

TMD measurements at COMPASS

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on behalf of the **COMPASS** collaboration

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Outline

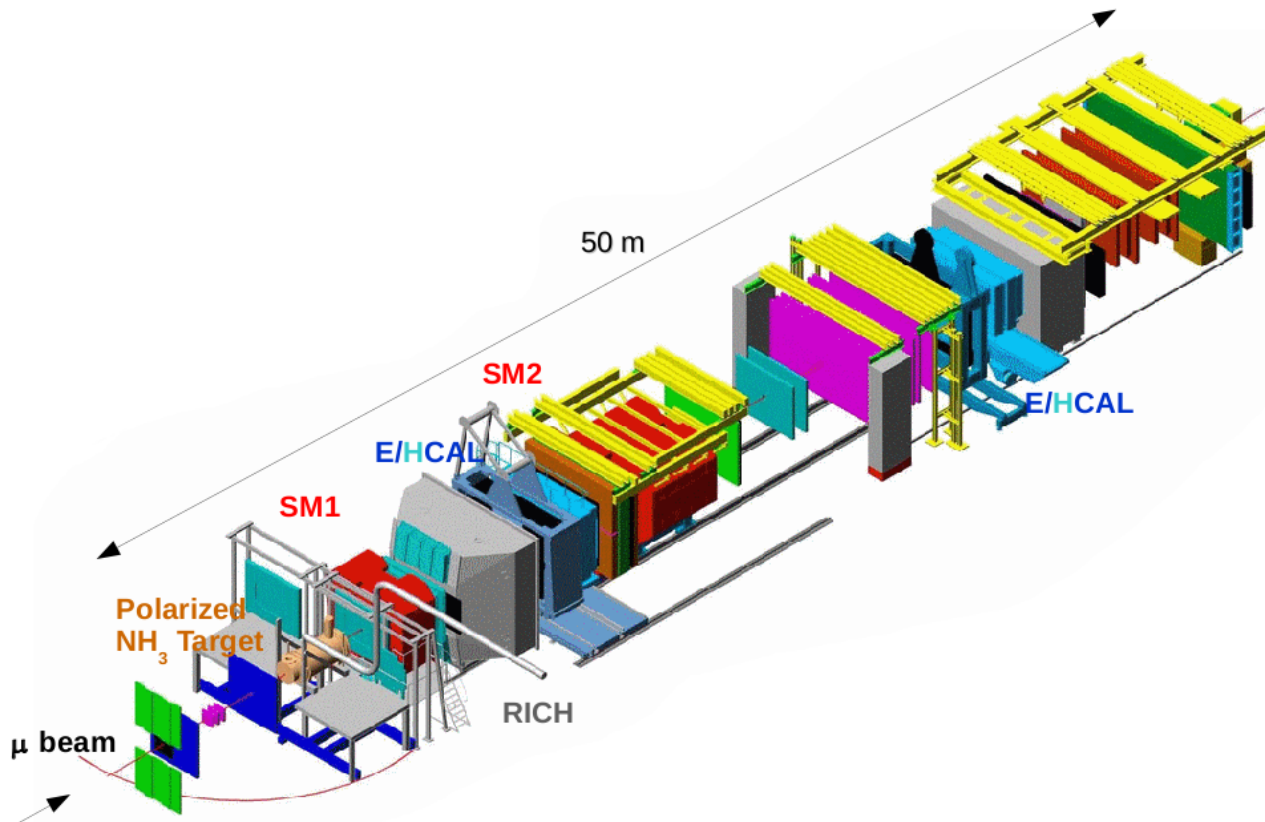
- 1 The COMPASS experiment
- 2 Theoretical framework
- 3 Data selection
- 4 Collins and Sivers asymmetries
- 5 The $+6$ transverse spin asymmetries
- 6 Unpolarized azimuthal asymmetries
- 7 Dihadron asymmetry
- 8 Conclusions & outlook

The COMPASS experiment

The COMPASS experiment ► at CERN



The COMPASS experiment ► spectrometer & lepton beam



e.g.

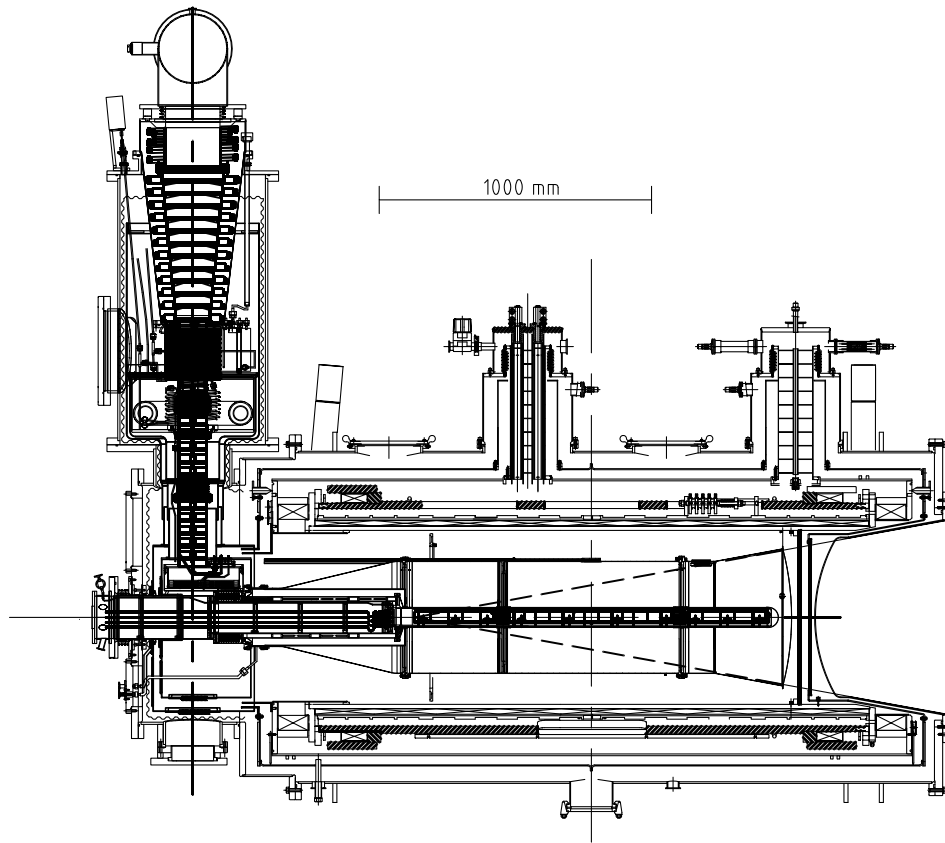
COMPASS setup 2007

- Two stage spectrometer
- Longitudinally polarized μ^+ -beam
- 2002-04 transversely polarized deuteron (^6LiD) target
- 2007/10 transversely polarized proton (NH_3) target
- 2011 longitudinally polarized proton (NH_3) target

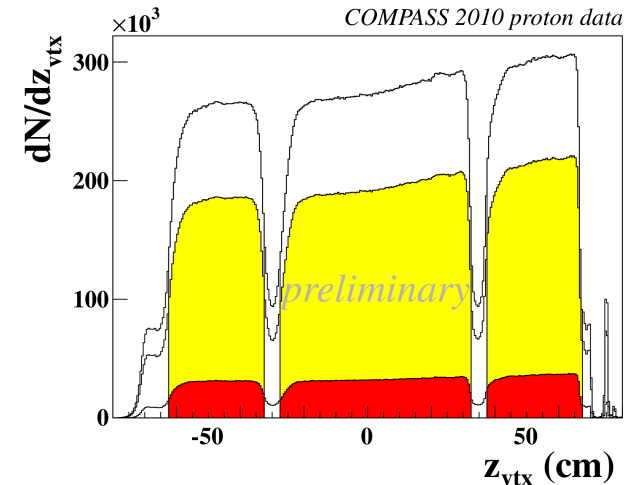
- $p_{\text{beam}} 2007/10$
160 GeV/c
- Intensity per spill
 $3.5 \cdot 10^8 \mu^+$
- Luminosity
 $5 \cdot 10^{32} \text{cm}^{-2} \text{s}^{-1}$
- polarization
 $\lambda \approx 80 \%$

- Tracking
- Calorimetry
- PID (RICH)

The COMPASS experiment ► polarized target system



- Upgrade of target system in 2005
- Three cells with opposite polarization
- ± 180 mrad geometrical acceptance
- Transverse polarization reversed every week via microwave



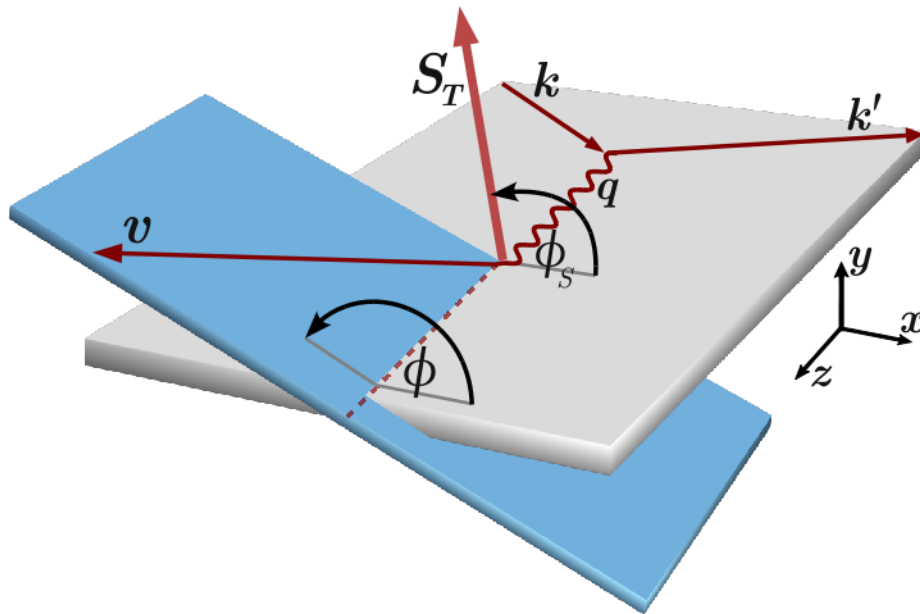
- proton (NH_3):
 - polarization $P_T \approx 90\%$
 - dilution factor $f \approx 16\%$
- deuteron (${}^6\text{LiD}$):
 - $P_T \approx 50\%$
 - $f \approx 40\%$

Theoretical framework

Theoretical framework ► single hadron reaction scheme

$$l p^\uparrow \rightarrow l' h$$

Fragmentation of a transversely polarized quark into one unpolarized hadron


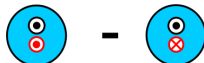



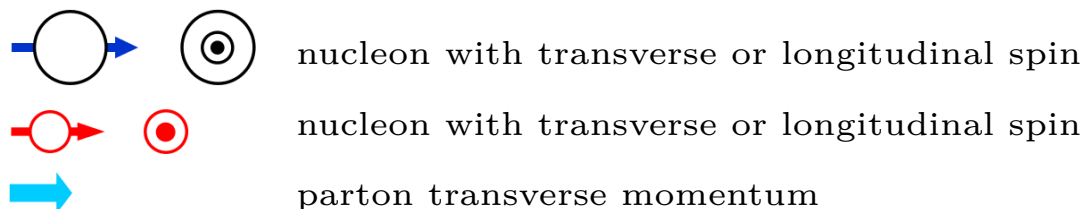
- k, k' and q are 4-momenta of incoming l , scattered lepton l' and virtual photon γ^*
- P is the 4-momenta of the scattered nucleon
- Φ_S azimuthal angle of the spin of the fragmenting quark S_T
- Φ_h azimuthal angle of the lepton scattering plane *w.r.t.* the lepton plane
- $Q^2 = -q^2$
- $W = \sqrt{(P + q)^2}$
- $x = \frac{Q^2}{2P \cdot q}$
- $y = \frac{P \cdot q}{p \cdot k} \Big|_{\text{lab}} = \frac{E - E'}{E}$
- $z = \frac{P \cdot p}{P \cdot q} \Big|_{\text{lab}} = \frac{E_h}{E - E'}$

in courtesy of H. Wollny

Theoretical framework ► from spin structure to Transversity

3 independent parton distribution functions (PDFs) are necessary to describe the spin structure of the nucleon in leading order in the collinear case:

nucleon	quark		
	U	L	T
U	$f_1^q(x)$ 		
L		$g_1^q(x)$ 	
T			$h_1^q(x)$ 



Proton goes out of the screen.
Photon goes into the screen.

Quark distribution:
 $f_1^q(x) = q^+(x) + q^-(x)$

Helicity distribution:
 $g_1^q(x) = q^+(x) - q^-(x)$





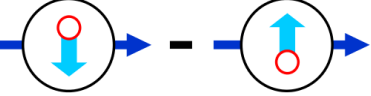
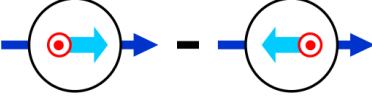
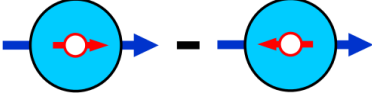
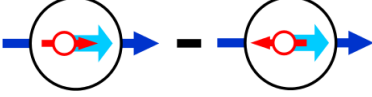
Transversity distribution:
 $h_1^q(x) = q^{\uparrow\uparrow}(x) - q^{\uparrow\downarrow}(x)$

Collins FF: $lN^\uparrow \rightarrow l'h$
Interference FF: $lN^\uparrow \rightarrow l'hh$
 Λ FF: $lN^\uparrow \rightarrow l'\Lambda$

in courtesy of B. Parsamyan

Theoretical framework ► from spin structure to Transversity

Taking into account the quark intrinsic transverse momentum k_T , at leading order in total 8 TMD PDFs are needed for a full description of the nucleon structure:

nucleon	quark		
	U	L	T
U	quark dstrbtn $f_1^q(x)$ 		$h_1^{\perp q}$ Boer-Mulders 
L		Helicity $g_1^q(x)$ 	$h_{1L}^{\perp q}$ Worm-gear L 
T	$f_{1T}^{\perp q}$ Sivers 	g_{1T}^q Worm-gear T 	$h_1^q(x)$ Transversity  $h_{1T}^{\perp q}$ Pretzelosity 

Theoretical framework ► SIDIS cross-section

$$\begin{aligned}
 \frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\psi} &= \left[\frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \right] \times \left(F_{UU,T} + \varepsilon F_{UU,L} \right) \times \left(\right. \\
 &S_L \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_h A_{UL}^{\sin \phi_h} + \varepsilon \sin(2\phi_h) A_{UL}^{\sin 2\phi_h} \right] + \\
 &S_L \lambda \left[\sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_h A_{LL}^{\cos \phi_h} \right] + \text{see talk by M. Stolarski} \\
 &1 + \cos \phi_h \times \sqrt{1\varepsilon(1+\varepsilon)} A_{UU}^{\cos \phi_h} + \cos(2\phi_h) \times \varepsilon A_{UU}^{\cos(2\phi_h)} + \lambda \sin \phi_h \times \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin \phi_h} + \\
 &S_T \left[\right. \\
 &\sin \phi_S \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin \phi_S}) \\
 &\sin(\phi_h - \phi_S) \times (A_{UT}^{\sin(\phi_h - \phi_S)}) \\
 &\sin(\phi_h + \phi_S) \times (\varepsilon A_{UT}^{\sin(\phi_h + \phi_S)}) \\
 &\sin(2\phi_h - \phi_S) \times (\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h - \phi_S)}) \\
 &\sin(3\phi_h - \phi_S) \times (\varepsilon A_{UT}^{\sin(3\phi_h - \phi_S)}) \\
 &\left. \right] + S_T \lambda \left[\right. \\
 &\cos \phi_S \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos \phi_S}) \\
 &\cos(\phi_h - \phi_S) \times (\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_S)}) \\
 &\cos(2\phi_h - \phi_S) \times (\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h - \phi_S)}) \\
 &\left. \right] \left. \right)
 \end{aligned}$$

Twits-2 ;
Twist-2 + k_T/Q kinematical
corrections

$$A_{U(L),T}^{\omega(\phi_h, \phi_S)} = \frac{F_{U(L),T}^{\omega(\phi_h, \phi_S)}}{F_{UU,T} + \varepsilon F_{UU,L}}$$

$$\varepsilon = \frac{1-y-\frac{1}{4}\gamma^2 y^2}{1-y+\frac{1}{2}y^2+\frac{1}{4}\gamma^2 y^2}, \quad \gamma = \frac{2Mx}{Q}$$

Kotzinian, Nucl. Phys. B441, 234 (1995)

Bacchetta, Diehl, Goeke, Metz, Mulders and Schlegel, JHEP (2007) 0702:093

Theoretical framework ► Interpretation of the asymmetries

Within QCD parton model $A_i \propto \mathbf{DF} \otimes \mathbf{FF}$ with $i = 1, \dots, 11$

Twist-2

unpolarized

$$A_{UU}^{\cos \phi_h} \propto f_1^q \otimes D_{1q}^h + h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

$$A_{UU}^{\cos 2\phi_h} \propto f_1^q \otimes D_{1q}^h + h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

single spin

$$A_{UT}^{\sin(\phi_h + \phi_S)} \propto h_1^q \otimes H_{1q}^{\perp h}$$

$$A_{UT}^{\sin(\phi_h - \phi_S)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$

$$A_{UT}^{\sin(3\phi_h - \phi_S)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

double spin

$$A_{LT}^{\cos(\phi_h - \phi_S)} \propto g_{1T}^q \otimes D_{1q}^h$$

Twist-2 + k_T/Q kinematical corrections

unpolarized

$$A_{LU}^{\sin \phi_h}$$

single spin

$$A_{UT}^{\sin \phi_S} \propto \frac{M}{Q} (h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h)$$

$$A_{UT}^{\sin(2\phi_h - \phi_S)} \propto \frac{M}{Q} (h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h)$$

double spin

$$A_{LT}^{\cos \phi_S} \propto \frac{M}{Q} g_{1T}^q \otimes D_{1q}^h$$

$$A_{LT}^{\cos(2\phi_h - \phi_S)} \propto \frac{M}{Q} g_{1T}^q \otimes D_{1q}^h$$

Theoretical framework ► From raw to physics asymmetries

$$A_{UU}^{\omega(\phi_h, \phi_S)} = \frac{A_{UU, raw}^{\omega(\phi_h, \phi_S)}}{D^{\omega(\phi_h, \phi_S)}(y)} ; A_{LU}^{\omega(\phi_h, \phi_S)} = \frac{A_{LU, raw}^{\omega(\phi_h, \phi_S)}}{D^{\omega(\phi_h, \phi_S)}(y)\lambda}$$

$$A_{UT}^{\omega(\phi_h, \phi_S)} = \frac{A_{UT, raw}^{\omega(\phi_h, \phi_S)}}{D^{\omega(\phi_h, \phi_S)}(y)f|P_T|} ; A_{LT}^{\omega(\phi_h, \phi_S)} = \frac{A_{LT, raw}^{\omega(\phi_h, \phi_S)}}{D^{\omega(\phi_h, \phi_S)}(y)f\lambda|P_T|}$$

$$D^{\sin(\phi_h - \phi_S)}(y) = 1$$

$$D^{\cos(2\phi_h)}(y) = D^{\sin(\phi_h + \phi_S)}(y) = D^{\sin(3\phi_h - \phi_S)}(y) = \varepsilon \approx \frac{2(1-y)}{1+(1-y)^2}$$

$$D^{\cos(\phi_h - \phi_S)}(y) = \sqrt{1 - \varepsilon^2} \approx \frac{y(2-y)}{1+(1-y)^2}$$

$$D^{\cos(\phi_h)}(y) = D^{\sin(2\phi_h - \phi_S)}(y) = D^{\sin(\phi_S)}(y) = \sqrt{2\varepsilon(1 + \varepsilon)} \approx \frac{2(2-y)\sqrt{1-y}}{1+(1-y)^2}$$

$$D^{\sin(\phi_h)}(y) = D^{\cos(2\phi_h - \phi_S)}(y) = D^{\cos(\phi_S)}(y) = \sqrt{2\varepsilon(1 - \varepsilon)} \approx \frac{2y\sqrt{1-y}}{1+(1-y)^2}$$

$D^{\omega_i(\phi_h, \phi_S)}$ = depolarization factor

f = target dilution factor

P_T = target polarization

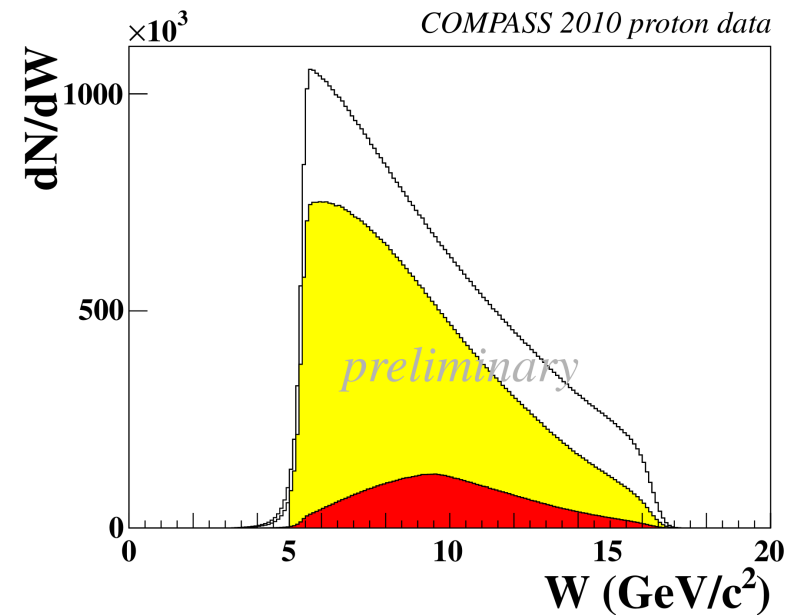
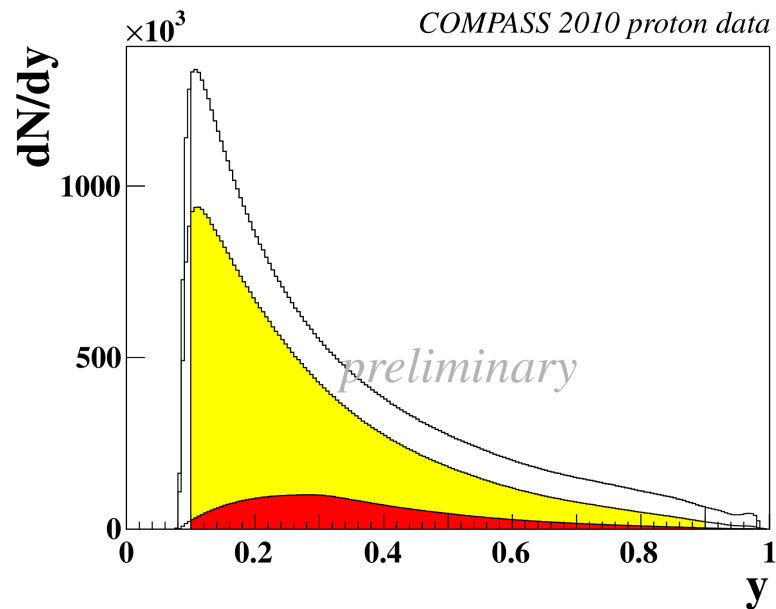
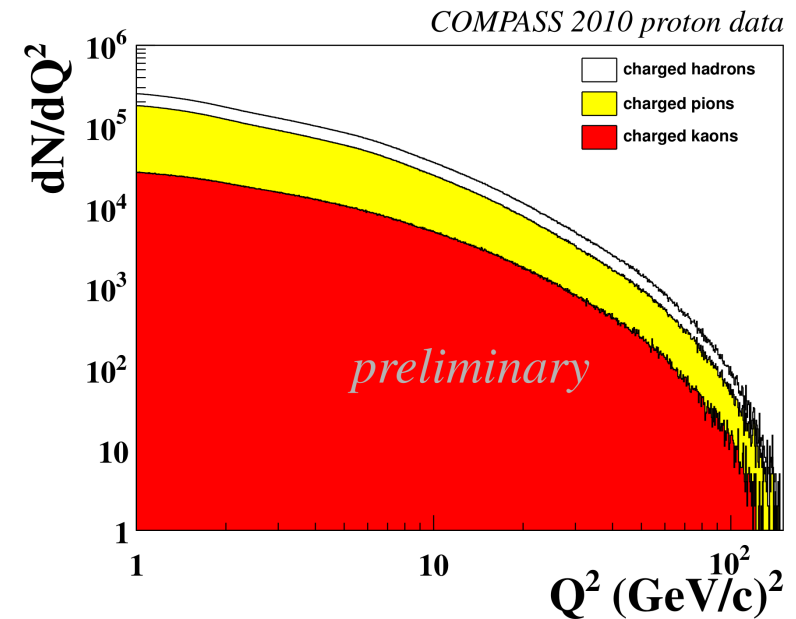
λ = beam polarization

Data selection

Data selection ► DIS cuts

DIS cuts on events:

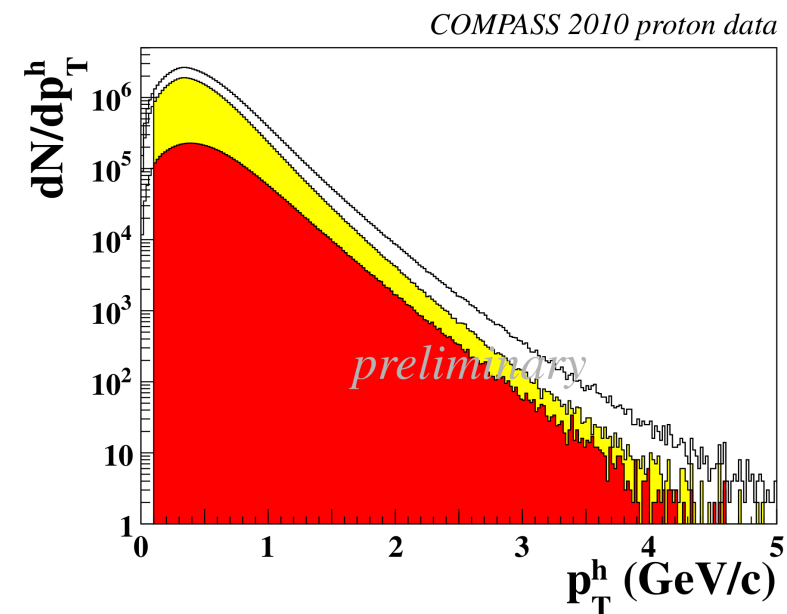
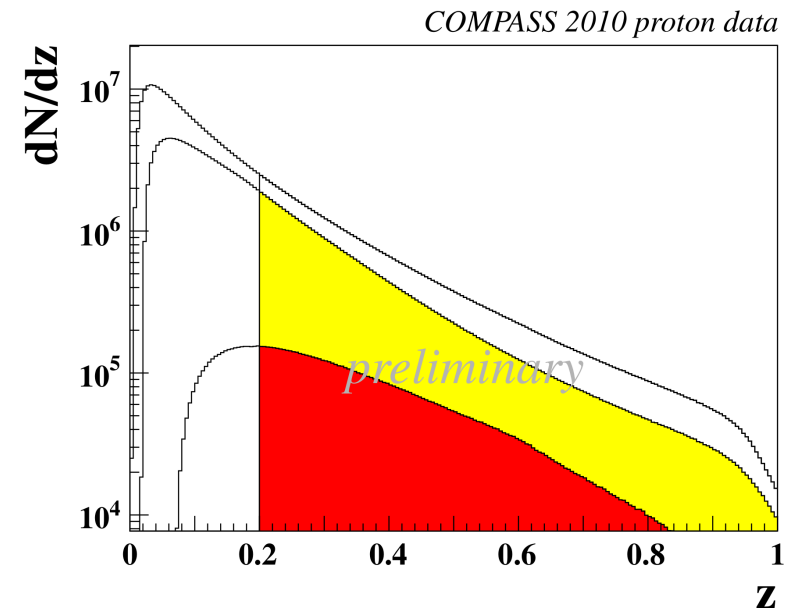
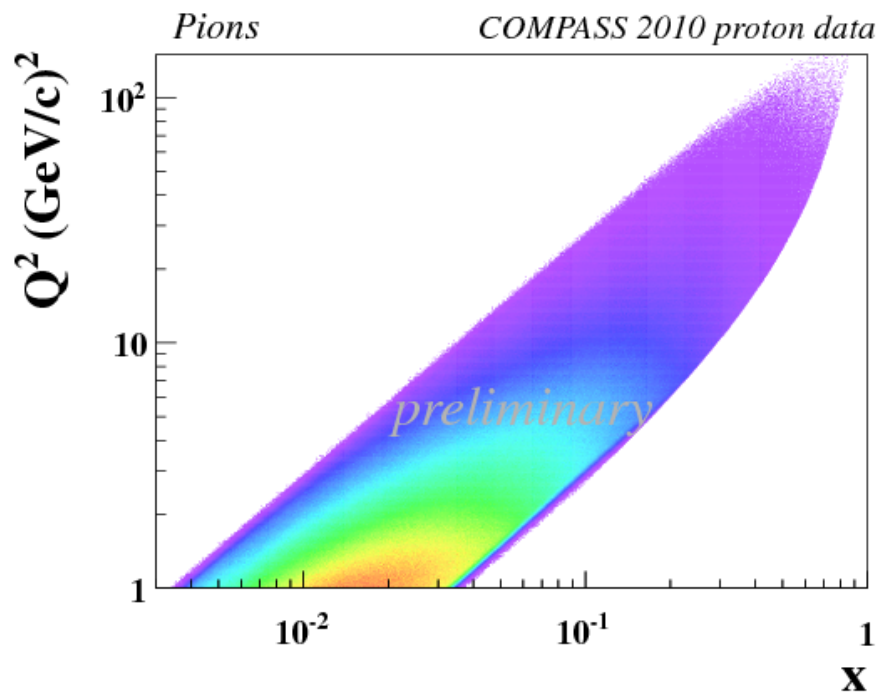
- $Q^2 > 1 \text{ (GeV/c)}^2$
- $0.1 < y < 0.9$
- $W > 5 \text{ GeV/c}^2$
- spectrometer acceptance:
 $0.003 < x < 0.7$



Data selection ► single hadron cuts

single hadron cuts:

- $z > 0.2$ for A_{UT} analysis
- $0.2 > z > 0.85$ for $A_{UU/LU}$ analysis
- $p_T > 0.1$ GeV/c



Data selection ► COMPASS TMD data

⇒ For the first time the recent COMPASS results on TMDs were shown at **SPIN2010** in Dubna September 2012.

Asymmetries	hadrons/-pairs	target	year of data	by
Collins and Sivers	$\pi^{+/-}, K^{+/-}$	p	07/10	A. Martin
Other 6	$h^{+/-}$	d, p	02-04,07/10	B. Parsamyan
Unpolarized	$h^{+/-}$	d	04	G. Sbrizzai
Dihadron	$\pi^+ \pi^-, K^+ K^-$ $\pi^+ K^-, K^+ \pi^-$	p	10	C. Braun

Collins asymmetry

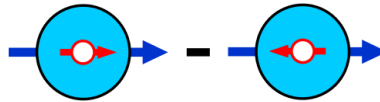
proton data 2010

Collins asymmetry ► charged hadrons ► 2010 data

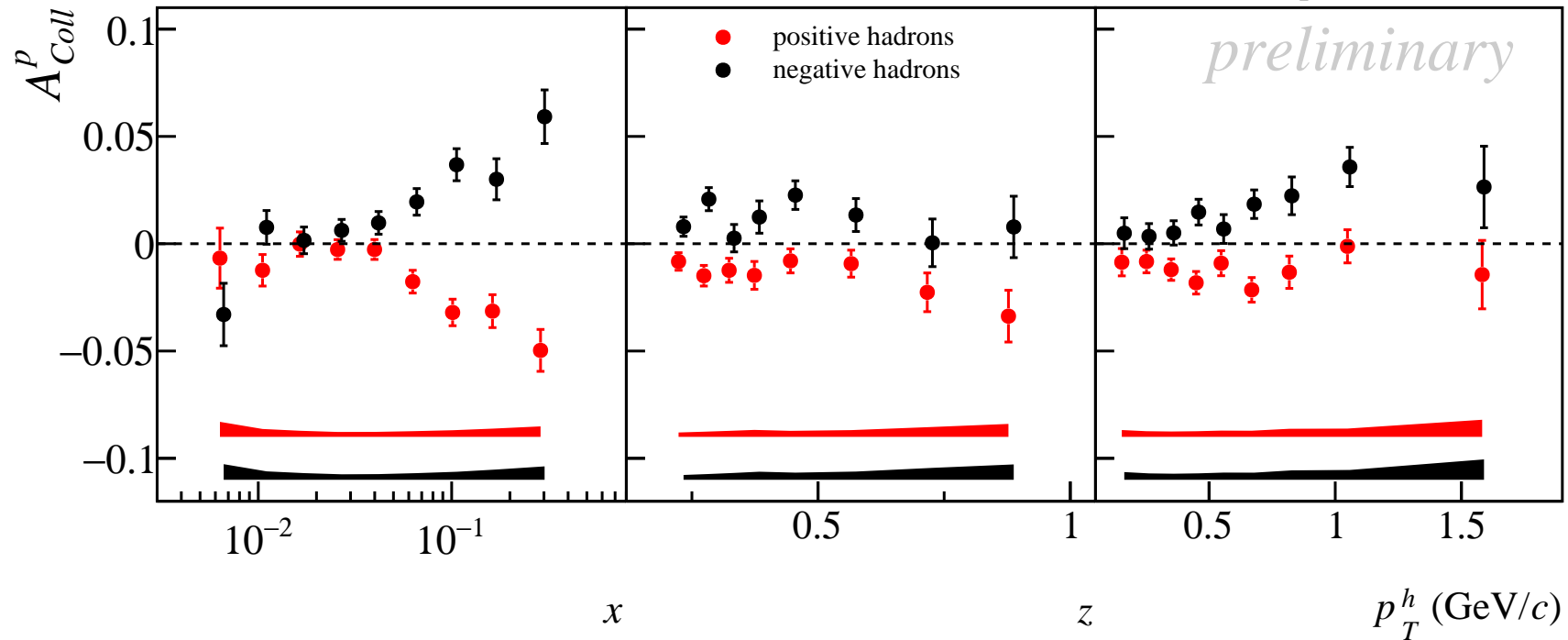
Twist-2

$$A_{UT}^{\sin(\phi_h + \phi_S)}$$

$$h_1^q(x)$$



COMPASS 2010 proton data



the COMPASS collaboration, C. Adolph *et al.*, Phys. Lett. B 717 (2012), 376-382

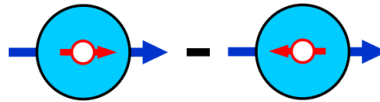
↪ very **precise** measurement of the Collins asymmetry of $h^{+/-}$
 ↪ clear signal

Collins asymmetry ► pions ► 2010 data

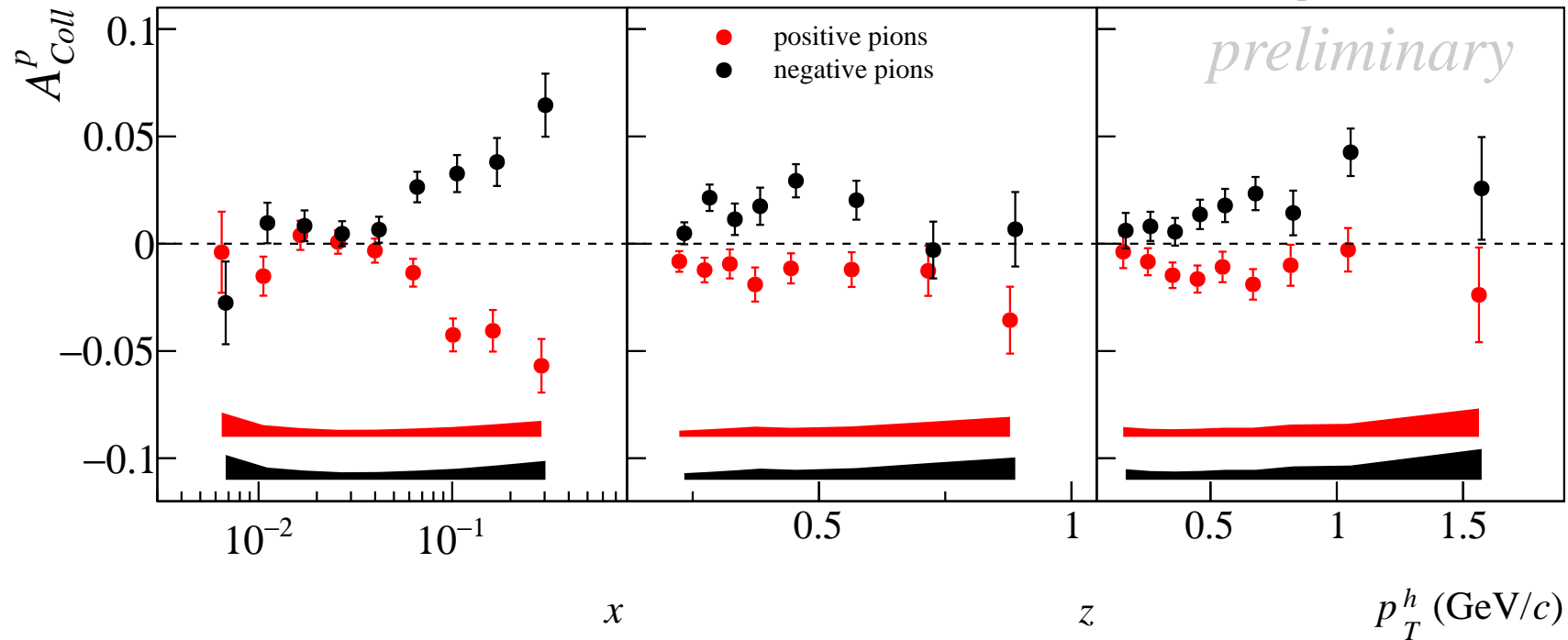
Twist-2

$$A_{UT}^{\sin(\phi_h + \phi_S)}$$

$$h_1^q(x)$$



COMPASS 2010 proton data



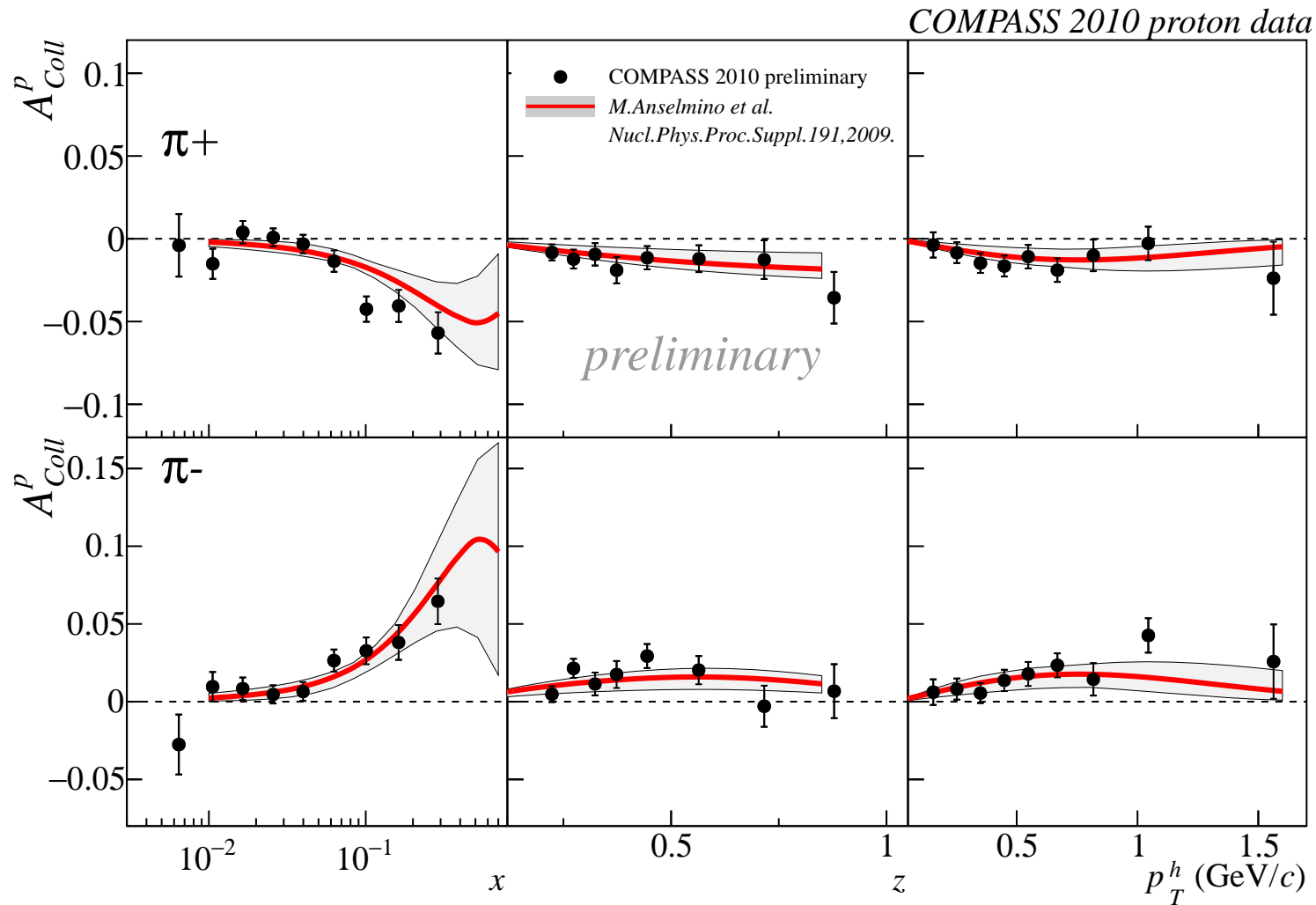
↳ Very **precise** measurement of Collins asymmetry of pions

↳ clear signal up to 7 %

↳ opposite signs for $\pi^{+/-}$ in x , z and p_T^h

↳ high statistics at small x are important for the extraction of the tensor charge

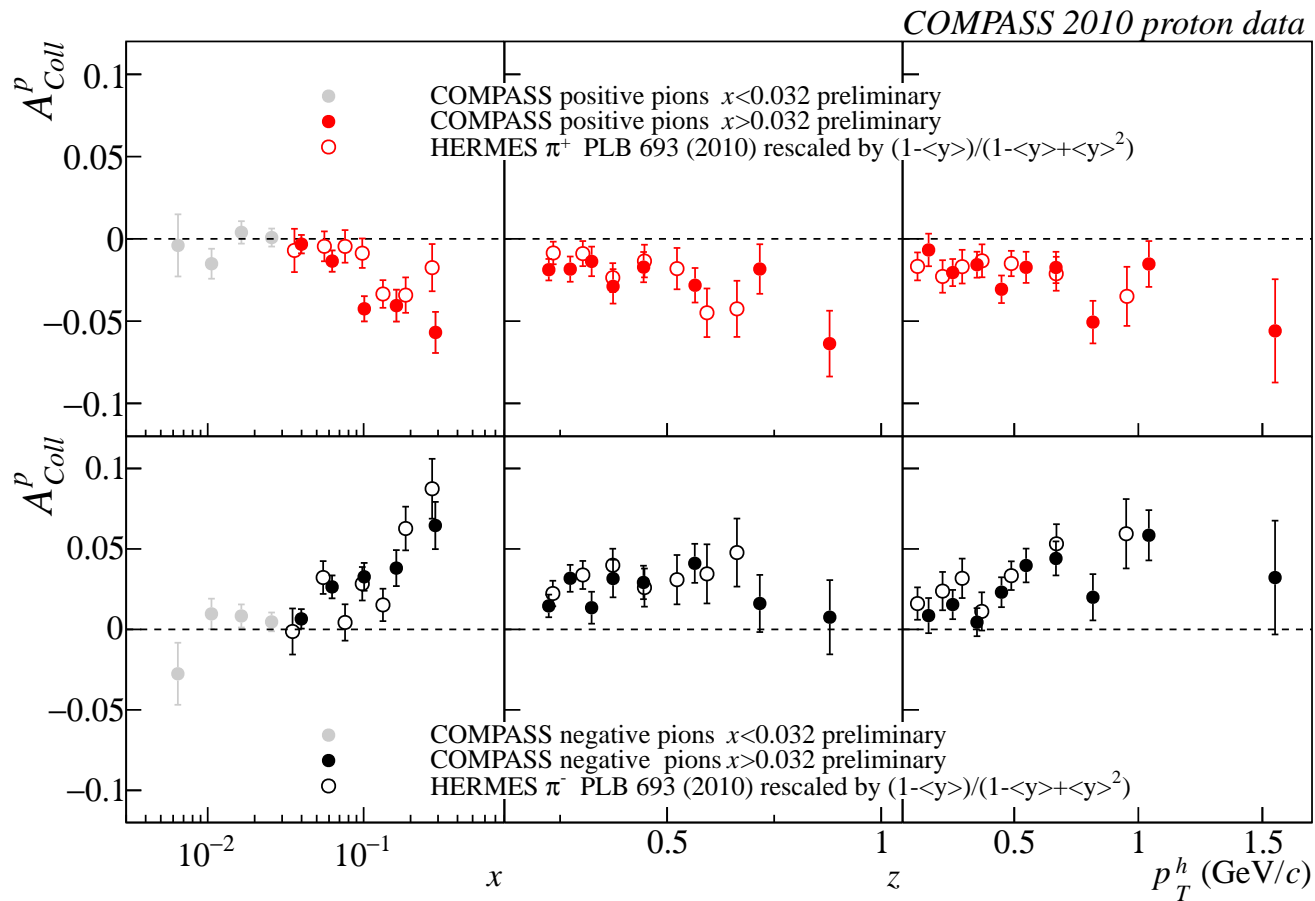
Collins asymmetry ► pions ► 2010 data *vs.* model predictions



↪ good agreement for x , z and p_T^h within the uncertainties

... but some more work to be done.

Collins asymmetry ► pions ► $x > 0.032$ and HERMES comp.



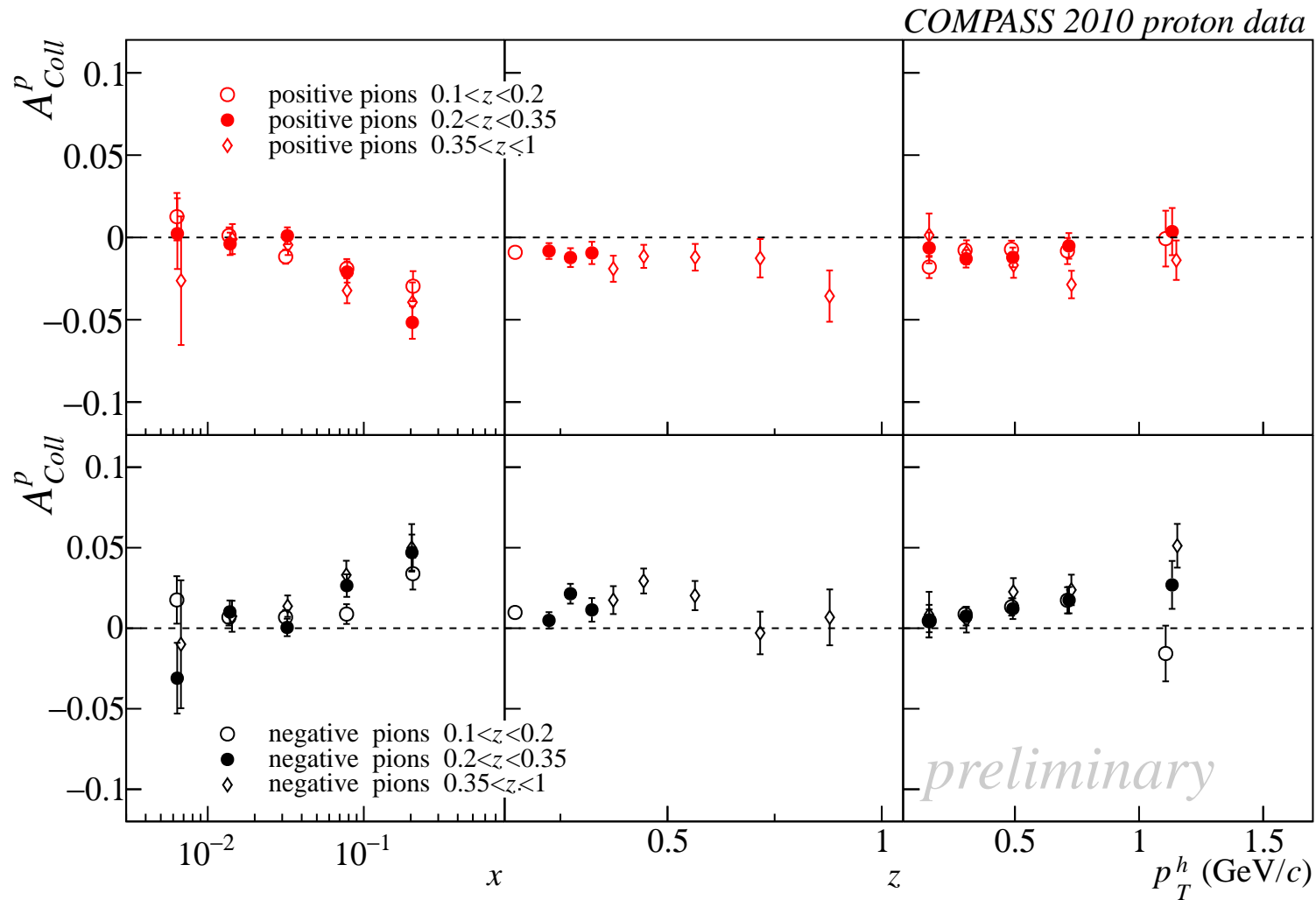
↪ Clearer dependence in z and p_T^h for $x > 0.032$

↪ Same strength of the signal within the uncertainties

but different $\langle Q^2 \rangle$ values of HERMES (≈ 4) and COMPASS (≈ 12)

⇒ Indication for non higher twist effect & no strong Q^2 dependence

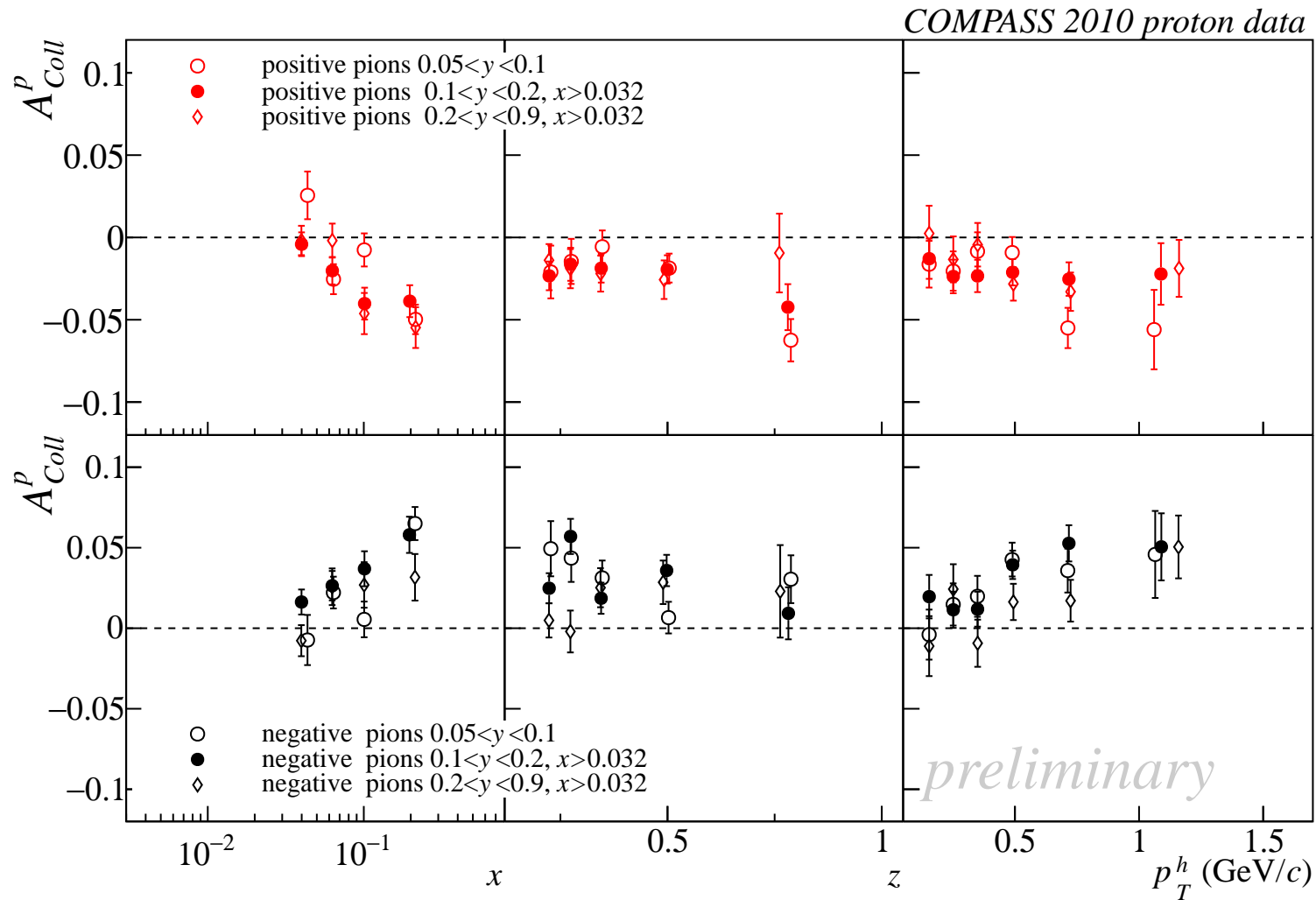
Collins asymmetry ► pions ► multi-dimensional analysis in z



3 z ranges: $0.1 < z_{\text{low}} < 0.2 < z_{\text{mid}} < 0.35 < z_{\text{high}} < 1.0$

↪ no clear dependence in x and p_T^h

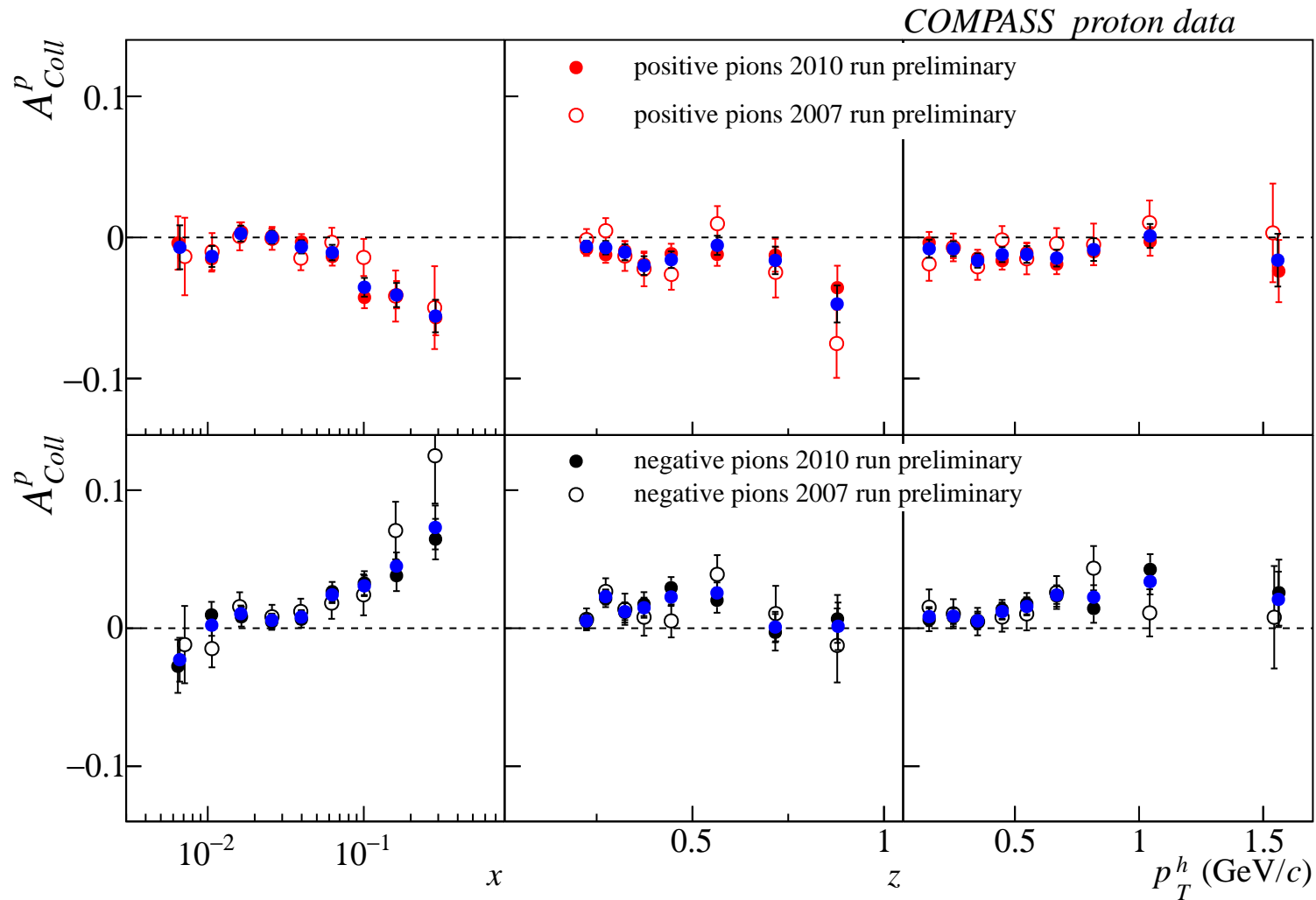
Collins asymmetry ► pions ► multi-dimensional analysis in y



3 y ranges: $0.05 < y_{\text{low}} < 0.1 < y_{\text{mid}} < 0.2 < y_{\text{high}} < 0.9$

↪ no clear dependence *w.r.t.* the uncertainties

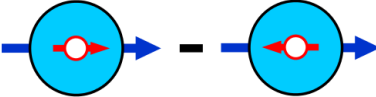
Collins asymmetry ► pions ► combined '07 and '10 data

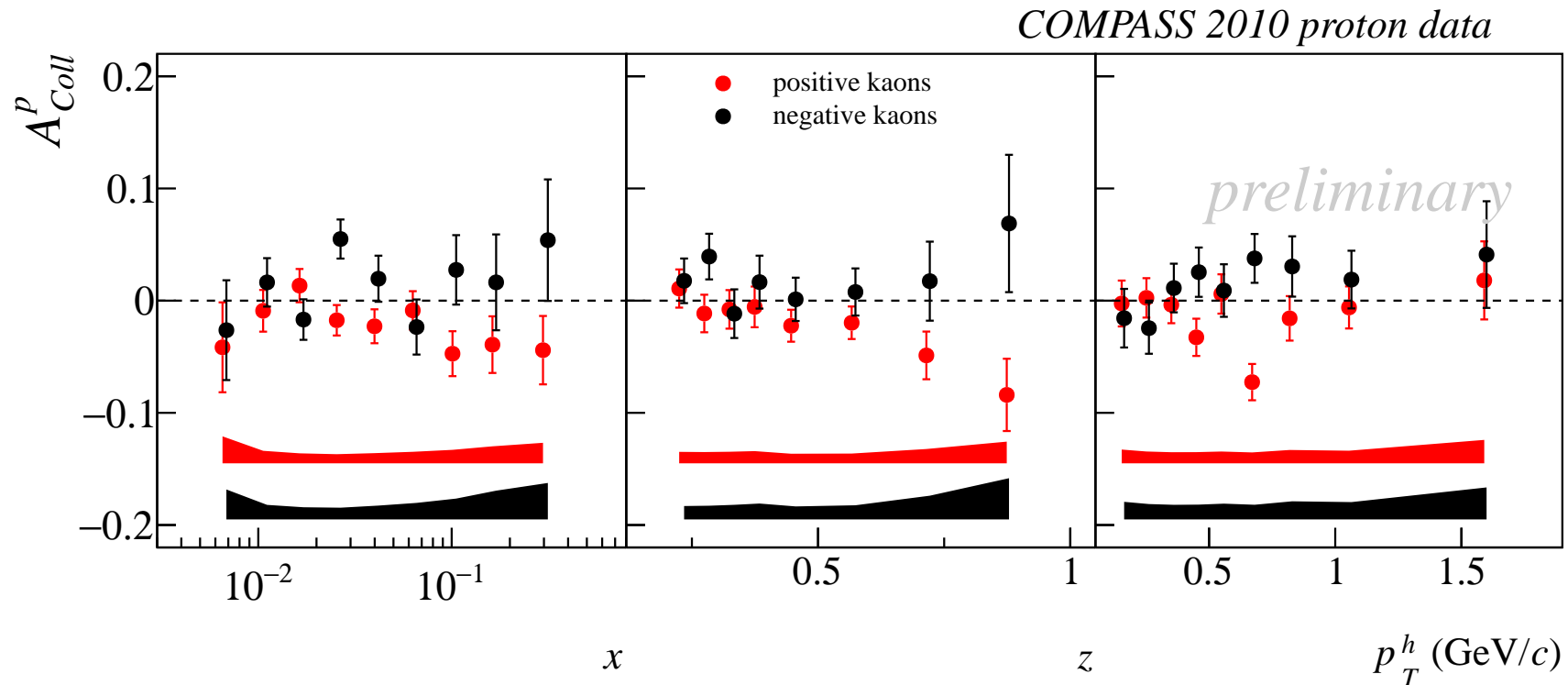


↪ '10 confirm '07 results with improved statistics

data combined by taking into account statistical and systematical uncertainties

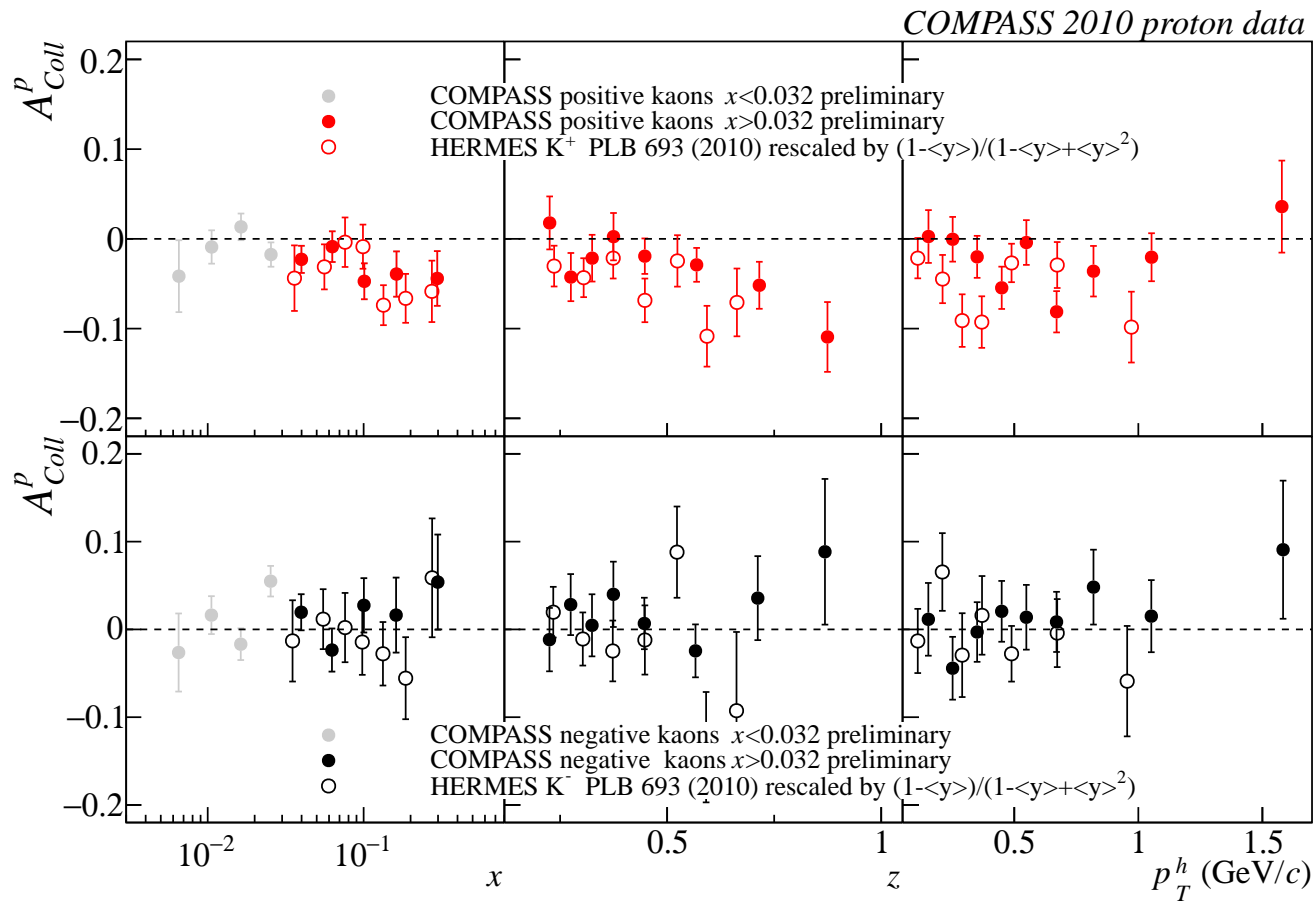
Collins asymmetry ► kaons ► 2010 data

Twist-2 $A_{UT}^{\sin(\phi_h + \phi_S)}$ $h_1^q(x)$ 



- ↳ different from zero
- ↳ indication of opposite signs for $K^{+/-}$ mean values
- ↳ indication for signal also at very small x

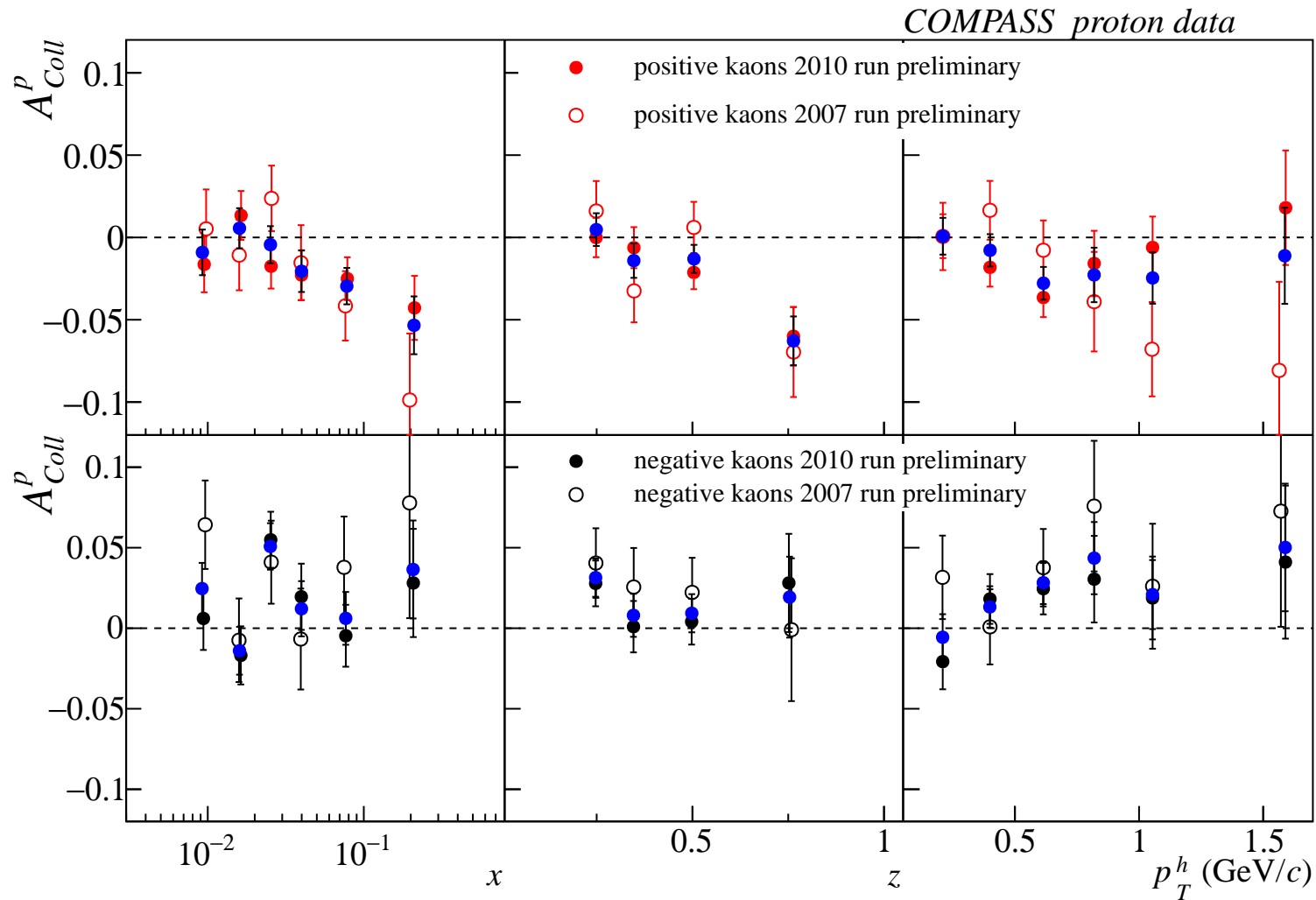
Collins asymmetry ► kaons ► $x > 0.032$ and HERMES comp.



↪ HERMES and COMPASS compatible within the uncertainties

HERMES asymmetries systematical larger for K^+ in x , z and p_T^h

Collins asymmetry ► kaons ► combined '07 and '10 data



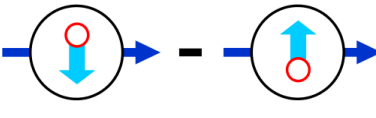
↪ '10 confirm '07 results with improved statistics

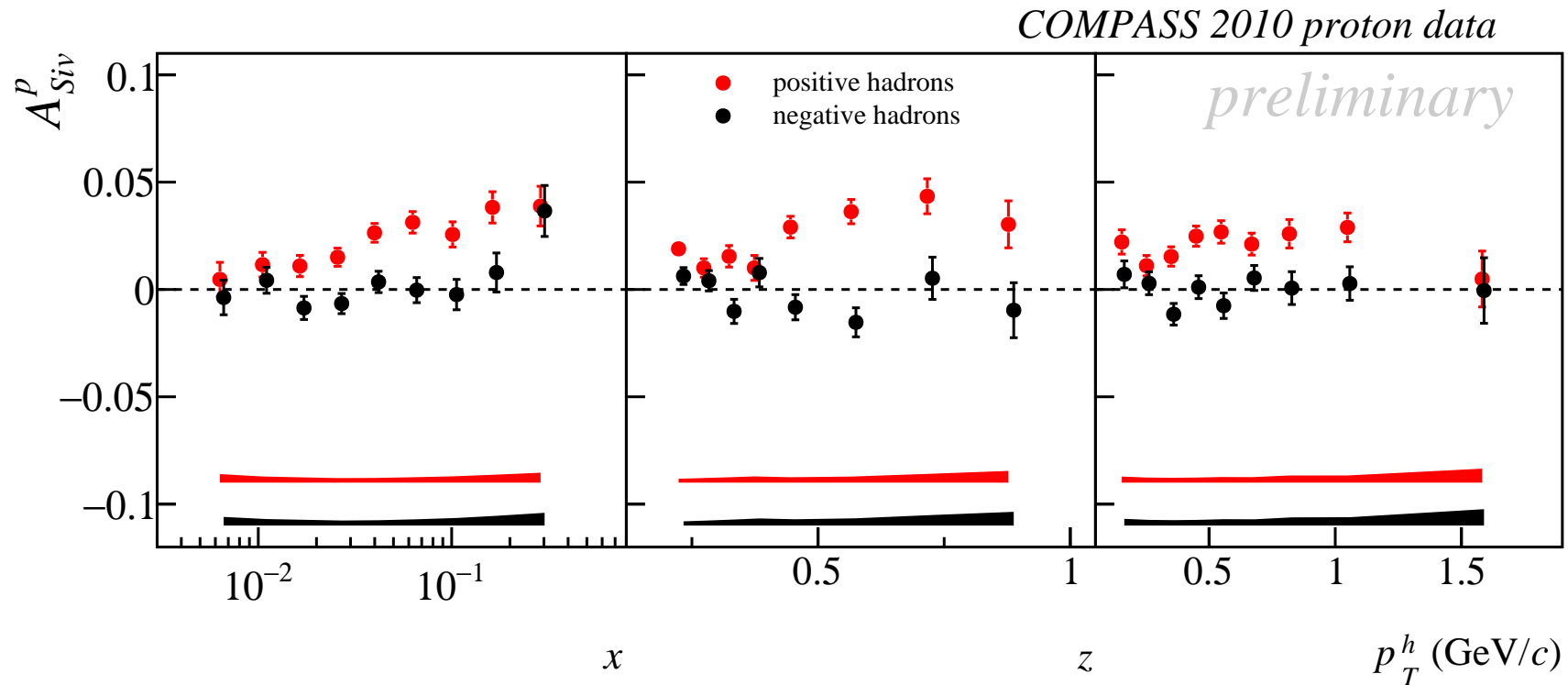
data combined by taking into account statistical and systematical uncertainties

Sivers asymmetry

proton data 2010

Sivers asymmetry ► charged hadrons ► 2010 data

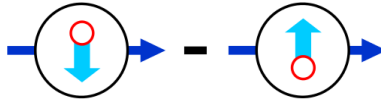
Twist-2 $A_{UT}^{\sin(\phi_h - \phi_S)}$ $f_{1T}^{\perp q}(x)$ 

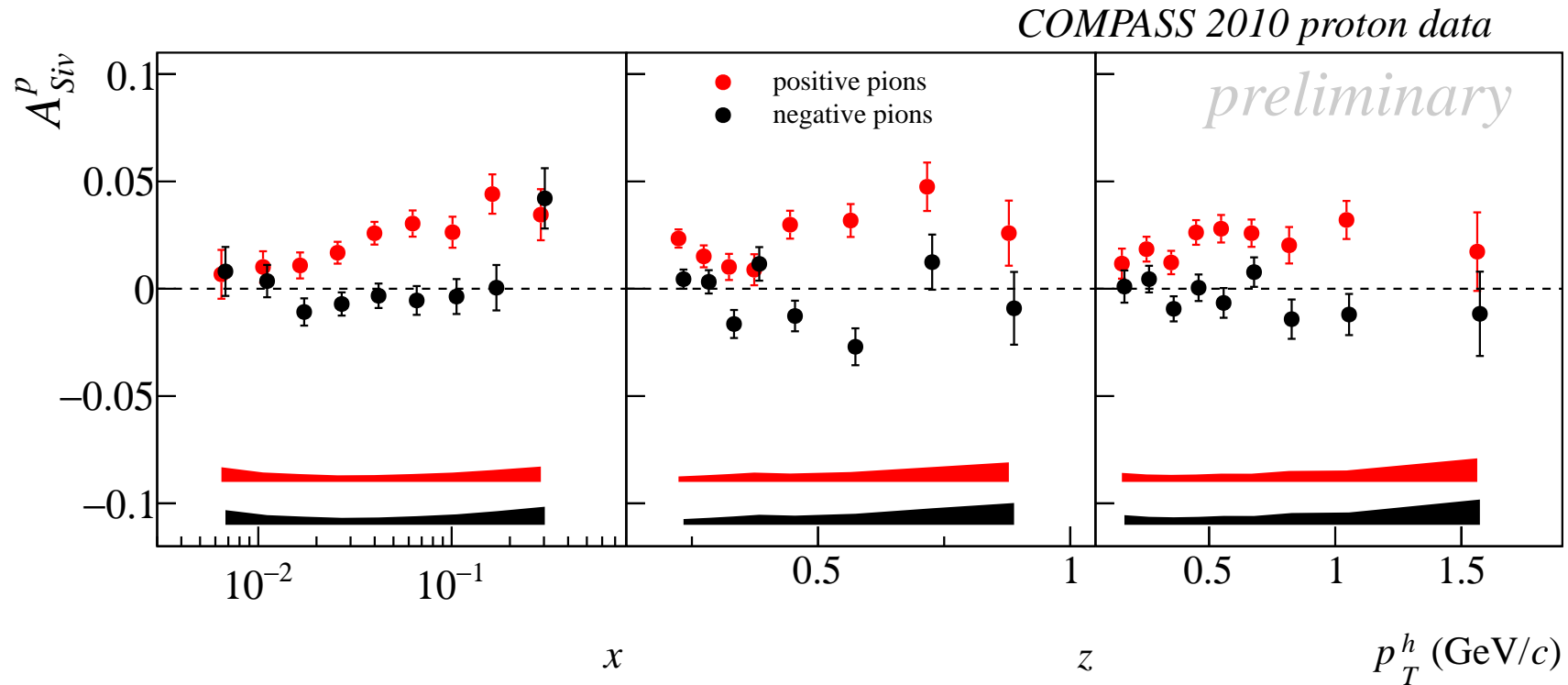


the COMPASS collaboration, C. Adolph *et al.*, Phys. Lett. B 717 (2012), 383-389

- ↪ very **precise** measurement of the Sivers asymmetry of $h^{+/-}$
- ↪ clear signal for positive hadrons

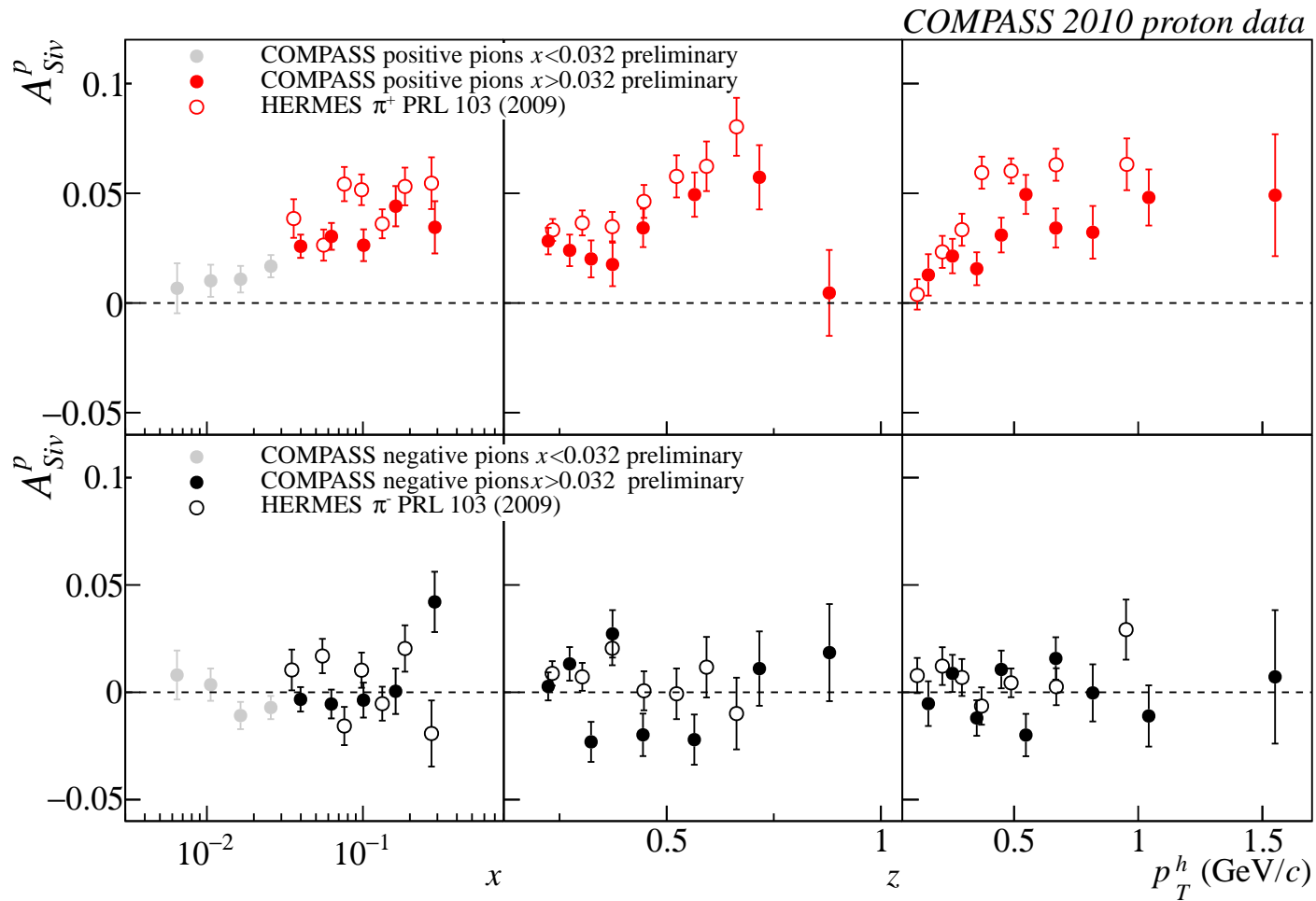
Sivers asymmetry ► pions ► 2010 data

Twist-2 $A_{UT}^{\sin(\phi_h - \phi_S)}$ $f_{1T}^{\perp q}(x)$ 



- ↪ π^+ : clear signal up to 5 % in x , z and p_T^h
- ↪ π^+ : signal also at very small x , as for h^+
- ↪ π^- : mostly compatible with zero within the uncertainties

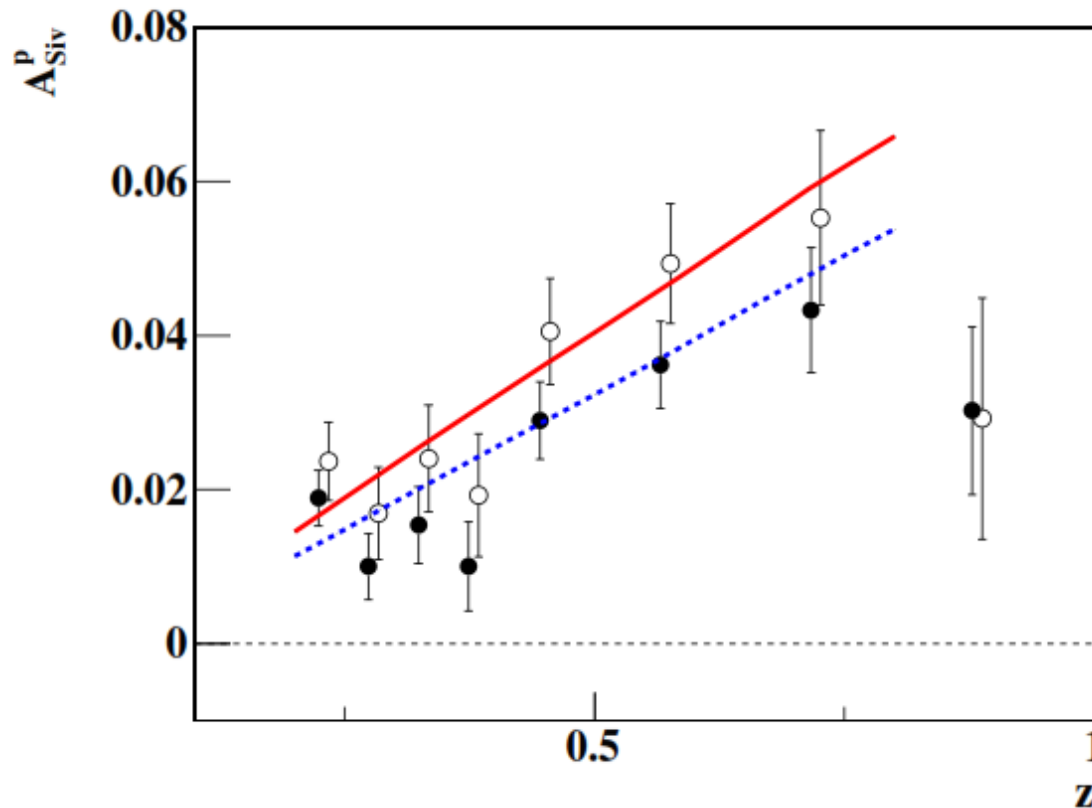
Sivers asymmetry ► pions ► $x > 0.032$ and HERMES comp.



↪ same trend for HERMES and COMPASS

HERMES asymmetries systematical larger for π^+ in x , z and p_T^h

Q^2 evolution ► charged hadrons ► model calculations *vs.*
COMPASS 2010 data



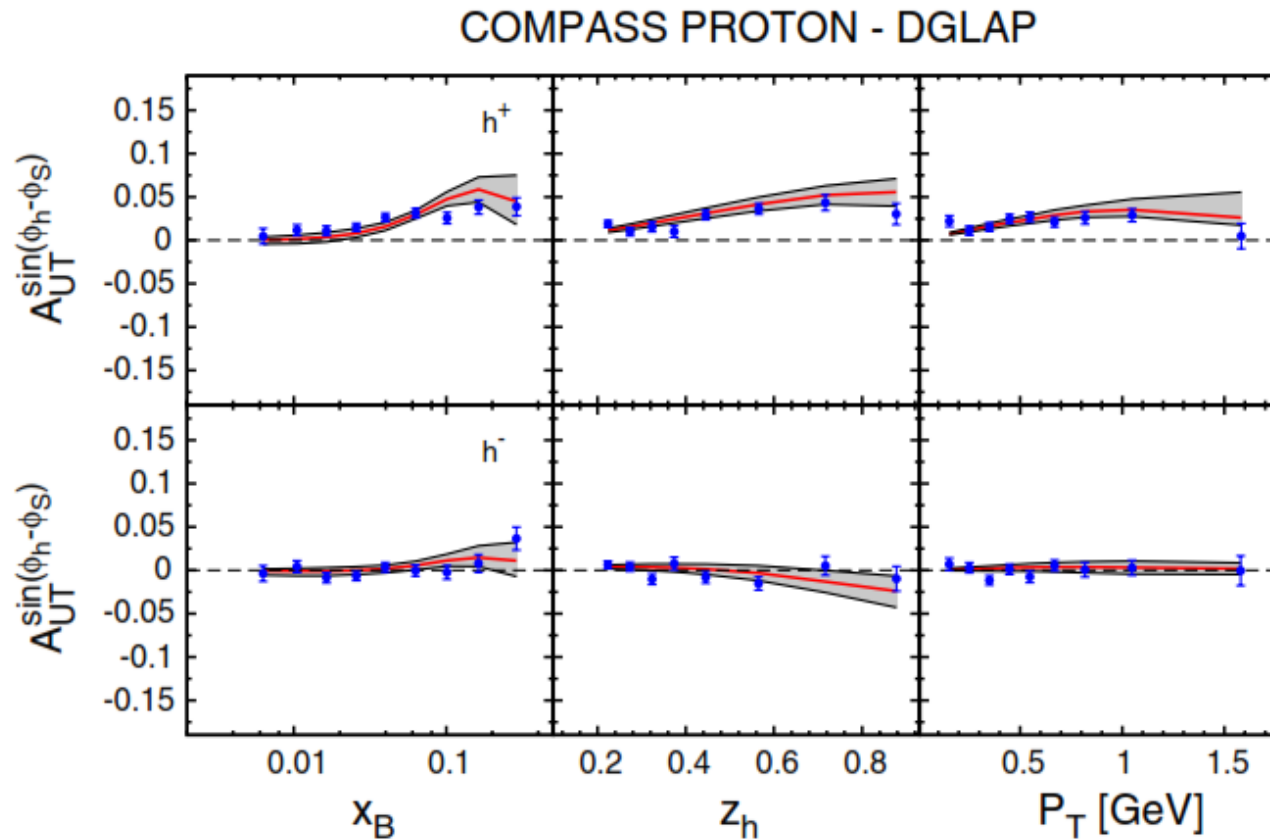
$x > 0.032 \Rightarrow$
 $\langle Q^2 \rangle = 8.7 \text{ GeV}/c^2$

full x range \Rightarrow
 $\langle Q^2 \rangle = 3.8 \text{ GeV}/c^2$

S. M. Aybat, A. Prokudin and T. C. Rogers, PRL 108 (2012) 242003

↪ good agreement between data and model calculations

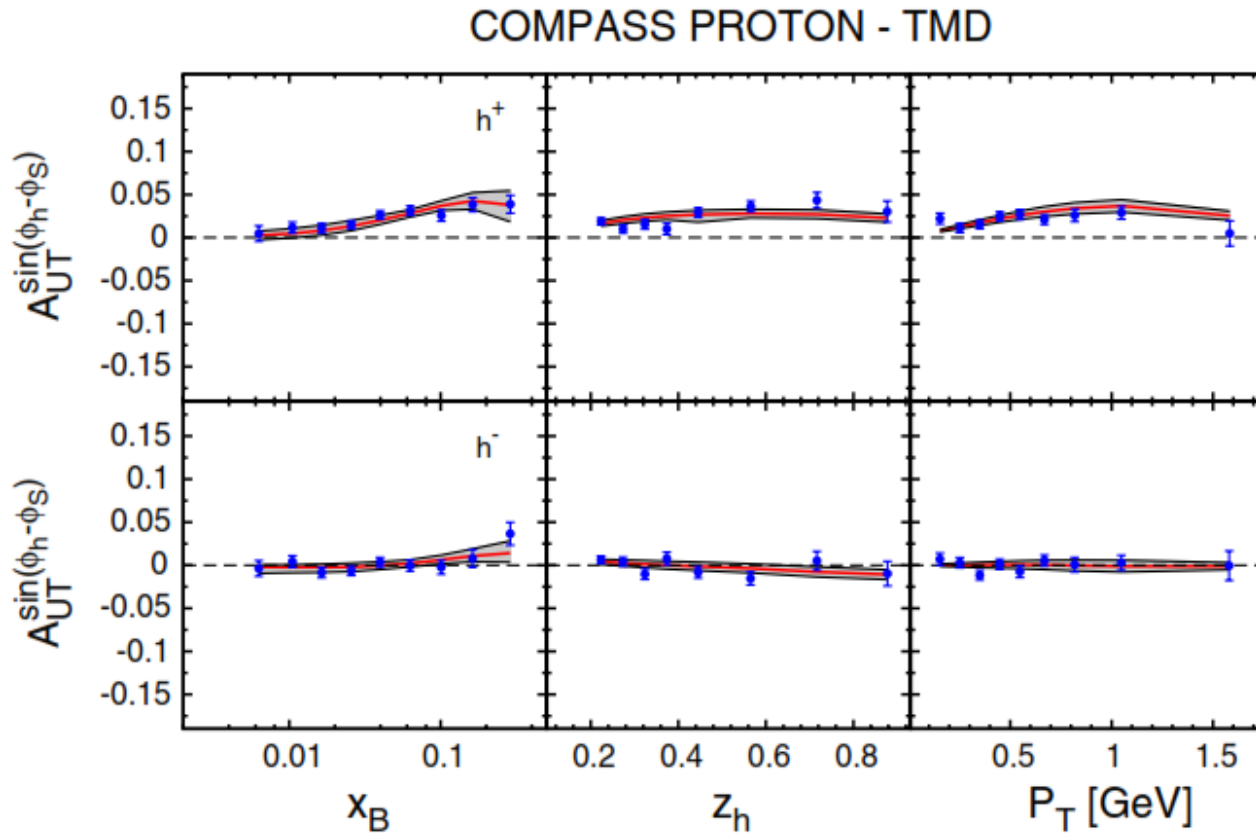
Q^2 evolution ► charged hadrons ► model calculations *vs.*
COMPASS 2010 data



M. Anselmino, M. Boglione and S. Melis, PRD86 (2012) 014028

- Calculated with a fit to HERMES p and COMPASS d and p 2010 data
- Evolution was calculated using the **DGLAP** equation

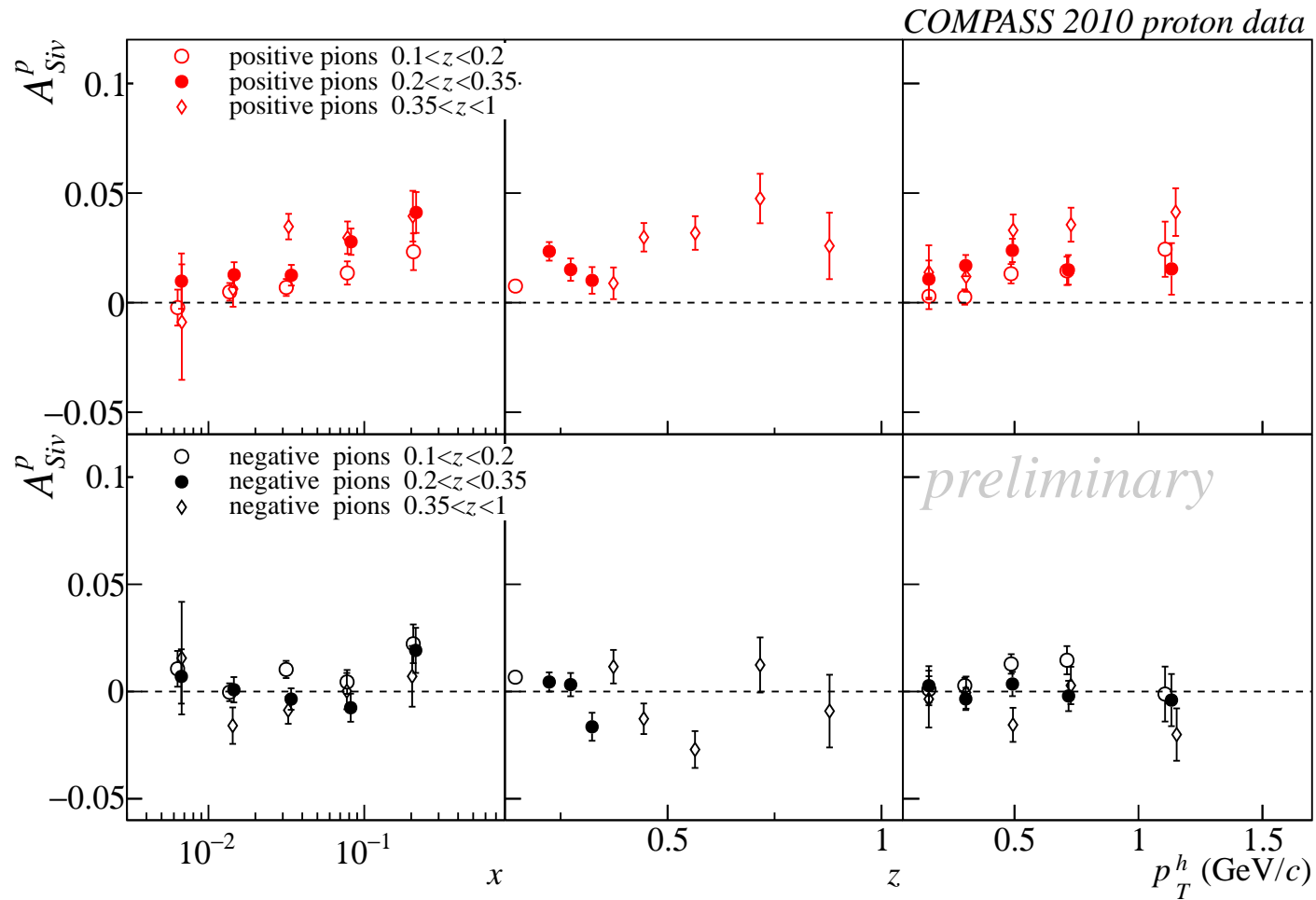
Q^2 evolution ► charged hadrons ► model calculations *vs.* COMPASS 2010 data



M. Anselmino, M. Boglione and S. Melis, PRD86 (2012) 014028

↪ better agreement between data and model calculations with Q^2 evolution

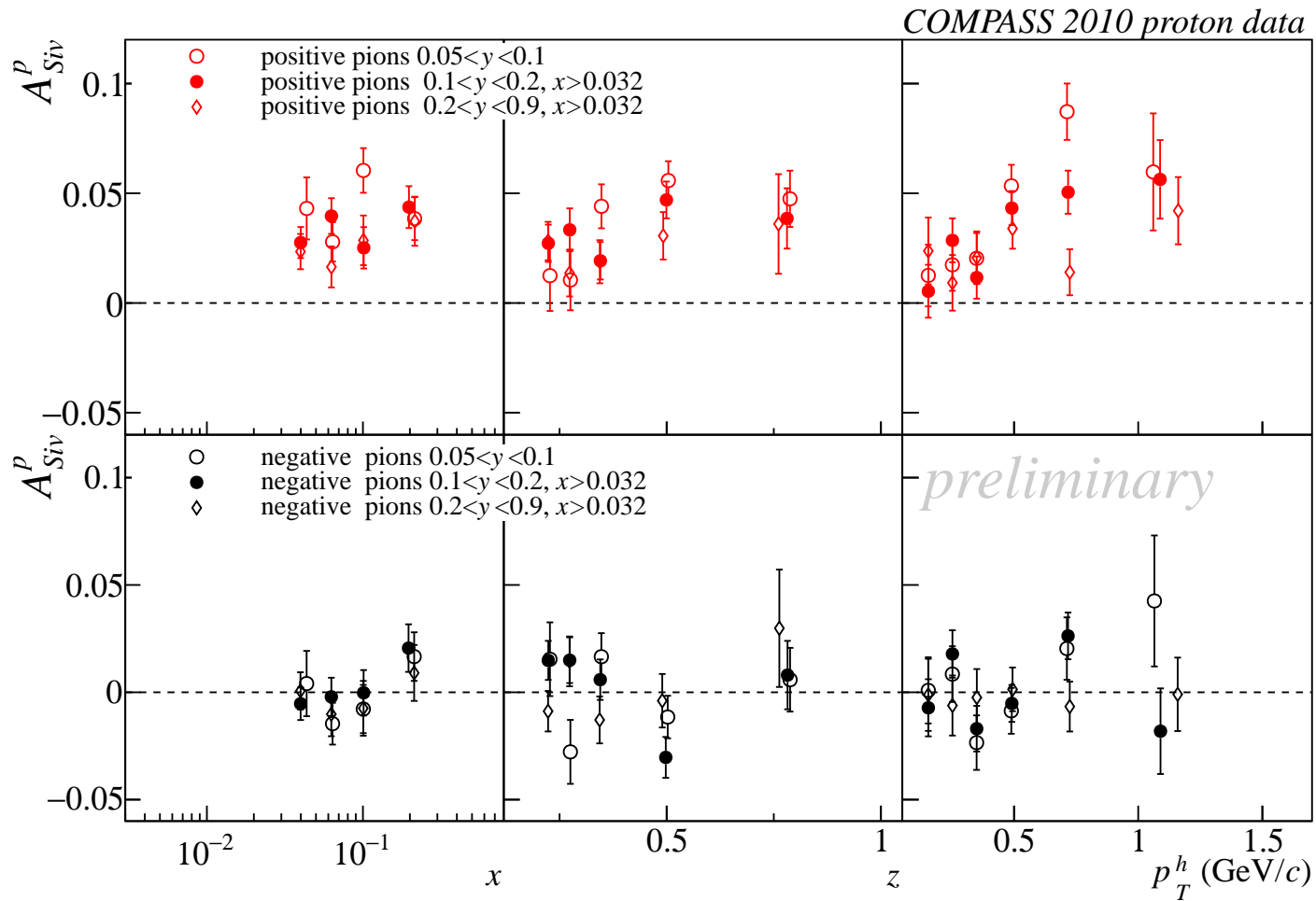
Sivers asymmetry ► pions ► multi-dimensional analysis in z



3 z ranges: $0.1 < z_{\text{low}} < 0.2 < z_{\text{mid}} < 0.35 < z_{\text{high}} < 1.0$

↪ smaller asymmetries for π^+ in z_{low} region

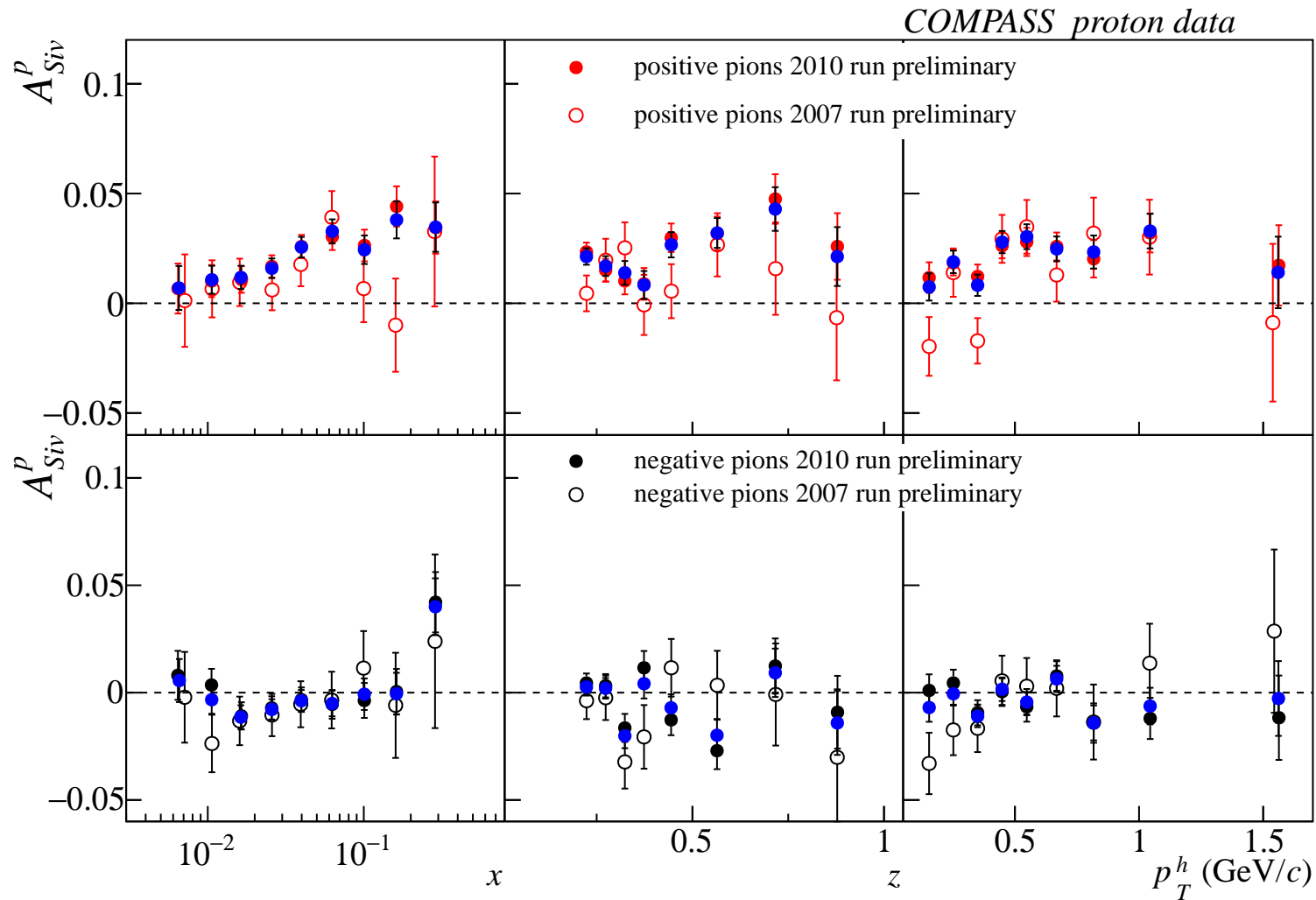
Sivers asymmetry ► pions ► multi-dimensional analysis in y



3 y ranges: $0.05 < y_{\text{low}} < 0.1 < y_{\text{mid}} < 0.2 < y_{\text{high}} < 0.9$

↪ no significant systematic effect *w.r.t.* the uncertainties

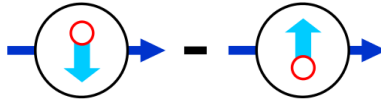
Sivers asymmetry ► pions ► combined '07 and '10 data

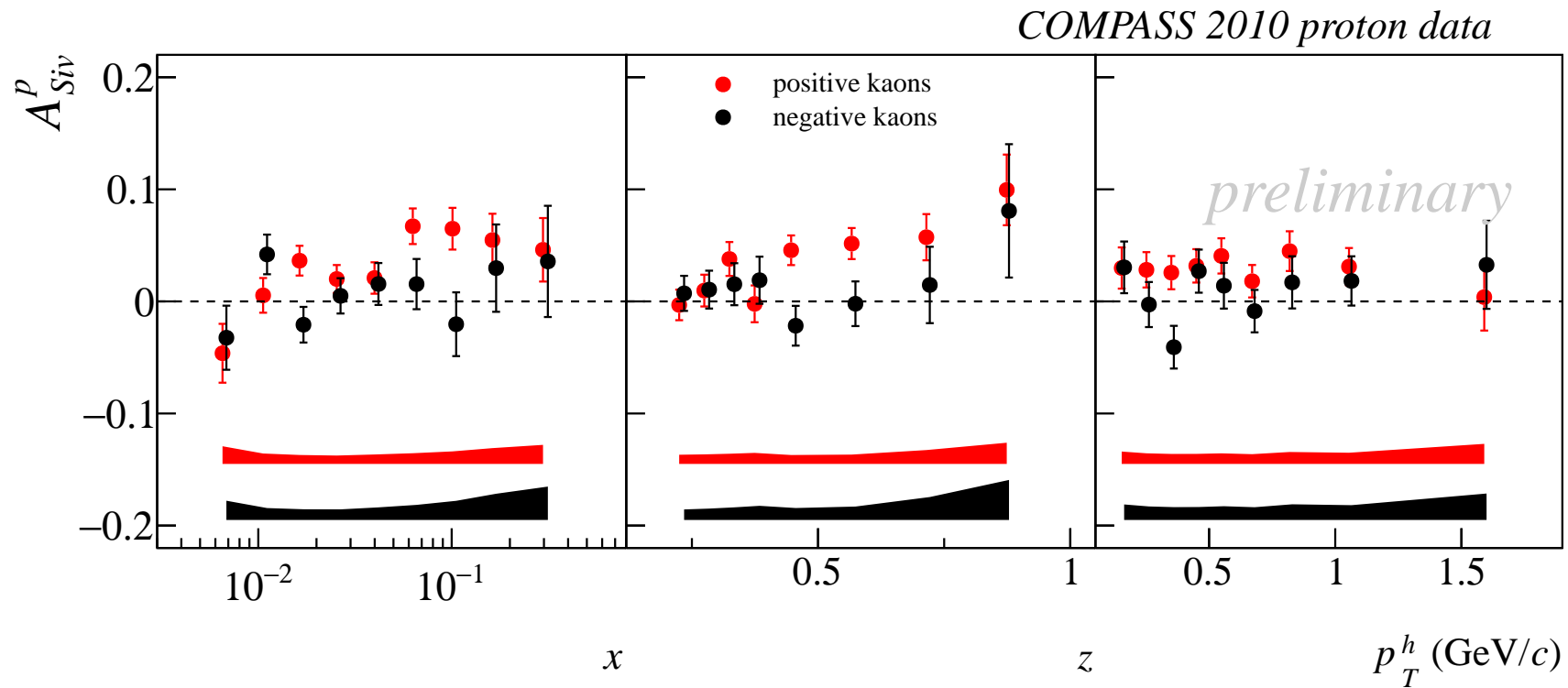


↪ good agreement of '10 and '07 data

data combined by taking into account statistical and systematical uncertainties

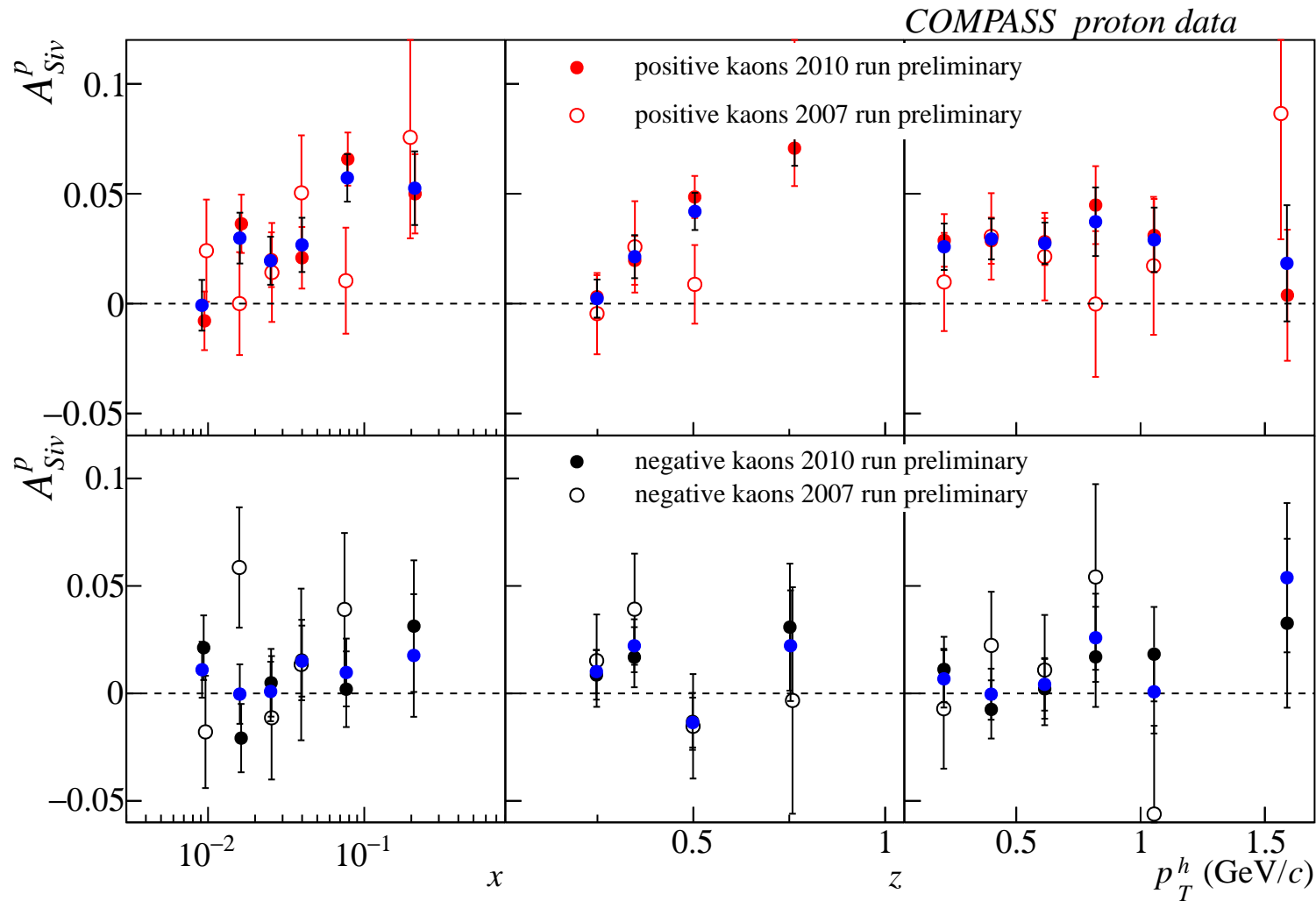
Sivers asymmetry ► kaons ► 2010 data

Twist-2 $A_{UT}^{\sin(\phi_h - \phi_S)}$ $f_{1T}^{\perp q}(x)$ 



- ↪ K^+ : clear signal up to 7 % in x , 10 % in z and non-zero in p_T^h
- ↪ K^- : mostly compatible with zero within the uncertainties

Sivers asymmetry ► kaons ► combined '07 and '10 data



↪ '10 with its higher statistics dominates combined results

↪ clear non-zero asymmetry for K^+

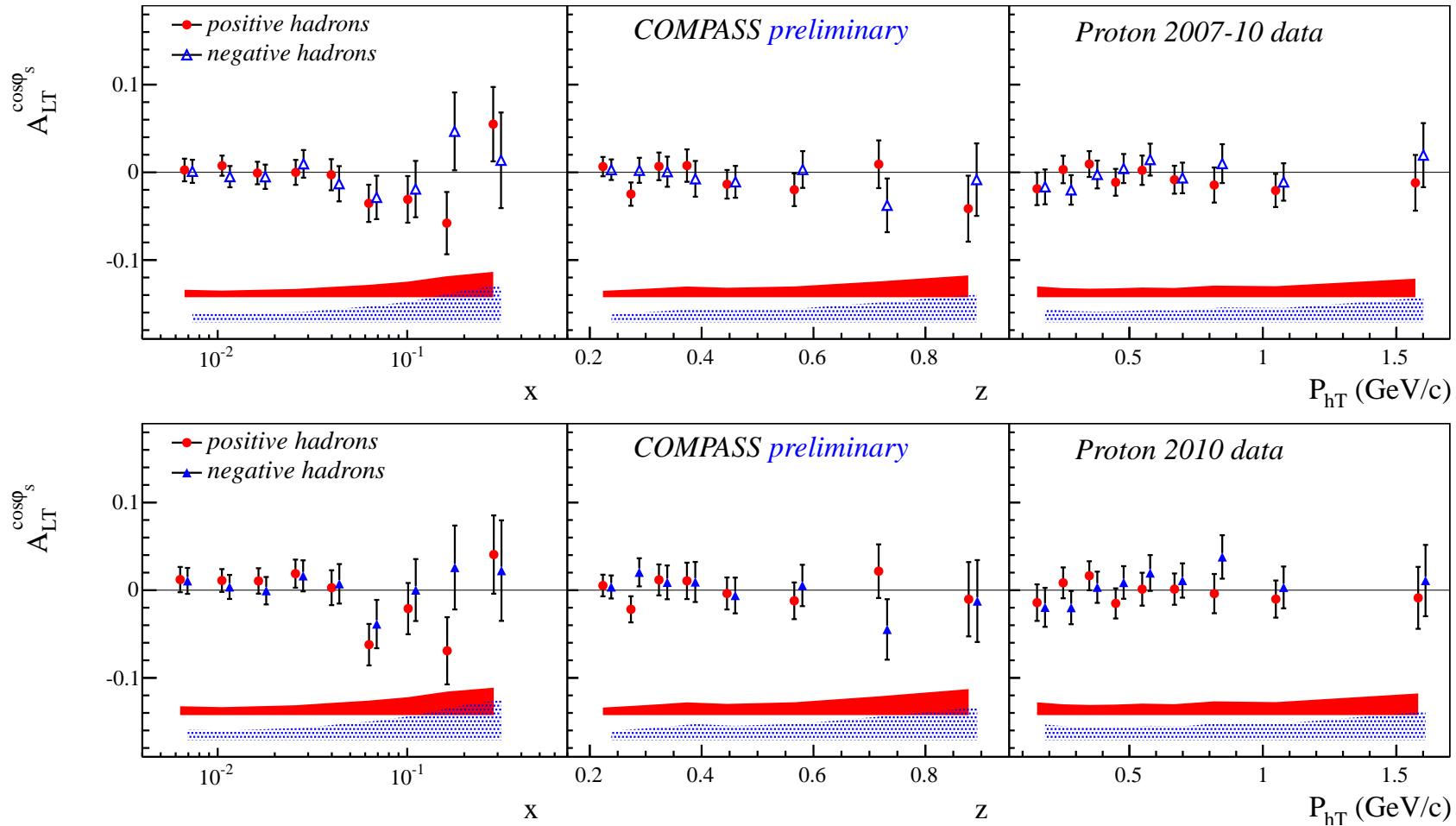
data combined by taking into account statistical and systematical uncertainties

The +6 transverse spin asymmetries

deuteron data 2002-04 & proton data 2007 and 2010

A_{LT1} ► charged hadrons ► p 2010 and combined data

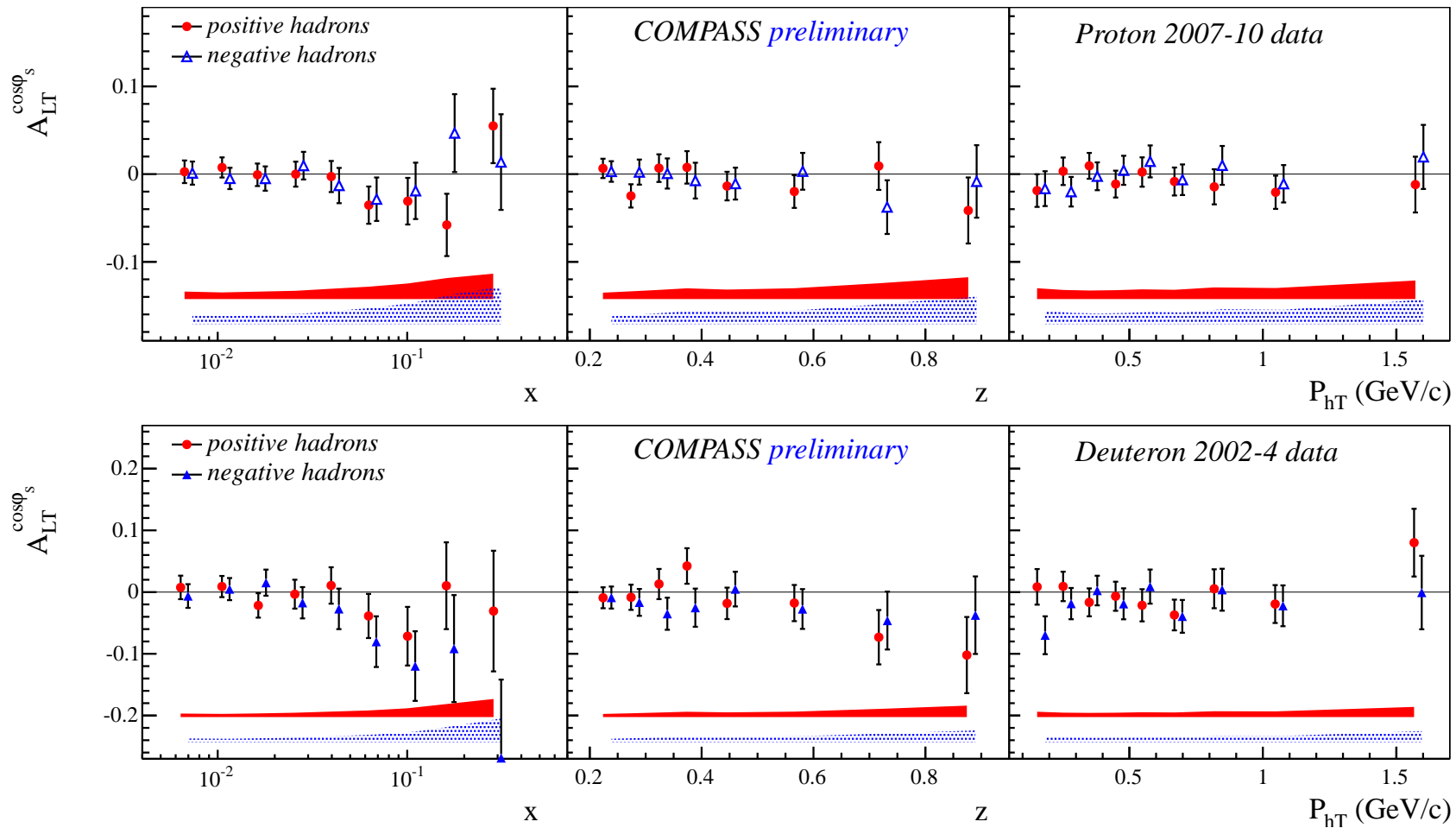
Twist-3 $A_{LT}^{\cos(\phi_S)}$ Worm-gear $g_{1T}^{q\perp}(x)$ 



↪ proton data compatible with zero within the uncertainties

A_{LT1} ► charged hadrons ► proton *vs.* deuteron data

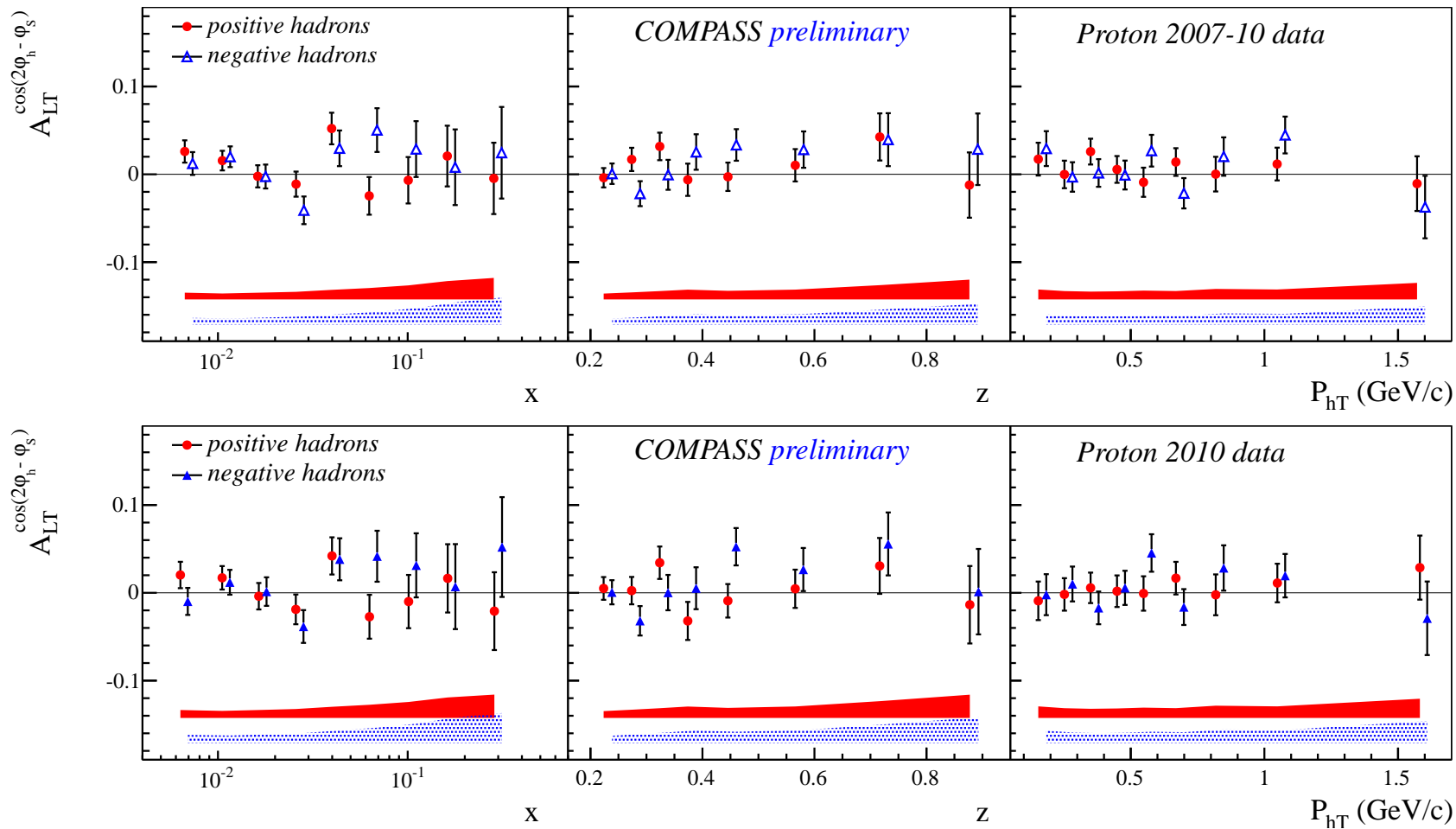
Twist-3 $A_{LT}^{\cos(\phi_S)}$ Worm-gear $g_{1T}^{q\perp}(x)$ 



↪ deuteron data compatible with zero within the uncertainties

A_{LT2} ► charged hadrons ► p 2010 and combined data

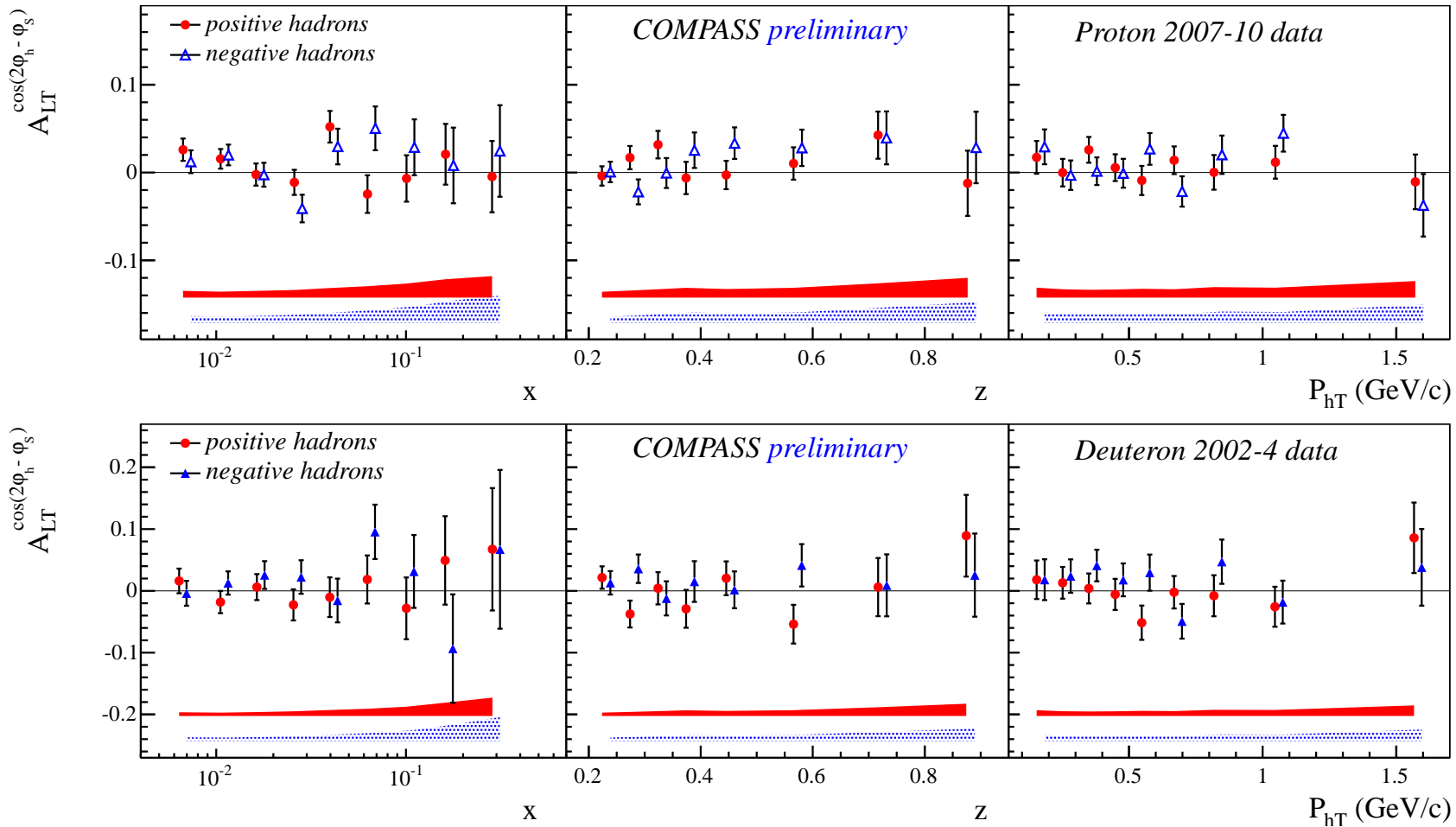
Twist-3 $A_{LT}^{\cos(2\phi_h - \phi_S)}$ Worm-gear $g_{1T}^{q\perp}(x)$ 



↪ proton data compatible with zero within the uncertainties

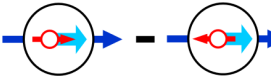
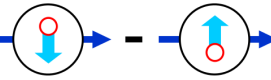
A_{LT2} ► charged hadrons ► proton *vs.* deuteron data

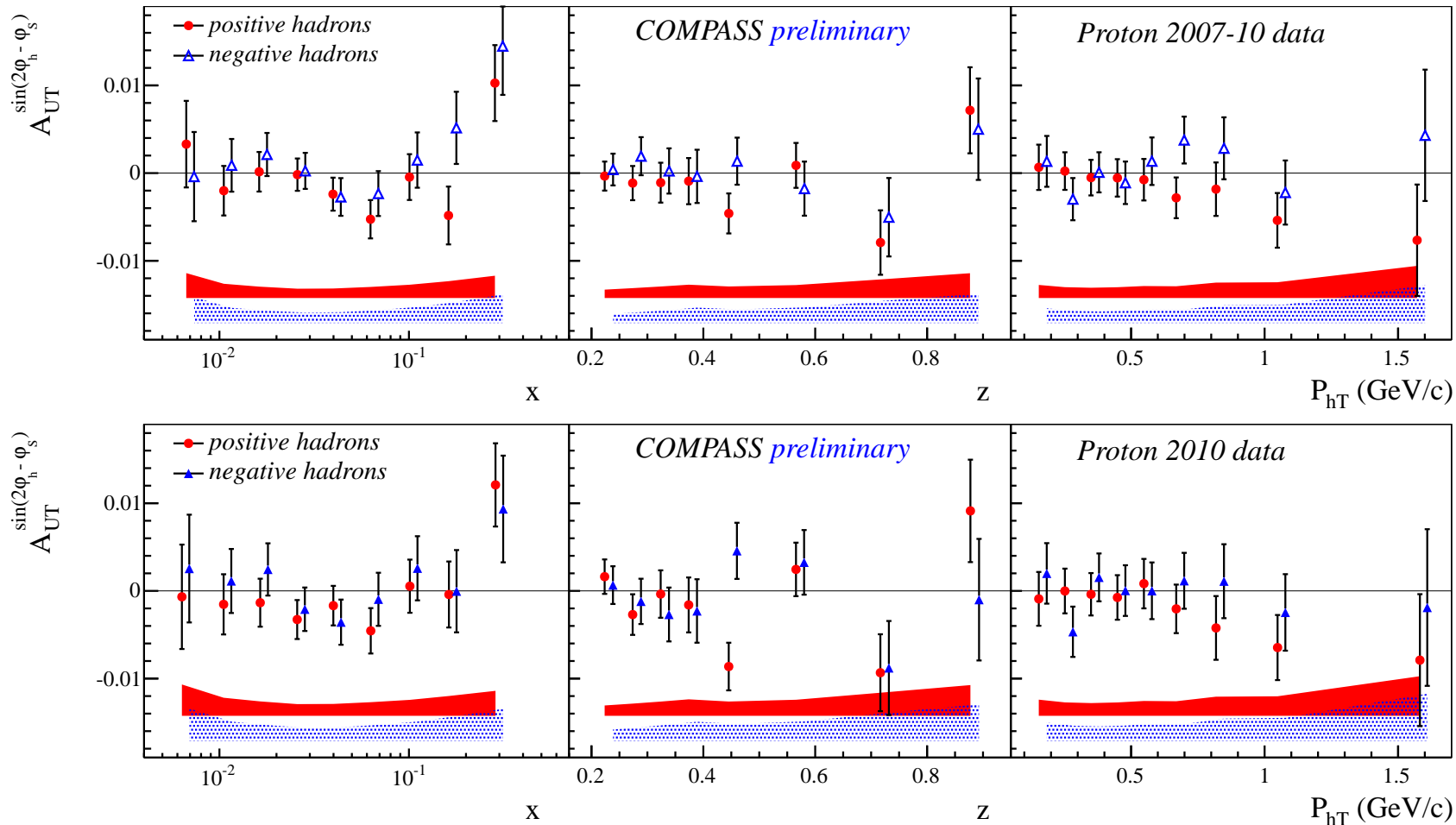
Twist-3 $A_{LT}^{\cos(2\phi_h - \phi_S)}$ Worm-gear $g_{1T}^{q\perp}(x)$ 



↪ deuteron data compatible with zero within the uncertainties


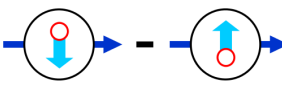
A_{UT2} ► charged hadrons ► p 2010 and combined data

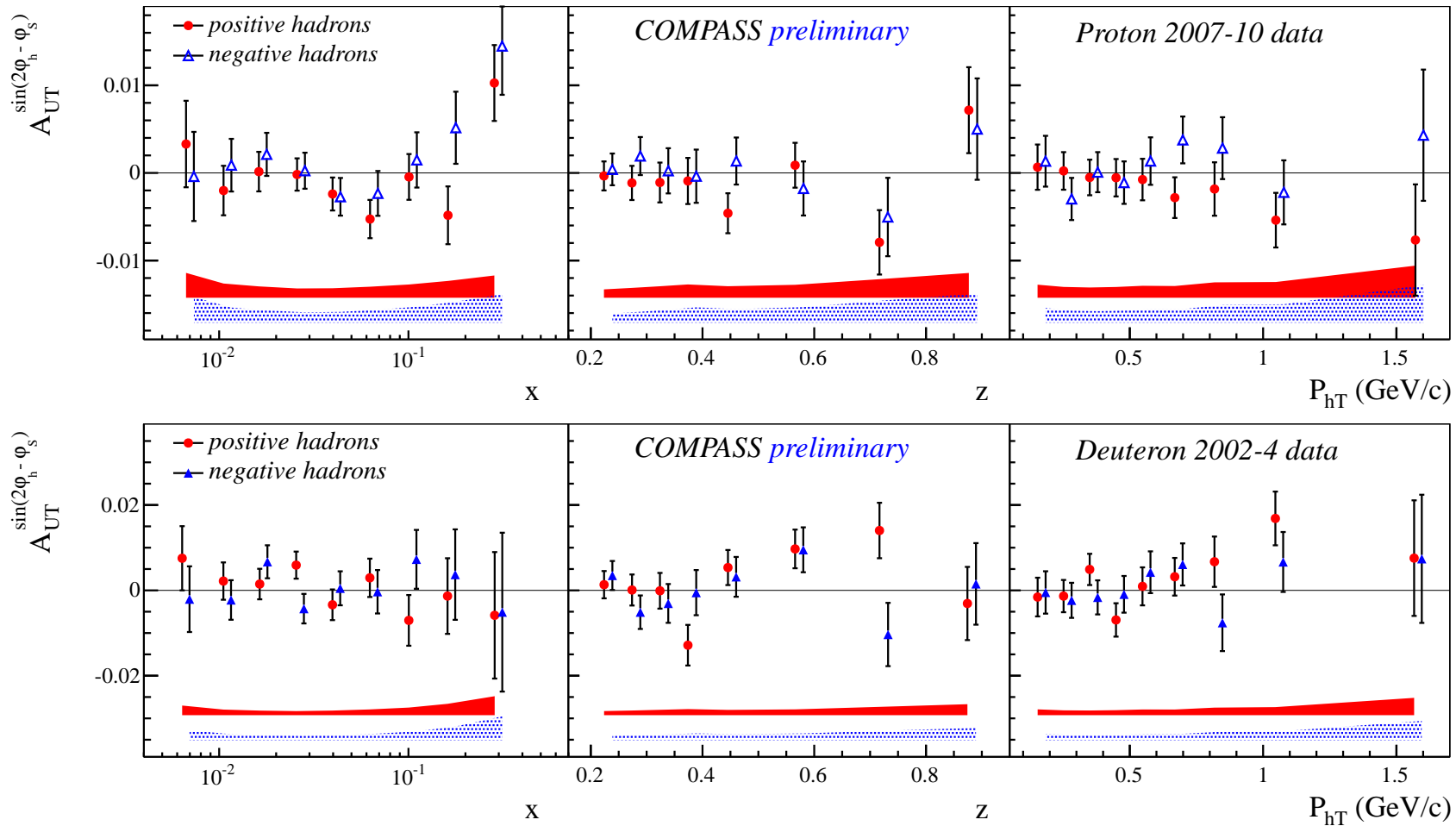
Twist-3 $A_{UT}^{\sin(2\phi_h - \phi_S)}$ Pretzelosity $h_{1T}^{q\perp}(x)$ ; Sivers $f_{1T}^{\perp q}(x)$ 



↪ proton data compatible with zero within the uncertainties

A_{UT2} ► charged hadrons ► proton vs. deuteron data

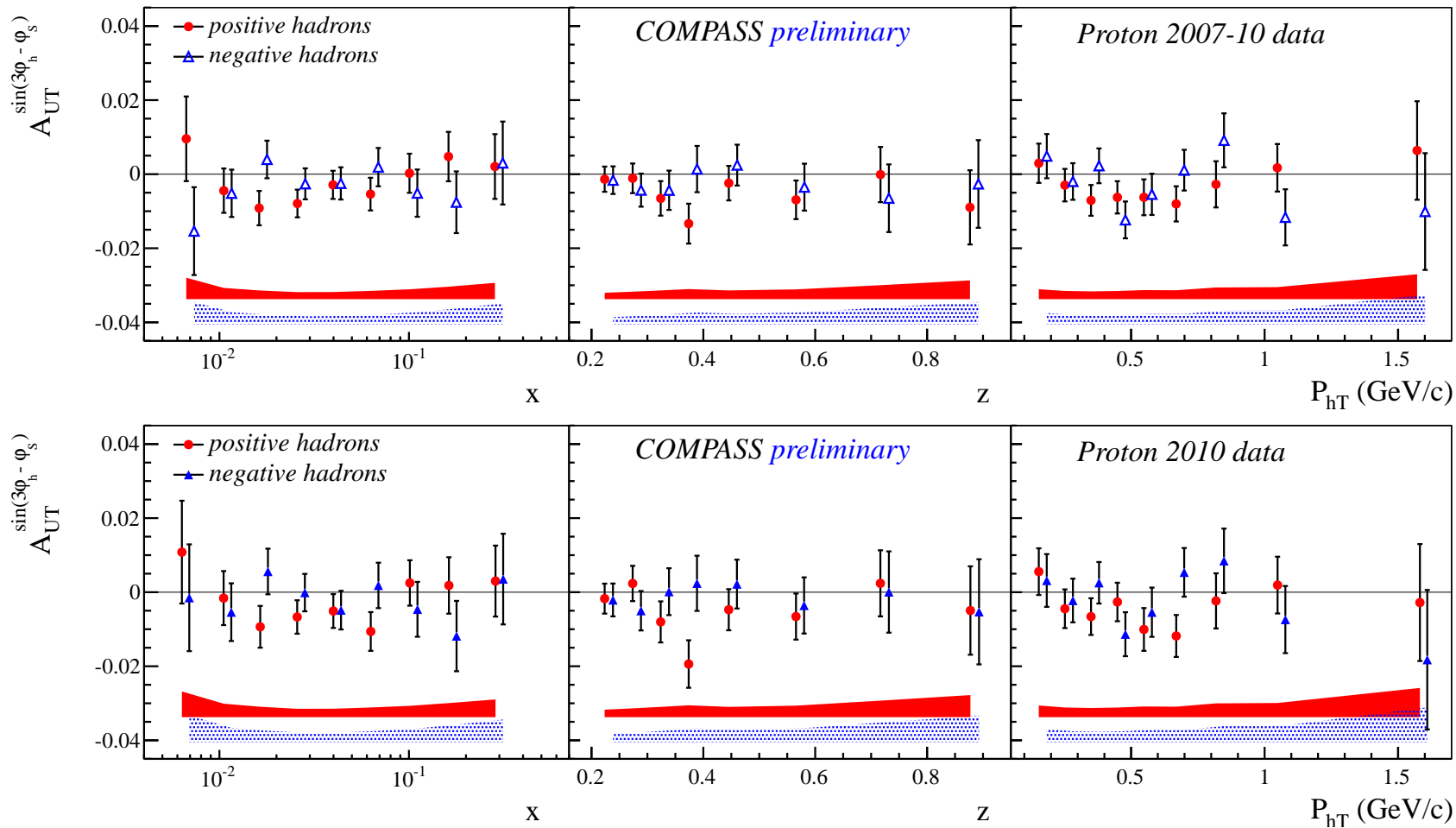
Twist-3 $A_{UT}^{\sin(2\phi_h - \phi_S)}$ Pretzelosity $h_{1T}^{q\perp}(x)$ ; Sivers $f_{1T}^{\perp q}(x)$ 



↪ deuteron data non-zero in mid z range

Pretzelosity \blacktriangleright charged hadrons \blacktriangleright p 2010 and combined data

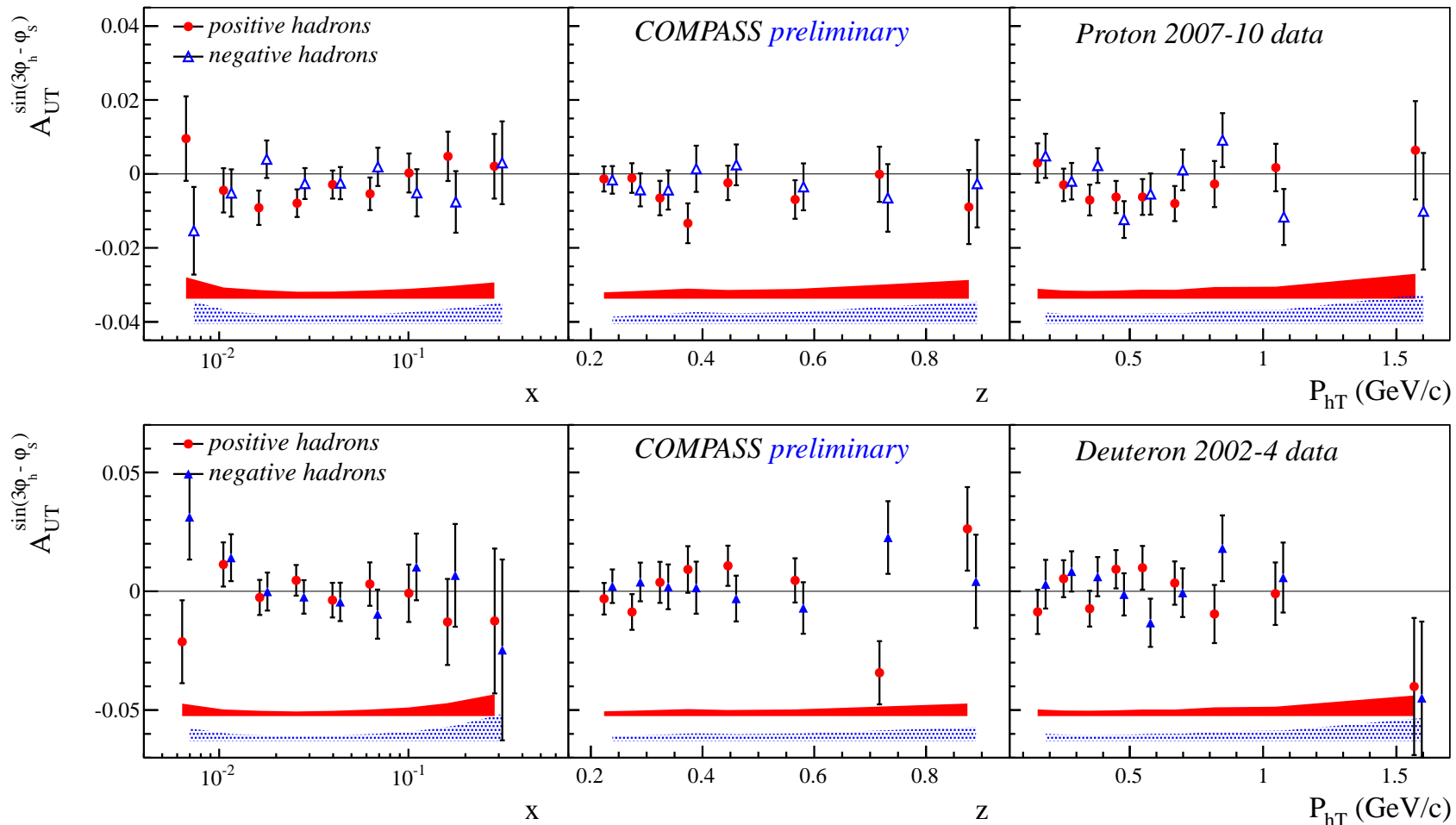
Twist-2 $A_{UT}^{\sin(3\phi_h - \phi_S)}$ Pretzelosity $h_{1T}^{q\perp}(x)$ 



\hookrightarrow proton data compatible with zero within the uncertainties

Pretzelosity ► charged hadrons ► proton *vs.* deuteron data

Twist-2 $A_{UT}^{\sin(3\phi_h - \phi_S)}$ Pretzelosity $h_{1T}^{q\perp}(x)$



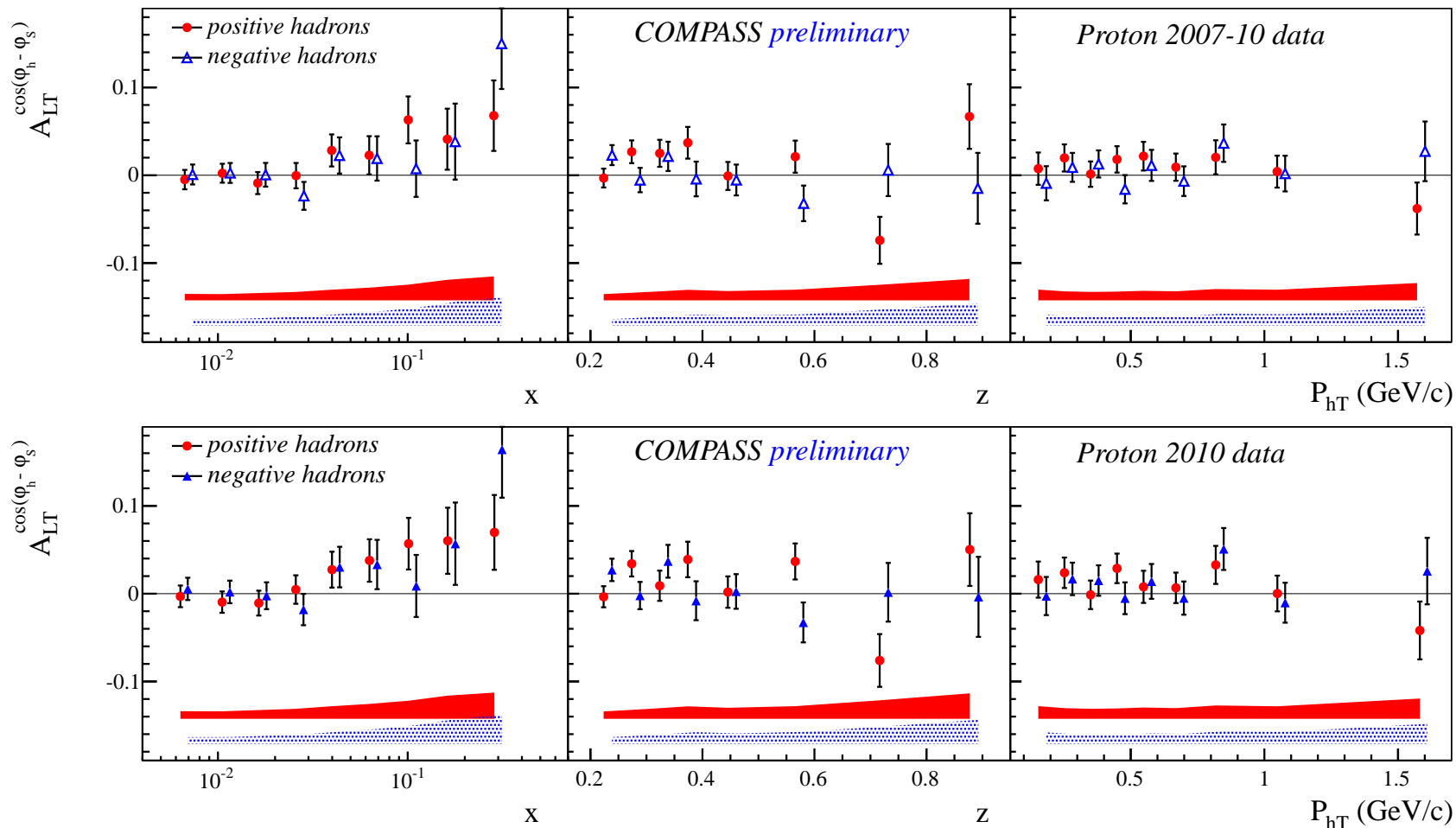
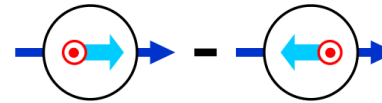
↪ deuteron data compatible with zero within the uncertainties

Worm-gear \blacktriangleright charged hadrons \blacktriangleright p 2010 and combined data

Twist-2

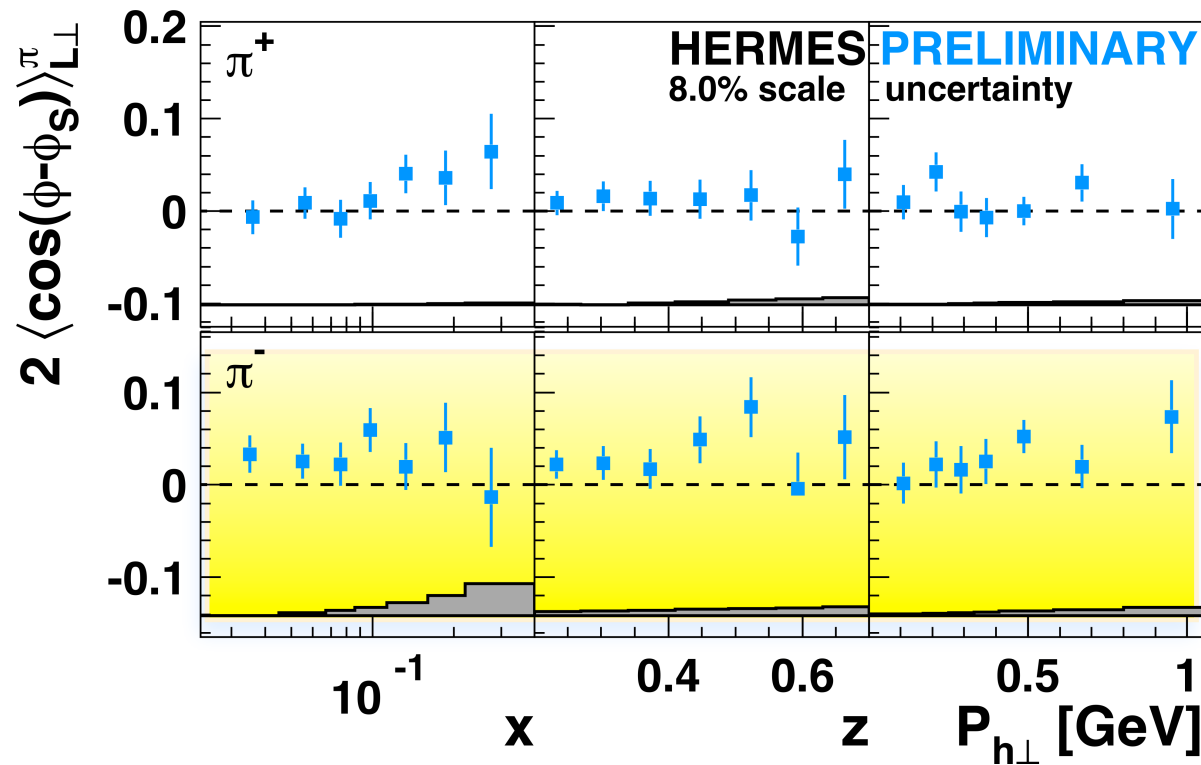
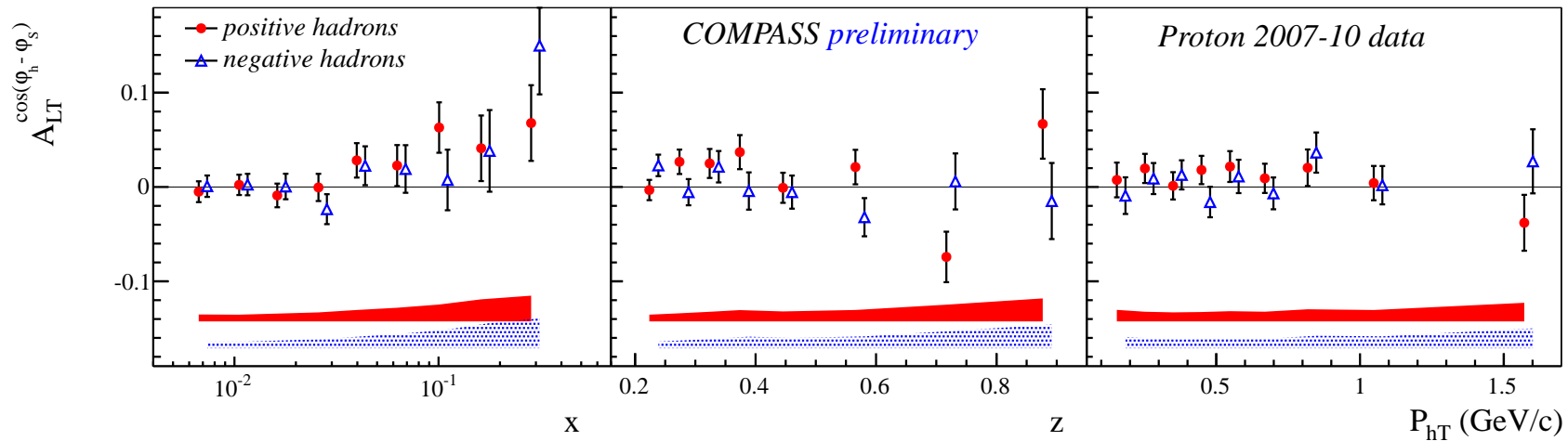
$$A_{LT}^{\cos(\phi_h - \phi_S)}$$

Worm-gear $g_{1T}^{q\perp}(x)$



\hookrightarrow proton data shows non-zero trend in x for positive charged hadrons at relatively large x

Worm-gear \blacktriangleright charged hadrons \blacktriangleright HERMES *vs.* COMPASS



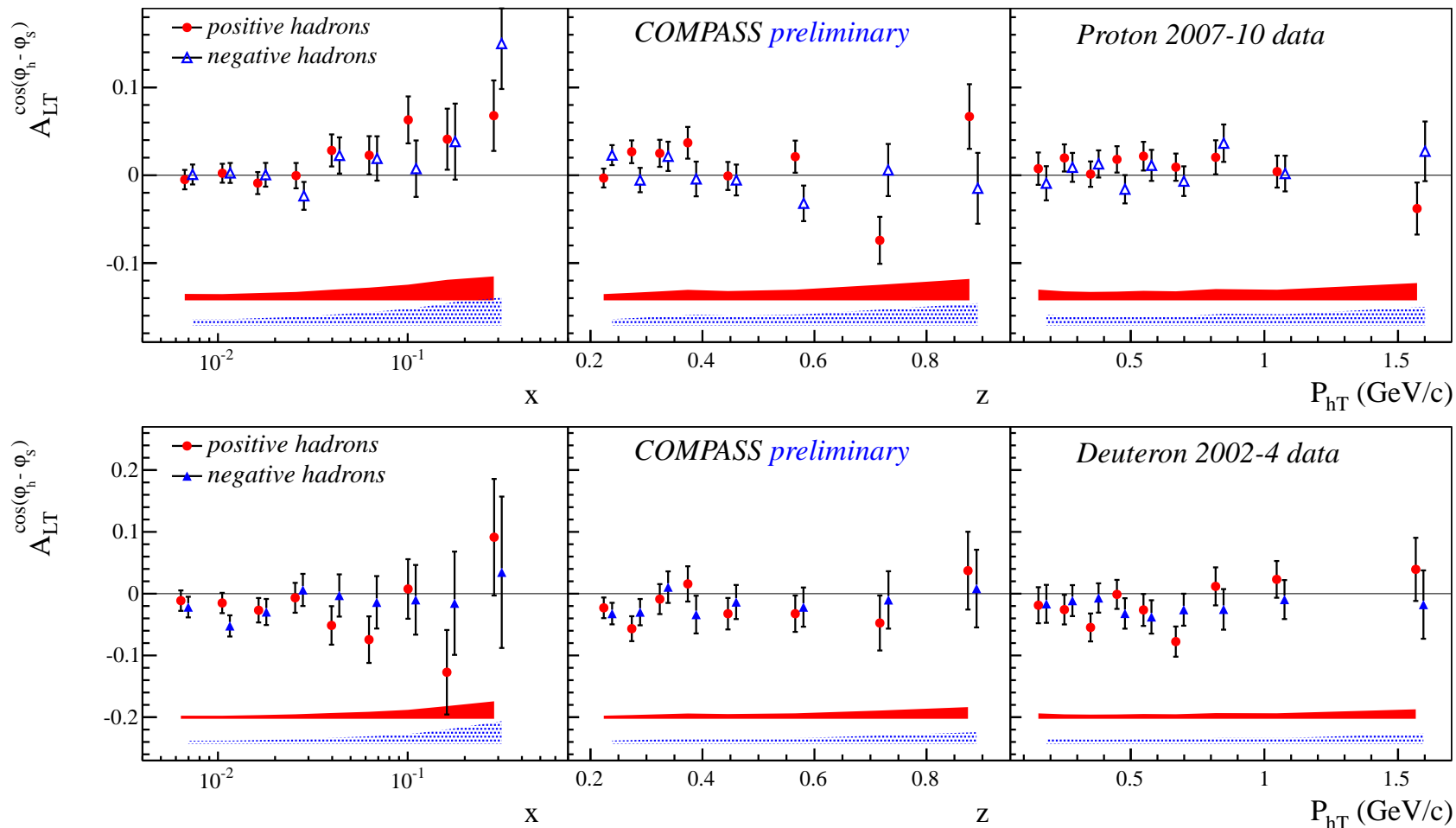
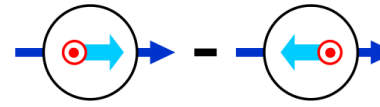
\hookrightarrow Similar trend in x for HERMES and COMPASS

Worm-gear \blacktriangleright charged hadrons \blacktriangleright proton *vs.* deuteron data

Twist-2


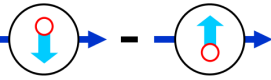
$$A_{LT}^{\cos(\phi_h - \phi_S)}$$

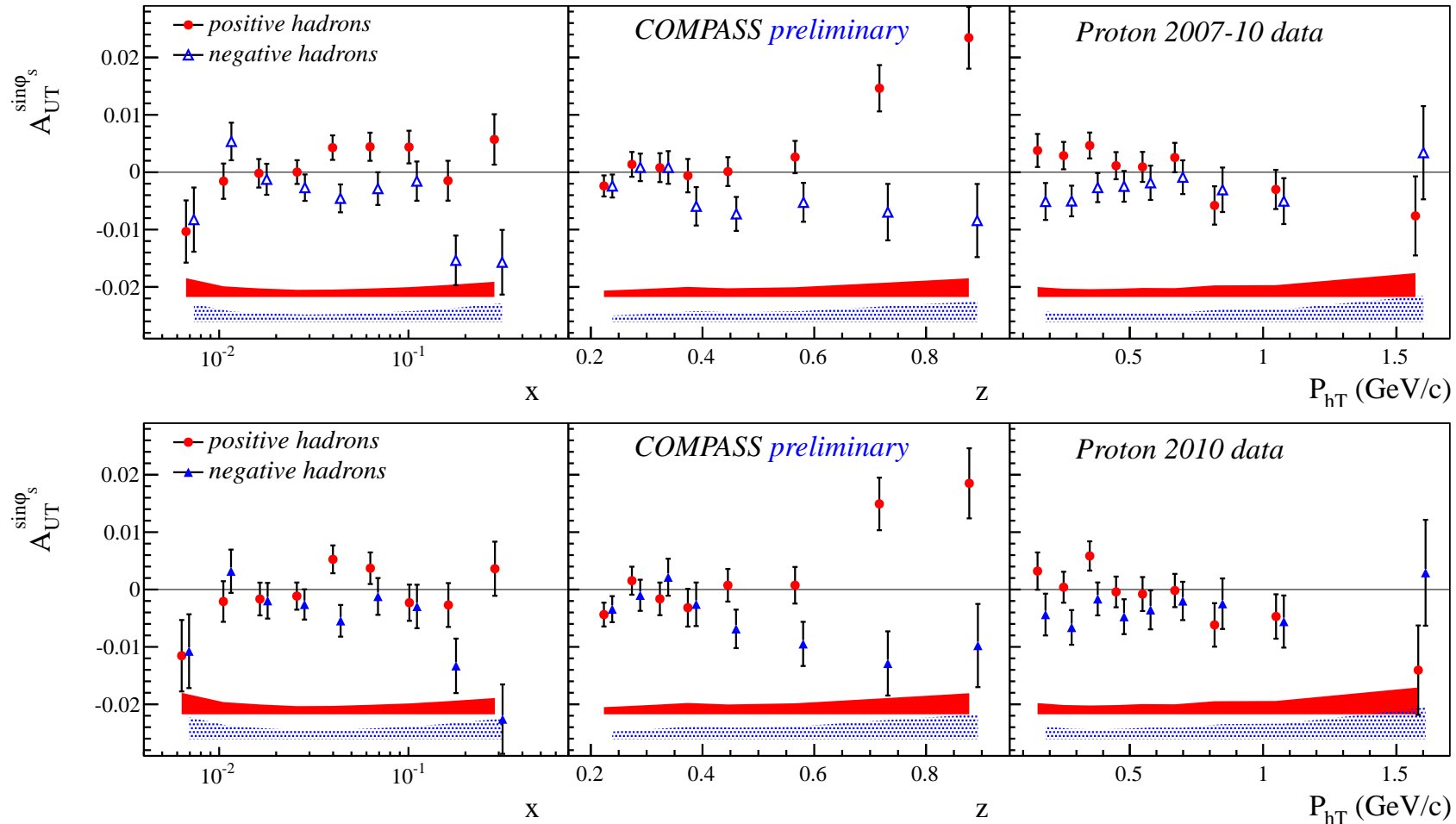
$$\text{Worm-gear } g_{1T}^{q\perp}(x)$$



\hookrightarrow deuteron data compatible with zero within the uncertainties
 \hookrightarrow indication of negative mean value

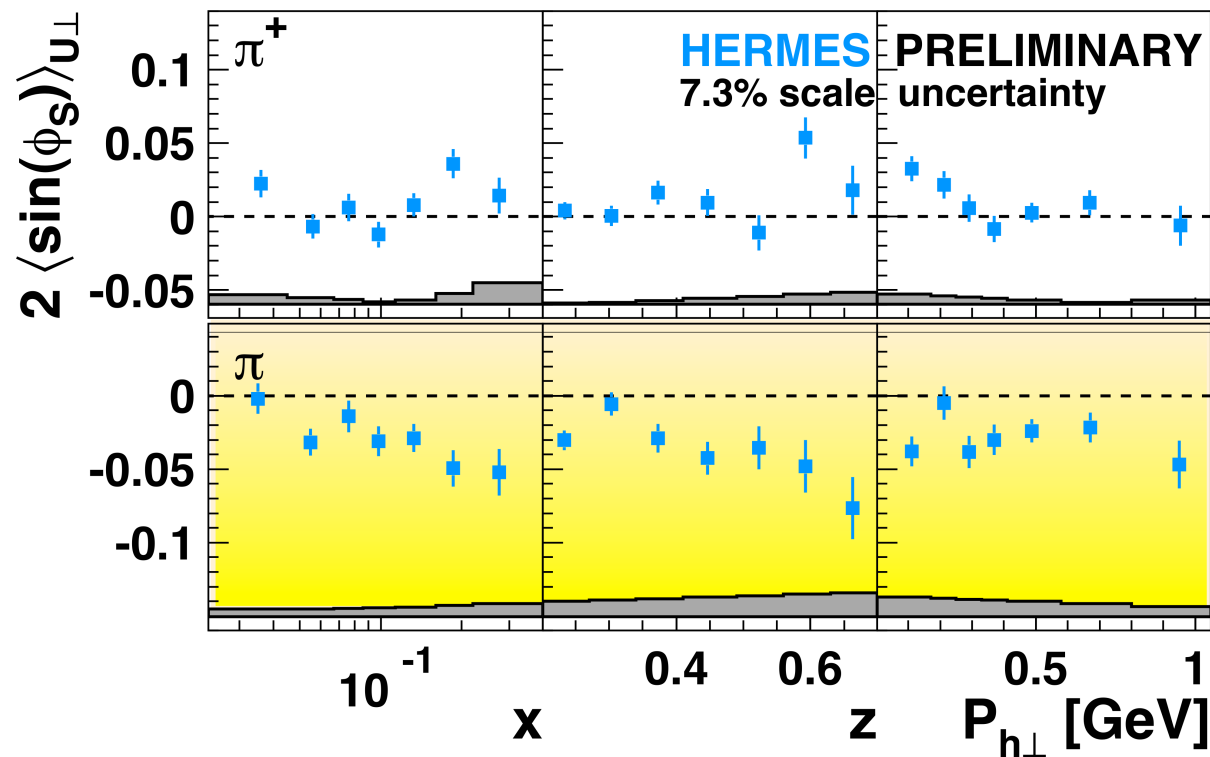
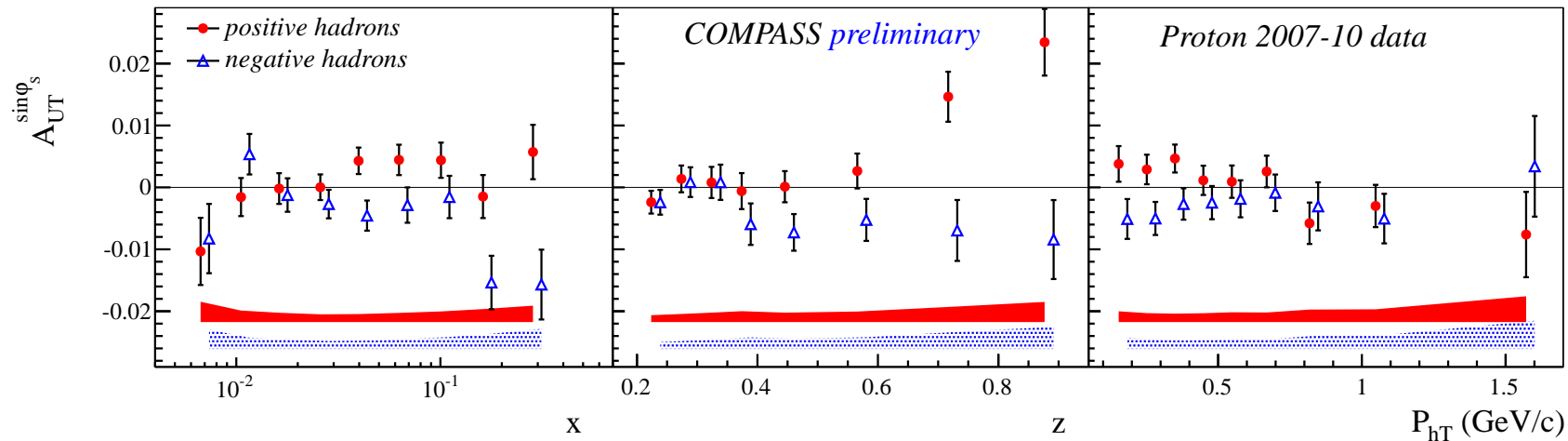
A_{UT1} ► charged hadrons ► p 2010 and combined data

Twist-3 $A_{UT}^{\sin(\phi_S)}$ Transversity $h_1^q(x)$ ; Sivers $f_{1T}^{\perp q}(x)$ 



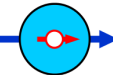
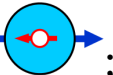
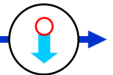

↪ proton data shows non-zero negative trend for h^- in x

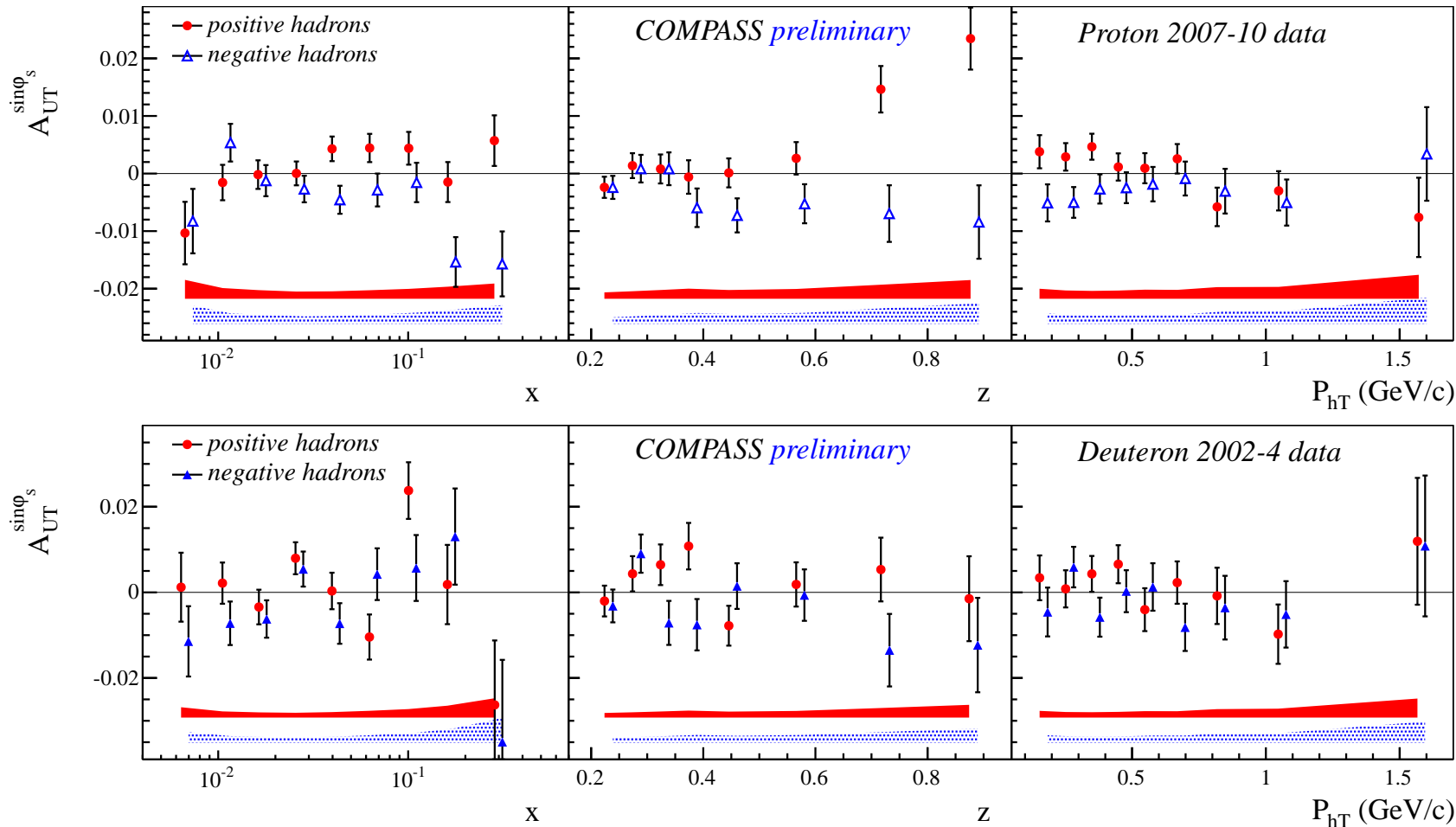
A_{UT1} ► charged hadrons ► HERMES *vs.* COMPASS



↪ similar trends in x , z and p_T^h for HERMES π^- and COMPASS h^-

A_{UT1} ► charged hadrons ► proton *vs.* deuteron data

Twist-3 $A_{UT}^{\sin(\phi_S)}$ Transversity $h_1^q(x)$  -  ; Sivers $f_{1T}^{\perp q}(x)$  - 






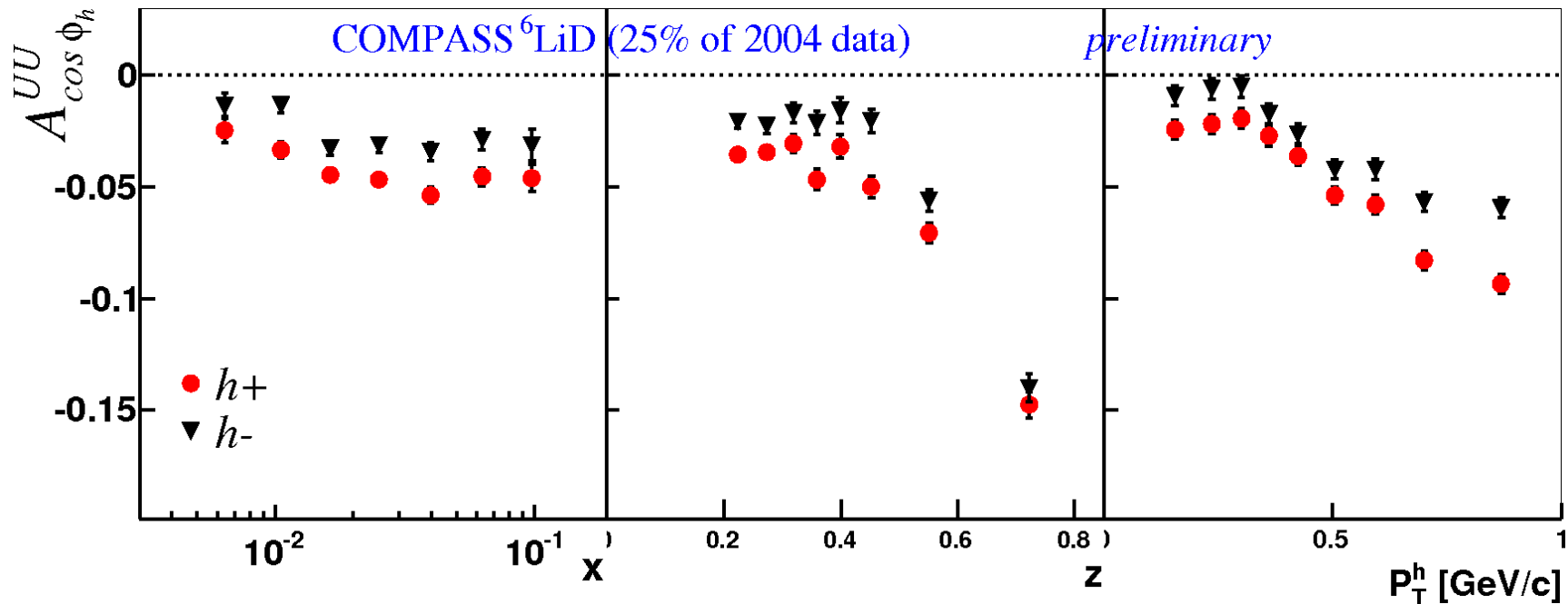
↪ deuteron data is compatible with zero within the uncertainties

Unpolarized (target) azimuthal asymmetries

deuteron data 2004

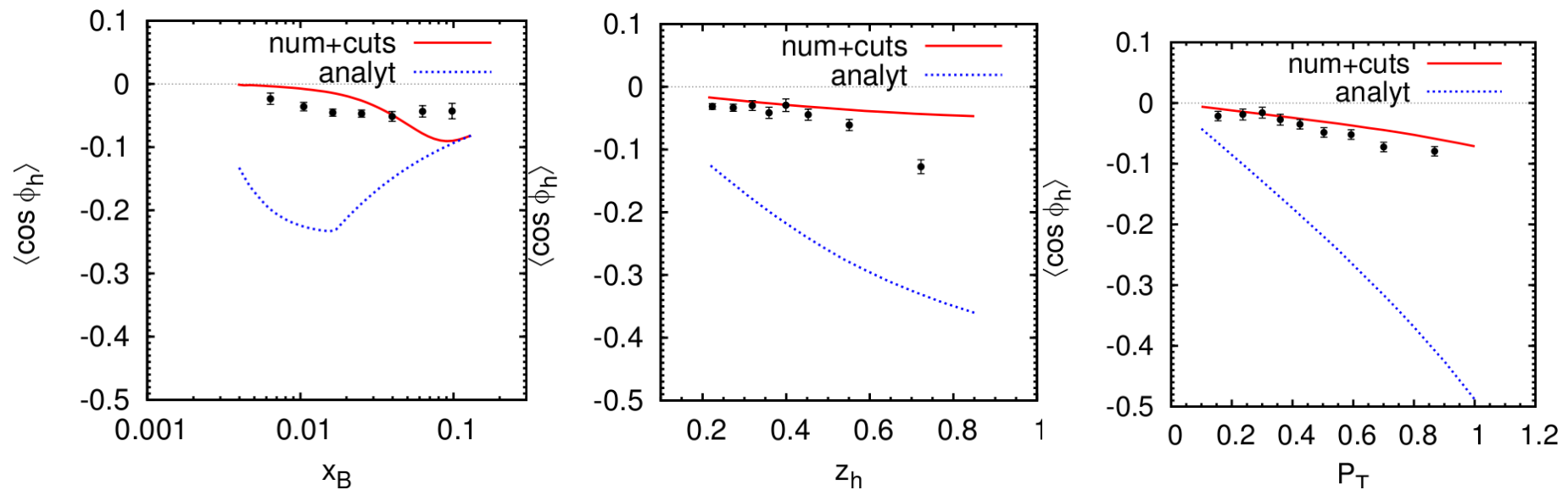
A_{UU1} ► charged hadrons ► 2004 data

Twist-2 $A_{UU}^{\cos \Phi_h}$ Cahn $f_1^q(x)$ ; Boer-Mulders $h_1^{\perp q}(x)$  - 



- ↳ clear asymmetry in x and p_T^h
- ↳ strong z dependence for $z > 0.5$
- ↳ h^+ asymmetries systematical larger than h^-

$A_{UU1} \triangleright h^+ \triangleright$ 2004 data *vs.* model calculations



M. Boglione, S. Melis and A. Prokudin, Phys.Rev.D84, arXiv:1107.4436v1

↪ same trend and strength in p_T^h and low z region

Unpolarized ► charged hadrons ► 2004 data

Towards a multi dimensional analysis:

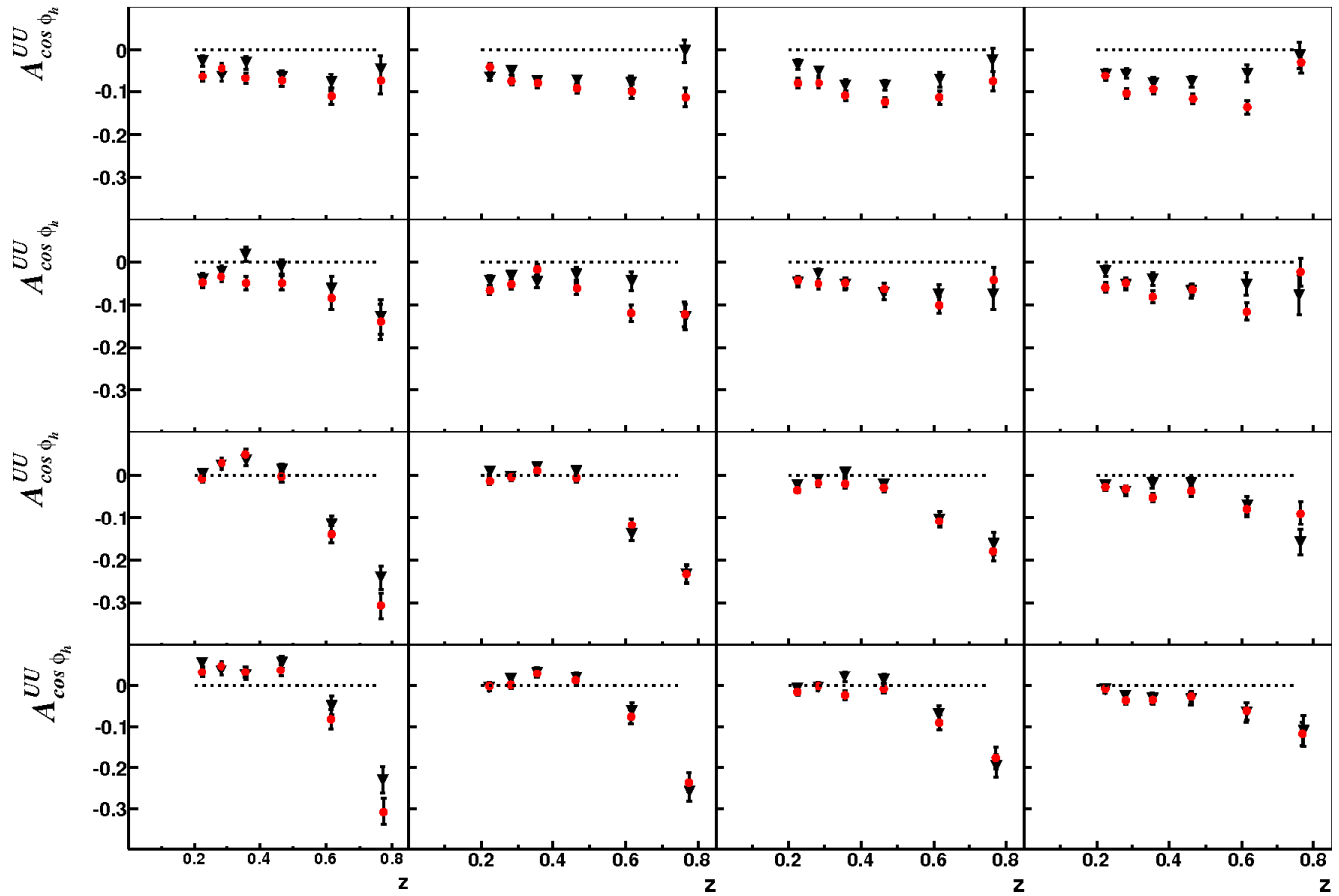
to get a better understanding of the kinematical dependencies in x , z and p_T^h .

Using a simultaneous binning:

x	p_T^h	z
0.003 – 0.012	0.10 – 0.30	0.20 – 0.25
0.012 – 0.020	0.30 – 0.50	0.25 – 0.32
0.020 – 0.038	0.50 – 0.64	0.32 – 0.40
0.038 – 0.130	0.64 – 1.00	0.40 – 0.55
		0.55 – 0.70
		0.70 – 0.85

A_{UU1} ► charged hadrons ► 2004 data preliminary

COMPASS⁶LiD (25% of 2004 data)






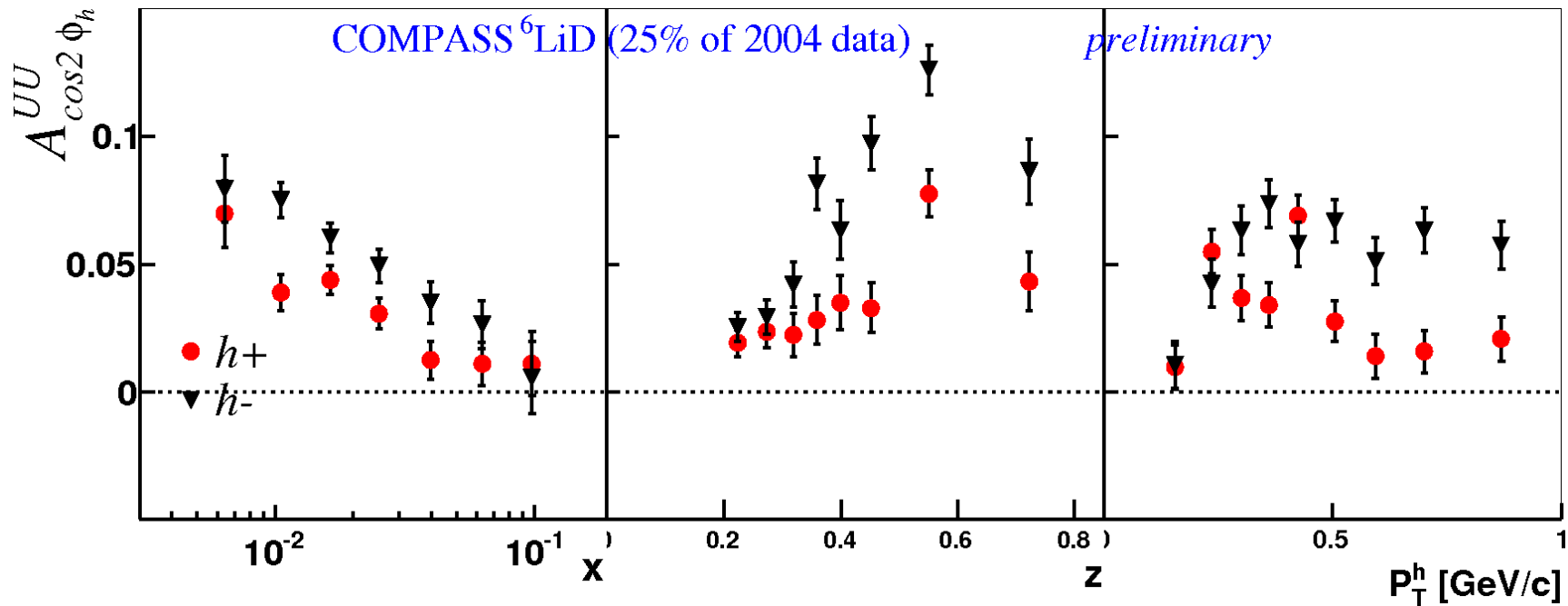
↑ p_T^h ; → x

$\sigma_{sys} \approx 2 \cdot \sigma_{stat}$

↪ strong dependence in z more evident at small x and small p_T^h

A_{UU2} ► charged hadrons ► 2004 data

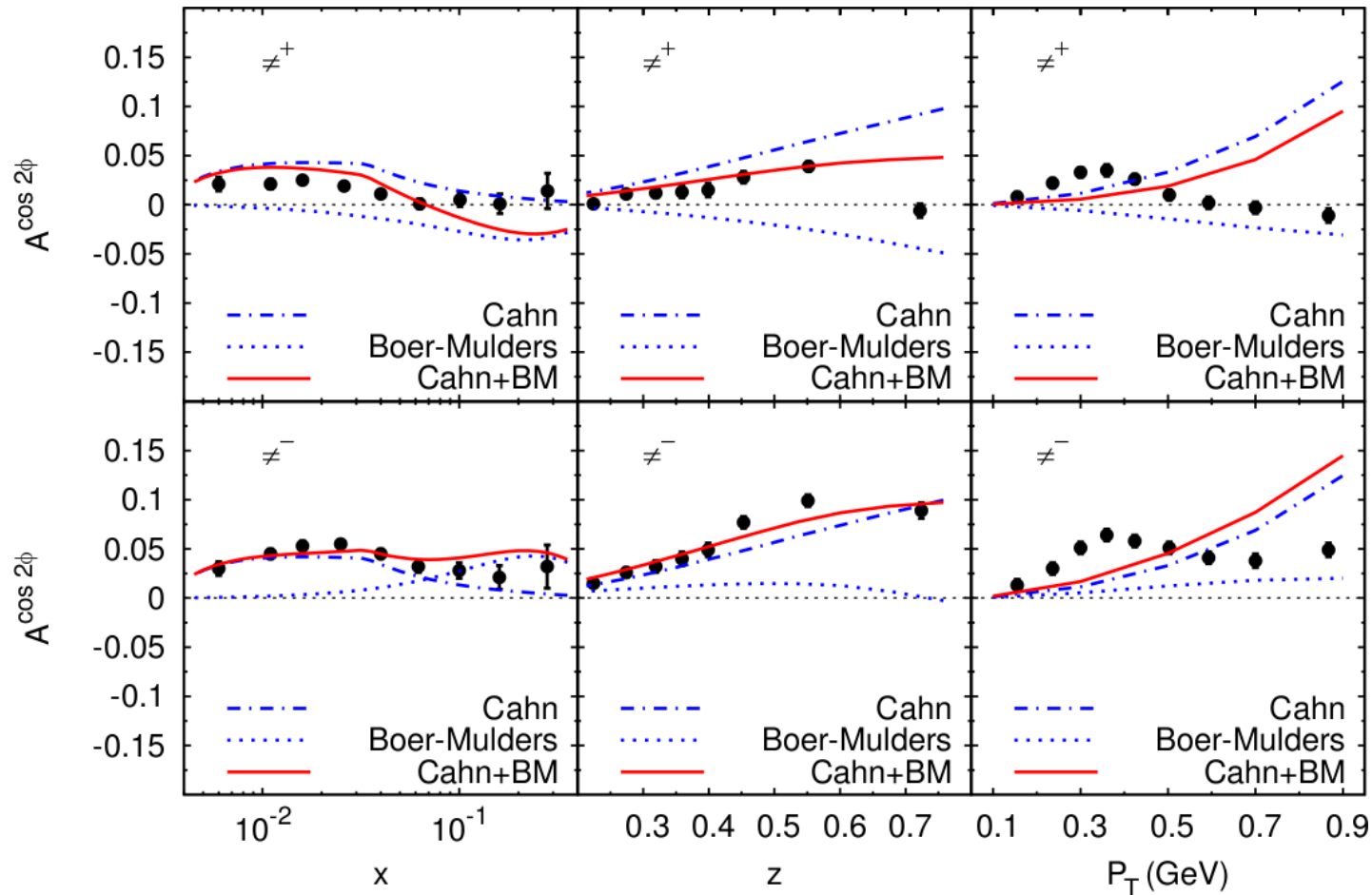
Twist-2 $A_{UU}^{\cos 2\Phi_h}$ Cahn $f_1^q(x)$ ; Boer-Mulders $h_1^{\perp q}(x)$  - 



first shown at SPIN2010 by G. Sbrizzai

- ↳ clear asymmetry in low x and high z
- ↳ p_T^h dependence shows saturation for h^-
- ↳ h^- asymmetries systematical larger than h^+

A_{UU2} ► charged hadrons ► 2004 data *vs.* model calculations

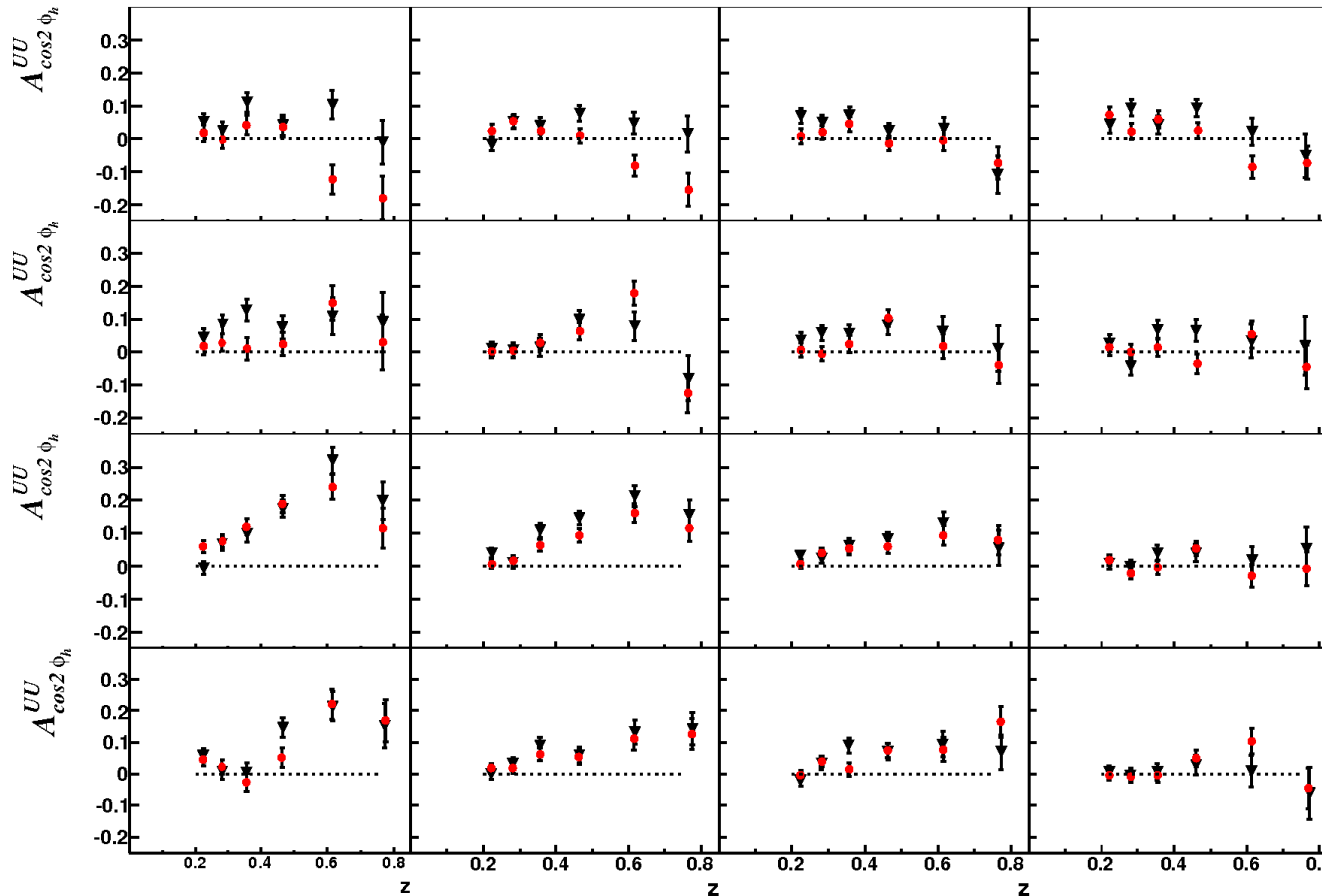


V. Barone, S. Melis and A. Prokudin, Phys.Rev.D81, arXiv:0912.5194v2

- ↪ same trend and strength in x and low z region
- ↪ p_T^h dependence difficult to reproduce

A_{UU2} ► charged hadrons ► 2004 data preliminary

COMPASS⁶LiD (25% of 2004 data)



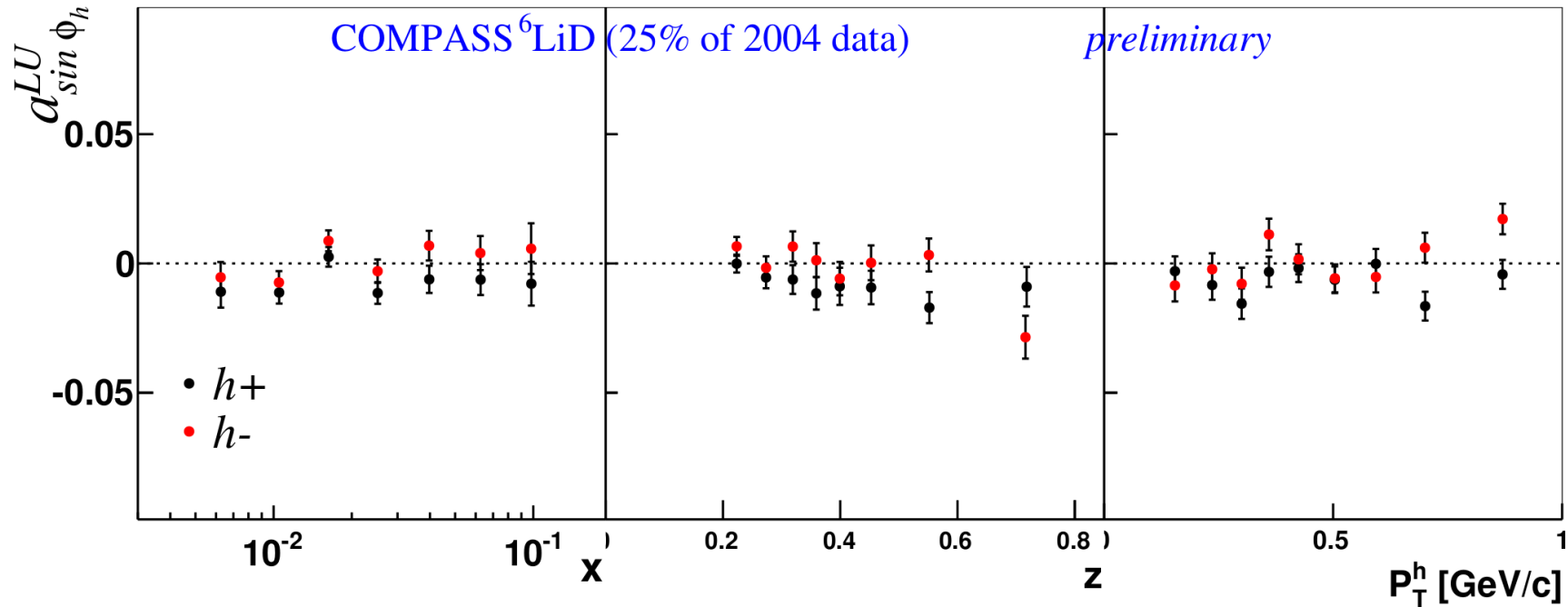
↑ p_T^h ; → x

$\sigma_{sys} \approx 2 \cdot \sigma_{stat}$

↪ strongest signal at low x and low p_T^h

A_{LU} ► charged hadrons ► 2004 data

Twist-3 $A_{LU}^{\sin \phi_h}$



first shown at SPIN2010 by G. Sbrizzai

↔ mostly compatible with zero for all charged hadrons

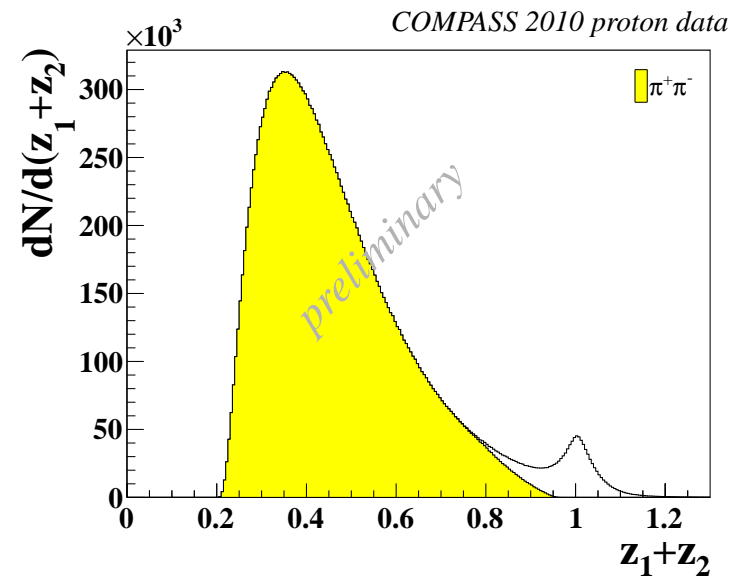
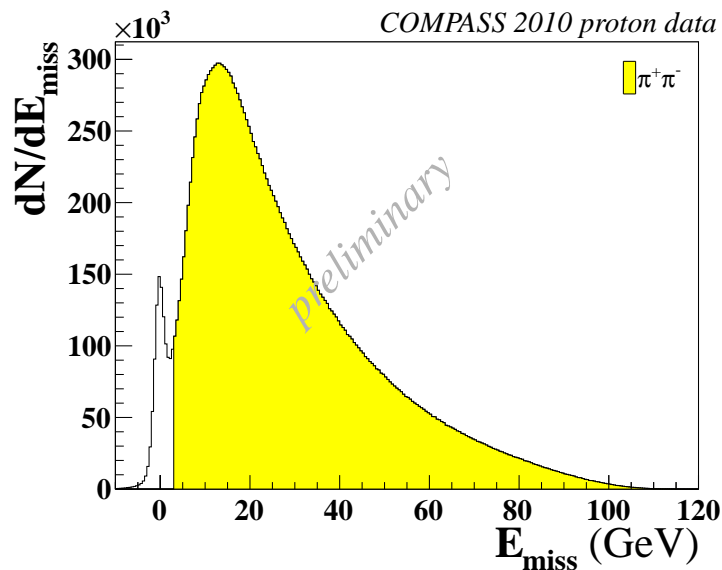
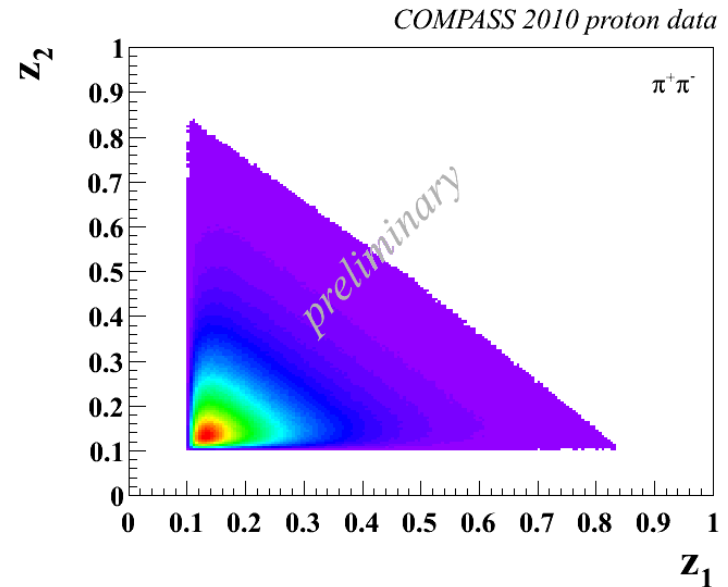
Dihadron asymmetry

proton data 2010

Data selection ► dihadron asymmetry

hadron & hadron pair cuts:

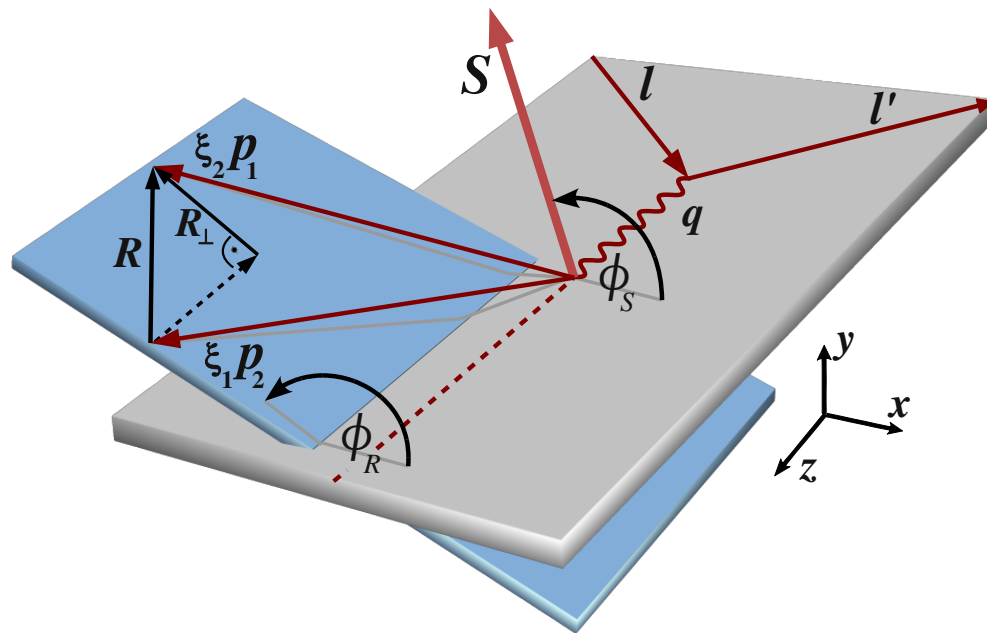
- at least 2 outgoing hadrons with opposite charge
- $z > 0.1$ for each hadron
- $x_F > 0.1$ for each hadron
- $E_{miss} > 3 \text{ GeV}/c^2$ for each pair
- $R_T > 0.07 \text{ GeV}/c$ for each pair



$A_{UT}^{\sin \Phi_{RS}}$ ► framework ► angle definitions

$$l p^\uparrow \rightarrow l' h_1 h_2$$

Fragmentation of transversely polarized quark into two unpolarized hadrons



in courtesy of H. Wollny

- l, l' and q are 3-momenta of incoming l , scattered lepton l' and virtual photon γ^*
- Φ_S azimuthal angle of the spin of the fragmenting quark S
- $z_i = \frac{\mathbf{p}_i}{\mathbf{p}}$
- $\mathbf{R} = \frac{z_2 \mathbf{p}_1 - z_1 \mathbf{p}_2}{z_1 + z_2} = \xi_2 \mathbf{p}_1 - \xi_1 \mathbf{p}_2$
- \mathbf{R}_T is the component of \mathbf{R} perpendicular to \mathbf{q}
- Azimuthal angle of \mathbf{R} :

$$\Phi_R = \frac{(\mathbf{q} \times \mathbf{l}) \cdot \mathbf{R}}{|(\mathbf{q} \times \mathbf{l}) \cdot \mathbf{R}|} \arccos \left(\frac{(\mathbf{q} \times \mathbf{l}) \cdot (\mathbf{q} \times \mathbf{R})}{|\mathbf{q} \times \mathbf{l}| |\mathbf{q} \times \mathbf{R}|} \right)$$

$A_{UT}^{\sin \Phi_{RS}}$ ► framework ► cross section

The differential two-hadron cross section reads:

$$\frac{d^7\sigma}{d\cos\theta dM_h^2 d\Phi_R dz dx dy d\Phi_S} =$$

$$\frac{\alpha^2}{2\pi Q^2 y} \left(\left(1 - y + \frac{y^2}{2}\right) \sum_q e_q^2 f_1^q(x) D_{1,q}(z, M_h^2, \cos\theta) \right.$$

$$\left. + (1 - y) S_\perp \sum_q e_q^2 \frac{|\mathbf{p}_1 - \mathbf{p}_2|}{2M_h} \sin(\theta) h_1^q(x) H_{1,q}^{\triangleleft}(z, M_h^2, \cos\theta) \sin(\Phi_{RS}) \right)$$

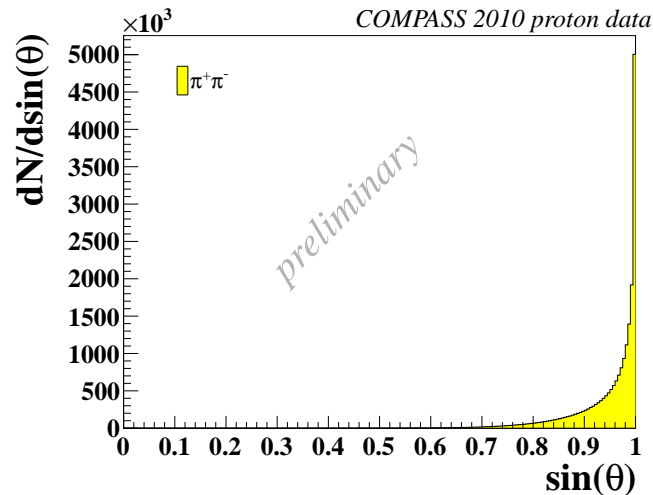
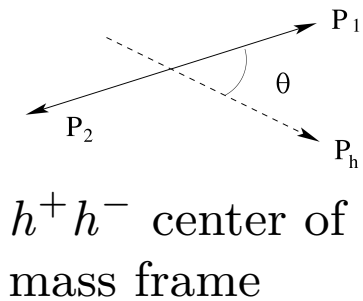
$$\text{with } \Phi_{RS} = \Phi_R + \Phi_S - \pi$$

Where $h_1(x)$ is the Transversity PDF and $H_{1,q}^{\triangleleft}$ is the two-hadron Interference FF, which describes the Fragmentation of a transversely polarized quark into two unpolarized hadrons. $D_{1,q}$ is the unpolarized two-hadron fragmentation function².

² see Nour Makke's talk on hadron multiplicities

$A_{UT}^{\sin \Phi_{RS}}$ ► framework ► asymmetries extraction

$$N_{2h}(x, y, z, M_h^2, \cos(\theta), \Phi_{RS}) \propto \sigma_{UU}(1 \pm fP_T D_{NN} A_{UT}^{\sin \Phi_{RS}} \sin \theta \sin \Phi_{RS})$$



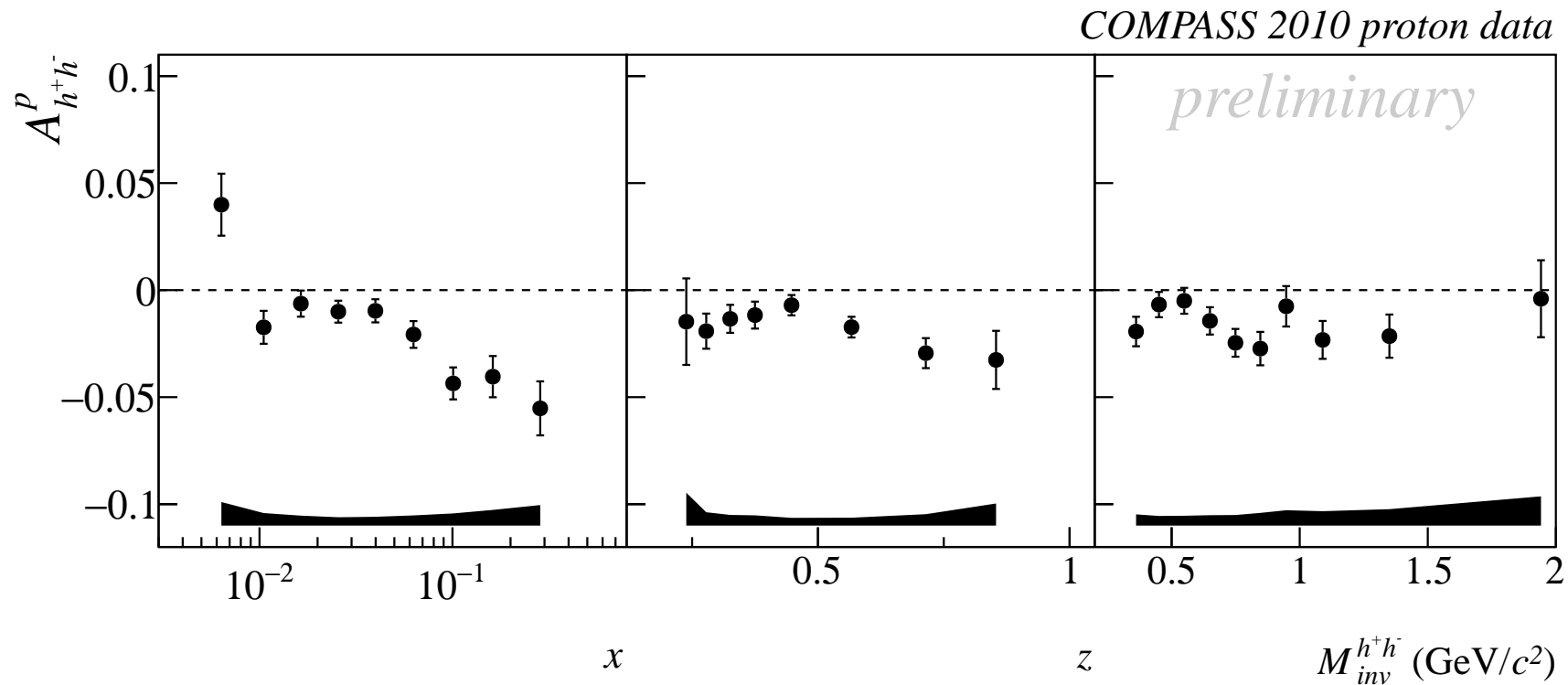
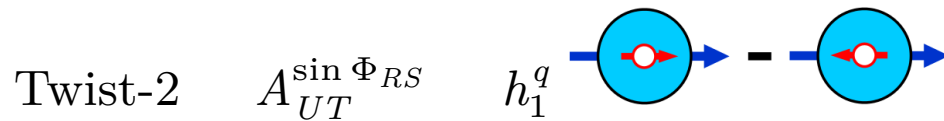
σ_{UU} = unpolarized cross section
 \pm indicates nucleon spin orientation
 f = target dilution factor
 P_T = target polarization
 D_{NN} = transv. spin transfer coef.

$$D_{NN} = \frac{1-y}{1-y+\frac{y^2}{2}}$$

$\langle \sin \theta \rangle = 0.943$
 \Rightarrow can be neglected

$$A_{UT}^{\sin \Phi_{RS}} = \frac{|\mathbf{p}_1 - \mathbf{p}_2|}{2M_h} \frac{\sum_q e_q^2 h_1^q(x) H_{1,q}^{\triangleleft}(z, M_h^2, \cos \theta)}{\sum_q e_q^2 f_1^q(x) D_{1,q}(z, M_h^2, \cos \theta)}$$

$A_{UT}^{\sin \Phi_{RS}}$ ► charged hadrons ► 2010 data



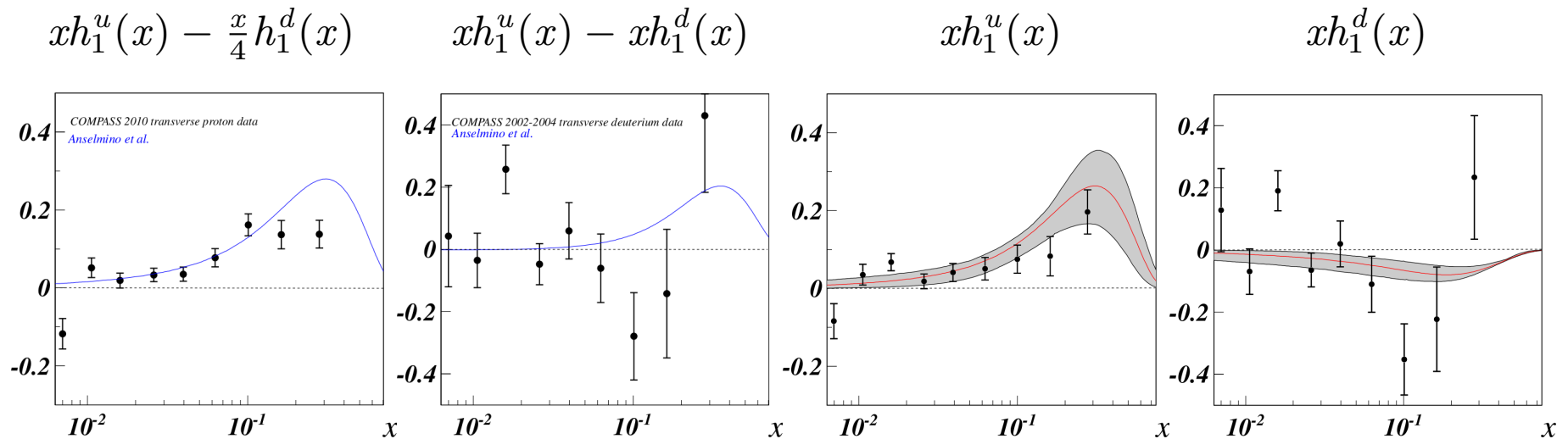
↔ Clear asymmetries of h^+h^- with improved errors *w.r.t.* 2007 data

TRANSVERSITY 2011 proceedings:
Braun C. *o.b.o.* the COMPASS Collab. Nuovo Cimento C **035** (2012) 02

$A_{UT}^{\sin \Phi_{RS}}$ ► 1st extraction of u and d transversity from 2010 proton data

Extract information on DiFF from BELLE data as in "Bacchetta, Courtoy, Radici, PRL 107:012001,2011"

→ u and d transversity PDFs can be extracted using COMPASS deuterium and 2010 proton data

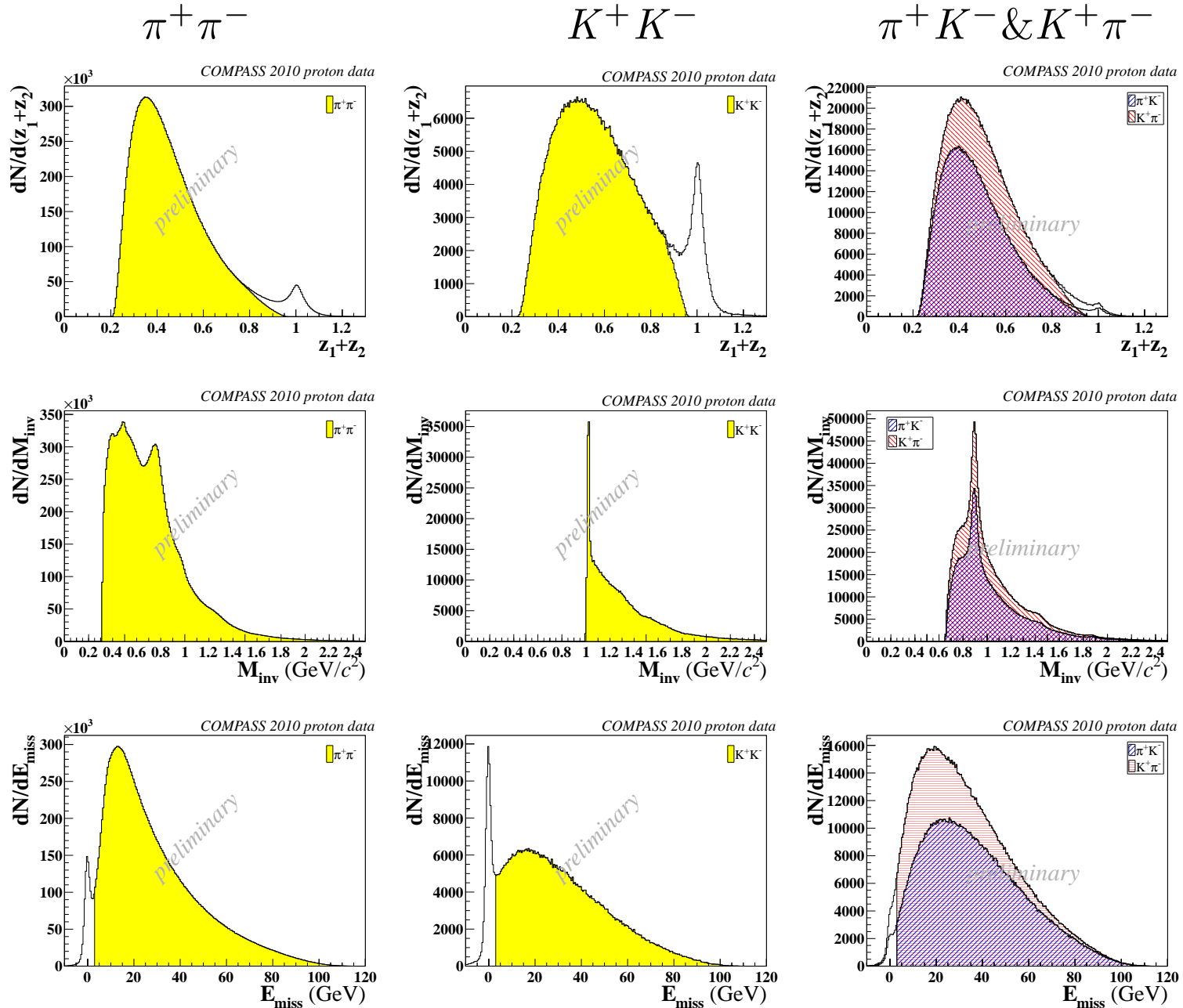


PhD thesis C. Elia, Trieste 2011 & F. Sozzi at IWHSS 2012

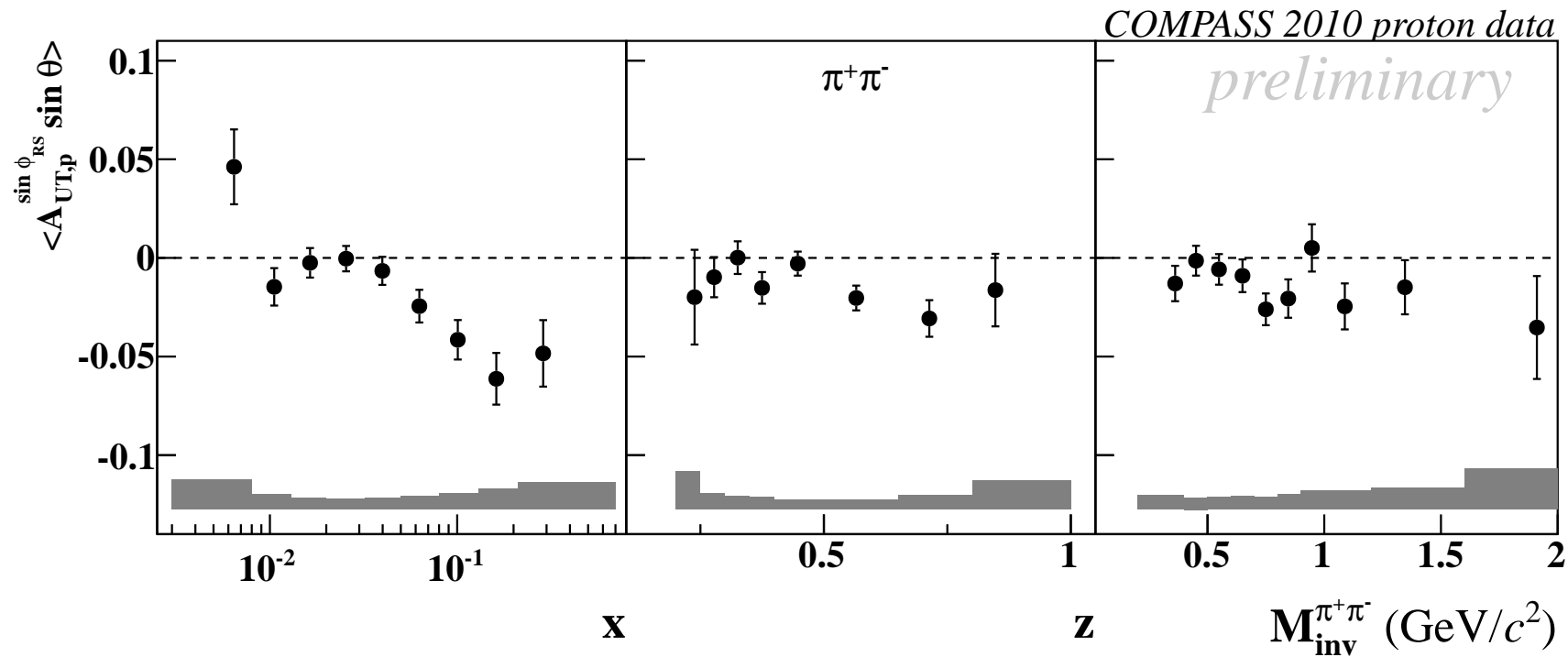
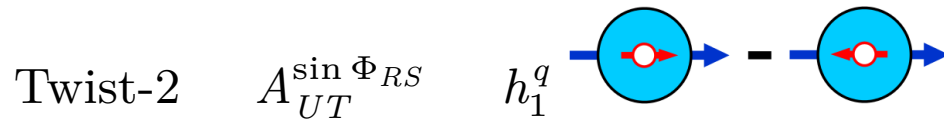
See also DIS2012 proceeding by

A. Courtoy, A. Bacchetta & M. Radici, arXiv:1206.1836

► kin. distributions $z_1 + z_2$, M_{inv} and E_{miss}

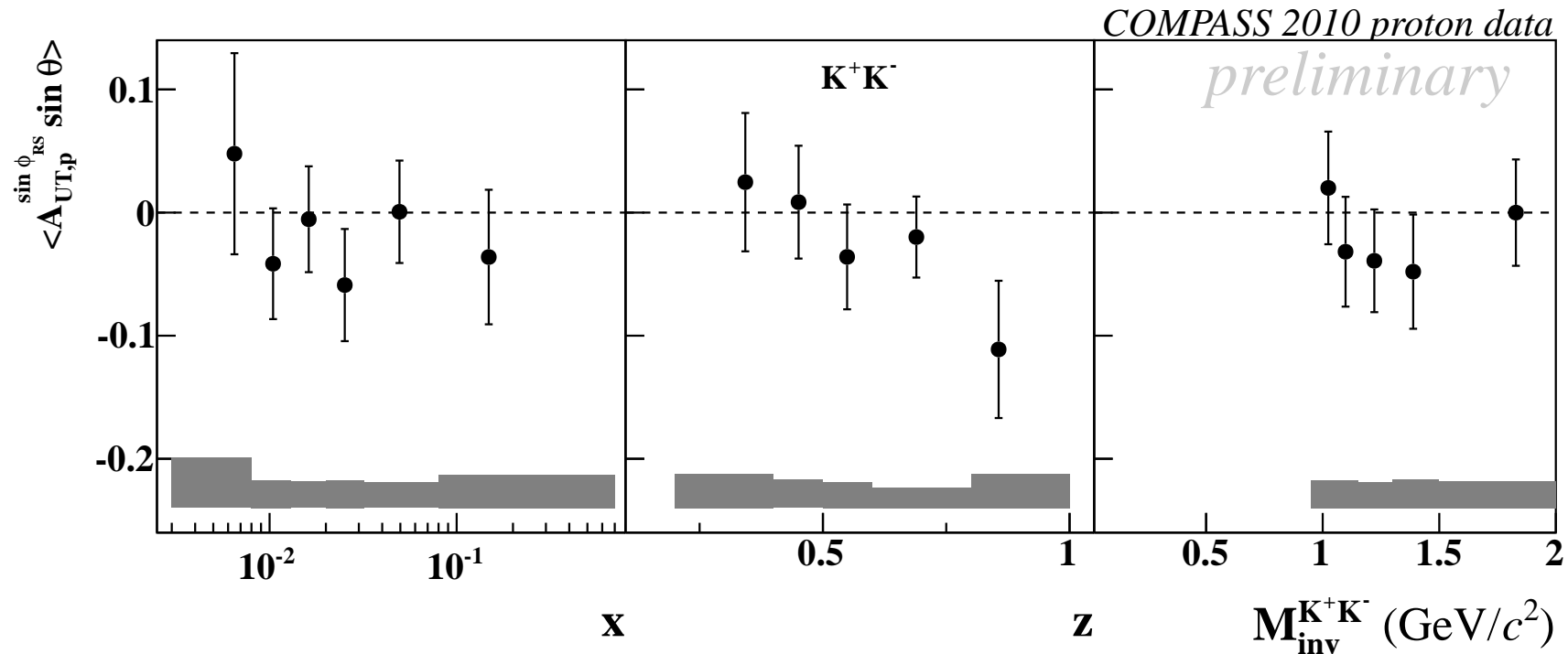
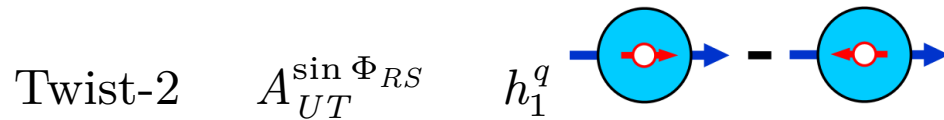


$A_{UT}^{\sin \Phi_{RS}}$ \triangleright $\pi^+ \pi^-$ pairs \triangleright p 2010 data



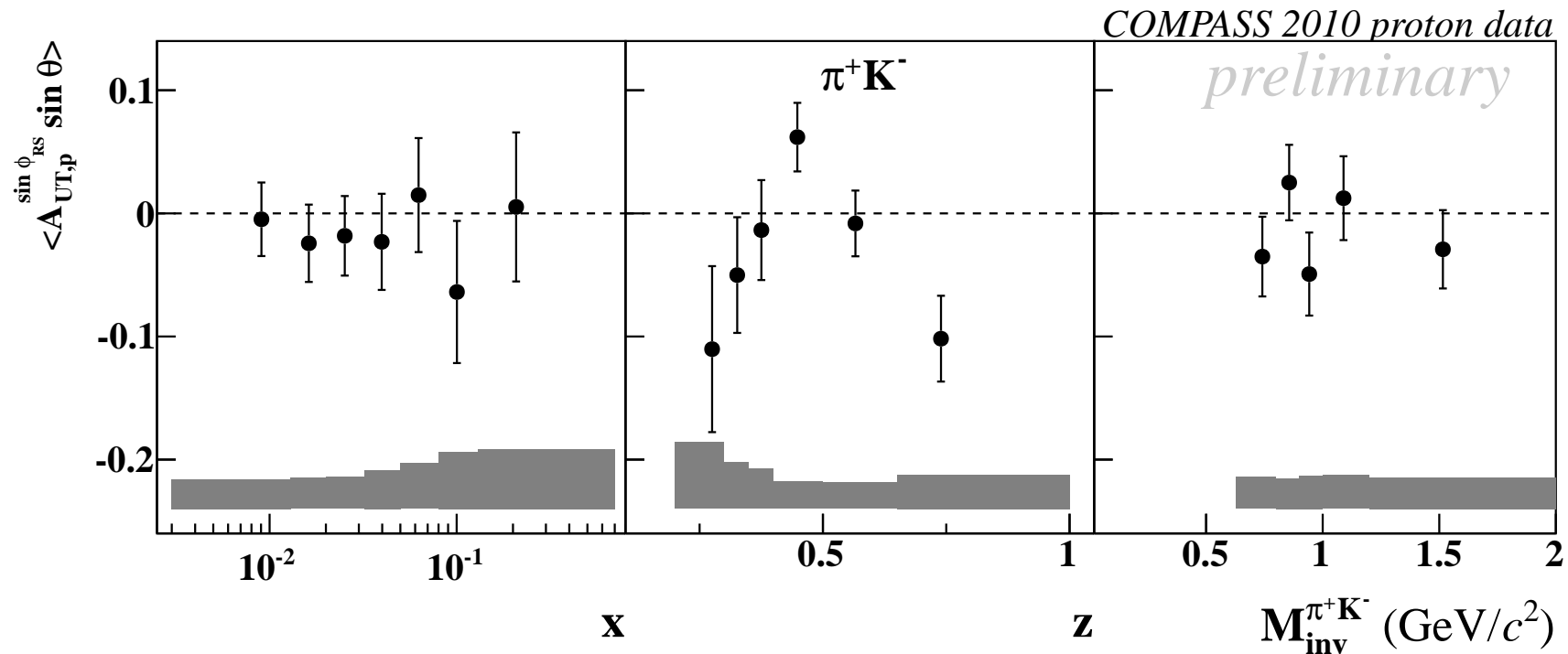
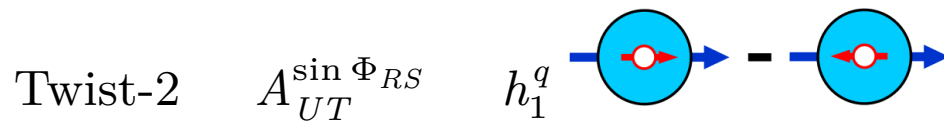
- \hookrightarrow Clear asymmetries of $\pi^+ \pi^-$ pairs $\hookrightarrow x$: up to 6 %
- $\hookrightarrow z$: compatible with a constant function
- $\hookrightarrow M_{inv}$: peak around ρ^0 mass

$A_{UT}^{\sin \Phi_{RS}}$ \blacktriangleright $K^+ K^-$ pairs \blacktriangleright p 2010 data



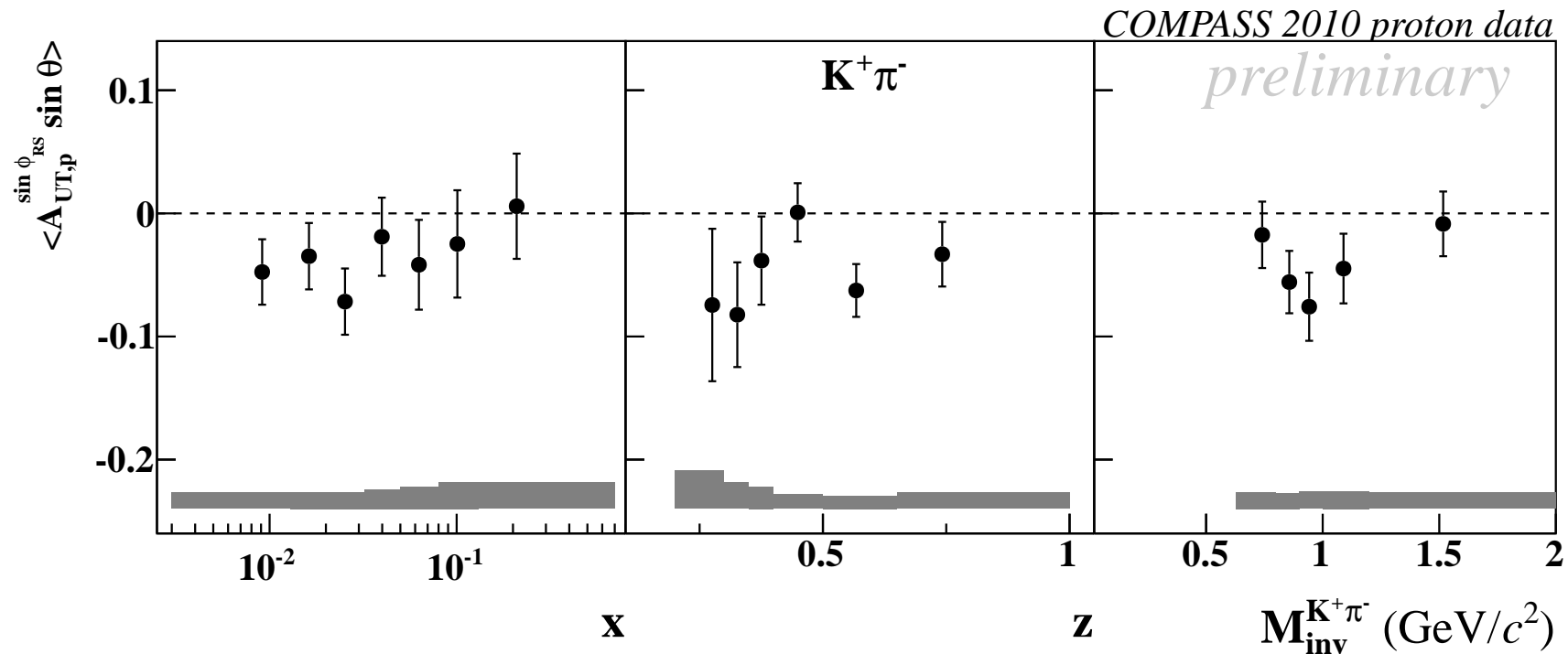
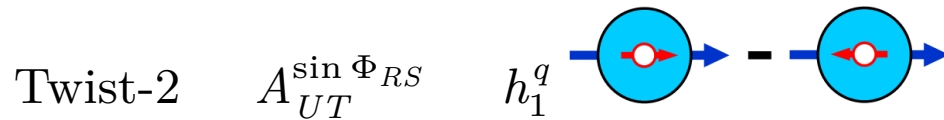
- \hookrightarrow no clear trend & compatible with 0 within the statistical errors
- \hookrightarrow no signal in x and z
- \hookrightarrow M_{inv} : negative mean value

$A_{UT}^{\sin \Phi_{RS}}$ \blacktriangleright $\pi^+ K^-$ pairs \blacktriangleright 2010 data



- \hookrightarrow no clear trend & compatible with 0 within the statistical errors
- $\hookrightarrow x$: no signal
- $\hookrightarrow z$: negative mean value with positive peak around 0.45
- $\hookrightarrow M_{inv}$: no signal

$A_{UT}^{\sin \Phi_{RS}}$ \blacktriangleright $K^+ \pi^-$ pairs \blacktriangleright 2010 data

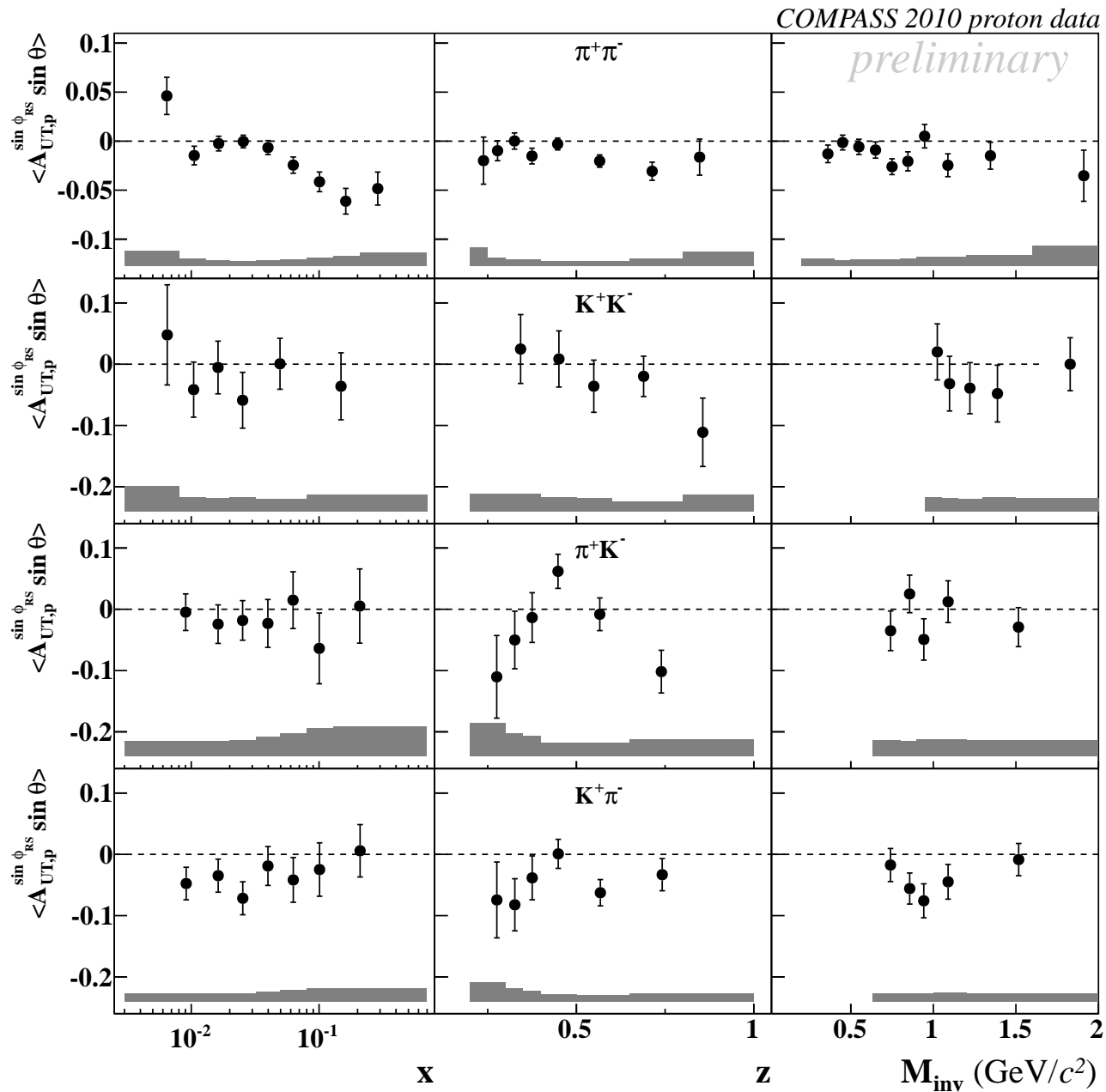


\hookrightarrow compatible with 0 within the statistical errors $\hookrightarrow x$: negative mean value

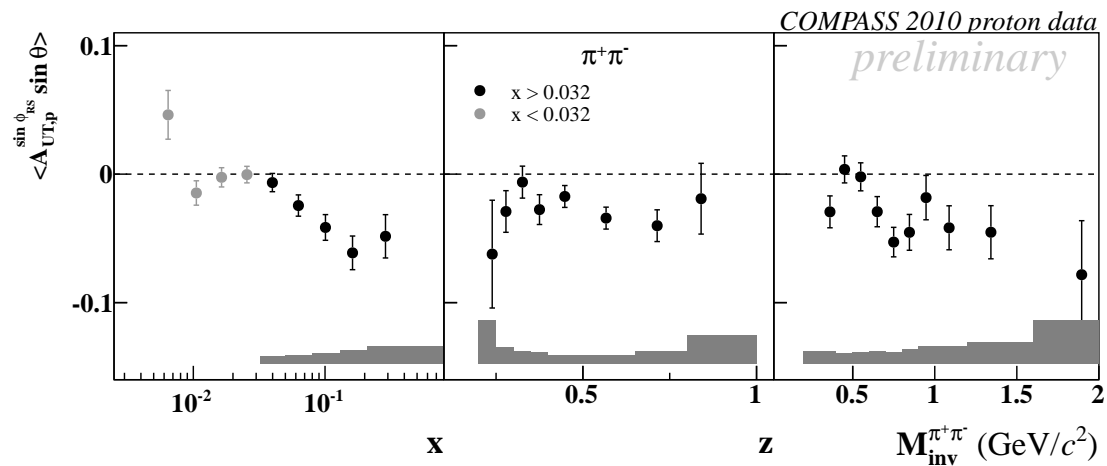
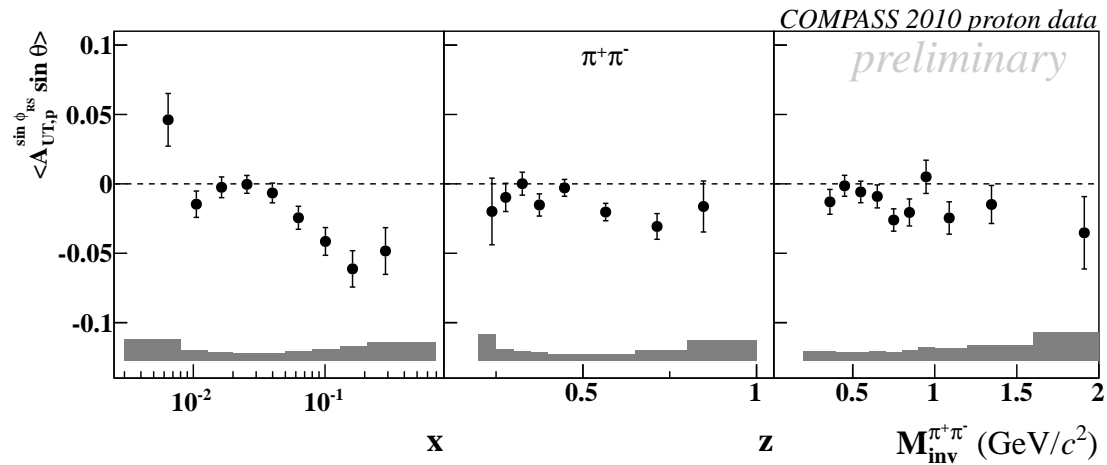
$\hookrightarrow z$: negative mean value

$\hookrightarrow M_{inv}$: negative peak around $0.9 \text{ GeV}/c^2$

$A_{UT}^{\sin \Phi_{RS}}$ ► identified pairs ► 2010 data



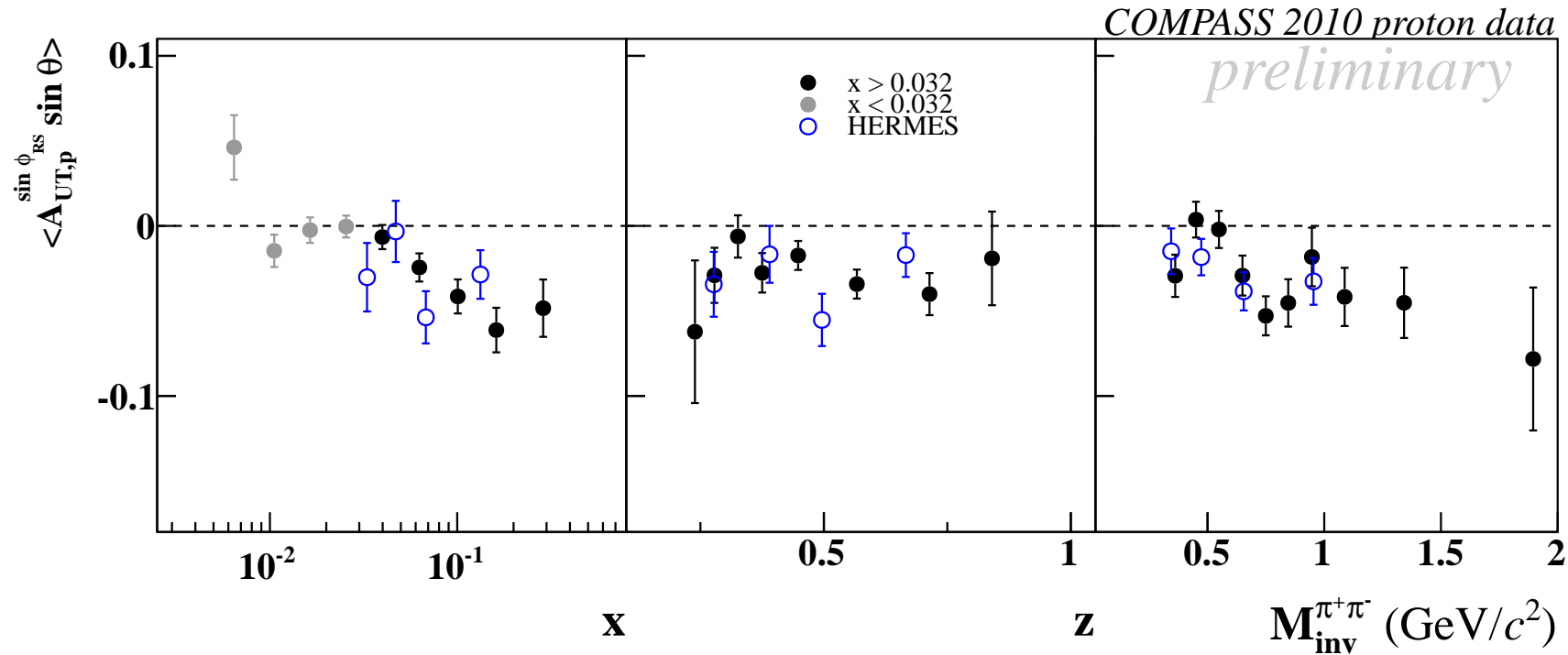
$A_{UT}^{\sin \Phi_{RS}}$ ► $\pi^+\pi^-$ valence region ► 2010 data



↪ $\pi^+\pi^-$ valence region $x_{bj} > 0.032$

clear signal around ρ^0 mass is pronounced in valence region sample

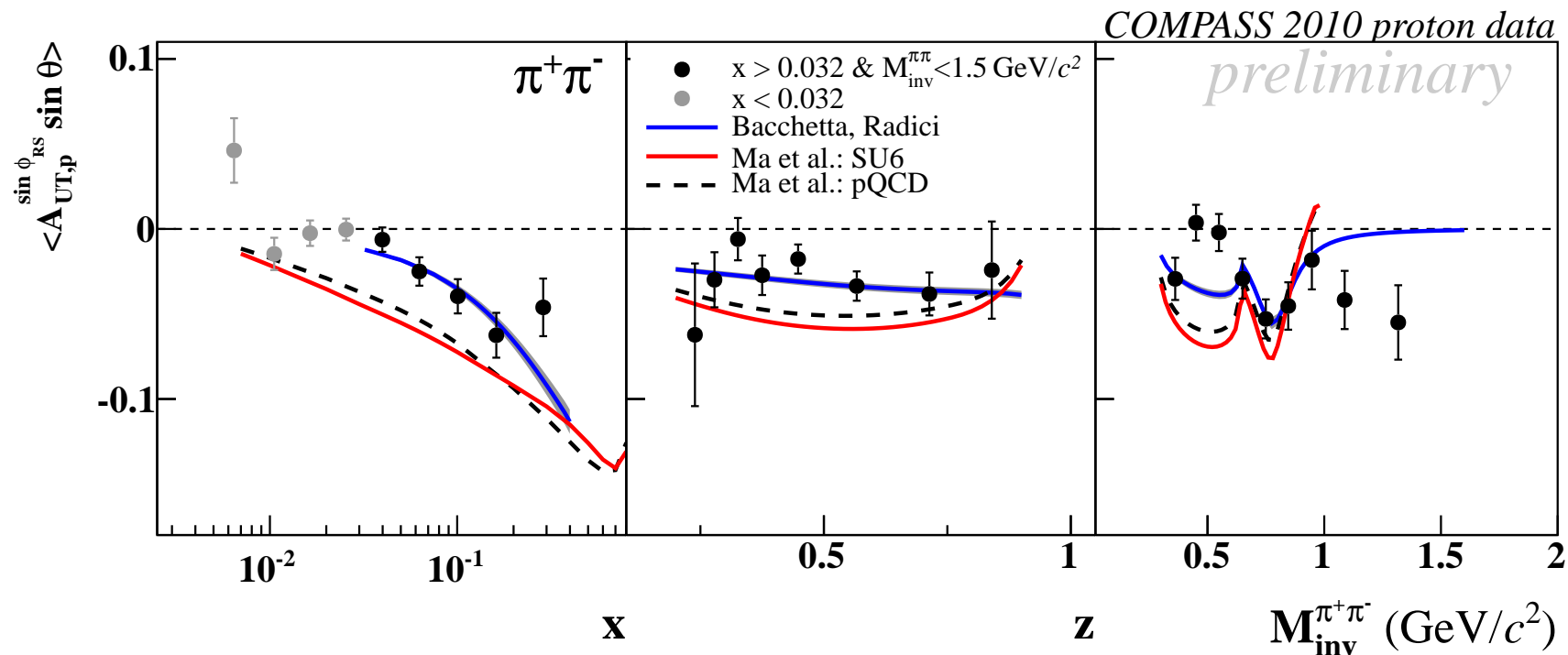
$A_{UT}^{\sin \Phi_{RS}}$ $\pi^+ \pi^-$ \blacktriangleright HERMES *vs.* COMPASS data



Airapetian *et. al.*, JHEP, **06** (2008) 017 scaled with $\frac{1}{D_{nn}}$ and sign changed

\hookrightarrow Good agreement of COMPASS $\pi^+ \pi^-$ data, with its higher precision, with HERMES $\pi^+ \pi^-$ data within the error bars

$A_{UT}^{\sin \Phi_{RS}}$ $\pi^+\pi^-$ valence region \blacktriangleright COMPASS *vs.* model predictions



Bacchetta *et al.*, hep-ph/0608037
Ma *et al.*, arXiv:0711.0817

- $\hookrightarrow x_{bj}$: Ma trend confirmed | Bacchetta good agreement
- $\hookrightarrow z$: compatible within the errors
- $\hookrightarrow M_{inv}$: good agreement around ρ^0 mass

Conclusions

- Clear signals of Collins and Sivers asymmetries on proton target for charged and identified hadrons
- Interesting kinematical dependences for different z and y ranges
- New inputs to study Q^2 evolution and for the extraction of Transversity and Sivers PDFs
- Six beyond-Collins-and-Sivers transverse spin asymmetries on proton and deuteron
- Non-zero trend for the $A_{LT}^{\cos(\phi_h - \phi_S)}$ and $A_{UT}^{\sin \phi_S}$ amplitudes
- Interesting kinematical dependencies of unpolarized asymmetries investigated in the x , z and p_T^h grid
- For the first time COMPASS proton data on transverse spin asymmetries in identified dihadron production
 - ▶ $\pi^+ \pi^-$ also measured by HERMES
 - ▶ $K^+ K^-$, $\pi^+ K^-$ and $K^+ \pi^-$ never measured before
- Important new input for the extraction of the Transversity PDF

Outlook

- Multi-dimensional analysis in x , z , p_T^h and Q^2 using proton data
- Possible measurements with:
 - ▶ transversely polarized proton target at 100 GeV/ c to further investigate on Q^2 evolution
 - ▶ transversely polarized deuteron target to improve the extraction of u and d quarks PDFs
- Other six asymmetries for pions and kaons
- New measurement starting from 2015 of the unpolarized azimuthal asymmetries at COMPASS II with a LH-target in parallel to DVCS
- Combined 2007/2010 results on identified dihadron asymmetries

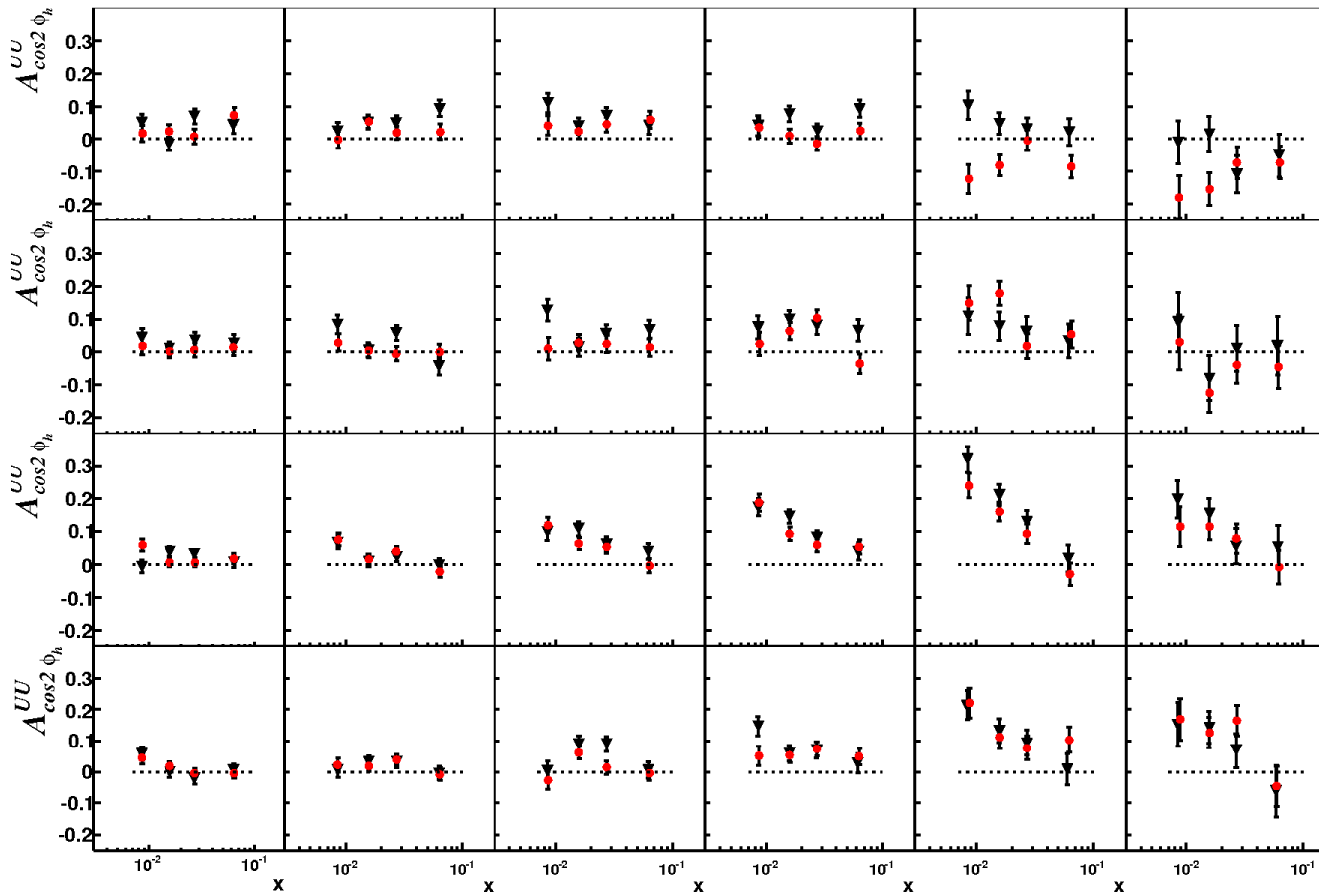
Thank you for your attention!

electronic address: christopher.braun@cern.ch

Back up

A_{UU2} ► charged hadrons ► 2004 data preliminary

COMPASS⁶LiD (25% of 2004 data)



↑ p_T^h ; → z

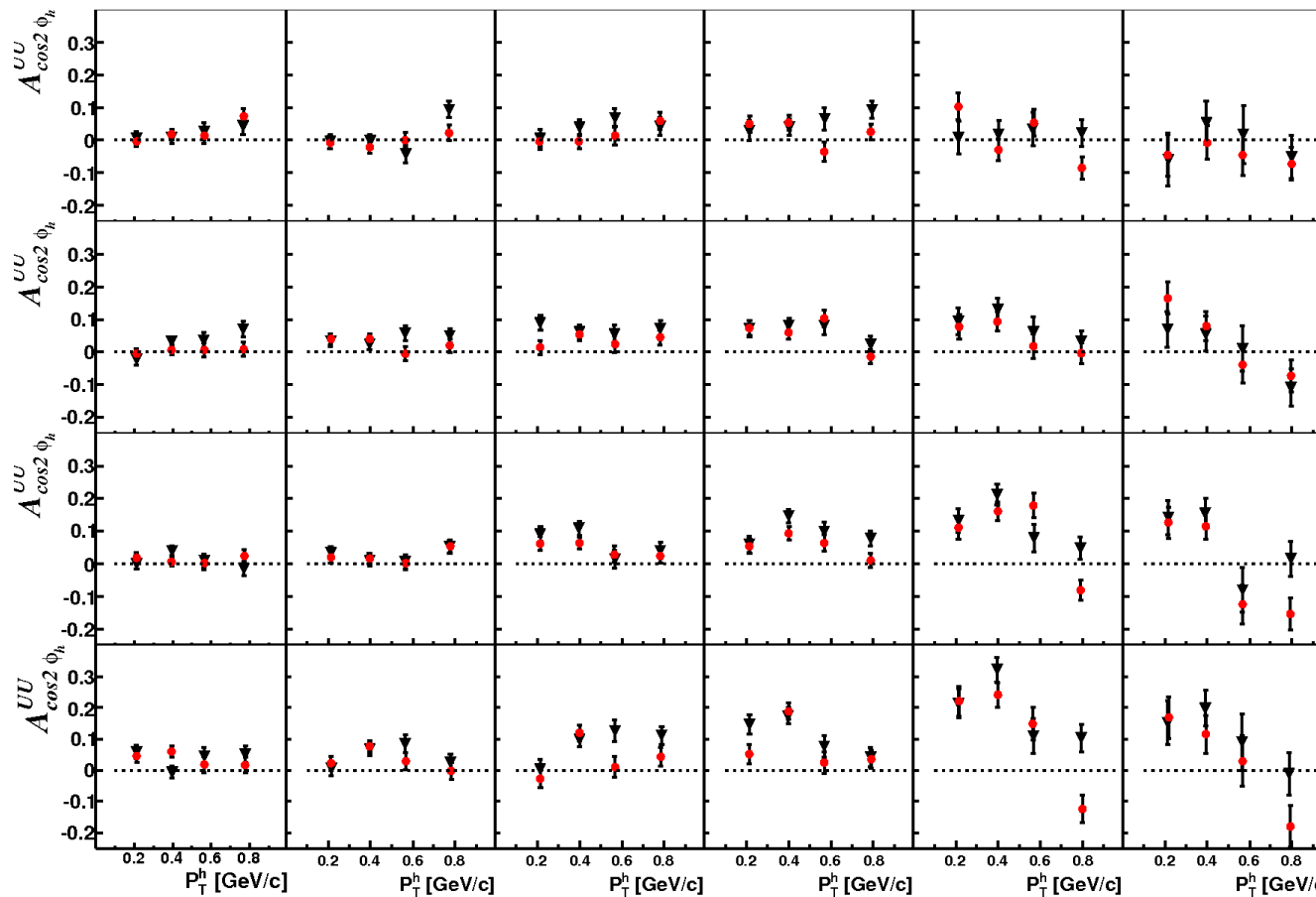
$\sigma_{sys} \approx 2 \cdot \sigma_{stat}$

⇒ largest difference between h^+ and h^- at large p_T^h
 ⇒ x trend changes going from small to large z values

same as for $A_{UU}^{\cos \Phi_h}$

A_{UU2} ► charged hadrons ► 2004 data preliminary

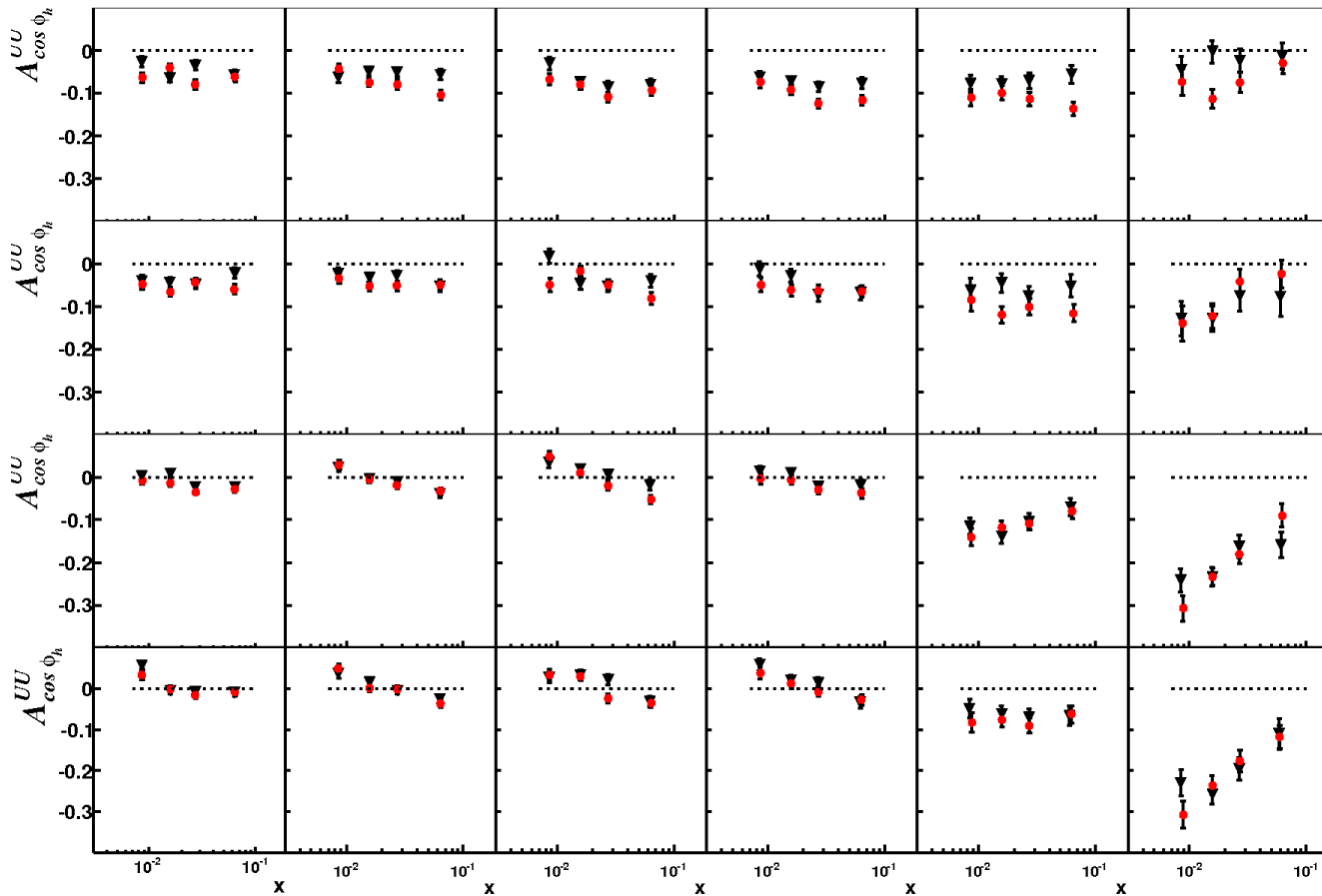
COMPASS⁶LiD (25% of 2004 data)



$\hookrightarrow p_T^h$ trend changes going from small to large z values
 \hookrightarrow The p_T^h trend, which is difficult to reproduce by models originates from large z and low x

A_{UU1} ► charged hadrons ► 2004 data preliminary

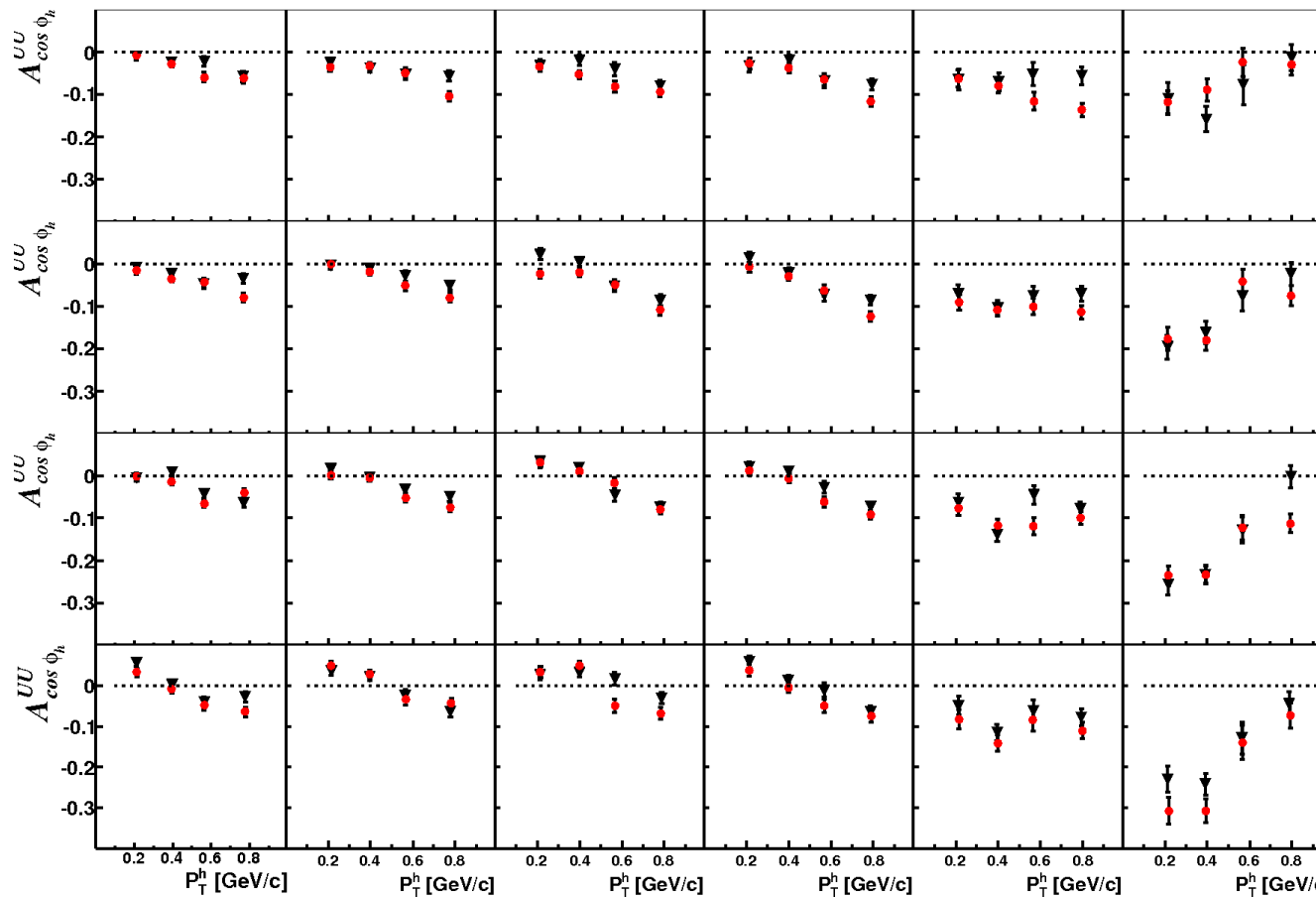
COMPASS⁶LiD (25% of 2004 data)



\hookrightarrow largest difference between h^+ and h^- at large p_T^h
 \hookrightarrow x trend changes going from small to large z values

A_{UU1} ► charged hadrons ► 2004 data preliminary

COMPASS⁶LiD (25% of 2004 data)

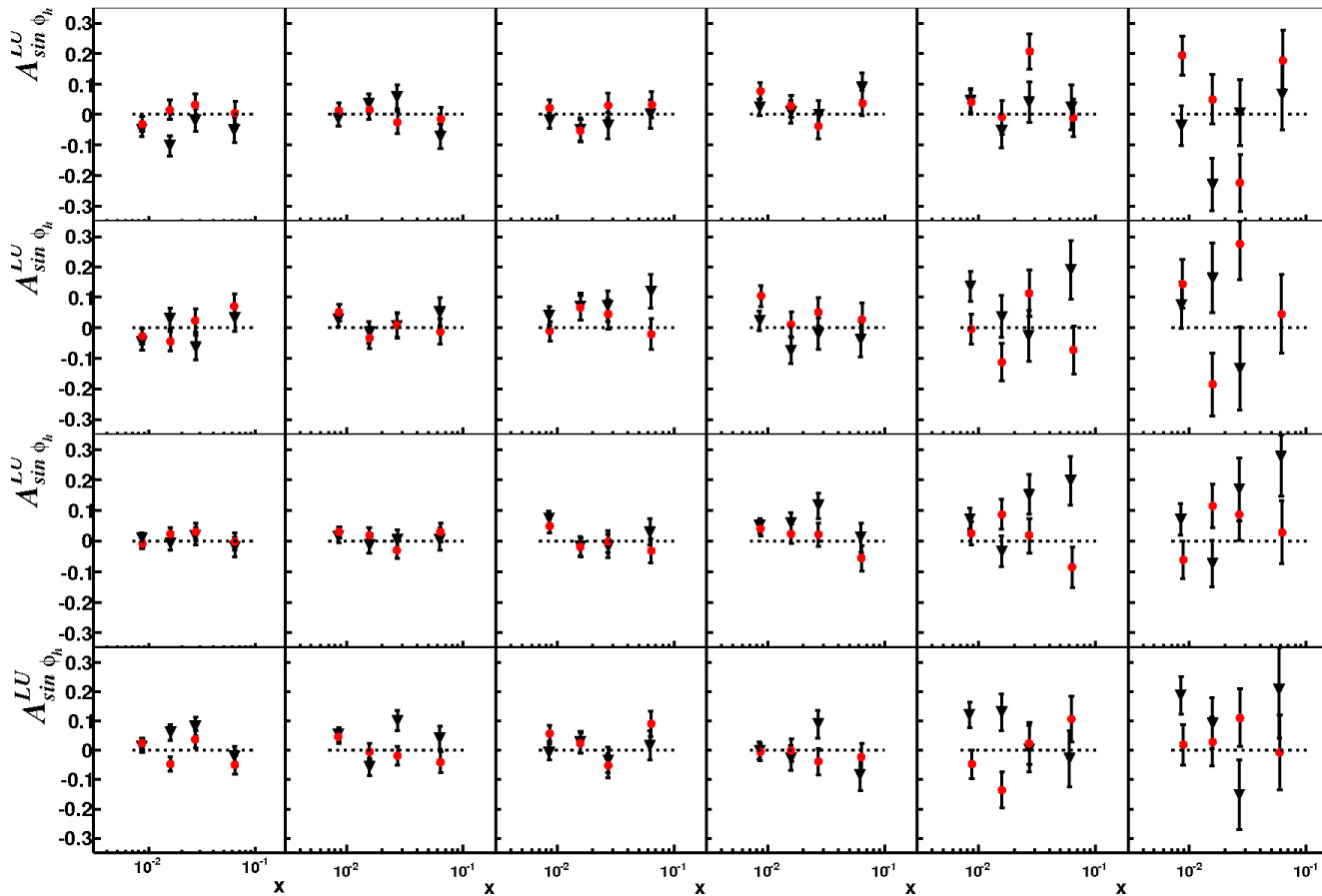


$$\sigma_{sys} \approx 2 \cdot \sigma_{stat}$$

- ↪ p_T^h trend changes going from small to large z values
- ↪ roughly same trend for all x intervals

$A_{LU} \blacktriangleright$ charged hadrons \blacktriangleright 2004 data preliminary

COMPASS⁶LiD (25% of 2004 data)



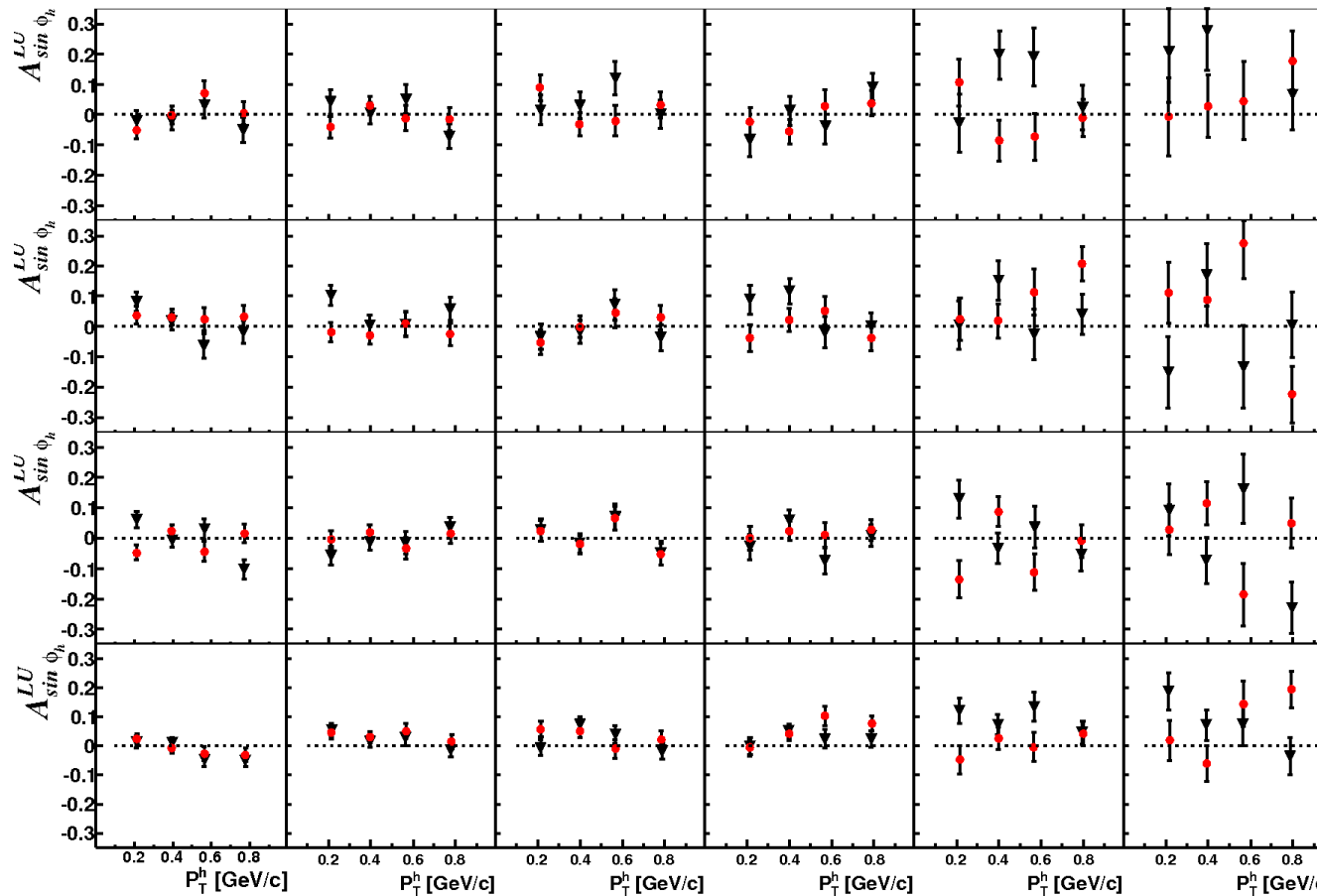
$\uparrow p_T^h; \rightarrow z$

$\sigma_{sys} \approx 2 \cdot \sigma_{stat}$

\hookrightarrow no significant signal within the uncertainties

A_{LU} ► charged hadrons ► 2004 data preliminary

COMPASS⁶LiD (25% of 2004 data)



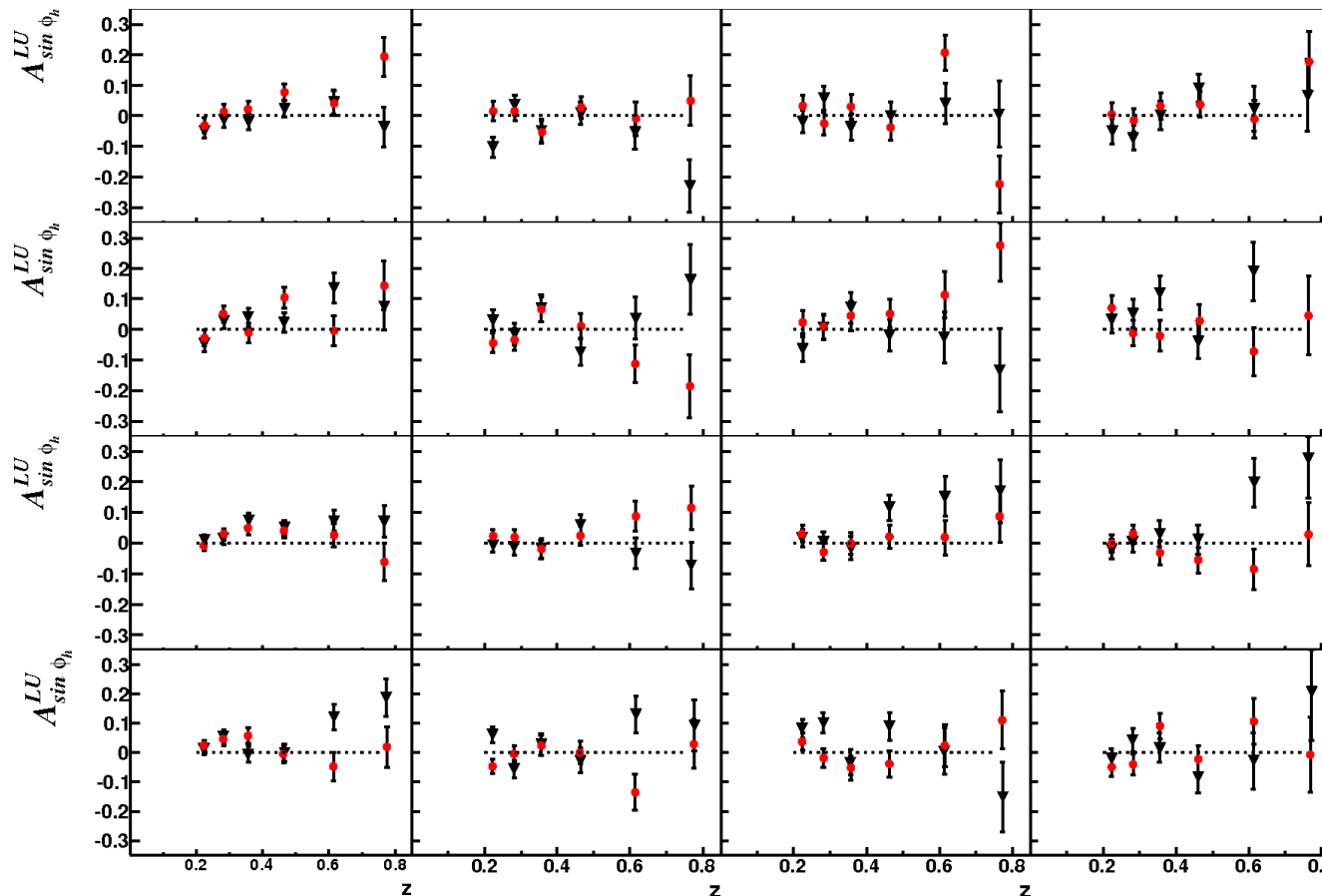
↑ x ; → z

$\sigma_{sys} \approx 2 \cdot \sigma_{stat}$

↔ some opposite trend for negative and positive charged hadrons visible

A_{LU} ► charged hadrons ► 2004 data preliminary

COMPASS⁶LiD (25% of 2004 data)

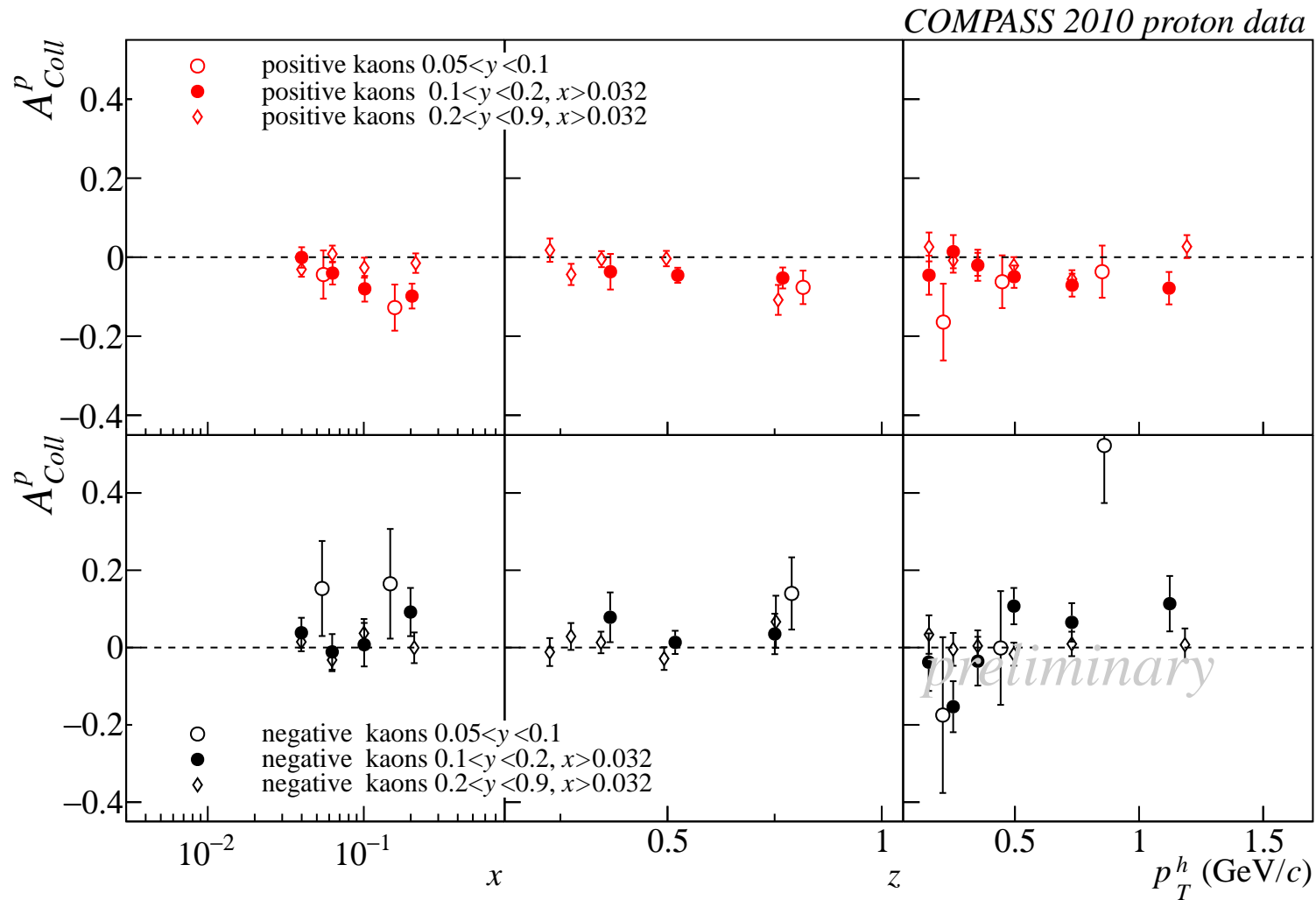


$\uparrow p_T^h; \rightarrow x$

$z\sigma_{sys} \approx 2 \cdot \sigma_{stat}$

↔ some opposite trend for negative and positive charged hadrons visible

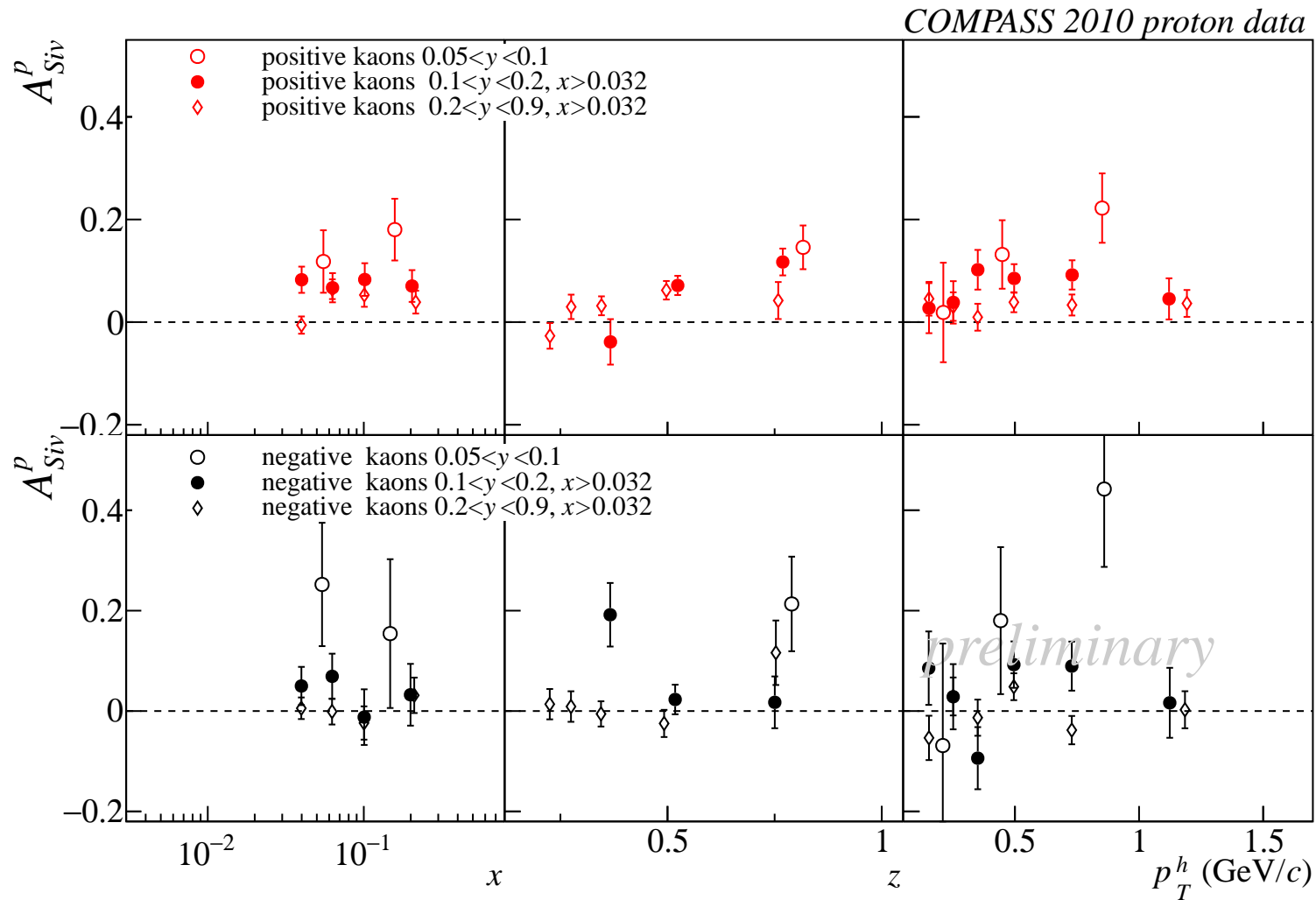
Collins asymmetry ► kaons ► multi-dimensional analysis in y



3 y ranges: $0.05 < y_{\text{low}} < 0.1 < y_{\text{mid}} < 0.2 < y_{\text{high}} < 0.9$

↪ no significant systematic effect *w.r.t.* the uncertainties

Sivers asymmetry ► kaons ► multi-dimensional analysis in y

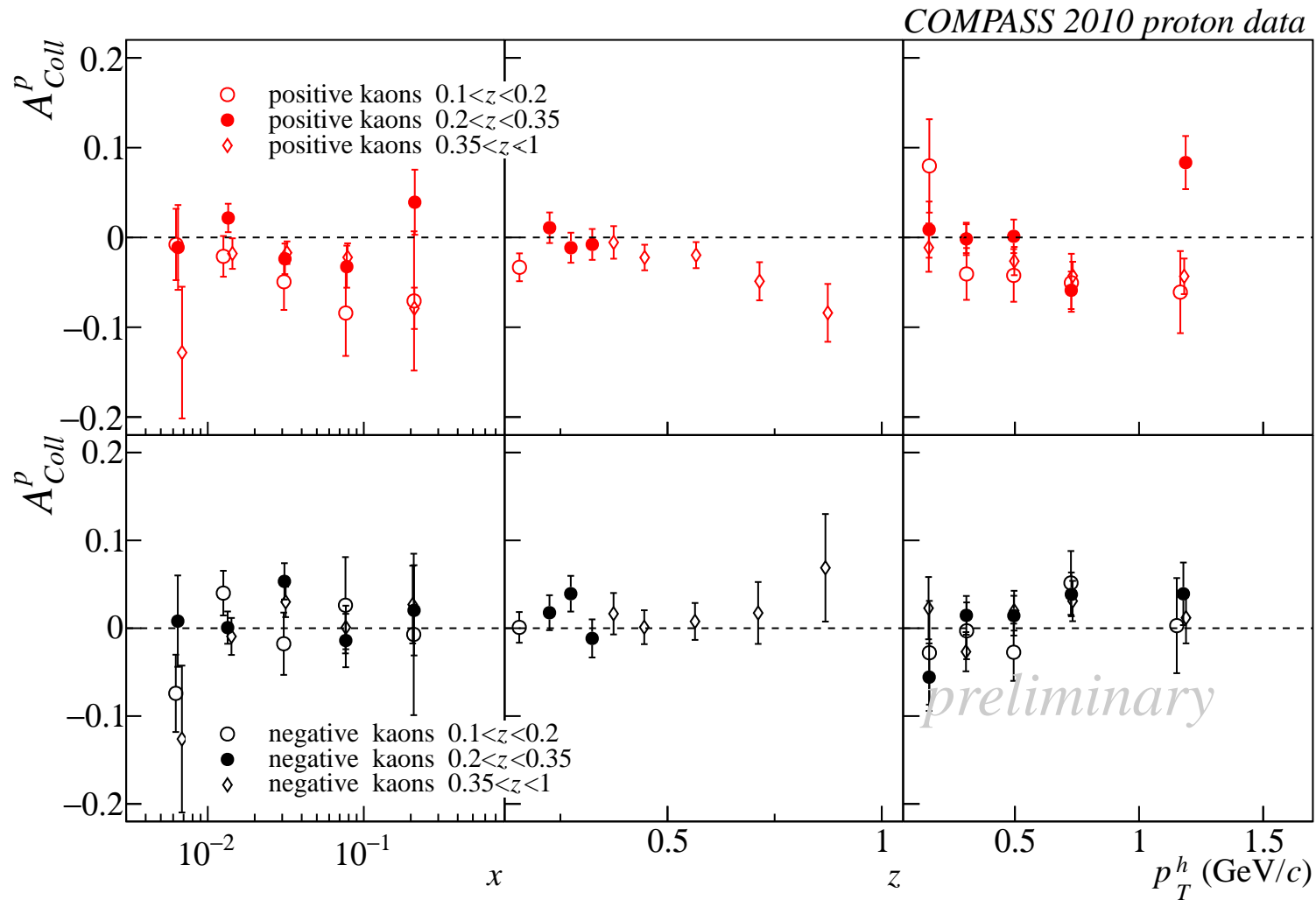


3 y ranges: $0.05 < y_{\text{low}} < 0.1 < y_{\text{mid}} < 0.2 < y_{\text{high}} < 0.9$

↪ very low statistics in y_{low} sample

↪ y_{mid} sample shows larger asymmetries than y_{high} sample

Collins asymmetry ► kaons ► multi-dimensional analysis in z

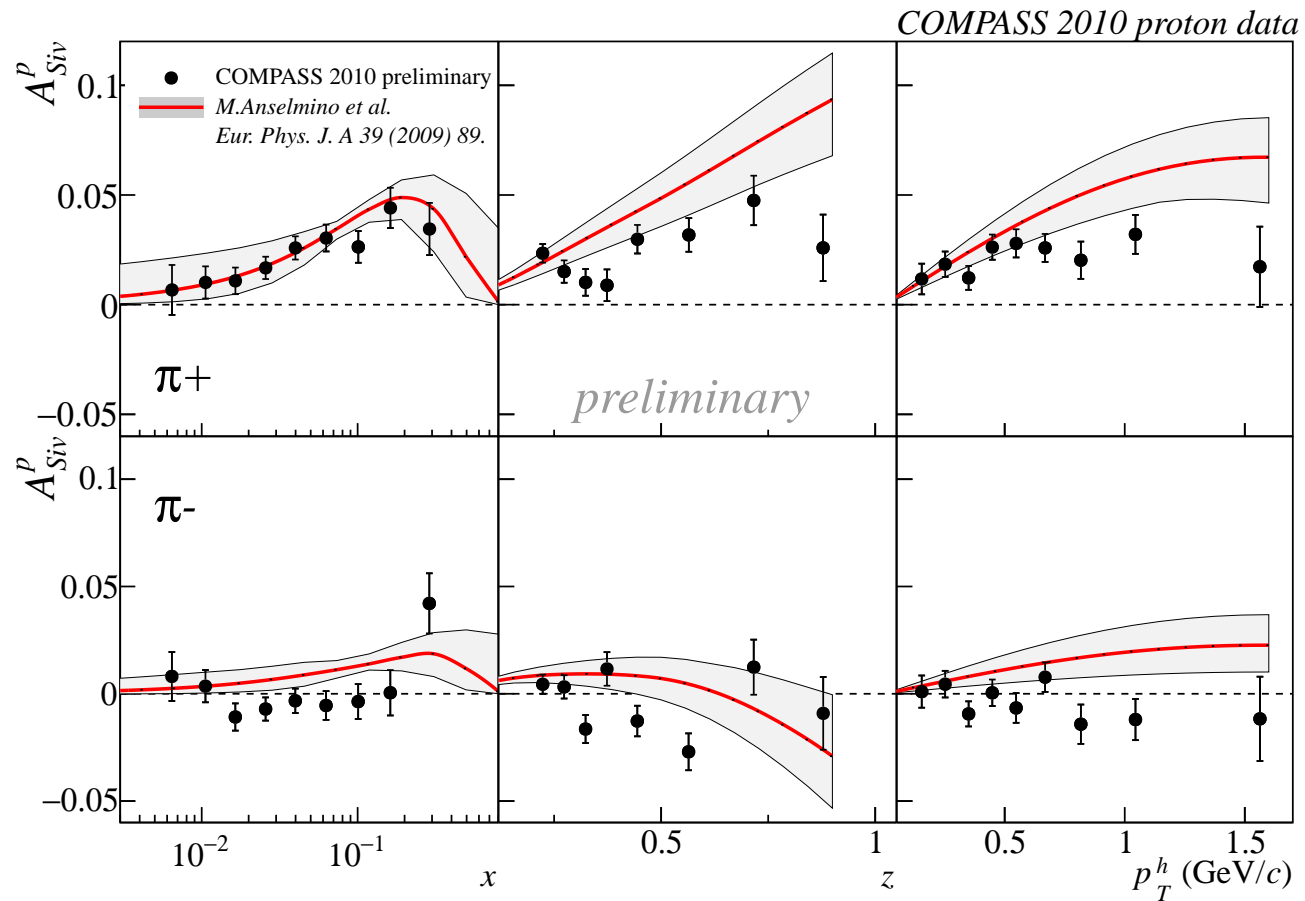


3 z ranges: $0.1 < z_{\text{low}} < 0.2 < z_{\text{mid}} < 0.35 < z_{\text{high}} < 1.0$

↪ larger asymmetries for K^+ in z_{low} region

↪ but large statistical uncertainties

Sivers asymmetry ► pions ► 2010 data *vs.* model predictions

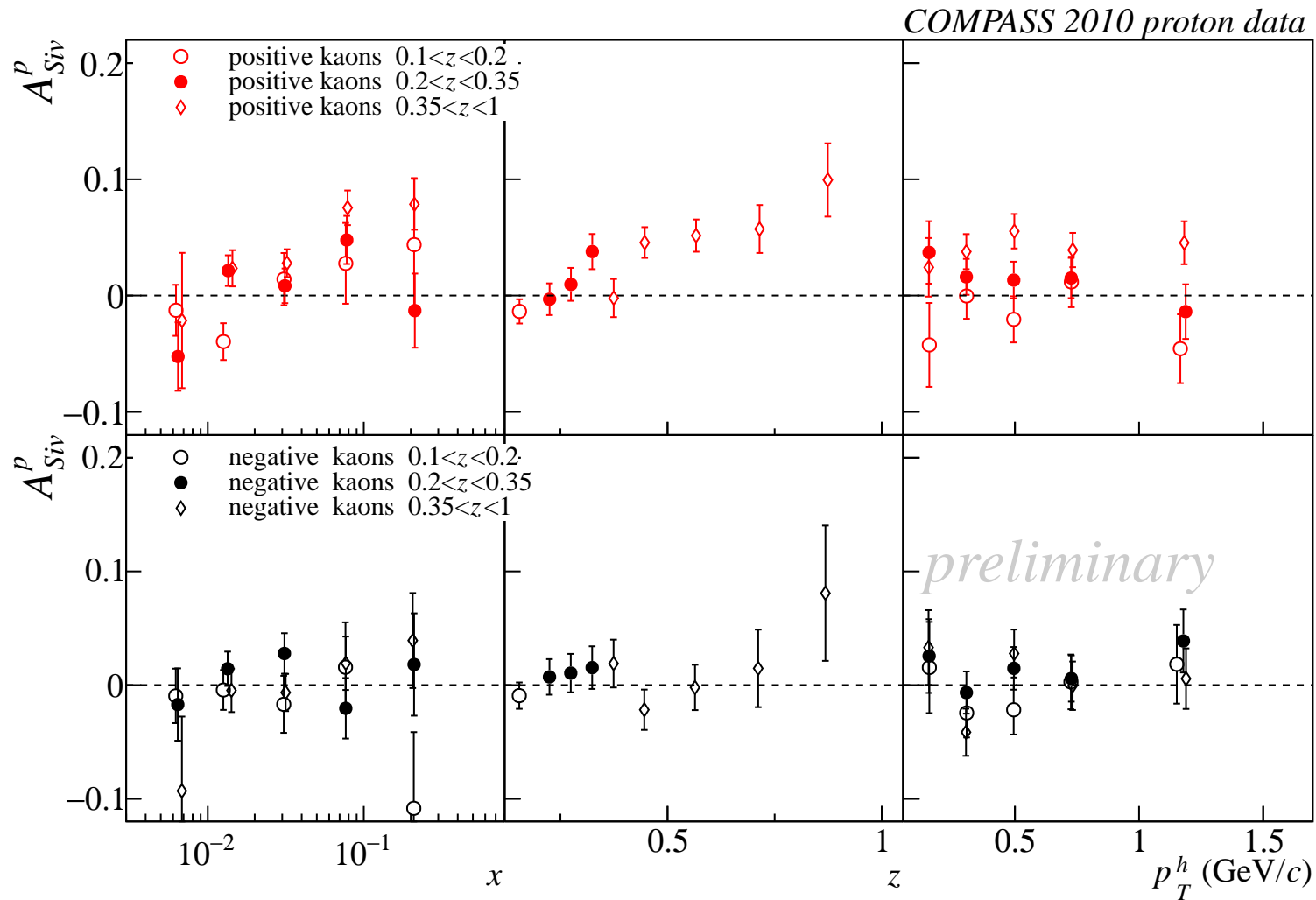


↪ π^+ : good agreement in x

↪ π^+ : predictions are larger than data for z & p_T^h

↪ π^- : less compatible, indication for opposite sign in x and p_T^h

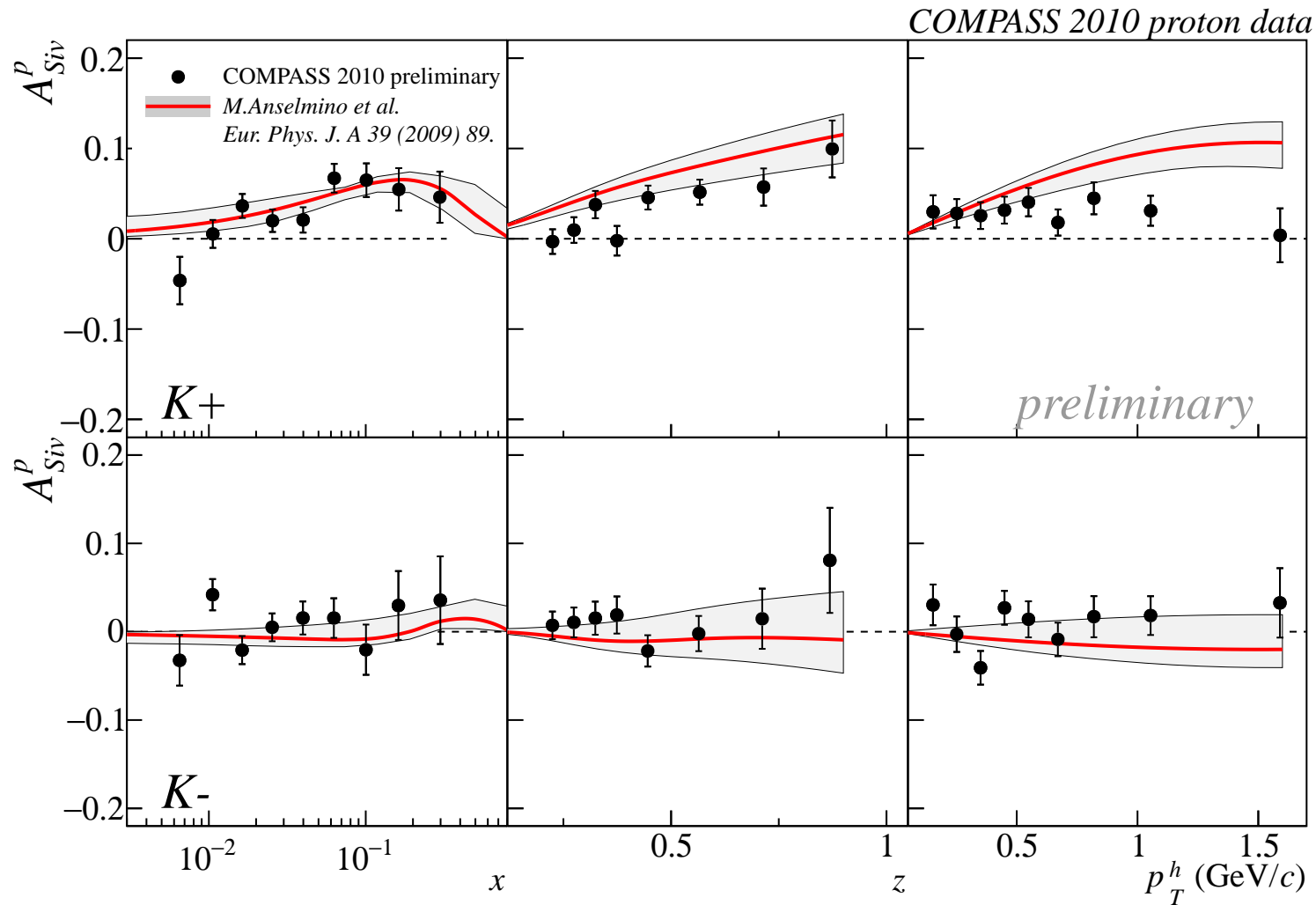
Sivers asymmetry ► kaons ► multi-dimensional analysis in z



3 z ranges: $0.1 < z_{\text{low}} < 0.2 < z_{\text{mid}} < 0.35 < z_{\text{high}} < 1.0$

↪ indication of different sign in p_T^h dependence for low and high z_{low} sample

Sivers asymmetry ► kaons ► 2010 data *vs.* model predictions

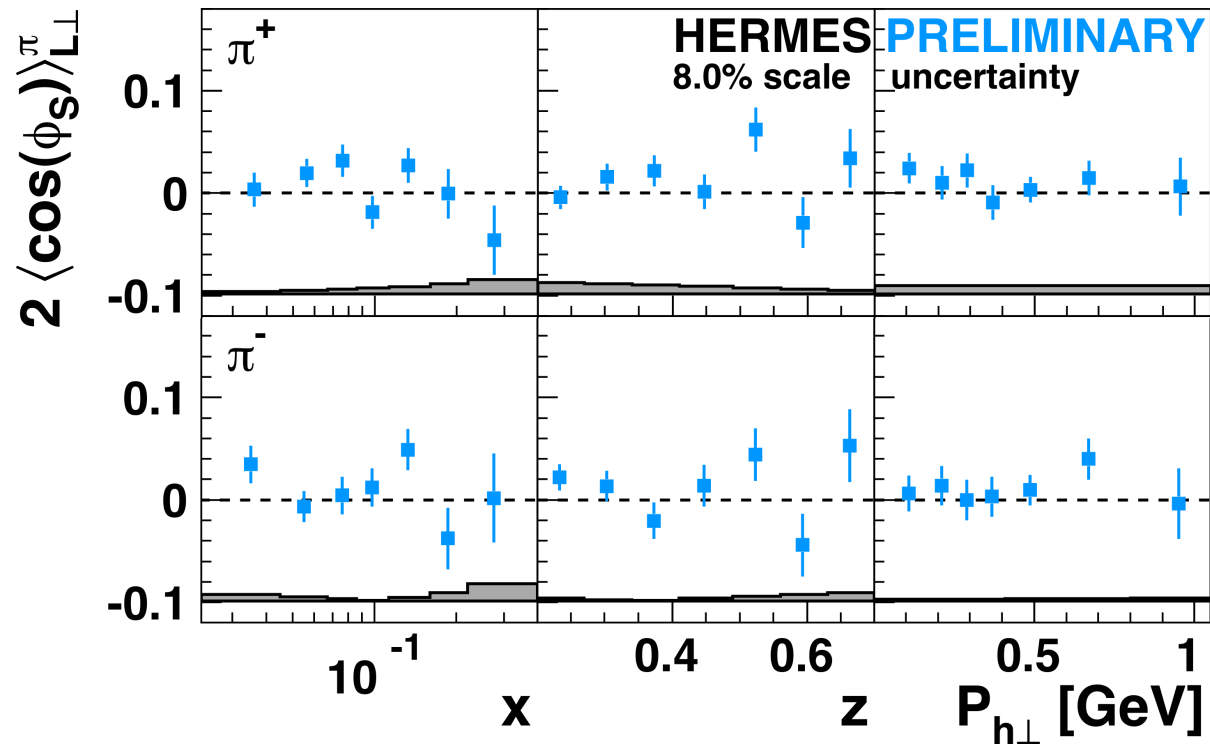
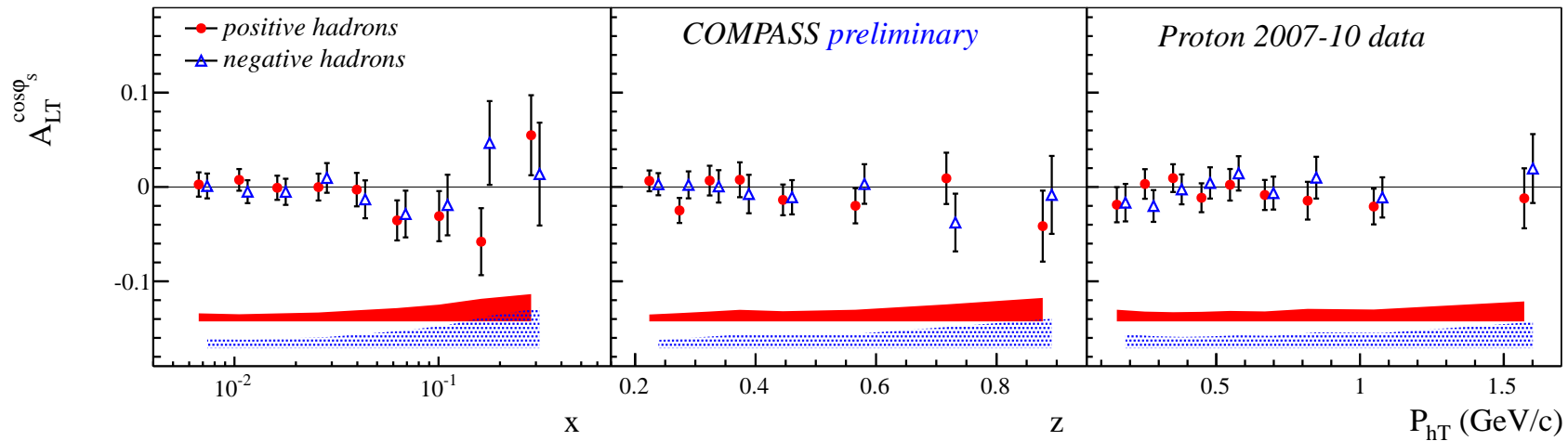


↪ good agreement in x and z within the uncertainties for $K^{+/-}$

↪ K^+ : overestimated for p_T^h dependence

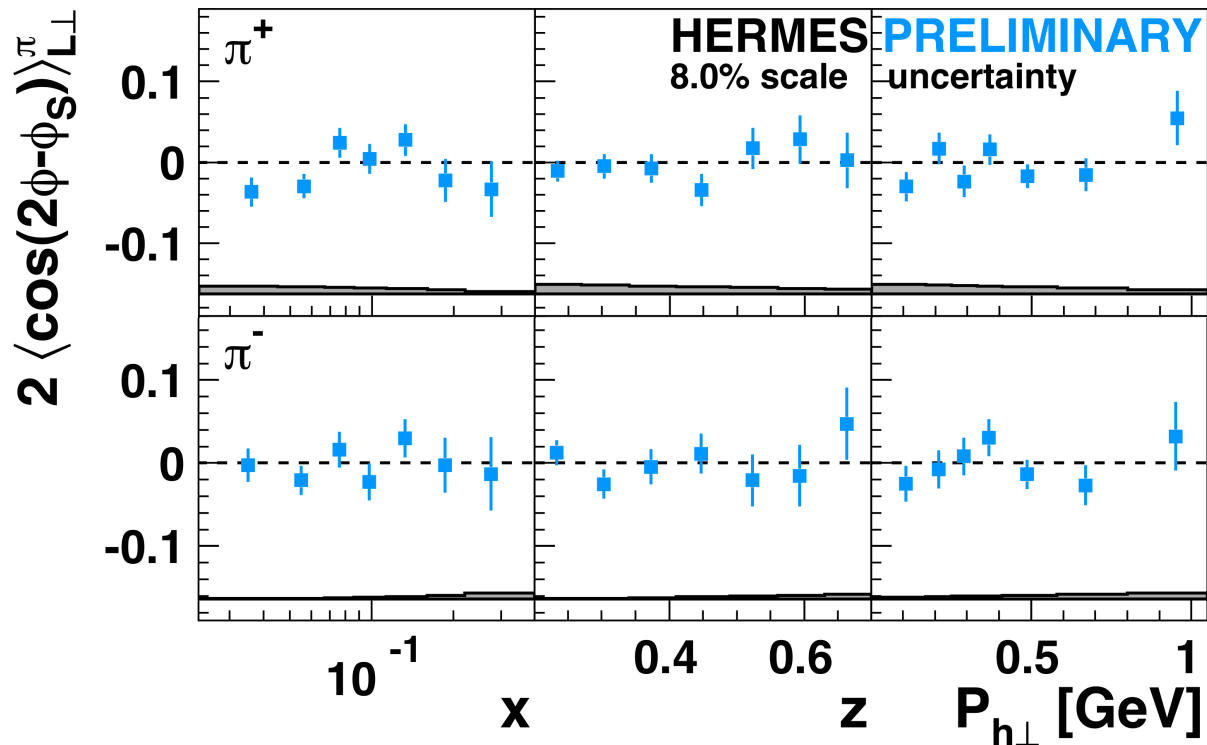
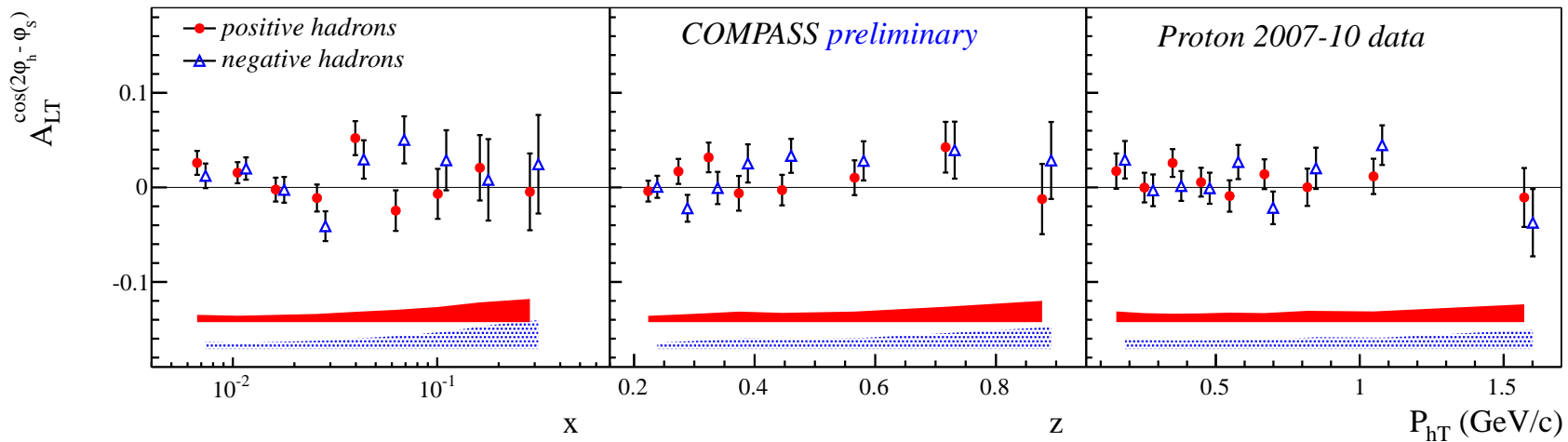
↪ K^- : model and data compatible with zero in p_T^h

A_{LT1} ► charged hadrons ► HERMES *vs.* COMPASS



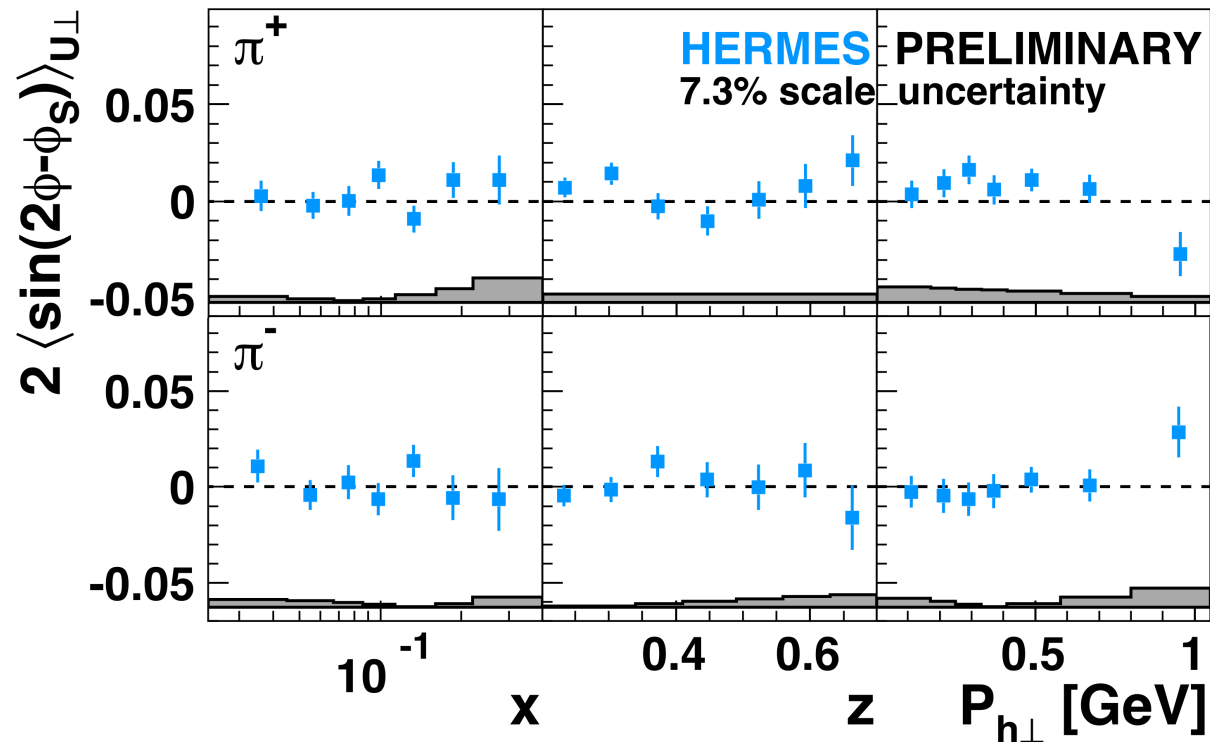
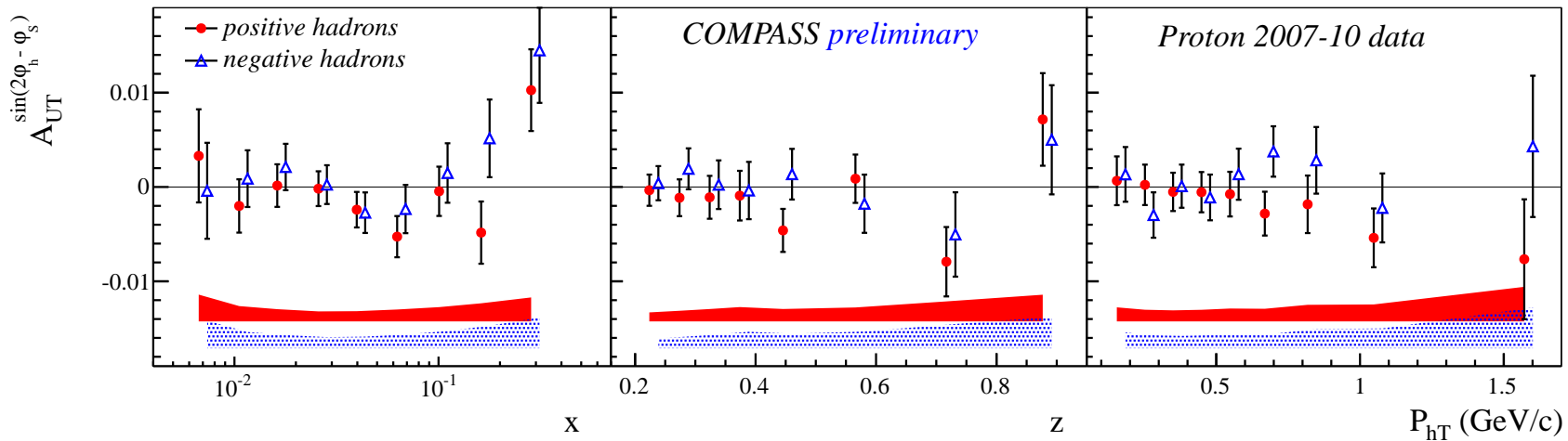
↪ compatible with zero within the uncertainties for both HERMES and COMPASS

A_{LT2} ► charged hadrons ► HERMES *vs.* COMPASS



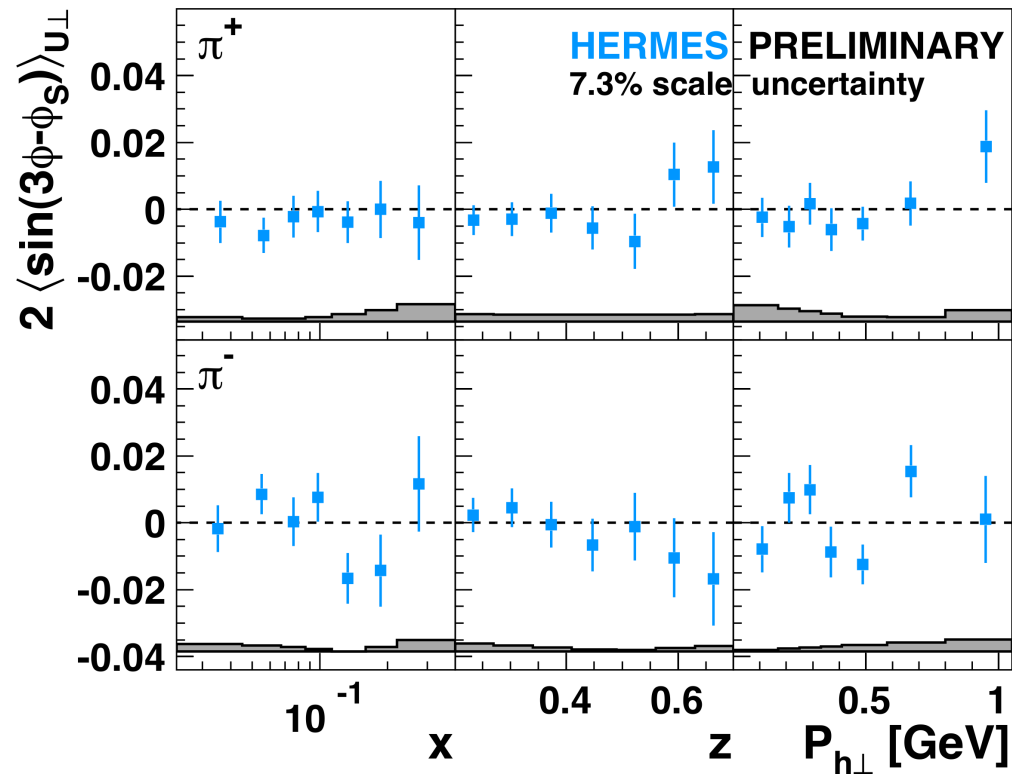
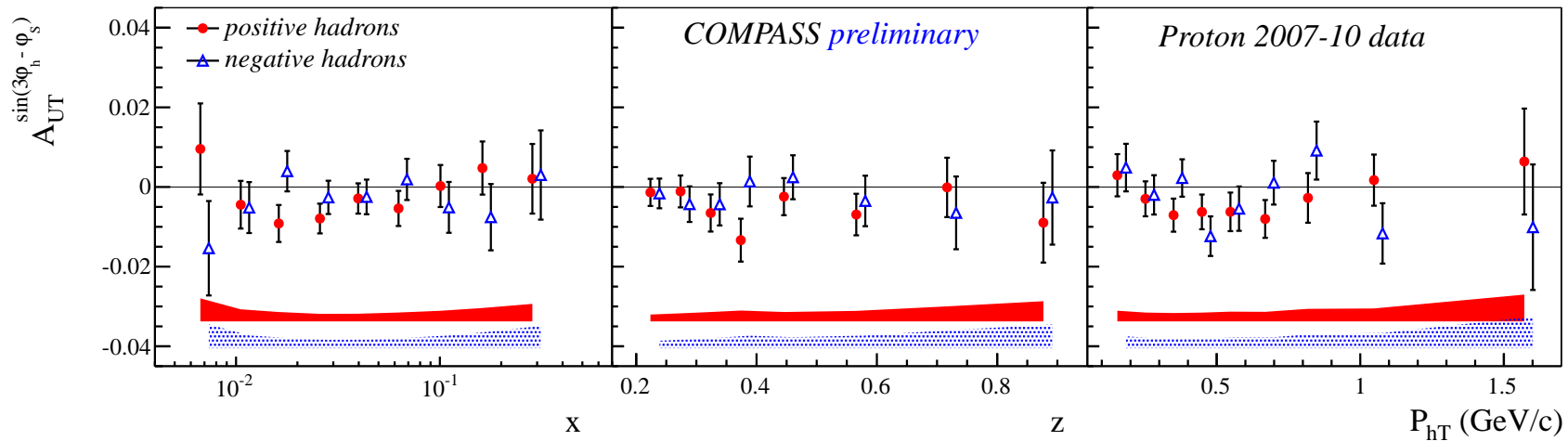
↪ compatible with zero within the uncertainties for both HERMES and COMPASS

A_{UT2} ► charged hadrons ► HERMES *vs.* COMPASS



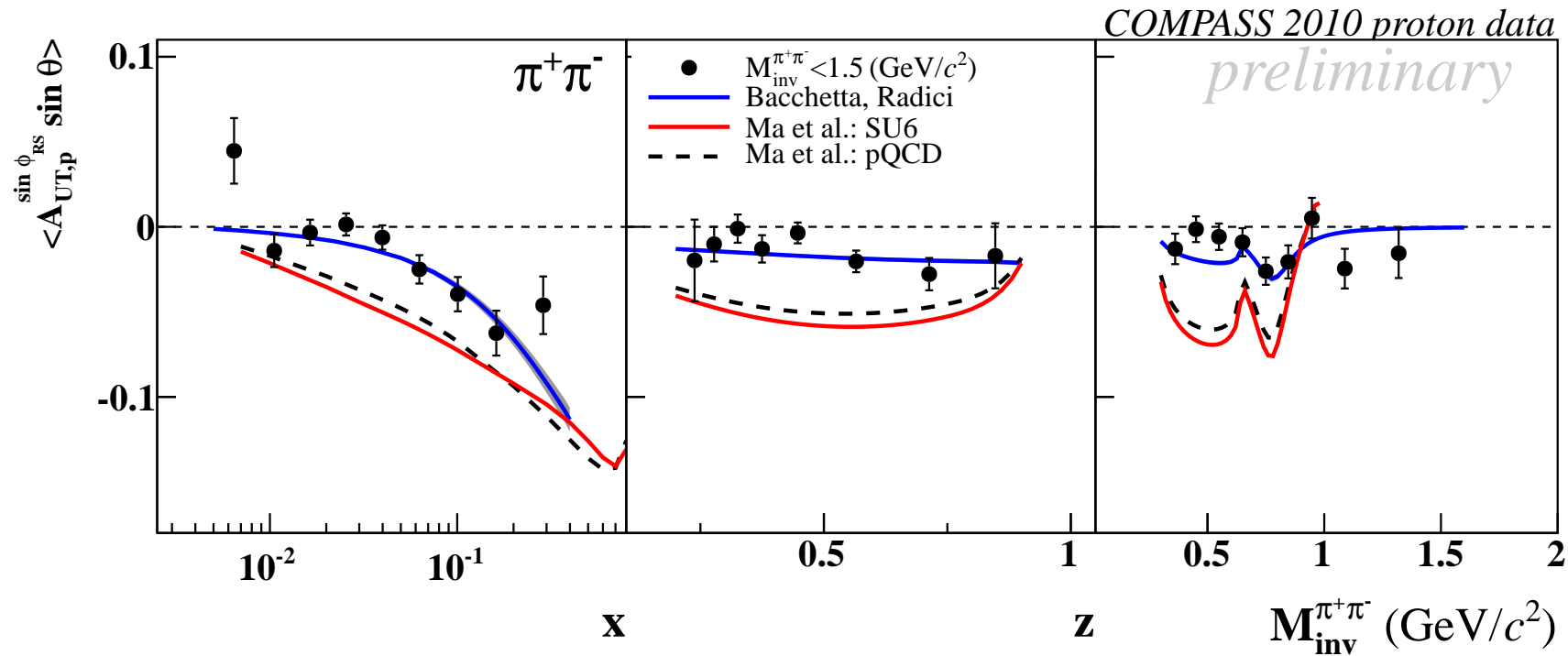
↪ compatible with zero within the uncertainties for both HERMES and COMPASS

Pretzelosity \blacktriangleright charged hadrons \blacktriangleright HERMES *vs.* COMPASS



\hookrightarrow compatible with zero within the uncertainties for both HERMES and COMPASS

$A_{UT}^{\sin \Phi_{RS}}$ \blacktriangleright $\pi^+ \pi^-$ \blacktriangleright COMPASS *vs.* model predictions



Bacchetta *et al.*, hep-ph/0608037
 Ma *et al.*, arXiv:0711.0817

- $\hookrightarrow x_{bj}$: *Ma* trend confirmed | *Bacchetta* good agreement
- $\hookrightarrow z$: *Ma* too large | *Bacchetta* compatible
- $\hookrightarrow M_{inv}$: *Ma* too large | *Bacchetta* good agreement around ρ^0 mass