

# Pion and Kaon Multiplicities in Muon-Nucleon Scattering

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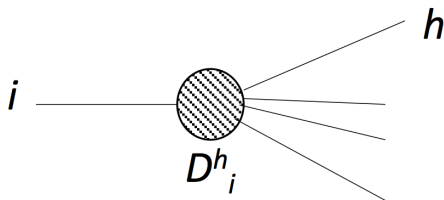
On behalf of the COMPASS collaboration

8<sup>th</sup> October 2013



# Fragmentation Functions

- Hadronisation in QDC
- Fragmentation functions  $D_i^h$
- Hadronisation of quark with flavour  $i$  to hadron  $h$
- Normalised, universal and process independent
- Favoured and unfavoured FFs



$$\sum_h \int_0^1 D_i^h(z) dz = 1$$
$$D_{fav.} \gg D_{unfav.}$$

# How to Access Fragmentation Functions

- $e^+e^-$  annihilation

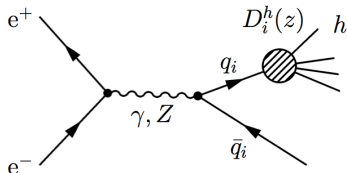
Precise and clean data

Only depends on FF

$q\bar{q}$  fragmentation not distinguishable

Charge sum

(LEP, BELLE,...)



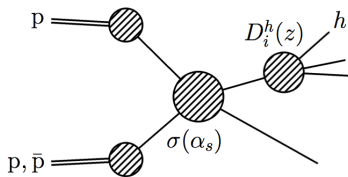
- pp collision

Gluon FF

Strongly dependant on PDFs

Difficult theoretical description

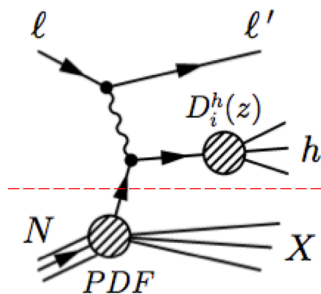
(RHIC, Fermi Lab., ...)



# Fragmentation Functions from SIDIS

- Semi-Inclusive Deep Inelastic Scattering  $\Rightarrow \ell + N \xrightarrow{\gamma^*} \ell' + h + X$

Allows flavour separation  
Wide coverage in  $x$  and  $Q^2$   
(COMPASS, HERMES,...)



$$Q^2 \equiv -\mathbf{q}^2 = -(\mathbf{k} - \mathbf{k}')^2 \stackrel{\text{lab}}{\simeq} 4EE' \sin^2 \frac{\theta}{2}$$

$$x \equiv \frac{Q^2}{2\mathbf{P} \cdot \mathbf{q}} \stackrel{\text{lab}}{=} \frac{Q^2}{2M\nu}$$

$$y \equiv \frac{\mathbf{P} \cdot \mathbf{q}}{\mathbf{P} \cdot \mathbf{k}} \stackrel{\text{lab}}{=} \frac{\nu}{E}$$

$$z \equiv \frac{\mathbf{p}_h \cdot \mathbf{P}}{\mathbf{q} \cdot \mathbf{P}} \stackrel{\text{lab}}{=} \frac{E_h}{\nu}$$

# The Strange Quark Helicity Density

Strangeness contribution to long. spin:

$$\Delta S = \int dx [\Delta s(x) + \Delta \bar{s}(x)]$$

- From **inclusive** measurements:

$g_1(x, Q^2)$  for proton and deuteron  
NLO QCD fits

$$\Delta s + \Delta \bar{s} = -0.08 \pm 0.01_{stat.} \pm 0.02_{sys.}$$

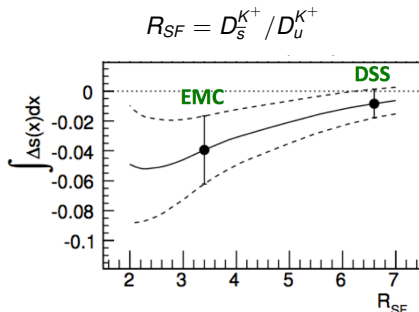
Incl - Phys. Lett. B684 (2010) 216

- From **SIDIS** (LO):

Semi-inclusive asymmetries  
In combination of PDFs  
And fragmentation functions

$$\Delta s + \Delta \bar{s} = -0.02 \pm 0.02_{stat.} \pm 0.02_{sys.}$$

SemIncl - Phys. Lett. B693 (2010) 227



DSS - Phys. Rev. D75 (2007) 114010

EMC - Nucl. Phys. B321 (1989) 541

## Multiplicities as Observables

- Factorisation theorem
- SIDIS cross section in leading-twist

Hard scattering cross section  
Parton distribution function  
Fragmentation functions

$$\sigma^h = \sum_i \sigma^0 \cdot q_i(x) \cdot D_i^h(z, Q^2)$$

Extraction of FF from hadron multiplicities

$$M^h(x, Q^2, z) = \frac{1}{\sigma^{DIS}} \frac{d\sigma^h}{dx dz dQ^2} = \frac{\sum_q e_q^2 q(x, Q^2) D_q^h(z, Q^2)}{\sum_q e_q^2 q(x, Q^2)}$$

Depends on the unpolarised parton distribution functions  $q(x, Q^2)$

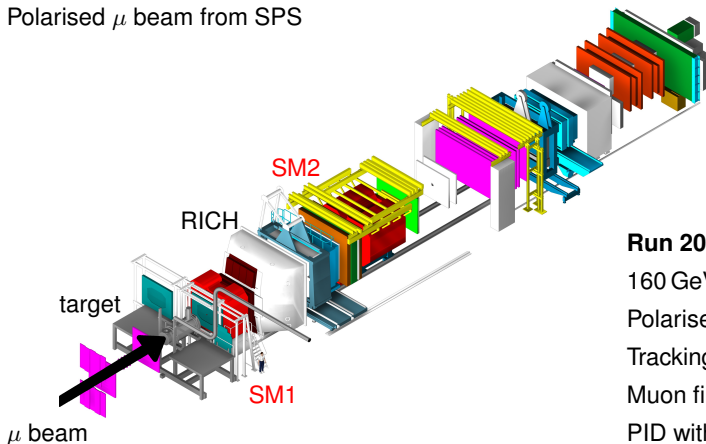
- Unpolarised up/down PDFs well known
- Strange PDFs poorly known

# The COMPASS Experiment

**CO**mmun **M**uon and **P**roton **A**pparatus for **S**tructure and **S**pectroscopy

Fixed target experiment @CERN

Polarised  $\mu$  beam from SPS



**Run 2006:**

160 GeV/c  $\mu^+$

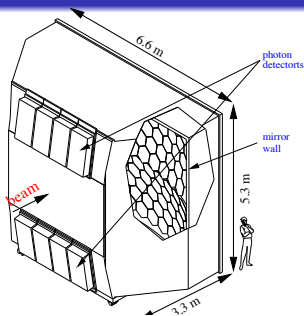
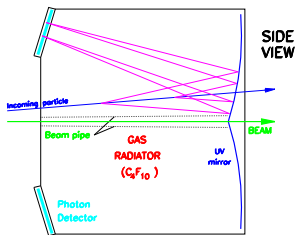
Polarised  ${}^6\text{LiD}$  target

Tracking

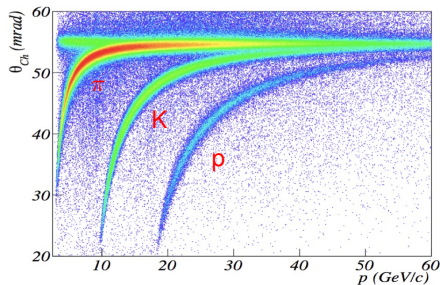
Muon filter for  $\mu'$  ID

PID with RICH

# RICH: Kaon and Pion Separation



- $C_4F_{10}$  radiator gas
- $20 \text{ m}^2$  mirror surface with good UV reflectivity
- Photon detection: MAPMT and MWPC coated with CsI
- $\pi$ -K separation from 10 GeV to 50 GeV





3 weeks of data taking 2006 on  ${}^6\text{LiD}$  target  
 $\approx 700\text{M}$  events from "inclusive" triggers

- Inclusive Kinematic cuts:

$$Q^2 > 1 \text{ GeV}^2$$

$$0.1 < y < 0.9$$

$$0.004 < x < 0.7$$

- Hadron Kinematic cuts:

$$0.2 < z < 0.85$$

$$10 < P_h < 40 \text{ GeV}$$

- Analysis method

3-dimensional binning (x,y,z)

Get raw hadron multiplicities (unidentified and identified)

Correct for apparatus acceptance

Correct for PID efficiencies

## Monte Carlo simulation

- Taking into account geometric acceptance of the apparatus
- Detector efficiencies

LEPTO generator with PDFs

JETSET for hadronisation

GEANT3 with COMPASS detector models

$$A^h(x, y, z) = \frac{M_r^h(x_r, y_r, z_r)}{M_g^h(x_g, y_g, z_g)}$$

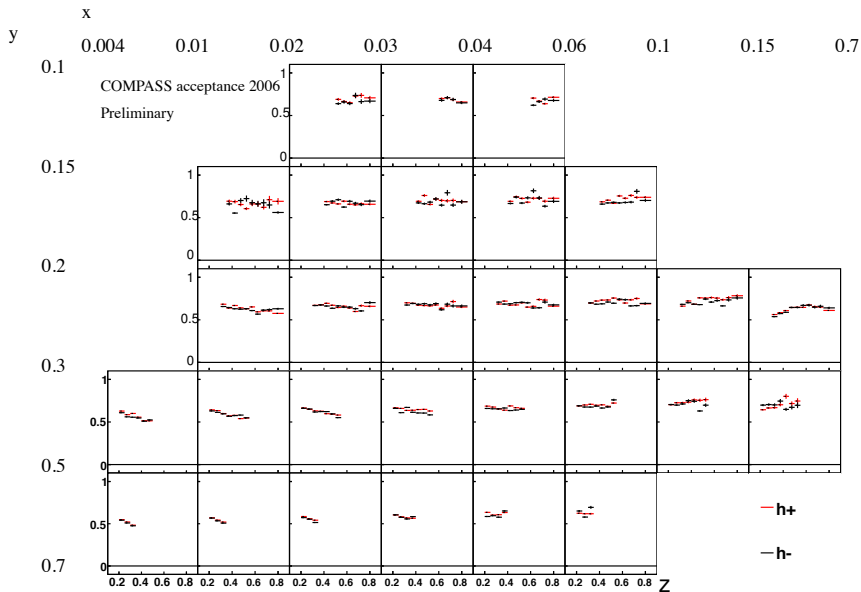
*r* for reconstructed and *g* for generated MC

## LEPTO extrapolation:

Not all bins are completely filled (cuts)

Fill up with LEPTO model

# Acceptance Correction for Unidentified Hadrons



### **Radiative Corrections**

QED radiative effects with TERAD

### **Muon dependent systematics**

Muon acceptance and systematic uncertainties cancel out

### **MC model dependence**

Using different quark fragmentation models in JETSET

Different parton distribution functions in LEPTO

$\approx 5\%$

### **LEPTO dependence**

Effects in smaller and larger  $z$  region

Only using bins where LEPTO contribution is small ( $<10\%$ )

Small systematic uncertainty



Experimental method to extract RICH efficiencies and missidentification  
Tagging hadrons from known decays

$\Lambda^0 \rightarrow p + \pi^-$  for protons,  $K_S^0 \rightarrow \pi^+ + \pi^-$  for pions and  $\phi \rightarrow K^+ + K^-$  for kaons

## RICH table example

- $\pi^+ \rightarrow \pi^+ \approx 98\%$
- $\pi^+ \rightarrow K < 2\%$
- $\pi^+ \rightarrow p < 1\%$

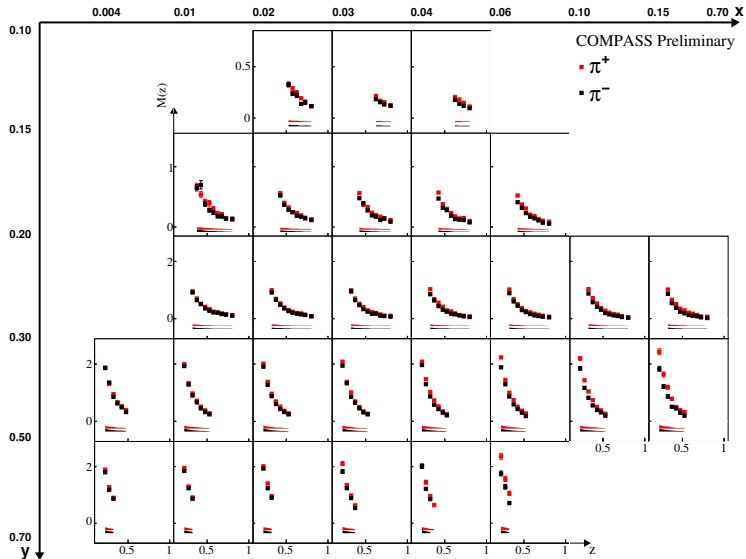
Hadron momentum dependence

$$\begin{pmatrix} I_\pi \\ I_K \\ I_p \end{pmatrix} = \begin{pmatrix} P_\pi^\pi & P_K^\pi & P_p^\pi \\ P_\pi^K & P_K^K & P_p^K \\ P_\pi^p & P_K^p & P_p^p \end{pmatrix} \begin{pmatrix} T_\pi \\ T_K \\ T_p \end{pmatrix}$$
$$\vec{T} = \vec{I} \cdot P^{-1}$$

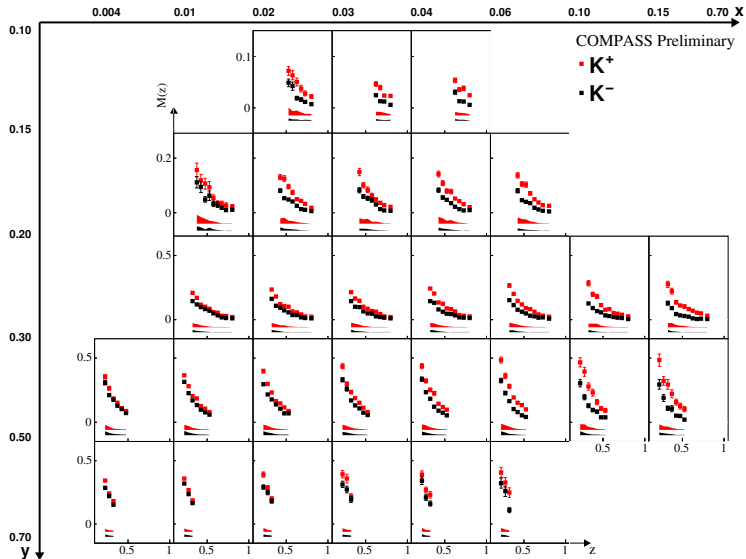
### Systematics:

1% - 3% for pions  
5% - 10% for kaons

# Pion Multiplicities



# Kaon Multiplicities





# The Sum of Charged Kaon Multiplicities

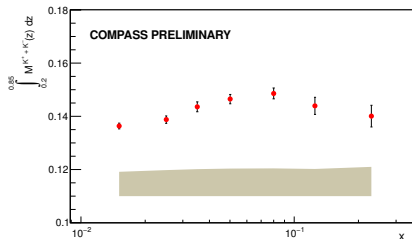
Dependence on strange quark distribution  $s(x)$  and  $D_S^K(z)$

$$\int M^{K^++K^-}(z) dz = \frac{1}{dN^{DIS}/dx} \frac{dN^K}{dx} = \frac{Q(x) \int D_Q^K(z) dz + S(x) \int D_S^K(z) dz}{5Q(x) + 2S(x)}$$

Expanding towards  $\frac{S(x)}{Q(x)}$ :

$$\propto 1 + \frac{S(x)}{Q(x)} \left( \frac{D_S^K}{D_Q^K} - \frac{2}{5} \right)$$

Expecting  $\uparrow S(x)$  with  $\downarrow x$



No visible  $x$  dependence  $\rightarrow$  small  $D_S^K$ ?

## Summary and Outlook

- 2006 run at COMPASS with  ${}^6\text{LiD}$  target and 160 GeV  $\mu^+$  beam
- Measured preliminary pion and kaon multiplicities in x, z, and y
- Final radiative corrections
- Estimation for exclusive vector meson production
- More statistic
- More MC
- QCD fits of FFs
  
- 2012 run on liquid hydrogen
- >2015 long runs with  $\approx 300 \text{ pb}^{-1}$
- Dihadron FFs

Thanks for your attention