

# Latest results on longitudinal spin physics at COMPASS

CIPANP2012 – St. Petersburg, Florida



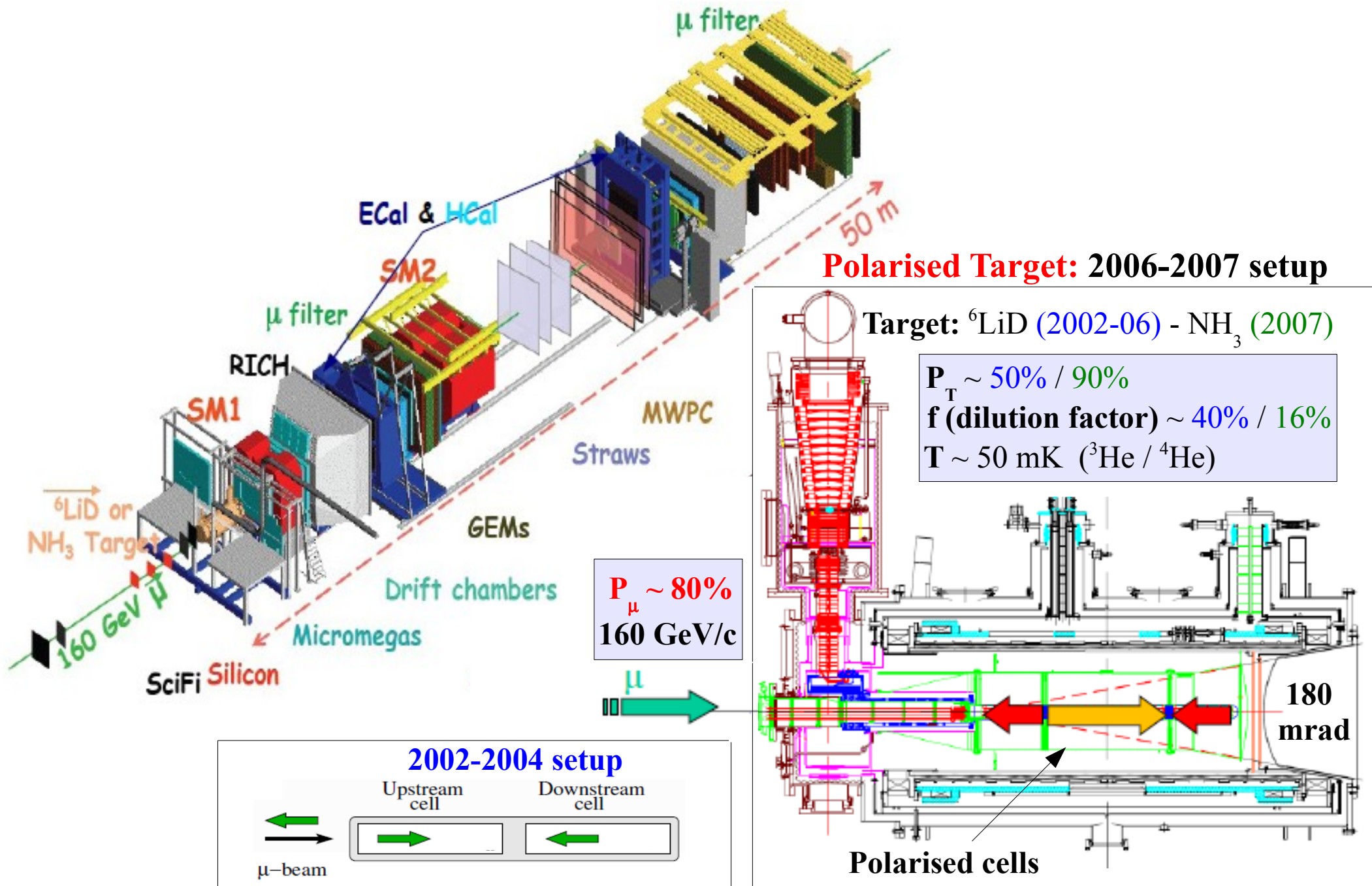
**Celso Franco** (*LIP – Lisboa*)  
*on behalf of the COMPASS collaboration*

# Outline

## Results from longitudinally polarised nucleons:

- $A_1^{d/p}$ ,  $g_1^{d/p}$ , and first moments of  $g_1^d$
- Semi-inclusive asymmetries and flavour separation
- Hadron multiplicities
- Gluon polarisation at LO in QCD:
  - Open Charm
  - High- $p_T$  hadron pairs
- Gluon polarisation at NLO in QCD:
  - Open Charm

# The spectrometer and polarised target



# **Inclusive asymmetries and spin structure functions**

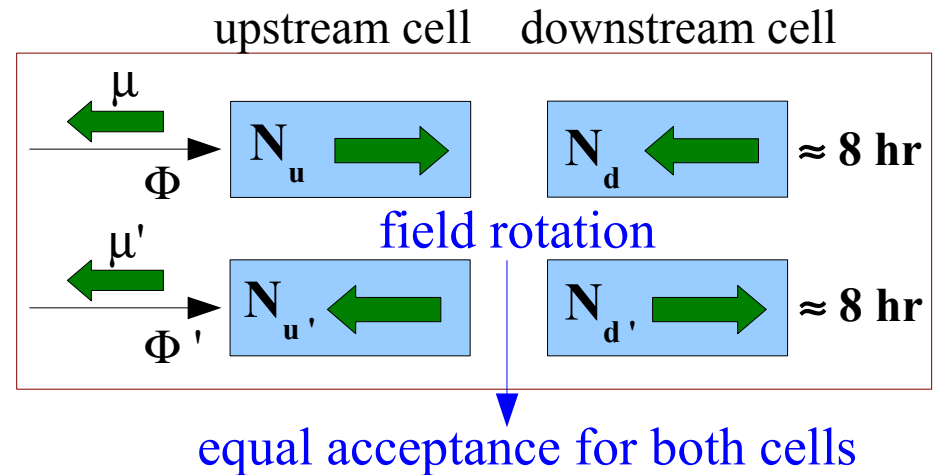
**Asymmetry measurement:**  $A_1^N := \frac{\Delta \sigma_{y^*N}}{\sigma_{y^*N}} = \frac{(\sigma_{y^*N}^{\rightarrow} - \sigma_{y^*N}^{\leftarrow})}{\sigma_{y^*N}^{\text{unpol}}}$

- The number of reconstructed events inside each spin configuration of the target,  $N_t$  ( $t = u, d, u', d'$ ), can be used to extract the  $A_1^d / A_1^p$  asymmetries:

$$A^{\text{exp}} = \frac{1}{2} \left( \frac{N_u - N_d}{N_u + N_d} + \frac{N_{d'} - N_{u'}}{N_{d'} + N_{u'}} \right)$$

$$= f \cdot P_\mu \cdot P_T \cdot (D \cdot A_1) \rightarrow A^{\mu N}$$

$D = \text{Depolarisation factor}$



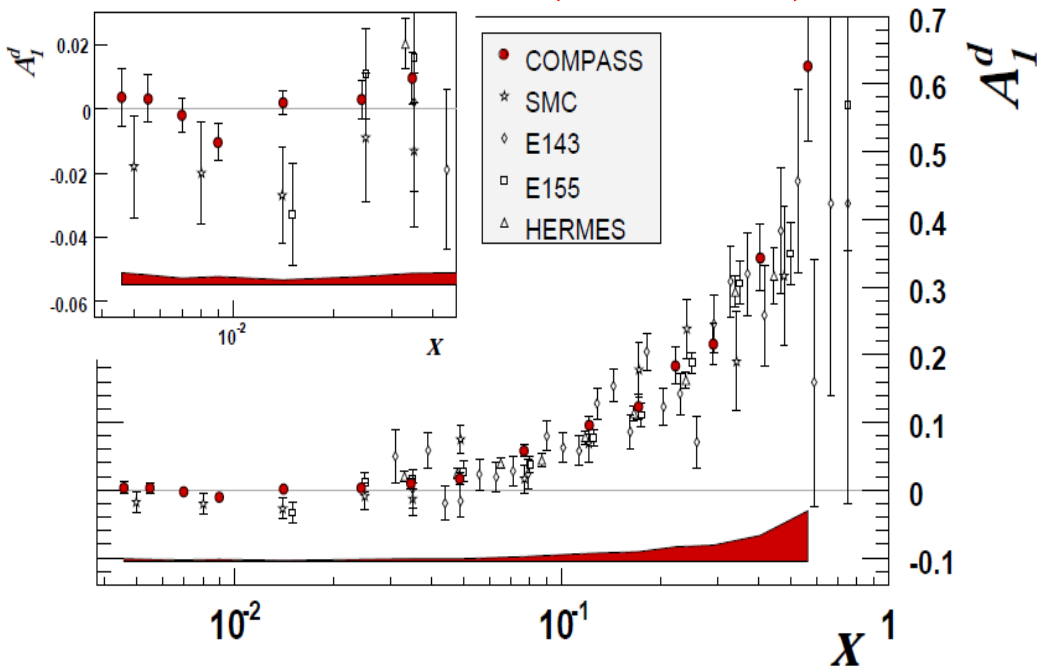
- Weighting each event with  $\omega = (fP_\mu D)$ :

$$A_1 = \frac{1}{2P_T} \left( \frac{\sum_{i=0}^{N_u} \omega_i - \sum_{i=0}^{N_d} \omega_i}{\sum_{i=0}^{N_u} \omega_i^2 + \sum_{i=0}^{N_d} \omega_i^2} + \frac{\sum_{i=0}^{N_{u'}} \omega_i - \sum_{i=0}^{N_{d'}} \omega_i}{\sum_{i=0}^{N_{u'}} \omega_i^2 + \sum_{i=0}^{N_{d'}} \omega_i^2} \right)$$

statistical gain:  $\frac{\left\langle \sum_{i=0}^{N_{\text{tot}}} \omega_i^2 \right\rangle}{\left\langle \sum_{i=0}^{N_{\text{tot}}} \omega_i \right\rangle^2}$

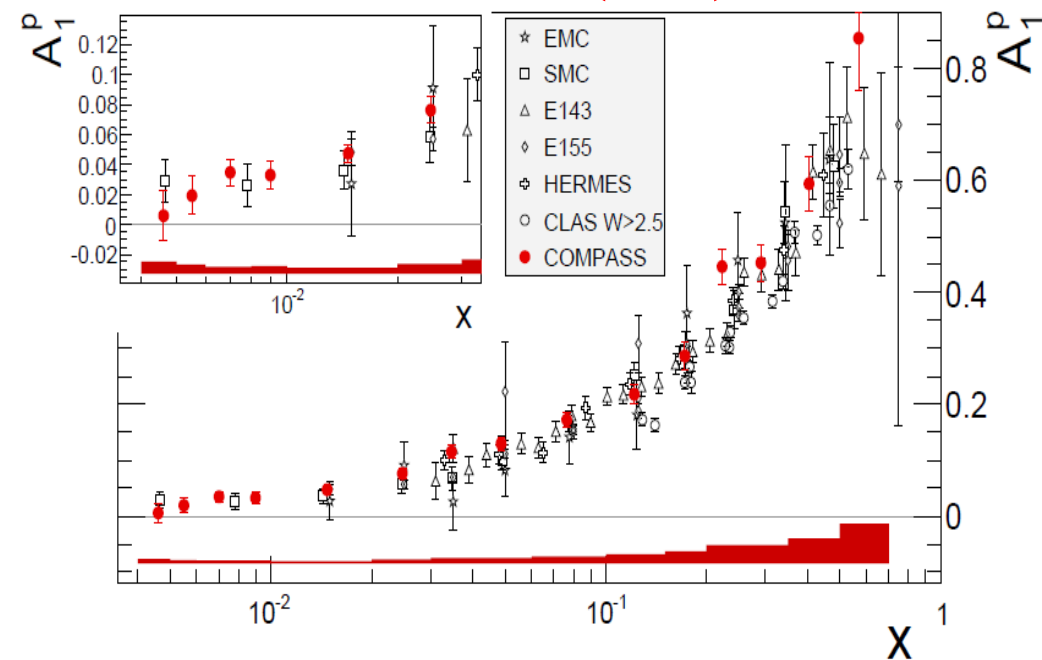
# Inclusive asymmetries $A_1^{d/p}$ : $Q^2 > 1$ (GeV/c)<sup>2</sup>

## Deuteron data (2002-2006)



COMPASS, PLB 647 (2007) 330-340

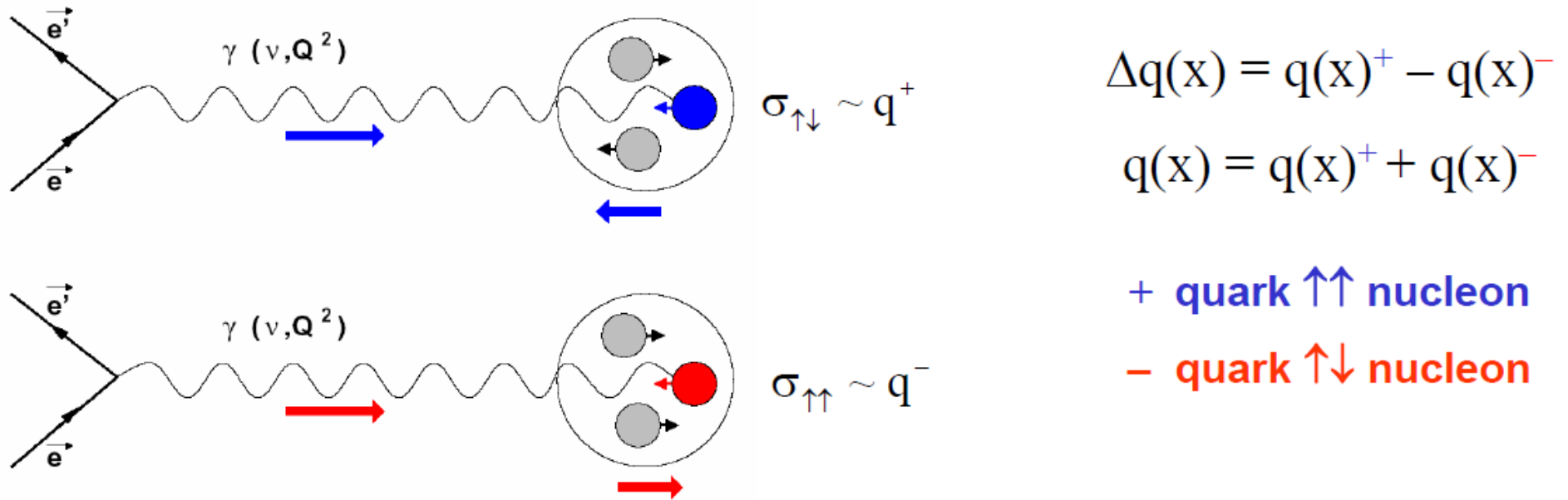
## Proton data (2007)



COMPASS, PLB 690 (2010) 466-472

- Good agreement between all experimental points
- Significant improvement of precision in the low  $x$  region:  $A_1^d$  compatible with zero for  $x < 0.01$
- No negative trend for  $A_1^d$

# Interpretation of $A_1$ in terms of structure functions

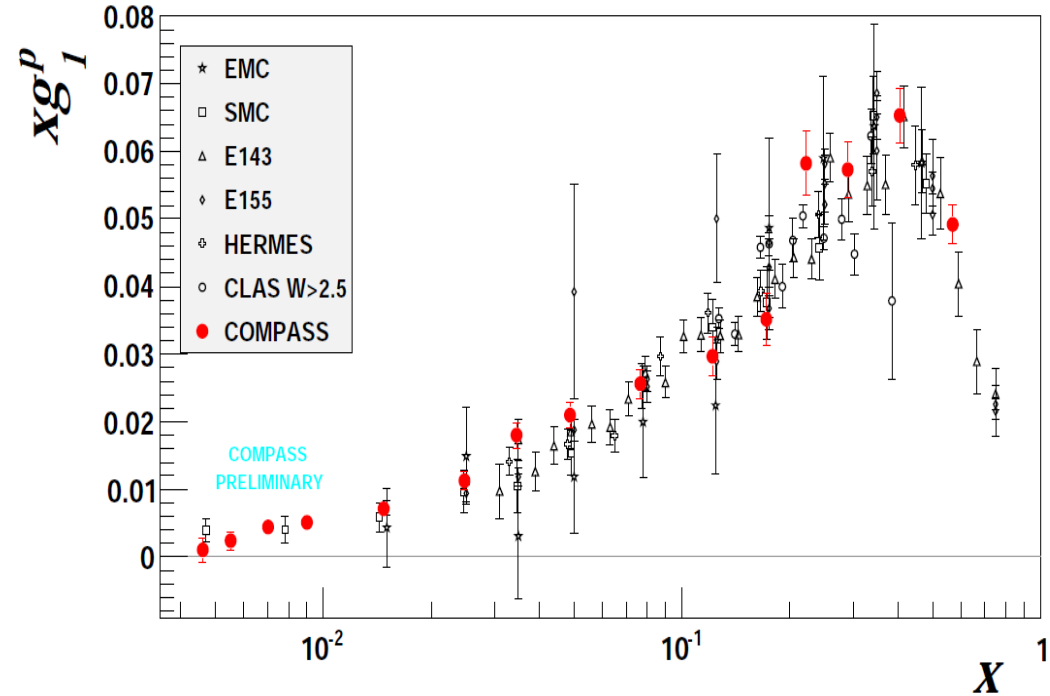
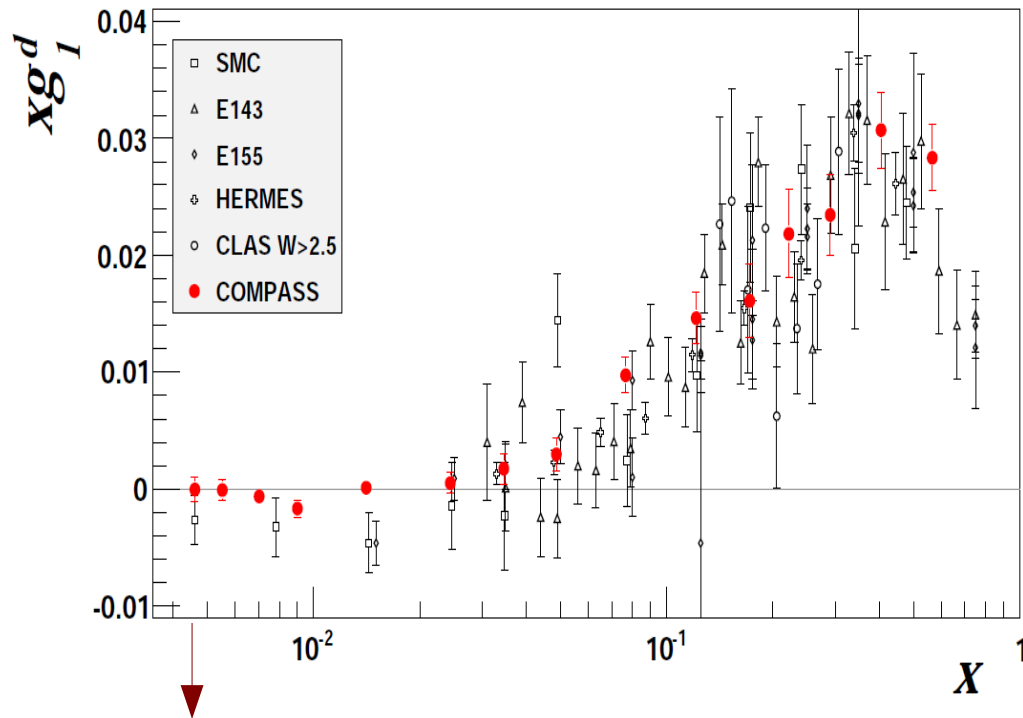


$$A_1(x, Q^2) = \frac{\sigma_{\uparrow\downarrow} - \sigma_{\uparrow\uparrow}}{\sigma_{\uparrow\downarrow} + \sigma_{\uparrow\uparrow}} \approx \frac{\sum_q e_q^2 \Delta q(x, Q^2)}{\sum_q e_q^2 q(x, Q^2)} = \frac{g_1(x, Q^2)}{F_1(x, Q^2)} = \frac{g_1(x, Q^2) 2x(1+R)}{F_2(x, Q^2)}$$

- $g_1$  (polarised structure function) is obtained from the asymmetry  $A_1$  using:

$F_2 \rightarrow$  SMC parameterisation      and       $R = \sigma^L/\sigma^T \rightarrow$  SLAC parameterisation

# COMPASS results for $g_1^{d/p}$ and first moments of $g_1^d$



$$\Gamma_1^N(Q_0^2=3(\text{GeV}/c)^2) = \int_0^1 g_1(x) dx = 0.0502 \pm 0.0028(\text{stat}) \pm 0.0020(\text{evol}) \pm 0.0051(\text{syst})$$

$$= \frac{1}{9} \left( 1 - \frac{\alpha_s(Q^2)}{\pi} + \mathcal{O}(\alpha_s^2) \right) \left( \mathbf{a}_0(Q^2) + \frac{1}{4} \mathbf{a}_8 \right) \Rightarrow \mathbf{a}_0 = 0.35 \pm 0.03(\text{stat}) \pm 0.05(\text{syst})$$

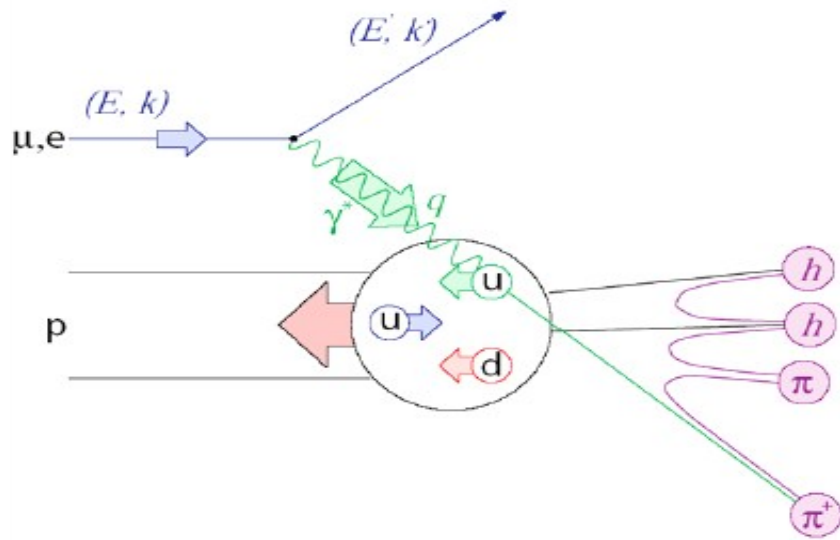
$$\Delta \Sigma^{\overline{\text{MS}}} = 0.33 \pm 0.03(\text{stat}) \pm 0.05(\text{syst}) \quad (\Delta \Sigma^{\overline{\text{MS}}} = \mathbf{a}_0 \text{ @ } Q^2 \rightarrow \infty)$$

$$(\Delta \mathbf{s} + \Delta \bar{\mathbf{s}}) = \frac{1}{3} (\Delta \Sigma^{\overline{\text{MS}}} - \mathbf{a}_8) = -0.08 \pm 0.01(\text{stat}) \pm 0.02(\text{syst})$$



# **Semi-inclusive asymmetries and flavour separation**

# Extraction of the quark helicity distributions from SIDIS



- The outgoing hadron tags the quark flavour
- Required: fragmentation function of a quark  $q$  to a hadron  $h$ :  $D_q^h(z, Q^2)$

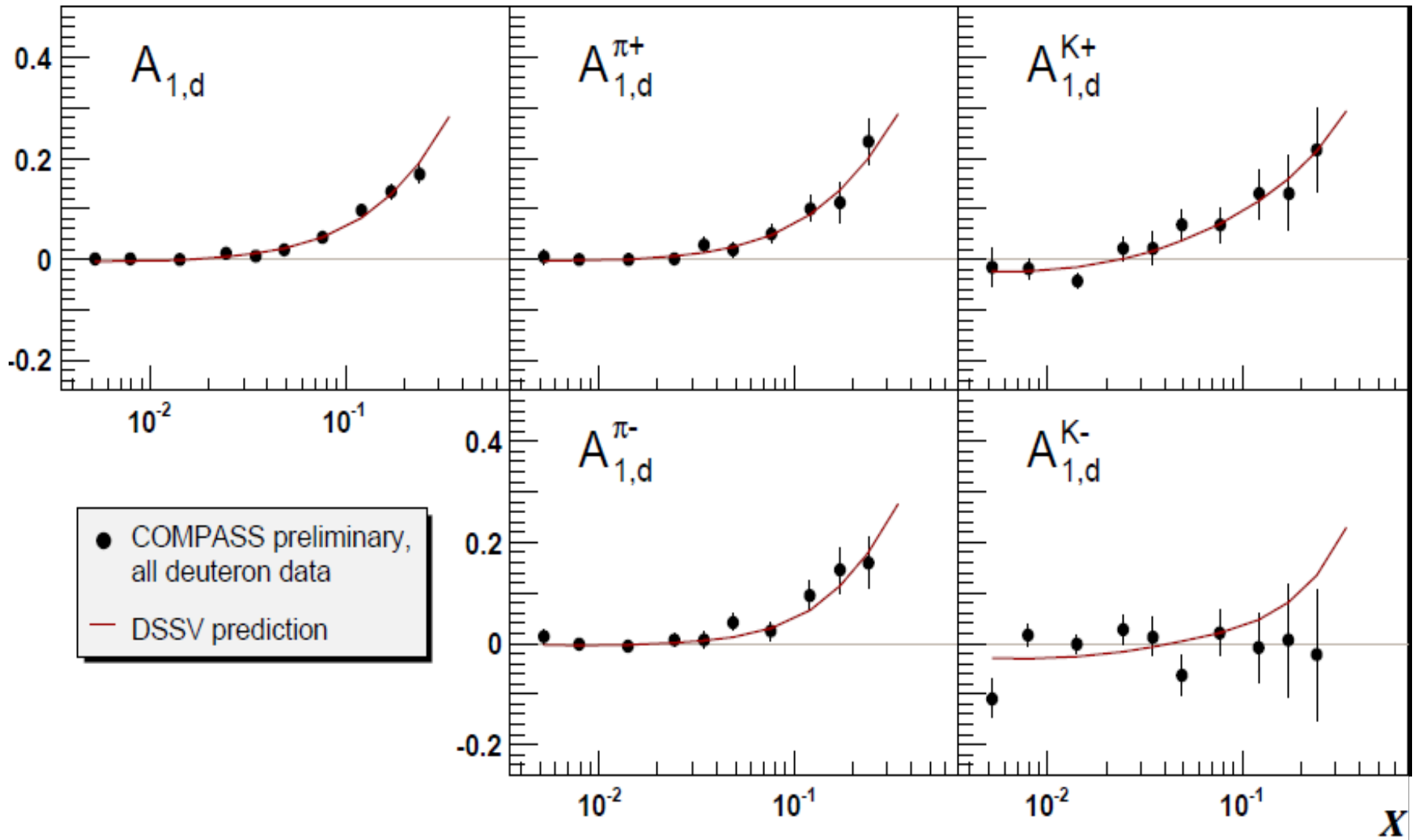
$$z = E_h / (E_\mu - E'_\mu)$$

- **The semi-inclusive asymmetries have the following interpretation (at LO):**

$$A_1^{h(p/d)}(x, z, Q^2) \approx \frac{\sum_q e_q^2 \Delta q(x, Q^2) D_q^h(z, Q^2)}{\sum_q e_q^2 q(x, Q^2) D_q^h(z, Q^2)}$$

- **Inputs needed for the extraction of  $\Delta q(x, Q^2)$ :**
  - Unpolarised PDFs ( $q(x, Q^2)$ )  $\rightarrow$  [MRST04](#)
  - $D_q^h(z, Q^2) \rightarrow$  [DSS parameterisation](#)

# Inclusive and semi-inclusive spin asymmetries: Deuteron data

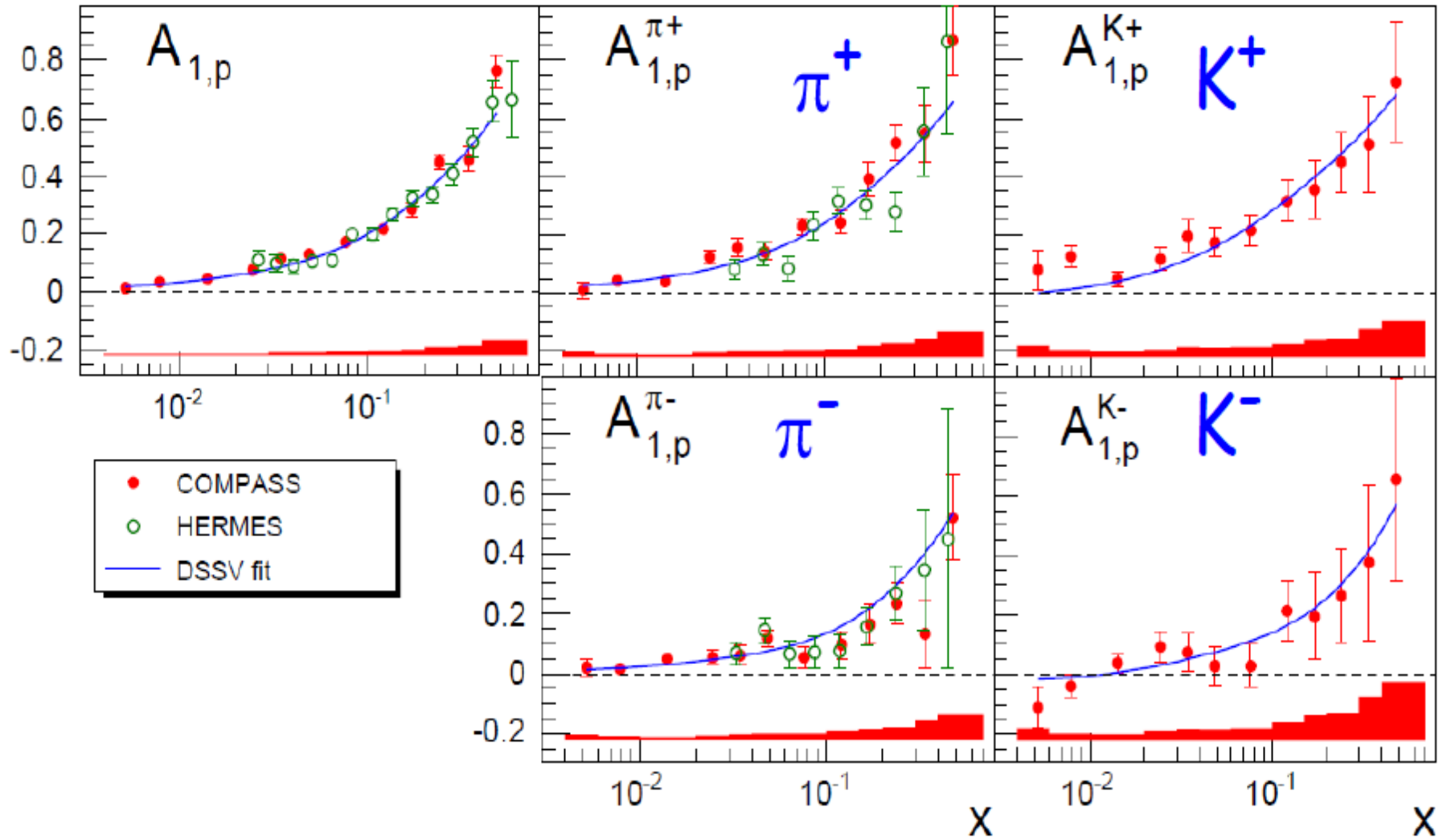


- From these asymmetries one can extract:

$$\Delta u + \Delta d, \quad \Delta \bar{u} + \Delta \bar{d} \quad \text{and} \quad \Delta s = \Delta \bar{s}$$

# Inclusive and semi-inclusive spin asymmetries: Proton data

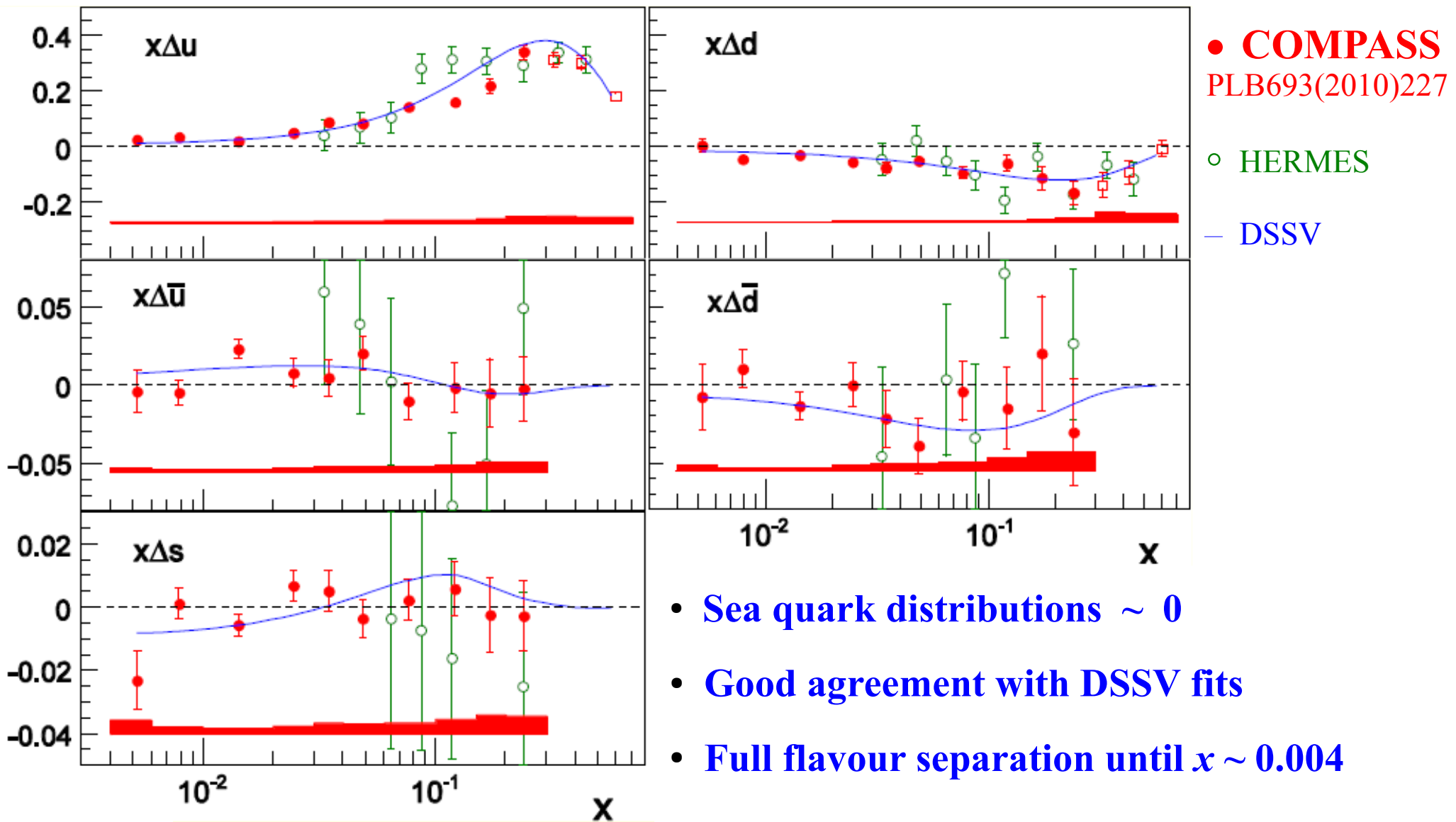
First measurement ever of  $A_{1,p}^K$



- Using  $A_{1,p}^h$  and  $A_{1,d}^h$ , we can separately extract:

$\Delta u$ ,  $\Delta d$ ,  $\Delta \bar{u}$ ,  $\Delta \bar{d}$ ,  $\Delta s$  and  $\Delta \bar{s}$

# Quark helicities from SIDIS ( $Q^2 = 3 \text{ (GeV/c)}^2$ and $x < 0.3$ )

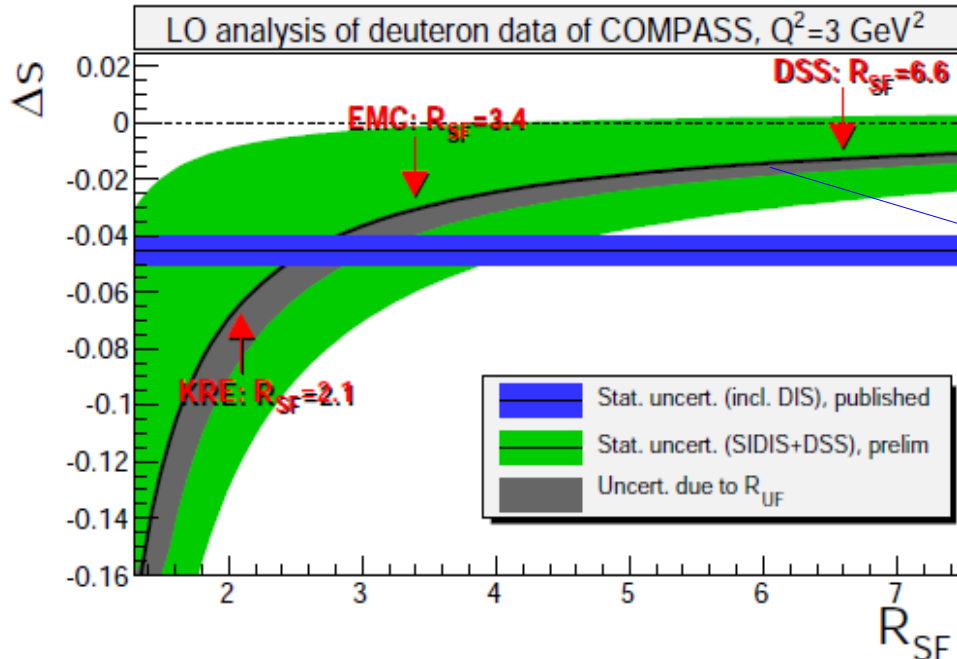


$$\Delta s(\text{SIDIS}) = -0.01 \pm 0.01(\text{stat}) \pm 0.01(\text{syst}) \quad @ \quad 0.003 < x < 0.3$$

## Δs dependence on FFs

- The relation between the semi-inclusive asymmetries and Δs depends only on the following ratios:

$$R_{UF} = \frac{\int_{0.2}^{0.85} D_d^{K^+}(z) dz}{\int_{0.2}^{0.85} D_u^{K^+}(z) dz}, \quad R_{SF} = \frac{\int_{0.2}^{0.85} D_{\bar{s}}^{K^+}(z) dz}{\int_{0.2}^{0.85} D_u^{K^+}(z) dz}$$



$R_{UF}$  is varied linearly from 0.13 (DSS) at  $R_{SF} = 6.6$  to 0.35 (EMC) at  $R_{SF} = 3.4$  (to maintain constant the  $K^+$  multiplicity)

- Determination of  $R_{SF}$  from hadron multiplicities on the way

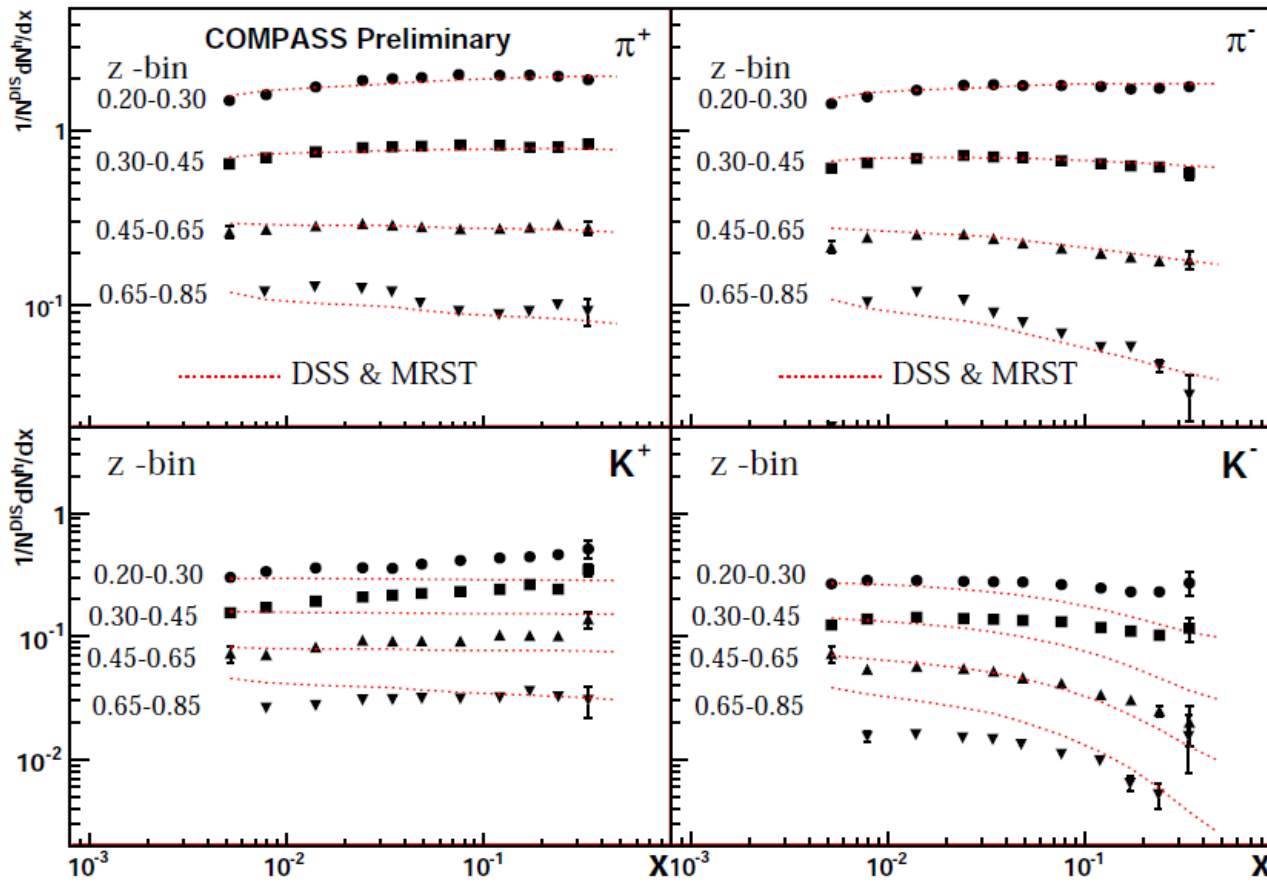
# Hadron Multiplicities

# A first look on hadron multiplicities

- Assuming the quark parton model (leading order):

$$\frac{dM^h(x, Q^2, z)}{dz} = \frac{\sum_q e_q^2 \overset{\text{PDF}}{f_q(x, Q^2)} \overset{\text{FF}}{D_q^h(z, Q^2)}}{\sum_q e_q^2 f_q(x, Q^2)} = \frac{\text{hadron yields}}{\text{DIS events yields}}$$

Experimental definition



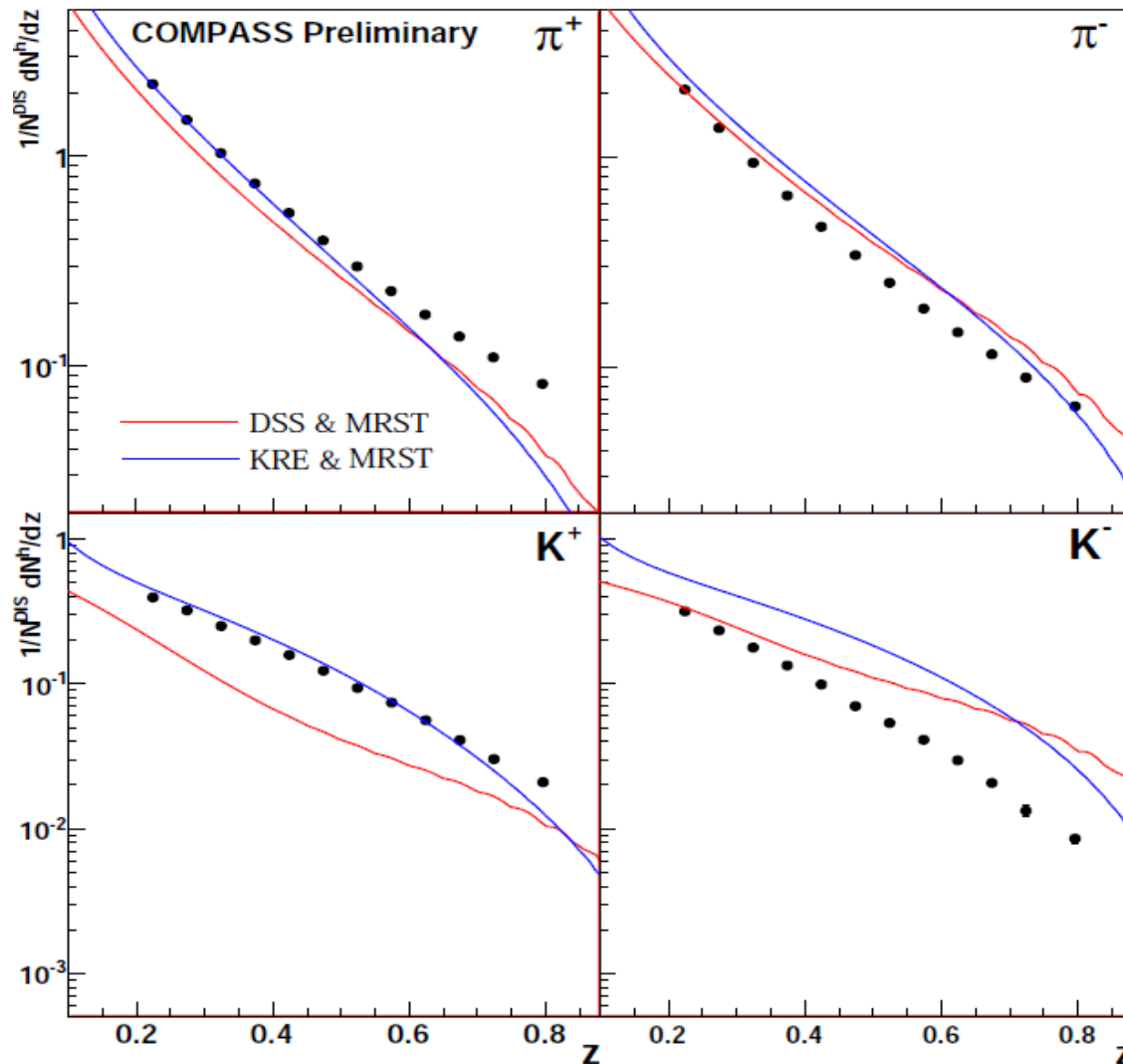
$x$  dependence of

$$\frac{1}{N_{\text{DIS}}} \frac{dN^h}{dz dx}$$

Obtained from a small part of  ${}^6\text{LiD}$  data



# Comparison to parameterisations

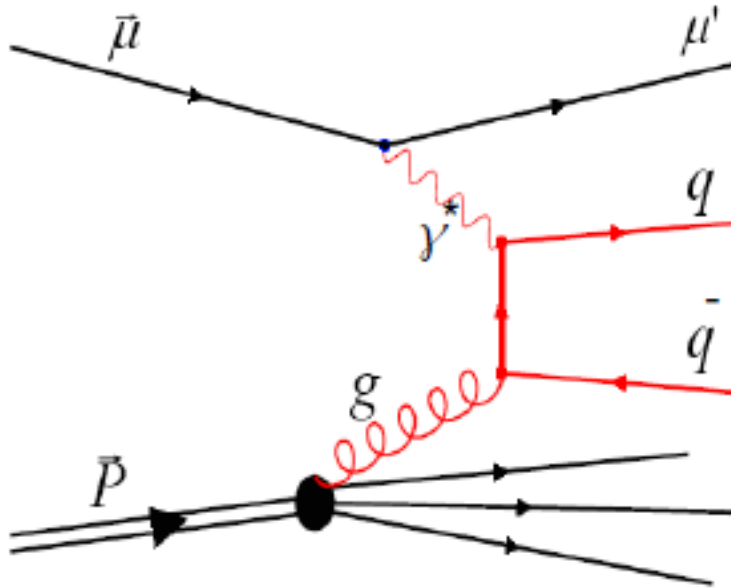


- The existence of discrepancies are evident (especially for K)
- Data can be used to improve our knowledge on FFs (also good for  $\Delta s$ ) and also on poorly known PDFs (like  $s(x)$ )
- It will contribute significantly to our knowledge of the hadronisation process

# **Gluon Polarisation**

# Direct measurement of $\Delta G/G$ at LO in QCD

photon-gluon fusion process (PGF)



$$A_{\mu N}^{\text{PGF}} = \frac{\int d\hat{s} \Delta \sigma^{\text{PGF}} \Delta G(\mathbf{x}_G, \hat{s})}{\int d\hat{s} \sigma^{\text{PGF}} G(\mathbf{x}_G, \hat{s})}$$

$$\approx \langle \mathbf{a}_{LL}^{\text{PGF}} \rangle \frac{\Delta G}{G}$$

Obtained from Monte Carlo and parameterised by a Neural Network (to be used on data)

There are two methods to tag this process:

- **Open Charm production**

- $\gamma^* g \rightarrow c\bar{c} \Rightarrow$  reconstruct  $D^0$  mesons
- **Hard scale:**  $M_c^2$
- **No intrinsic charm in COMPASS kinematics**
- **No physical background**
- **Weakly model dependent**
- **Low statistics**

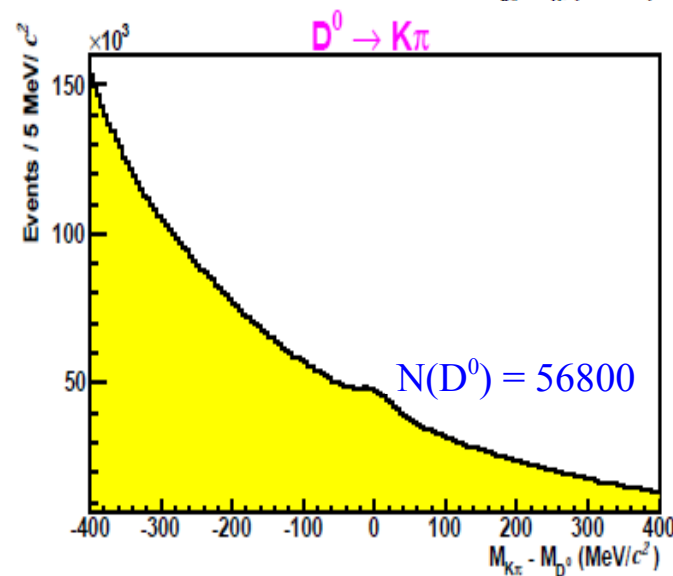
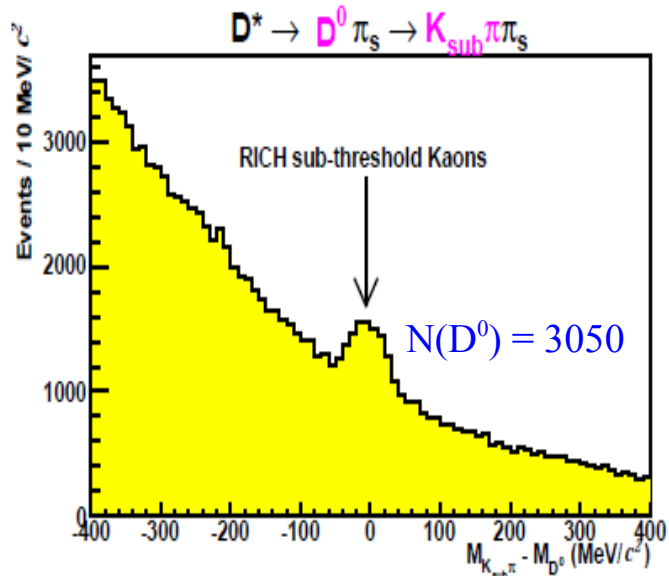
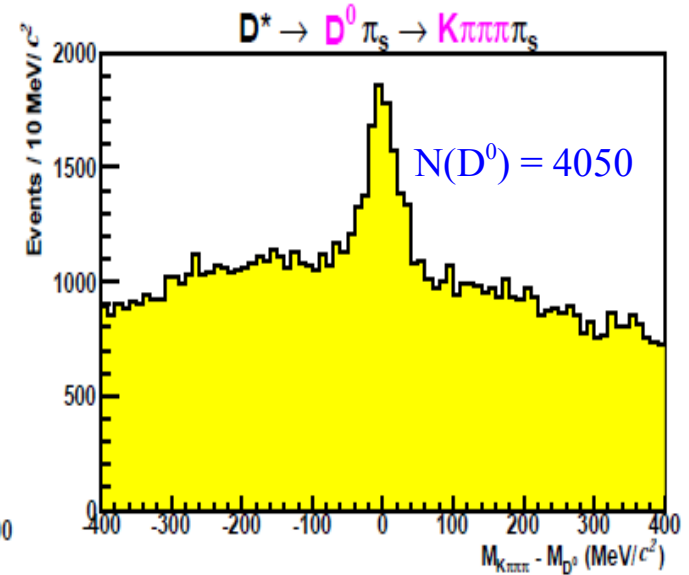
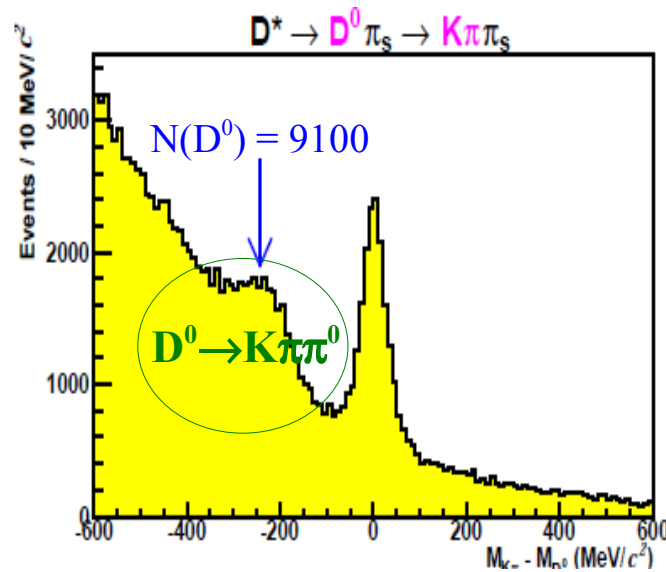
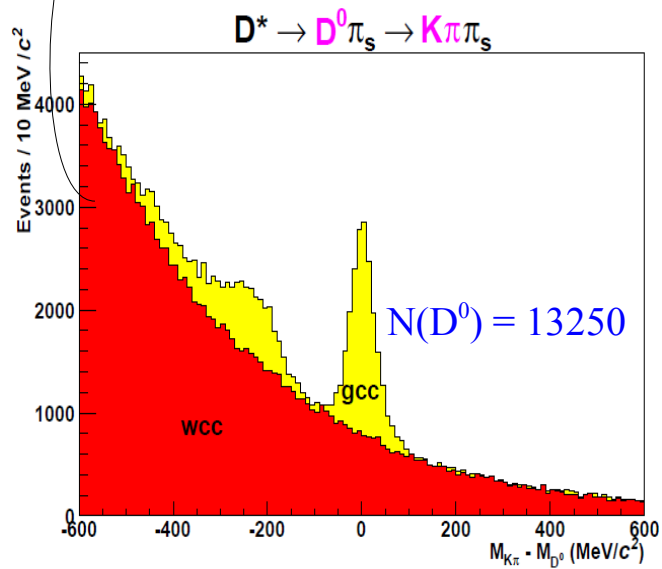
- **High- $p_T$  hadron pairs**

- $\gamma^* g \rightarrow q\bar{q} \Rightarrow$  reconstruct 2 jets or  $h^+h^-$
- **Hard scale:**  $Q^2$  or  $\Sigma p_T^2$  [ $Q^2 > 1$  or  $Q^2 < 1$  ( $\text{GeV}/c$ ) $^2$ ]
- **High statistics**
- **Physical background**
- **Strongly model dependent**

**Open Charm**

# D<sup>0</sup> mass spectra (all samples): $\left( A_{D^0}^{\text{exp}} = \text{fP}_\mu \text{P}_T \frac{S}{S+B} A_{\mu N}^{\text{PGF}} \right)$ D<sup>0</sup> probability

**Wrong Charge Combination of Kπ pairs:** Example of a background model used for the multidimensional kinematic parameterisation (performed by a Neural Network) of S/(S+B)

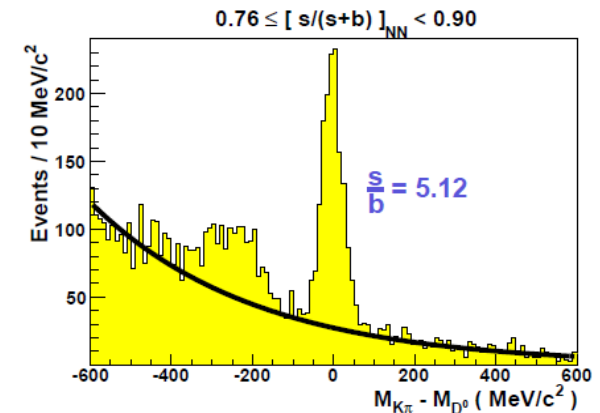
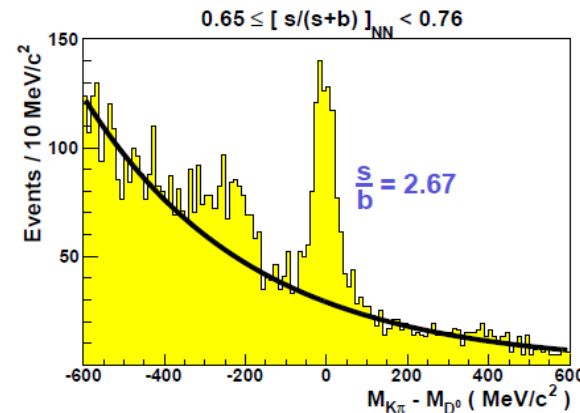
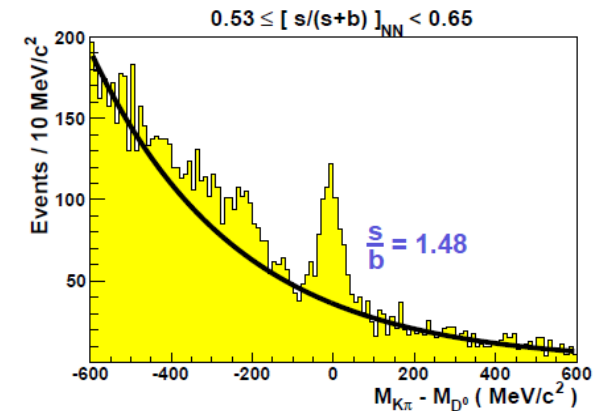
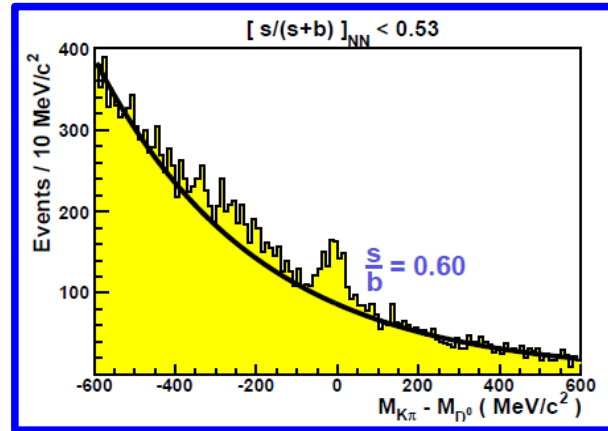


## Number of D<sup>0</sup>:

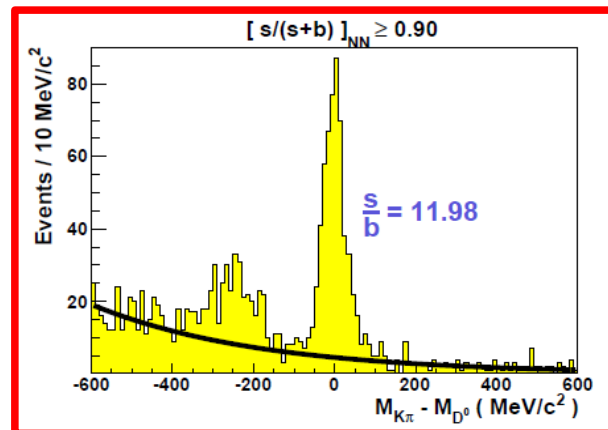
- Total → 86250
- <sup>6</sup>LiD → 57400
- NH<sub>3</sub> → 28850

# $s/(s+b)$ : Obtaining final probabilities for a $D^0$ candidate

- Events with small  $[s/(s+b)]_{NN}$ 
  - Mostly combinatorial background is selected



$s/(s+b)$  is obtained from a fit to these spectra (correcting all events with the corresponding values of  $[s/(s+b)]_{NN}$ )



- Events with large  $[s/(s+b)]_{NN}$ 
  - Mostly Open Charm events are selected

$$\delta\left(\frac{\Delta G}{G}\right) = \frac{1}{\text{FOM}}$$

**High- $p_T$  hadron pairs**

# High- $p_T$ asymmetries (2002-2006): $Q^2 > 1$ (GeV/c)<sup>2</sup>

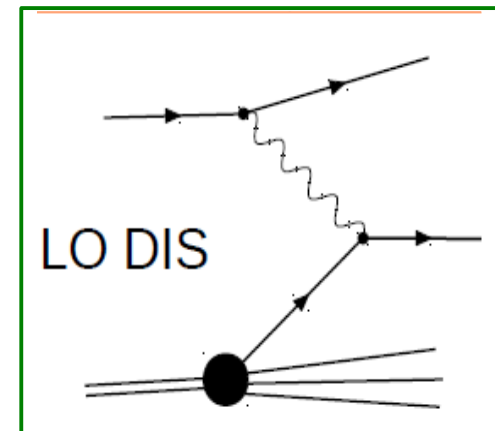
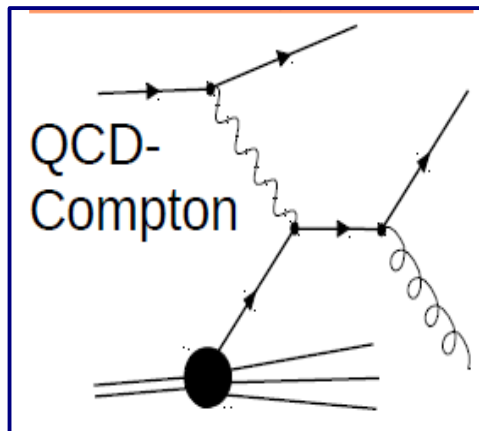
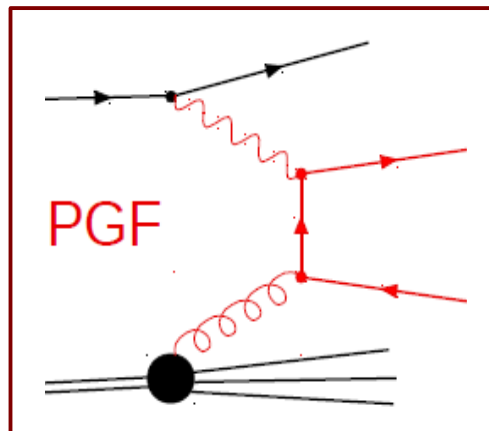
- Two samples are considered (fractions of the processes are estimated from MC):

→ Inclusive asymmetry

$$A_1^d(\mathbf{x}) = \frac{\Delta G}{G}(\mathbf{x}_g) \left( a_{LL}^{PGF,inc} \frac{\sigma^{PGF,inc}}{\sigma_{Tot,inc}} \right) + A_1^{LO}(\mathbf{x}_C) \left( a_{LL}^{C,inc} \frac{\sigma^{C,inc}}{\sigma_{Tot,inc}} \right) + A_1^{LO}(\mathbf{x}_{Bj}) \left( D \frac{\sigma^{LO,inc}}{\sigma_{Tot,inc}} \right)$$

$$A_{LL}^{2h}(\mathbf{x}) = \left( \frac{A^{exp}}{f P_\mu P_T} \right) = \frac{\Delta G}{G}(\mathbf{x}_g) \left( a_{LL}^{PGF} \frac{\sigma^{PGF}}{\sigma_{Tot}} \right) + A_1^{LO}(\mathbf{x}_C) \left( a_{LL}^C \frac{\sigma^C}{\sigma_{Tot}} \right) + A_1^{LO}(\mathbf{x}_{Bj}) \left( D \frac{\sigma^{LO}}{\sigma_{Tot}} \right)$$

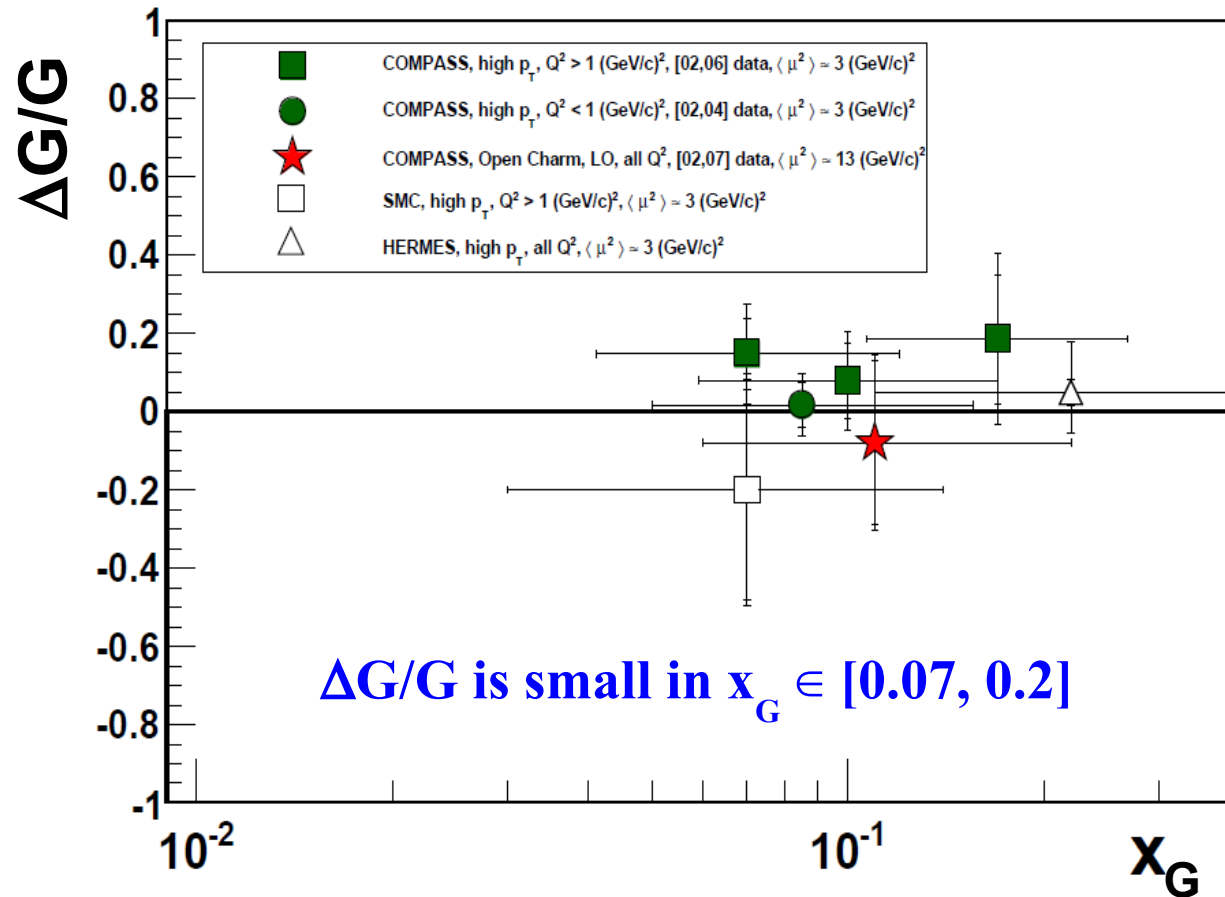
high- $p_T$  hadron pairs ( $p_{T1} / p_{T2} > 0.7 / 0.4$  GeV/c)  $\Rightarrow$  enhancement of the PGF contribution





# World measurements of $\Delta G/G$ at LO in QCD

- The gluon polarisation was obtained directly from the data, **at LO**, and was found to be compatible with zero

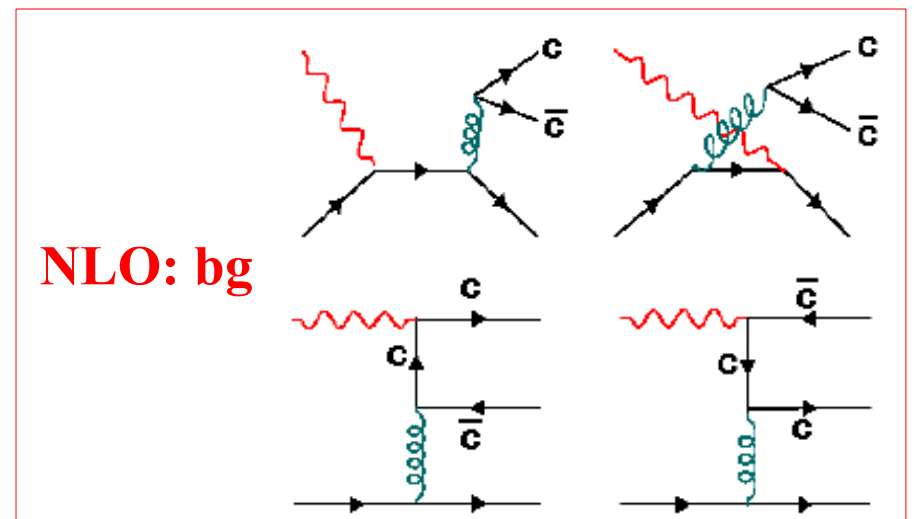
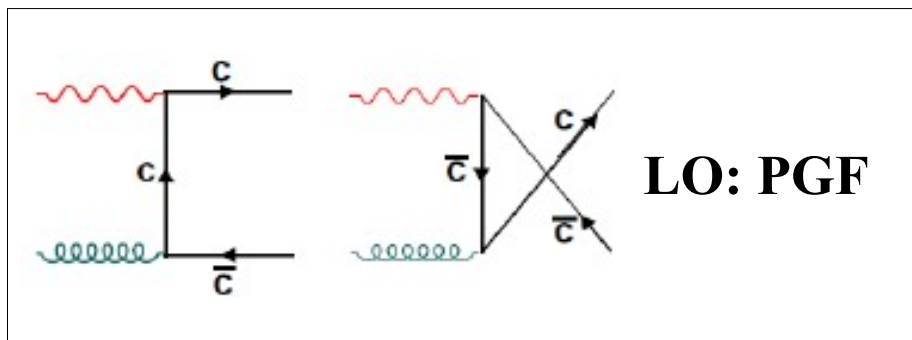
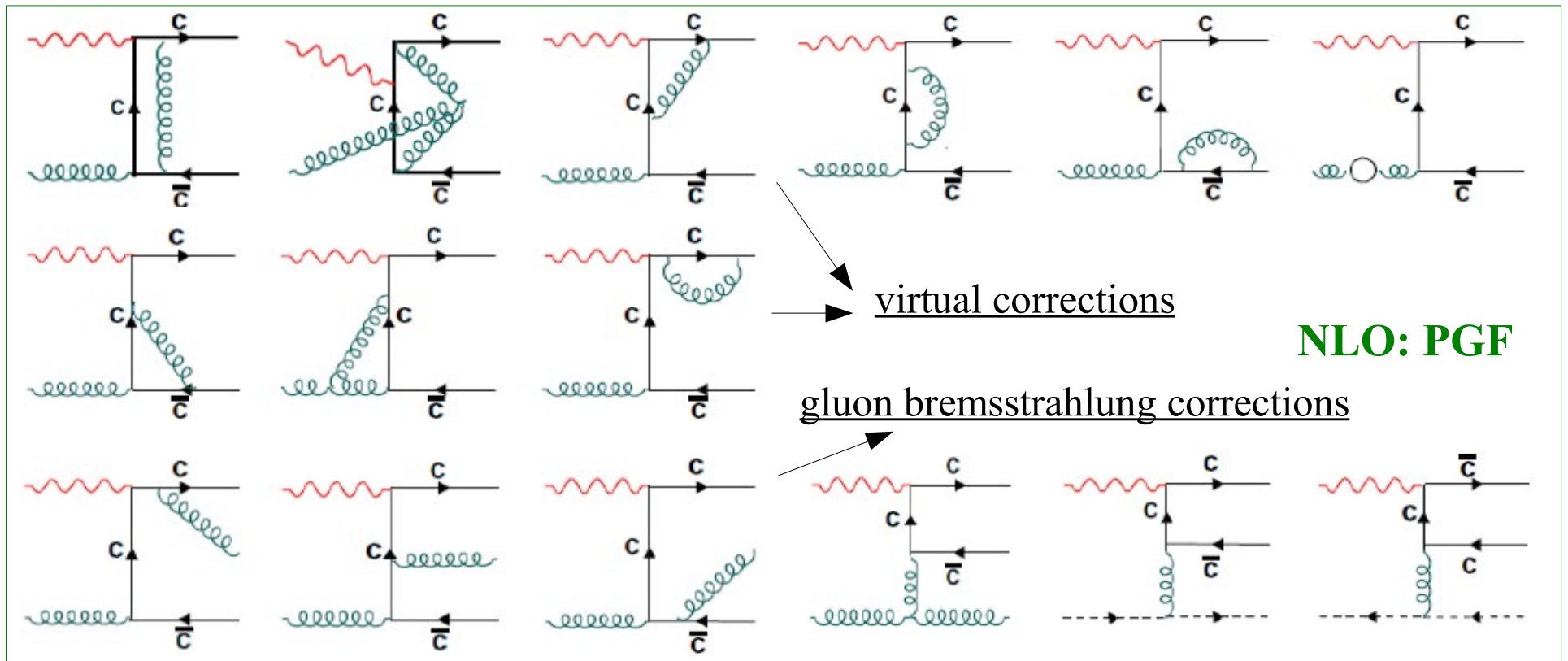


$$\Delta G/G \text{ (high-}p_T, Q^2 > 1) = 0.125 \pm 0.060 \text{ (stat)} \pm 0.063 \text{ (syst)} \quad @\langle x_G \rangle = 0.09^{+0.08}_{-0.04}$$

$$\Delta G/G \text{ (Open Charm)} = -0.081 \pm 0.213 \text{ (stat)} \pm 0.094 \text{ (syst)} \quad @\langle x_G \rangle = 0.11^{+0.11}_{-0.05}$$

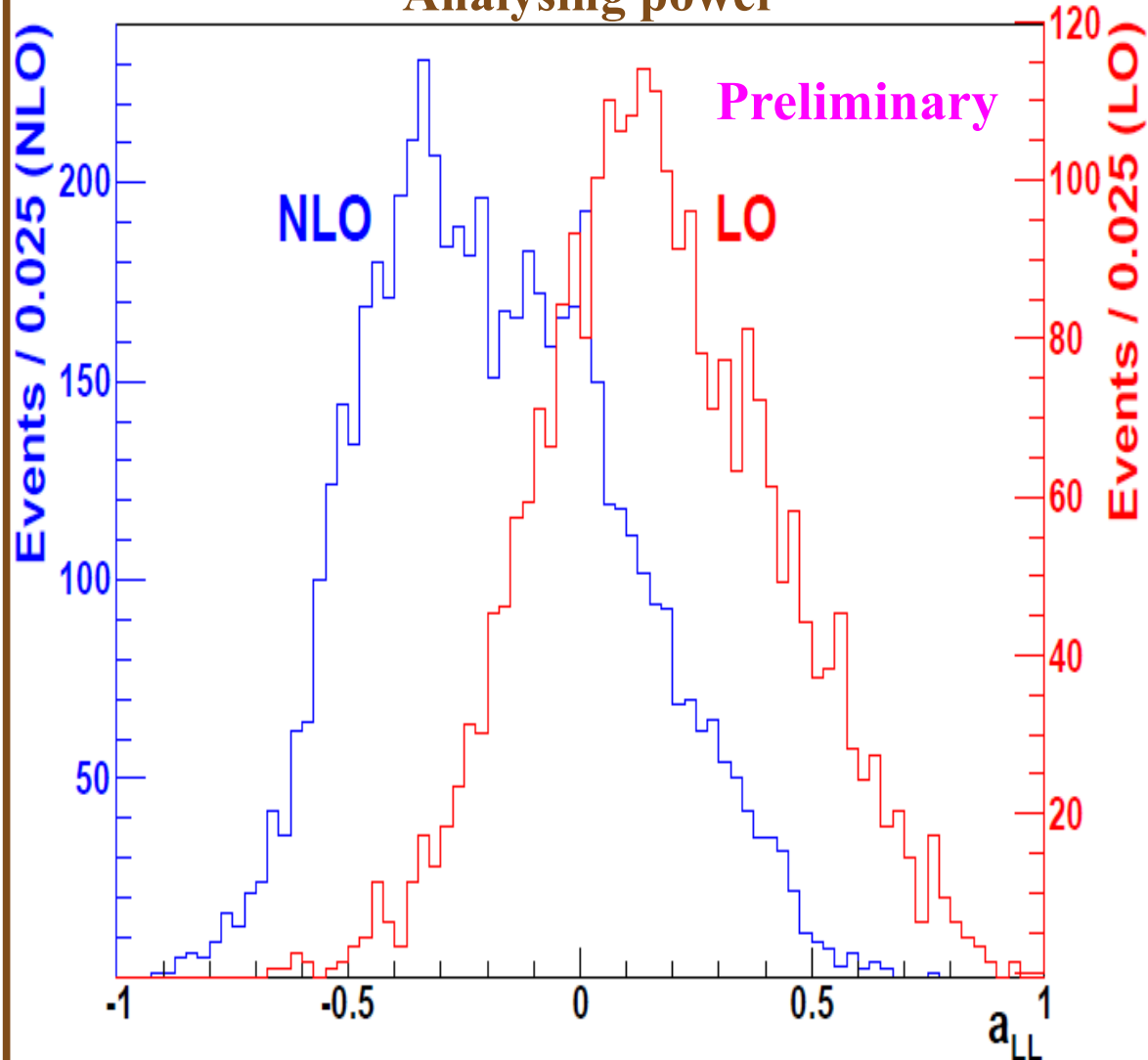
# **NLO results from Open Charm**

# NLO corrections to the analysing power $a_{LL}$

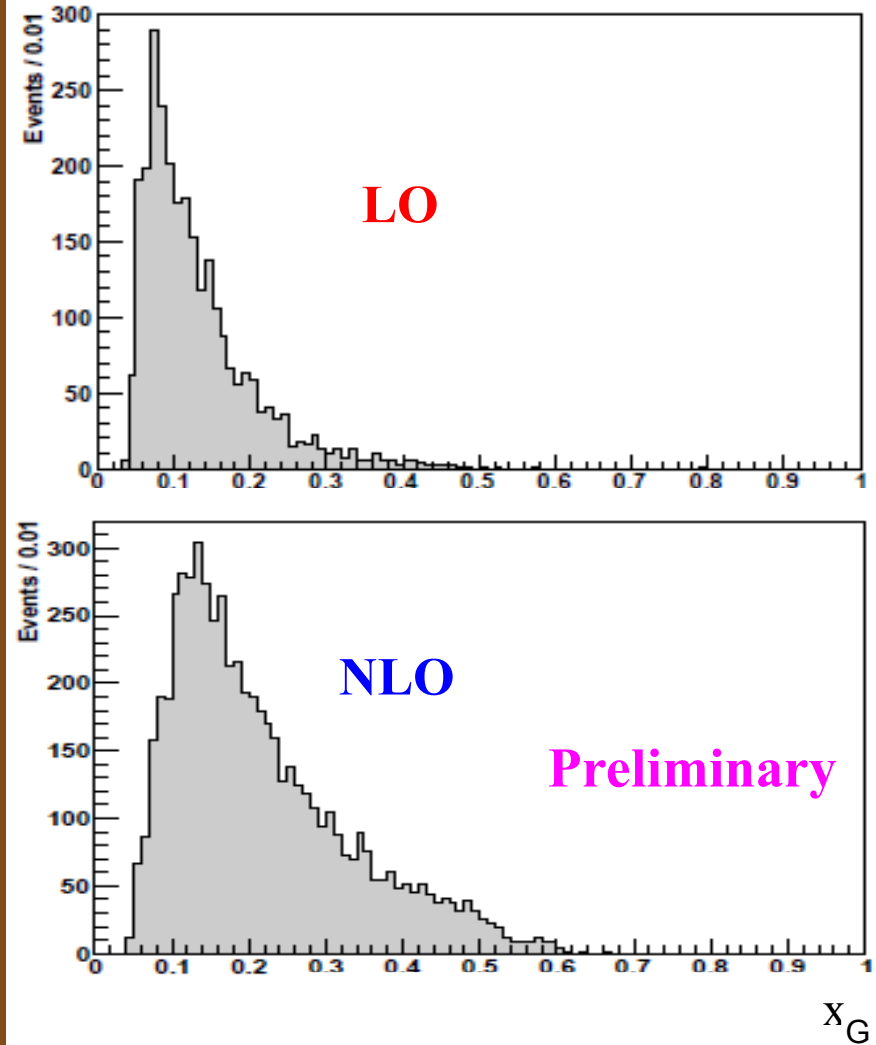


# Distributions of $a_{LL}$ and $x_G$ at LO and NLO in QCD

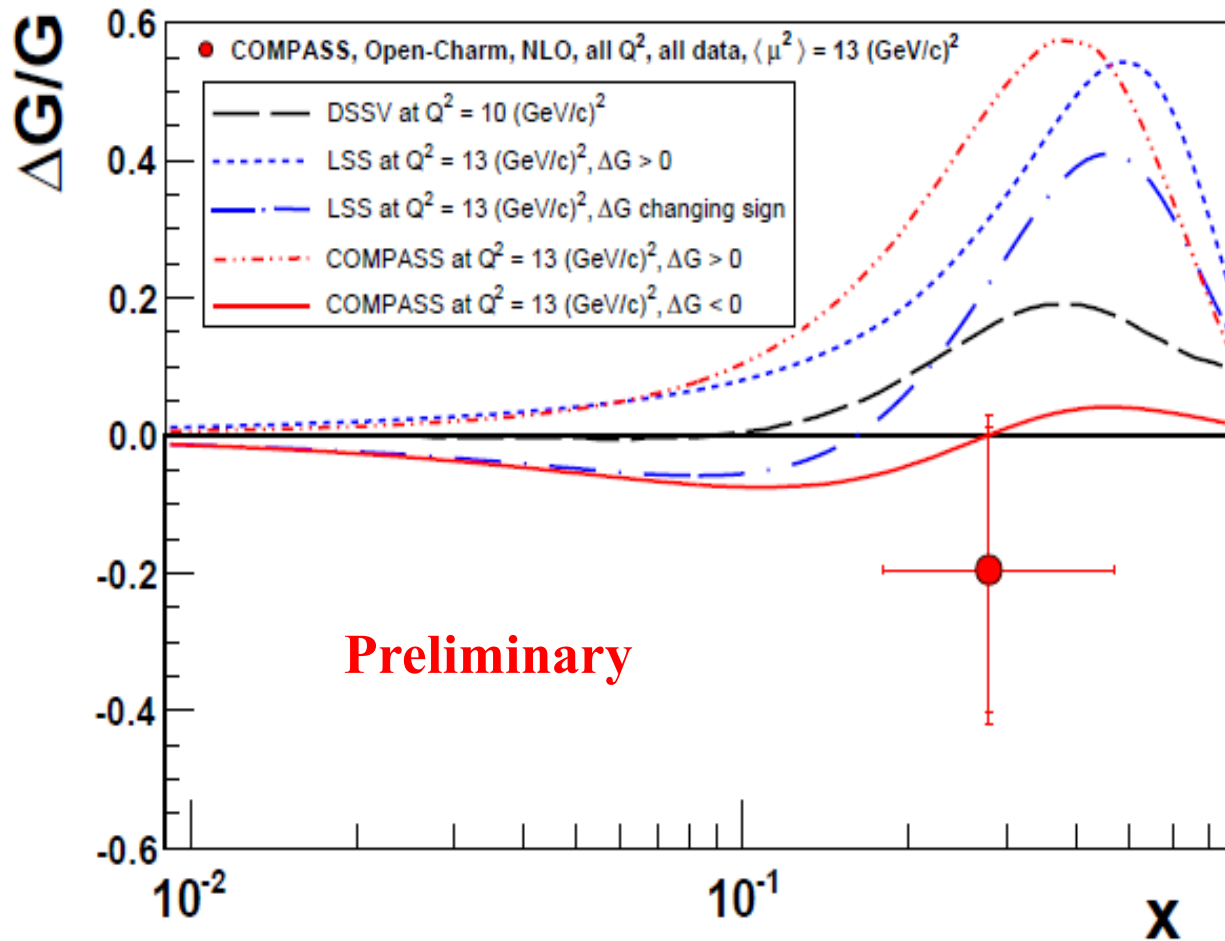
### Analysing power



### Gluon momentum fraction



# $\Delta G/G$ result at NLO in QCD $\rightarrow$ first world measurement

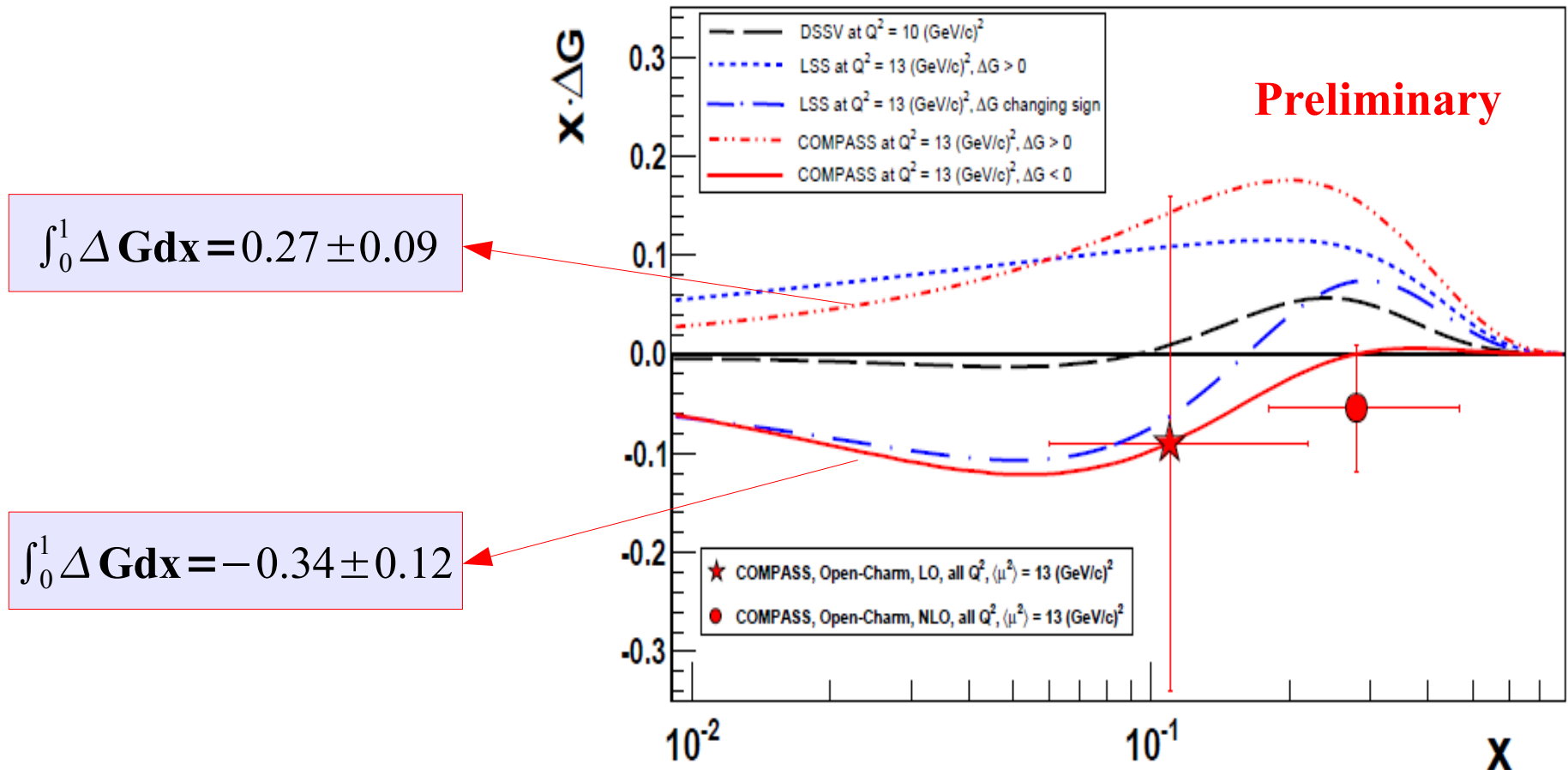


$$\frac{\Delta G}{G} = -0.20 \pm 0.21 \text{ (stat)} \pm 0.09 \text{ (syst)} \quad @ \langle x_G \rangle = 0.28_{-0.10}^{+0.19}, \quad \langle \mu^2 \rangle = 13 (\text{GeV}/c)^2$$

Only experimental: theoretical uncertainties associated with  $a_{LL}$  are still under study!

# Open Charm results for $x\Delta G$

- Using the LO and NLO parameterisations of  $xG$  corresponding to the ones used in the calculations of  $a_{LL}$ , we obtain the following results from  $\Delta G/G$  (the comparison of the LO point with the QCD fits is justified by  $xG(\text{LO}) \approx xG(\text{NLO})$ ):



**SPARES**

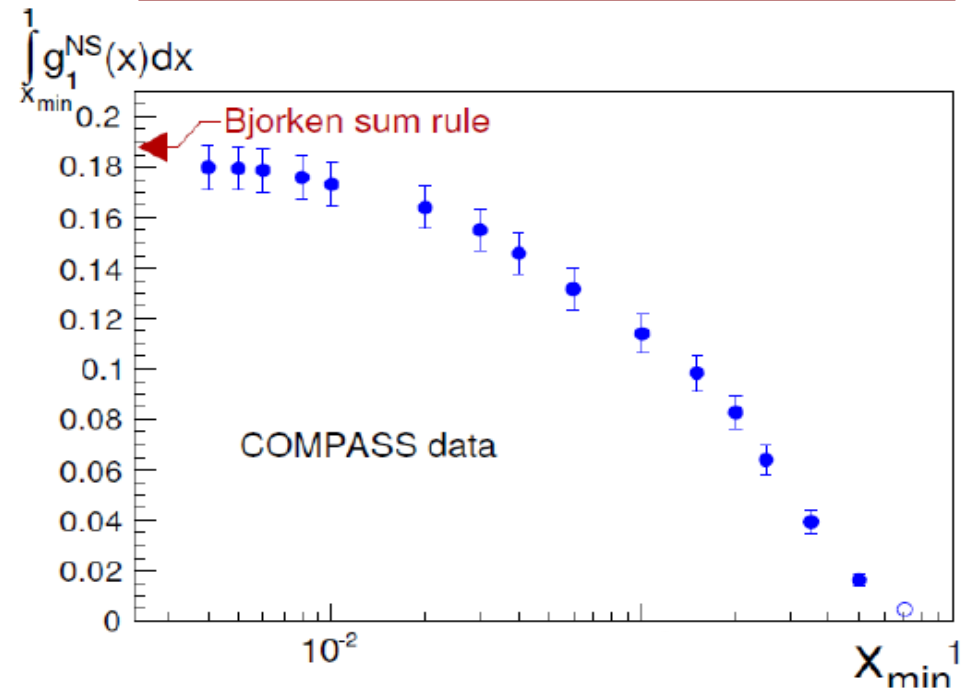
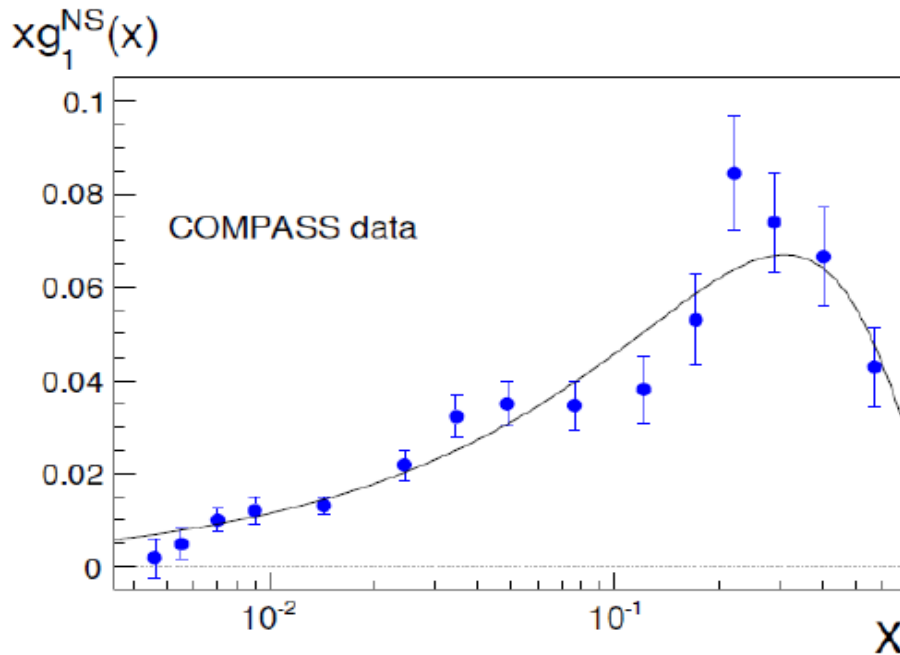
# Bjorken sum rule

- According to the Bjorken sum rule the first moment of the non-singlet spin structure function,  $g_1^{NS}$ , is proportional to the ratio of axial and vector coupling constants  $g_A/g_V$ :

$$\int_0^1 g_1^{NS}(x, Q^2) dx = \frac{1}{6} \left| \frac{g_A}{g_B} \right| C_1^{NS}(Q^2)$$

using

$$\begin{aligned} g_1^{NS}(x, Q^2) &= g_1^p(x, Q^2) - g_1^n(x, Q^2) \\ &= 2g_1^p - 2g_1^d / (1 - 1.5\omega_D) \end{aligned}$$



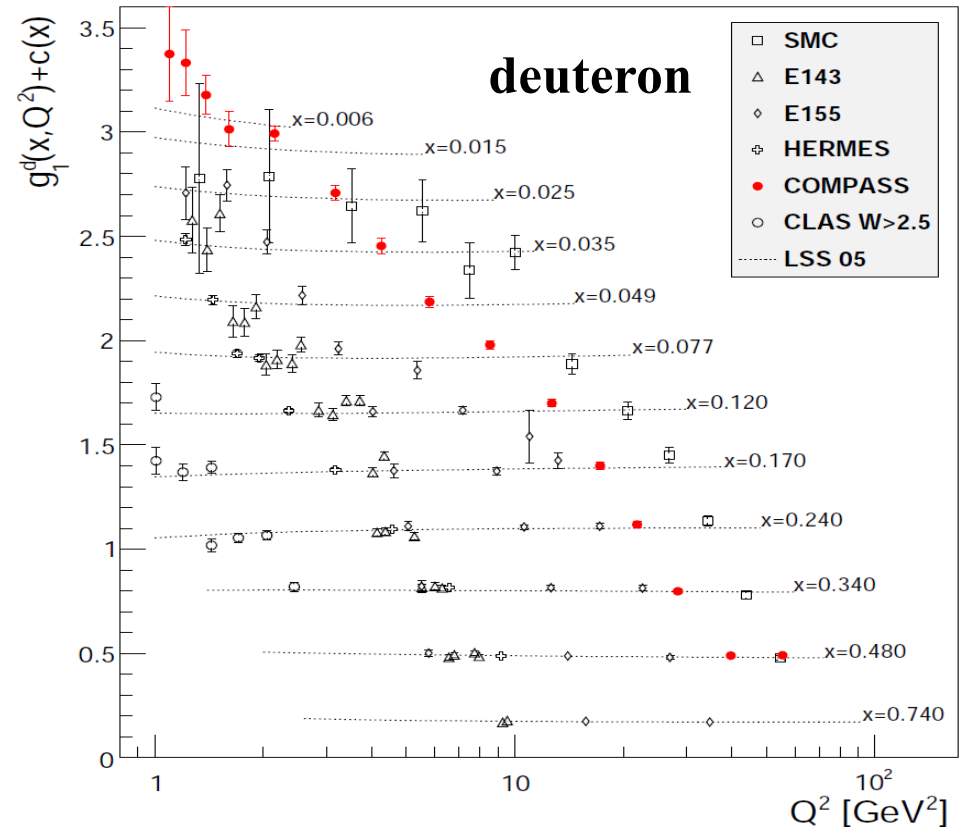
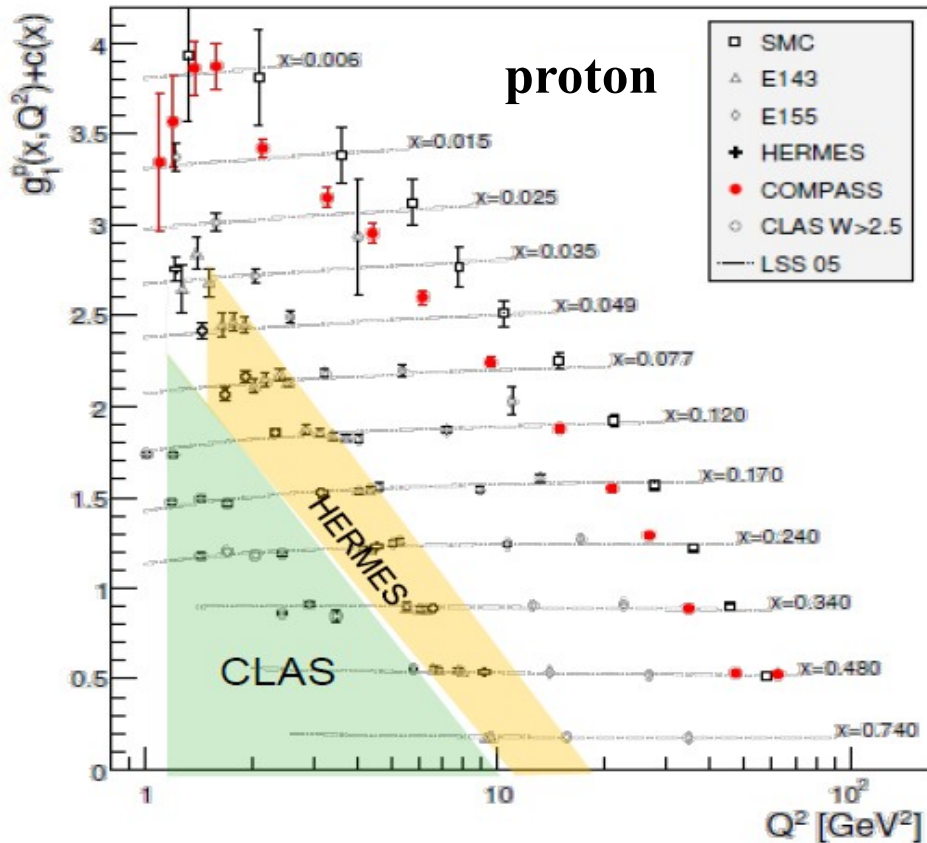
- QCD fit of COMPASS data using  $\Delta q^{NS} = |g_A/g_V| x^\alpha (1-x)^\beta$ :

$$\left| \frac{g_A}{g_V} \right| = 1.28 \pm 0.07(\text{stat}) \pm 0.10(\text{sys})$$

( PDG value:  $|g_A/g_V| = 1.269 \pm 0.003$  )



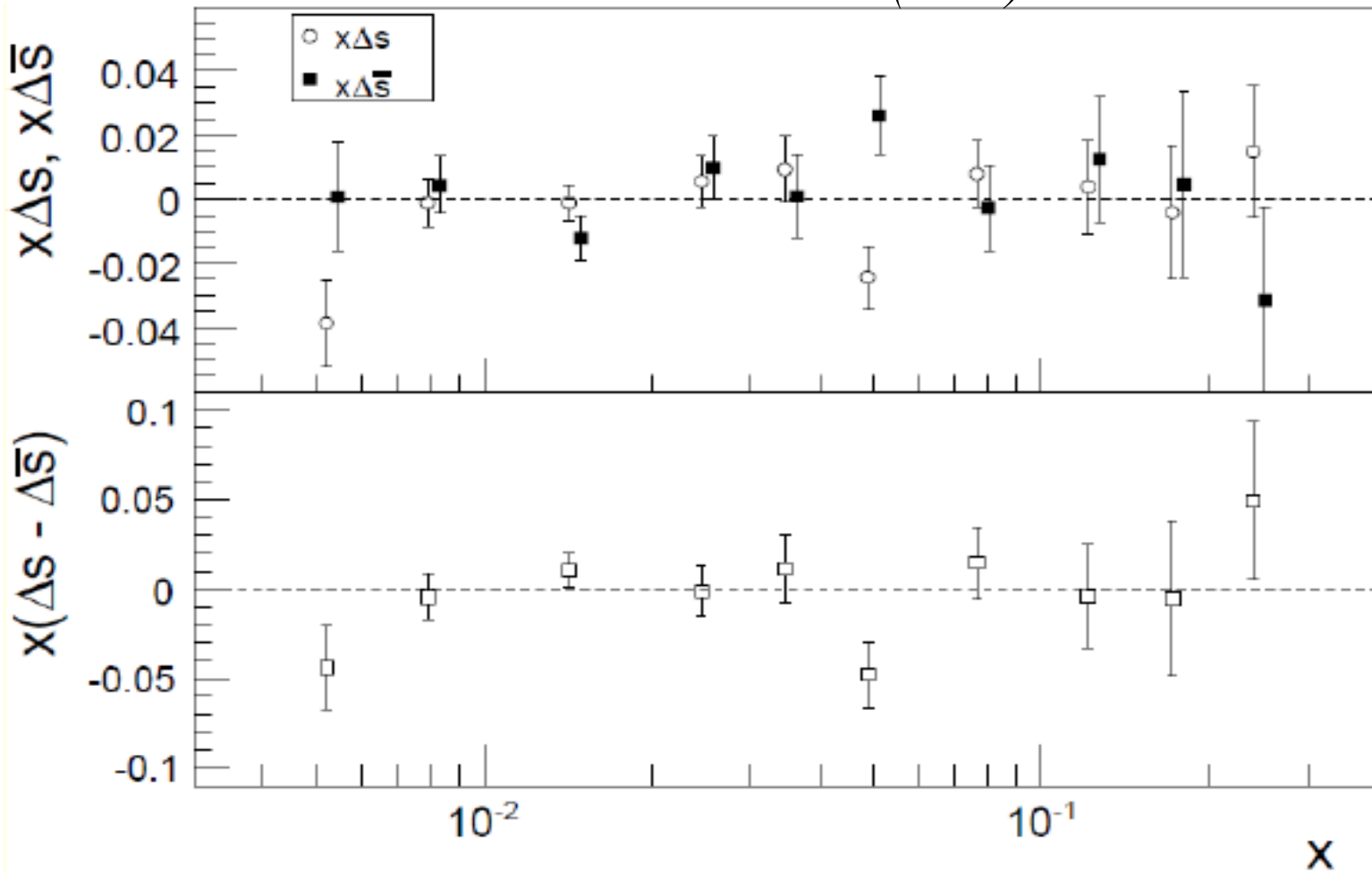
# $Q^2$ dependence of $g_1(x, Q^2)$ for DGLAP evolution



- The kinematic range is still limited (compared to the unpolarised  $F_2$ )
  - ➔ additional data from colliders is required!
- $(\Delta u + \Delta \bar{u})$  and  $(\Delta d + \Delta \bar{d})$  are well constrained by the data (*LSS PRD 80 2009*)
- $\Delta s$  comes out negative and  $\Delta g$  is small ( $< 0.5$ ) ➔ Still with large uncertainties

# Comparison of $\Delta s$ with $\Delta \bar{s}$

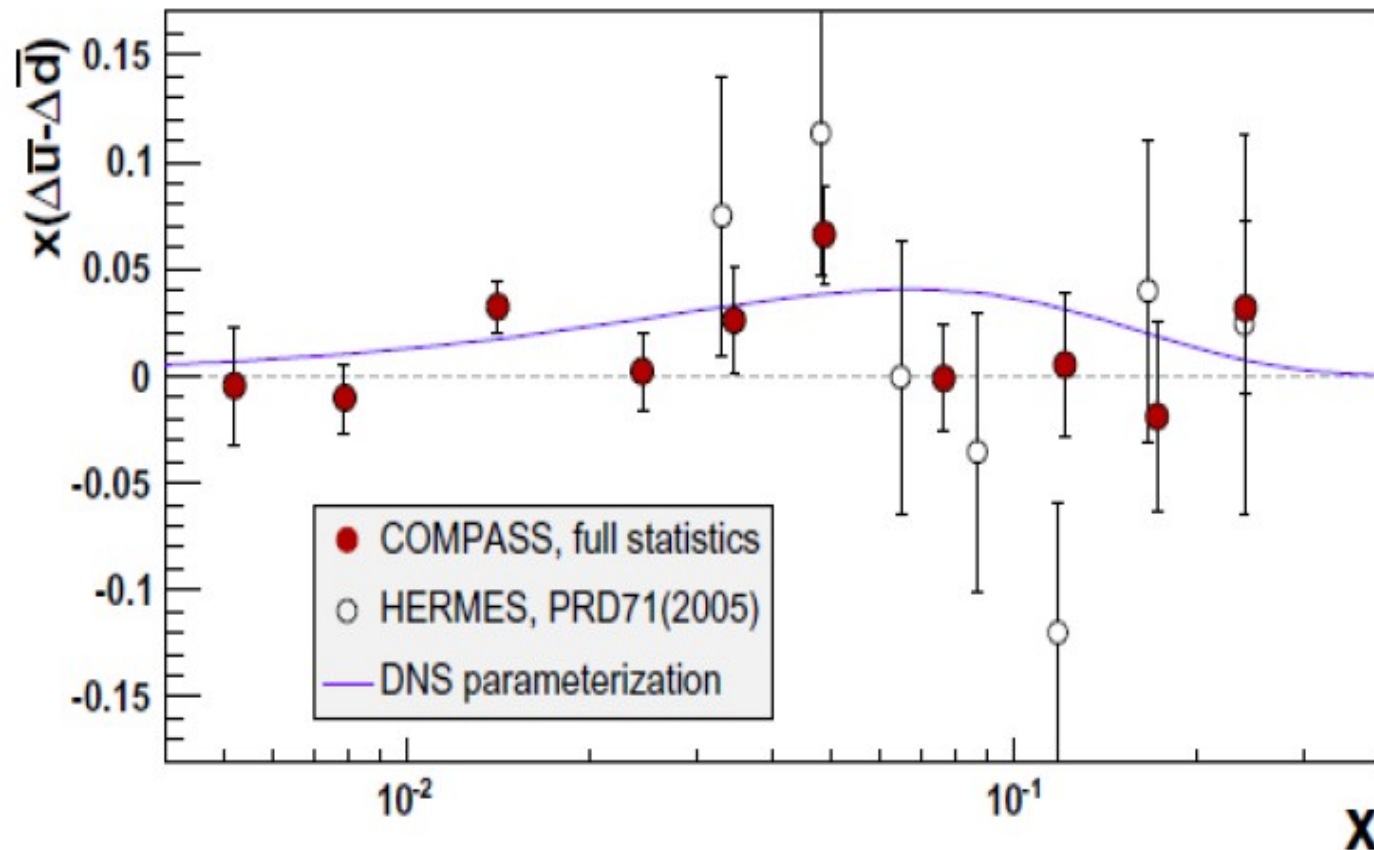
COMPASS PLB 693 (2010) 227



$\Delta s - \Delta \bar{s}$  is compatible with 0  $\rightarrow$   $\Delta s = \Delta \bar{s}$  is assumed in the analysis

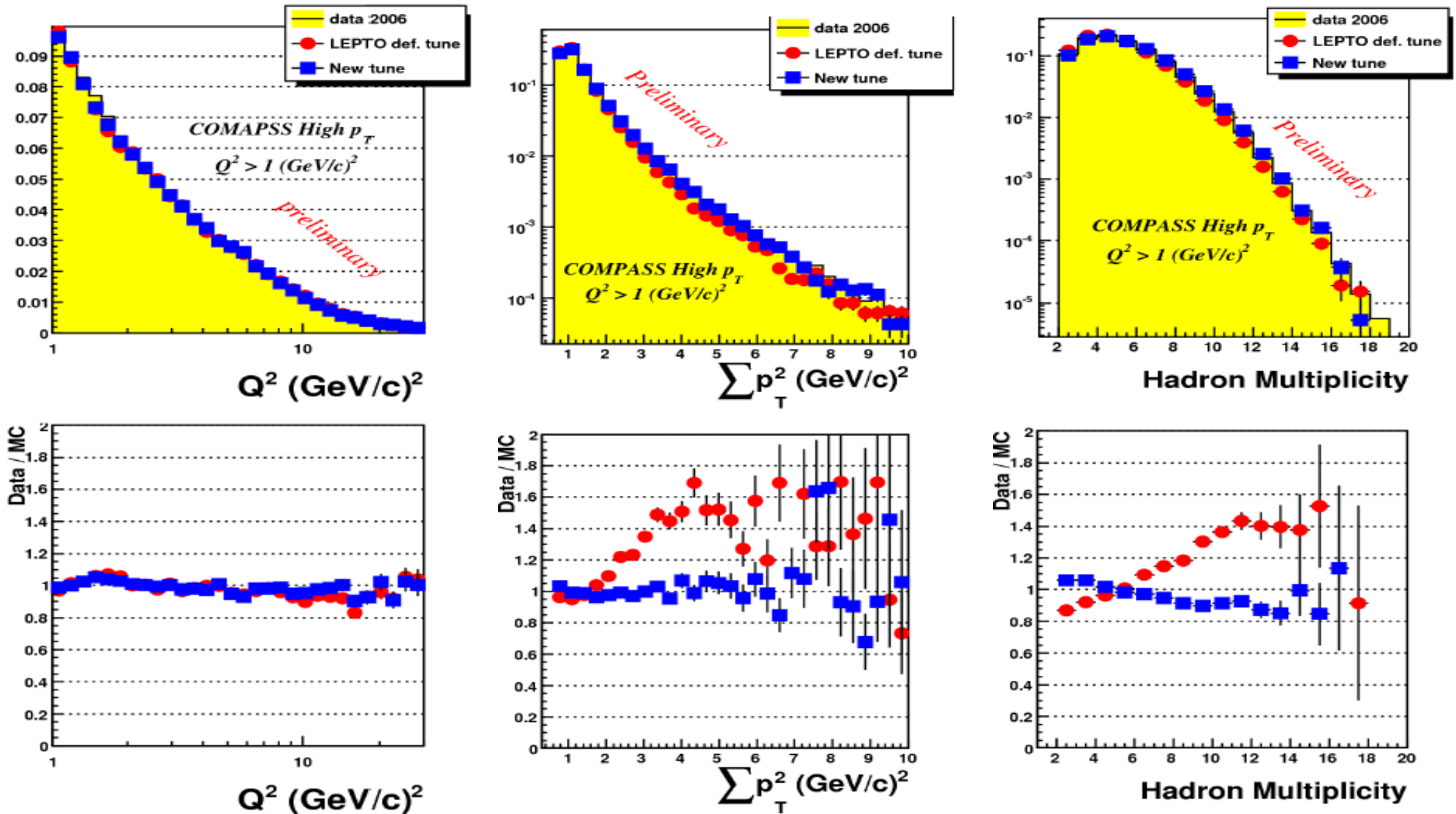
## $\Delta\bar{u} - \Delta\bar{d}$ : Flavour asymmetry?

- The considerable asymmetry observed for  $(\bar{u} - \bar{d})$  is not verified in the polarised case :
- $\Delta\bar{u} - \Delta\bar{d}$  is slightly positive but compatible with zero!



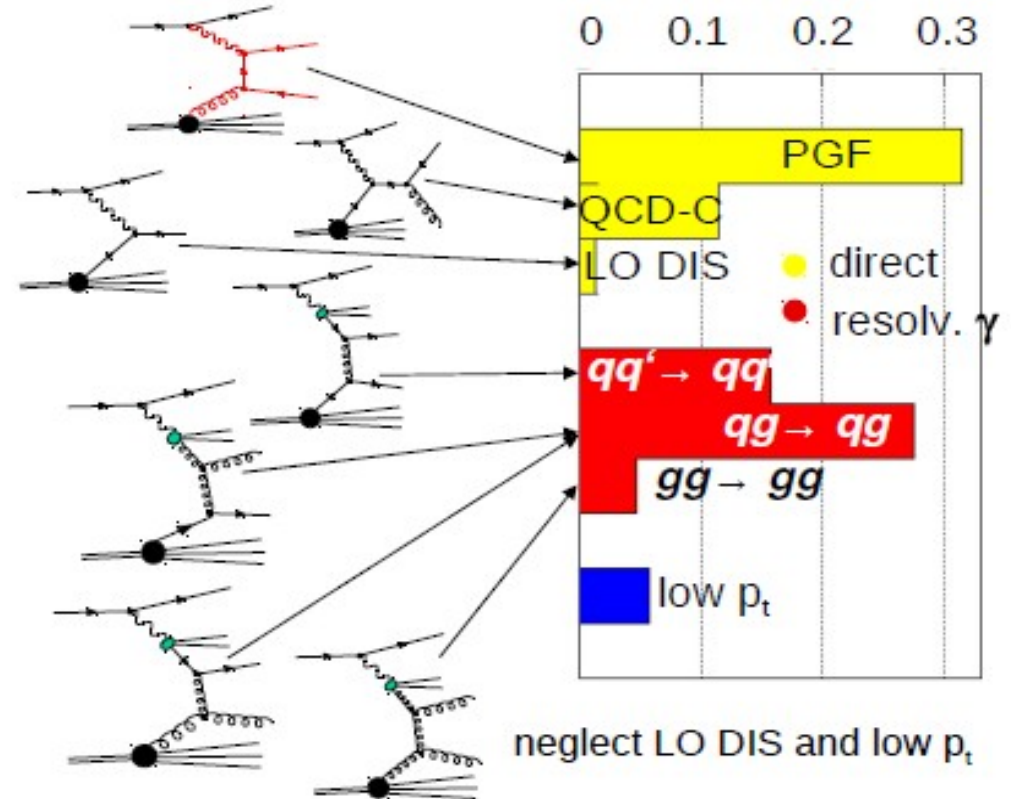
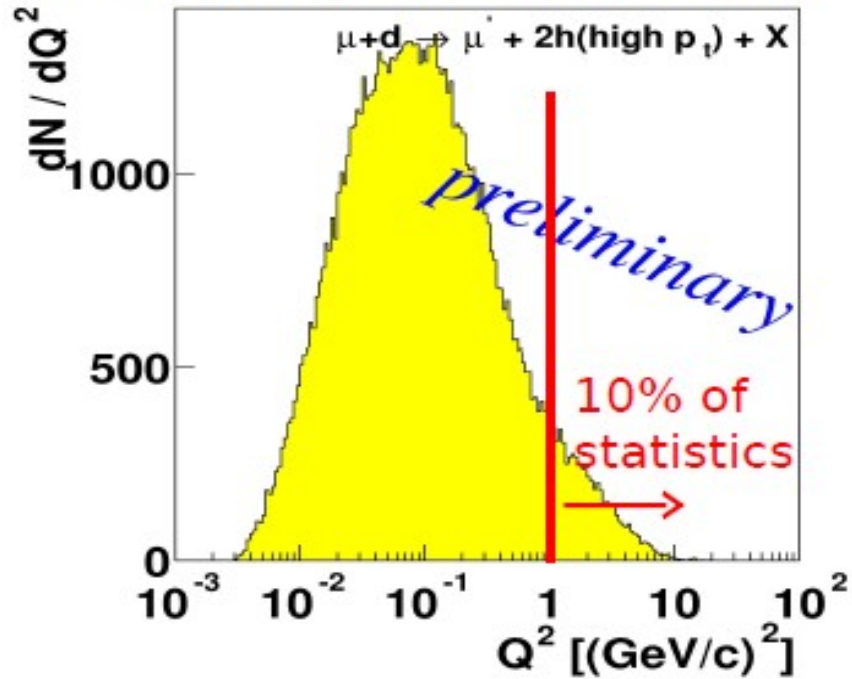
# Data vs Monte Carlo: Comparison of $Q^2$ and hadron variables

Monte Carlo (PS on): **LEPTO** generator with PDFs from **MSTW2008LO**



The impact of this tuning is included in the systematic error

# High- $p_T$ analysis: $Q^2 < 1 \text{ (GeV/c)}^2$



**2002-2004 Preliminary:**

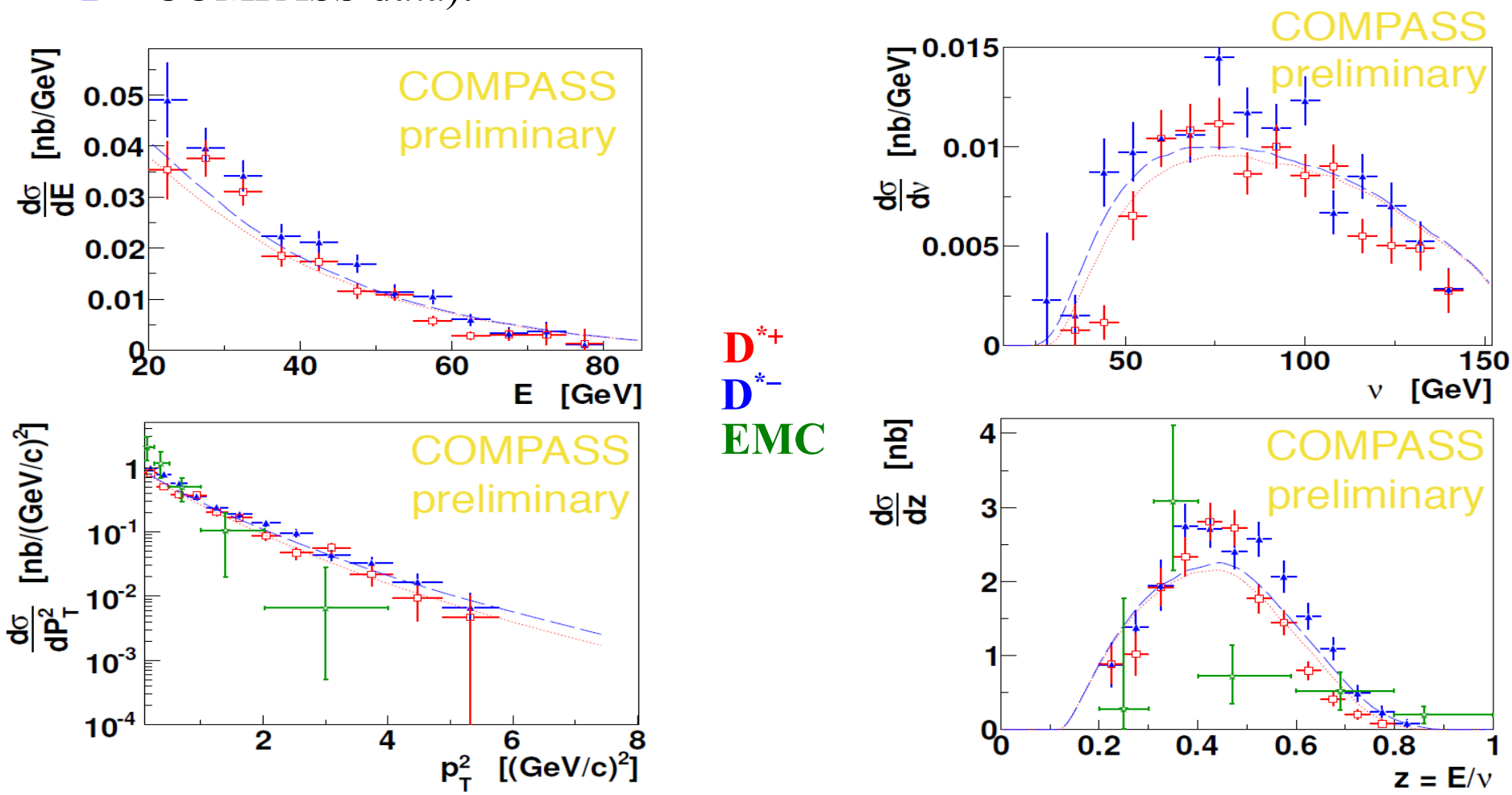
$$\Delta G/G = 0.016 \pm 0.058 \text{ (stat)} \pm 0.055 \text{ (syst)}$$

**2002-2003 Published:**

$$\Delta G/G = 0.024 \pm 0.089 \text{ (stat)} \pm 0.057 \text{ (syst)} \rightarrow \textit{Phys. Lett. B 633 (2006) 25 - 32}$$

# AROMA with PS-ON versus COMPASS data

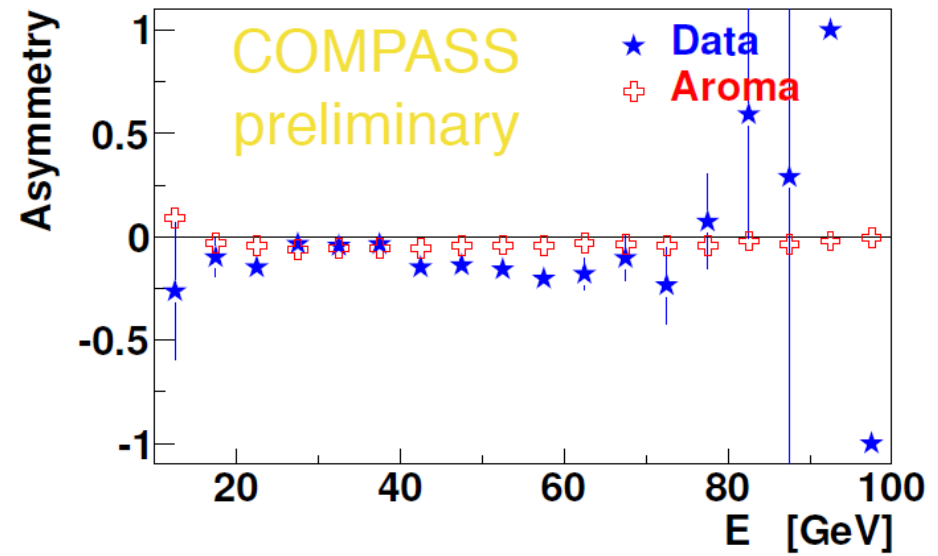
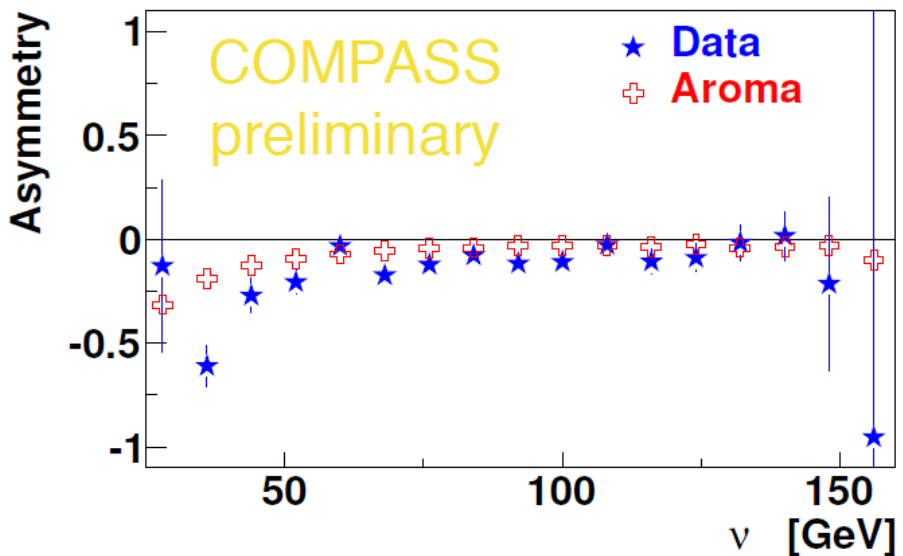
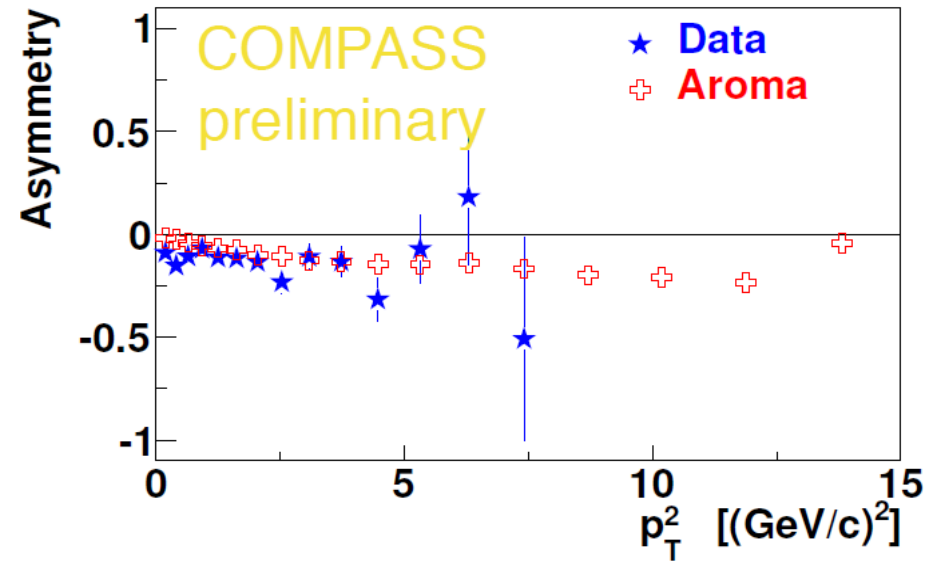
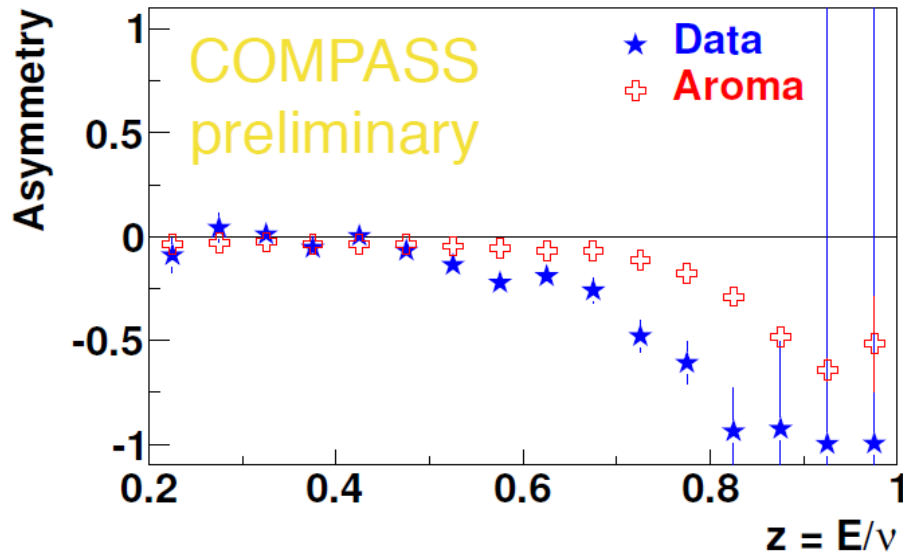
- Differential cross section for  $D^*$  meson production ( $D^0_{K\pi}$  (2004) from  $D^{*+}$  and  $D^{*-}$  COMPASS data):

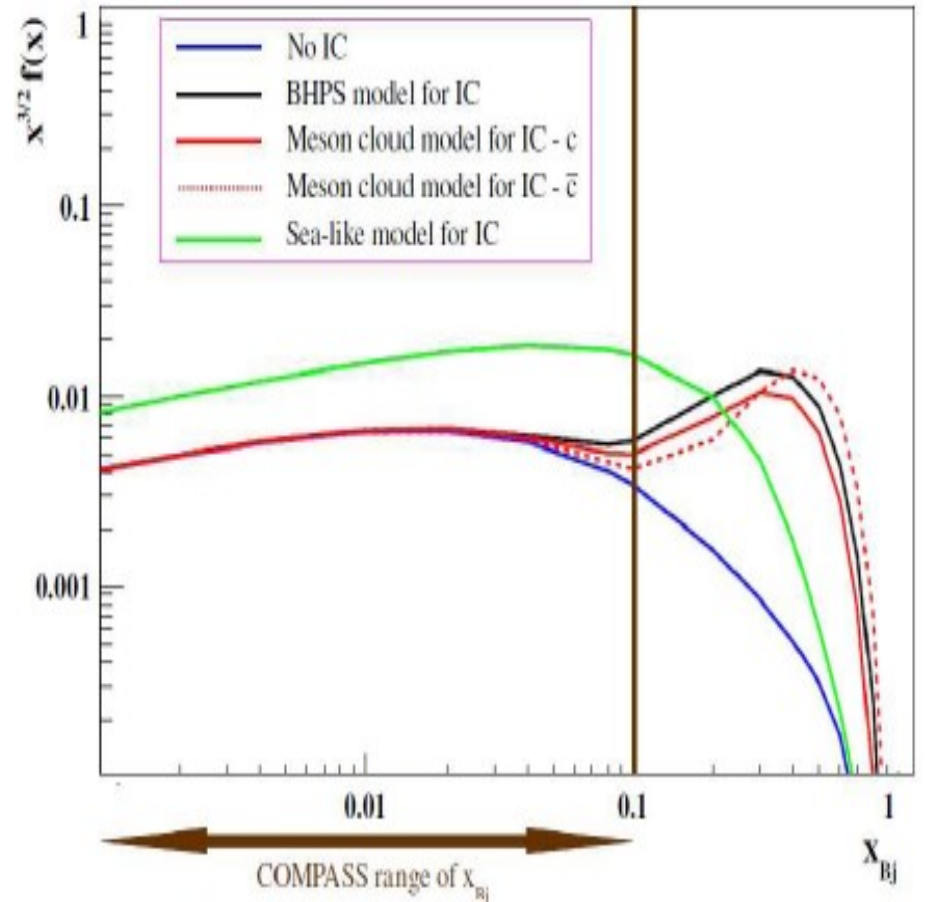
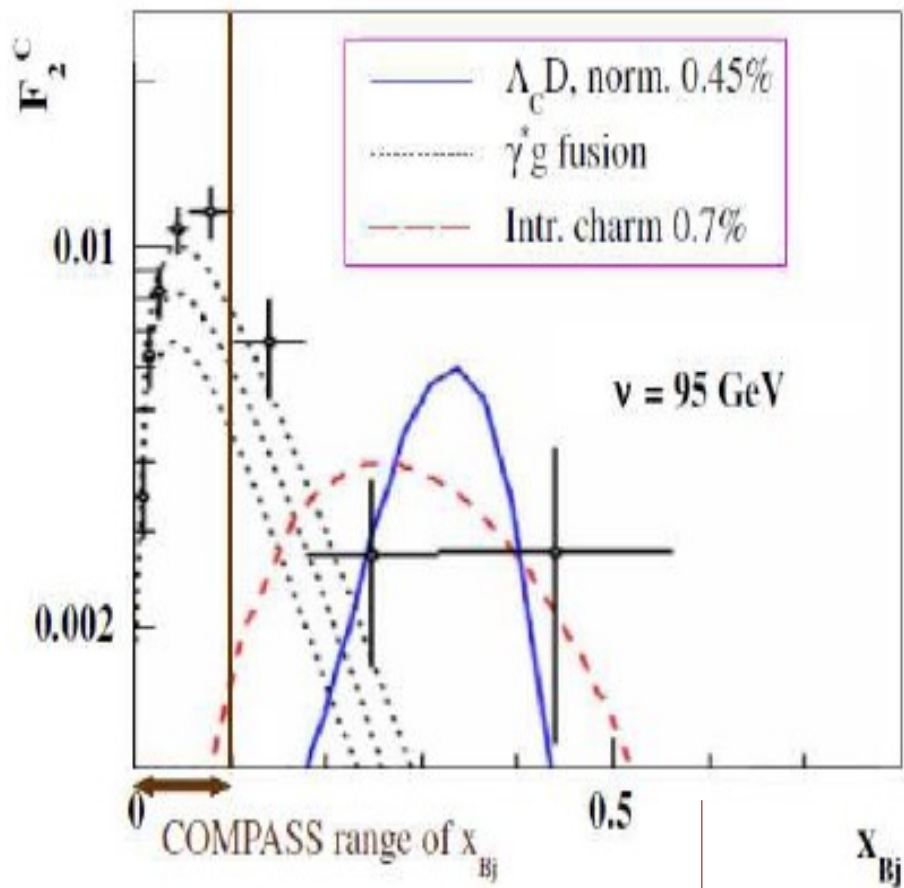


$\sigma(D^{*\pm}) = 1.8 \pm 0.4 \text{ nb}$   
 within  $20 \text{ GeV} < E_D < 80 \text{ GeV}$

# $D^{*+}/D^{*-}$ asymmetry:

$$A(X) = \frac{d\sigma^{D^{*+}}(X) - d\sigma^{D^{*-}}(X)}{d\sigma^{D^{*+}}(X) + d\sigma^{D^{*-}}(X)}$$





Ref. [Hep-ph/0508126](#) and [hep-ph/9508403](#)  
[Phys. Lett. B93 \(1980\) 451](#)  
 Data from EMC: [Nucl. Phys. B213, 31\(1983\)](#)



