



Six “beyond Collins & Sivers” transverse spin asymmetries at COMPASS

UNIVERSITÀ
DEGLI STUDI
DI TORINO

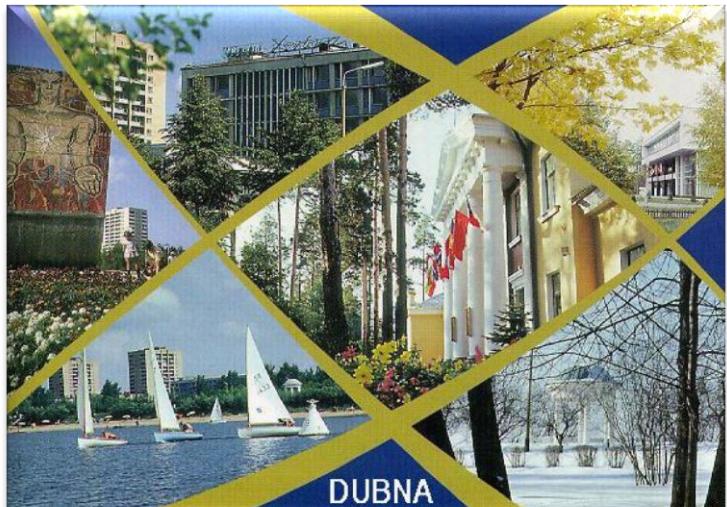
ALMA UNIVERSITAS
TAURINENSIS



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on behalf of the COMPASS Collaboration



The 20th INTERNATIONAL SYMPOSIUM
on Spin Physics (SPIN2012)
JINR, Dubna, Russia
September 17 - 22, 2012



Outline

- Introduction
- COMPASS experiment
- Measured asymmetries and theory expectations
 - Re-evaluation of $A_{LT}^{cos\varphi_S}$ from the lp to $\gamma*p$ cross-section
 - Theory expectations
- Summary

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- **Introduction**
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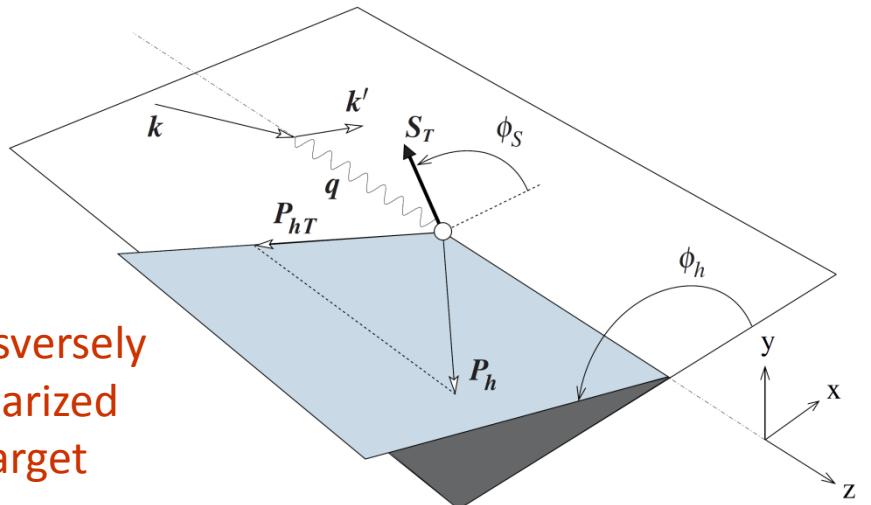
SIDIS x-section

A.Kotzinian, Nucl. Phys. B441, 234 (1995). Bacchetta, Diehl, Goeke, Metz, Mulders and Schlegel JHEP 0702:093,2007

$$\frac{d\sigma}{dxdydzdP_{hT}^2d\phi_h d\psi} = \left[\frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times \\ \left[1 + \cos \phi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \phi_h} + \cos(2\phi_h) \times \varepsilon A_{UU}^{\cos(2\phi_h)} + \lambda \sin \phi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \phi_h} + \right. \\ S_L \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_h A_{UL}^{\sin \phi_h} + \varepsilon \sin(2\phi_h) A_{UL}^{\sin(2\phi_h)} \right] + \\ S_L \lambda \left[\sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_h A_{LL}^{\cos \phi_h} \right] + \\ \left. S_T \left[\begin{array}{l} \sin \phi_S \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \phi_S}) + \\ \sin(\phi_h - \phi_S) \times (A_{UT}^{\sin(\phi_h - \phi_S)}) + \\ \sin(\phi_h + \phi_S) \times (\varepsilon A_{UT}^{\sin(\phi_h + \phi_S)}) + \\ \sin(2\phi_h - \phi_S) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h - \phi_S)}) + \\ \sin(3\phi_h - \phi_S) \times (\varepsilon A_{UT}^{\sin(3\phi_h - \phi_S)}) \end{array} \right] + \right. \\ \left. S_T \lambda \left[\begin{array}{l} \cos \phi_S \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \phi_S}) + \\ \cos(\phi_h - \phi_S) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_S)}) + \\ \cos(2\phi_h - \phi_S) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h - \phi_S)}) \end{array} \right] \right]$$

$$A_{U(L),T}^{w(\phi_h,\phi_s)} = \frac{F_{U(L),T}^{w(\phi_h,\phi_s)}}{F_{UU,T} + \varepsilon F_{UU,L}}$$

$$\varepsilon = \frac{1 - y - \frac{1}{4}\gamma^2 y^2}{1 - y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}, \quad \gamma = \frac{2Mx}{Q}$$



transversely
polarized
target

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$$1 + \cos \varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos \varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \lambda \sin \varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \varphi_h} + \\ S_L \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin \varphi_h A_{UL}^{\sin \varphi_h} + \varepsilon \sin(2\varphi_h) A_{UL}^{\sin(2\varphi_h)} \right] + \\ S_L \lambda \left[\sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \varphi_h A_{LL}^{\cos \varphi_h} \right] +$$

See talk by G. Sbrizzai

See talk by E. Zemlyanichkina

$$\boxed{\begin{aligned} & \sin \varphi_S \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \varphi_S}) + \\ & \sin(\varphi_h - \varphi_S) \times (A_{UT}^{\sin(\varphi_h - \varphi_S)}) + \\ & \sin(\varphi_h + \varphi_S) \times (\varepsilon A_{UT}^{\sin(\varphi_h + \varphi_S)}) + \\ & \sin(2\varphi_h - \varphi_S) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_S)}) + \\ & \sin(3\varphi_h - \varphi_S) \times (\varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_S)}) \end{aligned}} \quad \text{Sivers \& Collins}$$

Presetned by A. Martin

Twist-2

SSA

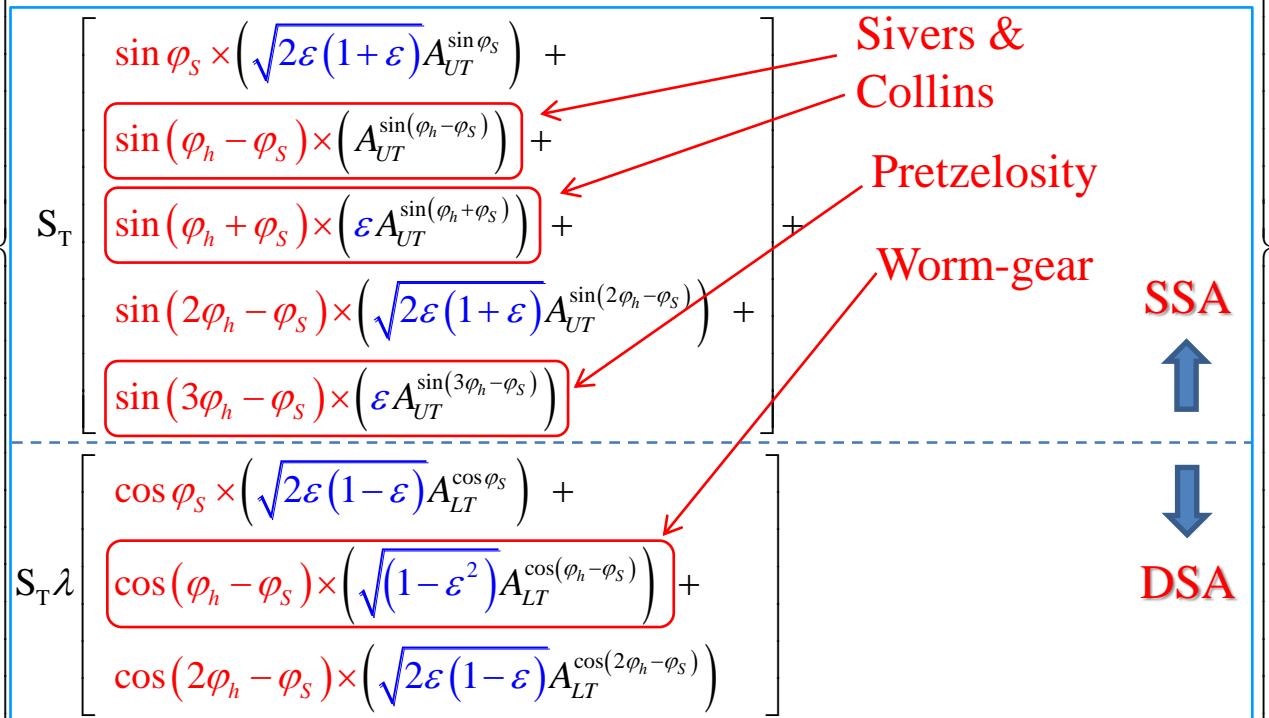
DSA

$$\boxed{\begin{aligned} & \cos \varphi_S \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \varphi_S}) + \\ & \cos(\varphi_h - \varphi_S) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_S)}) + \\ & \cos(2\varphi_h - \varphi_S) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_S)}) \end{aligned}}$$

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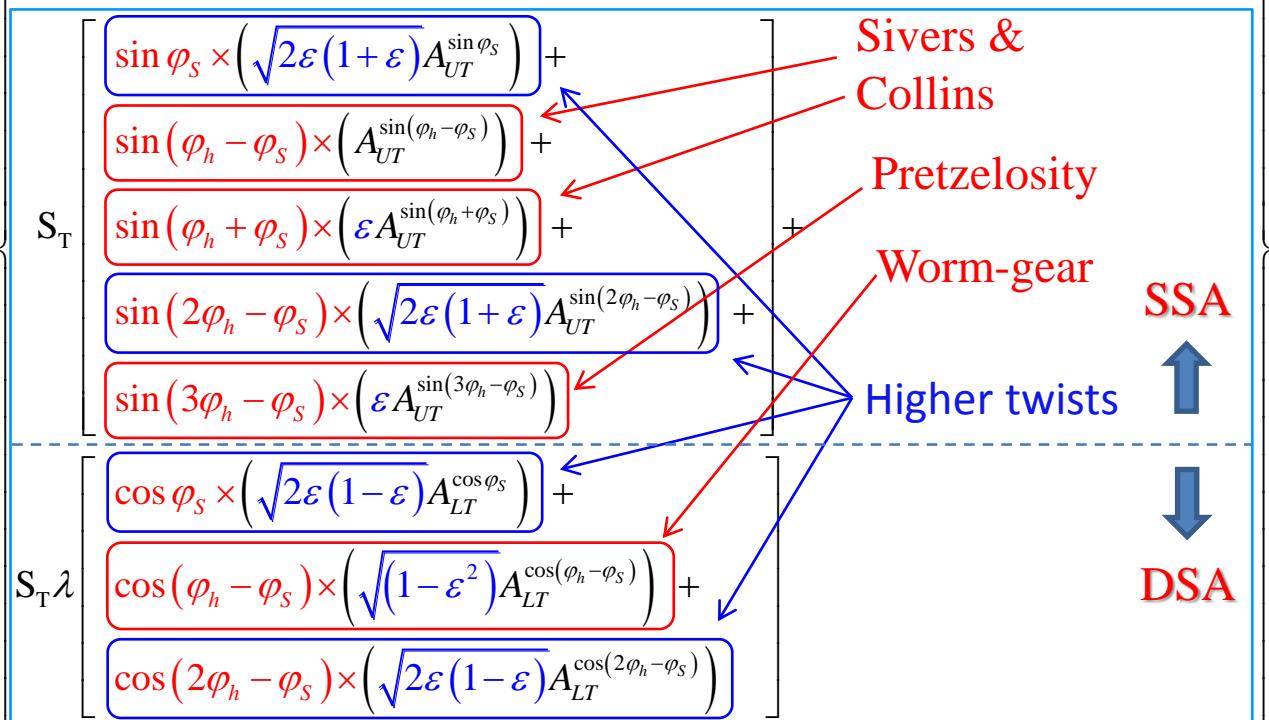
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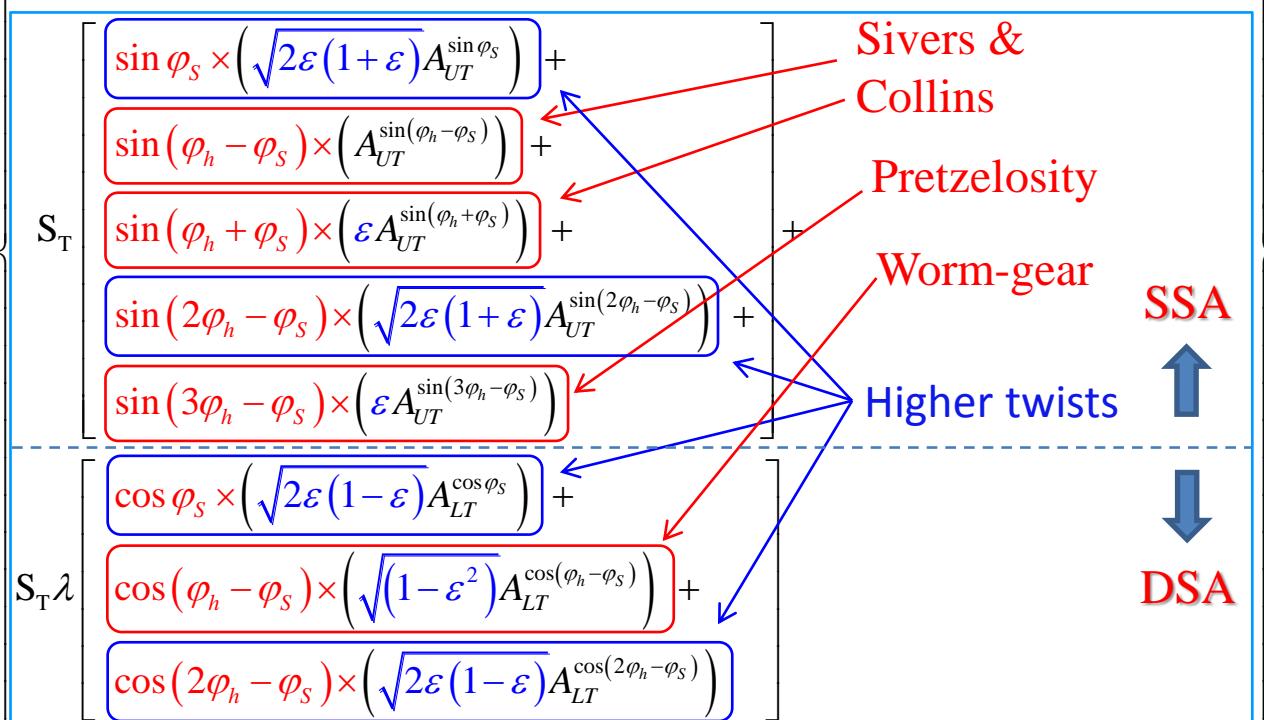
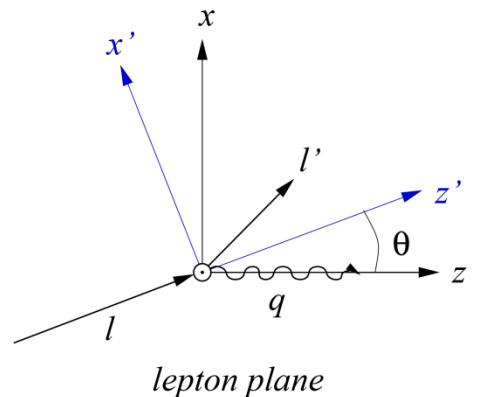
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SIDIS x-section: from lp to $\gamma * p$ ($P_L=0$)

$$\frac{d\sigma}{dxdydzdP_{hT}^2d\varphi_h d\varphi_s} = \left[\frac{\cos\theta}{1 - \sin^2\theta \sin^2\varphi_s} \right] \times \left[\frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times$$

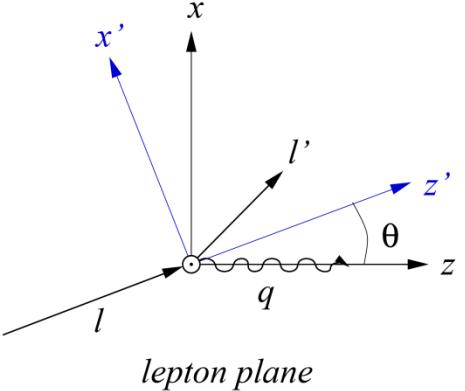
$$\left[1 + \cos\varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \lambda \sin\varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin\varphi_h} + \right.$$

$$\left. \begin{aligned} & \sin\varphi_s \times (\cos\theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\varphi_s}) + \\ & \sin(\varphi_h - \varphi_s) \times \left(\cos\theta A_{UT}^{\sin(\varphi_h - \varphi_s)} + \frac{1}{2} \sin\theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\varphi_h} \right) + \\ & \sin(\varphi_h + \varphi_s) \times \left(\cos\theta \varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)} + \frac{1}{2} \sin\theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\varphi_h} \right) + \\ & \sin(2\varphi_h - \varphi_s) \times \left(\cos\theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)} + \frac{1}{2} \sin\theta \varepsilon A_{UL}^{\sin 2\varphi_h} \right) + \\ & \sin(2\varphi_h + \varphi_s) \times \left(\frac{1}{2} \sin\theta \varepsilon A_{UL}^{\sin 2\varphi_h} \right) + \\ & \sin(3\varphi_h - \varphi_s) \times (\cos\theta \varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)}) \end{aligned} \right] +$$

$$\left[\begin{aligned} & \cos\varphi_s \times (\cos\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\varphi_s} + \sin\theta \sqrt{(1-\varepsilon)^2} A_{LL}) + \\ & \cos(\varphi_h - \varphi_s) \times \left(\cos\theta \sqrt{(1-\varepsilon)^2} A_{LT}^{\cos(\varphi_h - \varphi_s)} + \frac{1}{2} \sin\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\varphi_h} \right) + \\ & \cos(\varphi_h + \varphi_s) \times \left(\frac{1}{2} \sin\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\varphi_h} \right) + \\ & \cos(2\varphi_h - \varphi_s) \times (\cos\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)}) \end{aligned} \right]$$

$\frac{P_T}{\sqrt{1 - \sin^2\theta \sin^2\varphi_s}}$

$\frac{P_T \lambda}{\sqrt{1 - \sin^2\theta \sin^2\varphi_s}}$



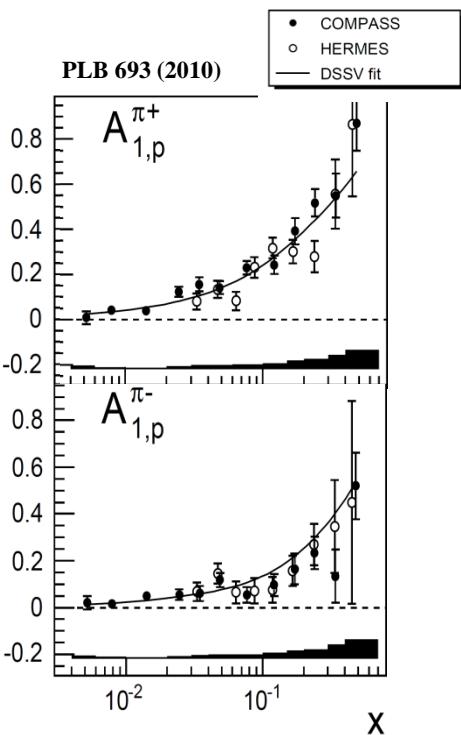
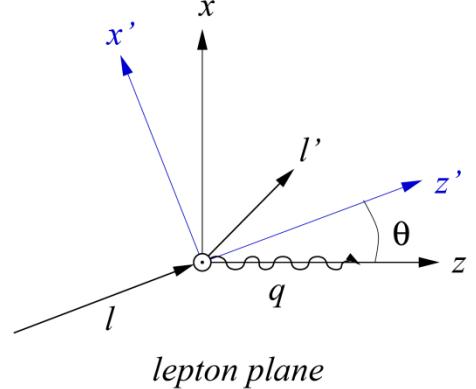
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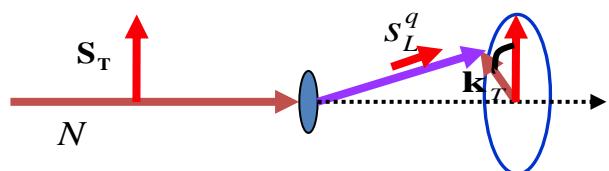
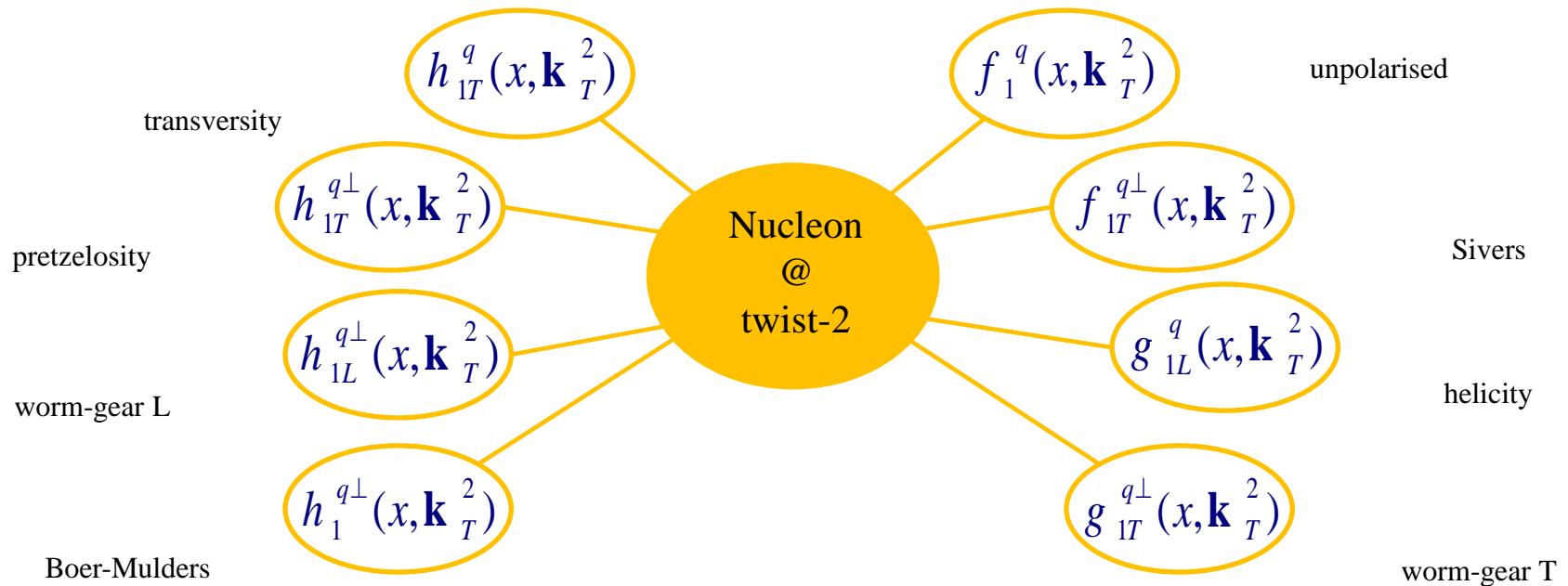
$$\begin{aligned} & \boxed{\cos\varphi_s \times (\cos\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\varphi_s} + \sin\theta \sqrt{(1-\varepsilon)^2} A_{LL}^{\cos\varphi_s})} + \\ & \cos(\varphi_h - \varphi_s) \times \left(\cos\theta \sqrt{(1-\varepsilon)^2} A_{LT}^{\cos(\varphi_h - \varphi_s)} + \frac{1}{2} \sin\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\varphi_h} \right) + \\ & \cos(\varphi_h + \varphi_s) \times \left(\frac{1}{2} \sin\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\varphi_h} \right) + \\ & \cos(2\varphi_h - \varphi_s) \times \left(\cos\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)} \right) \end{aligned}$$



TMD parton distribution functions

Collins, Soper (81,82); Ji, Ma, Yuan (03, 04); Collins, Metz (04) – Definition of TMD DF's and FF's & QCD factorization of SIDIS.

LO QCD = Simple parton model + Factorized twist-2 PDF & FF

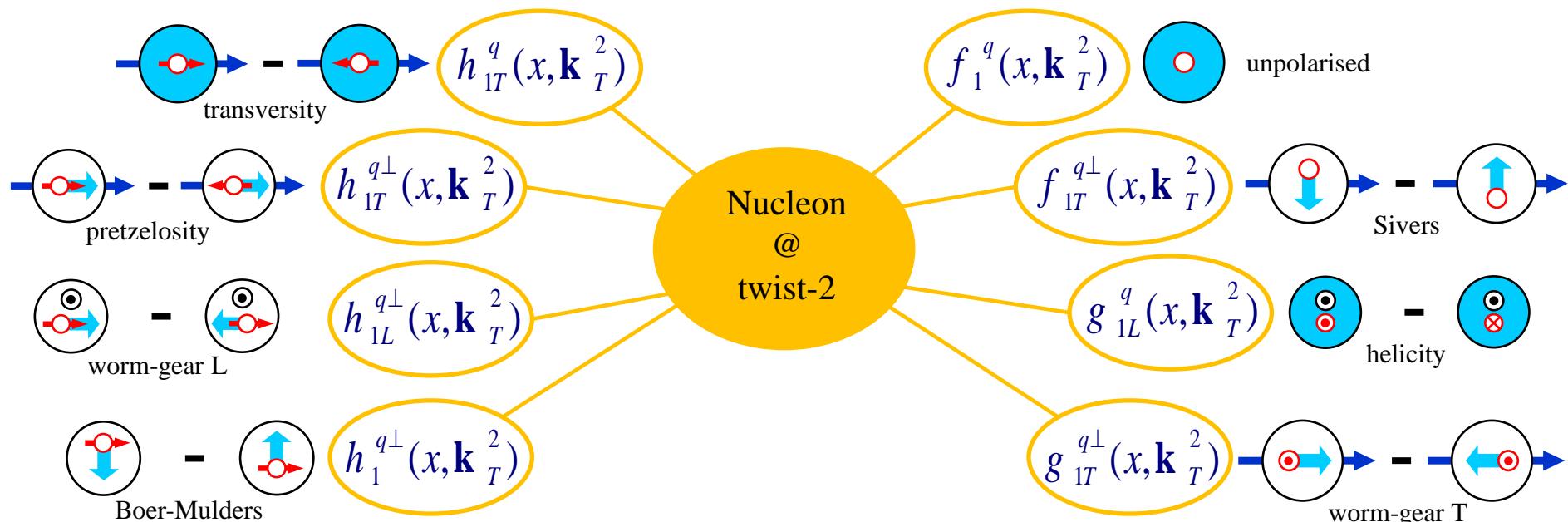


\mathbf{k}_T – intrinsic transverse momentum of the quark

TMD parton distribution functions

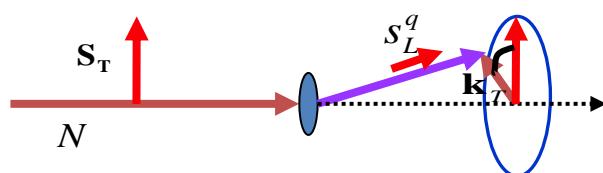
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- → ○ nucleon with transverse or longitudinal spin
- → ● parton with transverse or longitudinal spin
- parton transverse momentum

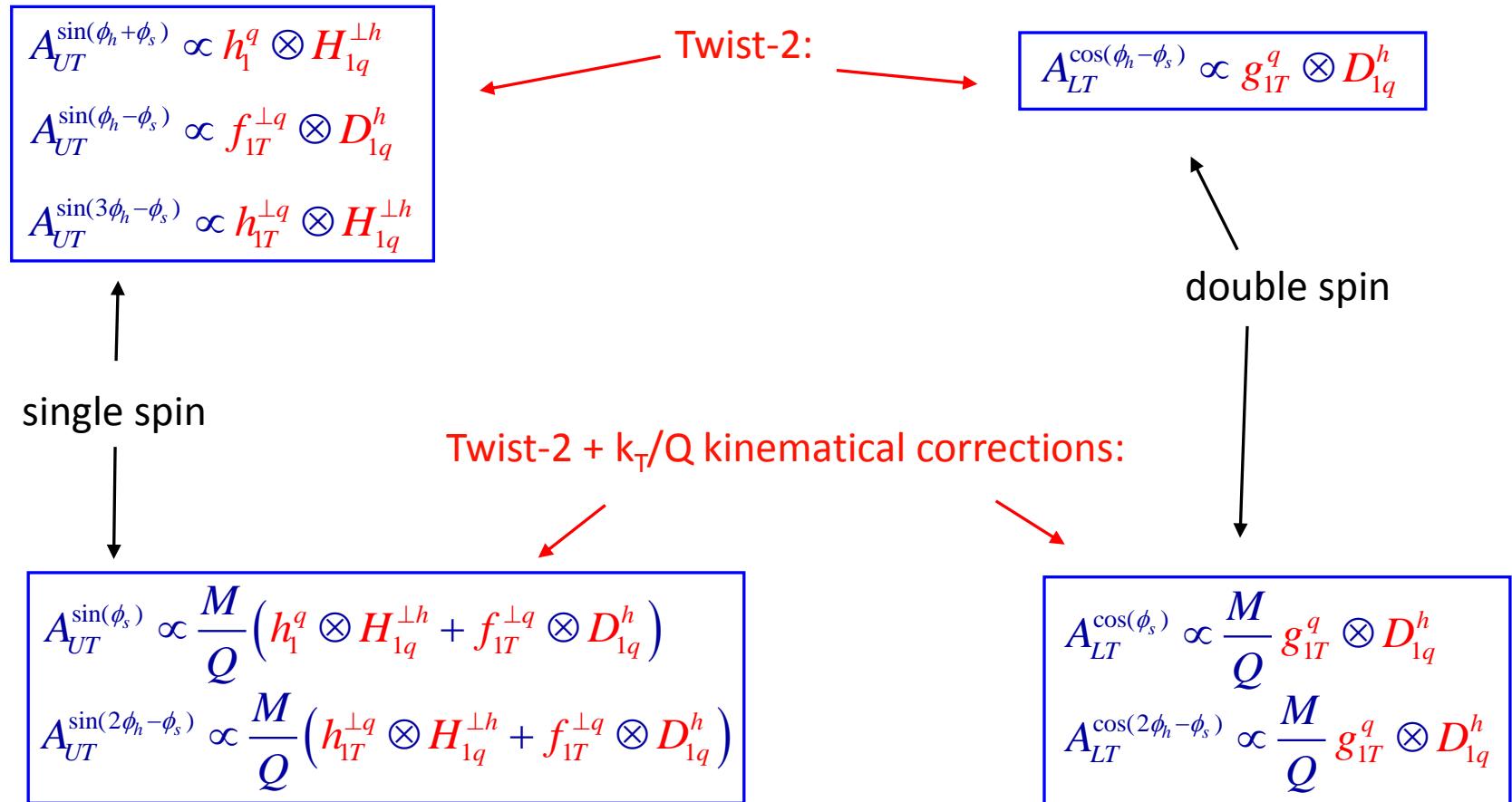
Proton goes out of the screen. Photon goes into the screen



\mathbf{k}_T – intrinsic transverse momentum of the quark

Interpretation of the transverse asymmetries

Within QCD parton model $\gamma A_i \propto DF \otimes FF \quad (i=1..8)$





From “raw” to physics asymmetries

$$A_{UT}^{w(\phi_h, \phi_s)} = \frac{A_{UT, raw}^{w(\phi_h, \phi_s)}}{D^{w(\phi_h, \phi_s)}(y) f |P_T|}, A_{LT}^{w(\phi_h, \phi_s)} = \frac{A_{LT, raw}^{w(\phi_h, \phi_s)}}{D^{w(\phi_h, \phi_s)}(y) f P_{beam} |P_T|}$$

$$D^{\sin(\phi_h - \phi_s)}(y) = 1$$

$$D^{\sin(\phi_h + \phi_s)}(y) = D^{\sin(3\phi_h - \phi_s)}(y) = \varepsilon \approx \frac{2(1-y)}{1+(1-y)^2}$$

$$D^{\sin(2\phi_h - \phi_s)}(y) = D^{\sin(\phi_s)}(y) = \sqrt{2\varepsilon(1+\varepsilon)} \approx \frac{2(2-y)\sqrt{1-y}}{1+(1-y)^2}$$

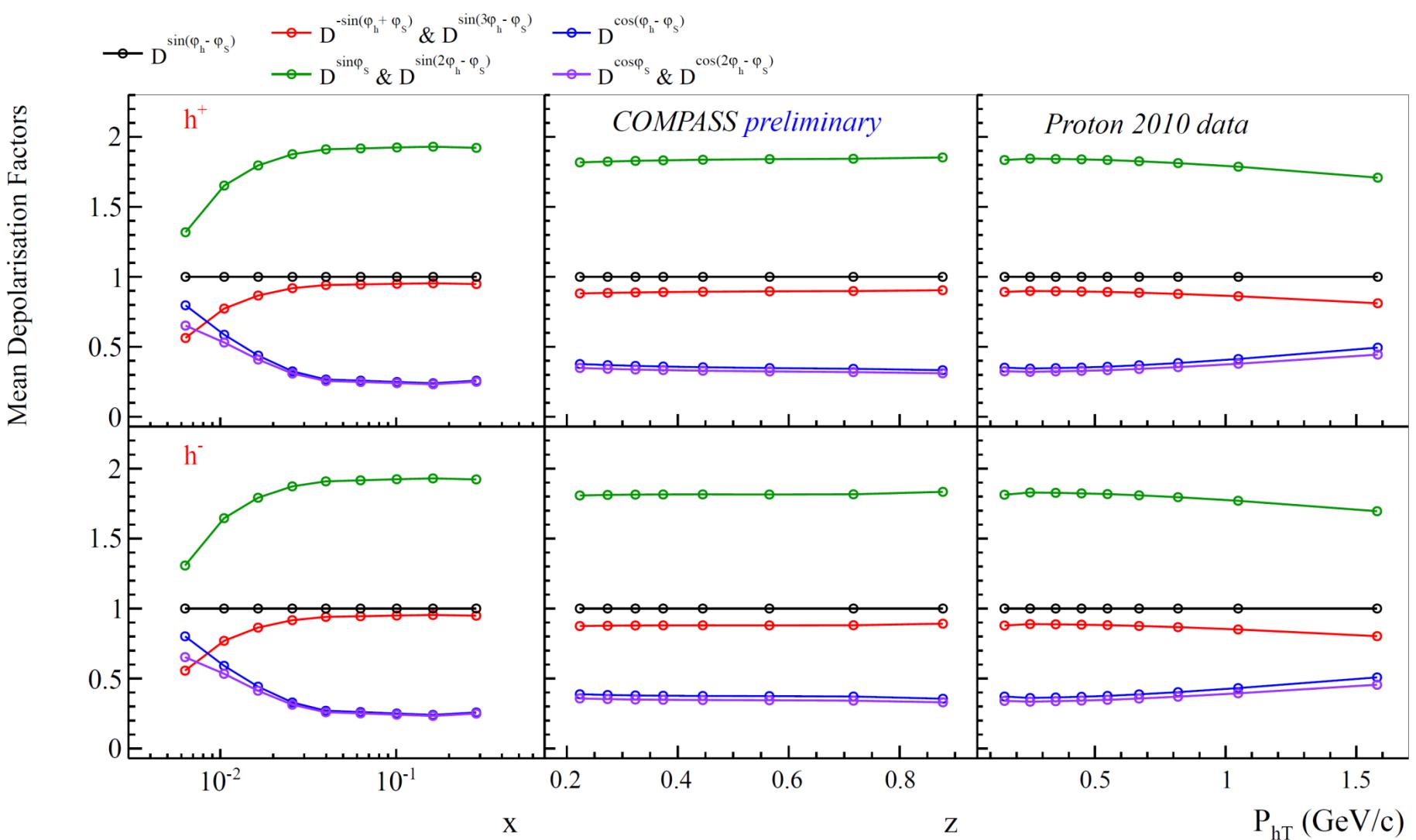
$$D^{\cos(2\phi_h - \phi_s)}(y) = D^{\cos(\phi_s)}(y) = \sqrt{2\varepsilon(1-\varepsilon)} \approx \frac{2y\sqrt{1-y}}{1+(1-y)^2}$$

$$D^{\cos(\phi_h - \phi_s)}(y) = \sqrt{(1-\varepsilon^2)} \approx \frac{y(2-y)}{1+(1-y)^2}$$

$$\varepsilon = \frac{1-y - \frac{1}{4}\gamma^2 y^2}{1-y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}, \quad \gamma = \frac{2Mx}{Q}$$

$D^{w_i(\phi_h, \phi_s)}$ – Depolarization factor, f - target dilution factor, P_T - target polarization, P_{beam} - beam polarization

Mean Depolarization Factors



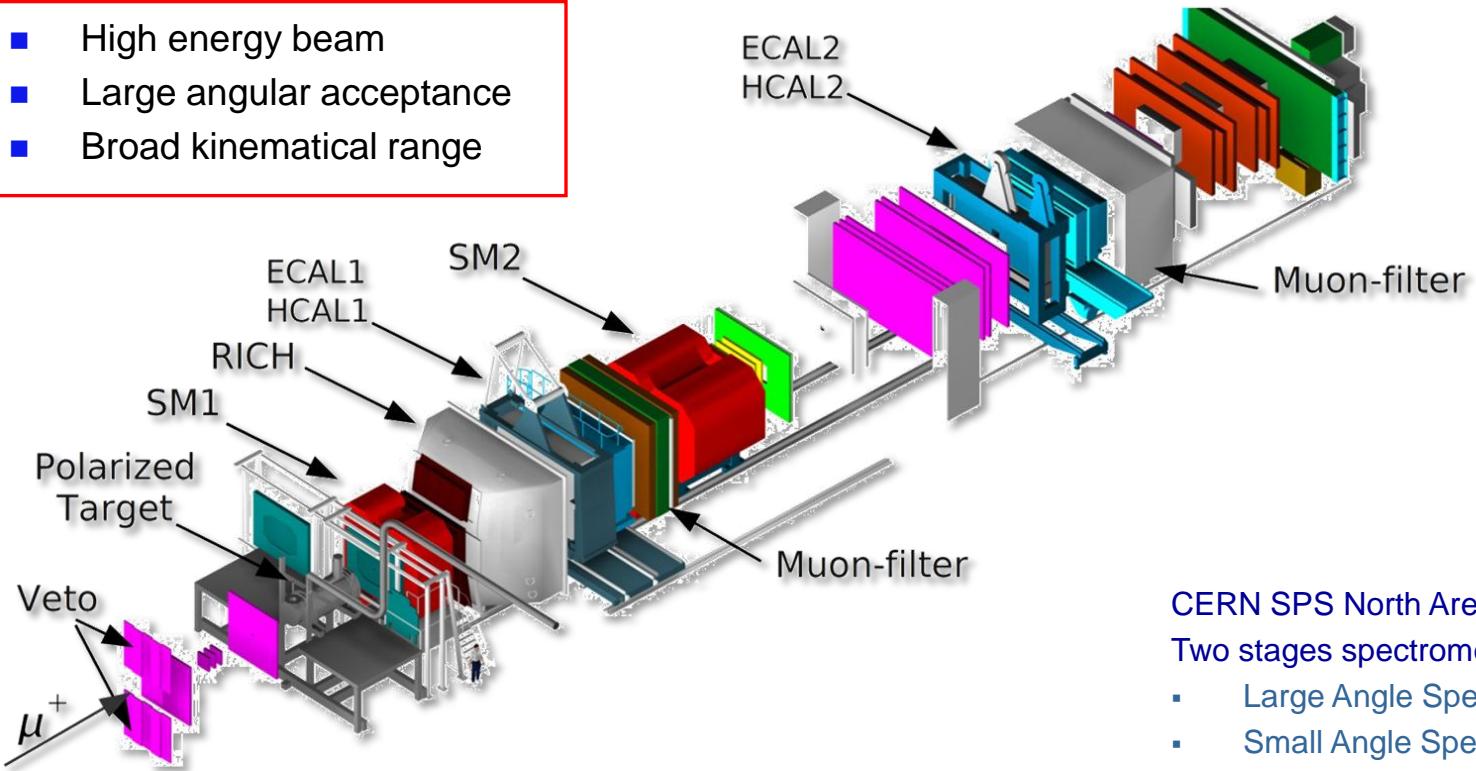
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COMPASS experimental setup

COmmon Muon Proton Apparatus for Structure and Spectroscopy

- High energy beam
- Large angular acceptance
- Broad kinematical range



Longitudinally polarized μ^+ beam (160 GeV/c).

Longitudinally or Transversely polarized ${}^6\text{LiD}$ or NH_3 target

Momentum, tracking and calorimetric measurements, PID

CERN SPS North Area.

Two stages spectrometer

- Large Angle Spectrometer (SM1)
- Small Angle Spectrometer (SM2)

Hadron & Muon high energy beams.

Beam rates: 10^8 muons/s, $5 \cdot 10^7$ hadrons/s.

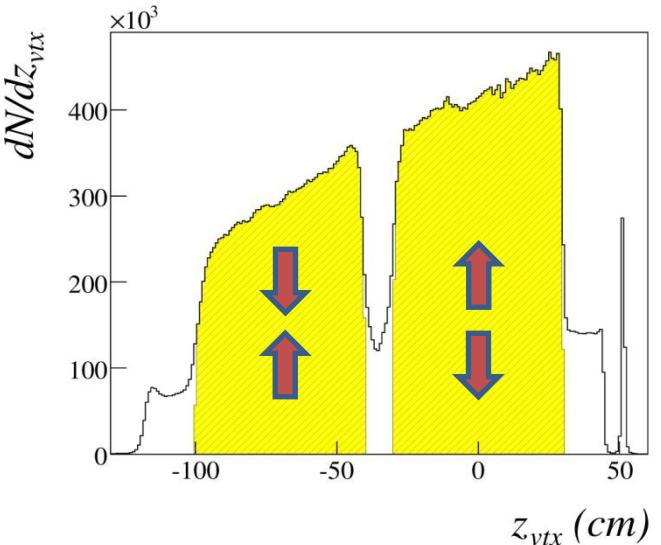
COMPASS Polarized target system

solid state target operated in frozen spin mode

Years 2002-2004

Deuteron - ${}^6\text{LiD}$:

- Two 60 cm long ${}^6\text{LiD}$ cells with opposite polarization
- Polar angle acceptance – 70 mrad
- Target Polarization $\pm 50\%$
- dilution factor $f = 0.38$

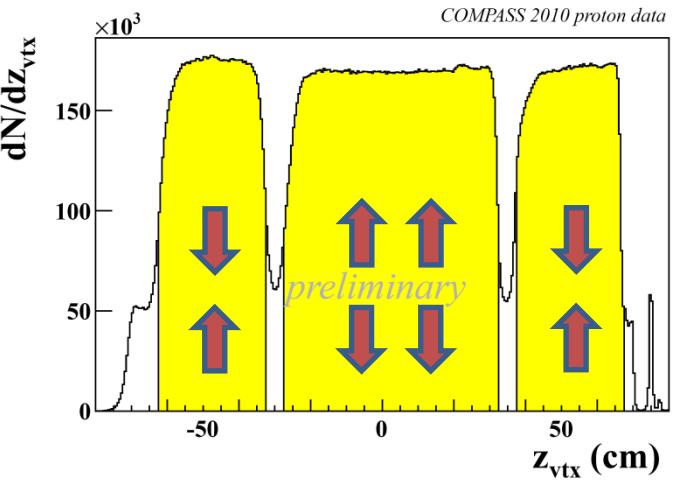


Data is collected simultaneously for the two target spin orientations
Polarization reversal after each ~4-5 days

Years 2007 and 2010

Proton - NH_3 :

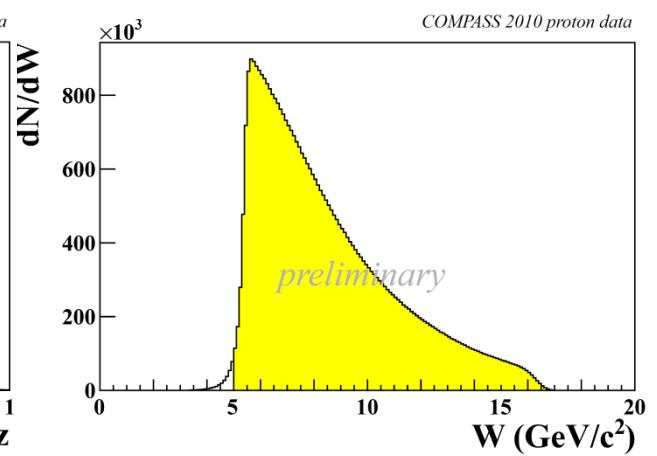
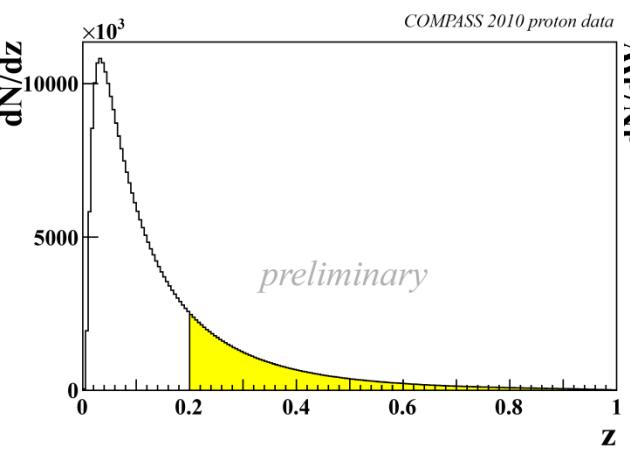
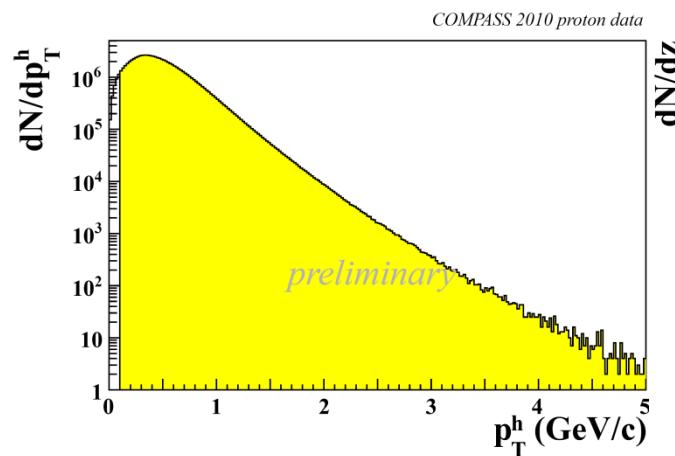
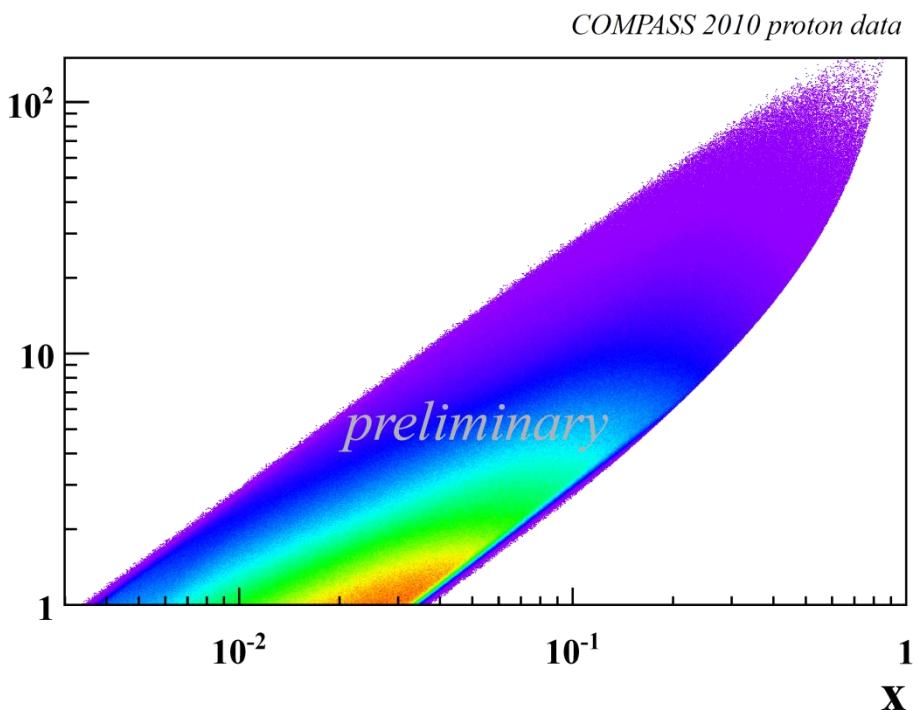
- Three cells system (30 cm, 60cm, 30cm)
- Polar angle acceptance – 180 mrad (new magnet in 2006)
- Target Polarization $\pm 90\%$
- dilution factor $f = 0.14$



Data selection

- DIS cuts :
 - $Q^2 > 1 \text{ GeV}^2$
 - $0.1 < y < 0.9$
 - $W > 5 \text{ GeV}$

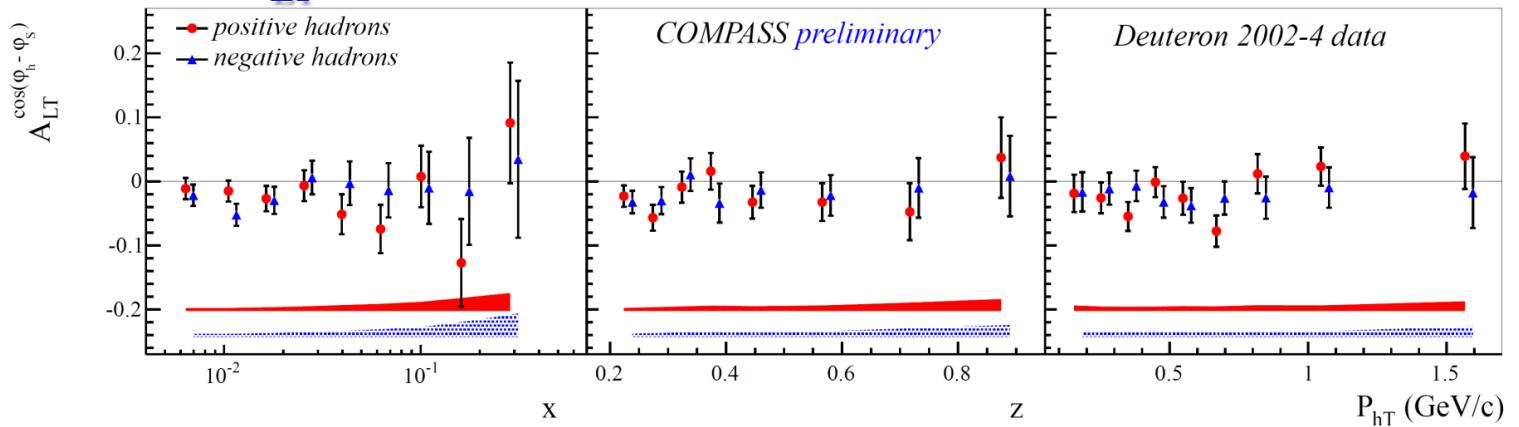
- Hadron cuts :
 - $z > 0.2$
 - $P_{hT} > 0.1 \text{ GeV}/c$



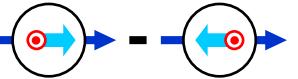
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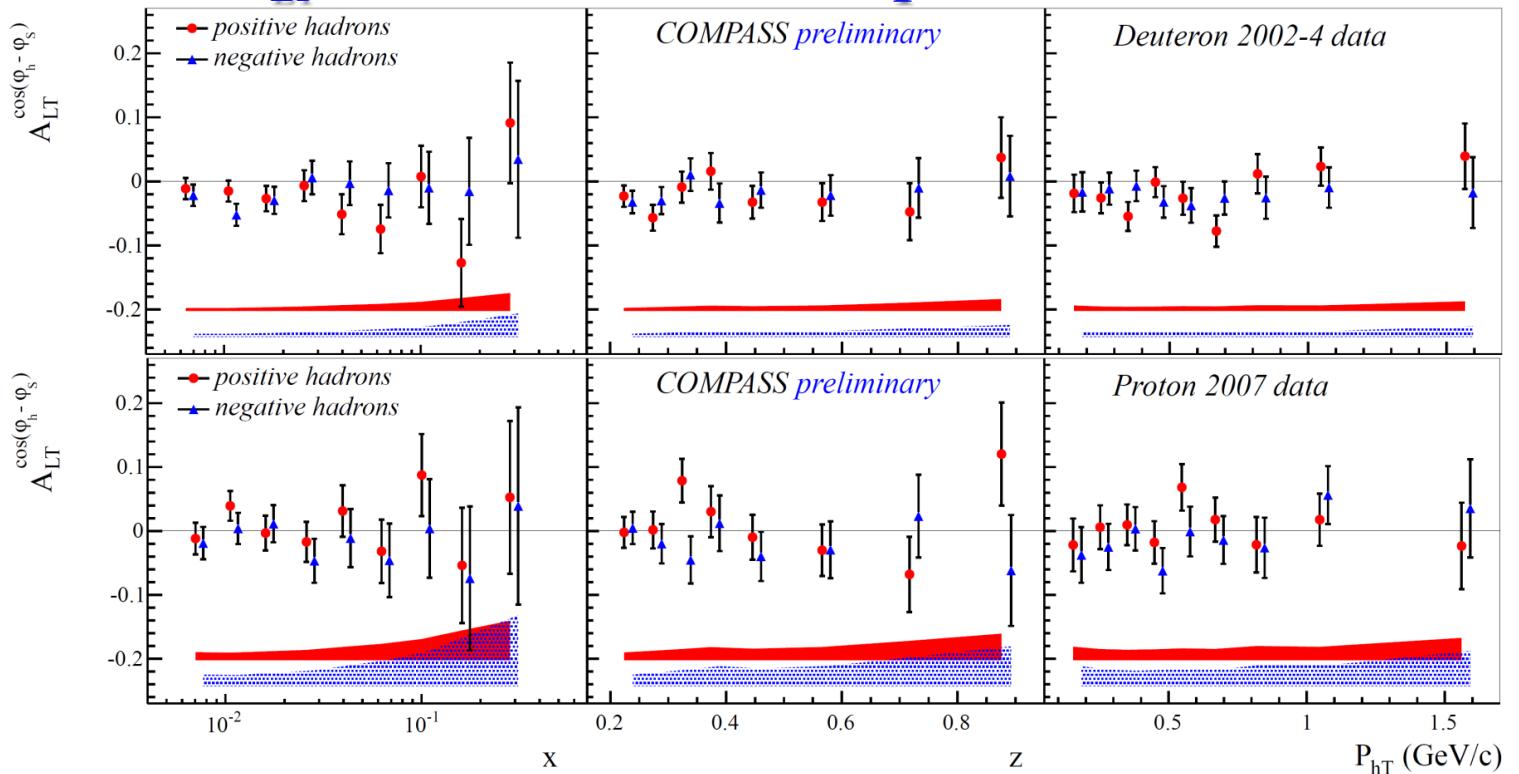
Results for $A_{LT}^{\cos(\phi_h - \phi_s)}$ deuteron



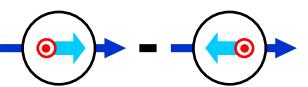
$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$, "Worm Gear" PDF g_{1T}^q :



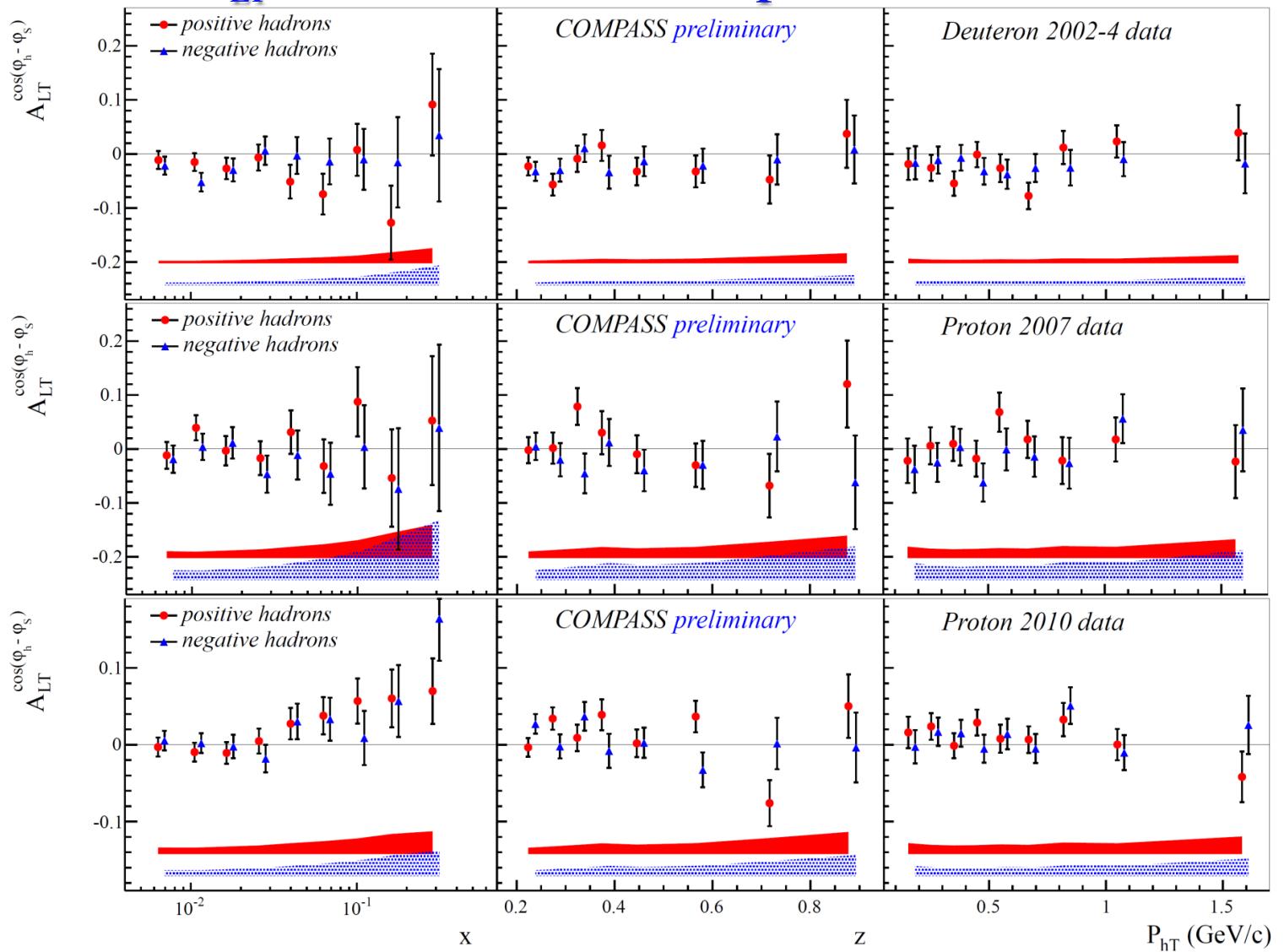
Results for $A_{LT}^{\cos(\phi_h - \phi_s)}$ deuteron & proton 2007



$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$, "Worm Gear" PDF g_{1T}^q :

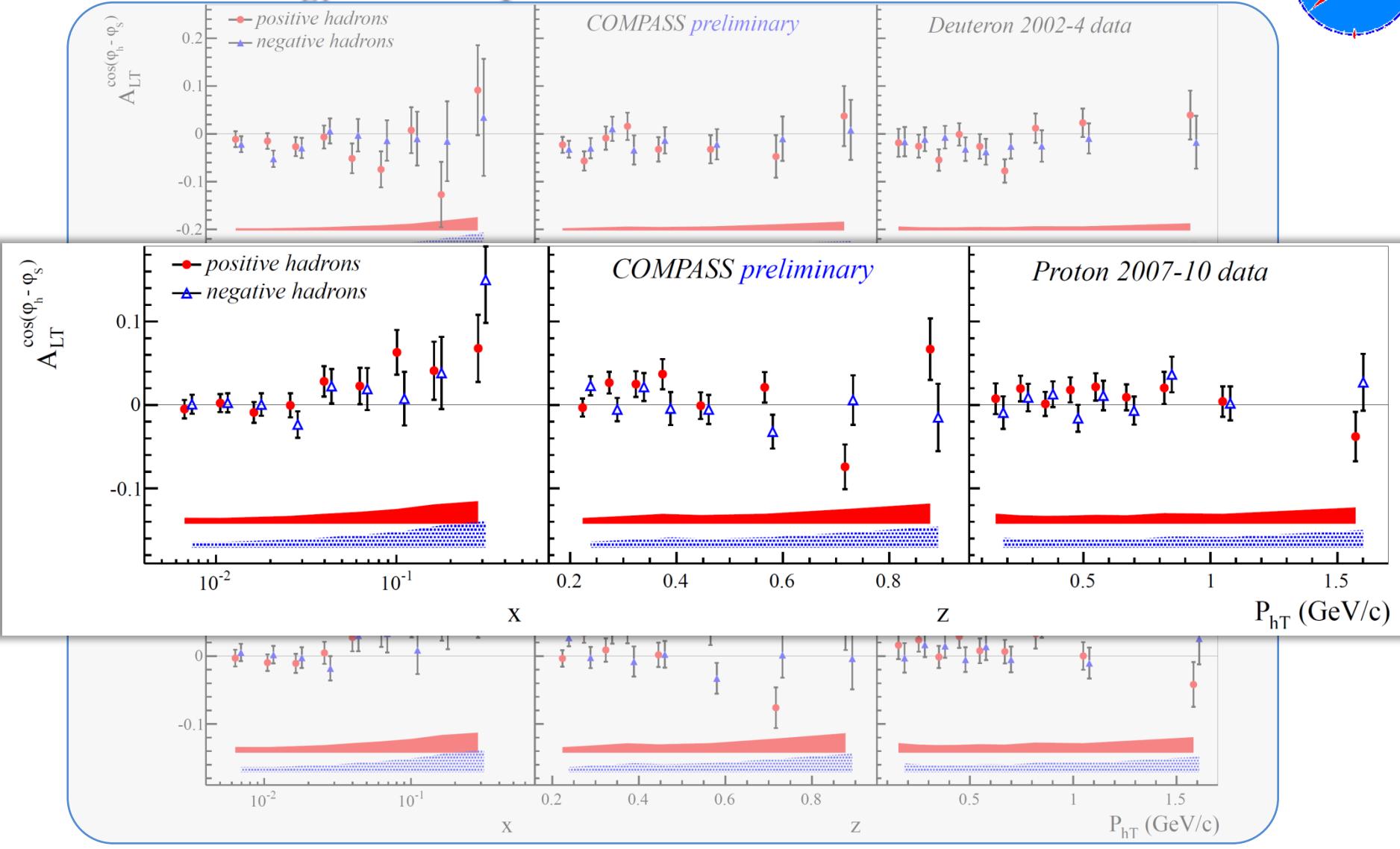


Results for $A_{LT}^{\cos(\phi_h - \phi_s)}$ deuteron & proton



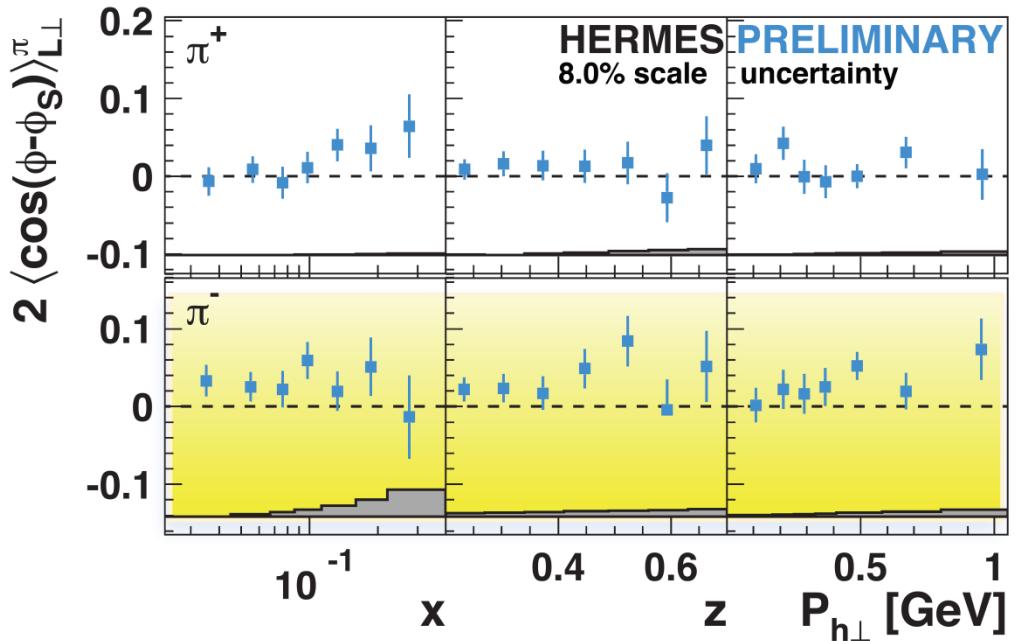
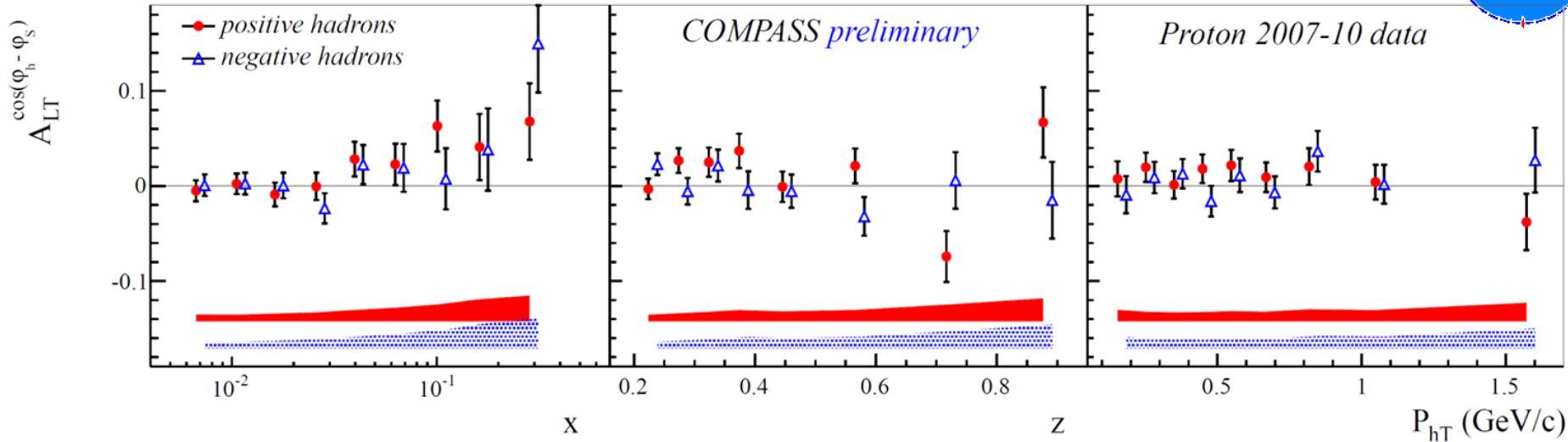
$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$, "Worm Gear" PDF g_{1T}^q :

Results for $A_{LT}^{\cos(\phi_h - \phi_s)}$ proton 2007-2010



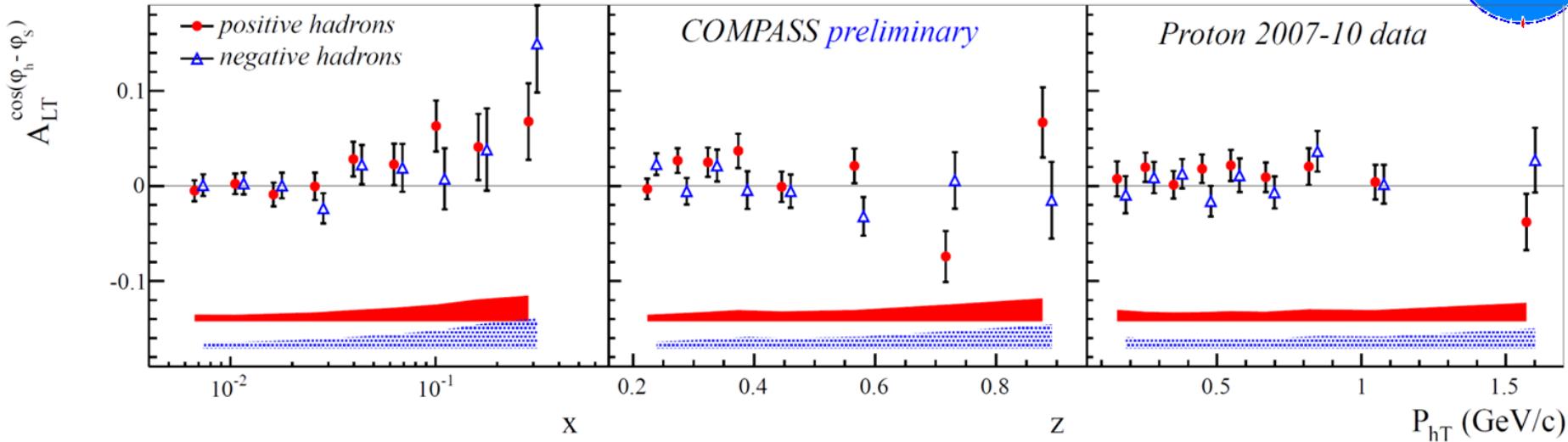
$$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h, \text{ "Worm Gear" PDF } g_{1T}^q : \text{---} \circlearrowleft \rightarrow \text{---} \circlearrowright \rightarrow$$

Results for $A_{LT}^{\cos(\phi_h - \phi_s)}$ COMPASS - HERMES

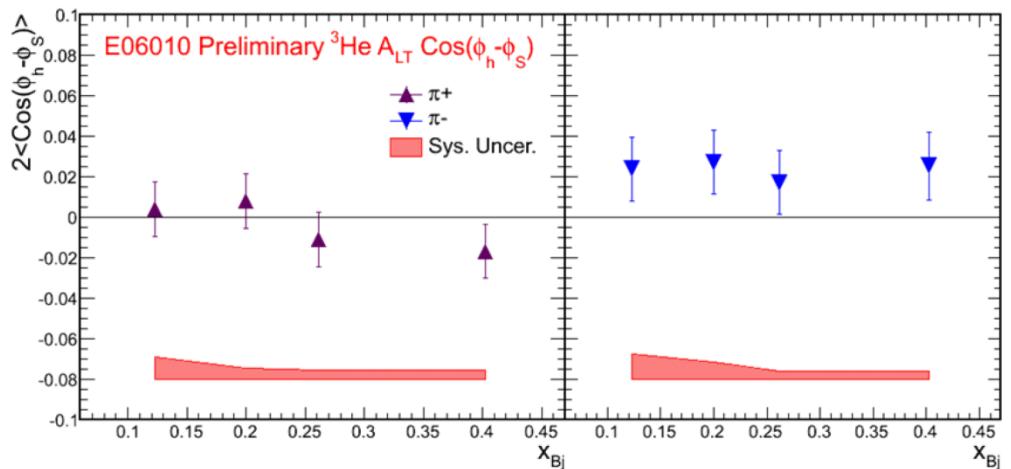


Similar trend for $A_{LT}^{\cos(\phi_h - \phi_s)}$
asymmetry is present in HERMES
preliminary results.

Results for $A_{LT}^{\cos(\phi_h - \phi_s)}$ COMPASS - JLab



${}^3\text{He}$ double-spin asymmetry A_{LT}



$$\propto \frac{g_{1T}^{\perp q}(x) \otimes D_{1q}^h(z)}{f_1^q(x) \otimes D_{1q}^h(z)}$$

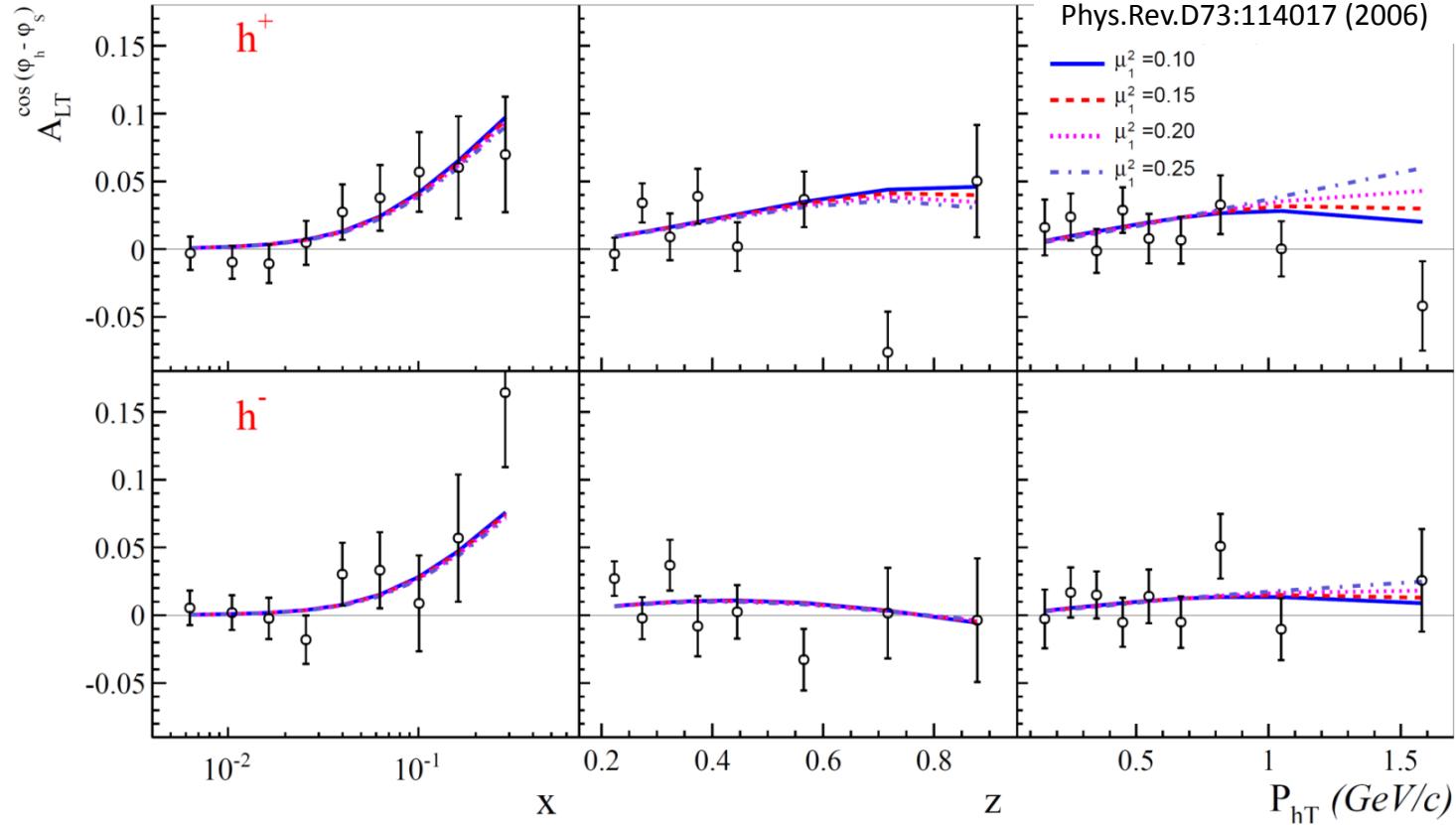
- First observation of a none-zero A_{LT} .
- First measurement on neutron(${}^3\text{He}$).
- Relate to quark TMD $g_{1T}(x, k_T)$.
- The real part of quark L=0 \otimes L=1 interference, “twin-brother” of Sivers.

Ph.D. thesis of J. Huang (MIT 2011).

$A_{LT}^{\cos(\phi_h - \phi_s)}$ and predictions from PRD 73, 114017(2006)

COMPASS *preliminary* Proton 2010

A. Kotzinian, B. Parsamyan, A. Prokudin
Phys.Rev.D73:114017 (2006)



Calculations are done using:
for g_{1T} the model:

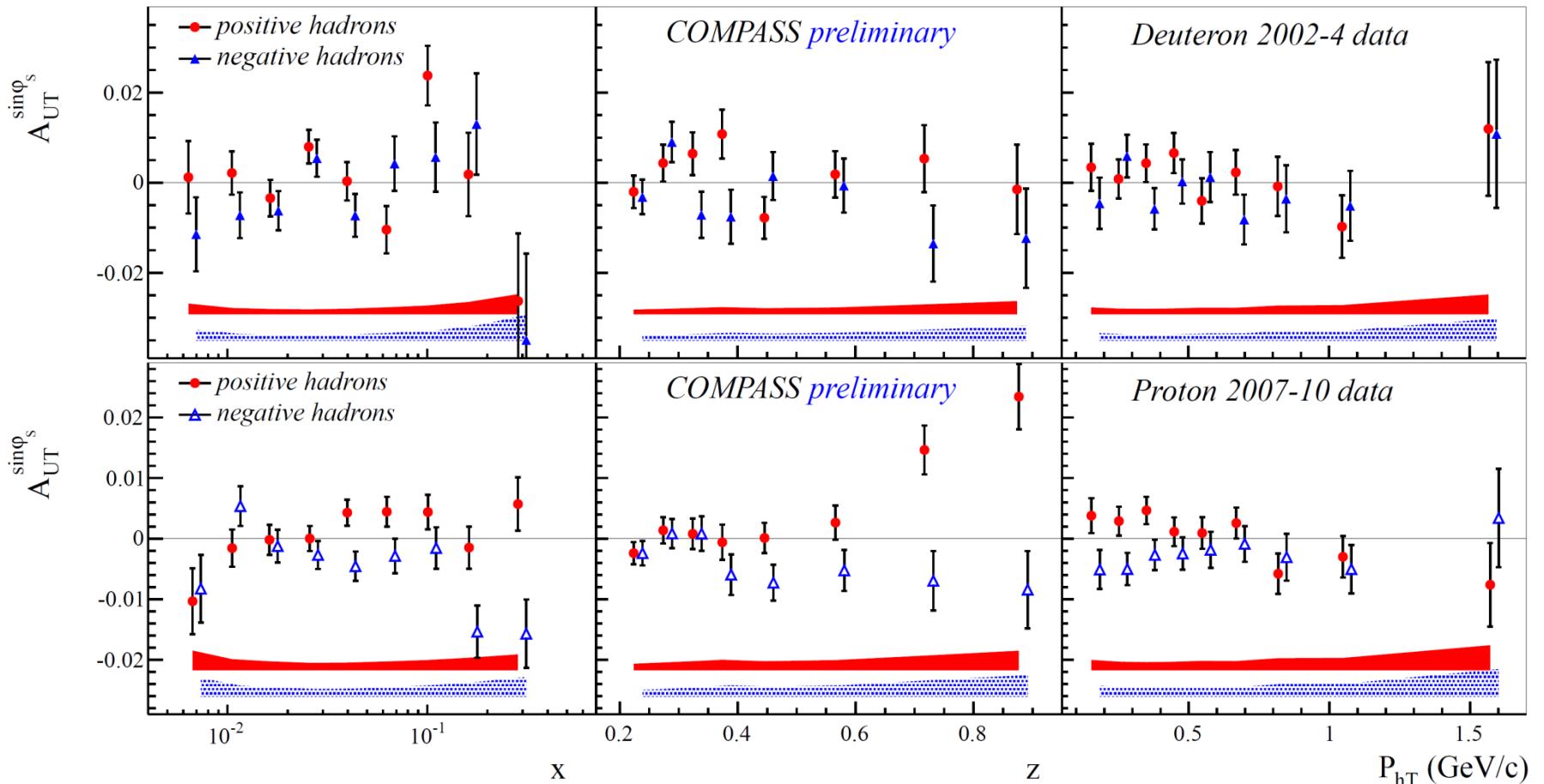
$$g_{1T}^{q(1)}(x, k_T^2) \approx x \int_x^1 dy \frac{g_1^q(y)}{y}$$

based on the Wandzura and Wilczek approximation;
Gaussian parameterization for k_T dependence;
LO GRV, GRV2000 DFs
and Kretzer FFs

Asymmetry is evaluated in COMPASS specific mean kinematic points extracted from the data.
The predictions shows a good level of agreement with the experimentally extracted asymmetry

$$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h, \quad \text{"Worm Gear" PDF } g_{1T}^q : \text{---} \rightarrow \text{---} \leftarrow \text{---} \rightarrow$$

Results for $A_{UT}^{\sin\phi_s}$ on deuteron and proton

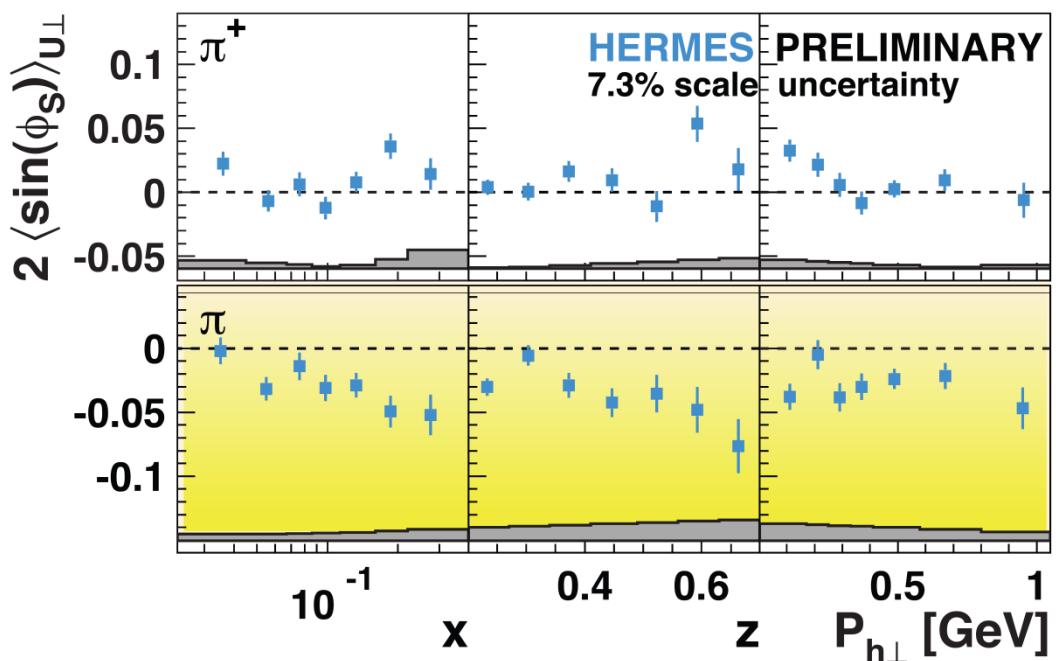
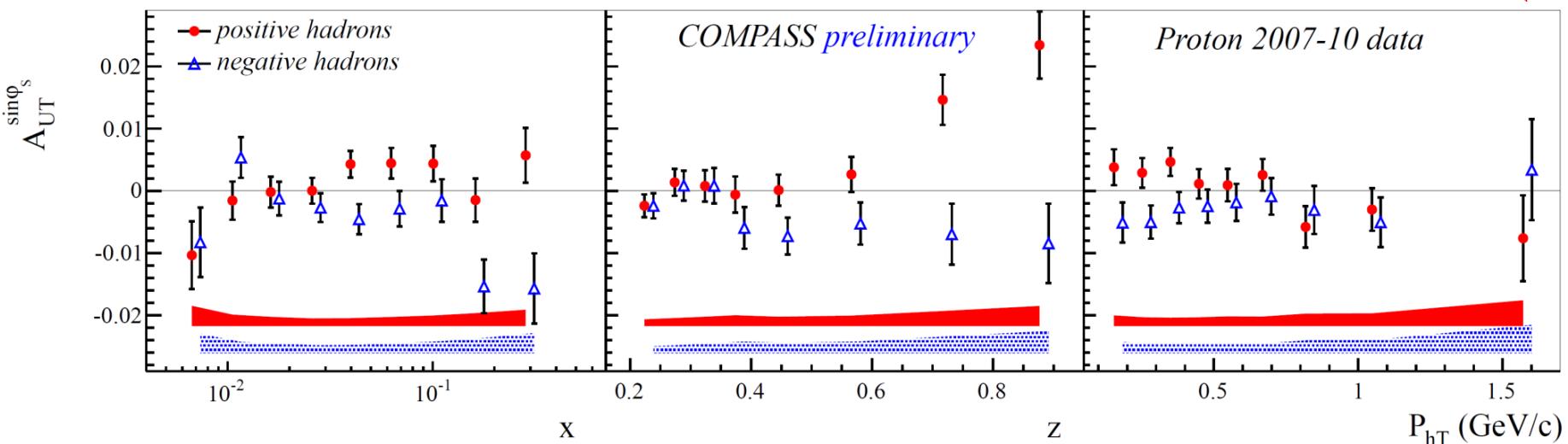


$$A_{UT}^{\sin\phi_s} \propto \frac{M}{Q} \left(h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h \right) + \dots$$

"Transversity" PDF h_1^q :

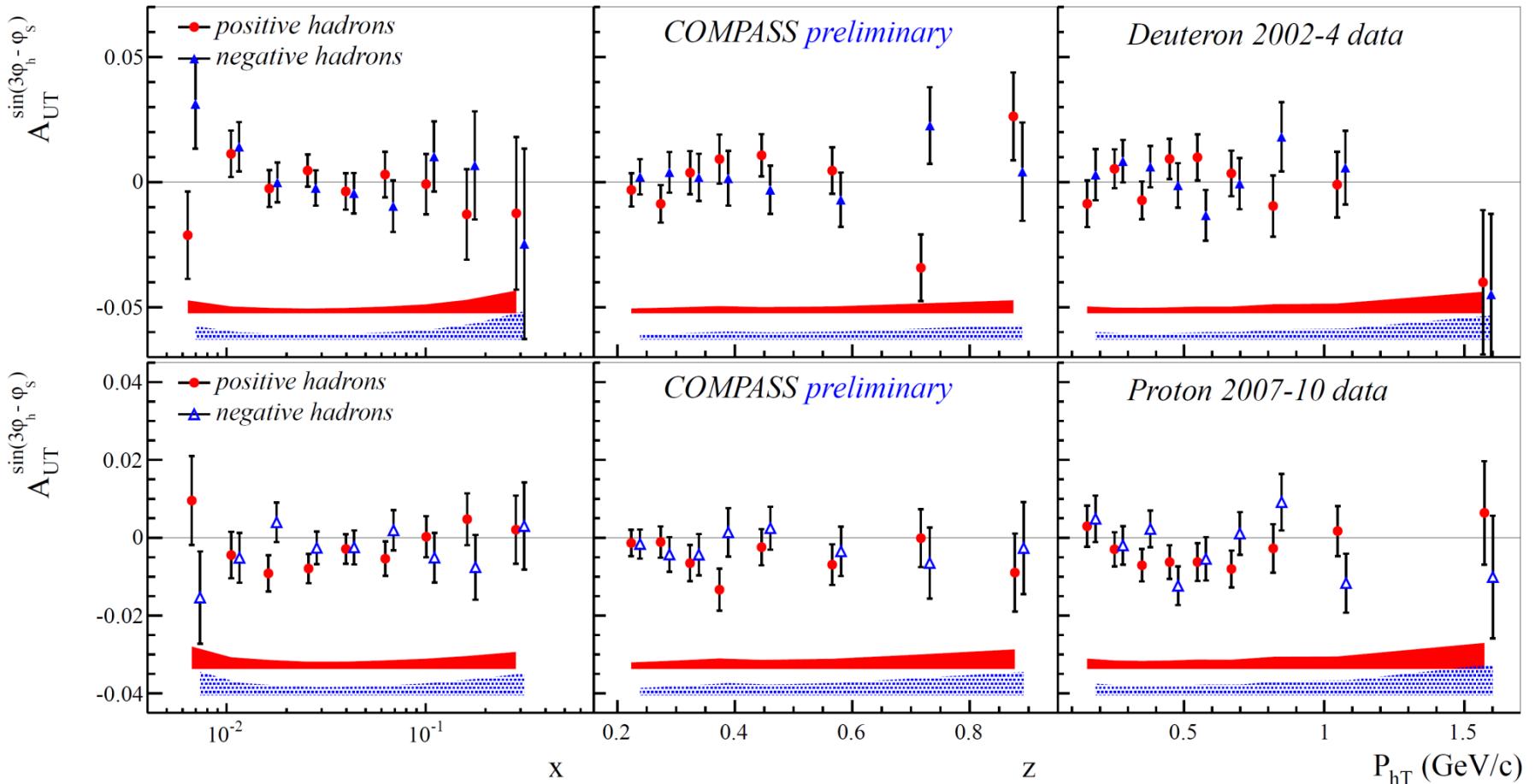
"Sivers" PDF $f_{1T}^{\perp q}$:

Results for $A_{UT}^{sin\phi_s}$ COMPASS - HERMES



Signs of a non-zero $A_{UT}^{sin\phi_s}$ asymmetry have been observed both by HERMES and COMPASS.

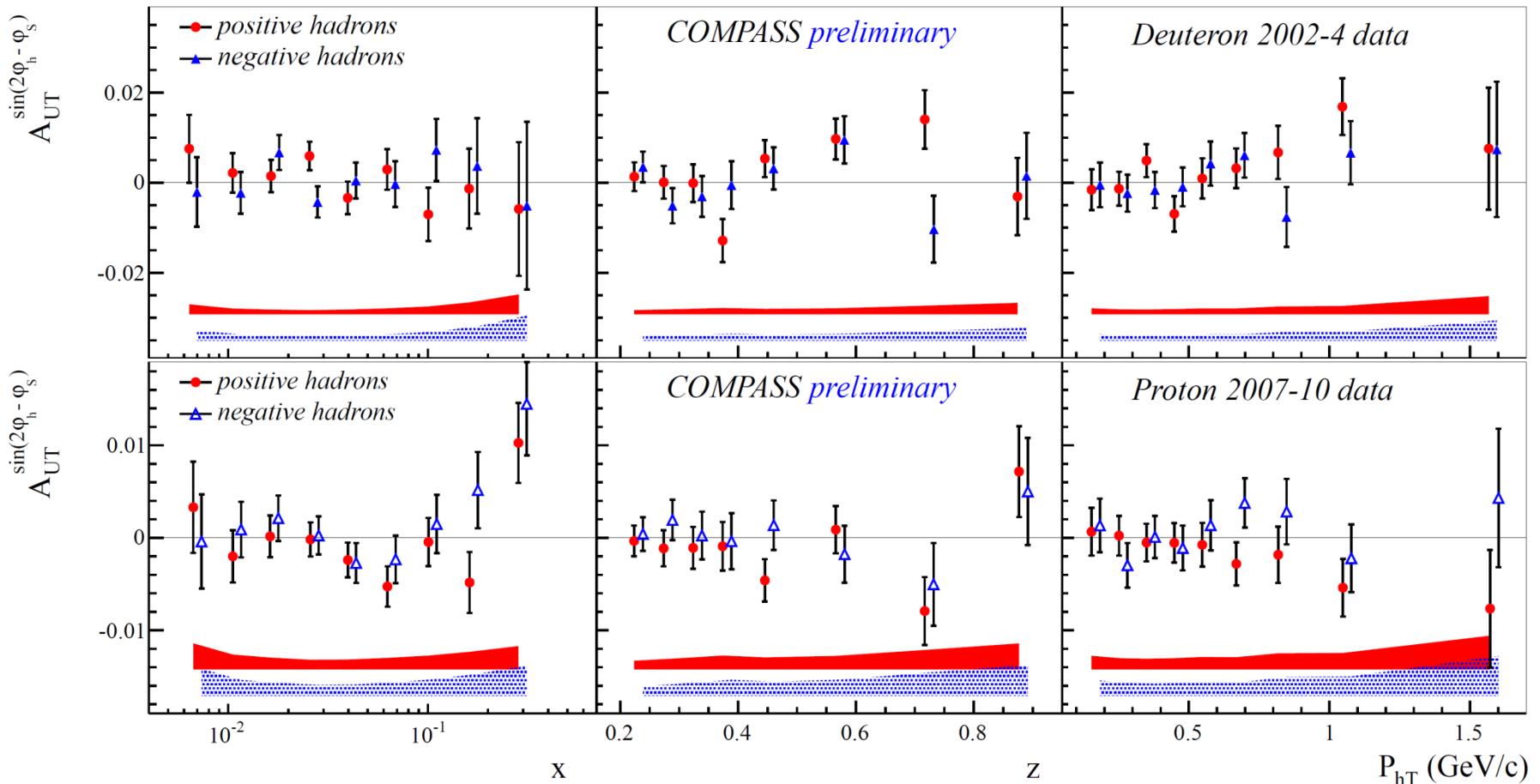
Results for $A_{UT}^{\sin(3\phi_h - \phi_s)}$ deuteron & proton



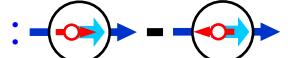
$$A_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}, \text{ "Pretzelosity" PDF } h_{1T}^{\perp q} : \text{---} \circlearrowleft \rightarrow \text{---} \circlearrowright \rightarrow$$

Asymmetries for both proton and deuteron are compatible with zero within uncertainties

Results for $A_{UT}^{\sin(2\phi_h - \phi_s)}$ deuteron & proton



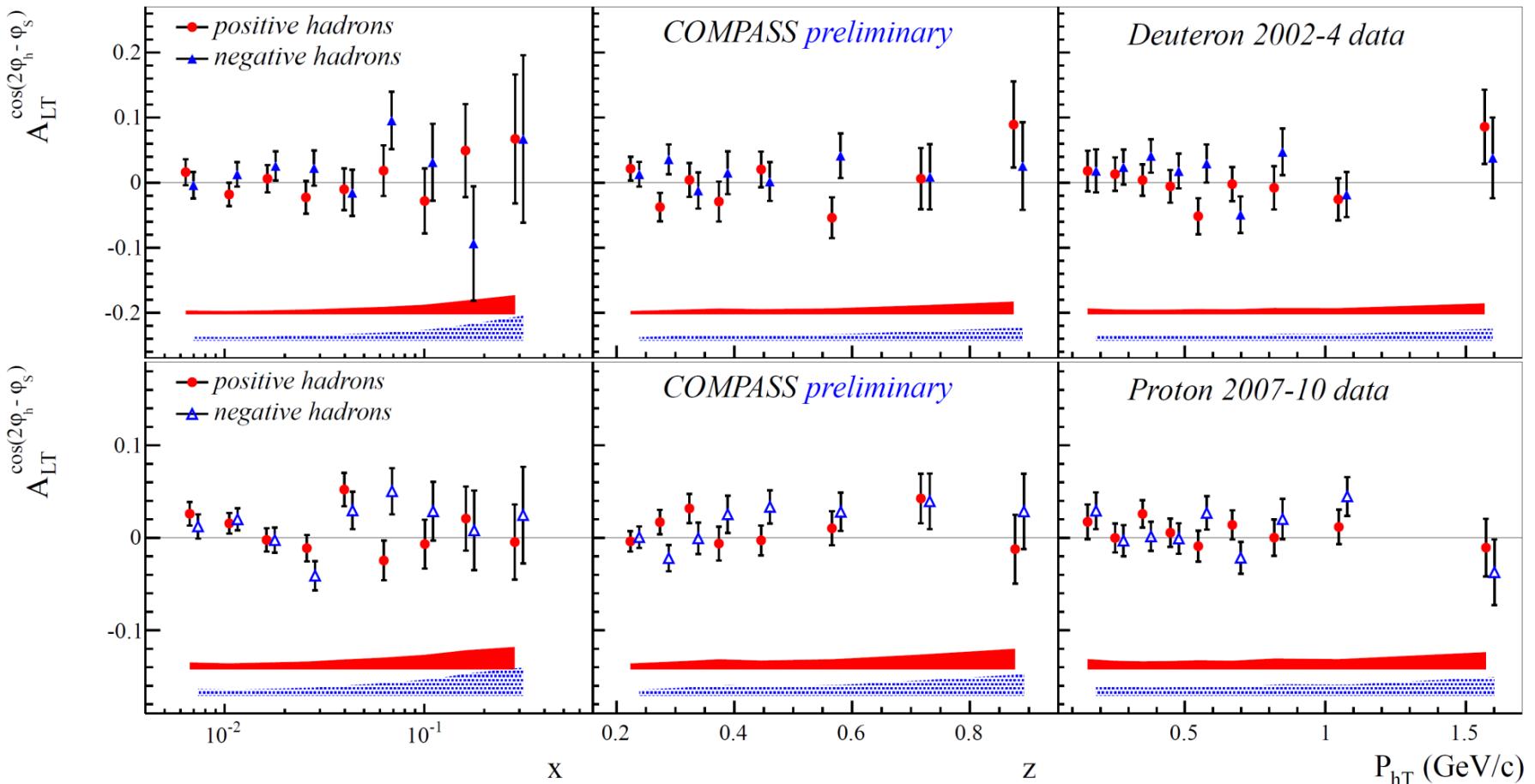
$$A_{UT}^{\sin(2\phi_h - \phi_s)} \propto \frac{M}{Q} \left(h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h \right) + \dots$$

"Pretzelosity" PDF $h_{1T}^{\perp q}$: 

"Sivers" PDF $f_{1T}^{\perp q}$: 

Asymmetries for both proton and deuteron are compatible with zero within uncertainties

Results for $A_{LT}^{\cos(2\phi_h - \phi_s)}$ deuteron & proton



$$A_{LT}^{\cos(2\phi_h - \phi_s)} \propto \frac{M}{Q} g_{1T}^q \otimes D_{1q}^h + \dots, \quad \text{"Worm Gear" PDF } g_{1T}^q : \begin{array}{c} \text{---} \\ \text{---} \end{array} \rightarrow \circlearrowleft \rightarrow \circlearrowright \rightarrow \circlearrowleft \text{---} \begin{array}{c} \text{---} \\ \text{---} \end{array}$$

Asymmetries for both proton and deuteron are compatible with zero within uncertainties

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SIDIS x-section: from lp to $\gamma * p$ ($P_L=0$)

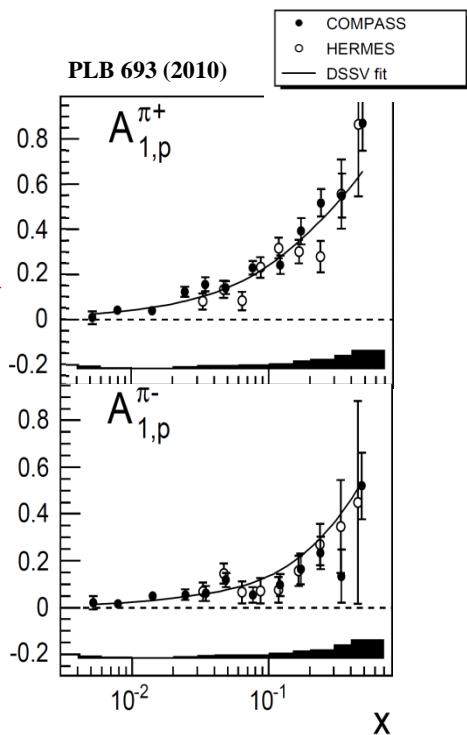
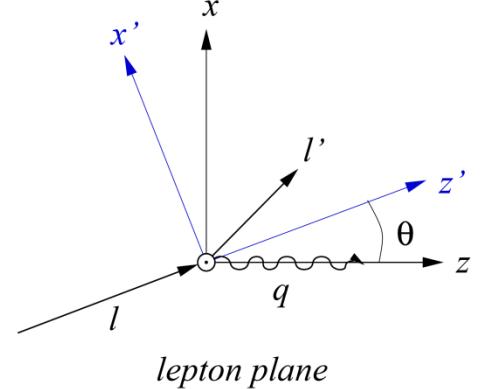
$$\frac{d\sigma}{dxdydzdP_{hT}^2d\varphi_h d\varphi_s} = \left[\frac{\cos\theta}{1 - \sin^2\theta \sin^2\varphi_s} \right] \times \left[\frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \times$$

$$\left[1 + \cos\varphi_h \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\varphi_h} + \cos(2\varphi_h) \times \varepsilon A_{UU}^{\cos(2\varphi_h)} + \lambda \sin\varphi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin\varphi_h} + \right.$$

$$\left. \begin{aligned} & \sin\varphi_s \times (\cos\theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\varphi_s}) + \\ & \sin(\varphi_h - \varphi_s) \times \left(\cos\theta A_{UT}^{\sin(\varphi_h - \varphi_s)} + \frac{1}{2} \sin\theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\varphi_h} \right) + \\ & \sin(\varphi_h + \varphi_s) \times \left(\cos\theta \varepsilon A_{UT}^{\sin(\varphi_h + \varphi_s)} + \frac{1}{2} \sin\theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\varphi_h} \right) + \\ & \sin(2\varphi_h - \varphi_s) \times \left(\cos\theta \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\varphi_h - \varphi_s)} + \frac{1}{2} \sin\theta \varepsilon A_{UL}^{\sin 2\varphi_h} \right) + \\ & \sin(2\varphi_h + \varphi_s) \times \left(\frac{1}{2} \sin\theta \varepsilon A_{UL}^{\sin 2\varphi_h} \right) + \\ & \sin(3\varphi_h - \varphi_s) \times (\cos\theta \varepsilon A_{UT}^{\sin(3\varphi_h - \varphi_s)}) \end{aligned} \right] +$$

$$\boxed{\left. \begin{aligned} & \cos\varphi_s \times (\cos\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\varphi_s} + \sin\theta \sqrt{(1-\varepsilon^2)} A_{LL}) + \\ & \cos(\varphi_h - \varphi_s) \times \left(\cos\theta \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\varphi_h - \varphi_s)} + \frac{1}{2} \sin\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\varphi_h} \right) + \\ & \cos(\varphi_h + \varphi_s) \times \left(\frac{1}{2} \sin\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\varphi_h} \right) + \\ & \cos(2\varphi_h - \varphi_s) \times (\cos\theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\varphi_h - \varphi_s)}) \end{aligned} \right]$$

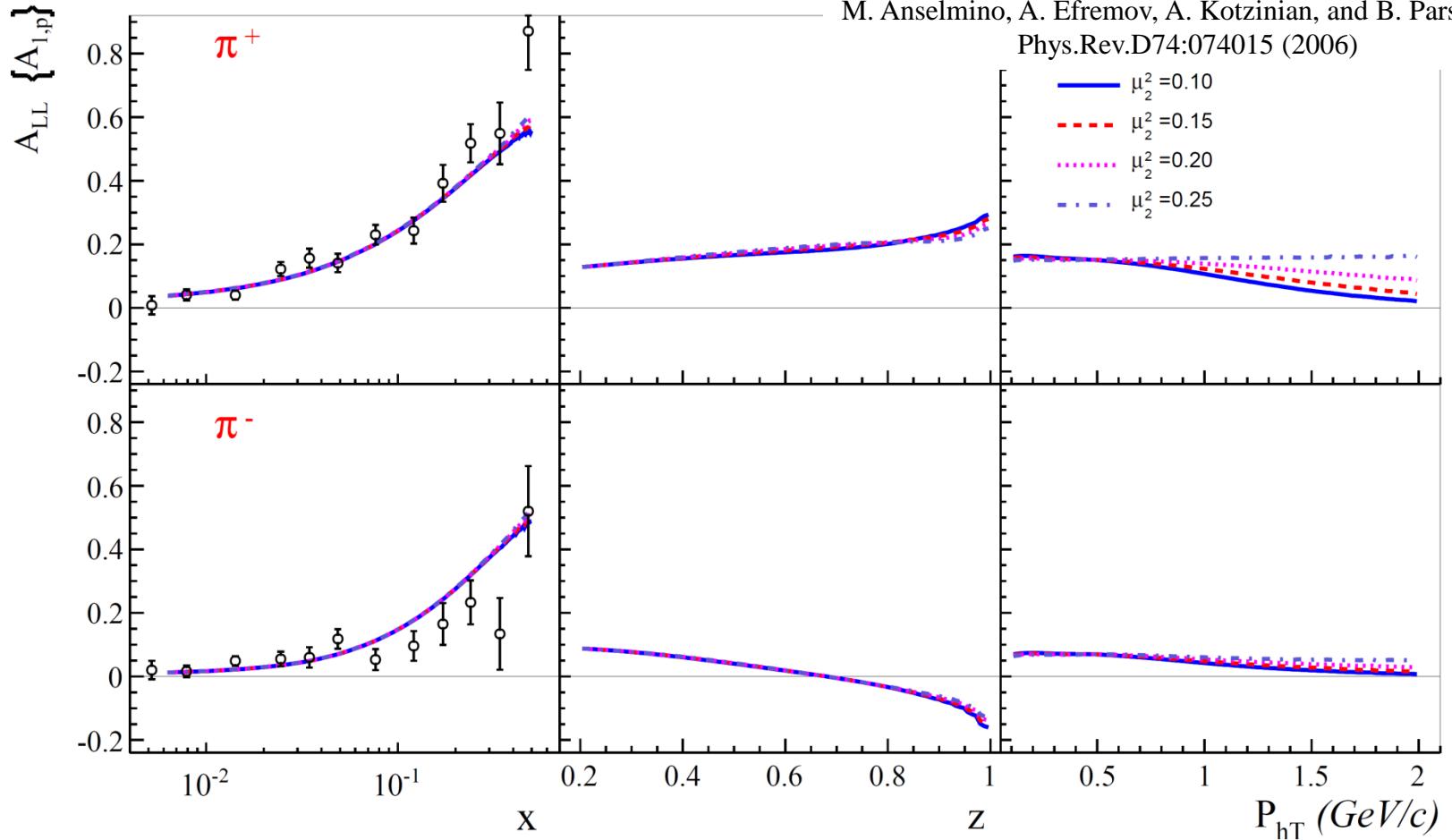
$$\frac{P_T}{\sqrt{1 - \sin^2\theta \sin^2\varphi_s}} \quad \frac{P_\lambda}{\sqrt{1 - \sin^2\theta \sin^2\varphi_s}}$$



A_{LL} evaluated according to the PRD 74, 074015 (2006)

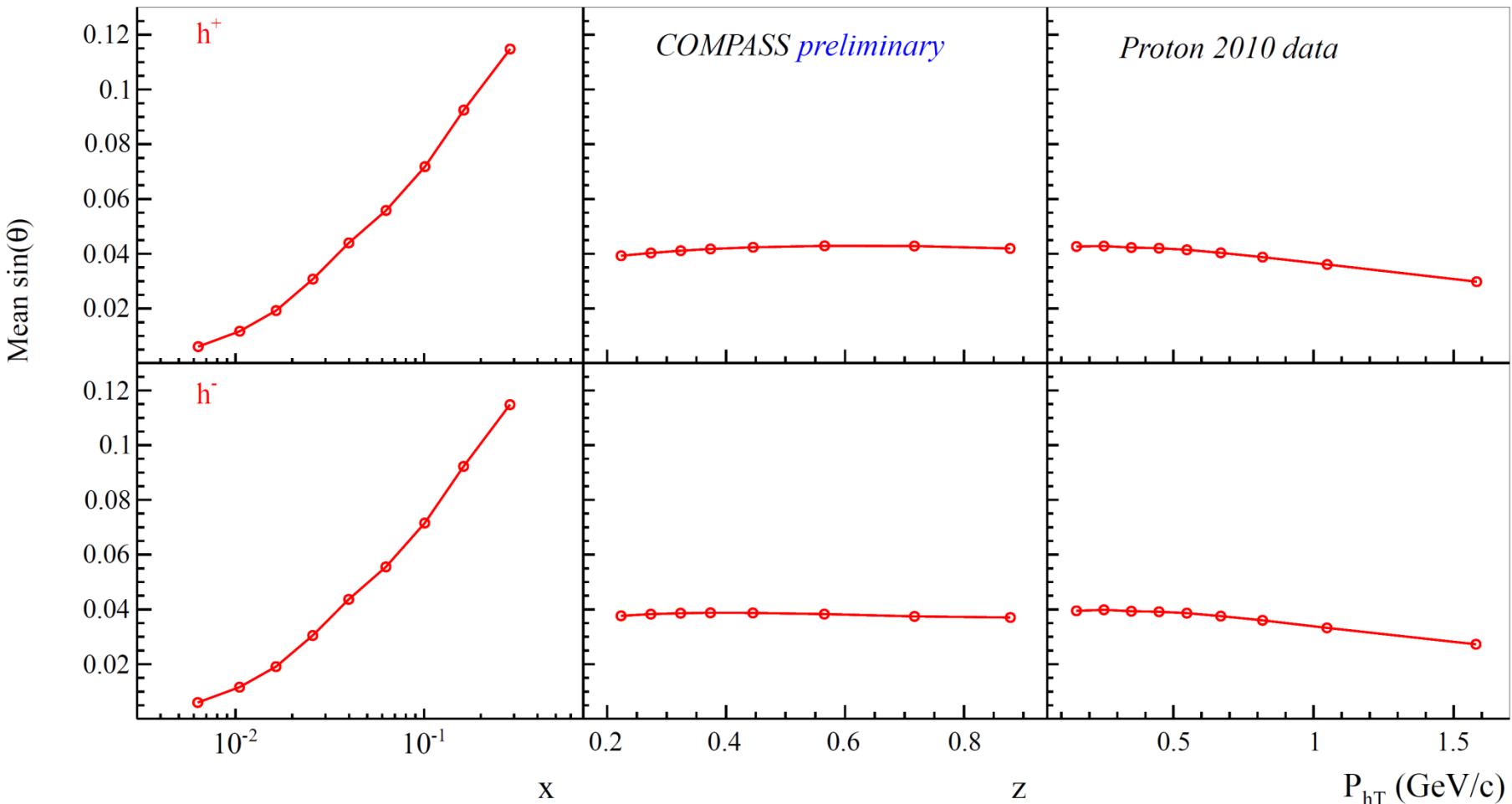
COMPASS Proton 2007 (PLB 693(2010))

M. Anselmino, A. Efremov, A. Kotzinian, and B. Parsamyan
Phys.Rev.D74:074015 (2006)



Asymmetry is evaluated in COMPASS specific mean kinematic points extracted from the data. Good level of agreement up to $x \approx 0.3$, which allows us to use the predicted z and P_{hT} – dependencies in $A_{LT}^{\cos(\varphi_S)}$ -correction.

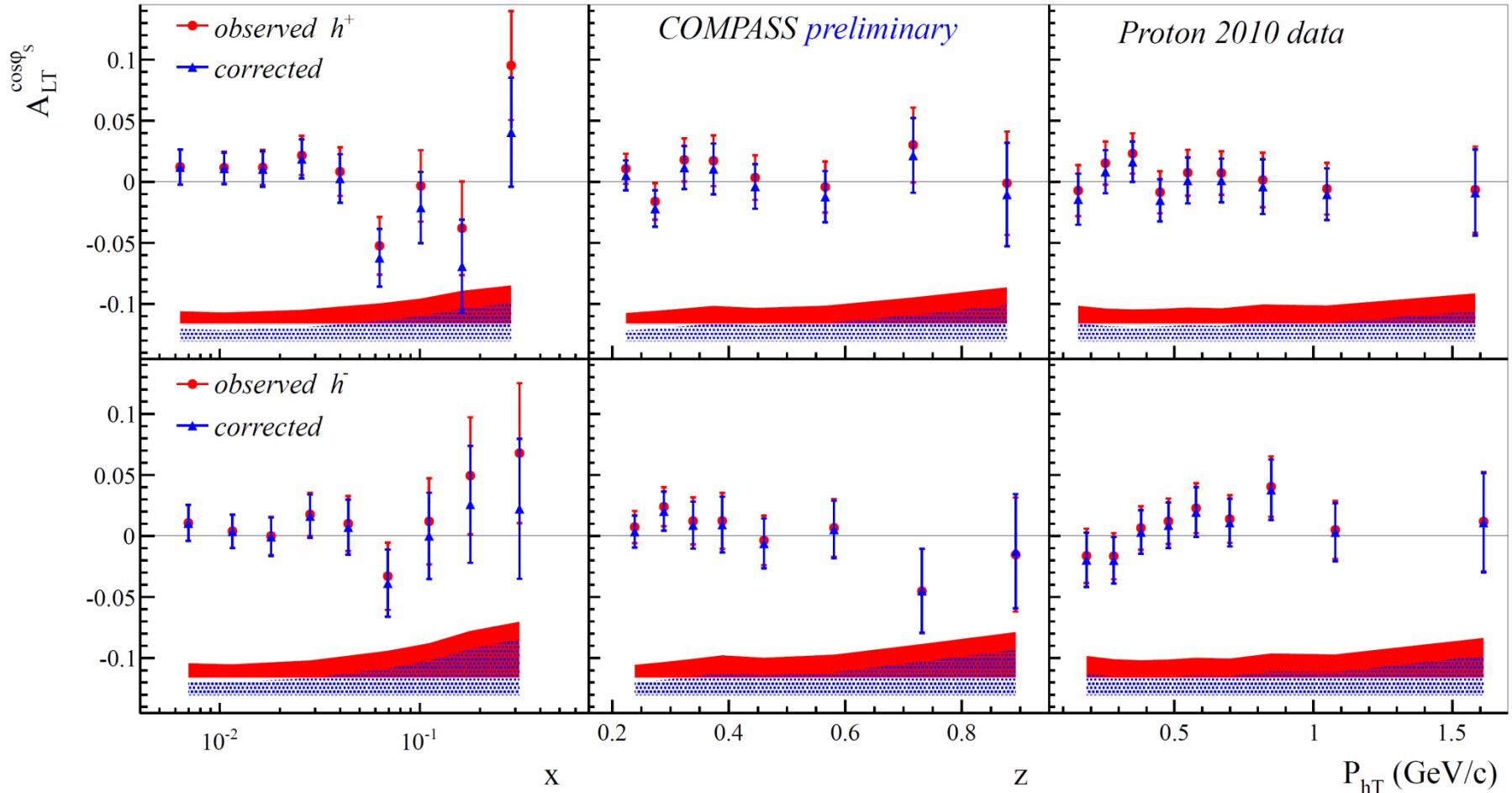
Mean $\sin\theta$ -values



The $\sin\theta$ is small at COMPASS kinematics. The maximum reached value is ~ 0.12 and the mean is around 0.04 ($\cos\theta \approx 1$).

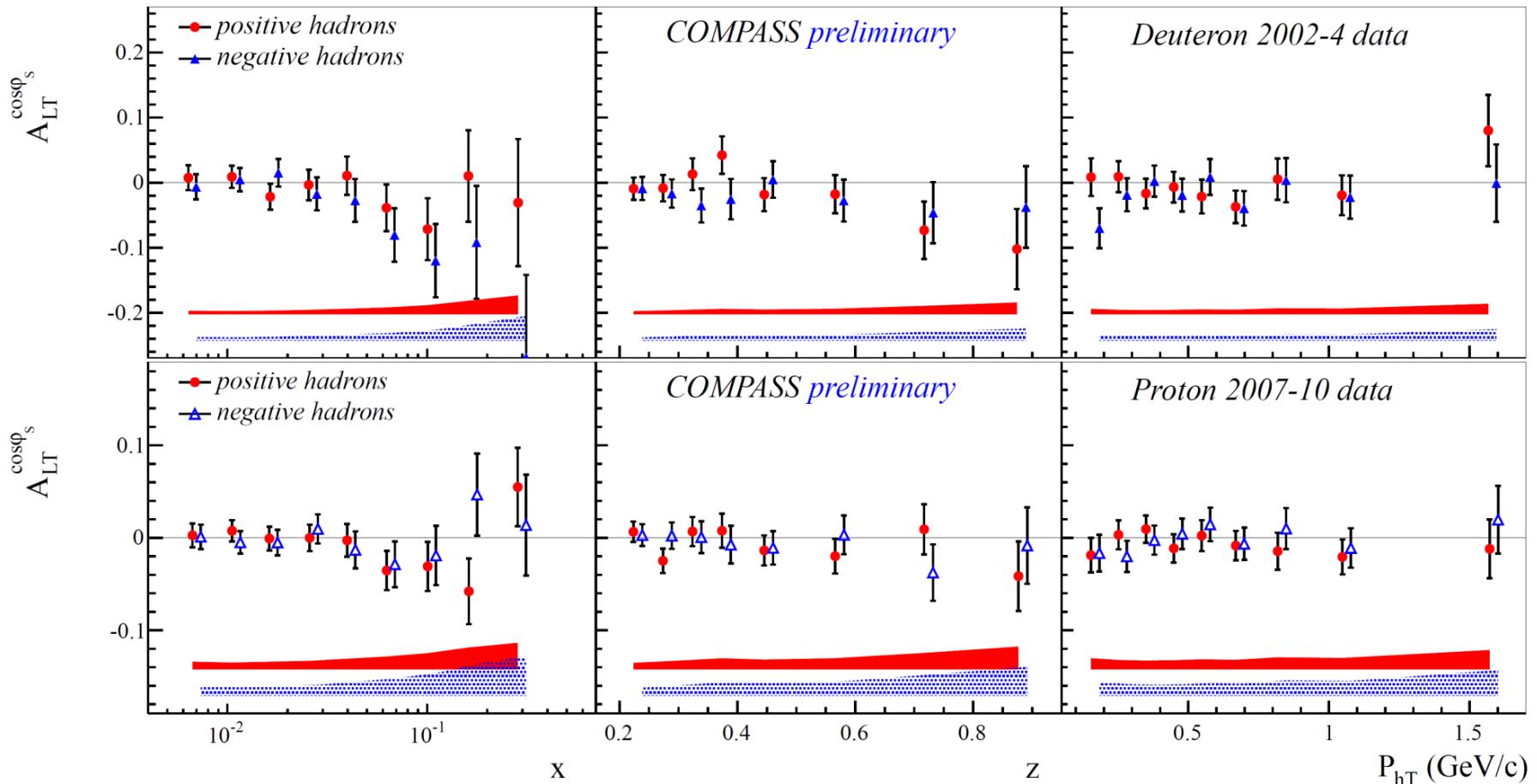
Corrected $A_{LT}^{\cos\varphi_s}$

$$A_{LT}^{\cos\varphi_s'} \approx \left(\cos \theta A_{LT}^{\cos\varphi_s} - \sin \theta \frac{\sqrt{(1-\varepsilon^2)}}{\sqrt{2\varepsilon(1-\varepsilon)}} A_{LL} \right)$$



As expected, at large x the corrections become sizable.

Results for $A_{LT}^{\cos\phi_s}$ deuteron & proton



$$A_{LT}^{\cos\phi_s} \propto \frac{M}{Q} g_{1T}^q \otimes D_{1q}^h + \dots, \quad \text{"Worm Gear" PDF } g_{1T}^q : \begin{array}{c} \text{---} \\ \text{---} \end{array} \rightarrow \circlearrowleft \rightarrow \circlearrowright \rightarrow \circlearrowleft \rightarrow \text{---} \text{---}$$

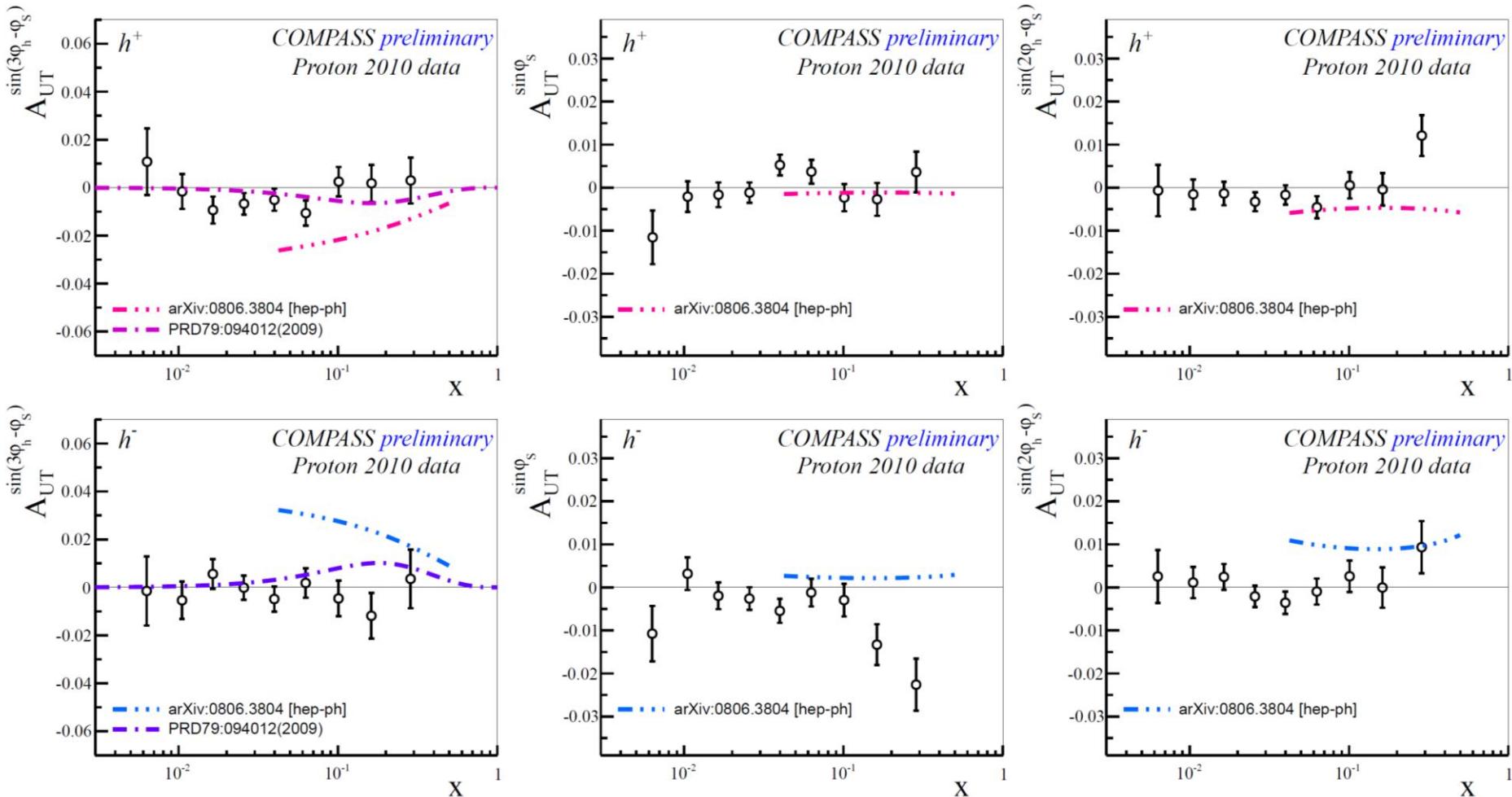
Asymmetries for both proton and deuteron are compatible with zero within uncertainties

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“UT” asymmetries and theoretical predictions x-dependence only

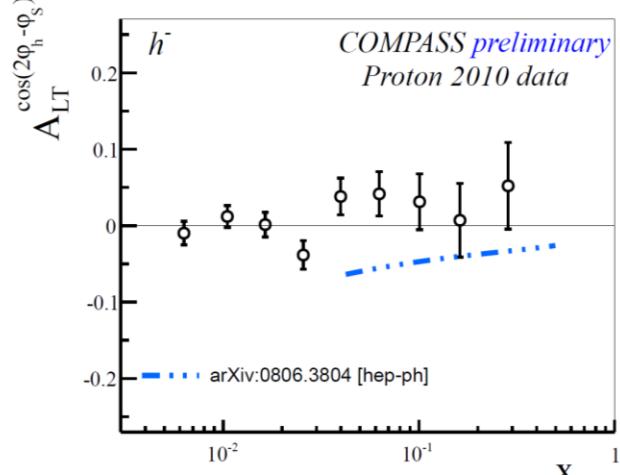
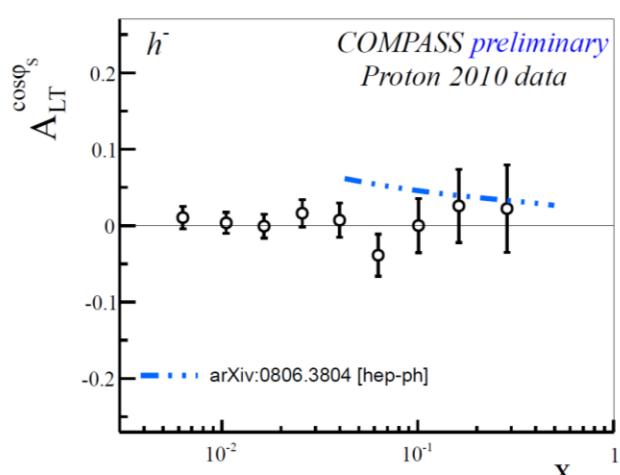
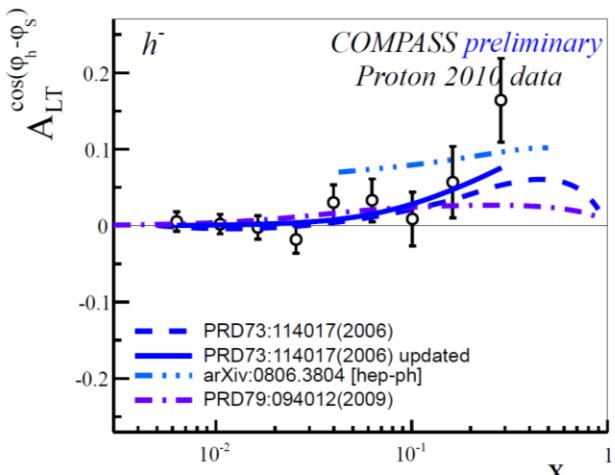
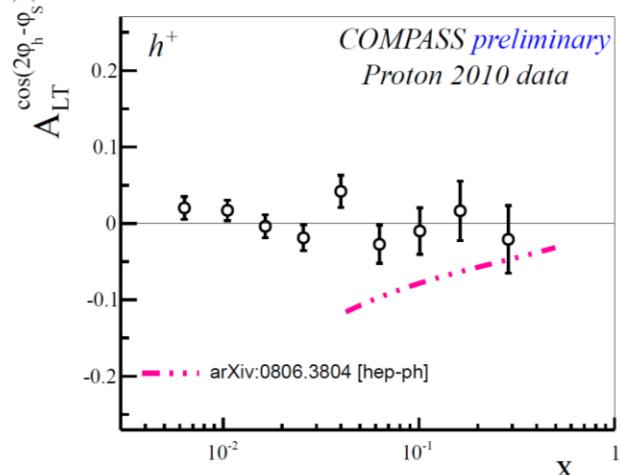
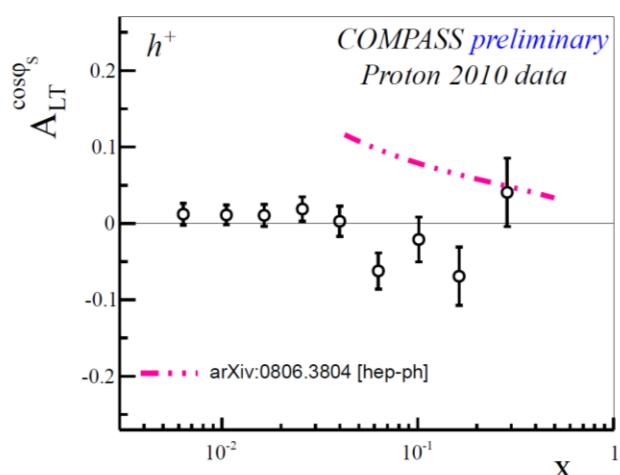
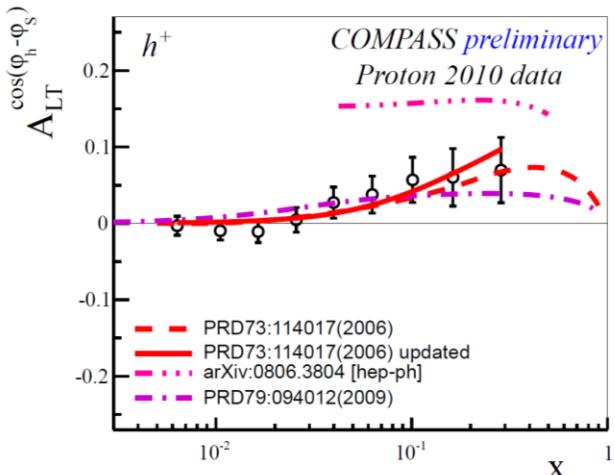
S. Boffi, A.V. Efremov, B. Pasquini and P. Schweitzer PRD79:094012(2009)
 A. Kotzinian arXiv:0806.3804[hep-ph]



“LT” asymmetries and theoretical predictions

x-dependence only

A. Kotzinian, B. Parsamyan, A. Prokudin Phys.Rev.D73:114017 (2006)
 S. Boffi, A.V. Efremov, B. Pasquini and P. Schweitzer PRD79:094012(2009)
 A. Kotzinian arXiv:0806.3804[hep-ph]



The predictions for $A_{LT}^{cos(\phi_h-\phi_s)}$ shows a good level of agreement with the experimentally extracted asymmetry.

Outline

- Introduction
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Summary

- Six “beyond Collins and Sivers” transverse spin asymmetries

$$A_{UT}^{\sin(3\phi_h - \phi_s)}, A_{UT}^{\sin\phi_s}, A_{UT}^{\sin(3\phi_h - \phi_s)}, A_{LT}^{\cos(\phi_h - \phi_s)}, A_{LT}^{\cos\phi_s} \& A_{LT}^{\cos(2\phi_h - \phi_s)}$$

have been extracted from COMPASS deuteron 2002-2004, proton 2007 and now also proton 2010 data.

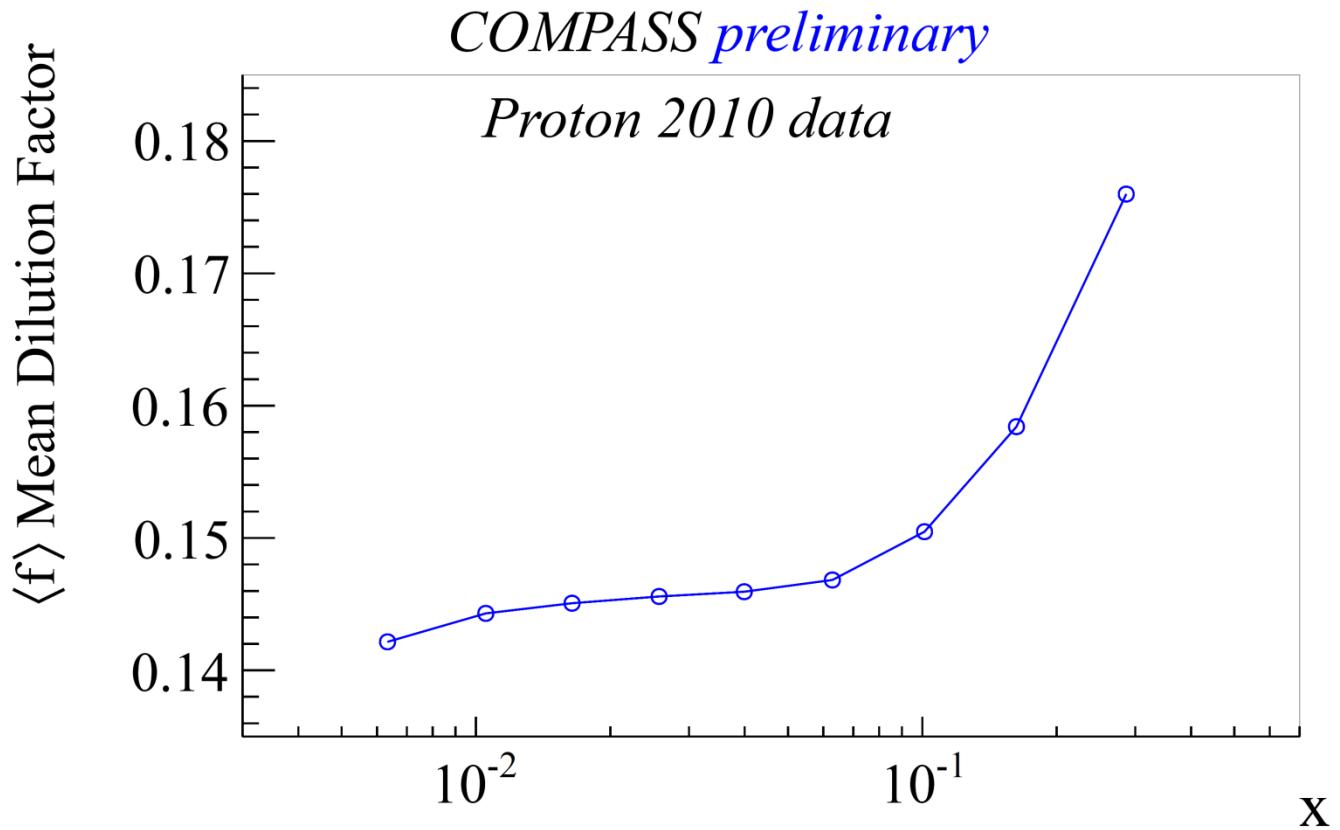
- “Deuteron” and “proton 2007” asymmetries found to be consistent with zero within the statistical accuracy of the measurement.
- Higher statistics and improved quality of the 2010 proton data allowed to reveal a non-zero trend for the $A_{LT}^{\cos(\phi_h - \phi_s)}$ and $A_{UT}^{\sin\phi_s}$ amplitudes.
- Observed effects confirm HERMES preliminary results.
- COMPASS results for the $A_{LT}^{\cos(\phi_h - \phi_s)}$ showed a good level of agreement with the theoretical predictions.
- Next → Six asymmetries for pions and kaons.

Thank you!



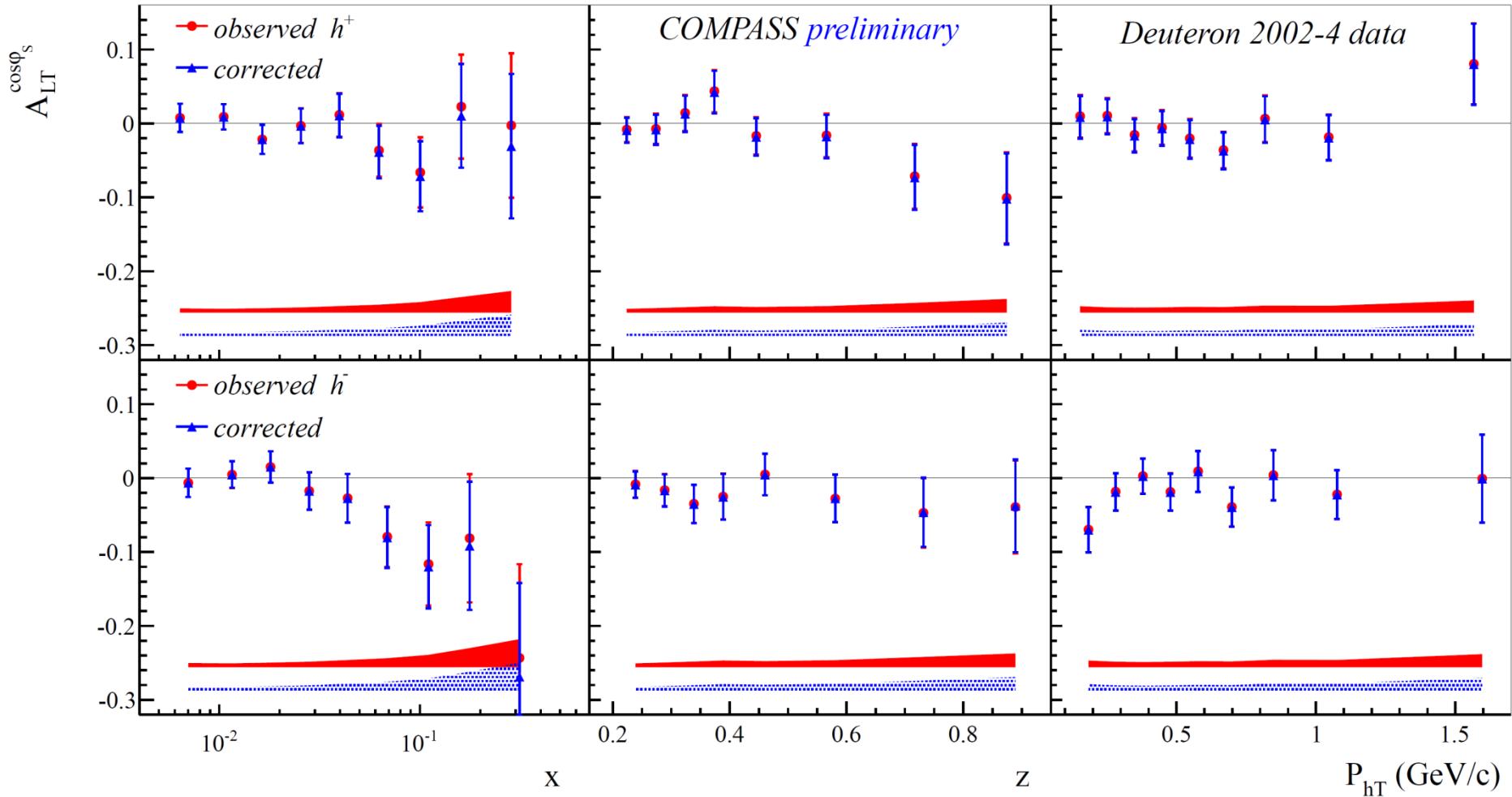
Spare slides

Dilution factor



Corrected $A_{LT}^{\cos\varphi_s}$ deuteron

$$A_{LT}^{\cos\varphi_s'} \approx \left(\cos \theta A_{LT}^{\cos\varphi_s} - \sin \theta \frac{\sqrt{(1-\varepsilon^2)}}{\sqrt{2\varepsilon(1-\varepsilon)}} A_{LL} \right)$$



$A_{LT}^{\cos(\phi_h - \phi_s)}$ asymmetry PRD73:114017,(2006)

There exists a relation between first momentum of g_{1T} and g_2 (follows from Lorentz invariance, Tangerman & Mulders) :

$$g_{1T}^{q(1)}(x) \equiv \int_0^x g_2^q(y) dy = - \int_x^1 g_2^q(y) dy = (WW - appr) = x \int_x^1 \frac{g_1^q(y)}{y} dy$$

$$f_1^q(x, k_T^2) = f_1^q(x) \frac{1}{\pi \mu_0^2} \exp\left(-\frac{k_T^2}{\mu_0^2}\right),$$

$$D_q^h(z, P_{hT}^2) = D_q^h(z) \frac{1}{\pi \mu_D^2} \exp\left(-\frac{P_{hT}^2}{\mu_D^2}\right),$$

$$g_{1T}^q(x, k_T^2) = g_{1T}^{q(1)}(x) N \exp\left(-\frac{k_T^2}{\mu_1^2}\right)$$

N is fixed by

$$g_{1T}^{q(1)}(x) = \int d^2 k_T \frac{k_T^2}{2M^2} g_{1T}^q(x, k_T^2)$$

$$g_{1T}^q(x, k_T^2) = g_{1T}^{q(1)}(x) \frac{2M^2}{\pi \mu_1^4} \exp\left(-\frac{k_T^2}{\mu_1^2}\right)$$

From analysis of unpolarized P_{hT} dependence and Cahn effect

$$\mu_0^2 = 0.25(GeV/c)^2, \quad \mu_D^2 = 0.2(GeV/c)^2$$

Naïve positivity constraint: $\frac{|k_T|}{M} |g_{1T}^q(x, k_T^2)| < f_1^q(x, k_T^2)$

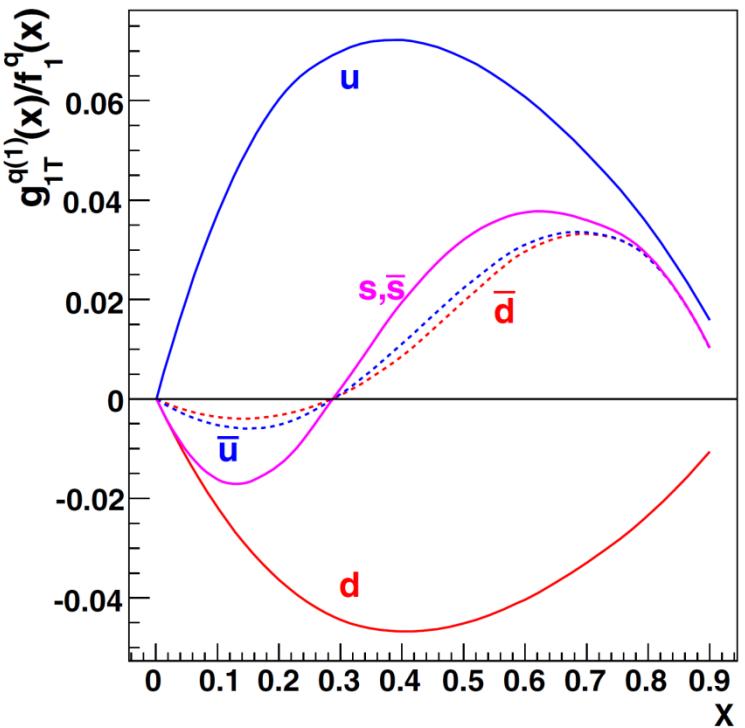
holds if $\mu_1^2 \leq 0.246 \text{ (GeV/c)}^2$

Predictions done for: $\mu_1^2 = 0.1, 0.15 \text{ and } 0.25(GeV/c)^2$

$$A_{LT}^{\cos \phi_h^S}(x, y, z, P_{hT}) = 2 \frac{\int_0^{2\pi} d\phi_h^S (d\sigma^{\rightarrow \uparrow} - d\sigma^{\rightarrow \downarrow}) \cos \phi_h^S}{\int_0^{2\pi} d\phi_h^S (d\sigma^{\rightarrow \uparrow} + d\sigma^{\rightarrow \downarrow})} = 2 \frac{\frac{2-y}{xy} \frac{Mz |P_{hT}|}{(\mu_D^2 + \mu_1^2 z^2)^2} \exp\left(-\frac{P_{hT}^2}{\mu_D^2 + \mu_1^2 z^2}\right) \sum_q e_q^2 g_{1T}^{q(1)}(x) D_q^h(z)}{\frac{1+(1-y)^2}{xy^2} \frac{1}{\mu_D^2 + \mu_0^2 z^2} \exp\left(-\frac{P_{hT}^2}{\mu_D^2 + \mu_0^2 z^2}\right) \sum_q e_q^2 f_1^q(x) D_q^h(z)}$$

$A_{LT} \cos(\varphi_h - \varphi_s)$ asymmetry *PRD73:114017,(2006)*

$$A_{TMD} = \frac{\text{Low } x, y, z \text{ & } p_T + \text{High } x, y, z \text{ & } p_T}{\text{Low } x, y, z \text{ & } p_T + \text{High } x, y, z \text{ & } p_T}$$



GRV98+GRSV2000 LO, std DFs Kretzer FFs

COMPASS - $Q^2 > 1.0 \text{ (GeV/c)}^2$, $W^2 > 25 \text{ GeV}^2$, $0.05 < x_{Bj} < 0.6$, $0.5 < y < 0.9$, $0.4 < z < 0.9$, $|P_{h,T}| > 0.5 \text{ GeV}/c$

HERMES - $Q^2 > 1.0 \text{ (GeV/c)}^2$, $W^2 > 10 \text{ GeV}^2$, $0.1 < x_{Bj} < 0.6$, $0.45 < y < 0.85$, $0.4 < z < 0.9$, $|P_{h,T}| > 0.5 \text{ GeV}/c$

JLab - $Q^2 > 1.0 \text{ (GeV/c)}^2$, $W^2 > 4 \text{ GeV}^2$, $0.2 < x_{Bj} < 0.6$, $0.4 < y < 0.7$, $0.4 < z < 0.7$, $|P_{h,T}| > 0.5 \text{ GeV}/c$