# Exclusive $\rho^{0}$ production off transversely polarized protons and deuterons 

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## Outline

- Motivation
- Theoretical framework (GPD formalism)
- COMPASS experiment
- Event selection and experimental method
- Results
- Recent development of the analysis
- Summary and outlook

Measurement of exclusive $\rho^{0}$ production off transversely polarized target provides constraints of GPDs, in particular of GPD E which is sensitive to orbital momentum

Deeply Virtual Coulomb Scattering

$$
\gamma^{*} \boldsymbol{p} \rightarrow \gamma \boldsymbol{p}^{\prime}
$$


factorization for large $Q^{2}$ and $-t<1(G e V / C)^{2}$

## GPDs (Generalized Parton Distributions):

| $H^{q, g}(x, \xi, t)$ | $E^{q, g}(x, \xi, t)$ |
| :--- | :---: |
| for sum over <br> parton helicities |  |
| $\tilde{H}^{q, g}(x, \xi, t)$ | $\widetilde{E}^{q, g}(x, \xi, t)$ |
| for difference over <br> for retained <br> proton helicity | for changed <br> proton helicity |
| where: |  |

x : average longitudinal momentum fraction of the parton
$2 \xi$ : longitudinal momentum fraction transferred by the parton

$$
\xi \approx \frac{x_{B}}{2-x_{B}} \quad \text { (in the Bjorken limit) }
$$

t : squared momentum transferred to the target nucleon

## Production meson dependence on different GPDs:

Deeply Virtual Meson Production

$$
\gamma^{*} p \rightarrow V p^{\prime}
$$



for example:

$$
\begin{aligned}
& H_{\rho^{o}}=\frac{1}{\sqrt{2}}\left(\frac{2}{3} H^{u}+\frac{1}{3} H^{d}+\frac{3}{8} H^{q}\right) \\
& H_{\omega}=\frac{1}{\sqrt{2}}\left(\frac{2}{3} H^{u}-\frac{1}{3} H^{d}+\frac{1}{8} H^{g}\right) \\
& H_{\phi}=-\frac{1}{3} H^{s}-\frac{1}{8} H^{g}
\end{aligned}
$$

- contribution from gluons at the same order of $\alpha_{s}$ as from quarks
- factorization is strictly proven only for longitudinal $\gamma^{*}$


## Total angular momentum:

$$
\int_{-1}^{1} d x x\left[H^{q}(x, \xi, 0)+E^{q}(x, \xi, 0)\right]=2 \mathrm{~J}^{q} \quad \text { (Ji's sum rule) }
$$

where:

$$
J^{q}=L^{q}+S^{q}
$$

## Considered reaction:

$$
\mu^{+}+p \rightarrow \mu^{+}+p^{\prime}+\rho^{0}
$$

## Relevant angles:

$\phi$ : azimuthal angle between lepton plane and hadron plane
$\phi_{s}$ : azimuthal angle between target spin vector and lepton plane

Spin-dependent photoabsorption cross sections and interference terms $\sigma_{m n}^{i j}$ :

$$
\sigma_{m n}^{i j}\left(x_{B}, Q^{2}, t\right) \propto \sum_{\text {spins }}\left(A_{m}^{i}\right)^{*} A_{n}^{j}
$$

where:
$A_{m}^{i}$ : amplitude for subprocess $\gamma^{*} \mathrm{p} \rightarrow \vee \mathrm{p}^{\prime}$ with photon helicity $m$ and target proton helicity $i$

## The cross section formula for exclusive meson production

General formula for cross-section including beam and target polarization

$$
\begin{aligned}
& {\left[\frac{\alpha_{\mathrm{em}}}{8 \pi^{3}} \frac{y^{2}}{1-\varepsilon} \frac{1-x_{B}}{x_{B}} \frac{1}{Q^{2}}\right]^{-1} \frac{d \sigma}{d x_{B} d Q^{2} d \phi d \phi_{S}}} \\
& =\frac{\frac{1}{2}\left(\sigma_{++}^{++}+\sigma_{++}^{--}\right)+\sigma_{00}^{++}-\varepsilon \cos (2 \phi) \operatorname{Re} \sigma_{+-}^{++}-\sqrt{\varepsilon(1+\varepsilon)} \cos \phi \operatorname{Re}\left(\sigma_{+0}^{++}+\sigma_{+0}^{--}\right)}{} \\
& \quad-P_{\ell} \sqrt{\varepsilon(1-\varepsilon)} \sin \phi \operatorname{Im}\left(\sigma_{+0}^{++}+\sigma_{+0}^{--}\right)
\end{aligned} \quad \begin{aligned}
& \quad-S_{L}\left[\varepsilon \sin (2 \phi) \operatorname{Im} \sigma_{+-}^{++}+\sqrt{\varepsilon(1+\varepsilon)} \sin \phi \operatorname{Im}\left(\sigma_{+0}^{++}-\sigma_{+0}^{--}\right)\right] \\
& \quad+S_{L} P_{\ell}\left[\sqrt{1-\varepsilon^{2}} \frac{1}{2}\left(\sigma_{++}^{++}-\sigma_{++}^{--}\right)-\sqrt{\varepsilon(1-\varepsilon)} \cos \phi \operatorname{Re}\left(\sigma_{+0}^{++}-\sigma_{+0}^{--}\right)\right] \\
& \quad-S_{T}\left[\frac{\sin \left(\phi-\phi_{S}\right) \operatorname{Im}\left(\sigma_{++}^{+-}+\sigma_{00}^{+-}\right)+\frac{\varepsilon}{2} \sin \left(\phi+\phi_{S}\right) \operatorname{Im} \sigma_{+-}^{+-}+\frac{\varepsilon}{2} \sin \left(3 \phi-\phi_{S}\right) \operatorname{Im} \sigma_{+-}^{-+}}{\left.\quad+\sqrt{\varepsilon(1+\varepsilon)} \sin \phi_{S} \operatorname{Im} \sigma_{+0}^{+-}+\sqrt{\varepsilon(1+\varepsilon)} \sin \left(2 \phi-\phi_{S}\right) \operatorname{Im} \sigma_{+0}^{-+}\right]}\right. \\
& \quad+S_{T} P_{\ell}\left[\sqrt{1-\varepsilon^{2}} \cos \left(\phi-\phi_{S}\right) \operatorname{Re} \sigma_{++}^{+-}\right. \\
& \left.\quad-\sqrt{\varepsilon(1-\varepsilon)} \cos \phi_{S} \operatorname{Re} \sigma_{+0}^{+-}-\sqrt{\varepsilon(1-\varepsilon)} \cos \left(2 \phi-\phi_{S}\right) \operatorname{Re} \sigma_{+0}^{-+}\right] .
\end{aligned}
$$

$$
\epsilon=\frac{1-y-\frac{1}{4} y^{2} \gamma^{2}}{1-y+\frac{1}{2} y^{2}+\frac{1}{4} \gamma^{2}} \quad \gamma=2 \mathrm{x}_{B j} M_{P} / Q
$$

## Access to GPDs through the exclusive $\rho^{0}$ production

## For vector mesons:

unpolarized cross section
$\frac{1}{\Gamma^{\prime}} \frac{d \sigma_{00}^{++}}{d t}=\left(1-\xi^{2}\right)\left|\mathcal{H}_{M}\right|^{2}-\left(\xi^{2}+\frac{t}{4 \mathrm{M}_{p}^{2}}\right)\left|\mathcal{E}_{M}\right|^{2}-2 \xi^{2} \operatorname{Re}\left(\mathscr{E}_{M}^{*} \mathcal{H}_{M}\right)$

$$
\begin{aligned}
\sigma_{0} & =\frac{1}{2}\left(\sigma_{++}^{++}+\sigma_{++}^{--}\right)+\epsilon \sigma_{00}^{++} \\
& \equiv \sigma_{T}+\epsilon \sigma_{L}
\end{aligned}
$$

$$
\frac{1}{\Gamma^{\prime}} \operatorname{Im} \frac{d \sigma_{00}^{+-}}{d t}=-\sqrt{1-\xi^{2}} \frac{\sqrt{t_{0}-t}}{M_{p}} \operatorname{Im}\left(\mathcal{E}_{M}^{*} \mathcal{H}_{M}\right)
$$

transverse target spin asymmetry

$$
A_{U T}=-\frac{\operatorname{Im}\left(\sigma_{++}^{+-}+\epsilon \sigma_{00}^{+-}\right)}{\sigma_{0}}
$$

where:
$\mathcal{H}_{M}, \mathcal{E}_{M}$ are convolutions of the GPDs $H^{q, g}, E^{q, g}$ with hard scattering kernel and meson GDA

$$
\Gamma^{\prime}=\frac{\alpha_{e m}}{Q^{6}} \frac{x_{B}^{2}}{1-x_{B}} \quad-t_{0}=\frac{4 \xi^{2} M_{P}^{2}}{1-\xi^{2}} \quad \xi \approx \frac{x_{B}}{2-x_{B}}
$$



## COMPASS experiment - 2007 setup

```
\mu}\mp@subsup{}{}{+}\mathrm{ beam at the SPS accelerator
\begin{tabular}{ll} 
luminosity: & \(5 \cdot 10^{32} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}\) \\
energy: & 160 GeV \\
polarization: & \(\approx 80 \%\)
\end{tabular}
\(\mu^{+}\)beam at the SPS accelerator
```

Two $\mathbf{3 0} \mathbf{c m}$ and one $\mathbf{6 0} \mathbf{~ c m}$ long target cells [two $\mathbf{6 0 c m}$ long cells in 2002-2004] with opposite polarization

```
material:
polarization: dilution factor for exclusive
\(\rho^{0}\) production: \(\quad \approx 25 \%[\approx 44 \%]\)
```



## Used data and event selection

Used data:

$$
\left.\begin{array}{l}
2002-2004 \text { (deuterons) } \\
2007 \text { (protons) }
\end{array}\right\} \begin{aligned}
& \text { for transverse } \\
& \text { target polarization }
\end{aligned}
$$

Analyzed decay channel:

$$
\rho^{0} \rightarrow \pi^{+}+\pi^{-} \quad B R \sim 100 \%
$$

Topology:

- one incident and one scattered muon
- two charged hadron tracks with opposite signs

Vertex in the target

Kinematics domain:

- $\mathrm{Q}^{2}>1\left[(\mathrm{GeV} / \mathrm{c})^{2}\right]$
- $\mathrm{W}>5$ [GeV]
- $0.1<y<0.9$
- $0.003<\mathrm{X}_{\mathrm{Bj}}<0.35$
where:
$\mathrm{Q}^{2}: \quad$ negative four-momentum squared of $\gamma^{\star}$
W: total energy in $\gamma^{\star}-N$ system
y : fraction of the lepton energy lost in the LAB
$\mathrm{X}_{\mathrm{Bj}}$ : Bjorken scaling variable


## Event selection - cuts on hadron variables





## Invariant mass

Pion mass is assumed for each outgoing hadron track

$$
-0.3<M_{\pi \pi}-M_{\rho}^{P D G}<0.3\left[\mathrm{GeV} / \mathrm{c}^{2}\right]
$$

## Missing energy

Recoil proton is not detected - check if the proton
is intact

$$
E_{\text {miss }}=\frac{M_{x}^{2}-M_{p}^{2}}{2 \mathrm{M}_{p}} \in[-2.5,2.5] \mathrm{GeV}
$$

$E_{\text {miss }}=0$ is the signature of the exclusivity
Squared transverse momentum of $\rho^{0}$ candidate w.r.t. virtual photon direction

To remove coherent production off target nuclei

$$
0.05<p_{t}^{2}\left[(\mathrm{GeV} / \mathrm{C})^{2}\right] \quad \text { for protons }
$$

To remove inefficient region of azimuthal angle reconstruction

$$
0.01<p_{t}^{2}\left[(\mathrm{GeV} / \mathrm{c})^{2}\right] \quad \text { for deuterons }
$$

To suppress non-exclusive background

$$
p_{t}^{2}<0.5\left[(\mathrm{GeV} / \mathrm{C})^{2}\right]
$$

for protons and deuterons

## Event selection - kinematic domain






## Double ratio method for extraction of transverse target spin asymmetry

## Acceptance

Number of
Flux
Dilution factor
observed events

$$
N\left(\phi-\phi_{s}\right)=F n a\left(\phi-\phi_{s}\right) \sigma_{0} \cdot\left(1 \pm f\left\langle P_{T}\right\rangle A_{U T} \sin \left(\phi-\phi_{s}\right)\right)
$$

Number of target nucleons
Mean target polarization

$$
A_{U T}=-\frac{\operatorname{Im}\left(\sigma_{++}^{+-}+\epsilon \sigma_{00}^{+-}\right)}{\sigma_{0}}
$$

$$
\begin{aligned}
\operatorname{DR}\left(\phi-\phi_{s}\right) & =\frac{N_{\text {Up/Down }}^{\uparrow}\left(\phi-\phi_{s}\right)}{N_{\text {Center }}^{\downarrow}\left(\phi-\phi_{s}\right)} \cdot \frac{N_{\text {Center }}^{\uparrow}\left(\phi-\phi_{s}\right)}{N_{U p / \text { Down }}^{\downarrow}\left(\phi-\phi_{s}\right)} \\
& =\frac{F_{U p / D o w n}^{\uparrow} F_{\text {Center }}^{\uparrow}}{F_{\text {Center }}^{\downarrow} F_{U p / \text { Down }}^{\downarrow}} \frac{a_{U p / \text { Down }}^{\uparrow}\left(\phi-\phi_{s}\right) a_{\text {Center }}^{\uparrow}\left(\phi-\phi_{s}\right)}{a_{\text {Center }}^{\downarrow}\left(\phi-\phi_{s}\right) a_{U p / D o w n}^{\downarrow}\left(\phi-\phi_{s}\right)} \frac{\left(1+f\left\langle P_{T}\right\rangle A_{U T} \sin \left(\phi-\phi_{s}\right)\right)^{2}}{\left(1-f\left\langle P_{T}\right\rangle A_{U T} \sin \left(\phi-\phi_{s}\right)\right)^{2}}
\end{aligned}
$$

Number of target nucleons, flux and $\sigma_{0}$ cancel

$$
\text { Acceptance cancel with reasonable assumption } \quad \frac{a_{U p / D o w n}^{\uparrow}}{a_{\text {Center }}^{\downarrow}}=\frac{a_{\text {Up/Down }}^{\downarrow}}{a_{\text {Center }}^{\uparrow}}
$$

$$
A_{U T} \text { from a fit to the } D R\left(\phi-\phi_{s}\right)
$$

$\left\langle Q^{2}\right\rangle \approx 2.2(\mathrm{GeV} / \mathrm{C})^{2}$


$$
\left\langle x_{B}\right\rangle \approx 0.04
$$



$$
\left\langle p_{t}^{2}\right\rangle \approx 0.18(\mathrm{GeV} / \mathrm{c})^{2}
$$



$$
A_{U T}^{\sin \left(\phi-\phi_{s}\right)} \text { compatible with } 0
$$

## Comparison with HERMES experiment

$\left\langle Q^{2}\right\rangle \approx 2.2(\mathrm{GeV} / \mathrm{c})^{2}$


$$
\left\langle p_{t}^{2}\right\rangle \approx 0.18(\mathrm{GeV} / \mathrm{c})^{2}
$$



Both results are in good agreement

## Comparison with GPD predictions



Model given by S. V. Goloskokov and P. Kroll (see Eur. Phys. J. C 594 (2009))

- "handbag model"
- GPDs constrained by CTEQ6 parametrization and nucleon form factors
- power corrections due to transverse quarks momenta
- predictions both for $\gamma_{L}^{*}$ and $\gamma^{*}{ }_{T}$

$$
\left.\begin{array}{l}
A_{U T}\left(\rho^{0}\right) \approx-0.02 \\
A_{U T}(\omega) \approx-0.10
\end{array}\right\} \text { for protons }
$$



Results are in good agreement with the model
without coherent/incoherent scattering separation ( $\left.0.01<p_{t}^{2}<0.5\left[(\mathrm{GeV} / \mathrm{c})^{2}\right]\right)$

$$
\left\langle Q^{2}\right\rangle \approx 2.0(\mathrm{GeV} / \mathrm{c})^{2}
$$

$$
\left\langle x_{B}\right\rangle \approx 0.03
$$

$$
\left\langle p_{t}\right\rangle \approx 0.11(\mathrm{GeV} / \mathrm{c})^{2}
$$





$$
A_{U T}^{\sin \left(\phi-\phi_{s}\right)} \text { compatible with } 0
$$

## Recent development of the analysis

## Main features of the new analysis

- background subtraction
- new method of asymmetry extraction $\rightarrow$ binned likelihood method
- detailed systematic studies $\rightarrow$ impact of false asymmetries, background subtraction, etc.

New release and publication of the paper expected soon

No significant changes of final results compared with the ones presented today

## Recent development of the analysis

## Background subtraction

- fraction of background measured from fit to $\mathrm{E}_{\text {miss }}$ distribution
- shape of exclusive distribution fitted directly to data
- shape of semi-inclusive distribution taken from MC
$\rightarrow$ LEPTO generator
- fraction of background extracted from data as a function of $\phi-\phi_{s}$ modulation
$\rightarrow$ background asymmetry


SIGNAL
BACKGROUND
TOTAL

## Summary and outlook

- Summary
- Transverse target spin asymmetry $A_{U T}$ was measured both for protons and deuterons
- Asymmetries are small, compatible with 0
- Results are compatible with HERMES experiment and with GPD predictions by
S. V. Goloskokov and P. Kroll
- In progress
- new analysis with background subtraction
- no significant changes of final results compared with the ones presented today
- release of results and dedicated paper expected soon


## Outlook

- 2010 data with transversely polarized proton target $\rightarrow$ increase of statistics for $\rho^{0}$ with 2010 data ( $\approx 3$ times)
$\gamma^{*}$ transverse/longitudinal separation
extraction of non-leading twist asymmetries
possible analysis of $\phi$ and $\omega$ mesons
- measurement with transversely polarized protons considered using GPD setup at COMPASS-II experiment (with Recoil Proton Detector)

