# **Overview of the nucleon spin studies** at COMPASS

**Nucleon:** *almost all visible matter*  **Spin:** *fundamental quantum number* 

#### **ICNFP 2013 - Crete, Greece**

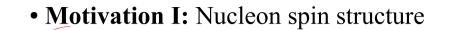


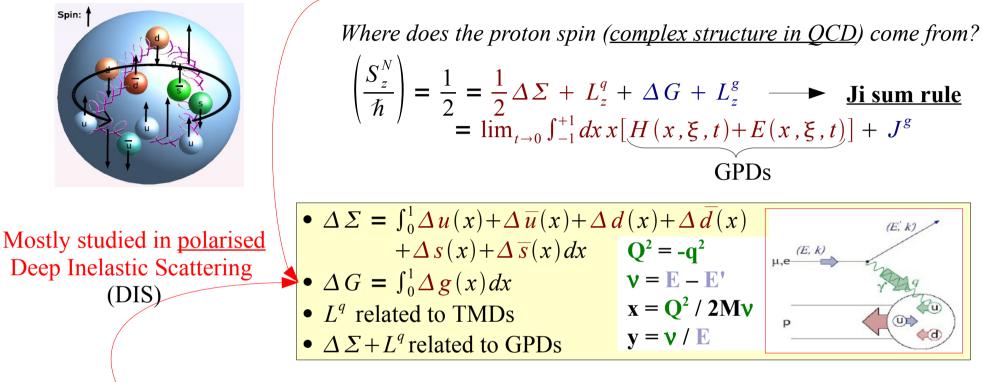




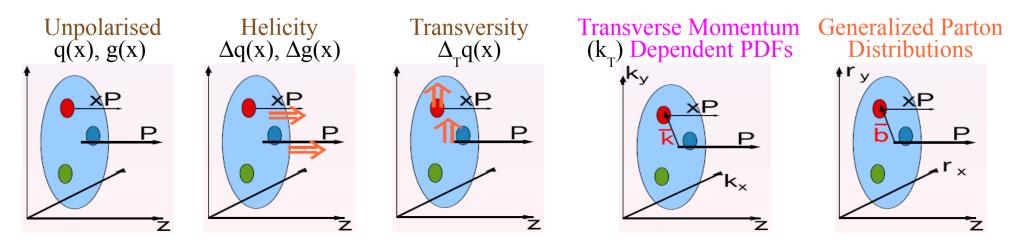
#### **Celso Franco** (LIP – Lisboa) on behalf of the COMPASS collaboration

#### **Motivation**





• Motivation II: Parton Distribution Functions (PDFs), TMDs and GPDs



#### **Common Muon and Proton Apparatus** for Structure and Spectroscopy

239 physicistsCOMPASS23 institutes12 countries + CERN

# Muon programmeHadron programme• Spin dependent structure function g<br/>• Gluon polarisation in the nucleon<br/>• Quark polarisation distributions<br/>• Transversity and TMDs<br/>• Vector meson production<br/>• $\Lambda$ polarisation• Primakoff effect, $\pi$ & K polarisabilities<br/>• Exotic states, gluballs<br/>• (Double) charmed baryons<br/>• Multiquark states<br/>(using $\pi^-$ beam)

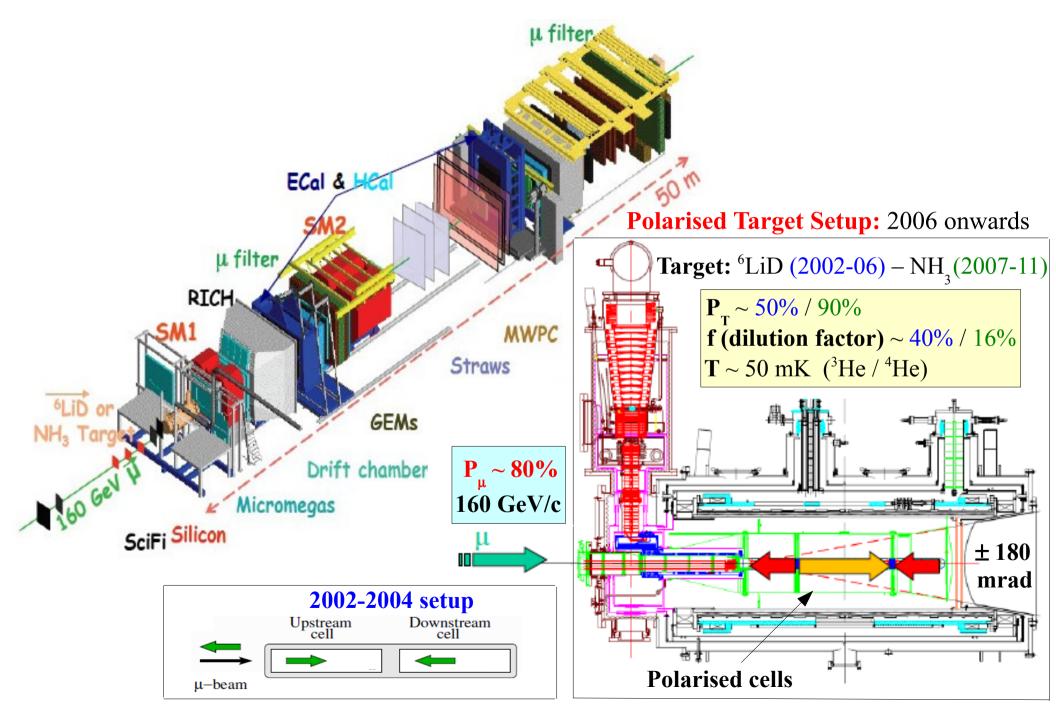
Future: Polarised Drell-Yan physics and DVCS for GPDs

#### Taking data since 2002 using:

Polarised <sup>6</sup>LiD and NH<sub>3</sub> targets

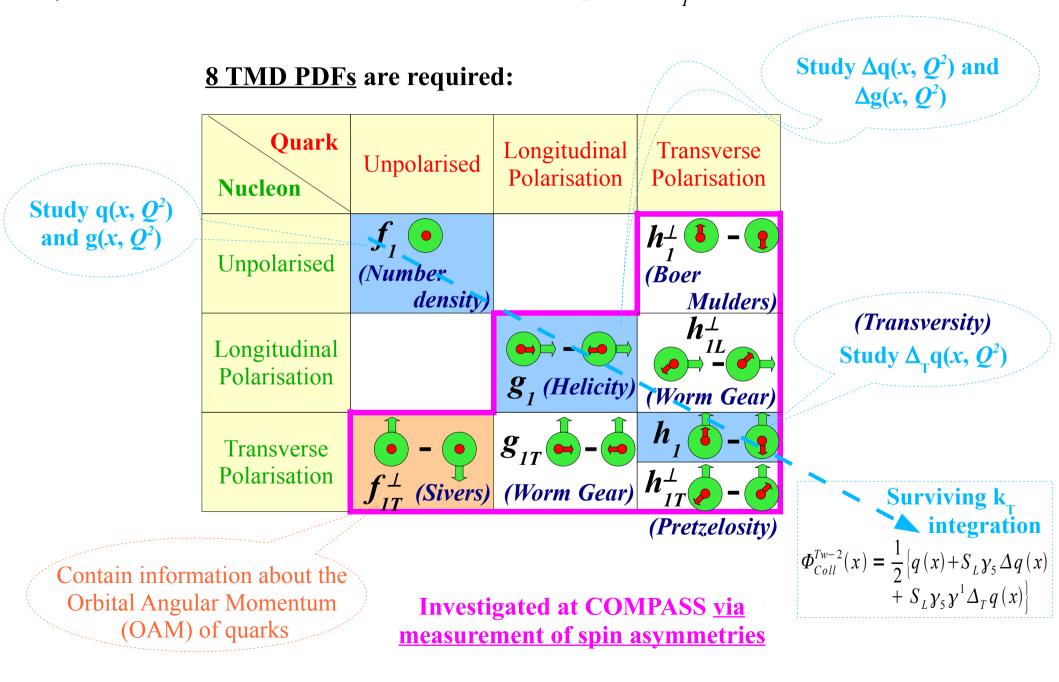
LH, target

#### The spectrometer and polarised (longitudinal example) target



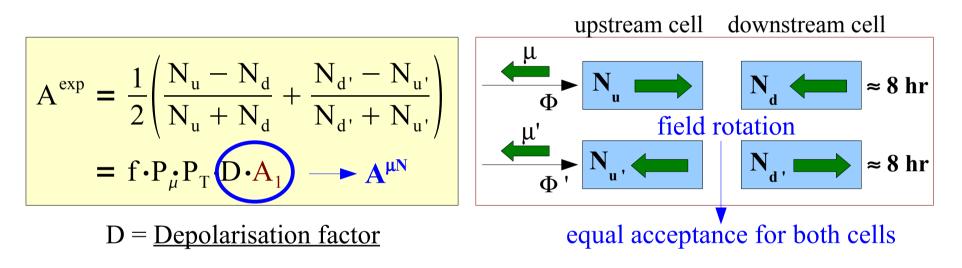
#### Leading Order (LO) description of the nucleon structure

(when the intrinsic transverse momentum of quarks,  $k_{\tau}$ , is also taken into account)



**COMPASS results with a longitudinally polarised target** 

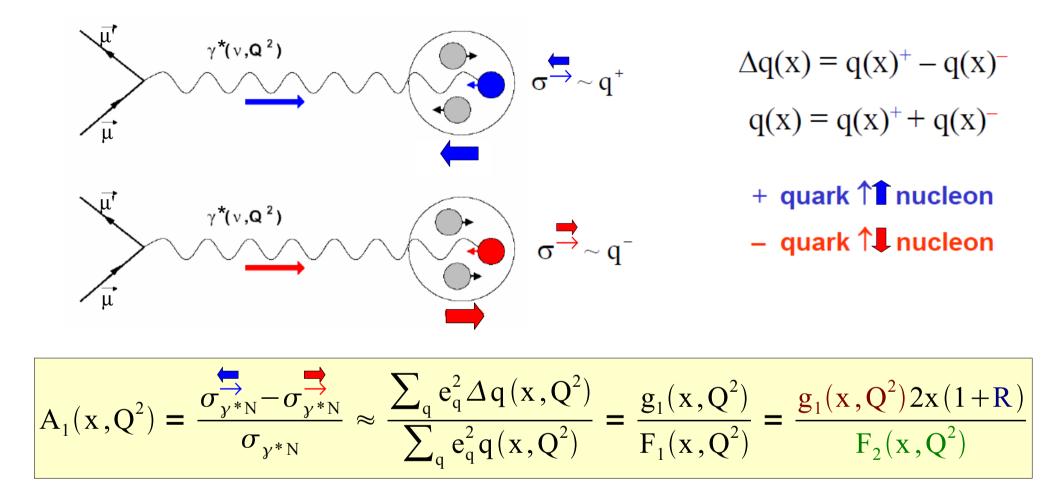
- Asymmetry measurement (example):  $A_1^N := \frac{\Delta \sigma_{\gamma*N}}{\sigma_{\gamma*N}} = \frac{\left(\sigma_{\gamma*N}^{\not\leftarrow} \sigma_{\gamma*N}^{\not\leftarrow}\right)}{\sigma_{\gamma*N}^{unpol}}$
- The number of reconstructed events inside each spin configuration of the target,  $N_{t}$  (t = u, d, u', d'), can be used to extract the inclusive  $A_{1}^{d}/A_{1}^{p}$  asymmetries:



• Weighting each event with  $\omega = (\mathbf{fP}_{\mu}\mathbf{D})$ :

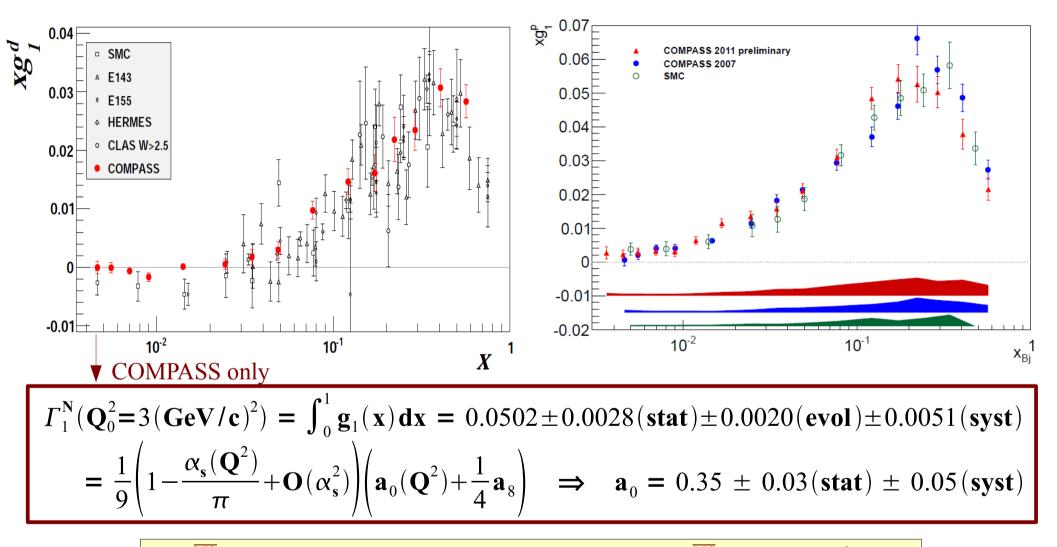
$$A_{1} = \frac{1}{2P_{T}} \left( \frac{\sum_{i=0}^{N_{u}} \omega_{i} - \sum_{i=0}^{N_{d}} \omega_{i}}{\sum_{i=0}^{N_{u}} \omega_{i}^{2} + \sum_{i=0}^{N_{d}} \omega_{i}^{2}} + \frac{\sum_{i=0}^{N_{u'}} \omega_{i} - \sum_{i=0}^{N_{d'}} \omega_{i}}{\sum_{i=0}^{N_{u'}} \omega_{i}^{2} + \sum_{i=0}^{N_{d'}} \omega_{i}^{2}} \right) \frac{\text{statistical gain:}}{\left\langle \sum_{i=0}^{N_{tot}} \omega_{i} \right\rangle^{2}}$$

#### Interpretation of A<sub>1</sub> in terms of structure functions



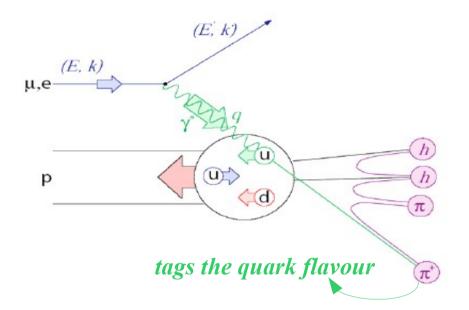
- $\mathbf{g}_1$  (polarised structure function) is obtained from the measured  $\mathbf{A}_1$  using:
  - $F_2 \rightarrow \underline{SMC \text{ parameterisation}}$  and  $R = \sigma^L / \sigma^T \rightarrow \underline{SLAC \text{ parameterisation}}$

#### **COMPASS results for g\_1^{d/p} and first moments of g\_1^{d}**



 $\Delta \Sigma^{\overline{\text{MS}}} = 0.33 \pm 0.03 (\text{stat}) \pm 0.05 (\text{syst}) \qquad (\Delta \Sigma^{\overline{\text{MS}}} = \mathbf{a}_0 \quad @ \quad \mathbf{Q}^2 \to \infty)$ = 0.30 ± 0.01 (stat) ± 0.02 (syst) (using world data on p, n, d)  $(\Delta \mathbf{s} + \Delta \overline{\mathbf{s}}) = \frac{1}{3} (\Delta \Sigma^{\overline{\text{MS}}} - \mathbf{a}_8) = -0.08 \pm 0.01 (\text{stat}) \pm 0.02 (\text{syst})$ 

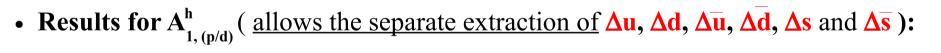
#### **Extraction of the quark helicity distributions from Semi-Inclusive DIS (SIDIS)**

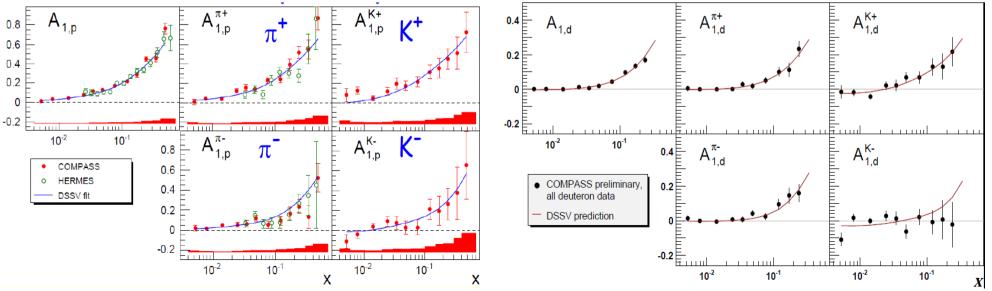


• We have at Leading Order (LO) in QCD :

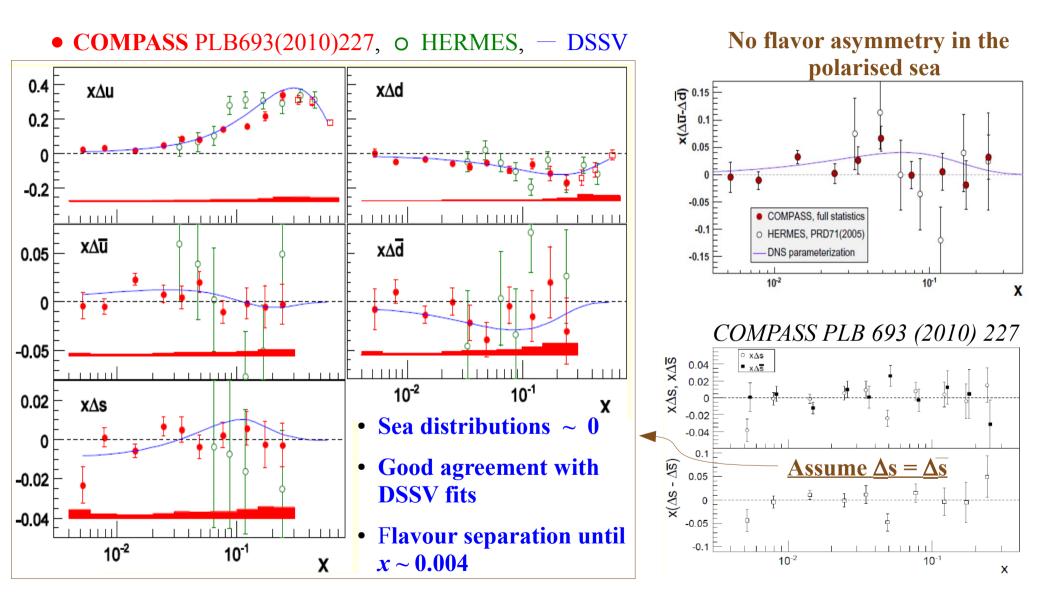
$$A_{1,(p/d)}^{h}(x,z,Q^{2}) \approx \frac{\sum_{q} e_{q}^{2} \Delta q(x,Q^{2}) D_{q}^{h}(z,Q^{2})}{\sum_{q} e_{q}^{2} q(x,Q^{2}) D_{q}^{h}(z,Q^{2})}$$

- Unpolarised PDFs ( $q(x, Q^2)$ )  $\rightarrow$  MRST04
- Fragmentation function of a quark to a hadron  $(D_a^h(z, Q^2)) \rightarrow \underline{\text{DSS parameterisation}}$





#### **Quark helicities from SIDIS:** $Q^2 = 3 (GeV/c)^2$ and x < 0.3

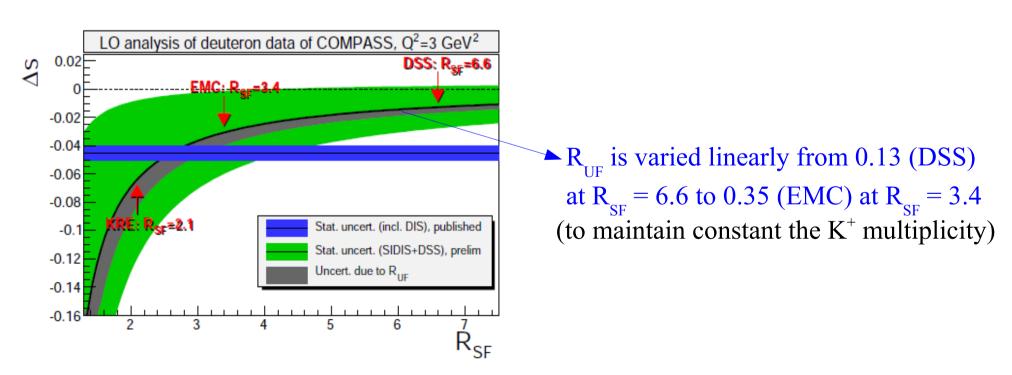


 $\Delta s(SIDIS) = -0.01 \pm 0.01(stat.) \pm 0.01(syst.)$  @ 0.003 < x < 0.3

#### **∆s dependence on Fragmentation Functions (FFs)**

• The relation between the semi-inclusive asymmetries and  $\Delta s$  depends only on the following ratios:

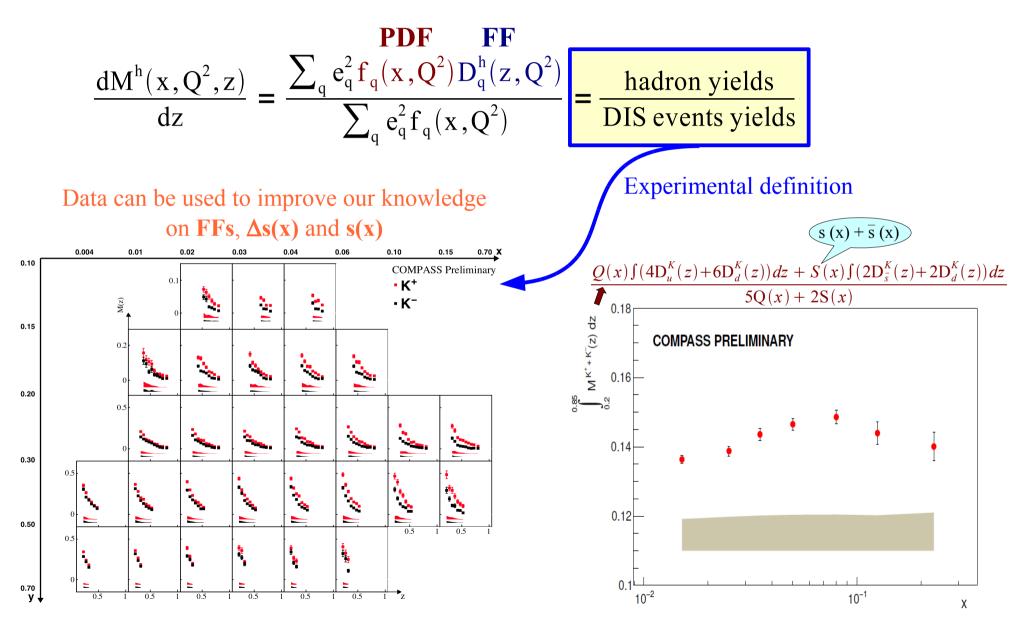
$$\mathbf{R}_{UF} = \frac{\int_{0.2}^{0.85} \mathbf{D}_{d}^{K^{+}}(z) dz}{\int_{0.2}^{0.85} \mathbf{D}_{u}^{K^{+}}(z) dz}, \quad \mathbf{R}_{SF} = \frac{\int_{0.2}^{0.85} \mathbf{D}_{\bar{s}}^{K^{+}}(z) dz}{\int_{0.2}^{0.85} \mathbf{D}_{u}^{K^{+}}(z) dz}$$



• Determination of  $R_{SF}$  from hadron multiplicities on the way

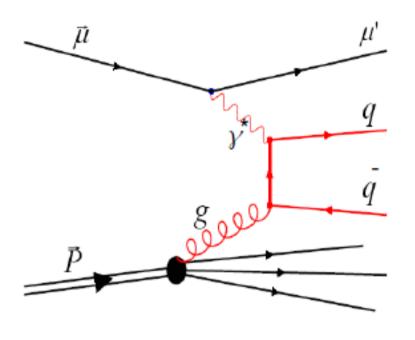
#### A first look on hadron multiplicities

• Assuming the quark parton model (leading order):



#### **Direct measurement of \Delta g/g at LO in QCD**





$$\mathbf{A}_{\mu \mathbf{N}}^{\mathbf{PGF}} = \frac{\int \mathbf{d}\,\hat{\mathbf{s}}\,\Delta\,\sigma^{\mathbf{PGF}}\Delta\,\mathbf{g}(\mathbf{x}_{\mathbf{g}},\hat{\mathbf{s}})}{\int \mathbf{d}\,\hat{\mathbf{s}}\,\sigma^{\mathbf{PGF}}\mathbf{g}(\mathbf{x}_{\mathbf{g}},\hat{\mathbf{s}})} \approx \frac{\langle \mathbf{a}_{\mathbf{LL}}^{\mathbf{PGF}} \rangle \frac{\Delta\,\mathbf{g}}{\mathbf{g}}}{\mathbf{p}}$$

Obtained from Monte Carlo and parameterised by a Neural Network (to be used on data)

There are two methods to tag this process:

- Open Charm production
  - $\gamma^* g \to c\overline{c} \implies \underline{reconstruct D^0 mesons}$
  - Hard scale:  $M_c^2$
  - No intrinsic charm in COMPASS kinematics
  - No physical background
  - Weakly model dependent
  - Low statistics
- High-p<sub>T</sub> hadron pairs
  - $\gamma^* g \to q \overline{q} \implies \underline{\text{reconstruct 2 jets or } h^+ h^-}$
  - Hard scale:  $Q^2$  or  $\Sigma p_T^2$  [ $Q^2 > 1$  or  $Q^2 < 1$  (GeV/c)<sup>2</sup>]
  - High statistics
  - Physical background
  - Strongly model dependent

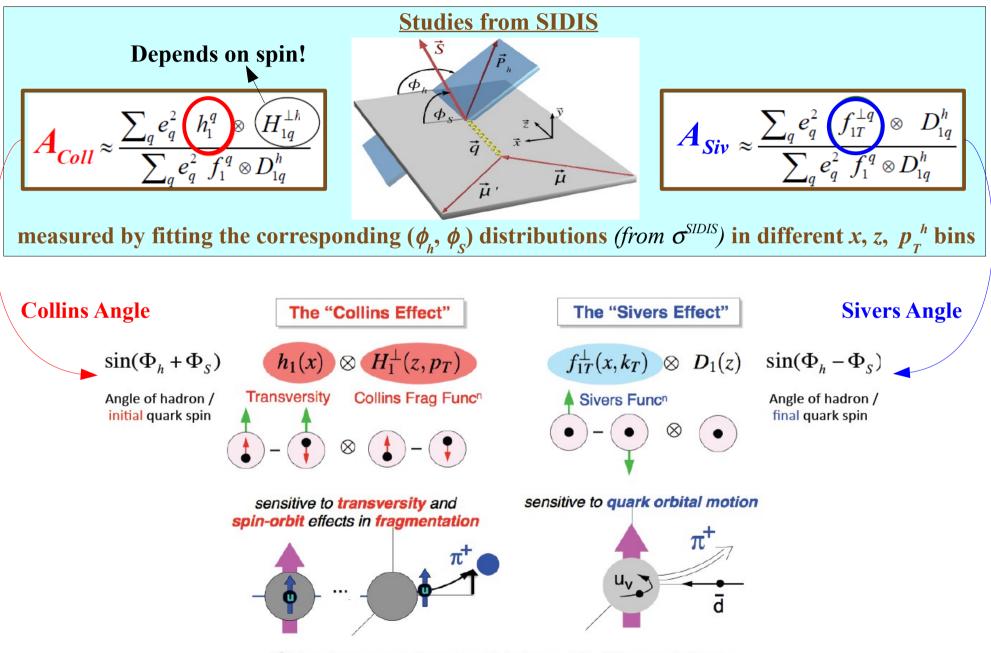
#### **Results on** $\Delta g/g$ and $x\Delta g$

**COMPASS Open-Charm at NLO** World data at LO **0.8 0.6 0**.6 COMPASS, high p \_, Q<sup>2</sup>>1 (GeV/c)<sup>2</sup>, 2002-2006 COMPASS, high p , Q<sup>2</sup><1 (GeV/c)<sup>2</sup>, 2002-2003 -^^^ -~~~~ COMPASS, open charm, 2002-2007 SMC, high  $p_{\tau}$ , Q<sup>2</sup>>1 (GeV/c)<sup>2</sup> П 0.4 HERMES, high p\_, all Q<sup>2</sup> C/ Λ С 0.2 -000000 ~ 000000 С Example of NLO diagrams -0.2 A Contraction -^^^ -0.4С -0.6LOODOL ZOODOL -0.8 10<sup>-2</sup>  $10^{-1}$ Χ 0.8 DSSV at Q<sup>2</sup> = 10 (GeV/c)<sup>2</sup> x.∆g  $Q^2 = 13 (GeV/c)^2$  $\int_{0}^{1} \Delta \, \mathbf{gdx} = 0.27 \pm 0.09$ J.3 LSS at  $Q^2 = 13 (GeV/c)^2$ ,  $\Delta G > 0$ ∆g/g COMPASS open charm \_SS at Q<sup>2</sup> = 13 (GeV/c)<sup>2</sup>, ∆G changing sign 0.6 COMPASS at  $Q^2 = 13 (GeV/c)^2$ .  $\Delta G > 0$ COMPASS (∆g>0) 0.2 COMPASS at  $Q^2 = 13 (GeV/c)^2$ ,  $\Delta G < 0$ COMPASS (∆g<0) DSSV 0.4 0.1 LSS (∆g>0) ..... LSS (∆g sign changing) 0.2 -0.1 -0.2-0.2 ★ COMPASS, Open-Charm, NLO, all Q<sup>2</sup>, ⟨µ<sup>2</sup>⟩ = 13 (GeV/c)<sup>2</sup>  $\int_0^1 \Delta \mathbf{gdx} = -0.34 \pm 0.12$ -0.4-0.3  $10^{-2}$ 10-1 10<sup>-2</sup> 10<sup>-1</sup> Х

Χ

**COMPASS results with a transversely polarised target** 

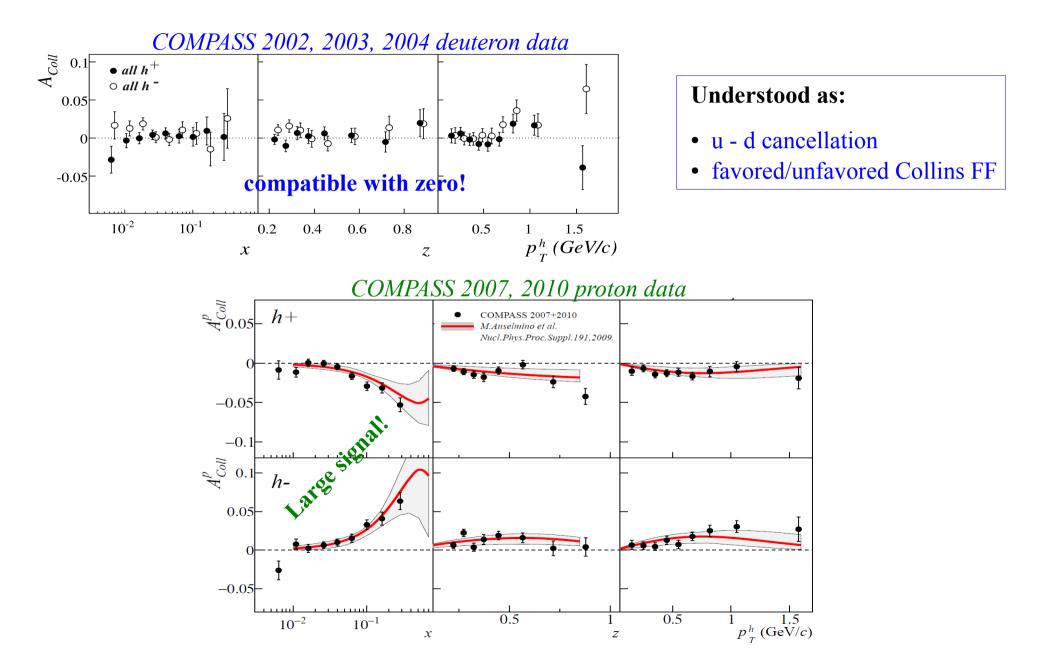
#### **Interpretation of Collins & Sivers asymmetries in terms of TMDs**



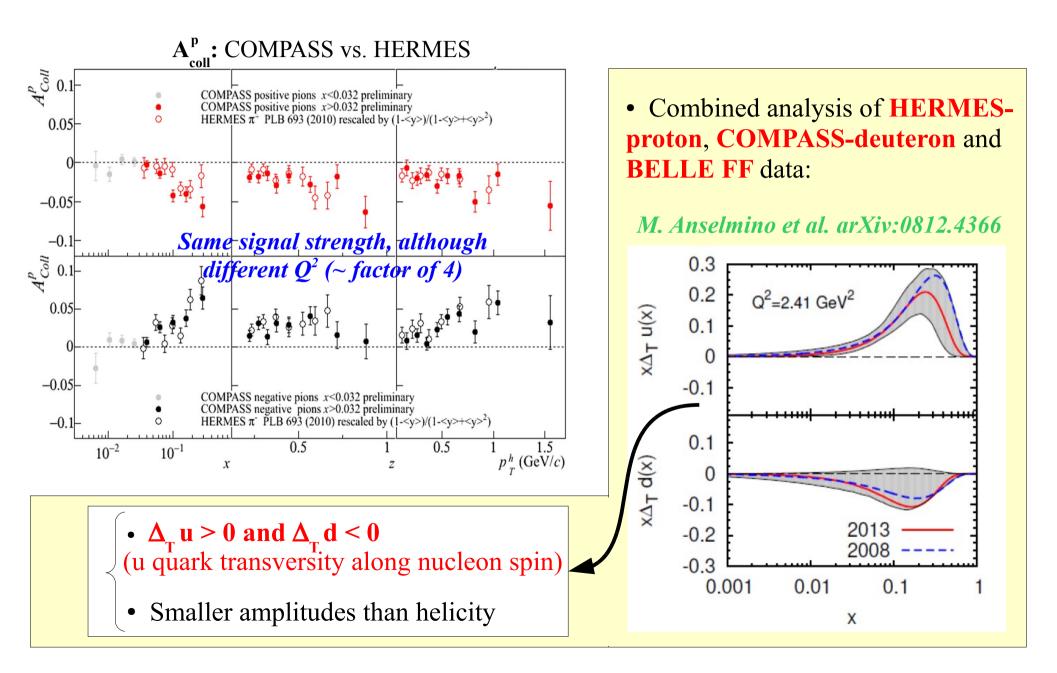
 $\otimes$  denotes convolution over intrinsic quark k<sub>T</sub> & fragmentation p<sub>T</sub>

#### **Results on the Collins asymmetry**

# (correlation between the hadron $p_T$ & the quark transverse spin in a transversely polarised nucleon)

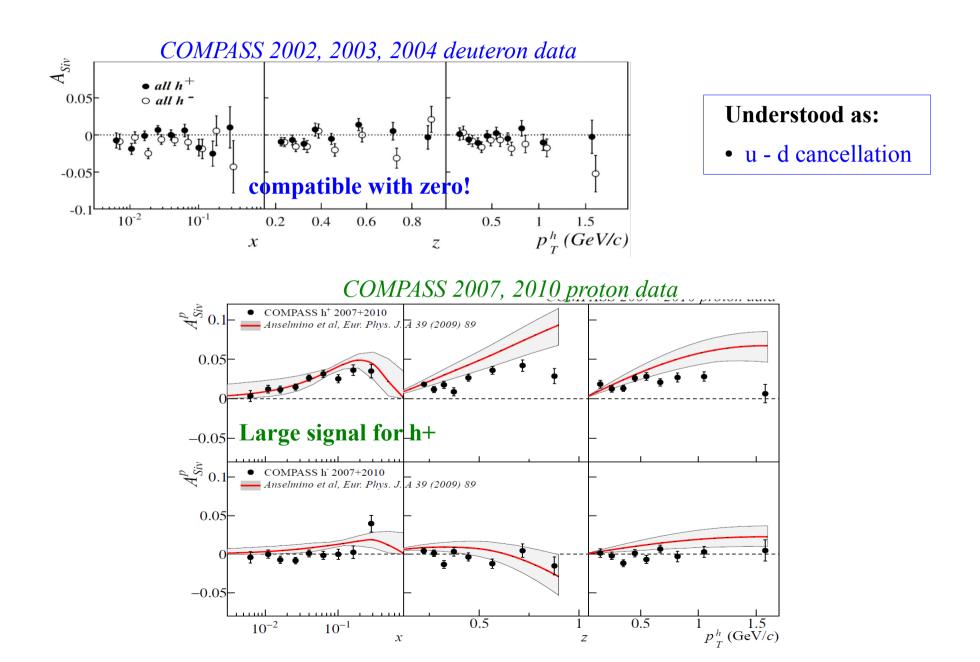


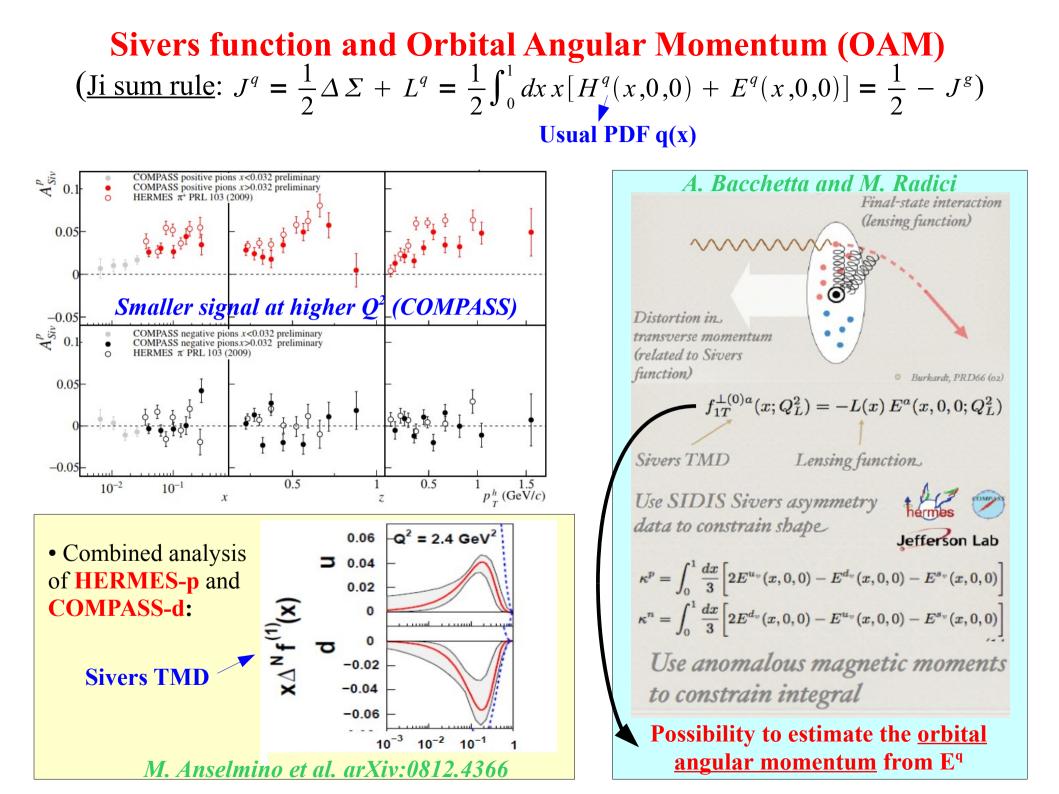
#### **Transversity from Collins asymmetry**



#### **Results on the Sivers asymmetry**

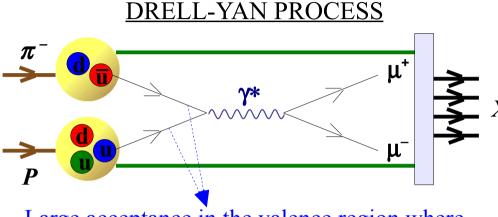
(correlation between the nucleon transverse spin and the quark  $k_{T}$ )





#### **COMPASS future**

#### **COMPASS future I (2015):** TMDs from polarised Drell-Yan



Large acceptance in the valence region where large single spin asymmetries (SSA) are expected

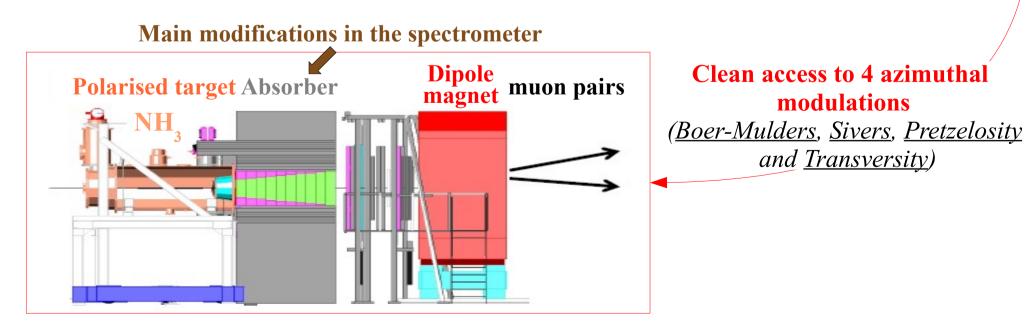
• **Convolution of 2 TMDs** (no FF involved):

$$\sigma_{DY} \propto f_{\bar{u}/\pi^-} \otimes f'_{u/P}$$

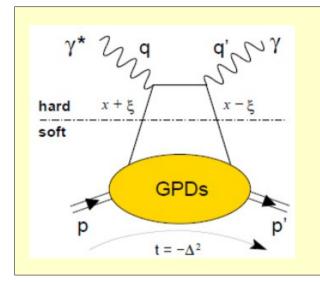
• Test of the TMD universality factorization approach (for the description of SSA):

$$f_{1T}^{\perp}|_{DY} = -f_{1T}^{\perp}|_{DIS} \& h_{1}^{\perp}|_{DY} = -h_{1}^{\perp}|_{DIS}$$

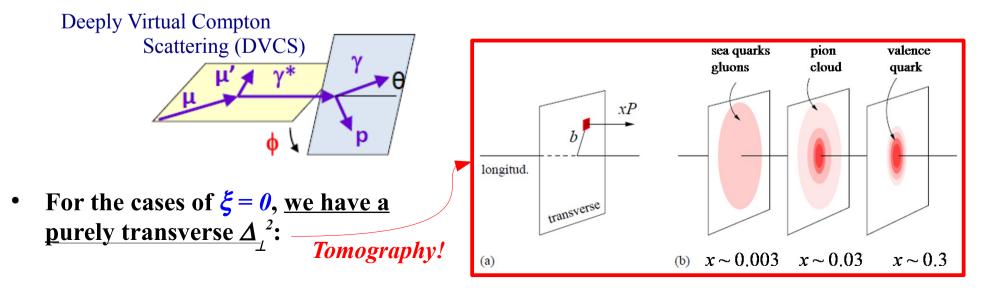
• Study the production mechanism and the polarisation of  $J/\Psi$ 



#### **COMPASS future II (2016, 2017):** GPDs and nucleon tomography



- Measurement of 4 generalised parton distributions *(GPDs)* for quarks:  $H, E, \tilde{H}, \tilde{E}(x, \xi, t)$ 
  - Contain normal PDF and elastic form factor as <u>limiting</u> cases:  $q(x) = H(x, \theta, \theta)$  and  $F(t) = \int dx H(x, \xi, t)$
  - Correlates transverse spatial and longitudinal momentum degrees of freedom *(nucleon tomography)*
  - Access the OAM of quarks via the Ji sum rule
- The GPD *H* will be determined by studying the azimuthal dependence of the DVCS cross-section (combining the data of  $\mu^+$  and  $\mu^-$  beams on a liquid hydrogen target):

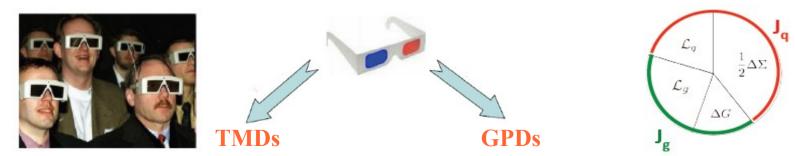


#### **Summary**

- Gluon contribution to the nucleon spin:
  - All measurements point to zero or small contribution
- Quark contribution to the nucleon spin:
  - Extraction for all flavours from SIDIS (more knowledge on FF is needed for  $\Delta s$ )
  - A global contribution of 30% was measured with high precision
- Transversity and TMDs
  - Precise results on Collins and Sivers asymmetries
- **Exciting future program in preparation** (polarised Drell-Yan and DVCS):

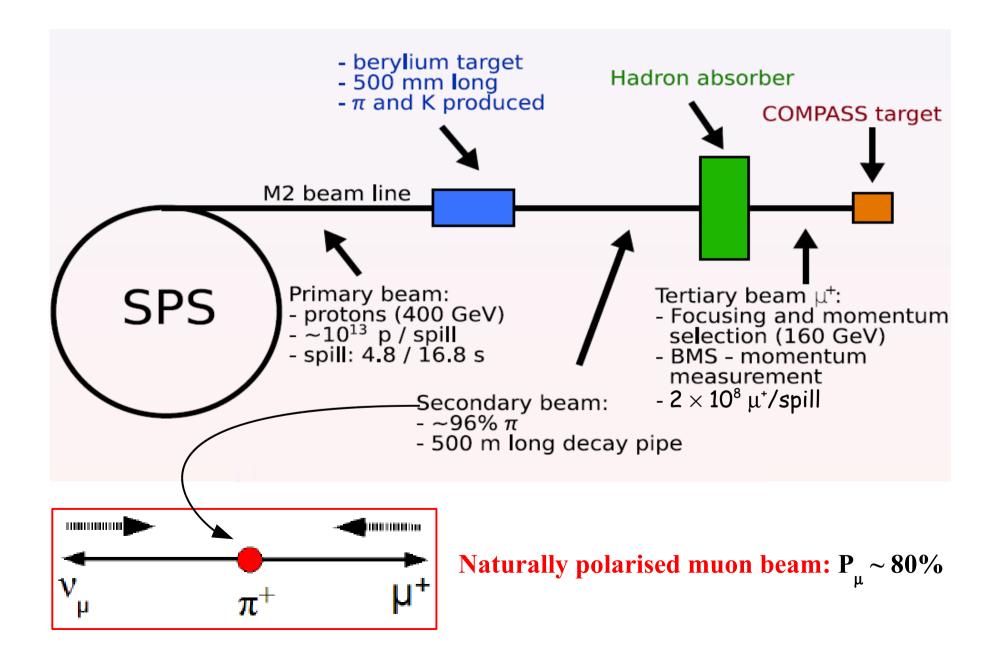
#### 3D imaging of the nucleon

**O**AM

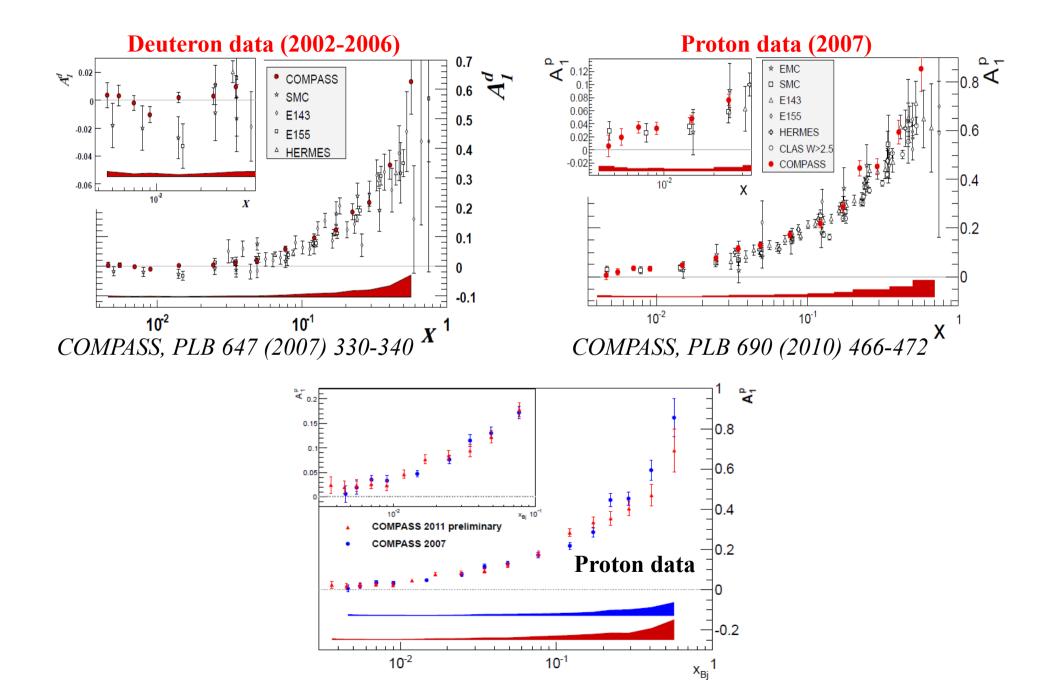


#### **SPARES**

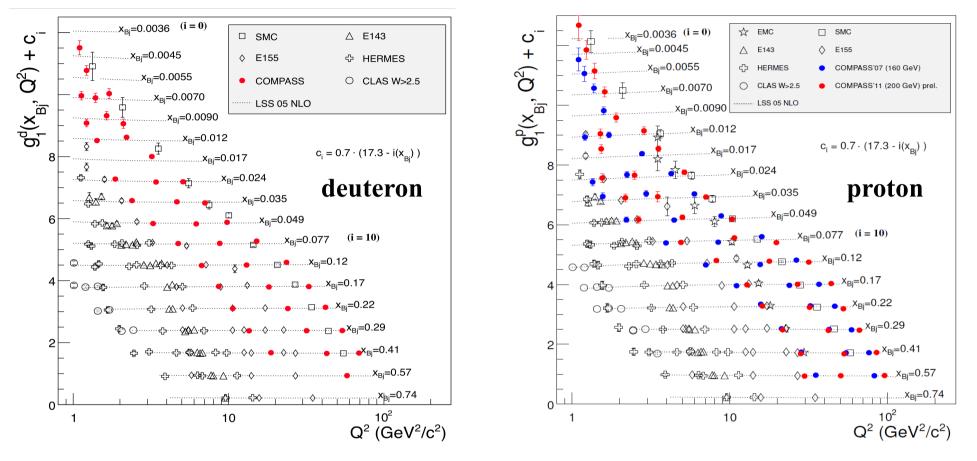
#### The polarised beam



## **Inclusive asymmetries** $A_1^{d/p}$ : $Q^2 > 1$ (GeV/c)<sup>2</sup>



### $Q^2$ dependence of $g_1(x, Q^2)$ for DGLAP evolution



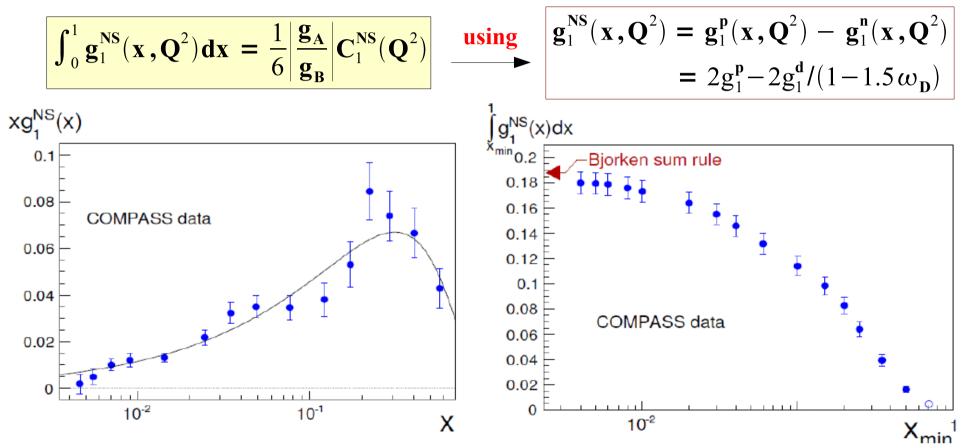
•  $\Delta \Sigma$  and  $\Delta G$  can be extracted from <u>Next-to-Leading Order (NLO)</u> fits to the  $\underline{g}_1 \text{ data} (g_1 \propto \Delta \Sigma \text{ and } \Delta G)$ , using their  $\mathbf{Q}^2$  evolution obtained from the DGLAP equations:

$$\frac{d}{dln Q^2} \Delta q^{NS} = \Delta P_{qq}^{NS} \otimes \Delta q^{NS}$$
$$\frac{d}{dln Q^2} \begin{pmatrix} \Delta q^S \\ \Delta g \end{pmatrix} = \begin{pmatrix} \Delta P_{qq}^S & \Delta P_{qg}^S \\ \Delta P_{gq}^S & \Delta P_{gg}^S \end{pmatrix} \otimes \begin{pmatrix} \Delta q^S \\ \Delta g \end{pmatrix}$$

- $(\Delta u + \Delta \overline{u})$  and  $(\Delta d + \Delta d)$  are well constrained by the data (*LSS PRD 80 2009*)
- Despite of the higher  $Q^2$  measurements by COMPASS, the kinematic coverage is not yet sufficient for  $\Delta G$

#### **Bjorken sum rule**

• According to the Bjorken sum rule the first moment of the non-singlet spin structure function,  $g_1^{NS}$ , is proportional to the ratio of axial and vector coupling constants  $g_A/g_V$ :



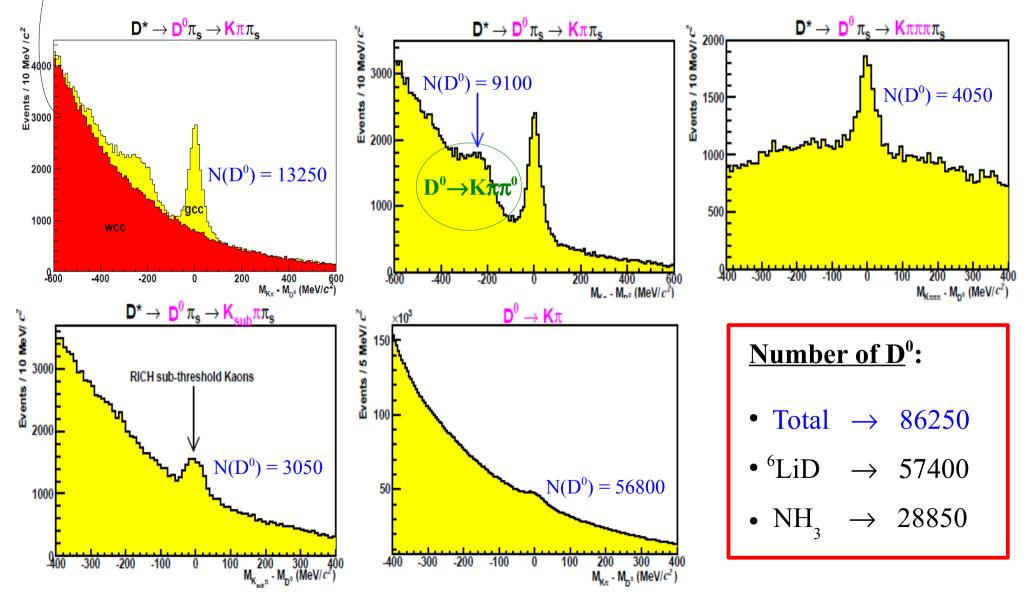
QCD fit of COMPASS data using  $\Delta q^{NS} = |g_A / g_V| x^{\alpha} (1 - x)^{\beta}$ :

 $\left|\frac{\mathbf{g}_{\mathbf{A}}}{\mathbf{g}_{\mathbf{V}}}\right| = 1.28 \pm 0.07(\mathbf{stat}) \pm 0.10(\mathbf{sys})$ 

 $(\underline{PDG value}: |g_A/g_V| = 1.269 \pm 0.003)$ 

**D<sup>0</sup> mass spectra (all samples):** 
$$\left( A_{D^0}^{exp} = f P_{\mu} P_{T} \frac{S}{S+B} A_{\mu N}^{PGF} \right)$$

• <u>Wrong Charge Combination of K $\pi$  pairs</u>: Example of a background model used for the multidimensional kinematic parameterisation (performed by a Neural Network) of S/(S+B)



#### **s/(s+b):** Obtaining final probabilities for a **D**<sup>0</sup> candidate

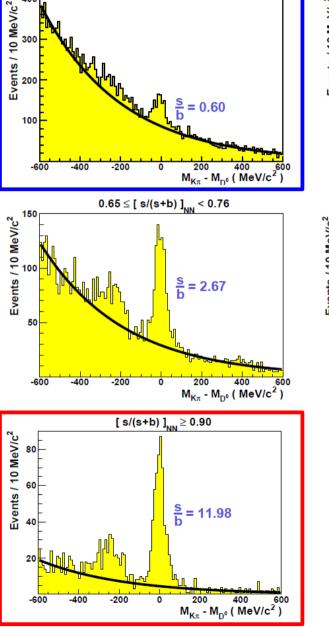
- Events with small [s/(s+b)]<sub>NN</sub>
  - Mostly combinatorial background is selected

s/(s+b) is obtained from a fit to these spectra (correcting all events with the corresponding values of  $[s/(s+b)]_{NN}$ )

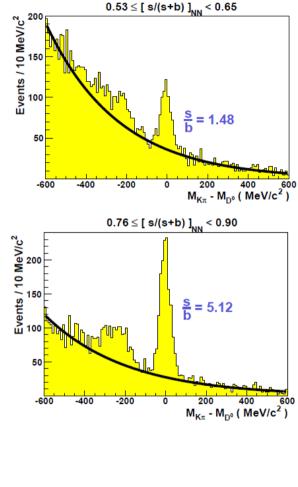
**Events with large [s/(s+b)]**<sub>NN</sub>

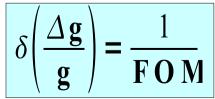
•

• Mostly Open Charm events are selected

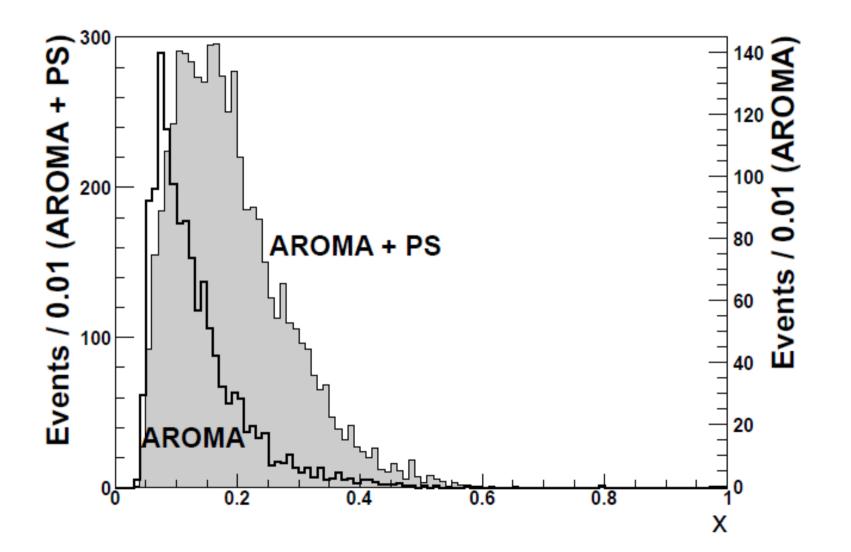


[ s/(s+b) ]<sub>NN</sub> < 0.53



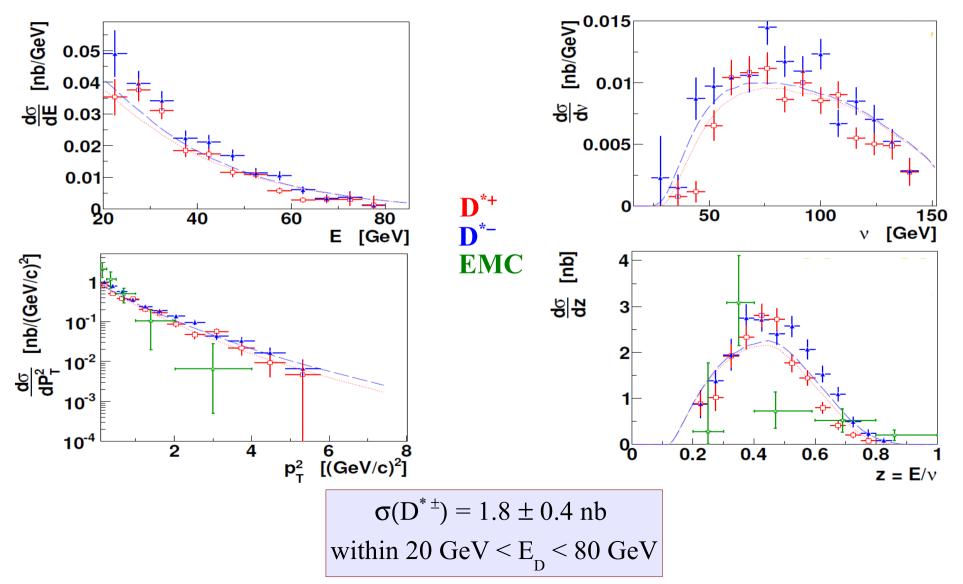


# **X**<sub>g</sub> from Open Charm

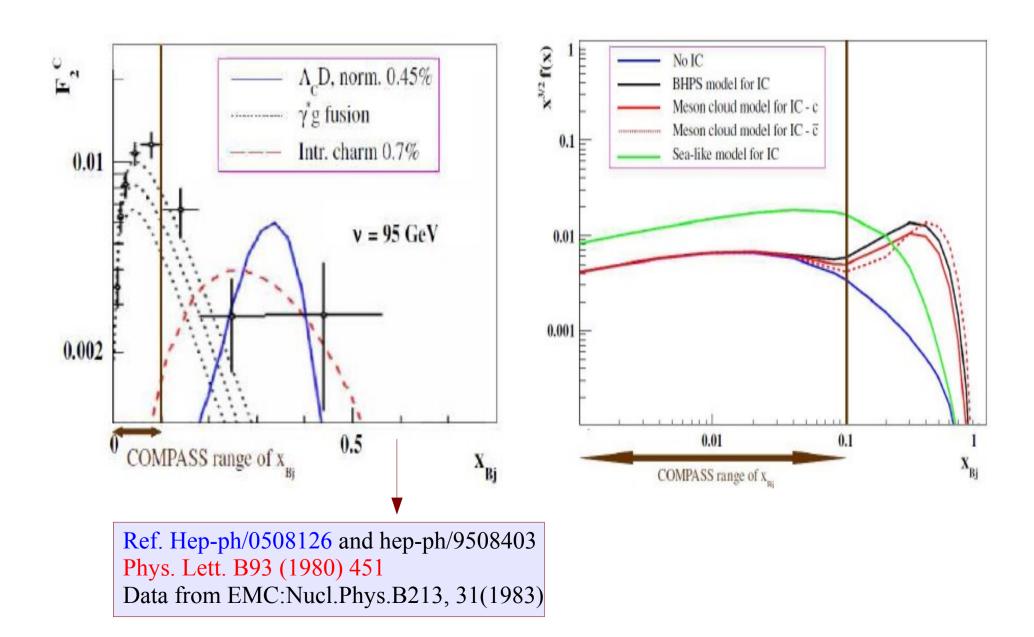


#### **AROMA with PS-ON versus COMPASS data**

• Differential cross section for  $D^*$  meson production (  $D^0_{K\pi}(2004)$  from  $D^{*+}$  and  $D^{*-}$  COMPASS data):



#### **Intrinsic charm models**



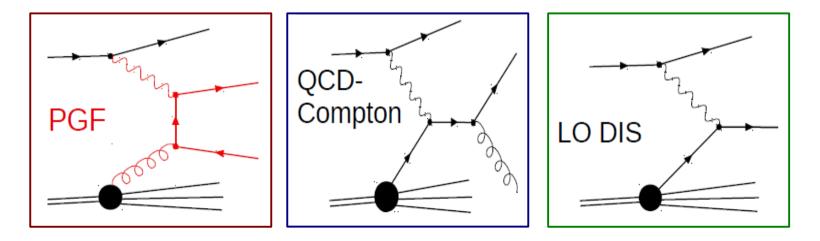
#### High- $p_{T}$ asymmetries (2002-2006): Q<sup>2</sup> > 1 (GeV/c)<sup>2</sup>

• Two samples are considered (fractions of the processes are estimated from MC):

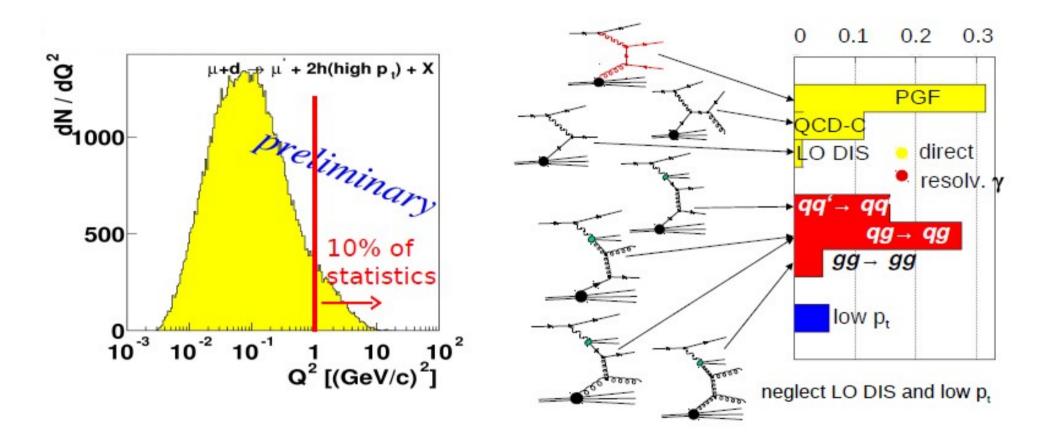
Inclusive asymmetry

$$\mathbf{A}_{1}^{\mathbf{d}}(\mathbf{x}) = \frac{\Delta \mathbf{g}}{\mathbf{g}}(\mathbf{x}_{g}) \left( \mathbf{a}_{LL}^{\mathsf{PGF,inc}} \frac{\sigma^{\mathsf{PGF,inc}}}{\sigma^{\mathsf{Tot,inc}}} \right) + \mathbf{A}_{1}^{\mathsf{LO}}(\mathbf{x}_{C}) \left( \mathbf{a}_{LL}^{\mathsf{C,inc}} \frac{\sigma^{\mathsf{C,inc}}}{\sigma^{\mathsf{Tot,inc}}} \right) + \mathbf{A}_{1}^{\mathsf{LO}}(\mathbf{x}_{Bj}) \left( \mathbf{D} \frac{\sigma^{\mathsf{LO,inc}}}{\sigma^{\mathsf{Tot,inc}}} \right) \\ \mathbf{A}_{LL}^{2h}(\mathbf{x}) = \left( \frac{\mathbf{A}^{\exp}}{\mathbf{f} \mathbf{P}_{\mu} \mathbf{P}_{T}} \right) = \frac{\Delta \mathbf{g}}{\mathbf{g}}(\mathbf{x}_{g}) \left( \mathbf{a}_{LL}^{\mathsf{PGF}} \frac{\sigma^{\mathsf{PGF}}}{\sigma^{\mathsf{Tot}}} \right) + \mathbf{A}_{1}^{\mathsf{LO}}(\mathbf{x}_{C}) \left( \mathbf{a}_{LL}^{\mathsf{C}} \frac{\sigma^{\mathsf{C}}}{\sigma^{\mathsf{Tot}}} \right) + \mathbf{A}_{1}^{\mathsf{LO}}(\mathbf{x}_{Bj}) \left( \mathbf{D} \frac{\sigma^{\mathsf{LO,inc}}}{\sigma^{\mathsf{Tot,inc}}} \right)$$

high- $p_{\rm T}$  hadron pairs  $(p_{\rm T1} / p_{\rm T2} > 0.7 / 0.4 \text{ GeV/c}) \Rightarrow \text{enhancement of the PGF contribution}$ 



#### **High-** $p_{\rm T}$ analysis: Q<sup>2</sup> < 1 (GeV/c)<sup>2</sup>



#### 2002-2004 Preliminary:

 $\Delta G/G = 0.016 \pm 0.058 \text{ (stat)} \pm 0.055 \text{ (syst)}$ 

#### 2002-2003 Published:

 $\Delta G/G = 0.024 \pm 0.089 \text{ (stat)} \pm 0.057 \text{ (syst)}$  Phys. Lett. B 633 (2006) 25 - 32