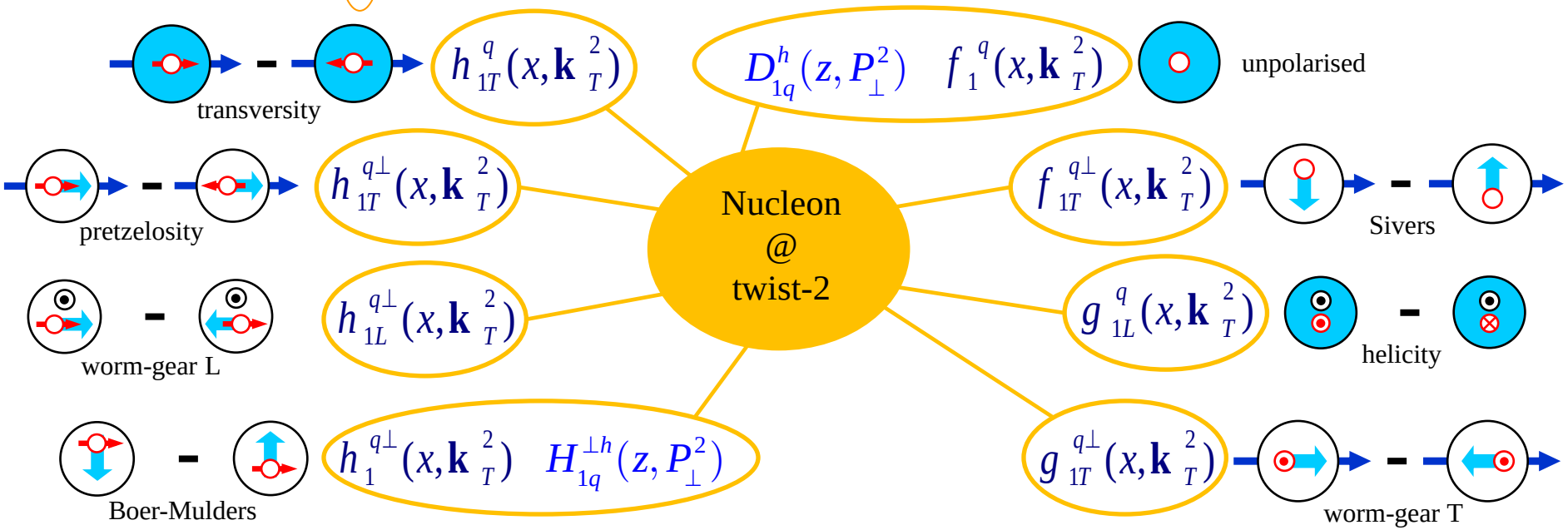


$\mathbf{P}_\perp$ – transverse momentum of the fragmenting quark w.r.t. the direction of the produced hadron



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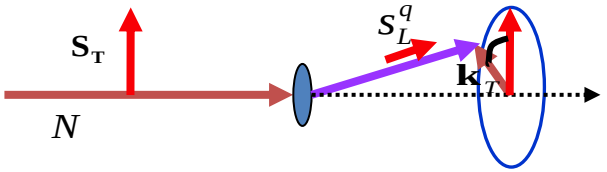


$\mathbf{k}_T$ – intrinsic transverse momentum of the quark

Interpretation of the transverse asymmetries

Bacchetta, Diehl, Goeke, Metz, Mulders and Schlegel JHEP 0702:093 (2007).

Within QCD parton model $A_i \propto DF \otimes FF \quad (i = 1,..8)$

$$A_{UT}^{\sin(\phi_h+\phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h}$$
$$A_{UT}^{\sin(\phi_h-\phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$
$$A_{UT}^{\sin(3\phi_h-\phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

Twist-2:

$$A_{LT}^{\cos(\phi_h-\phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$$

single spin

double spin

Twist-2 + k_T/Q kinematical corrections:

$$A_{UT}^{\sin(\phi_s)} \propto \frac{M}{Q}\left(h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \ldots\right)$$
$$A_{UT}^{\sin(2\phi_h-\phi_s)} \propto \frac{M}{Q}\left(h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \ldots\right)$$

$$A_{LT}^{\cos(\phi_s)} \propto \frac{M}{Q}\left(g_{1T}^q \otimes D_{1q}^h + \ldots\right)$$
$$A_{LT}^{\cos(2\phi_h-\phi_s)} \propto \frac{M}{Q}\left(g_{1T}^q \otimes D_{1q}^h + \ldots\right)$$

From “raw” to physics asymmetries

$$A_{UT}^{w(\phi_h,\phi_s)} = \frac{A_{UT,raw}^{w(\phi_h,\phi_s)}}{D^{w(\phi_h,\phi_s)}(y)\, f\, |P_T|}, \quad A_{LT}^{w(\phi_h,\phi_s)} = \frac{A_{LT,raw}^{w(\phi_h,\phi_s)}}{D^{w(\phi_h,\phi_s)}(y)\, f P_{beam}\, |P_T|}$$

$$D^{\sin(\phi_h-\phi_S)}(y) = 1$$

$$D^{\sin(\phi_h+\phi_S)}(y) = D^{\sin(3\phi_h-\phi_S)}(y) = \varepsilon \approx \frac{2(1-y)}{1+(1-y)^2}$$

$$D^{\sin(2\phi_h-\phi_S)}(y) = D^{\sin(\phi_S)}(y) = \sqrt{2\varepsilon(1+\varepsilon)} \approx \frac{2(2-y)\sqrt{1-y}}{1+(1-y)^2}$$

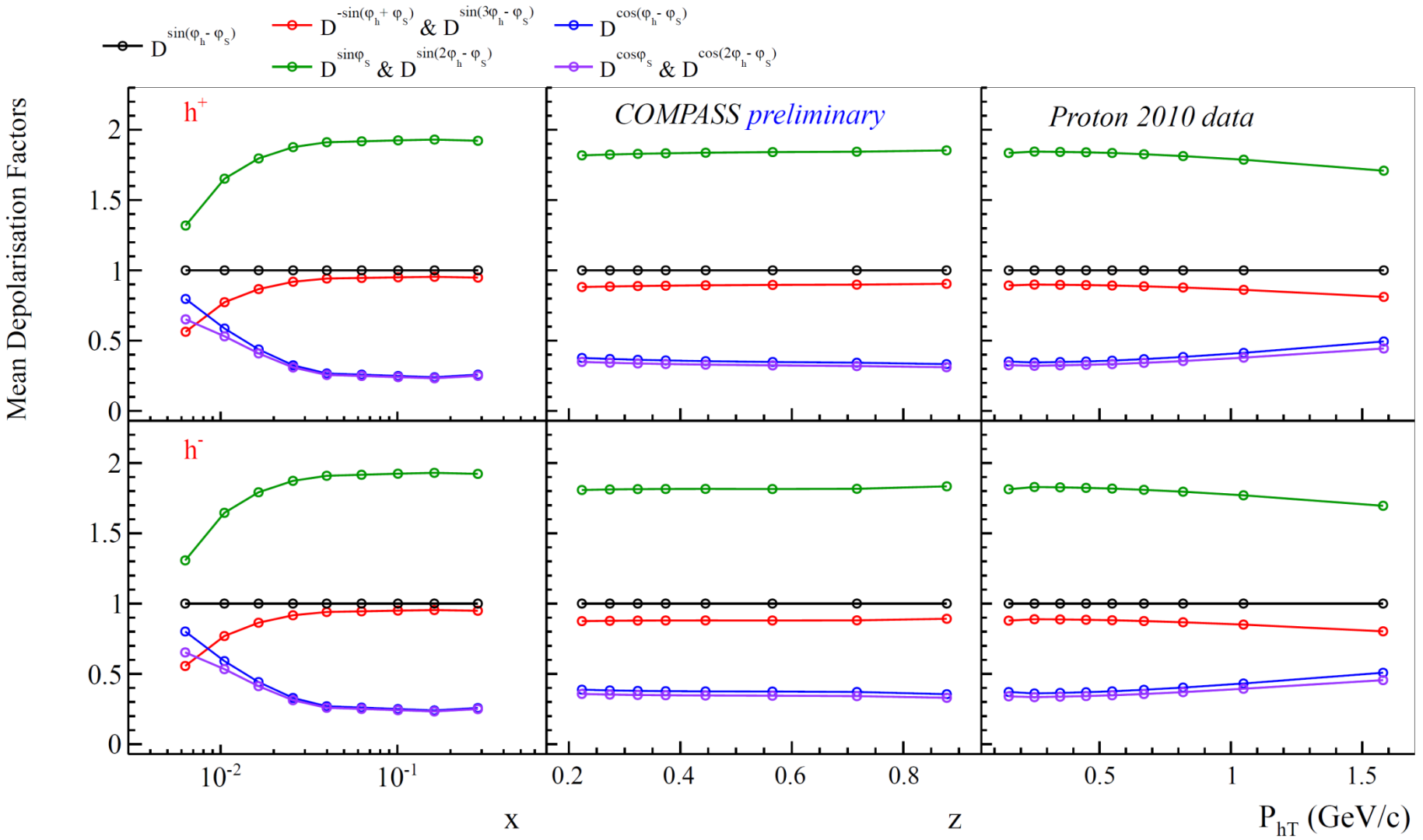
$$D^{\cos(2\phi_h-\phi_S)}(y) = D^{\cos(\phi_S)}(y) = \sqrt{2\varepsilon(1-\varepsilon)} \approx \frac{2y\sqrt{1-y}}{1+(1-y)^2}$$

$$D^{\cos(\phi_h-\phi_S)}(y) = \sqrt{(1-\varepsilon^2)} \approx \frac{y(2-y)}{1+(1-y)^2}$$

$$\varepsilon = \frac{1-y-\frac{1}{4}\gamma^2y^2}{1-y+\frac{1}{2}y^2+\frac{1}{4}\gamma^2y^2}, \quad \gamma = \frac{2Mx}{Q}$$

$D^{w_i(\phi_h,\phi_s)}$ – Depolarization factor, f - target dilution factor, P_T - target polarization, P_{beam} - beam polarization

Mean Depolarization Factors



Outline

- Introduction
- **COMPASS experiment**
- Measured asymmetries and theory expectations
  - Re-evaluation of $A_{LT}^{\cos\varphi_S}$ and $A_{LT}^{\cos(\varphi_h - \varphi_s)}$: from the lp to $\gamma^* p$ cross-section
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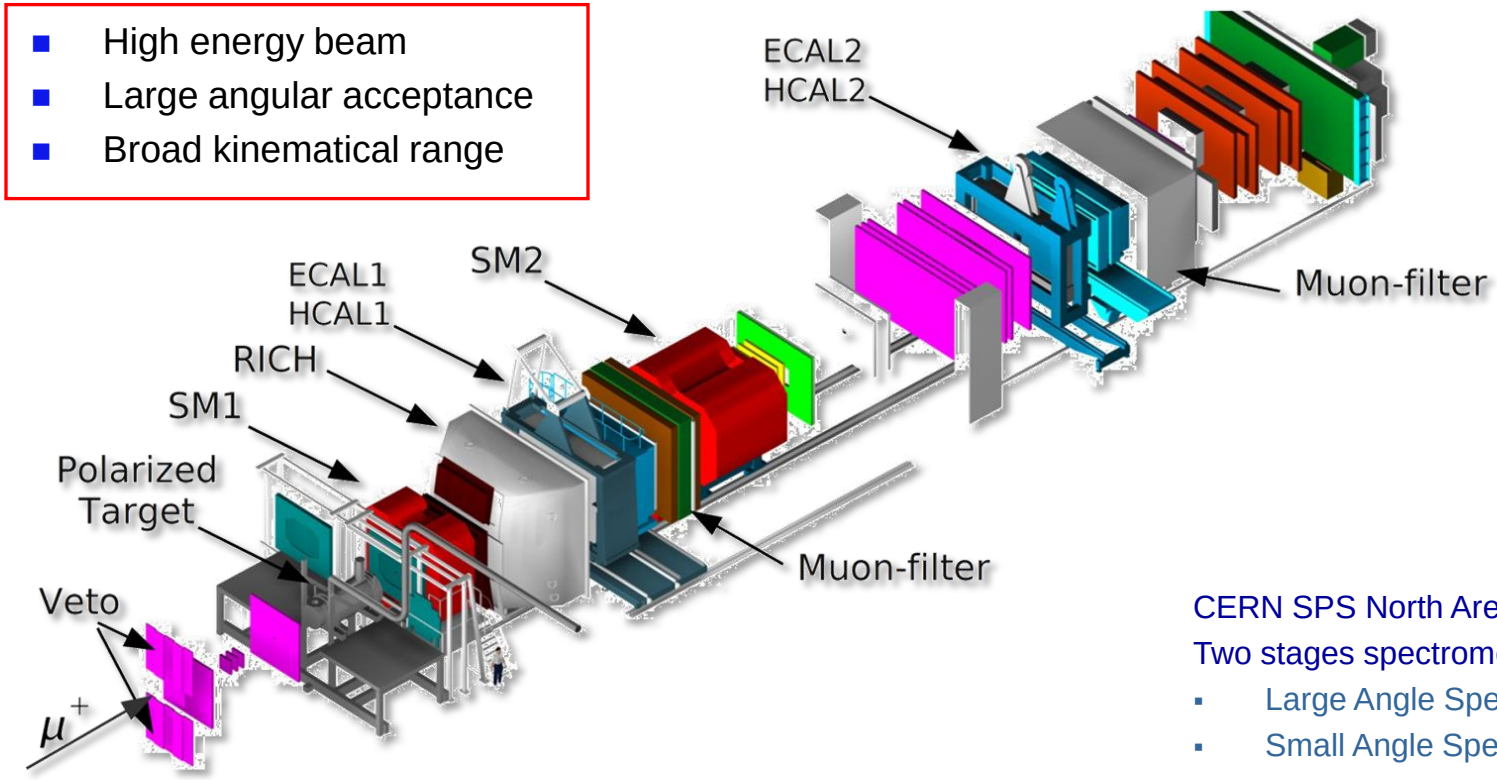
COMPASS experimental setup

COmmon Muon Proton Apparatus for Structure and Spectroscopy

- High energy beam
- Large angular acceptance
- Broad kinematical range



Longitudinally polarized μ^+ beam (160 Gev/c).

Longitudinally or Transversely polarized ^{6}LiD or NH_3 target

Momentum, tracking and calorimetric measurements, PID

CERN SPS North Area.

Two stages spectrometer

- Large Angle Spectrometer (SM1)
- Small Angle Spectrometer (SM2)

Hadron & Muon high energy beams.

Beam rates: 10^8 muons/s, $5 \cdot 10^7$ hadrons/s.

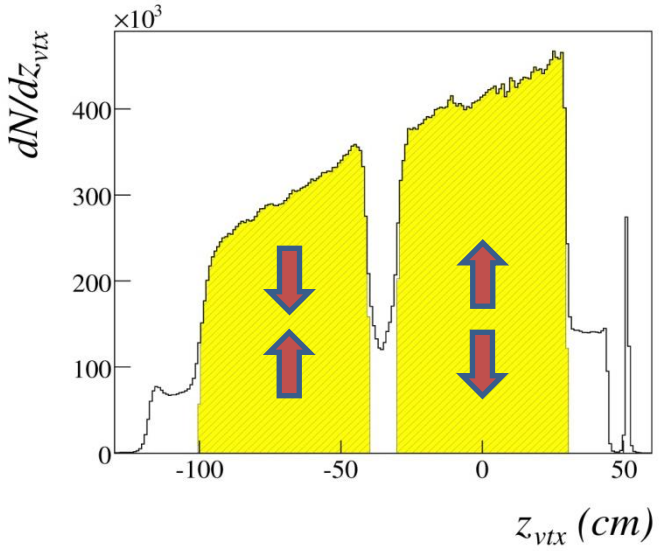
COMPASS Polarized target system

solid state target operated in frozen spin mode

Years 2002-2004

Deuteron - ^{6}LiD:

- Two 60 cm long ^{6}LiD cells with opposite polarization
- Polar angle acceptance – 70 mrad
- Target Polarization ±50%
- dilution factor f = 0.38

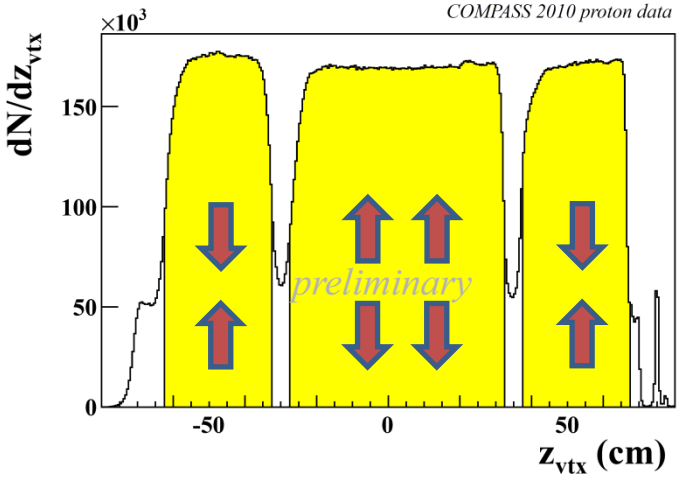


Data is collected simultaneously for the two target spin orientations
Polarization reversal after each ~4-5 days

Years 2007 and 2010

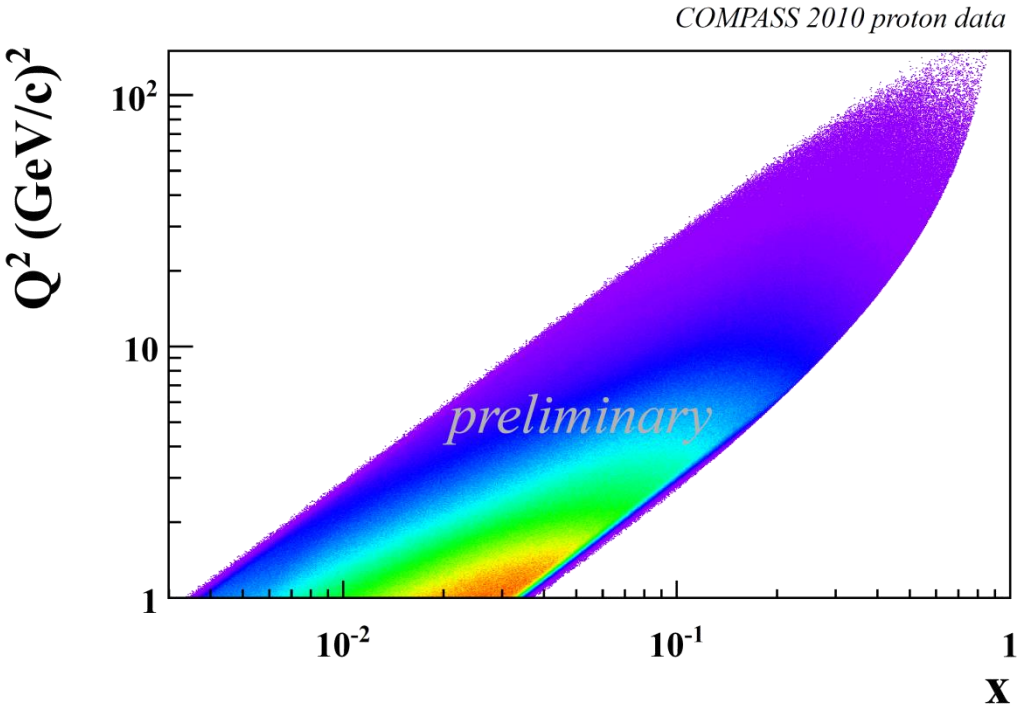
Proton - NH_3:

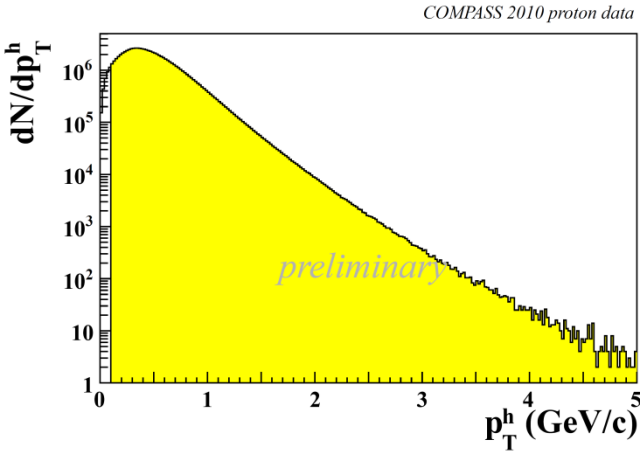
- Three cells system (30 cm,60cm, 30cm)
- Polar angle acceptance – 180 mrad (new magnet in 2006)
- Target Polarization ±90%
- dilution factor f = 0.14

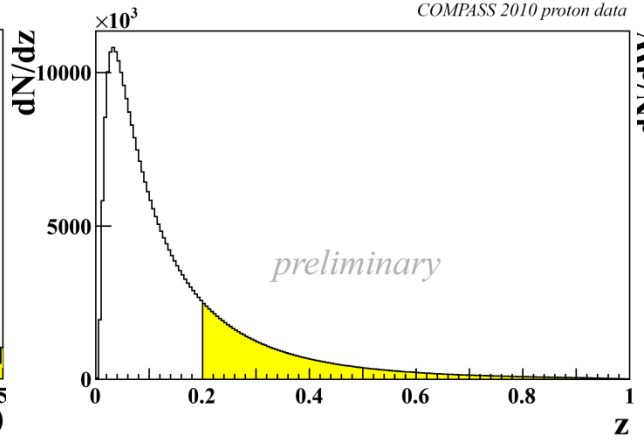


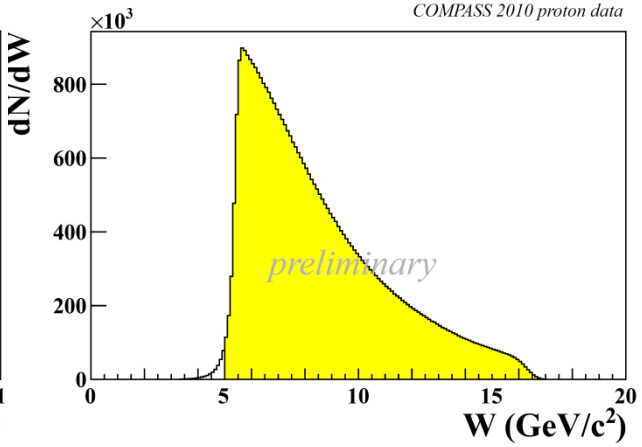
Data selection

- DIS cuts :
  - $Q^2 > 1\ GeV^2$
  - $0.1 < y < 0.9$
  - $W > 5\ GeV$
- Hadron cuts :
  - $z > 0.2$
  - $P_{hT} > 0.1\ GeV/c$









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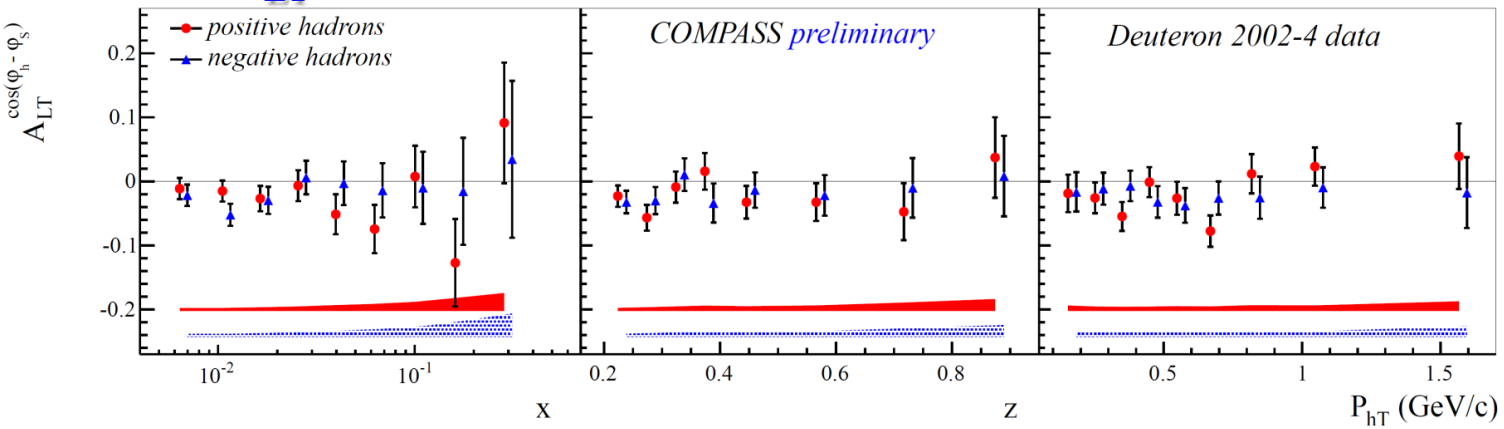
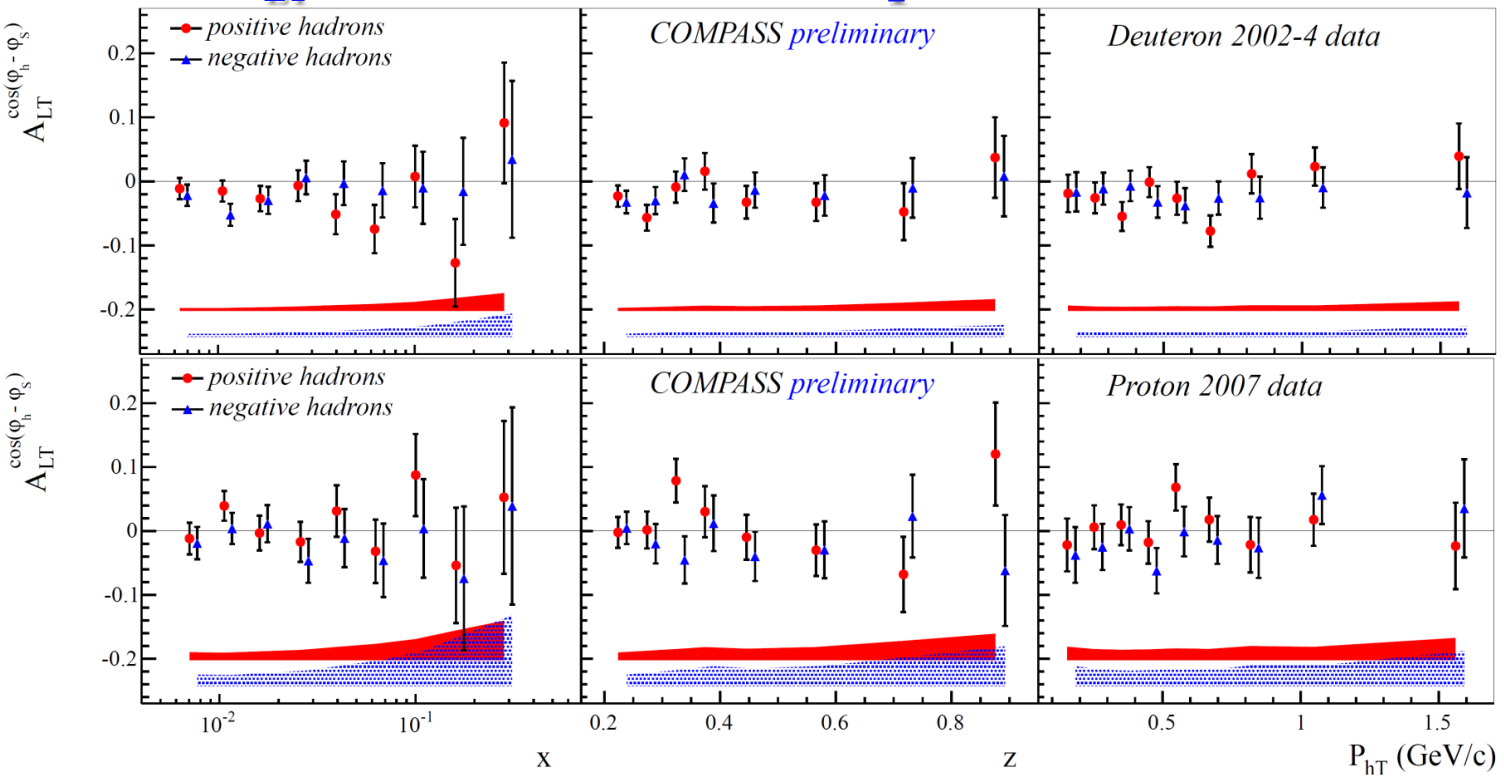
Results for $A_{LT}^{\cos(\varphi_h-\varphi_S)}$ deuteron



$A_{LT}^{\cos(\phi_h-\phi_s)} \propto g_{1T}^{q} \otimes D_{1q}^{h}$, "Worm Gear" PDF g_{1T}^{q} :

Results for $A_{LT}^{\cos(\varphi_h-\varphi_S)}$ deuteron & proton 2007



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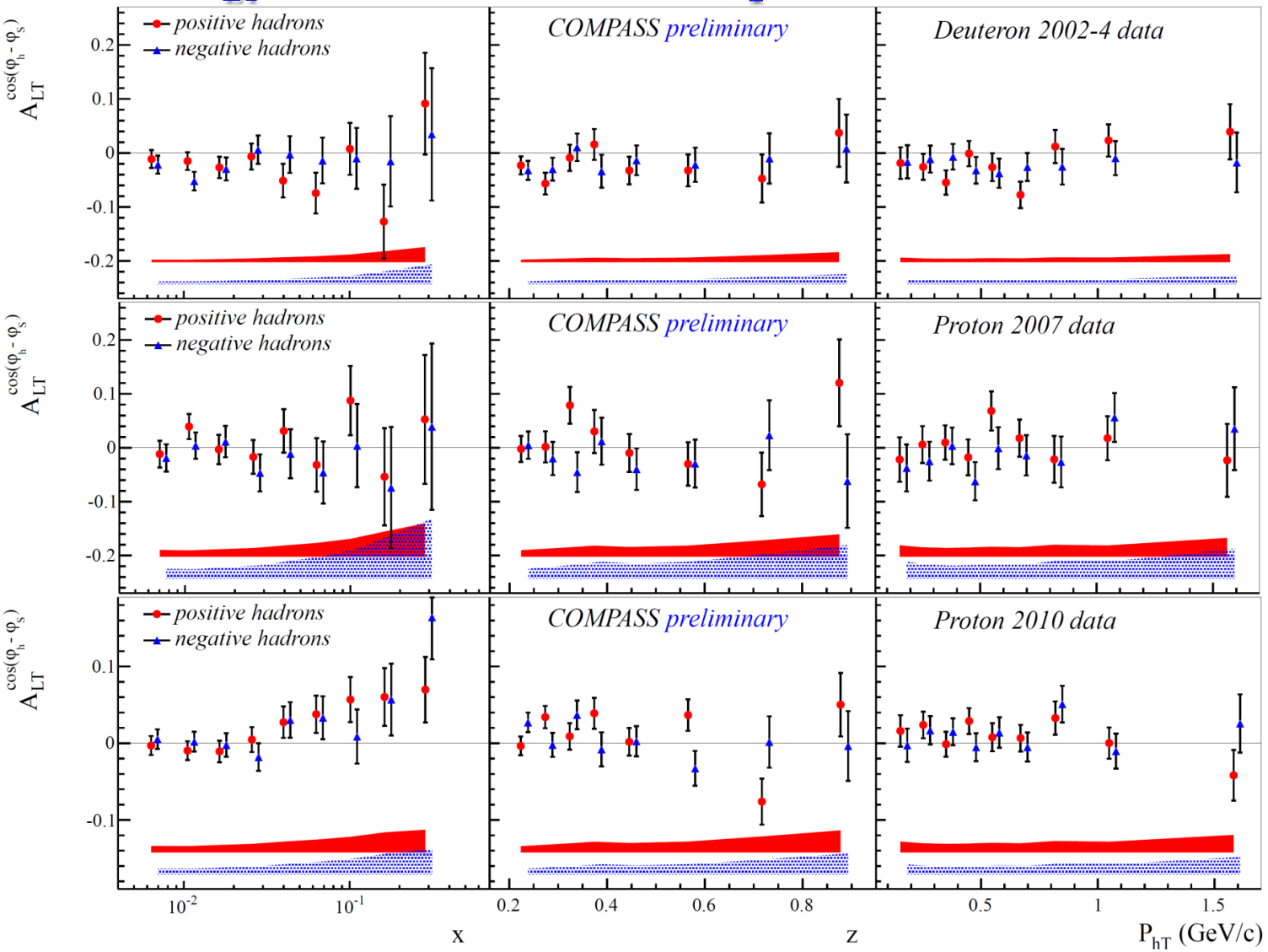
Results for $A_{LT}^{\cos(\varphi_h-\varphi_S)}$ deuteron & proton



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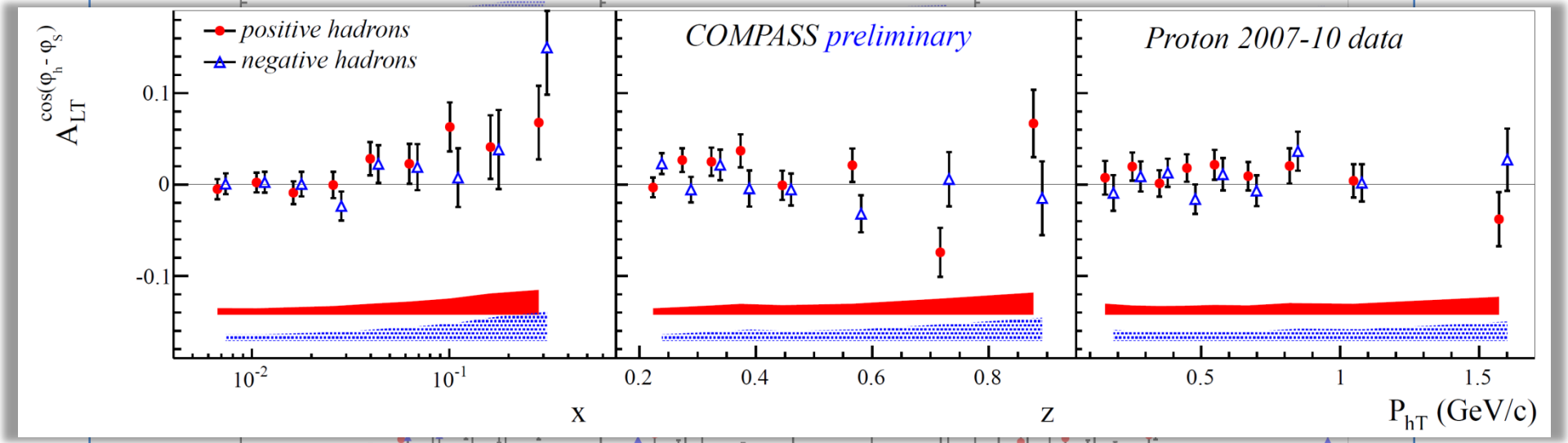
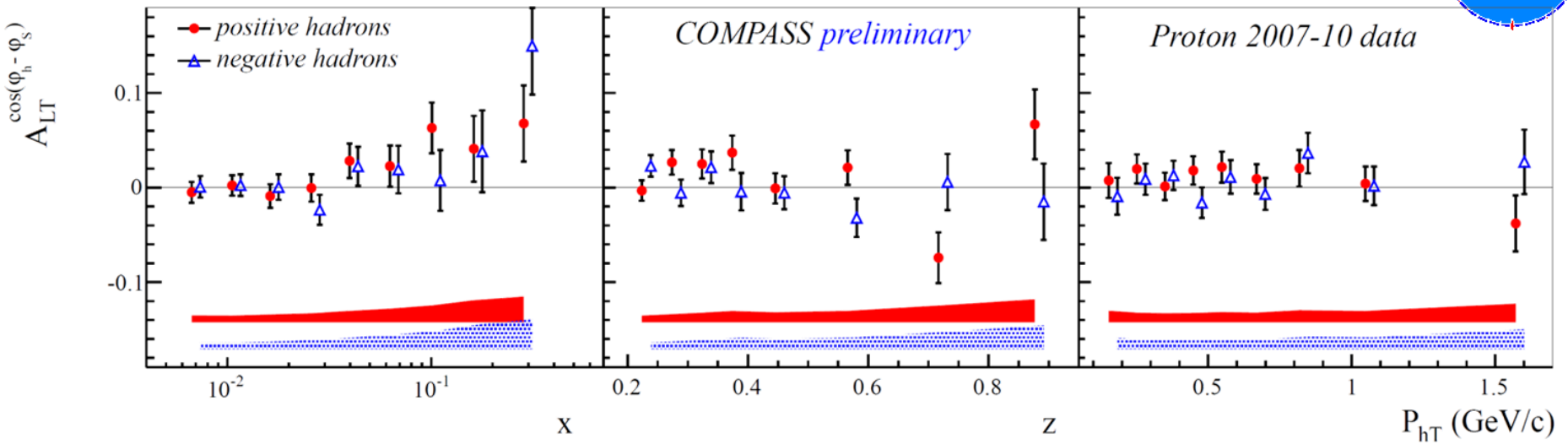
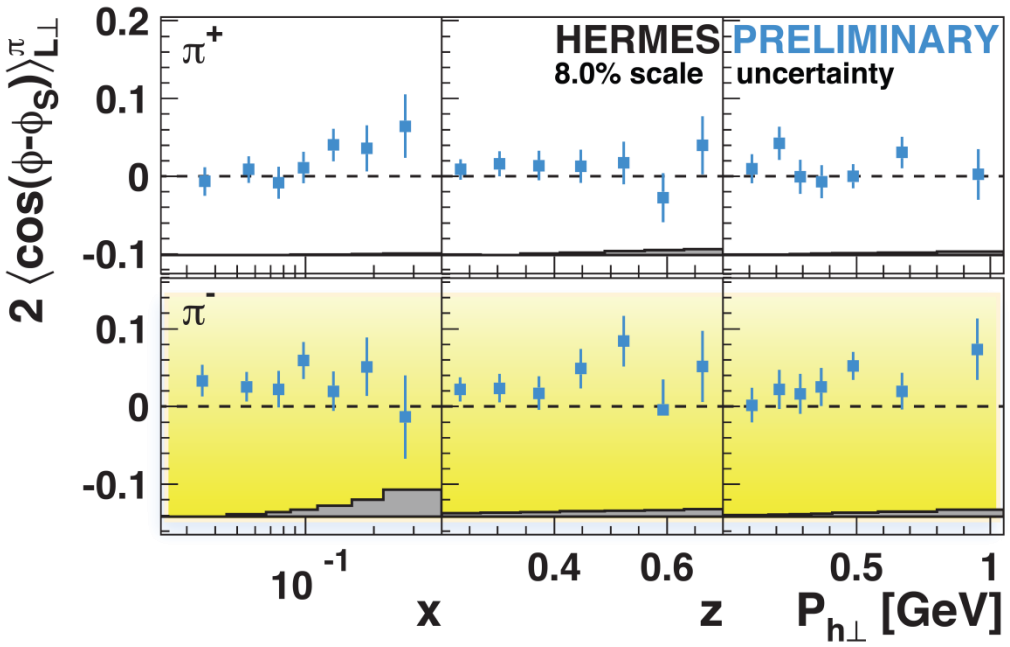
Results for $A_{LT}^{\cos(\varphi_h-\varphi_S)}$ proton 2007-2010



$A_{LT}^{\cos(\phi_h-\phi_s)} \propto g_{1T}^{q} \otimes D_{1q}^{h}$, "Worm Gear" PDF g_{1T}^{q} :

Results for $A_{LT}^{\cos(\varphi_h-\varphi_S)}$ COMPASS - HERMES

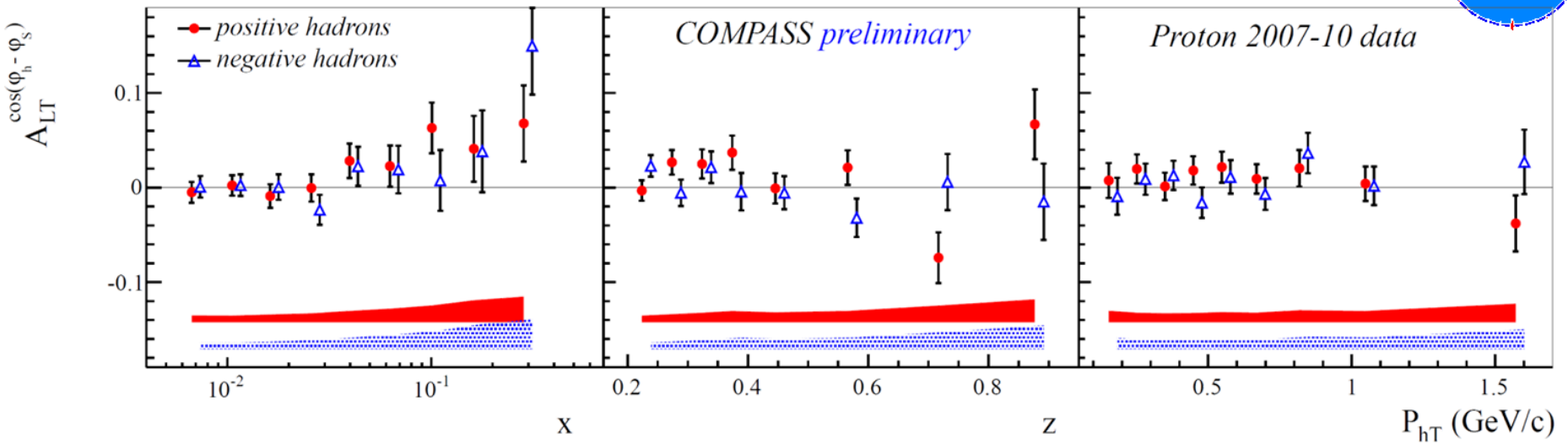




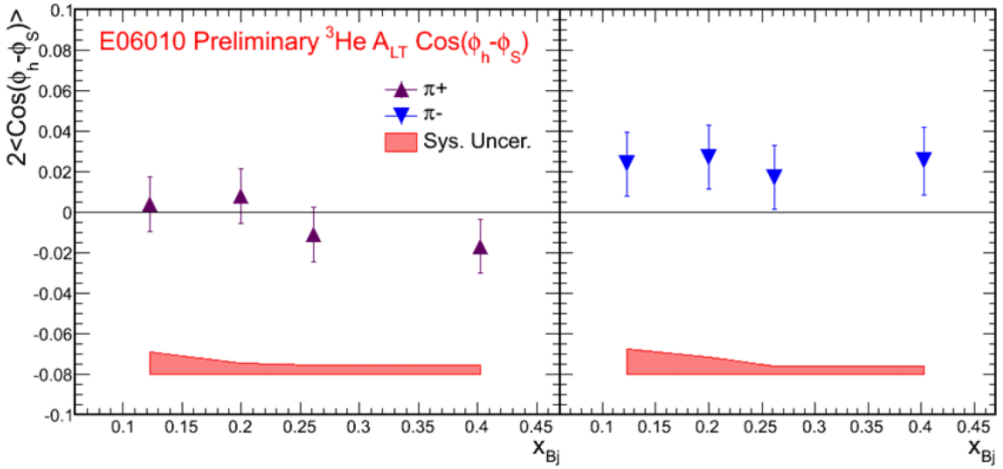
Similar trend for $A_{LT}^{\cos(\varphi_h-\varphi_S)}$ asymmetry is present in HERMES preliminary results.

See next talk by L. Pappalardo

Results for $A_{LT}^{\cos(\varphi_h-\varphi_S)}$ COMPASS - JLab



^{3}He double-spin asymmetry A_{LT}

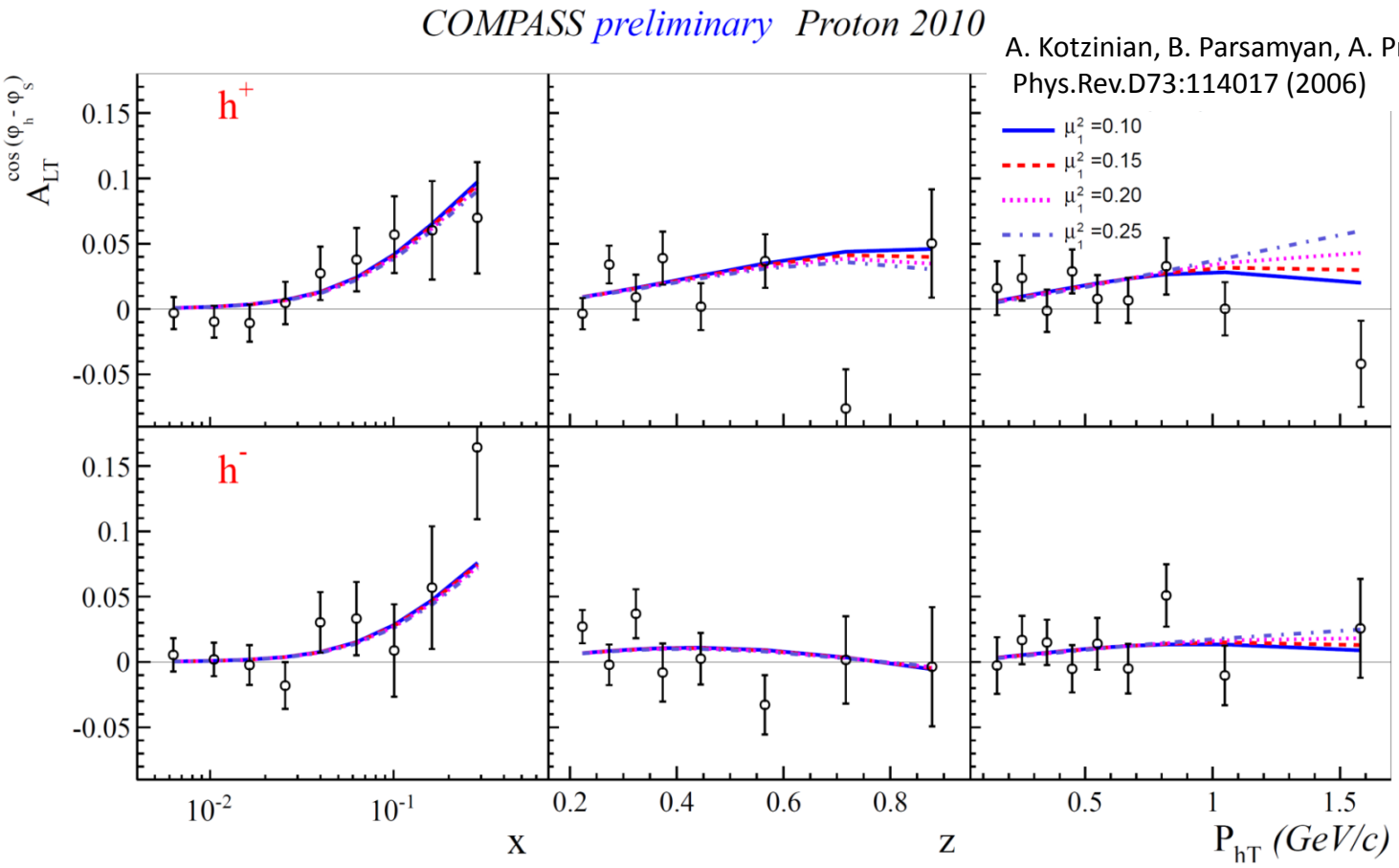


$$\propto \frac{g_{1T}^{\perp q}(x) \otimes D_{1q}^{h}(z)}{f_1^q(x) \otimes D_{1q}^{h}(z)}$$

- First observation of a none-zero A_{LT}.
- First measurement on neutron(^{3}He).
- Relate to quark TMD $g_{1T}(x, k_T)$.
- The real part of quark L=0 ✖ L=1 interference, "twin-brother" of Sivers.

Ph.D. thesis of J. Huang (MIT 2011).

$A_{LT}^{\cos(\varphi_h-\varphi_S)}$ and predictions from PRD 73, 114017(2006)



A. Kotzinian, B. Parsamyan, A. Prokudin
Phys.Rev.D73:114017 (2006)

Calculations are done using:
for g_{1T} the model:

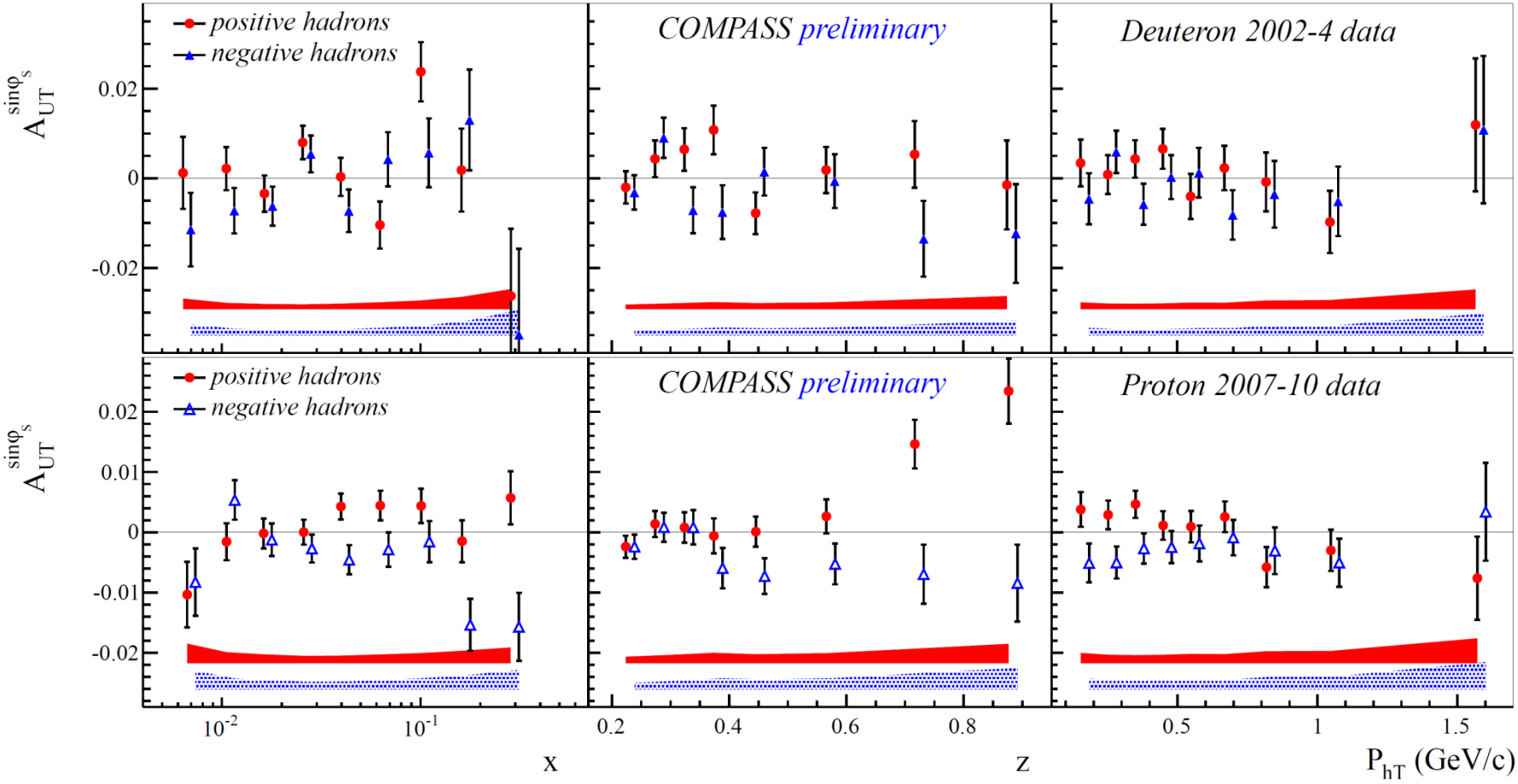
$$g_{1T}^{q(1)}(x,k_T^2) \approx x\int_x^1 dy \frac{g_1^q(y)}{y}$$

based on the Wandzura and Wilczek approximation;
Gaussian parameterization for k_T dependence;
LO GRV, GRSV2000 DFs and Kretzer FFs

Asymmetry is evaluated in COMPASS specific mean kinematic points extracted from the data.
The predictions shows a good level of agreement with the experimentally extracted asymmetry

$A_{LT}^{\cos(\phi_h-\phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$, "Worm Gear" PDF g_{1T}^q :

Results for $A_{UT}^{\sin\varphi_S}$ on deuteron and proton

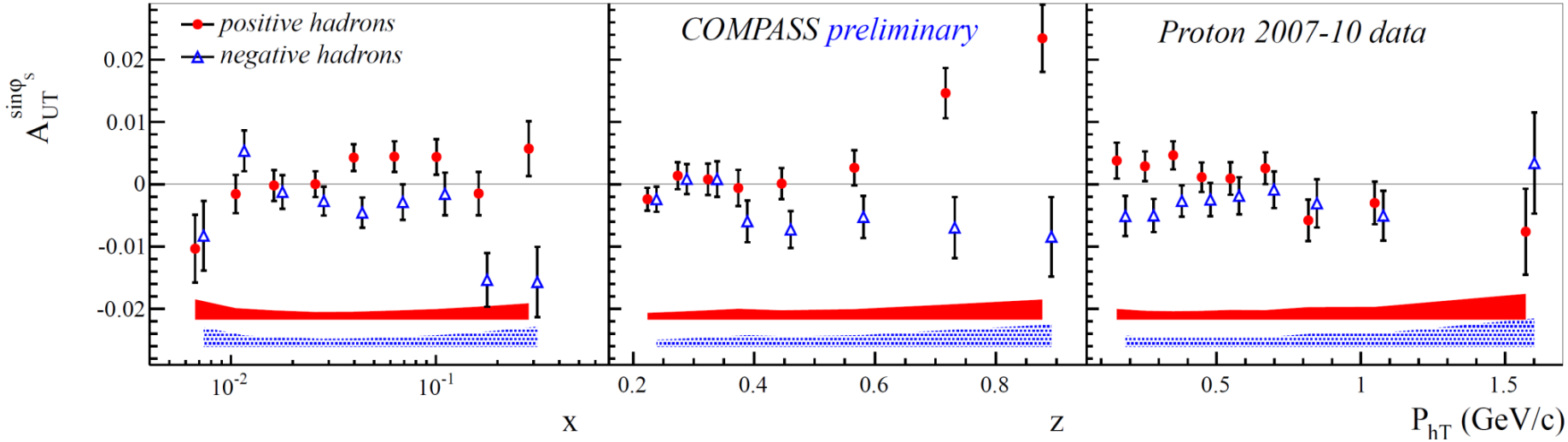


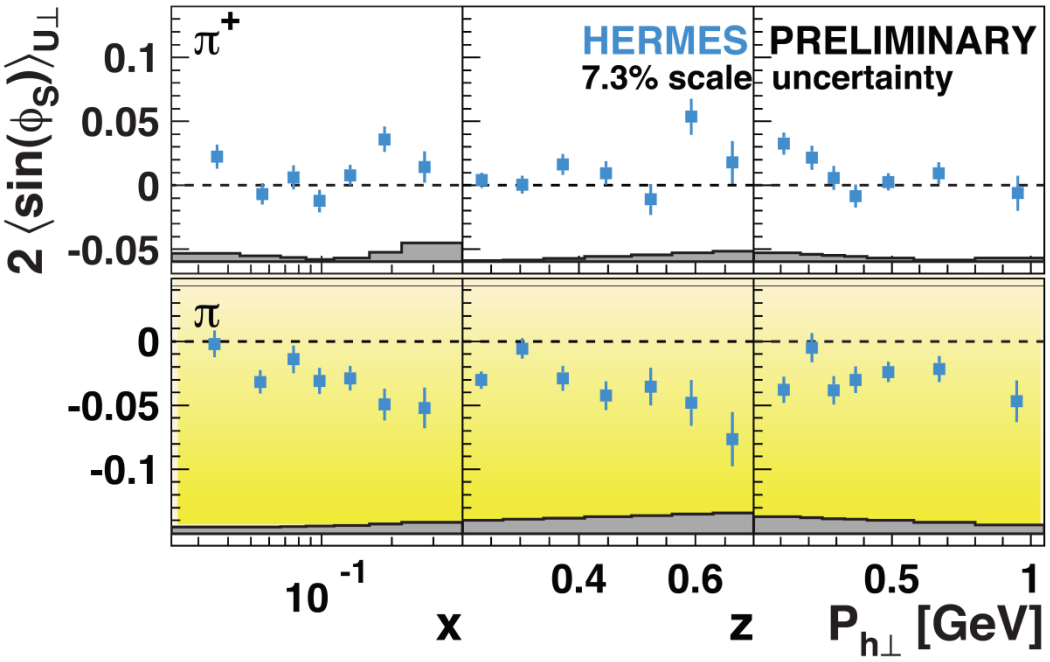
$$A_{UT}^{\sin\phi_s} \propto \frac{M}{Q}\left(h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^{h} + \ldots\right)$$

"Transversity" PDF h_1^q :

"Sivers" PDF $f_{1T}^{\perp q}$:

Results for $A_{UT}^{\sin\varphi_S}$ COMPASS - HERMES

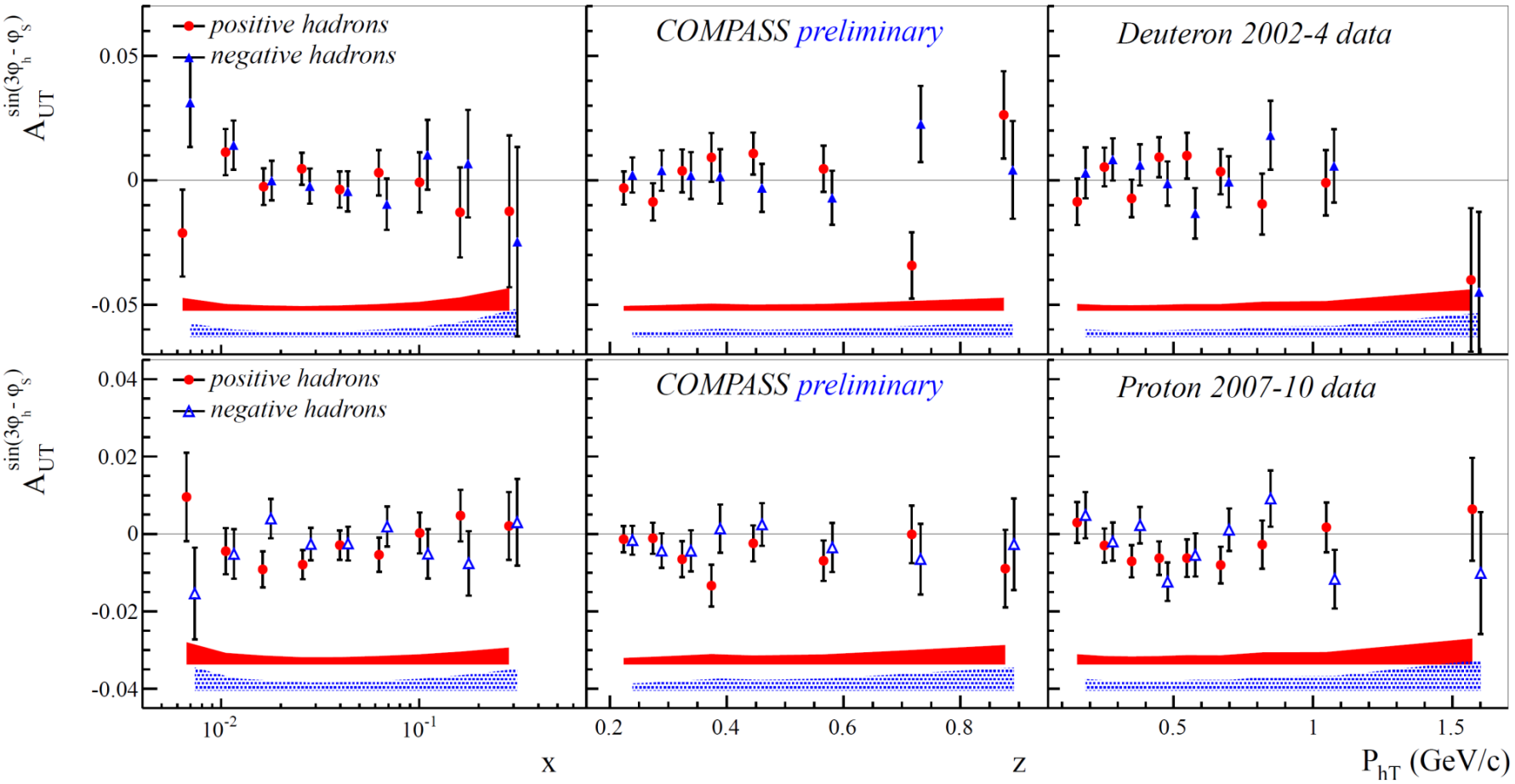




Signs of a non-zero $A_{UT}^{\sin\varphi_S}$ asymmetry have been observed both by HERMES and COMPASS.

See next talk by L. Pappalardo

Results for $A_{UT}^{\sin(3\varphi_h-\varphi_S)}$ deuteron & proton

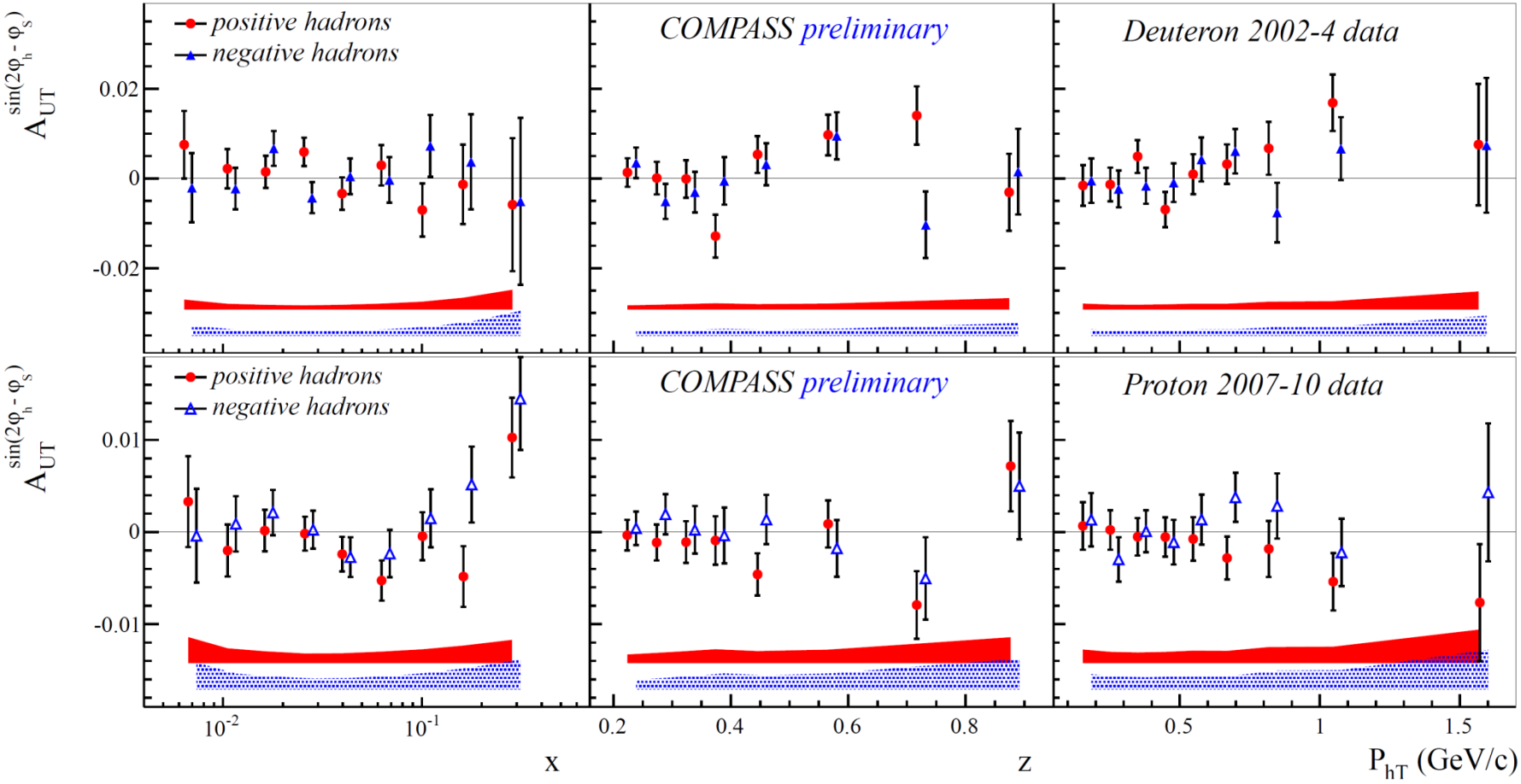


$A_{UT}^{\sin(3\phi_h-\phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$, "Pretzelosity" PDF $h_{1T}^{\perp q}$:

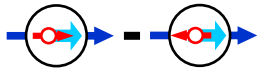
Expected to be suppressed by a factor of ~$|\mathbf{P_{hT}}|^2$ with respect to the Collins and Sivers amplitudes

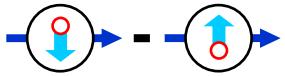
Asymmetries for both proton and deuteron are compatible with zero within uncertainties

Results for $A_{UT}^{\sin(2\varphi_h-\varphi_S)}$ deuteron & proton



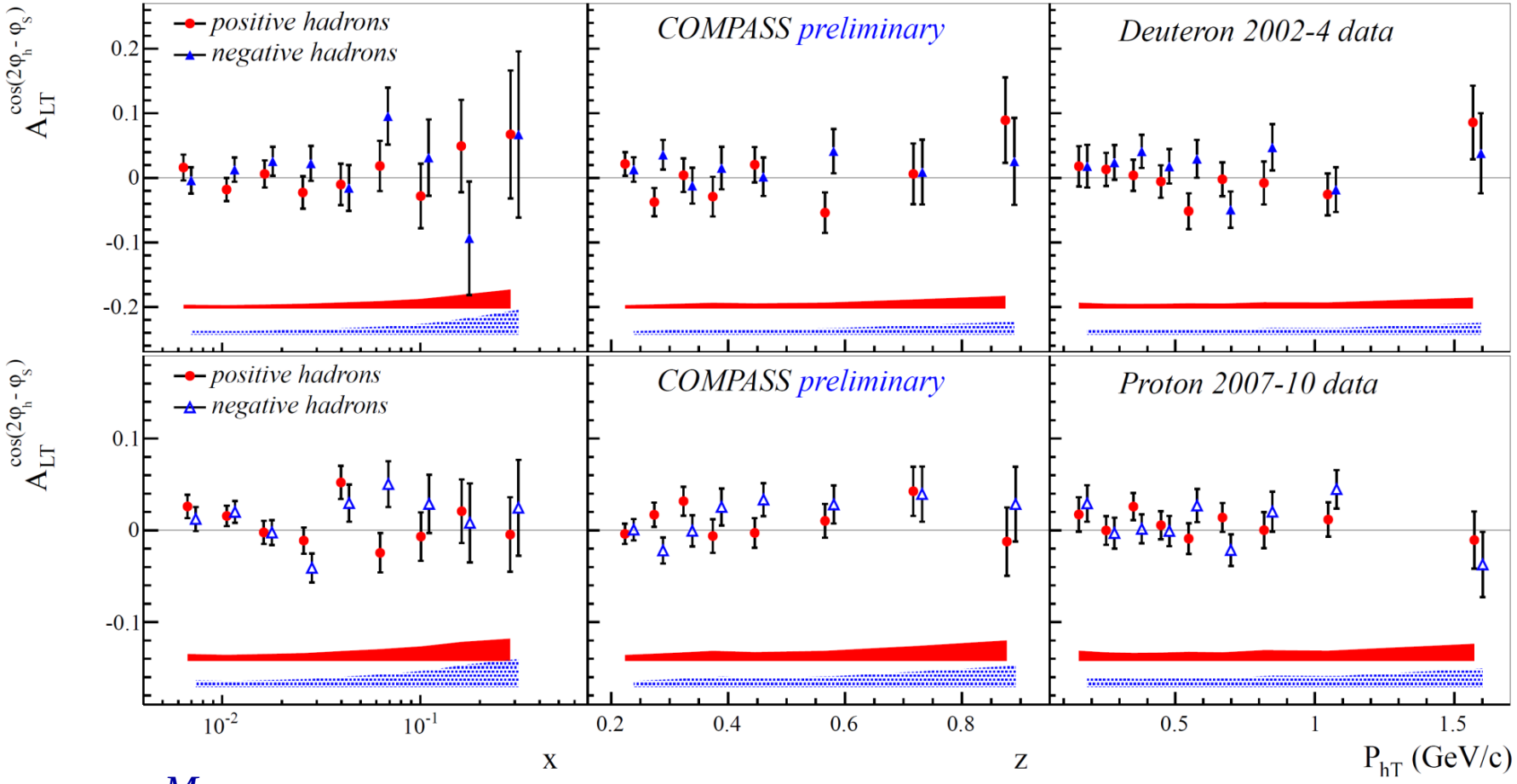
$$A_{UT}^{\sin(2\phi_h-\phi_s)} \propto \frac{M}{Q}\left(h_{1T}^{\perp q}\otimes H_{1q}^{\perp h} + f_{1T}^{\perp q}\otimes D_{1q}^{h} + \ldots\right)$$

"Pretzelosity" PDF $h_{1T}^{\perp q}$: 

"Sivers" PDF $f_{1T}^{\perp q}$: 

At low $|\mathbf{P_{hT}}|$ expected to be suppressed by a factor of ~$|\mathbf{P_{hT}}|$ with respect to the Collins and Sivers
Asymmetries for both proton and deuteron are compatible with zero within uncertainties

Results for $A_{LT}^{\cos(2\varphi_h-\varphi_S)}$ deuteron & proton



$$A_{LT}^{\cos(2\phi_h-\phi_s)} \propto \frac{M}{Q}\left(g_{1T}^{q} \otimes D_{1q}^{h} + \ldots\right),$$ "Worm Gear" PDF g_{1T}^{q} :

At low $|\mathbf{P_{hT}}|$ expected to be suppressed by a factor of ~$|\mathbf{P_{hT}}|$ with respect to the Collins and Sivers
Asymmetries for both proton and deuteron are compatible with zero within uncertainties

Outline

- Introduction
- COMPASS experiment
- **Measured asymmetries and theory expectations**
  - Re-evaluation of $A_{LT}^{\cos\varphi_S}$ and $A_{LT}^{\cos(\varphi_h - \varphi_S)}$: from the lp to $\gamma^* p$ cross-section
  - Theory expectations
- Summary

SIDIS x-section: from lp to $\gamma^* p$ (P_L=0)

Kotzinian et al.
hep-ph/9808368 (1998)
hep-ph/9908466 (1999)
M. Diehl and S. Sapeta,
Eur. Phys. J. C 41 (2005) 515

$$\frac{d\sigma}{dx dy dz dP_{hT}^2 d\varphi_h d\varphi_S} = \left[\frac{\cos\theta}{1-\sin^2\theta\sin^2\varphi_S}\right]\times\left[\frac{\alpha}{xyQ^2}\frac{y^2}{2(1-\varepsilon)}\left(1+\frac{\gamma^2}{2x}\right)\right]\times\left(F_{UU,T}+\varepsilon F_{UU,L}\right)\times$$

$$\left[1+\cos\varphi_h\times\sqrt{2\varepsilon(1+\varepsilon)}A_{UU}^{\cos\varphi_h}+\cos(2\varphi_h)\times\varepsilon A_{UU}^{\cos(2\varphi_h)}+\lambda\sin\varphi_h\times\sqrt{2\varepsilon(1-\varepsilon)}A_{LU}^{\sin\varphi_h}+\right.$$

$$\frac{P_T}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}}\left[\sin\varphi_S\times\left(\cos\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin\varphi_S}\right)+\right.$$

$$\sin(\varphi_h-\varphi_S)\times\left(\cos\theta A_{UT}^{\sin(\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UL}^{\sin\varphi_h}\right)+$$

$$\sin(\varphi_h+\varphi_S)\times\left(\cos\theta\varepsilon A_{UT}^{\sin(\varphi_h+\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UL}^{\sin\varphi_h}\right)+$$

$$\sin(2\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin(2\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\varepsilon A_{UL}^{\sin 2\varphi_h}\right)+$$

$$\sin(3\varphi_h-\varphi_S)\times\left(\cos\theta\varepsilon A_{UT}^{\sin(3\varphi_h-\varphi_S)}\right)+$$

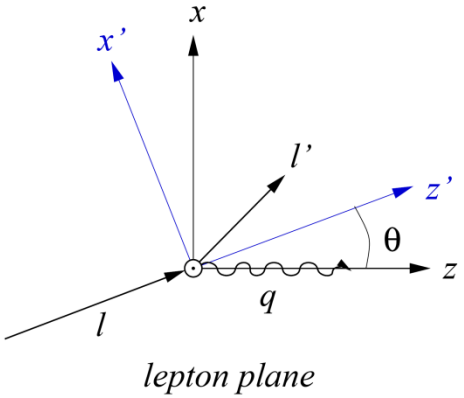
$$\left.\left.\sin(2\varphi_h+\varphi_S)\times\left(\frac{1}{2}\sin\theta\varepsilon A_{UL}^{\sin 2\varphi_h}\right)\right]+\right.$$

$$\frac{P_T\lambda}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}}\left[\cos\varphi_S\times\left(\cos\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos\varphi_S}+\sin\theta\sqrt{(1-\varepsilon^2)}A_{LL}\right)+\right.$$

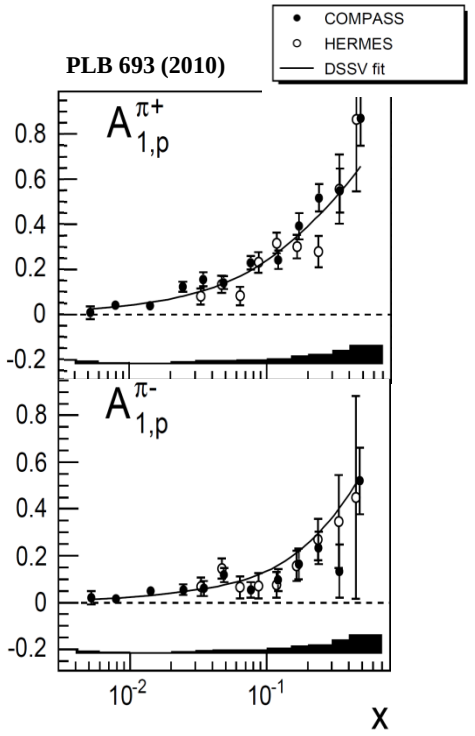
$$\cos(\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{(1-\varepsilon^2)}A_{LT}^{\cos(\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LL}^{\cos\varphi_h}\right)+$$

$$\cos(2\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos(2\varphi_h-\varphi_S)}\right)+$$

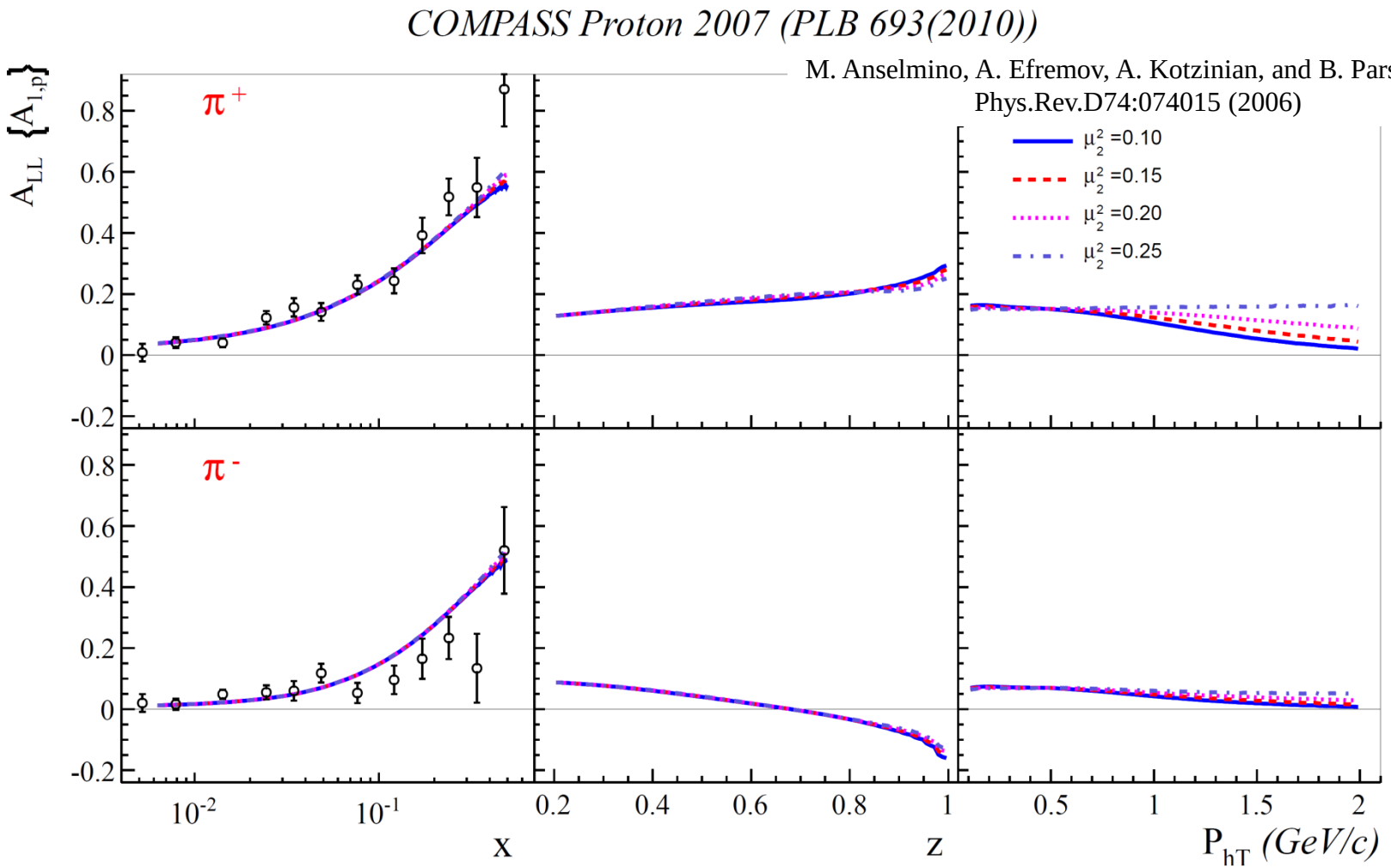
$$\left.\left.\cos(\varphi_h+\varphi_S)\times\left(\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LL}^{\cos\varphi_h}\right)\right]\right]$$



lepton plane



A_{LL} evaluated according to the PRD **74,** 074015 (2006)

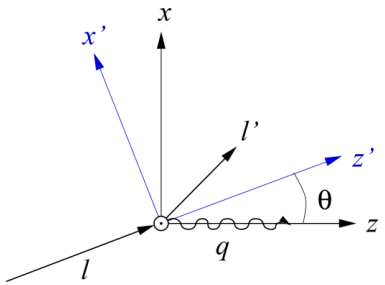


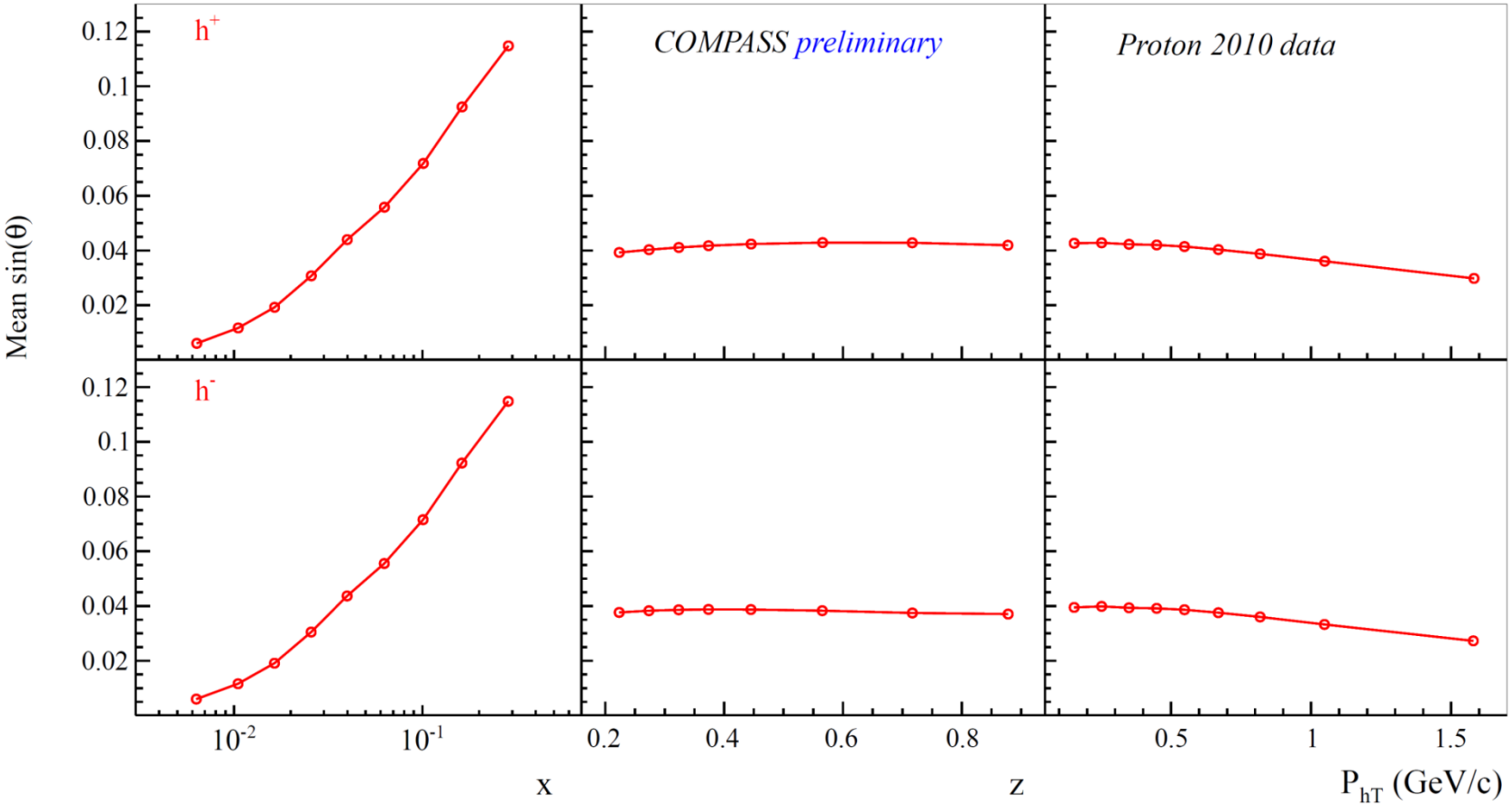
Asymmetry is evaluated in COMPASS specific mean kinematic points extracted from the data.
Good level of agreement up to x≈0.3, which allows us to use the predicted z and P_{hT} – dependencies in $A_{LT}^{\cos(\varphi_S)}$-*correction.*

Mean sinθ-values

$$\sin\theta = \gamma\sqrt{\frac{1-y-\frac{1}{4}\gamma^2y^2}{1+\gamma^2}},\ \gamma=\frac{2Mx}{Q};$$

$$\theta \xrightarrow[\text{Bjorken limit}]{} 0 \Rightarrow S_T \simeq P_T,\ S_L \simeq P_L$$



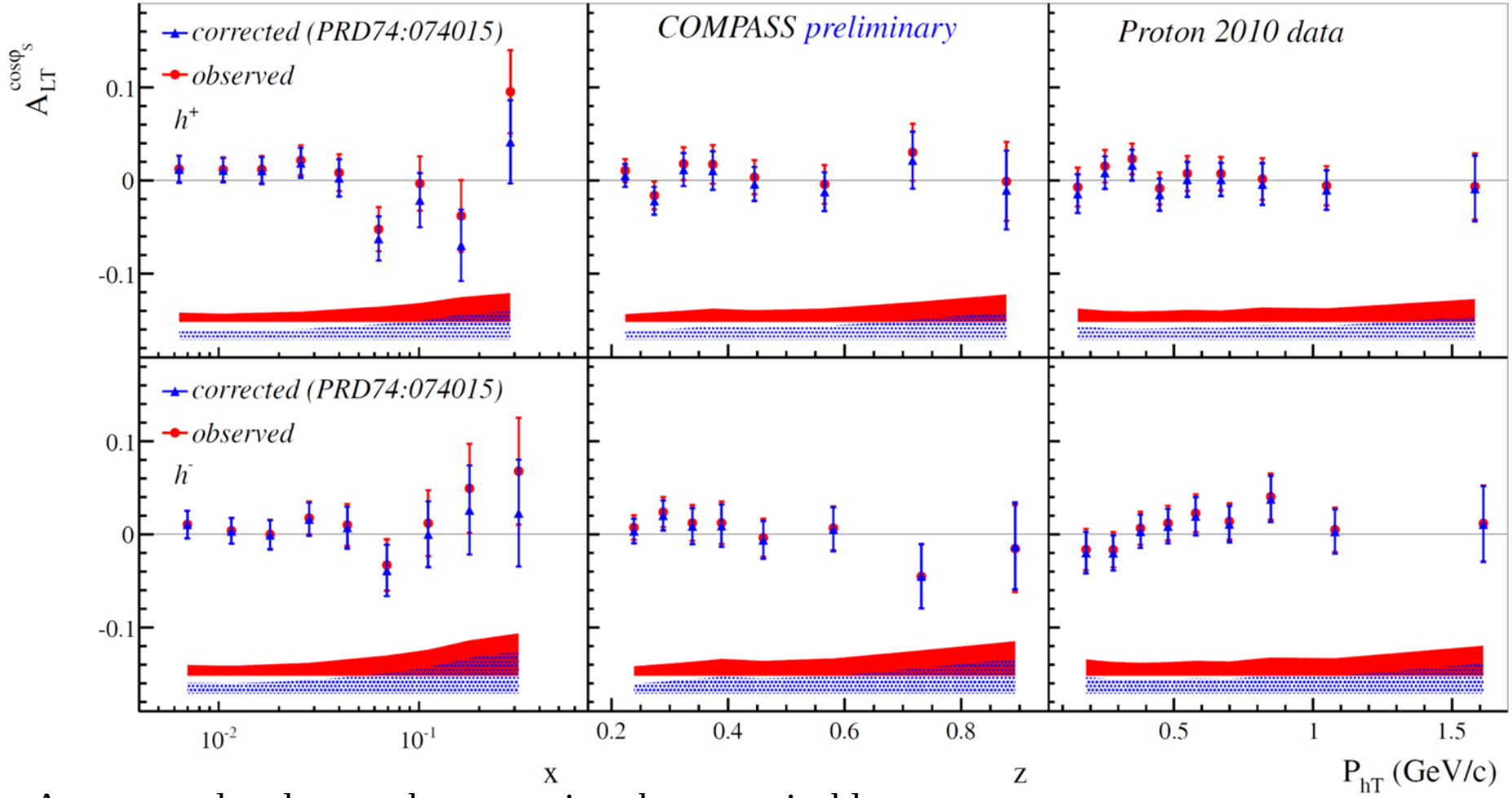


The sinθ is small at COMPASS kinematics. The maximum reached value is ~ 0.12 and the mean is around 0.04 (cosθ ≈ 1).

$A_{LT}^{\cos\varphi_S}$ corrected for A_{LL}-contribution

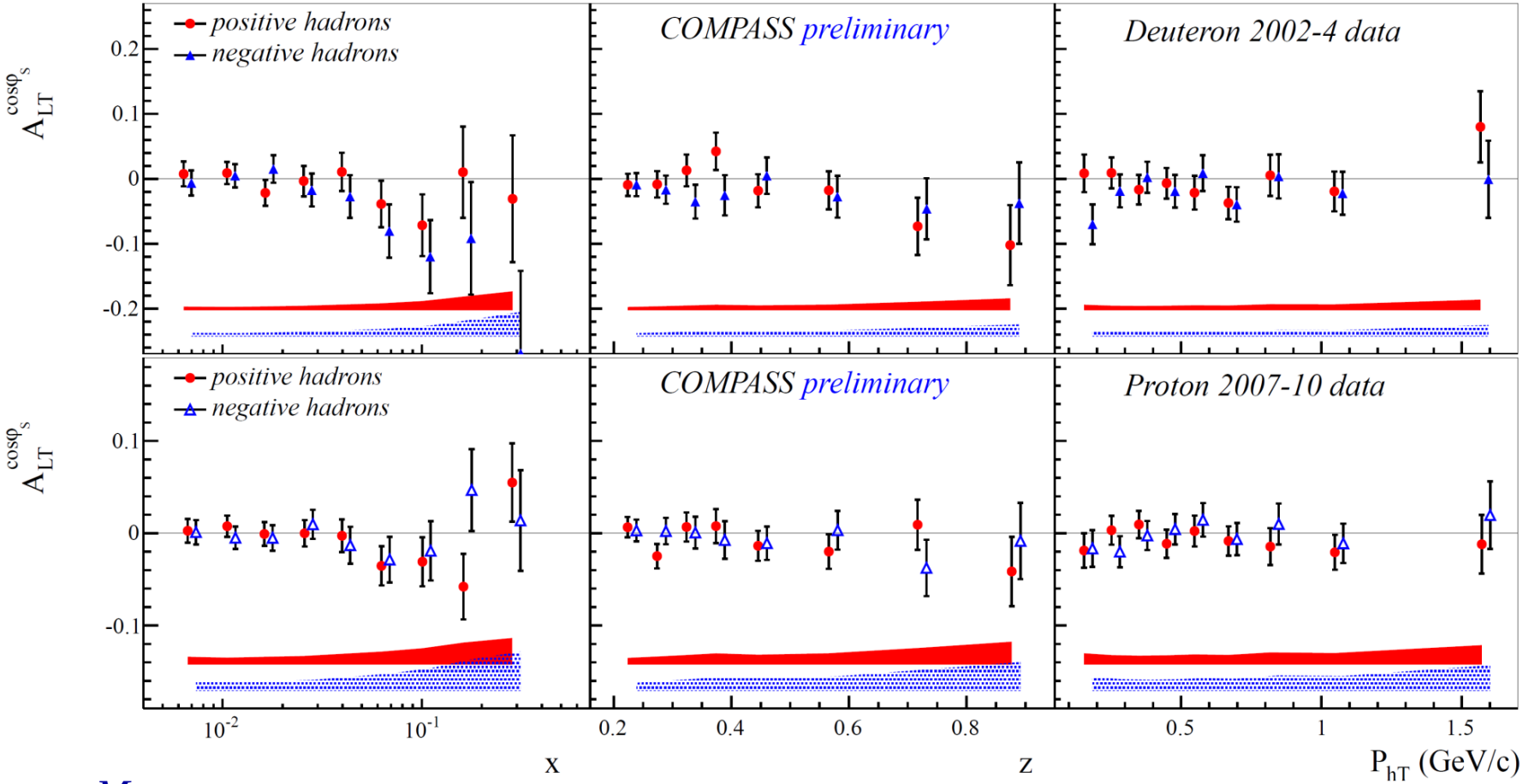
using A_{LL} from PRD **74,** 074015(2006)

$$A_{LT}^{\cos\varphi_S}{}' \approx \left(\cos\theta A_{LT}^{\cos\varphi_S} - \sin\theta \frac{\sqrt{(1-\varepsilon^2)}}{\sqrt{2\varepsilon(1-\varepsilon)}} A_{LL} \right)$$



As expected, at large *x* the corrections become sizable.

Results for $A_{LT}^{\cos\varphi_S}$ deuteron & proton



$$A_{LT}^{\cos\phi_s} \propto \frac{M}{Q}\left(g_{1T}^{q} \otimes D_{1q}^{h} + \ldots\right),$$ "Worm Gear" PDF g_{1T}^{q} :

Asymmetries for both proton and deuteron are compatible with zero within uncertainties

SIDIS x-section: from *lp* to $\gamma^* p$ (P_L=0)

Kotzinian et al.
hep-ph/9808368 (1998)
hep-ph/9908466 (1999)
M. Diehl and S. Sapeta,
Eur. Phys. J. C 41 (2005) 515

$$\frac{d\sigma}{dx dy dz dP_{hT}^2 d\varphi_h d\varphi_S} = \left[\frac{\cos\theta}{1-\sin^2\theta\sin^2\varphi_S}\right]\times\left[\frac{\alpha}{xyQ^2}\frac{y^2}{2(1-\varepsilon)}\left(1+\frac{\gamma^2}{2x}\right)\right]\times\left(F_{UU,T}+\varepsilon F_{UU,L}\right)\times$$

$$\left[1+\cos\varphi_h\times\sqrt{2\varepsilon(1+\varepsilon)}A_{UU}^{\cos\varphi_h}+\cos(2\varphi_h)\times\varepsilon A_{UU}^{\cos(2\varphi_h)}+\lambda\sin\varphi_h\times\sqrt{2\varepsilon(1-\varepsilon)}A_{LU}^{\sin\varphi_h}+\right.$$

$$\frac{P_T}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}}\left[\sin\varphi_S\times\left(\cos\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin\varphi_S}\right)+\right.$$

$$\sin(\varphi_h-\varphi_S)\times\left(\cos\theta A_{UT}^{\sin(\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UL}^{\sin\varphi_h}\right)+$$

$$\sin(\varphi_h+\varphi_S)\times\left(\cos\theta\varepsilon A_{UT}^{\sin(\varphi_h+\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UL}^{\sin\varphi_h}\right)+$$

$$\sin(2\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin(2\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\varepsilon A_{UL}^{\sin 2\varphi_h}\right)+$$

$$\sin(3\varphi_h-\varphi_S)\times\left(\cos\theta\varepsilon A_{UT}^{\sin(3\varphi_h-\varphi_S)}\right)+$$

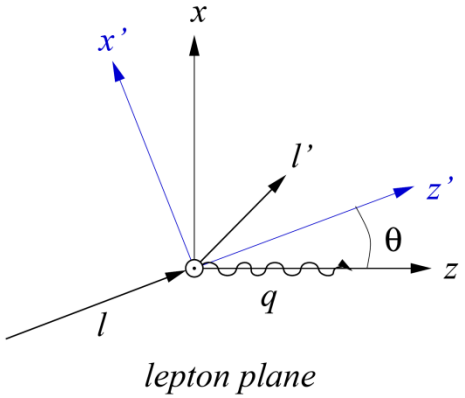
$$\left.\left.\sin(2\varphi_h+\varphi_S)\times\left(\frac{1}{2}\sin\theta\varepsilon A_{UL}^{\sin 2\varphi_h}\right)\right]+\right.$$

$$\frac{P_T\lambda}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}}\left[\cos\varphi_S\times\left(\cos\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos\varphi_S}+\sin\theta\sqrt{(1-\varepsilon^2)}A_{LL}\right)+\right.$$

$$\cos(\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{(1-\varepsilon^2)}A_{LT}^{\cos(\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LL}^{\cos\varphi_h}\right)+$$

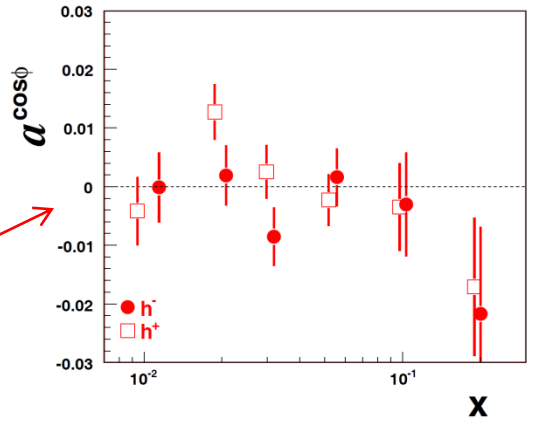
$$\cos(2\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos(2\varphi_h-\varphi_S)}\right)+$$

$$\left.\left.\cos(\varphi_h+\varphi_S)\times\left(\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LL}^{\cos\varphi_h}\right)\right]\right]$$



lepton plane

Eur.Phys.J.C70:39-49,2010



SIDIS x-section: from *lp* to $\gamma^* p$ (P_L=0)

Kotzinian et al.
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$$\frac{d\sigma}{dx dy dz dP_{hT}^2 d\varphi_h d\varphi_S} = \left[\frac{\cos\theta}{1-\sin^2\theta\sin^2\varphi_S}\right]\times\left[\frac{\alpha}{xyQ^2}\frac{y^2}{2(1-\varepsilon)}\left(1+\frac{\gamma^2}{2x}\right)\right]\times\left(F_{UU,T}+\varepsilon F_{UU,L}\right)\times$$

$$\left[1+\cos\varphi_h\times\sqrt{2\varepsilon(1+\varepsilon)}A_{UU}^{\cos\varphi_h}+\cos(2\varphi_h)\times\varepsilon A_{UU}^{\cos(2\varphi_h)}+\lambda\sin\varphi_h\times\sqrt{2\varepsilon(1-\varepsilon)}A_{LU}^{\sin\varphi_h}+\right.$$

$$\frac{P_T}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}}\left[\sin\varphi_S\times\left(\cos\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin\varphi_S}\right)+\right.$$

$$\sin(\varphi_h-\varphi_S)\times\left(\cos\theta A_{UT}^{\sin(\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UL}^{\sin\varphi_h}\right)+$$

$$\sin(\varphi_h+\varphi_S)\times\left(\cos\theta\varepsilon A_{UT}^{\sin(\varphi_h+\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UL}^{\sin\varphi_h}\right)+$$

$$\sin(2\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{2\varepsilon(1+\varepsilon)}A_{UT}^{\sin(2\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\varepsilon A_{UL}^{\sin 2\varphi_h}\right)+$$

$$\sin(3\varphi_h-\varphi_S)\times\left(\cos\theta\varepsilon A_{UT}^{\sin(3\varphi_h-\varphi_S)}\right)+$$

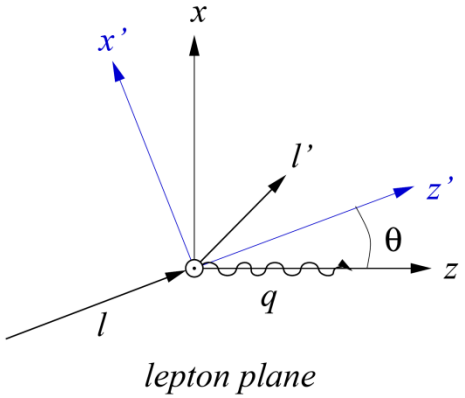
$$\left.\left.\sin(2\varphi_h+\varphi_S)\times\left(\frac{1}{2}\sin\theta\varepsilon A_{UL}^{\sin 2\varphi_h}\right)\right]+\right.$$

$$\frac{P_T\lambda}{\sqrt{1-\sin^2\theta\sin^2\varphi_S}}\left[\cos\varphi_S\times\left(\cos\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos\varphi_S}+\sin\theta\sqrt{(1-\varepsilon^2)}A_{LL}\right)+\right.$$

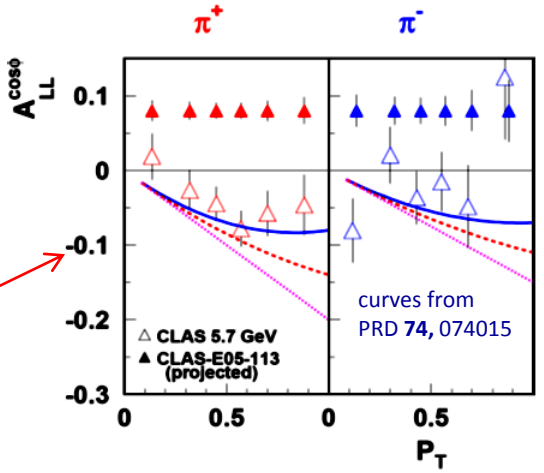
$$\cos(\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{(1-\varepsilon^2)}A_{LT}^{\cos(\varphi_h-\varphi_S)}+\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LL}^{\cos\varphi_h}\right)+$$

$$\cos(2\varphi_h-\varphi_S)\times\left(\cos\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LT}^{\cos(2\varphi_h-\varphi_S)}\right)+$$

$$\left.\cos(\varphi_h+\varphi_S)\times\left(\frac{1}{2}\sin\theta\sqrt{2\varepsilon(1-\varepsilon)}A_{LL}^{\cos\varphi_h}\right)\right]$$

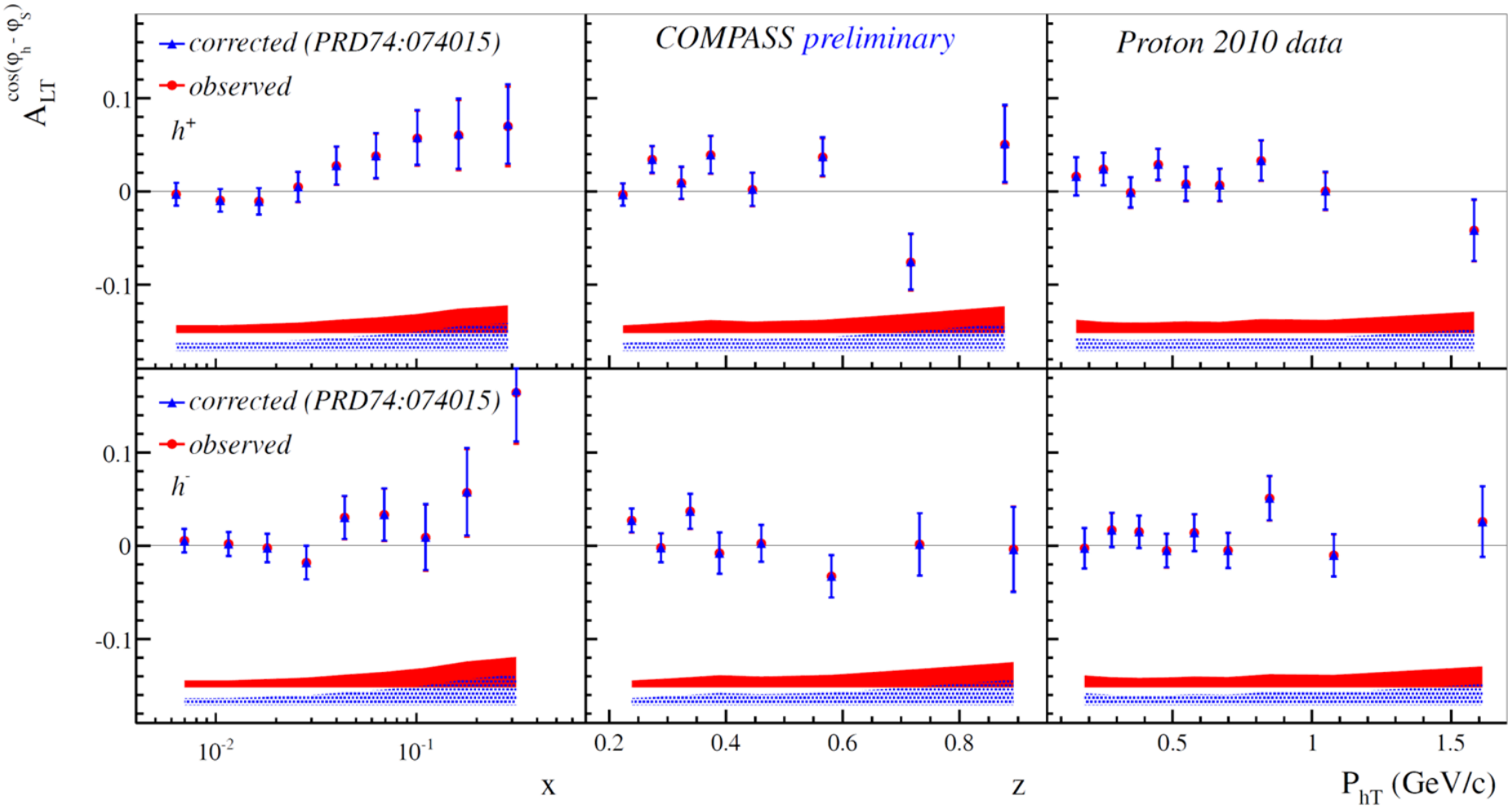


lepton plane



$A_{LT}^{\cos(\varphi_h - \varphi_S)}$ corrected for $A_{LL}^{\cos\varphi_h}$-contribution

using $A_{LL}^{\cos\varphi_h}$ from PRD **74,** 074015(2006)



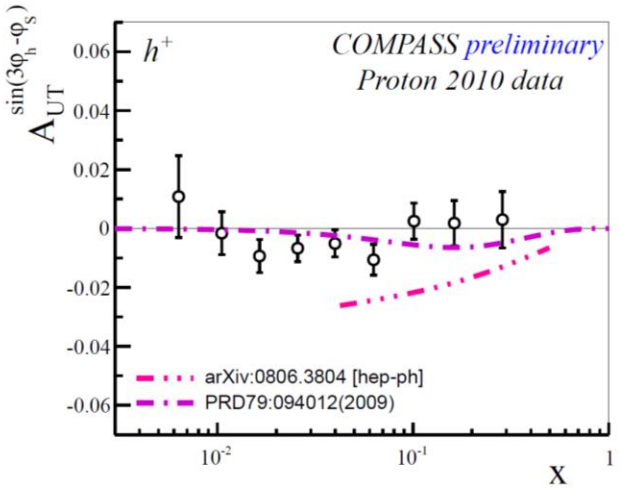
$A_{LL}^{\cos\varphi_h}$ contribution to the $A_{LT}^{\cos(\varphi_s - \varphi_h)}$ is negligible

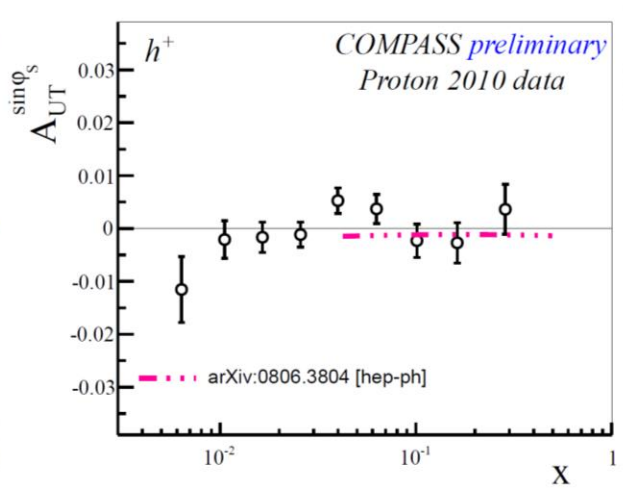
Outline

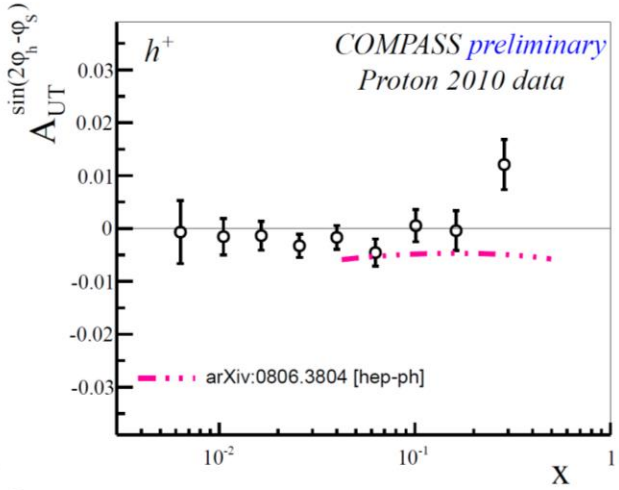
- Introduction
- COMPASS experiment
- **Measured asymmetries and theory expectations**
  - Re-evaluation of $A_{LT}^{\cos\varphi_S}$ and $A_{LT}^{\cos(\varphi_h - \varphi_S)}$: from the lp to $\gamma^* p$ cross-section
  - **Theory expectations**
- Summary

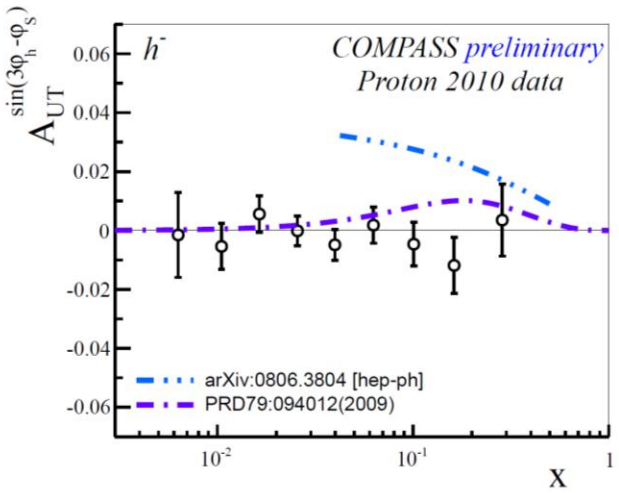
“UT” asymmetries and theoretical predictions x-dependence only

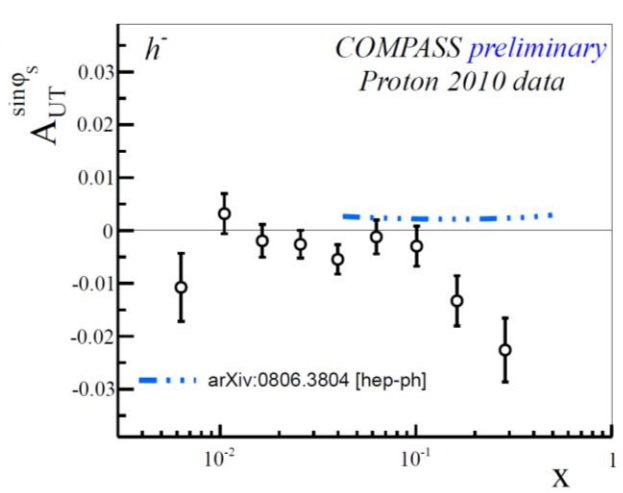
S. Boffi, A.V. Efremov, B. Pasquini and P. Schweitzer PRD79:094012(2009)
A. Kotzinian arXiv:0806.3804[hep-ph]

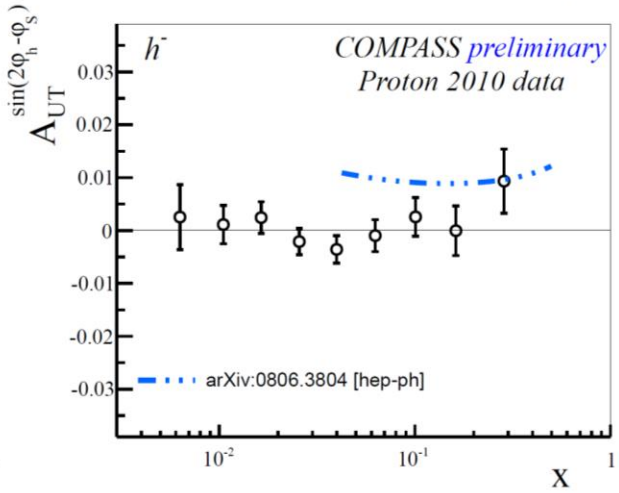






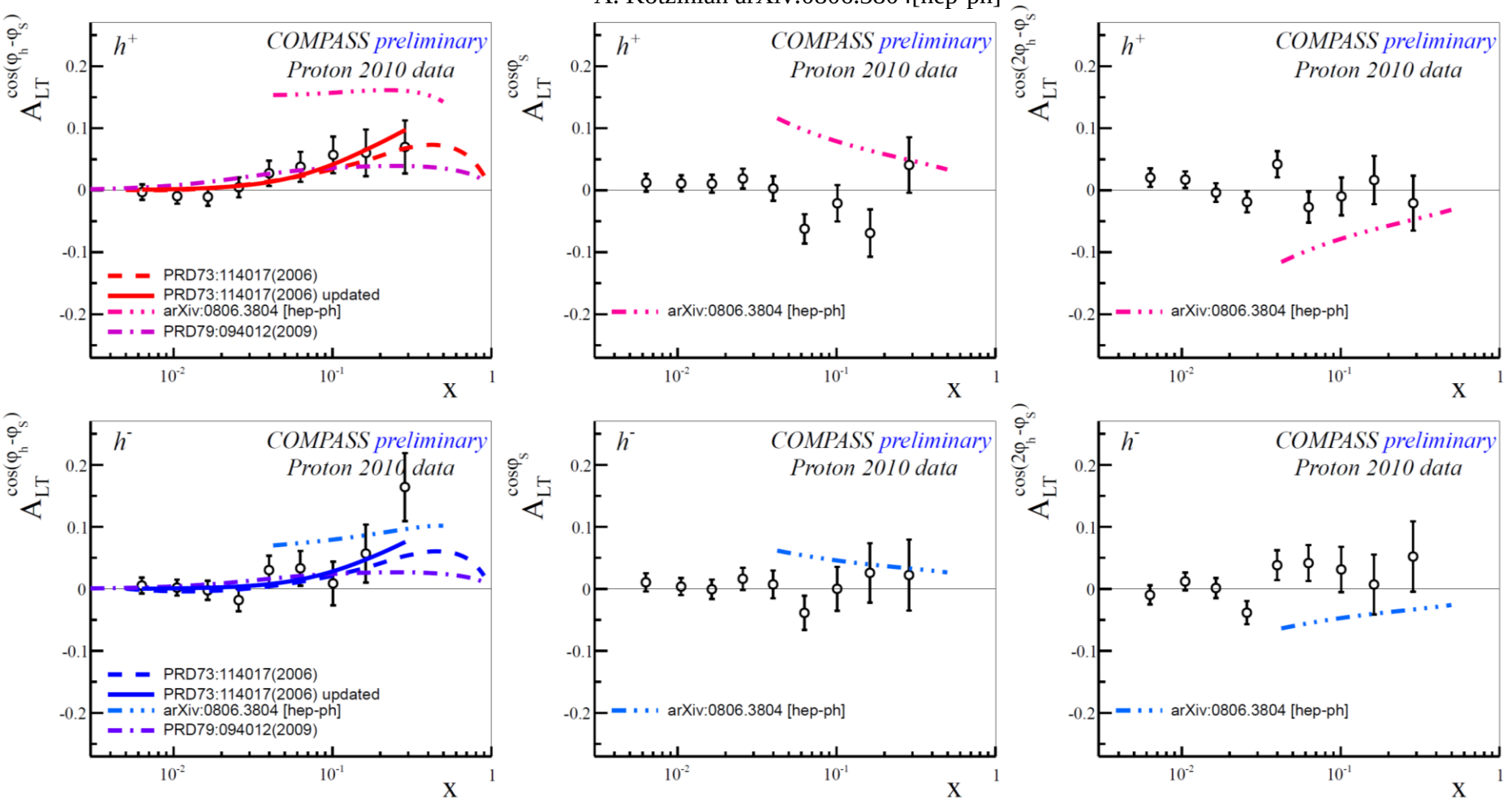






“LT” asymmetries and theoretical predictions x-dependence only

A. Kotzinian, B. Parsamyan, A. Prokudin Phys.Rev.D73:114017 (2006)
S. Boffi, A.V. Efremov, B. Pasquini and P. Schweitzer PRD79:094012(2009)
A. Kotzinian arXiv:0806.3804[hep-ph]



The predictions for $A_{LT}^{\cos(\varphi_h-\varphi_S)}$ shows a good level of agreement with the experimentally extracted asymmetry.

Outline

- Introduction
- COMPASS experiment
- Measured asymmetries and theory expectations
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- **Summary**

Summary

- Six "beyond Collins and Sivers" transverse spin asymmetries

$$A_{UT}^{\sin(3\varphi_h-\varphi_s)},\ A_{UT}^{\sin\varphi_s},\ A_{UT}^{\sin(3\varphi_h-\varphi_s)},\ A_{LT}^{\cos(\varphi_h-\varphi_s)},\ A_{LT}^{\cos\varphi_s}\ \&\ A_{LT}^{\cos(2\varphi_h-\varphi_s)}$$

have been extracted from COMPASS deuteron 2002-2004, proton 2007 and now also proton 2010 data.

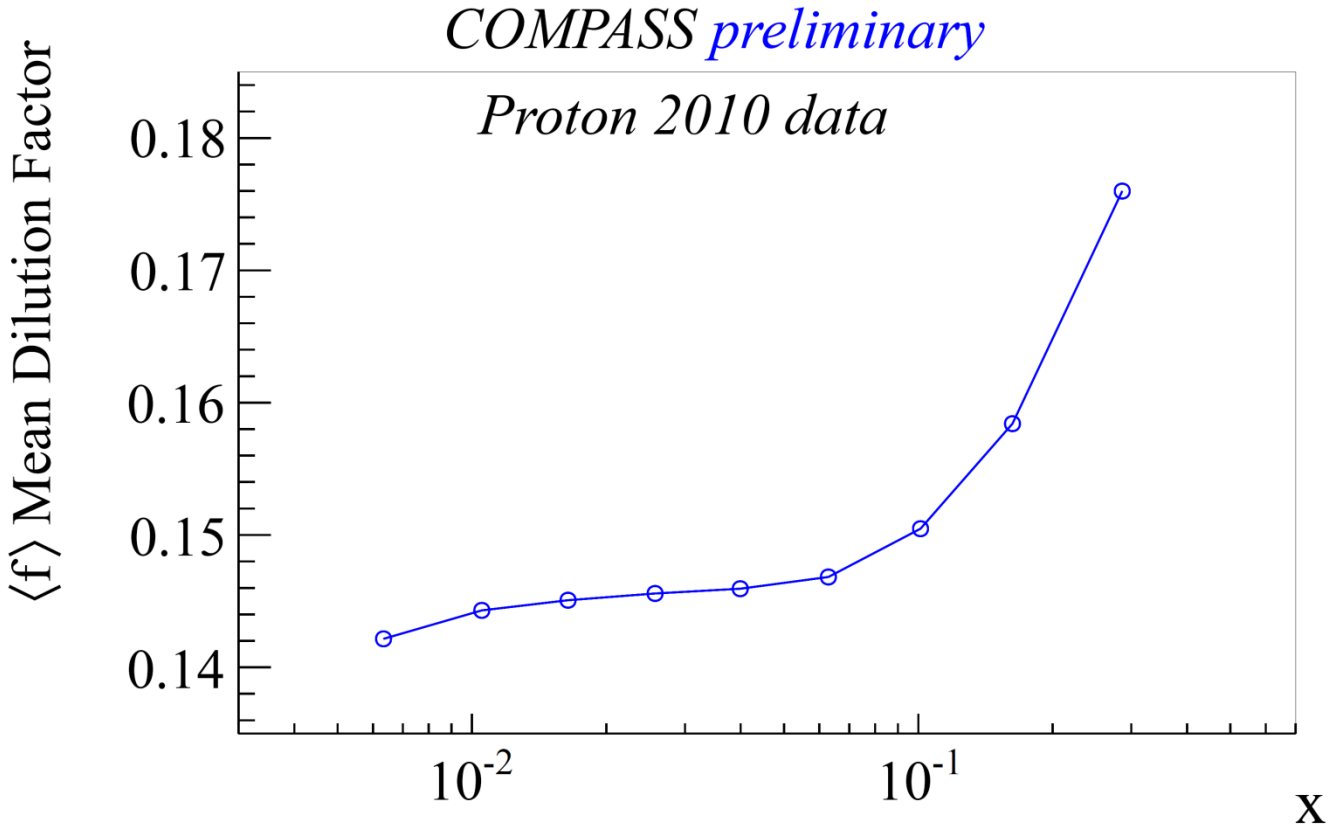
- "Deuteron" and "proton 2007" asymmetries found to be consistent with zero within the statistical accuracy of the measurement.
- Higher statistics and improved quality of the 2010 proton data allowed to reveal a non-zero trend for the $A_{LT}^{\cos(\varphi_h-\varphi_S)}$ and $A_{UT}^{\sin\varphi_S}$ amplitudes.
- Observed effects confirm HERMES preliminary results.
- COMPASS results for the $A_{LT}^{\cos(\varphi_h-\varphi_S)}$ showed a good level of agreement with the theoretical predictions.

- Next → Six asymmetries for pions and kaons.

Thank you!

Spare slides

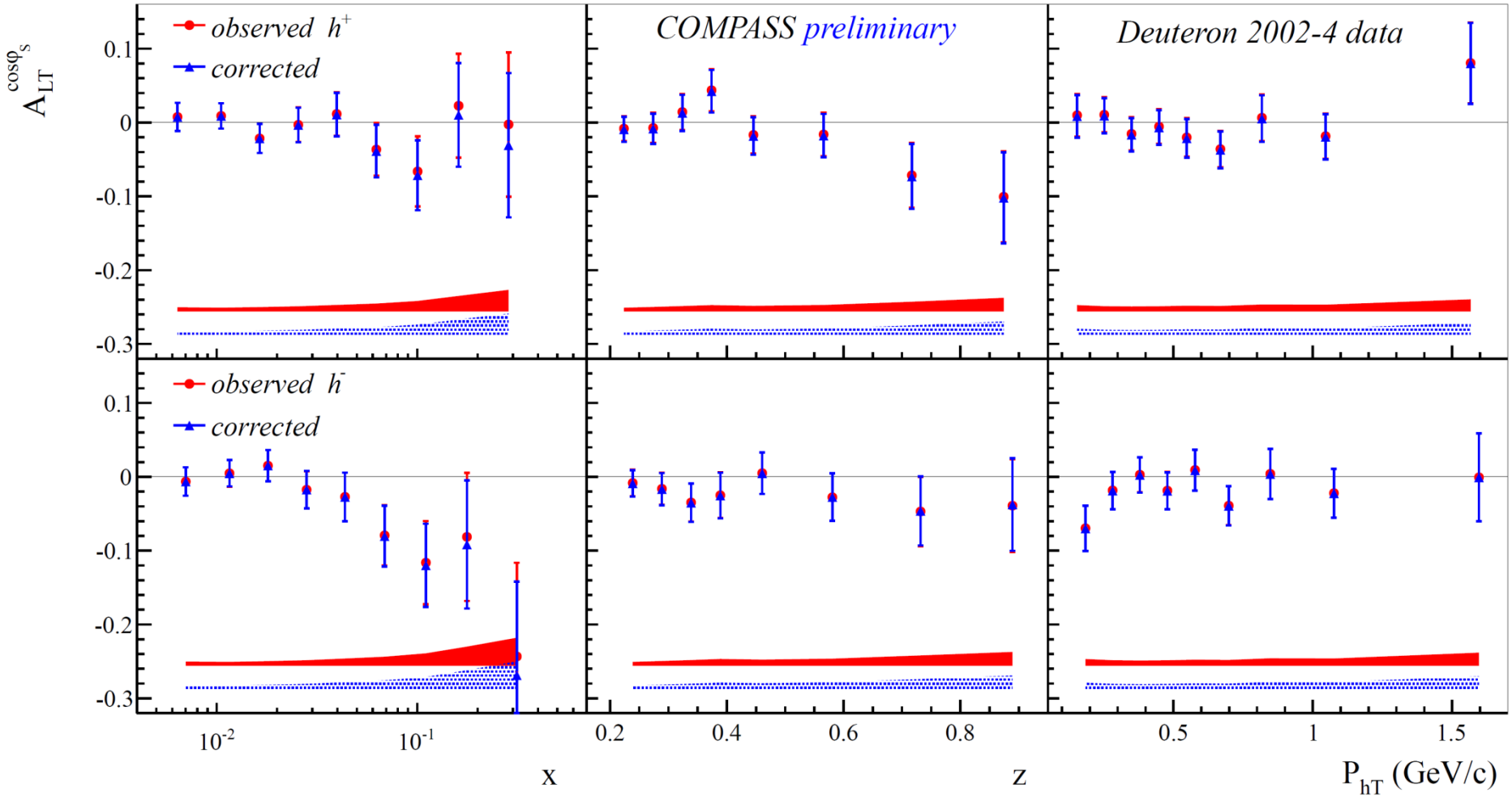
Dilution factor



$A_{LT}^{\cos\varphi_S}$ corrected for A_{LL} contribution:

using A_{LL} from PRD **74,** 074015

$$A_{LT}^{\cos\varphi_S}{}' \approx \left(\cos\theta A_{LT}^{\cos\varphi_S} - \sin\theta \frac{\sqrt{(1-\varepsilon^2)}}{\sqrt{2\varepsilon(1-\varepsilon)}} A_{LL} \right)$$



$A_{LT}^{\cos(\varphi_h-\varphi_S)}$ asymmetry *PRD73:114017,(2006)*

There exists a relation between first momentum of g_{1T} and g_2 (follows from Lorentz invariance, Tangerman & Mulders) :

$$g_{1T}^{q(1)}(x) \equiv \int_0^x g_2^q(y)dy = -\int_x^1 g_2^q(y)dy = (WW-appr) = x\int_x^1 \frac{g_1^q(y)}{y}dy$$

$$f_1^q(x,k_T^2) = f_1^q(x)\frac{1}{\pi\mu_0^2}\exp(-\frac{k_T^2}{\mu_0^2}),$$

$$D_q^h(z,P_{hT}^2) = D_q^h(z)\frac{1}{\pi\mu_D^2}\exp(-\frac{P_{hT}^2}{\mu_D^2}),$$

$$g_{1T}^q(x,k_T^2) = g_{1T}^q(x)N\exp(-\frac{k_T^2}{\mu_1^2})$$

N is fixed by

$$g_{1T}^{q(1)}(x) = \int d^2k_T\,\frac{k_T^2}{2M^2}\,g_{1T}^q(x,k_T^2)$$

$$g_{1T}^q(x,k_T^2) = g_{1T}^{q(1)}(x)\frac{2M^2}{\pi\mu_1^4}\exp(-\frac{k_T^2}{\mu_1^2})$$

From analysis of unpolarized P_{hT} dependence and Cahn effect

$$\mu_0^2 = 0.25(GeV/c)^2,\ \ \mu_D^2 = 0.2(GeV/c)^2$$

Naïve positivity constraint: $\frac{|k_T|}{M}\left|g_{1T}^q(x,k_T^2)\right| < f_1^q(x,k_T^2)$

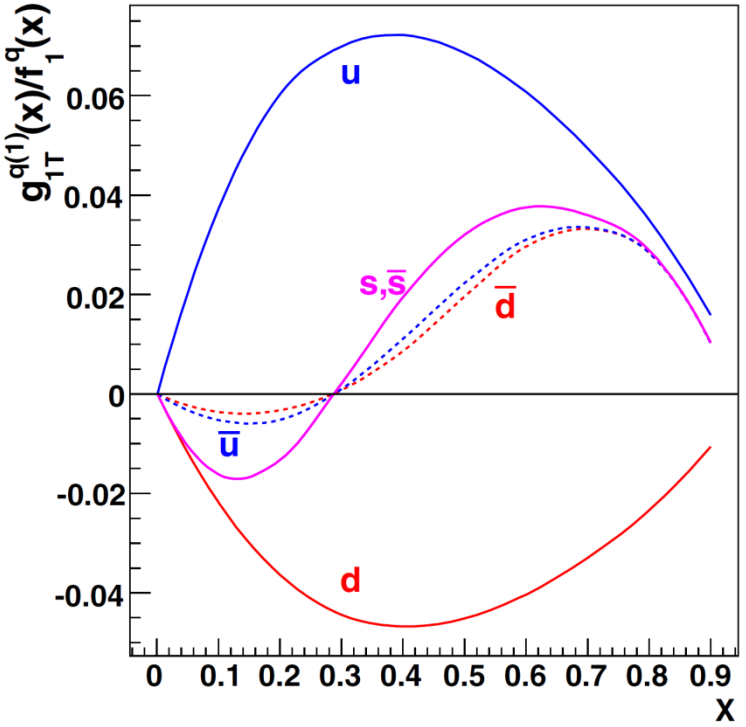
holds if $\mu_1^2 \le 0.246\ (\mathrm{GeV/c})^2$

Predictions done for: $\mu_1^2 = 0.1, 0.15\ and\ 0.25(GeV/c)^2$

$$A_{LT}^{\cos\phi_h^S}(x,y,z,P_{hT}) = 2\frac{\int_0^{2\pi} d\phi_h^S(d\sigma^{\rightarrow\Uparrow}-d\sigma^{\rightarrow\Downarrow})\cos\phi_h^S}{\int_0^{2\pi} d\phi_h^S(d\sigma^{\rightarrow\Uparrow}+d\sigma^{\rightarrow\Downarrow})} = 2\frac{\frac{2-y}{xy}\frac{Mz|P_{hT}|}{(\mu_D^2+\mu_1^2z^2)^2}\exp(-\frac{P_{hT}^2}{\mu_D^2+\mu_1^2z^2})\sum_q e_q^2 g_{1T}^{q(1)}(x)D_q^h(z)}{\frac{1+(1-y)^2}{xy^2}\frac{1}{\mu_D^2+\mu_0^2z^2}\exp(-\frac{P_{hT}^2}{\mu_D^2+\mu_0^2z^2})\sum_q e_q^2 f_1^q(x)D_q^h(z)}$$

$A_{LT}^{\cos(\varphi_h-\varphi_S)}$ asymmetry *PRD73:114017,(2006)*

$$A_{TMD} = \frac{\text{Low } x, y, z \,\&\, p_T \; + \; \text{High } x, y, z \,\&\, p_T}{\text{Low } x, y, z \,\&\, p_T \; + \; \text{High } x, y, z \,\&\, p_T}$$



GRV98+GRSV2000 LO, std DFs Kretzer FFs

COMPASS - $Q^2>1.0$ (GeV/c)^2, $W^2>25$ GeV^2, $0.05<x_{Bj}<0.6$, $0.5 < y < 0.9$, $0.4 < z < 0.9$, $|P_{h,T}| > 0.5$GeV/c

HERMES - $Q^2>1.0$ (GeV/c)^2, $W^2>10$ GeV^2, $0.1<x_{Bj}<0.6$, $0.45 < y < 0.85$, $0.4 < z < 0.9$, $|P_{h,T}| > 0.5$GeV/c

JLab - $Q^2>1.0$ (GeV/c)^2, $W^2>4$ GeV^2, $0.2<x_{Bj}<0.6$, $0.4 < y < 0.7$, $0.4 < z < 0.7$, $|P_{h,T}| > 0.5$GeV/c

COMPASS