

# Transverse Spin and Momentum Effects in SIDIS experimental overview

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# Transverse Spin and Momentum Effects in SIDIS

## experimental overview

- introduction
- the experiments
- azimuthal asymmetries:
  - some recent results
  - transversity, Sivers and Boer-Mulders PDFs



# the beginning

## large transverse spin effects observed in hadronic interactions

$$A_N \sim 10^{-1}$$

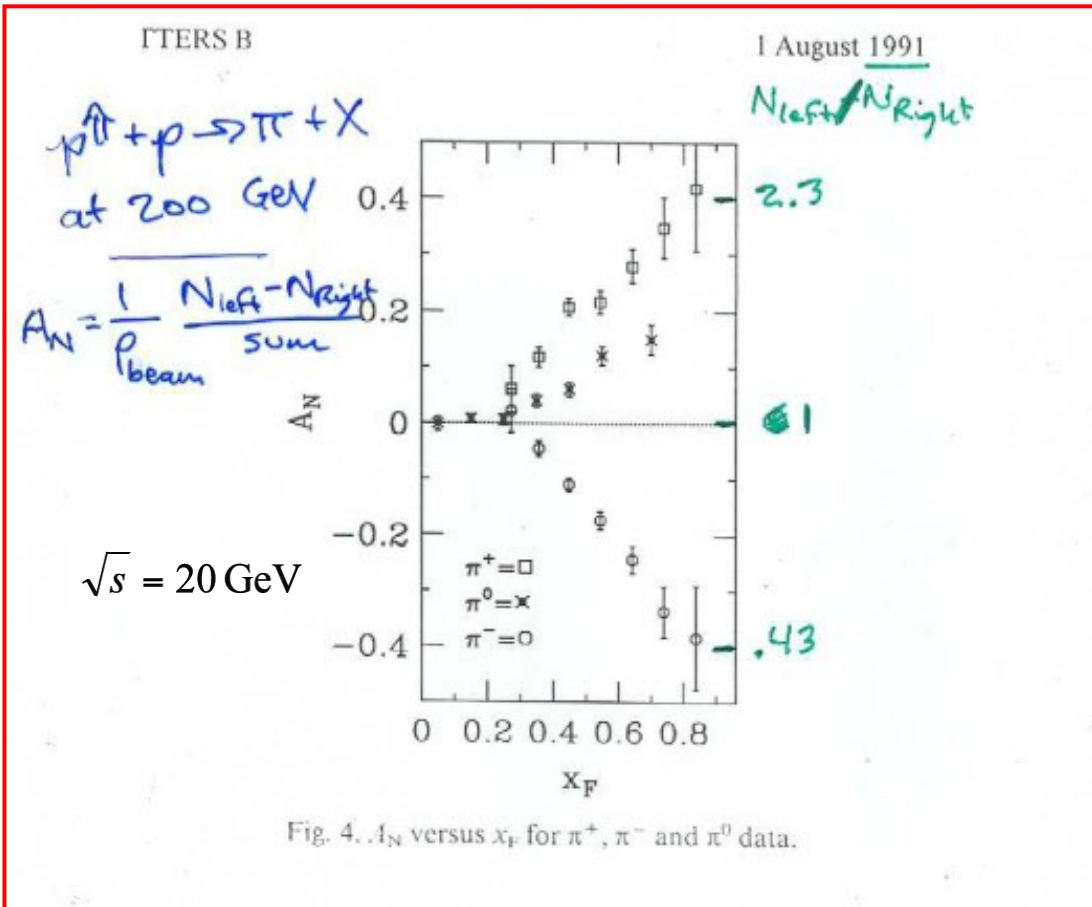
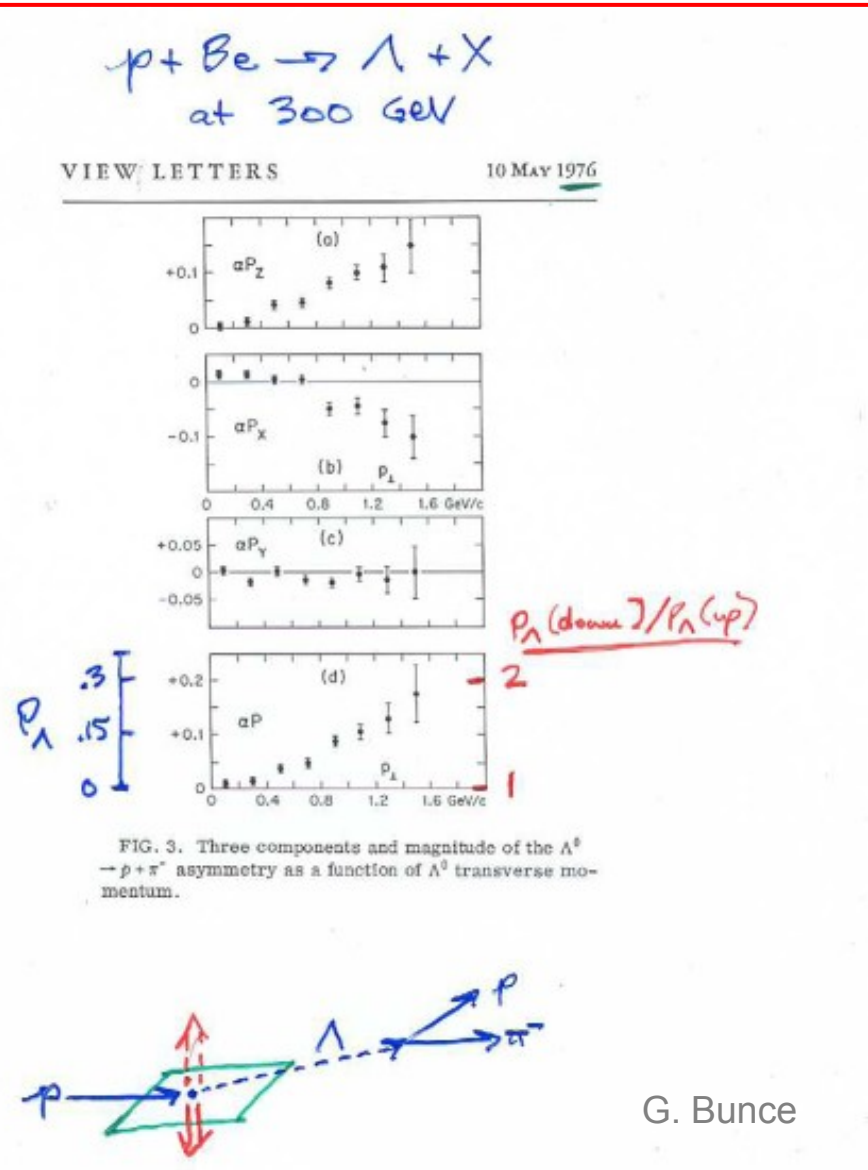
theory:

expected to be very small at high energies

(Kane, Pumplin, Repko, PRL 41 (1978) 1689)

$$A_N \sim 10^{-4}$$

$$A_N \propto \frac{m_q}{\sqrt{s}}$$



# Transverse Spin and Momentum Structure of the Nucleon

a large international theoretical and experimental effort

three distribution functions are necessary to describe the quark structure of the nucleon at LO in the **collinear case**
















**transversity PDF**  $\Delta_T \mathbf{q}$  or  $h_1$ : correlation between the transverse spin of the nucleon and the transverse spin of the quark

taking into account the **quark intrinsic transverse momentum**  $k_T$ , at leading order 8 PDFs are needed for a full description of the nucleon structure

**quark polarisation**

“TMDs”

**nucleon polarisation**

	nucleon polarisation			
	U	L	T	
U	$f_1$  <i>number density</i> $\mathbf{q}$		$f_{1T}^\perp$  -  <i>Sivers</i>	$\Delta_0^T \mathbf{q}$
L		$g_1$  -  <i>helicity</i> $\Delta \mathbf{q}$	$g_{1T}$  - 	
T	$h_1^\perp$  -  <i>Boer Mulders</i>	$h_{1L}^\perp$  - 	$h_1$  -  <i>transversity</i> $h_{1T}^\perp$  - 	$\Delta_T \mathbf{q}$

# Transverse Spin and Momentum Structure of the Nucleon

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












**transversity PDF**  $\Delta_T \mathbf{q}$  or  $h_1$ : correlation between the transverse spin of the nucleon and the transverse spin of the quark

**nucleon polarisation**

**Sivers function**  $f_{1T}^\perp$   
correlation between the transverse spin of the nucleon and the transverse momentum of the quark

**Boer-Mulders function**  $h_1^\perp$  **quark polarisation**  
correlation between the transverse spin and the transverse momentum of the quark in unpol nucleons

*T-odd TMDs*

	nucleon polarisation			
	U	L	T	
U	$f_1$  number density $\mathbf{q}$		$f_{1T}^\perp$  -  Sivers	$\Delta_0^T \mathbf{q}$
L		$g_1$  -  helicity $\Delta \mathbf{q}$	$g_{1T}$  - 	
T	$h_1^\perp$  -  Boer Mulders	$h_{1L}^\perp$  - 	$h_1$  -  transversity $h_{1T}^\perp$  - 	$\Delta_T \mathbf{q}$

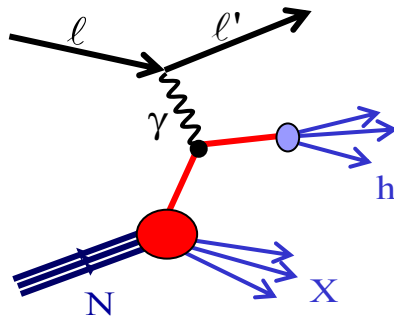
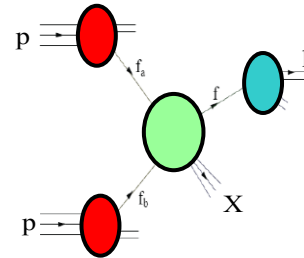
# Transverse Spin and Momentum Structure of the Nucleon

a large international theoretical and experimental effort

hard polarised **pp scattering**

RHIC / BNL

→ M. Grosse-Perdekamp



**SIDIS** off transversely polarised targets:

DESY (HERMES)

CERN (COMPASS)

JLab → Z.-E. Meziani

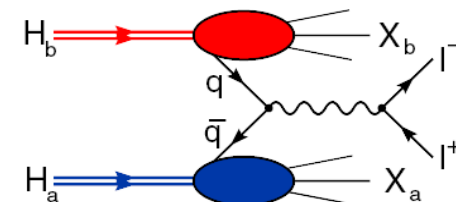
and eRHIC, EIC, ENC

and several (future) projects for (polarised) **Drell-Yan**:

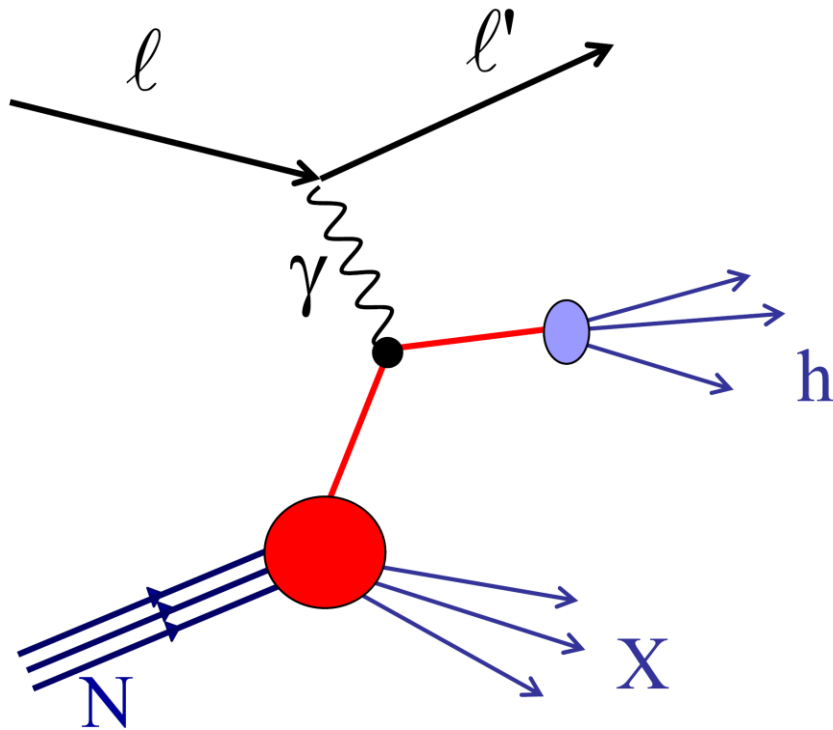
CERN (COMPASS)

FNAL, JParc, RHIC, JINR, IHEP, GSI

→ J.-C. Peng, A. Ogawa, A. Ferrero



# Semi-Inclusive Deep Inelastic Scattering



$$x = \frac{Q^2}{2P \cdot q} \quad y = \frac{P \cdot q}{P \cdot \ell} =_{LAB} \frac{E - E'}{E}$$

$$Q^2 = -q^2 \quad W^2 = (P + q)^2$$

$$z = \frac{P \cdot P_h}{P \cdot q} =_{LAB} \frac{E_h}{E - E'}$$

- the FFs must be known
- allows to disentangle the effects related to the different TMD PDFs and to access all of them
- by identifying the final state hadrons allows for flavor separation

$$\sigma^{\ell N \rightarrow \ell h X} \propto \sum_q q(x) \otimes \sigma^{\ell q \rightarrow \ell q} \otimes D_q^h(z)$$



# Semi-Inclusive Deep Inelastic Scattering

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

**18 structure functions**

**14 azimuthal modulations**

$\phi_h$  ( $\phi_S$ ) hadron (nucleon spin)  
azimuthal angle in GNS

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right.$$

$$+ \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h}$$

$$+ S_{\parallel} \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right]$$

**3 with unpolarised target**

$$+ |S_{\perp}| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right.$$

**3 with L polarised target**

$$+ \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)}$$

**8 with T polarised target**

$$+ \left. \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \right\}$$

$$+ |S_{\perp}| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right.$$

$$\left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \left. \right\}$$

**they can be measured  
from the same data**



**18 structure functions**

**14 azimuthal modulations**

$\phi_h(S)$  hadron (nucleon spin)  
azimuthal angle in GNS

$$F_{BT}^{mod} \propto x \sum_q e_q^2 f^q \otimes D_q^h$$

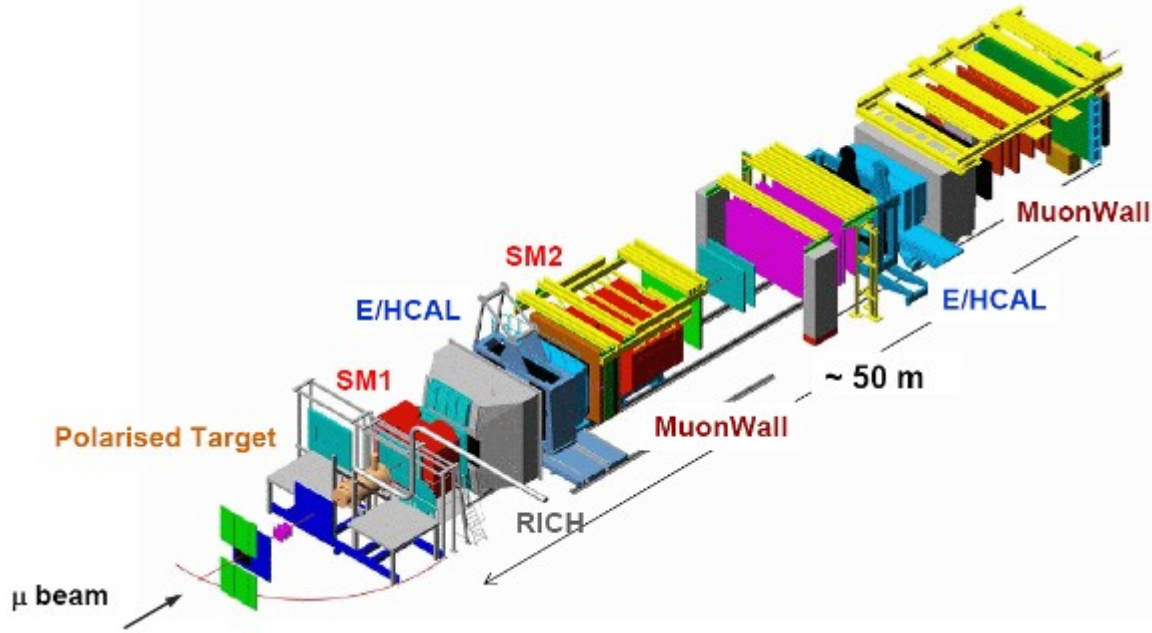
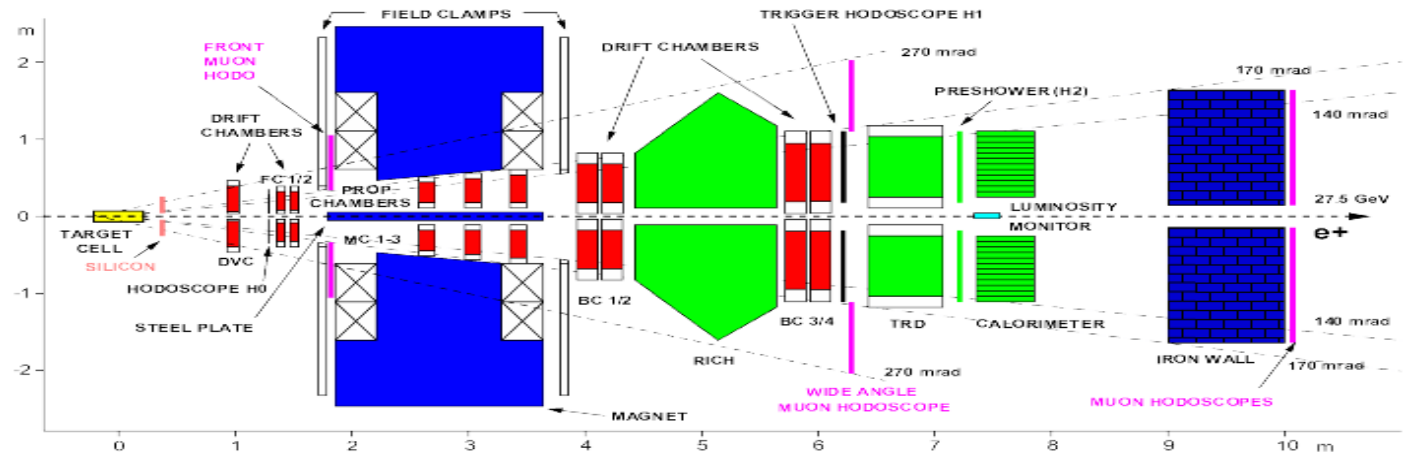
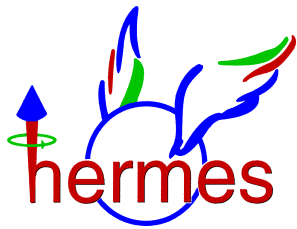
any TMD PDF

corresponding FF

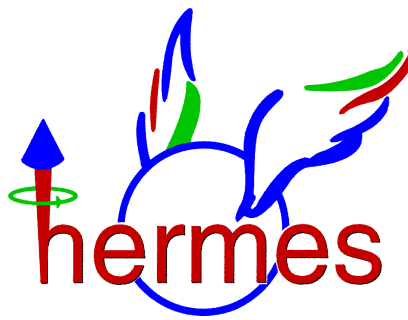
**the measurements of the structure functions using different targets with different polarisations and looking at different final state hadrons give information on the different TMD PDFs for the different quark flavours  $q$**

# the experiments





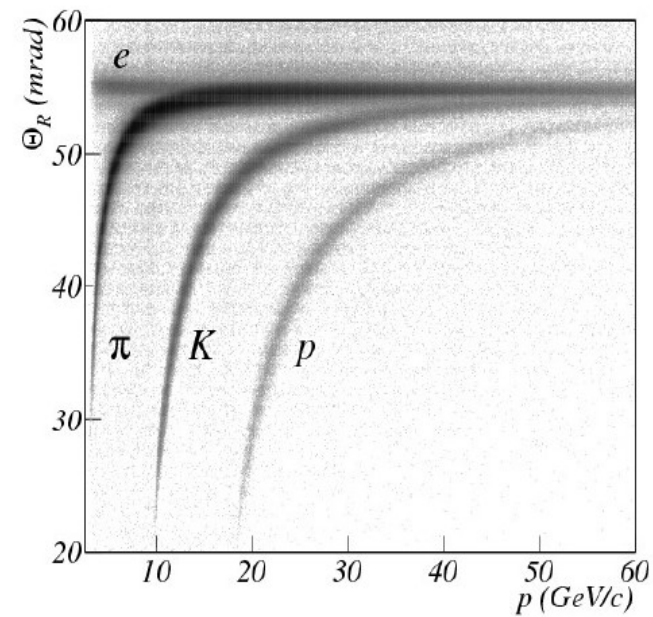
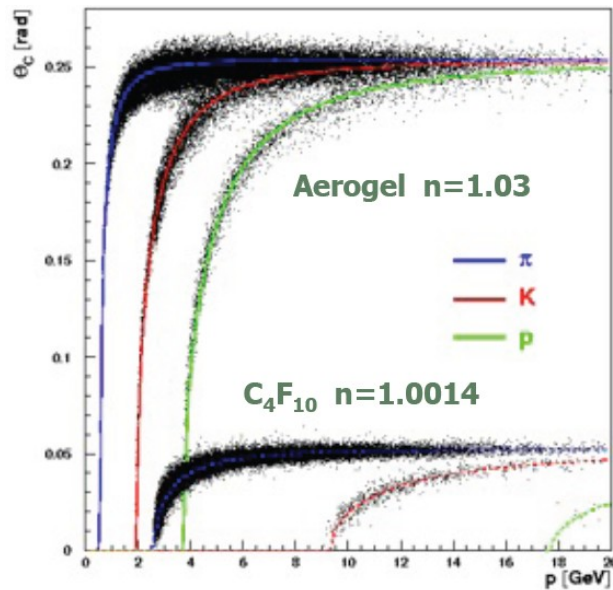
data taking with  
T polarised target:  
2002-2005 (p)



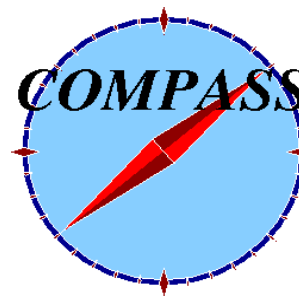
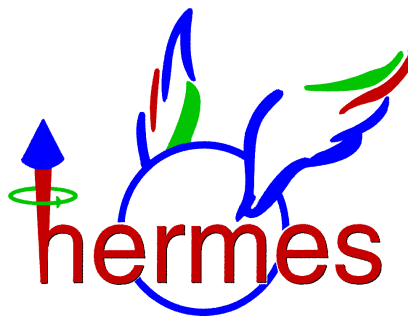
data taking with  
T polarised target:  
2002-2004 (d)  
2007 (p)  
2010 (p)

- polarized (<60%)  $e^+/e^-$  beam  
of **27 GeV**, both helicity states
- pure gas targets with T (p) and L (p,d)  
polarization,  
fast spin-flip of target
- RICH PID K: 2-15 GeV

- polarized ( $\sim$ -80%)  $\mu^+$   
of **160 GeV**
- **NH<sub>3</sub>** (p) and **<sup>6</sup>LiD** (d) targets with T and L  
polarization, 2 (3) cells with opposite P,  
polarisation reversal every  $\sim$ 8h
- RICH PID K: 9-50 GeV



data taking with  
T polarised target:  
2002-2005 (p)



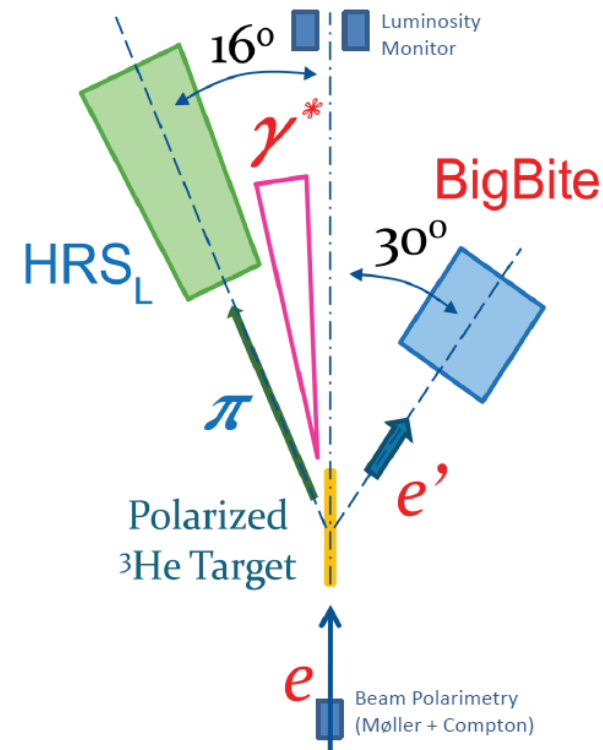
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2010 (p)

- polarized (<60%)  $e^+/e^-$  beam  
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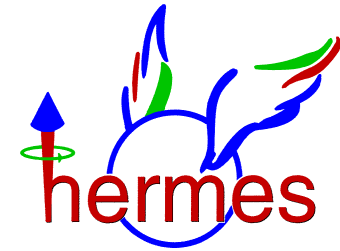
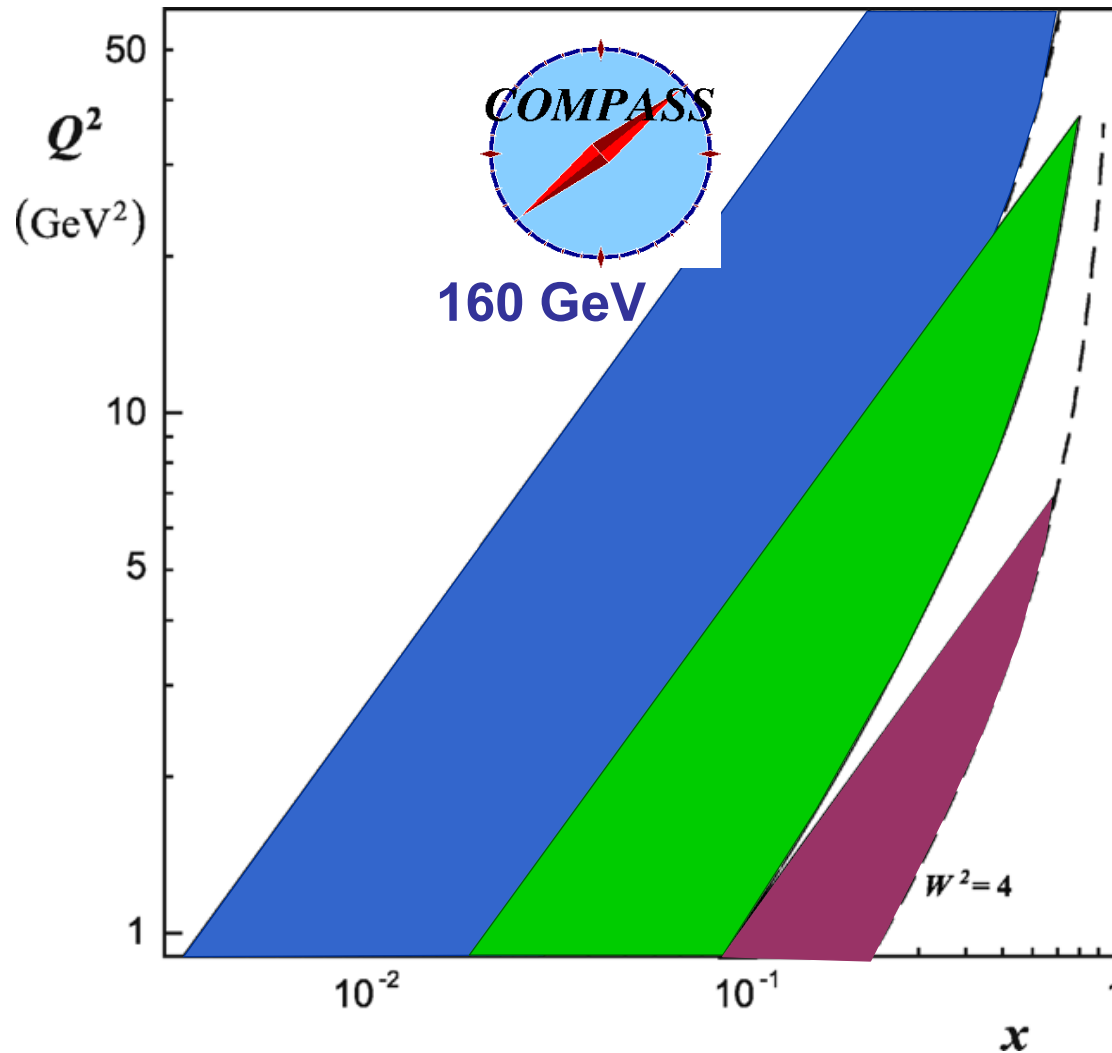
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## Jefferson Lab E06-010 Collaboration

- **6 GeV** electron beam
- transversely polarised **<sup>3</sup>He** target
- identified final state hadrons



# kinematical region



27.5 GeV

JLab 6 GeV



# results

azimuthal asymmetries

transverse target polarisation

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \dots$$

**Collins  
asymmetry**

$$\begin{aligned} & + |\mathbf{S}_\perp| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\ & \quad \left. + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \right. \\ & \quad \left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \\ & + |\mathbf{S}_\perp| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\ & \quad \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \end{aligned}$$

# Collins asymmetry

$$F_{UT}^{\sin(\phi_h + \phi_S)}$$

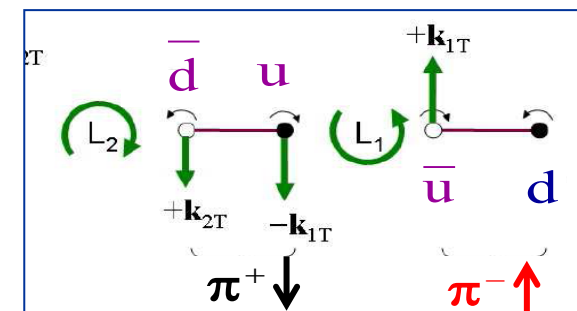
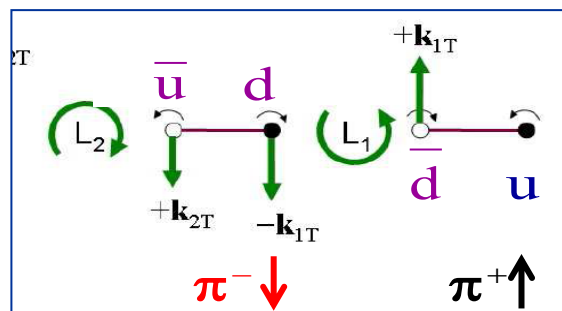
amplitude of the  $\sin(\phi_h + \phi_S - \pi)$  modulation  
in the azimuthal distribution of the final state hadrons

$$A_{Coll} \approx \frac{\sum_q e_q^2 \Delta_T^q \otimes \Delta_T^0 D_q^h}{\sum_q e_q^2 q \otimes D_q^h}$$

transversity
“Collins FF”

“recursive fragmentation  
model with quark spin”  
[X. Artru, arXiv:1001.1061]

D. Sivers, TMD2010



data from Belle (and BaBar)





# Collins asymmetry

$$F_{UT}^{\sin(\phi_h + \phi_S)}$$

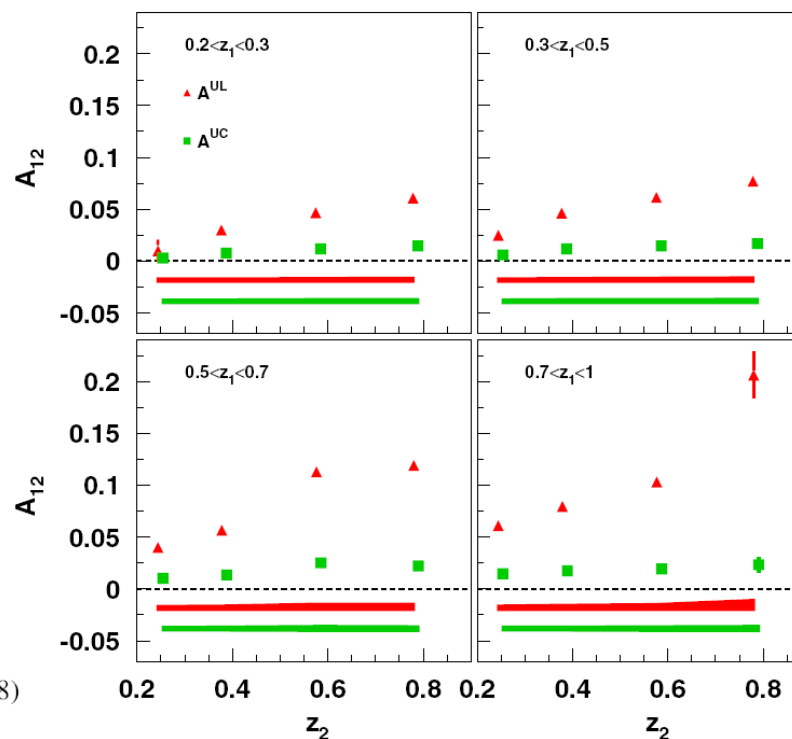
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transversity
“Collins FF”

data from Belle

$$e^+ e^- \rightarrow \pi^+ \pi^- X$$



PHYSICAL REVIEW D 78, 032011 (2008)

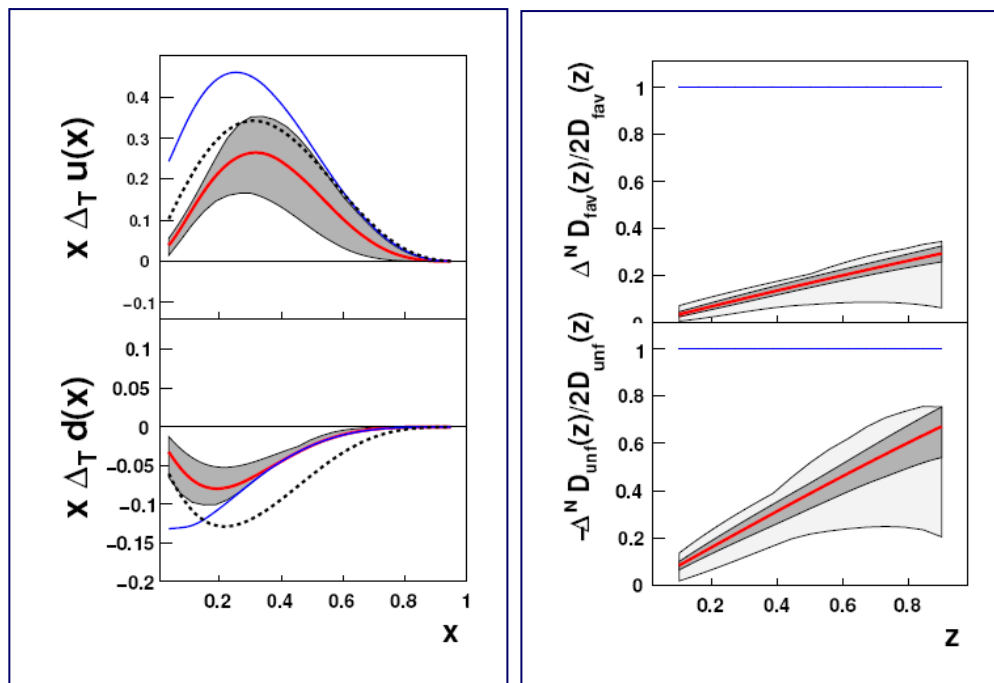


# Collins asymmetry

2005

- first strong signals seen by HERMES on protons: **MILESTONE!**
- no signal seen by COMPASS on deuterons

the COMPASS d, HERMES p, and BELLE data are well described in global fits  
→ first extractions of the Collins FFs and the transversity PDFs, and tensor charge



**M. Anselmino et al.,**  
Nucl.Phys.Proc.Supl.191 (2009) 98

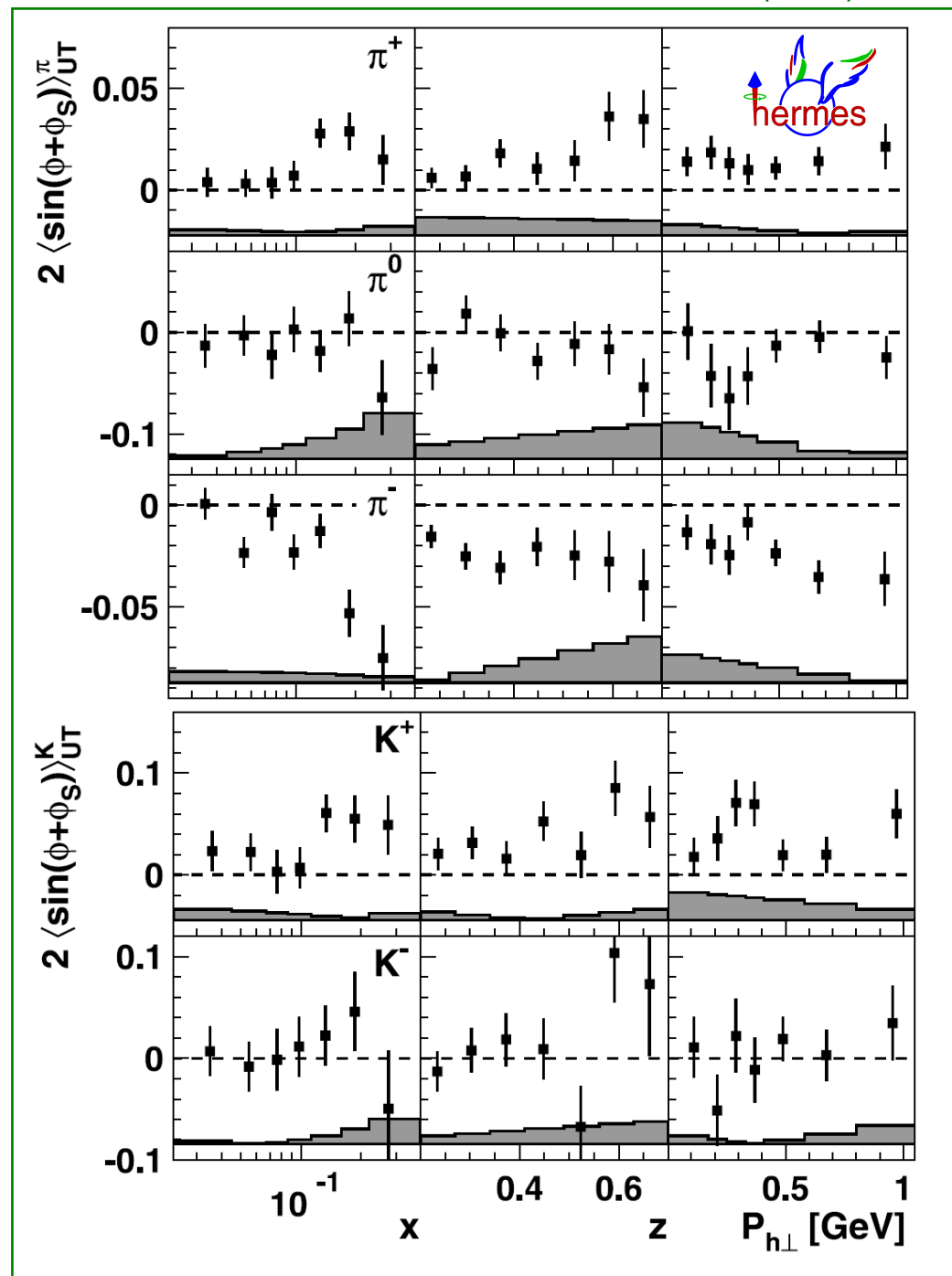


# Collins asymmetry - proton

PLB 693 (2010) 11

## final HERMES results

- clear signal for  $\pi^+$  and  $\pi^-$   $x > 0.1$   
opposite sign
- $K^+$  signal larger than  $\pi^+$ :  
role of sea quarks?
- *higher twist effects?*  
*limited statistics and range*  
*to study the  $Q^2$  dependence*

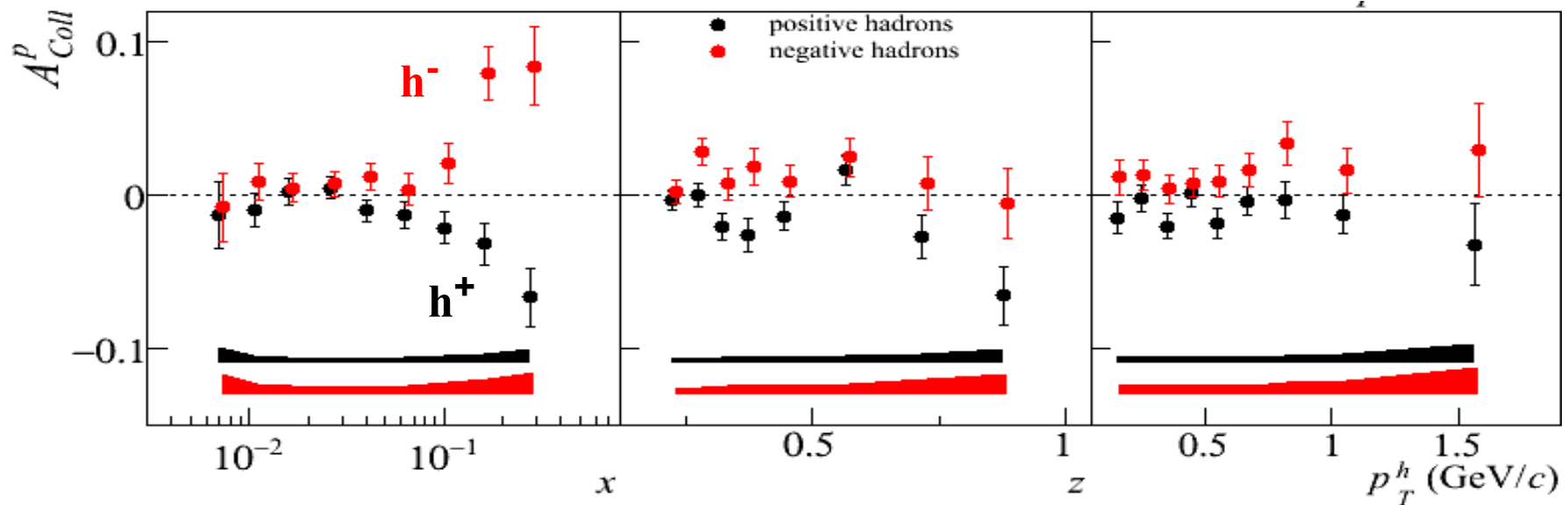


# Collins asymmetry - proton



final COMPASS results from 2007 data

PLB 692 (2010) 240



- at small  $x$ , the asymmetries are compatible with zero
- large signal in the valence region of opposite sign for positive and negative hadrons

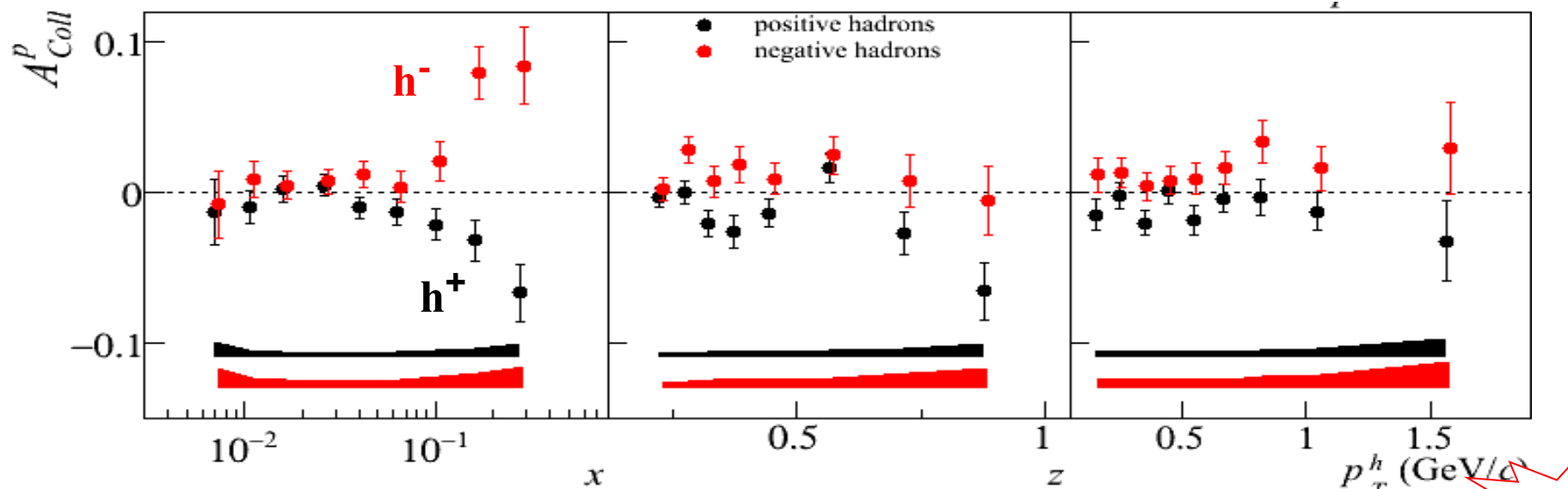


# Collins asymmetry - proton

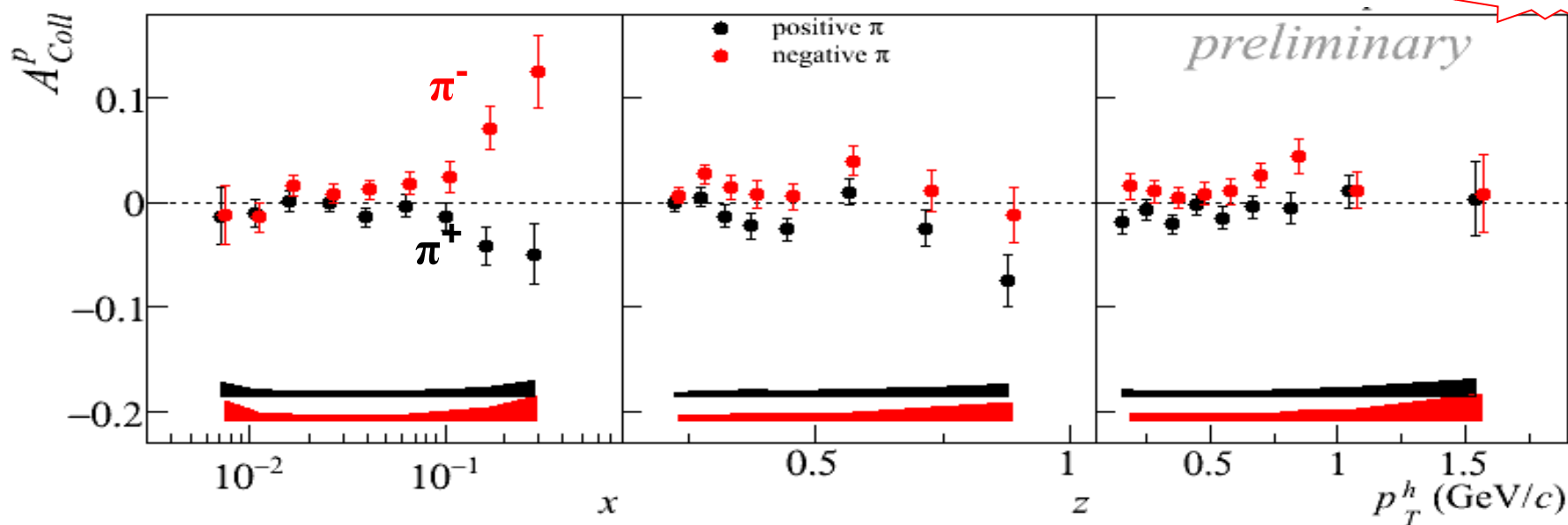


final COMPASS results from 2007 data

PLB 692 (2010) 240



SPIN2010

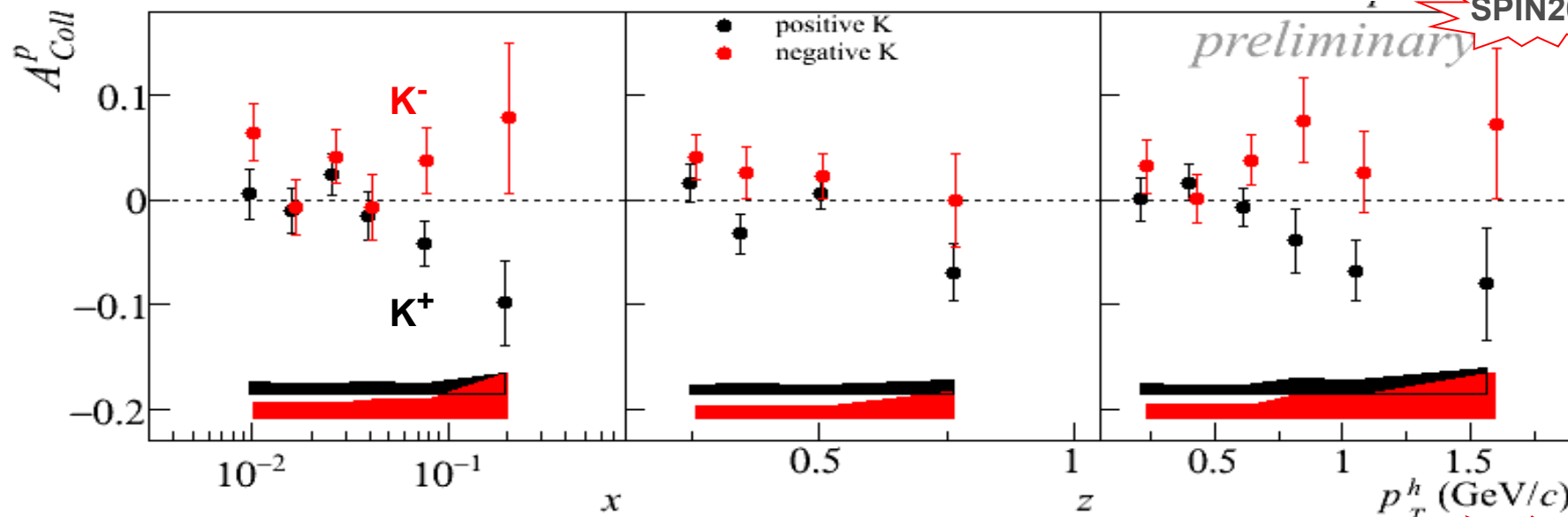


# Collins asymmetry - proton

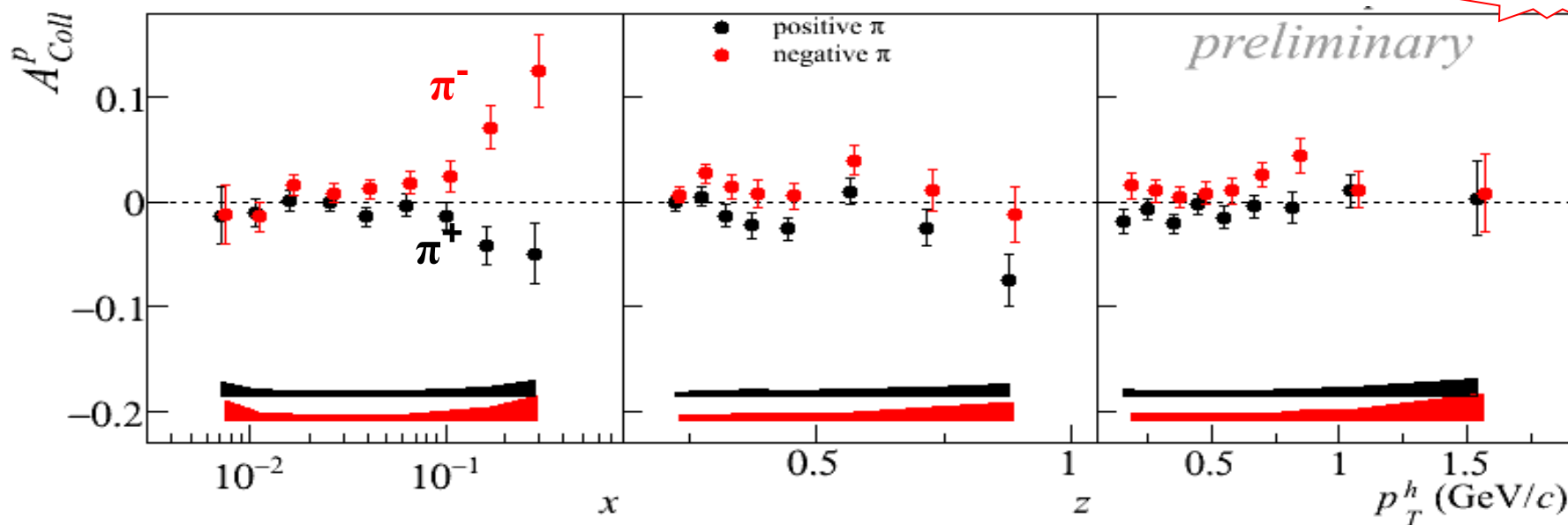


final COMPASS results from 2007 data

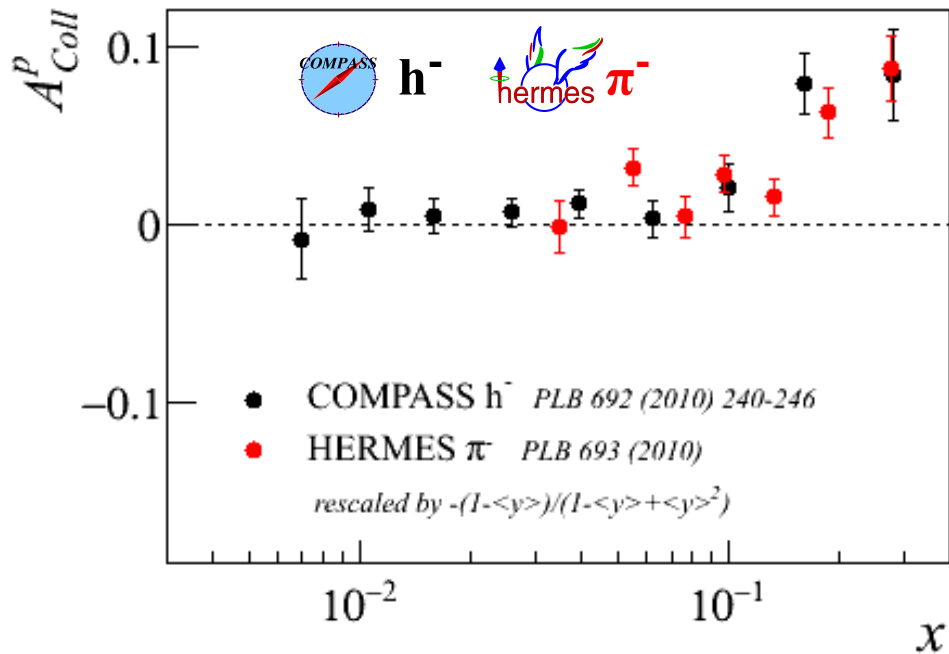
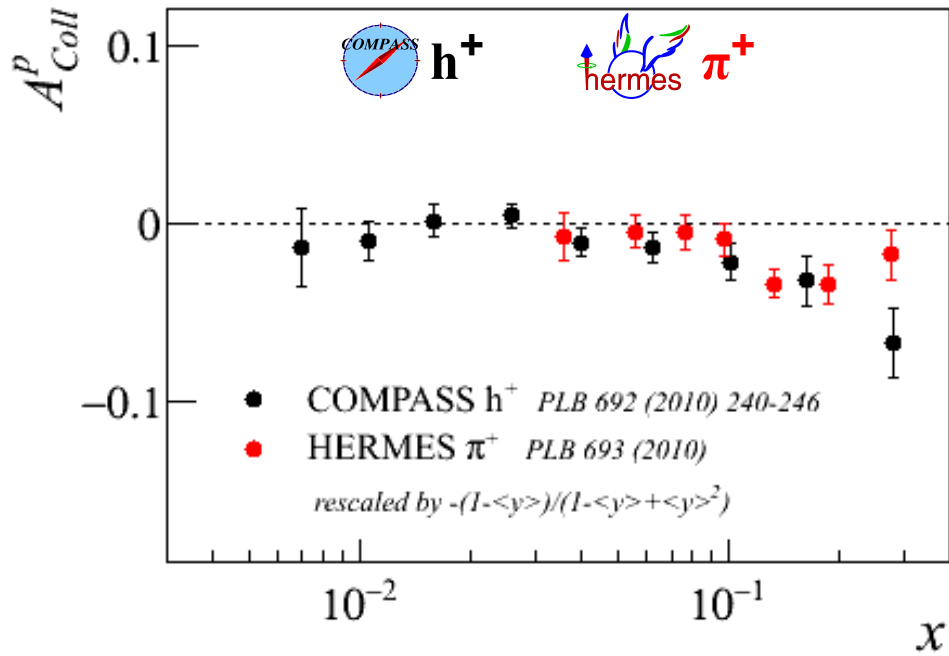
SPIN2010



SPIN2010

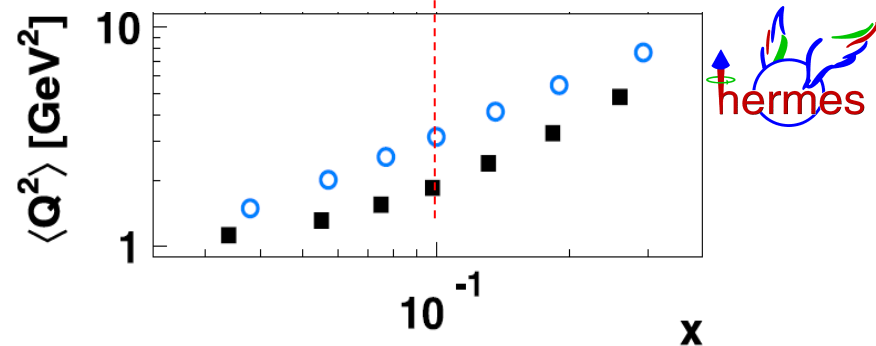
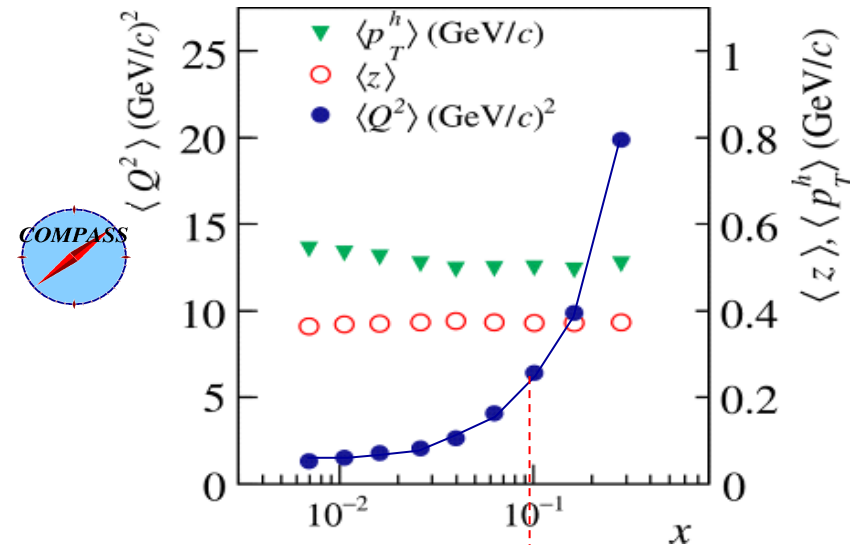


# Collins asymmetry - proton



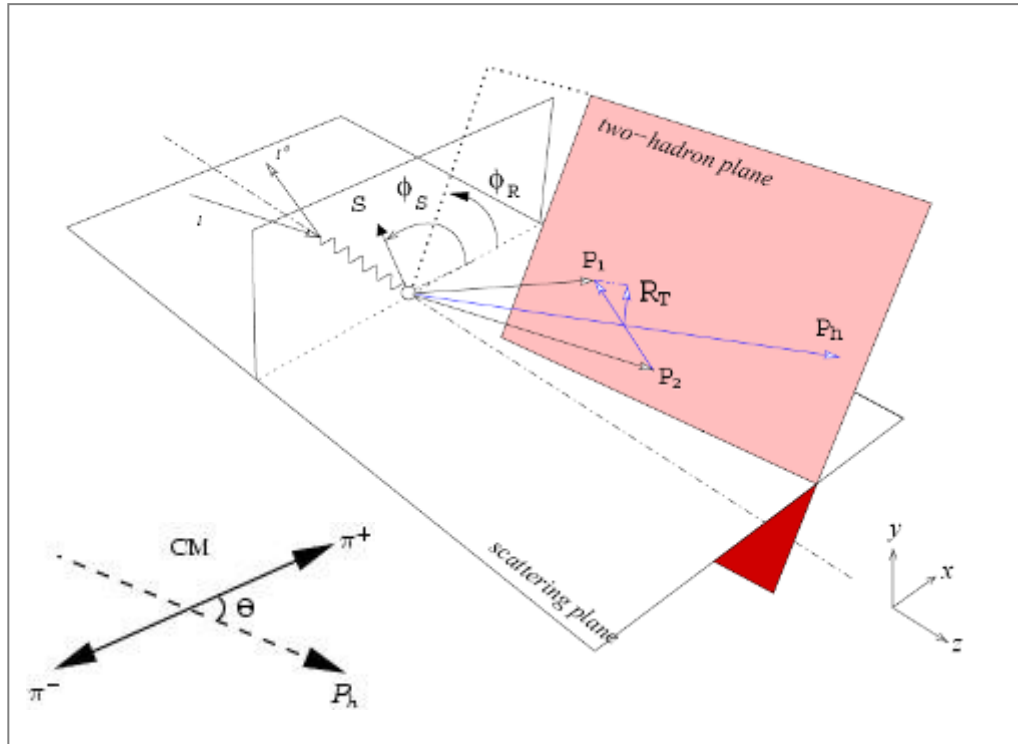
same sign and strength:  
a very important, not obvious result!

indication for: not a higher twist effect,  
weak  $Q^2$  dependence of the Collins FF



COMPASS sign convention

# Two Hadron Asymmetry



azimuthal asymmetry in

$$\phi_{RS} = \phi_{R\perp} - \phi_S,$$

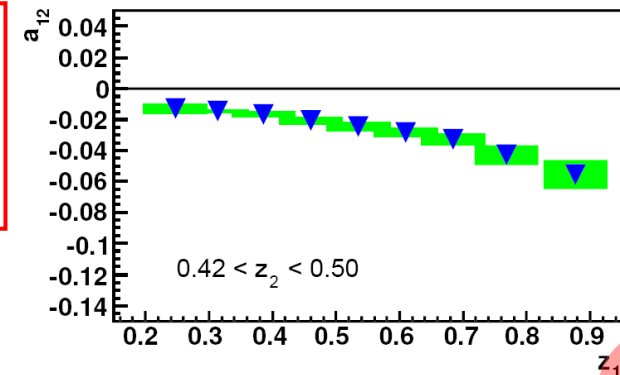
$\phi_{R\perp}$  is the azimuthal angle of the plane defined by the two hadrons

$$R = (z_1 p_2 - z_2 p_1) / (z_1 + z_2)$$

Interference Fragmentation Function

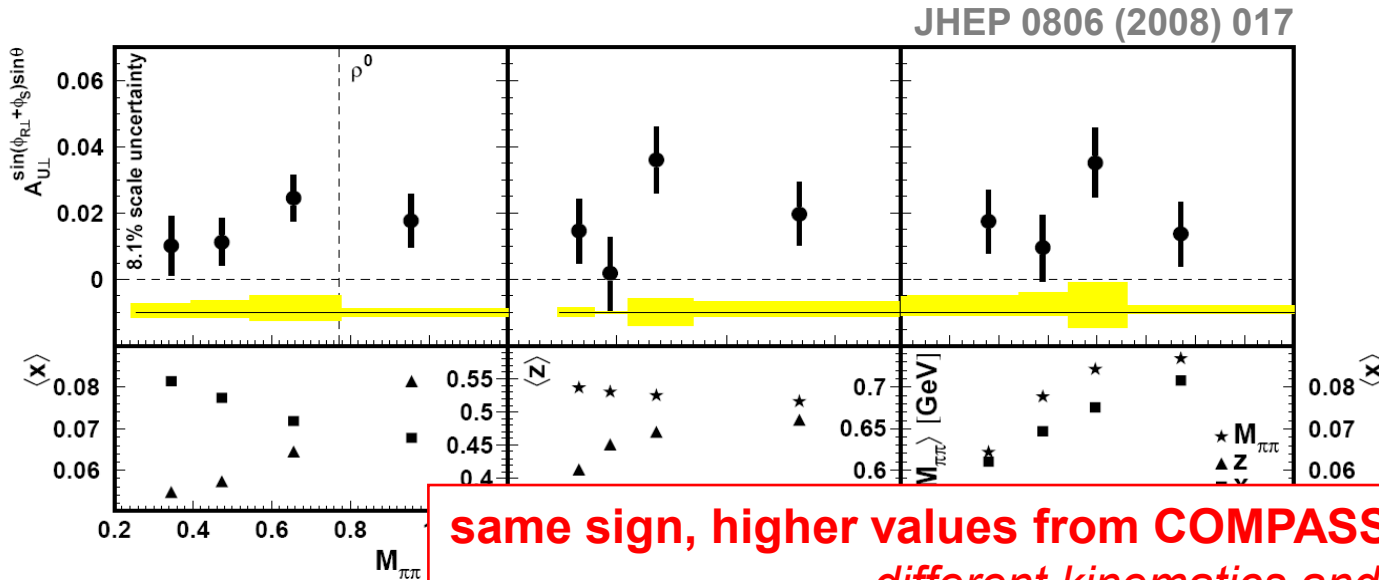
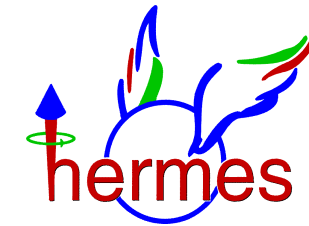
*BELLE*

$$A_{RS} = \frac{1}{f \cdot P_T \cdot D_{NN}} \cdot A = \frac{\sum_q e_q^2 \cdot \Delta_T q(x) \cdot H_q^{2h}(z, M_h^2)}{\sum_q e_q^2 \cdot q(x) \cdot D_q^{2h}(z, M_h^2)}$$





# Two Hadron Asymmetry



transversely polarised protons:  
**first evidence for a different from zero interference FF**

**same sign, higher values from COMPASS than from HERMES**  
*different kinematics and extraction*

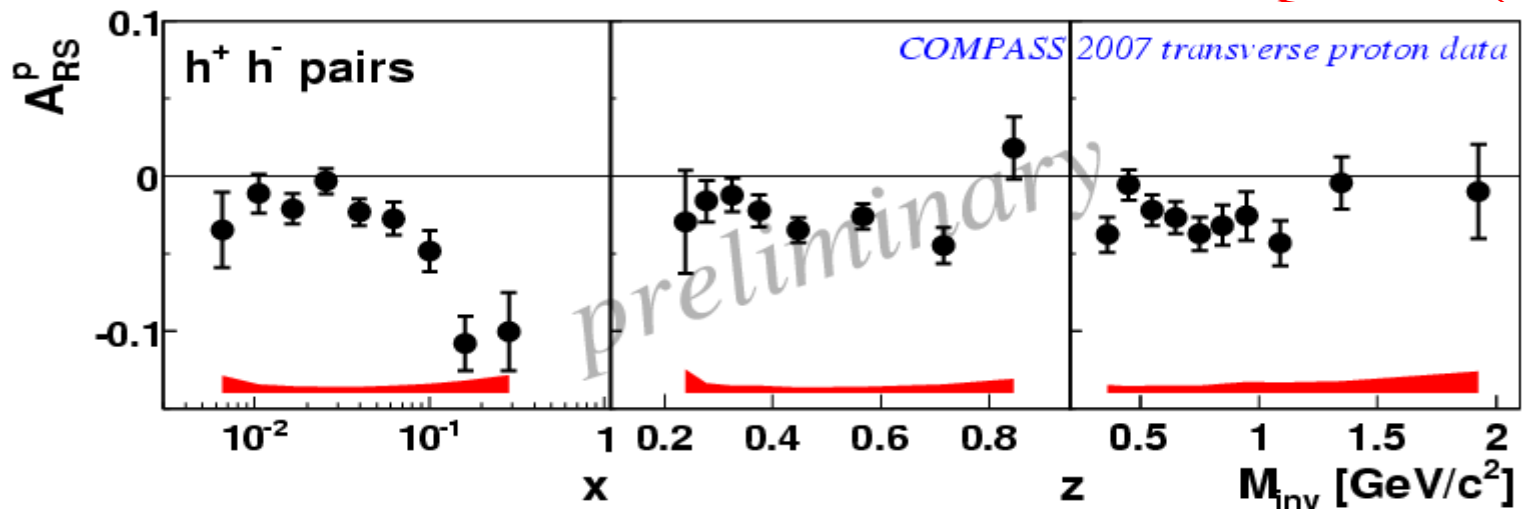
**difficult to describe both sets of data at the same time**

*[Bacchetta et al., Mah et al.]*



deuteron  
 proton:

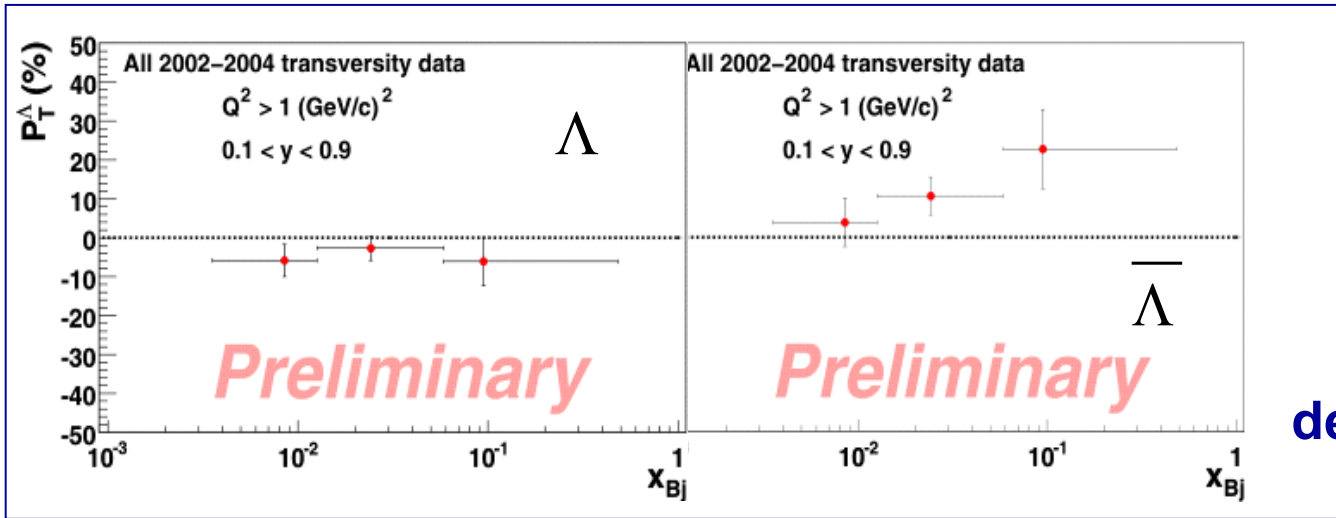
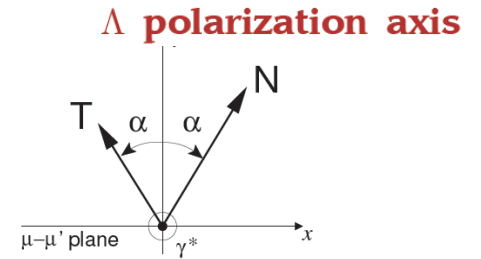
- sign in agreement with the Collins asymmetry
- strength ~ larger than the Collins asymmetry



# $\Lambda$ polarisation



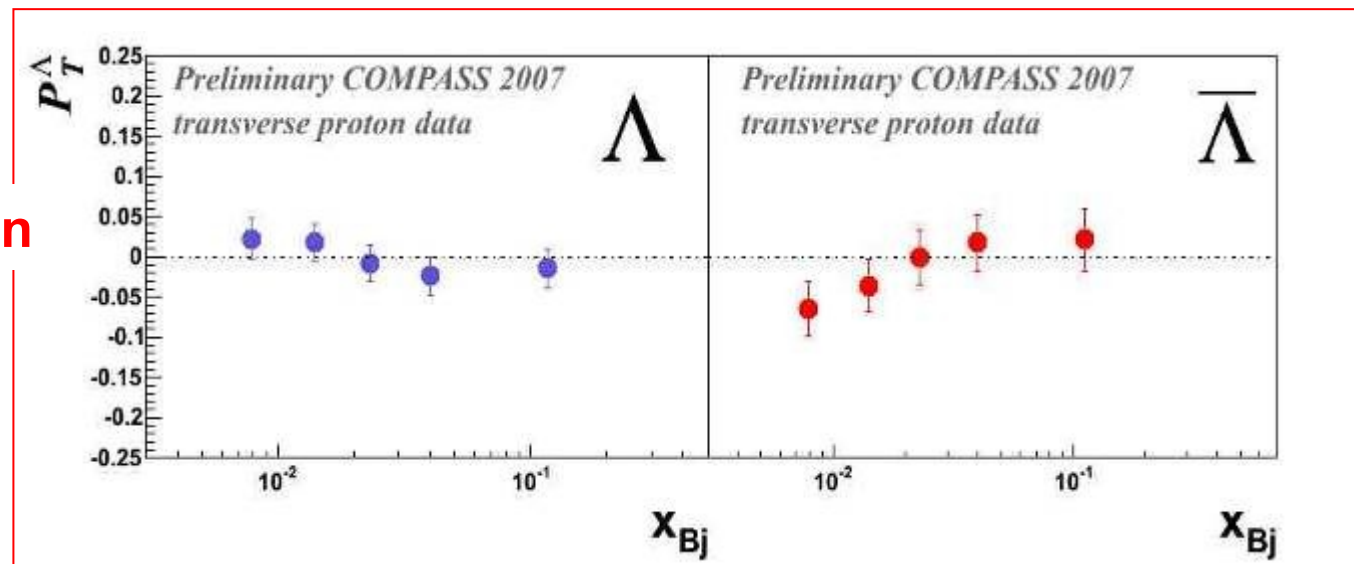
$$P_{T,exp}^{\Lambda} = f P_N D(y) \frac{\sum_q e_q^2 \Delta_T q(x) \Delta_T D_{\Lambda/q}(z)}{\sum_q e_q^2 q(x) D_{\Lambda/q}(z)}$$



deuteron

compatible with zero  
 more statistics is needed

proton

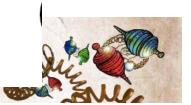


# azimuthal asymmetries

## transverse target polarisation

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \dots \quad \text{Sivers asymmetry} \quad A_{Siv} \approx \frac{\sum_q e_q^2 \mathbf{f}_{1T}^{\perp q} \otimes \mathbf{D}_1^q}{\sum_q e_q^2 \mathbf{f}_1 \otimes \mathbf{D}_1^q}$$

$$\begin{aligned}
 & + |\mathbf{S}_\perp| \left[ \boxed{\sin(\phi_h - \phi_S)} \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & \quad \left. \begin{array}{l} \text{Collins asymmetry} \\ h_\perp H_\perp^\perp \end{array} \right. \\
 & \quad + \varepsilon \boxed{\sin(\phi_h + \phi_S)} F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\
 & \quad \left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \\
 & + |\mathbf{S}_\perp| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\
 & \quad \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \Bigg\}
 \end{aligned}$$



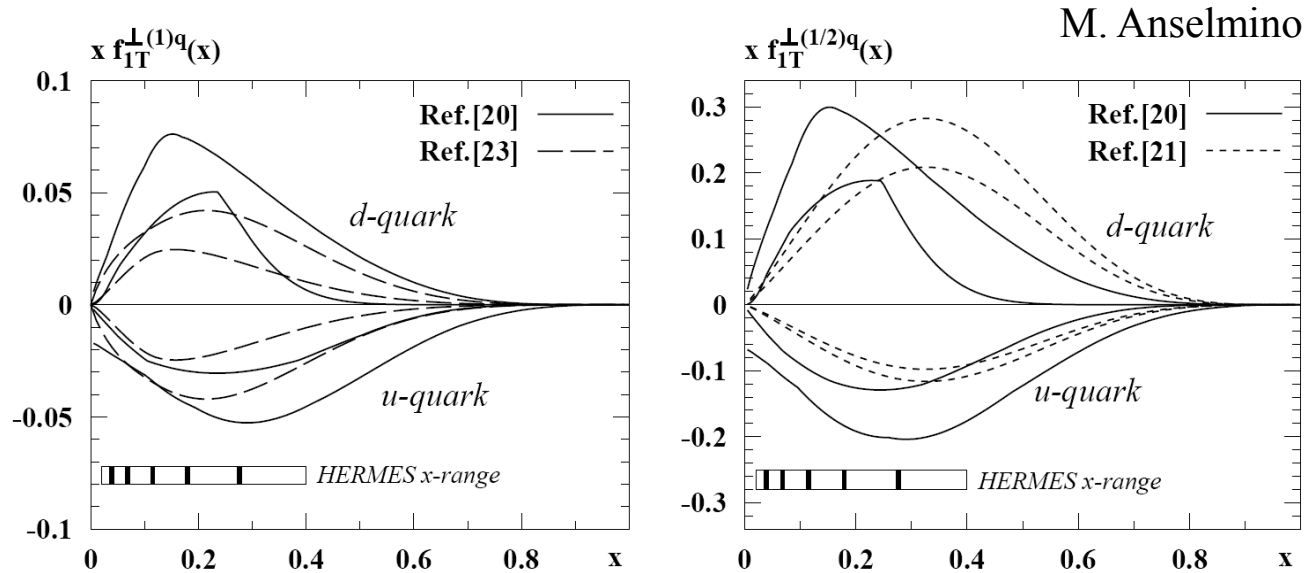
$$F_{UT,T}^{\sin(\phi_h - \phi_S)}$$

# Sivers asymmetry

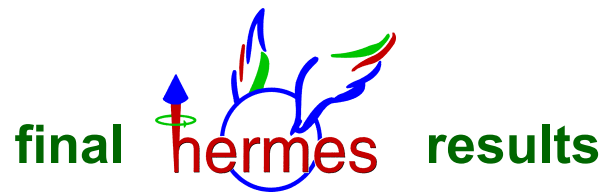
2005

- first strong signal seen by HERMES for  $\pi^+$  on protons
- no signal seen by COMPASS for  $h^+$  and  $h^-$  on deuterons

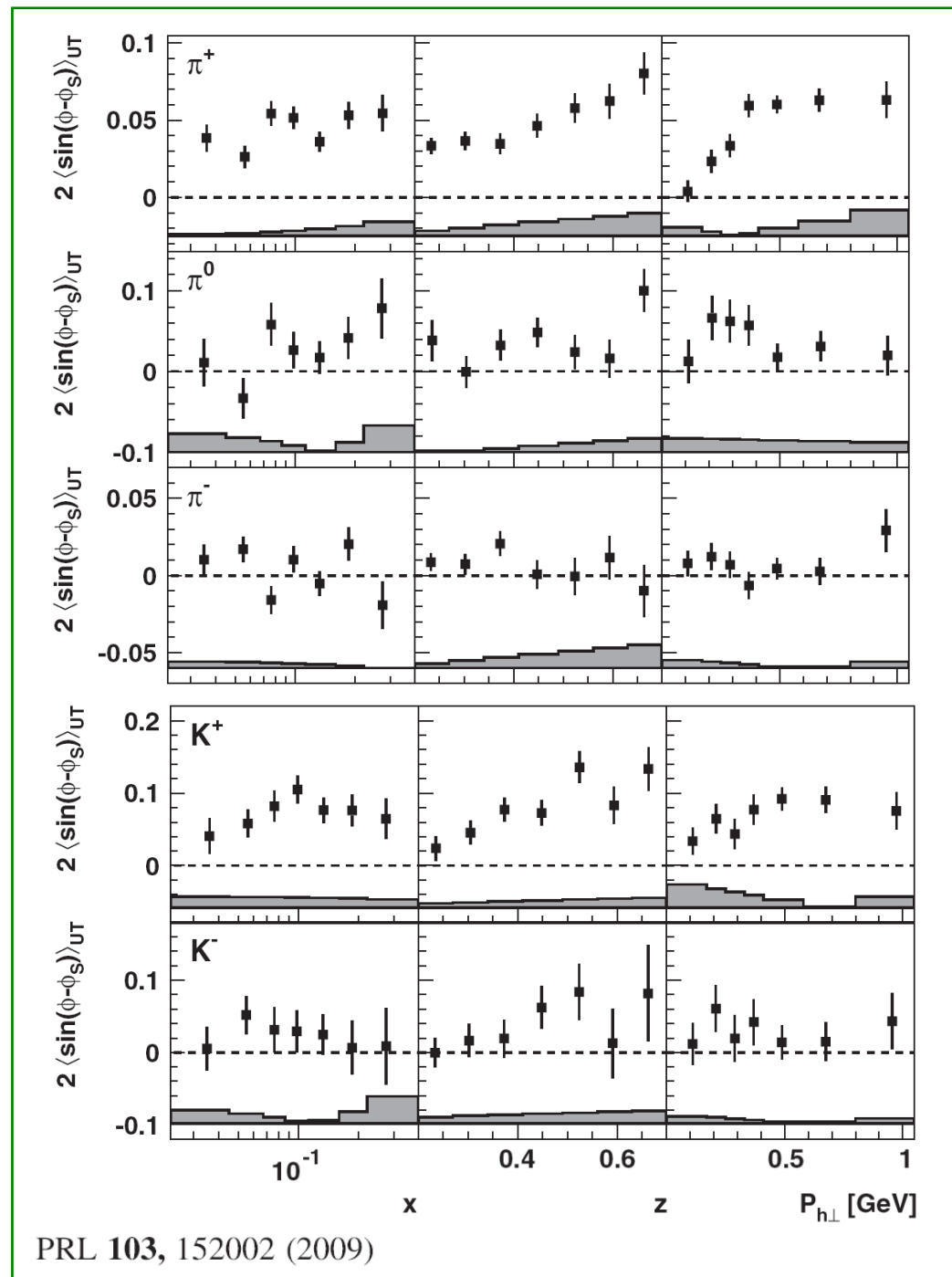
→ first extractions of the Sivers function from HERMES p (and COMPASS d) data  
*good description of the experimental results*



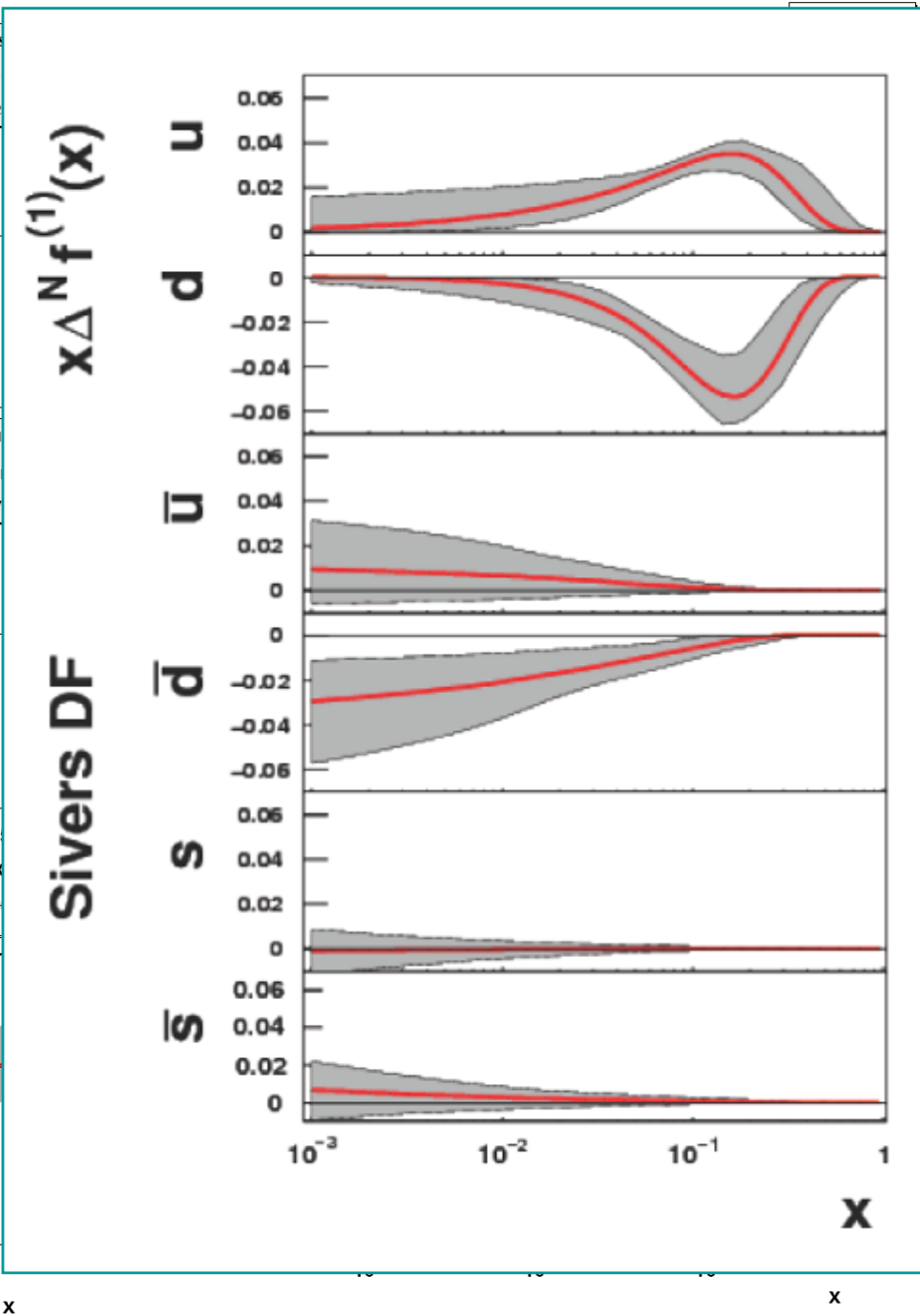
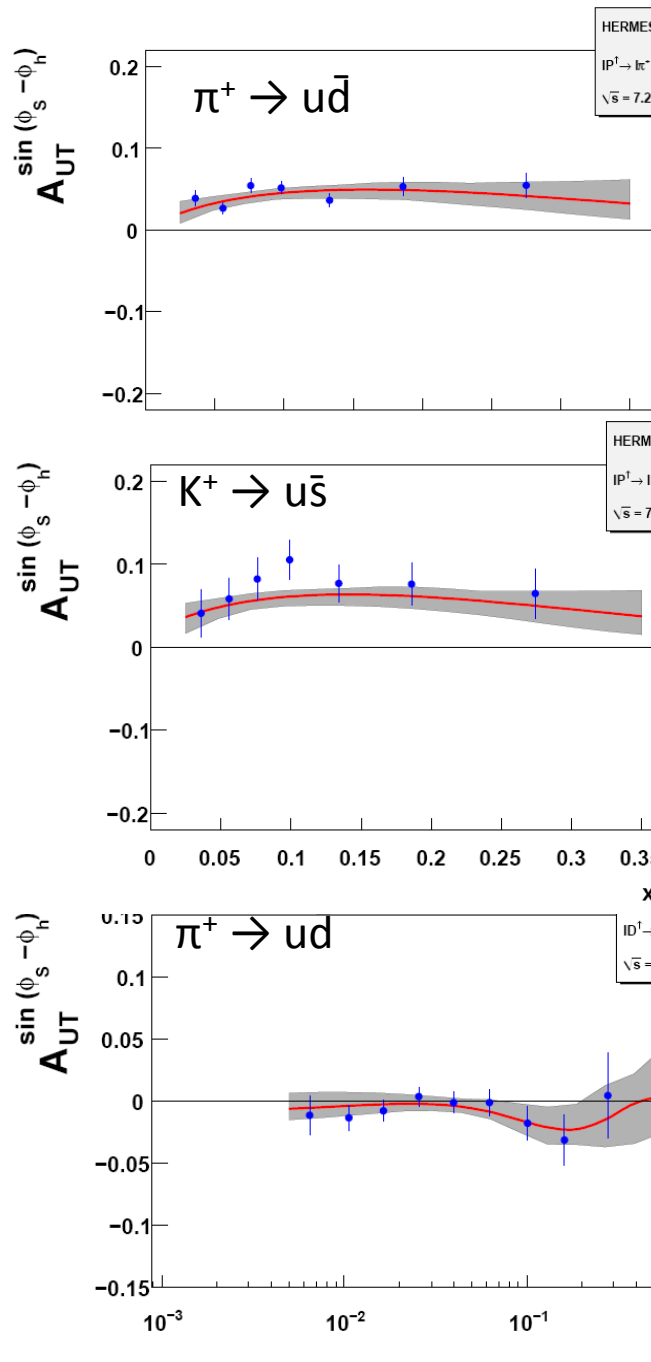
# Sivers asymmetry - proton



- clear signal for  $\pi^+$  and  $K^+$  over all the measured  $x$  range
- saturation for  $P_T^h > 0.4$  GeV/c
- difference between  $K^+$  and  $\pi^+$ :
  - role of sea quarks?
  - larger at lower  $Q^2$
  - higher twist effects in K production?



# Sivers asymmetry



New fit = valence + sea



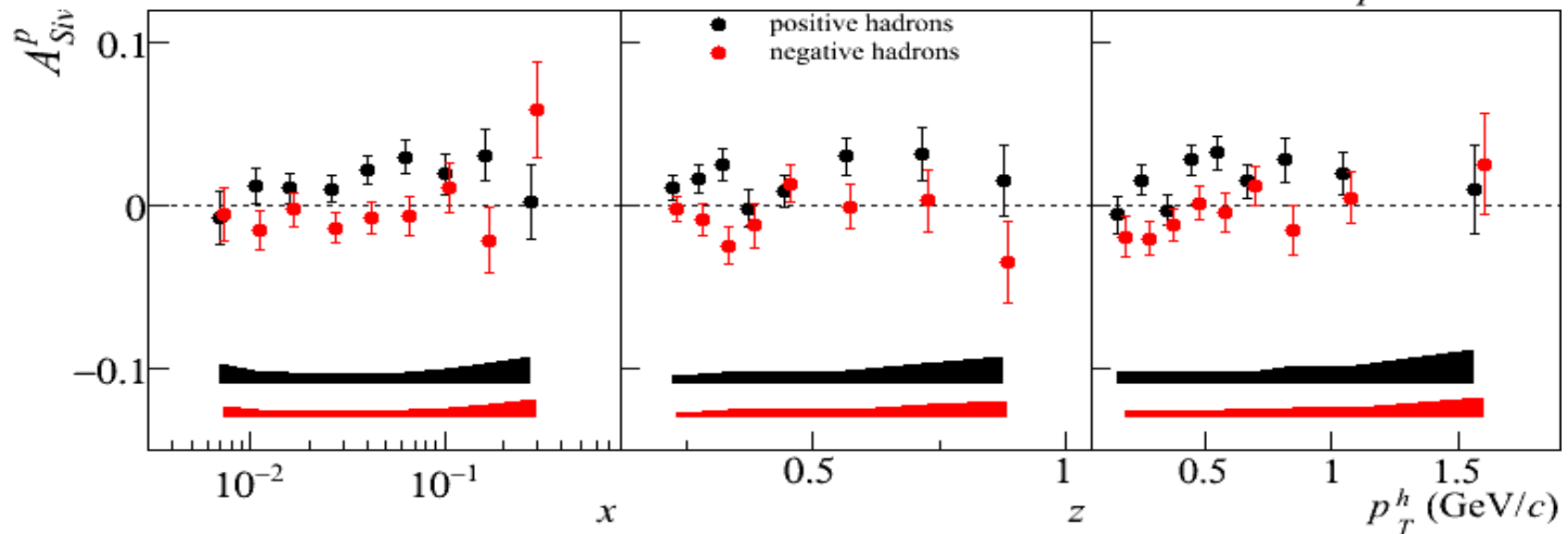
M. Boglione

# Sivers asymmetry - proton



final COMPASS results from 2007 data

PLB 692 (2010) 240



**evidence for a positive signal for  $h^+$ ,  
which extends to small  $x$ , in the region not measured before**

systematic errors

$$h^- \sim 0.5 \sigma_{\text{stat}}$$

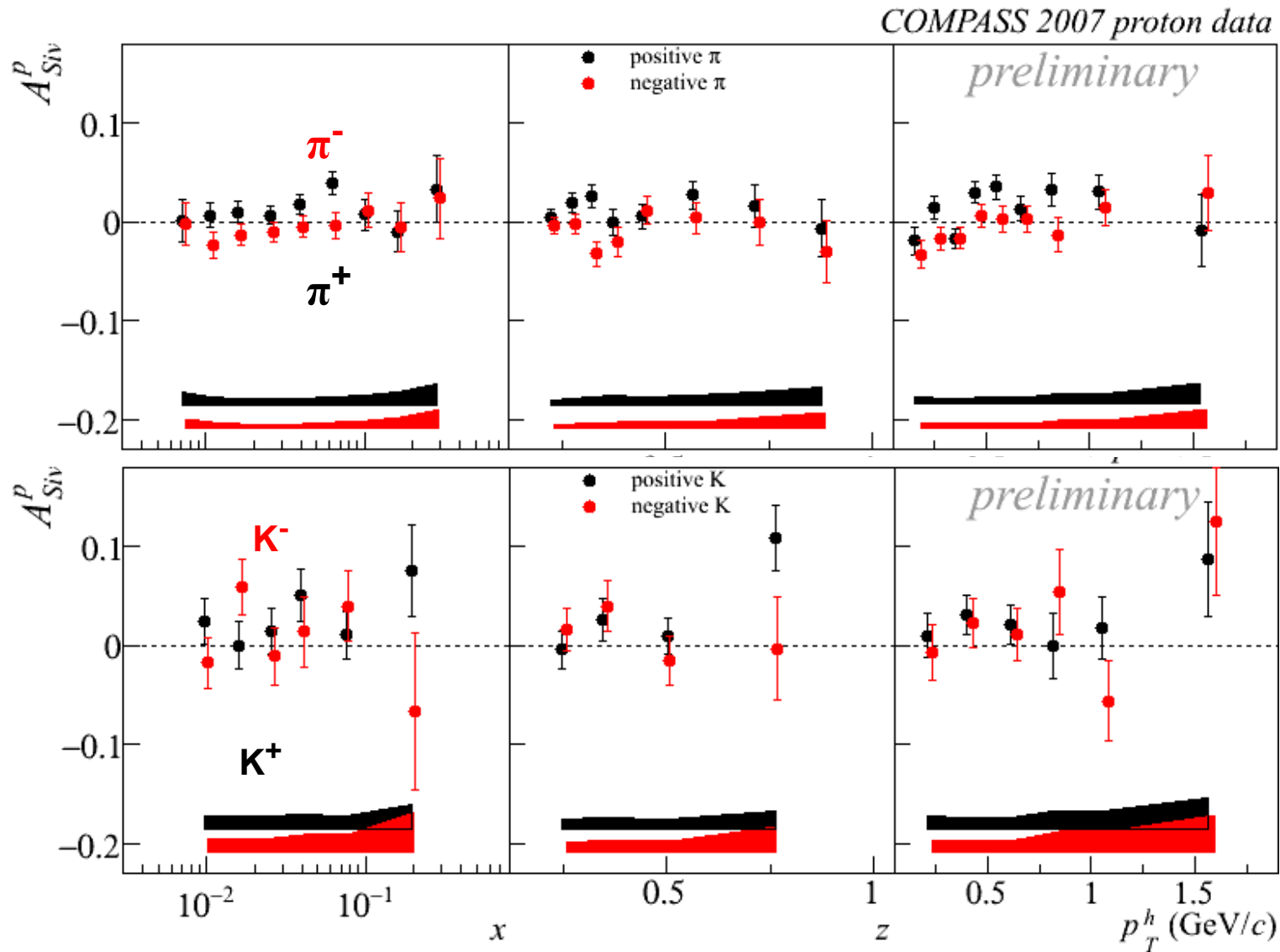
$$h^+ \sim 0.8 \sigma_{\text{stat}} \text{ plus a scale (abs) uncertainty of } \pm 0.01$$



# Sivers asymmetry - proton

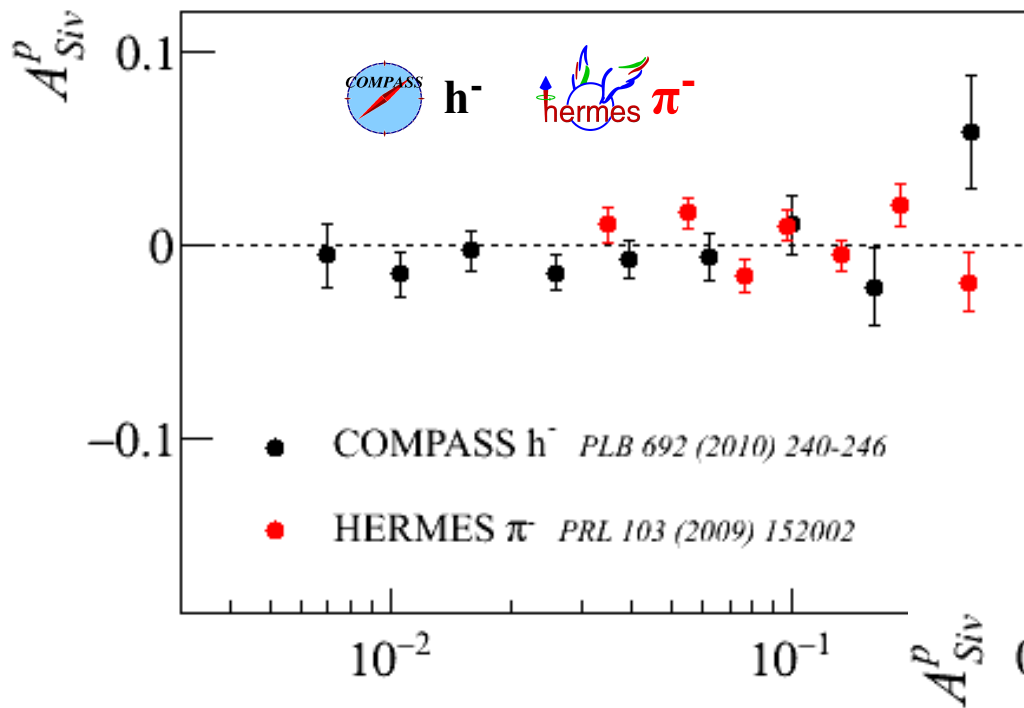


COMPASS results from 2007 data



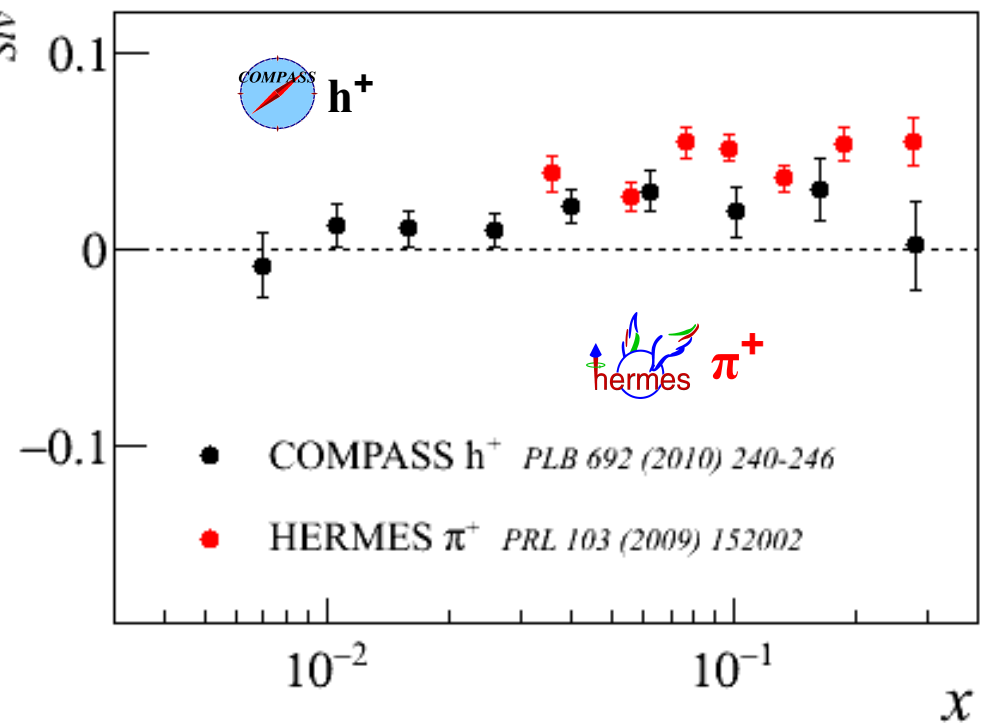


# Sivers asymmetry - proton

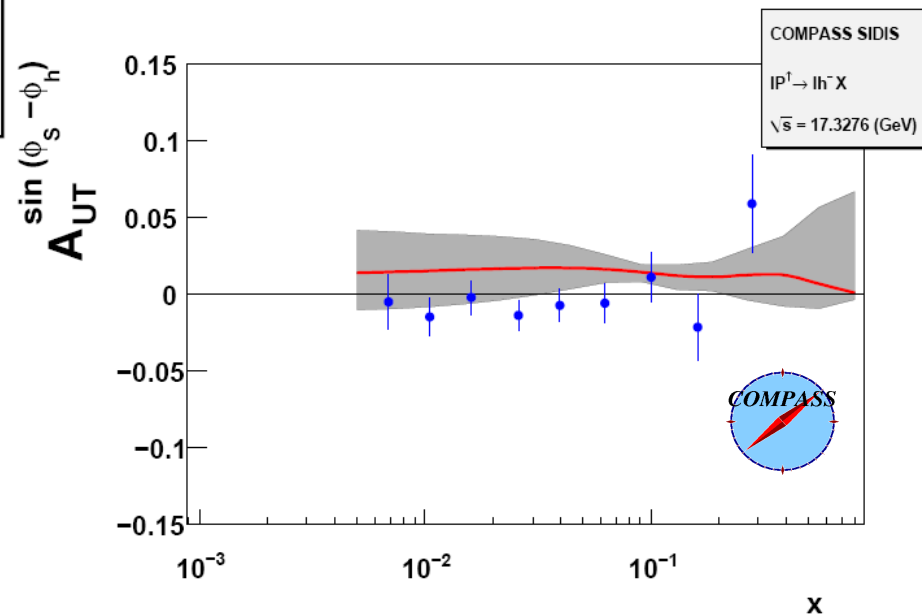
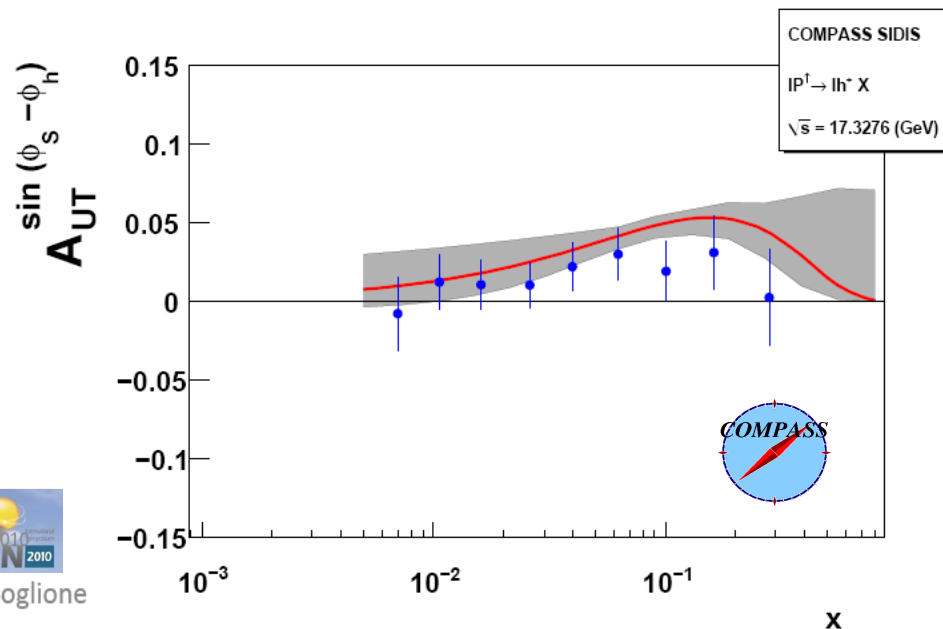


good agreements

- same sign
- COMPASS results in the overlap region smaller by a factor  $\sim 2$

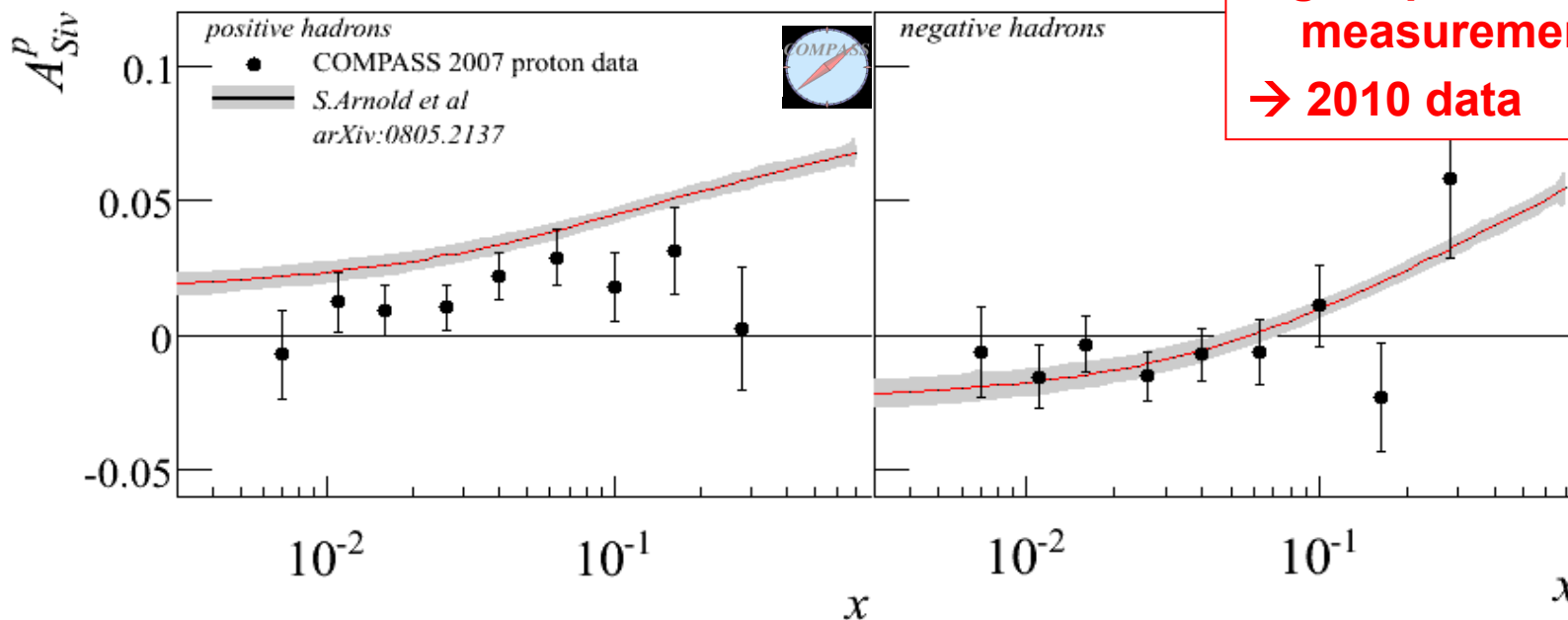


# Sivers asymmetry - proton



M. Boglione

**higher precision  
 measurements needed  
 → 2010 data**



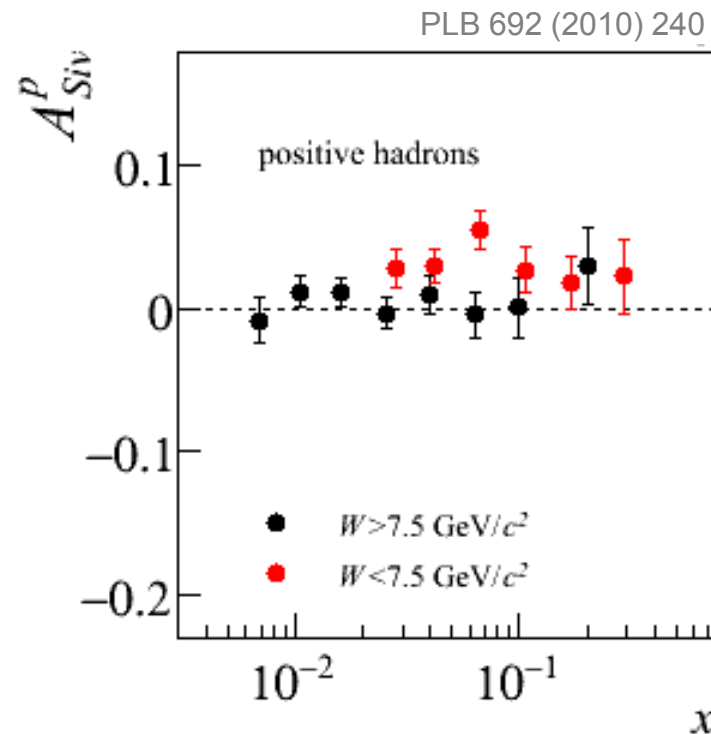
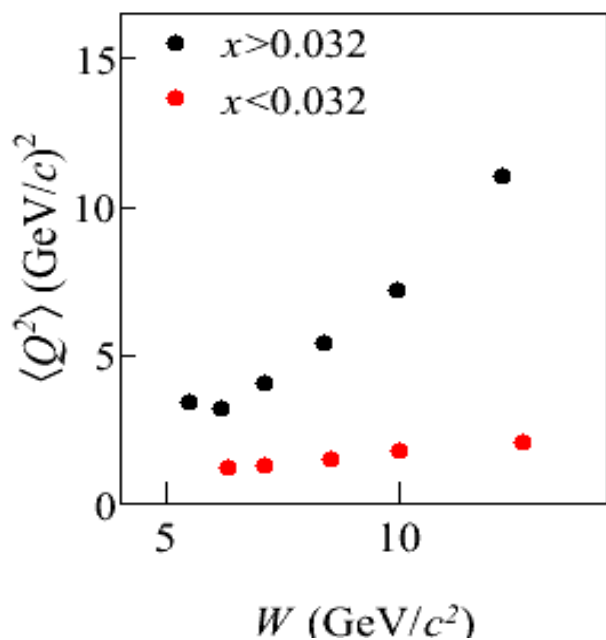
# Sivers asymmetry - proton



hints for a possible **unexpected**  
W dependence of the  $h^+$  Sivers asymmetry

same effect in  $K^+$  asymmetry (SPIN2010)

$Q^2$  dependence?



**no definite conclusion with  
the present accuracy:  
higher precision  
measurements are needed  
→ 2010 data**

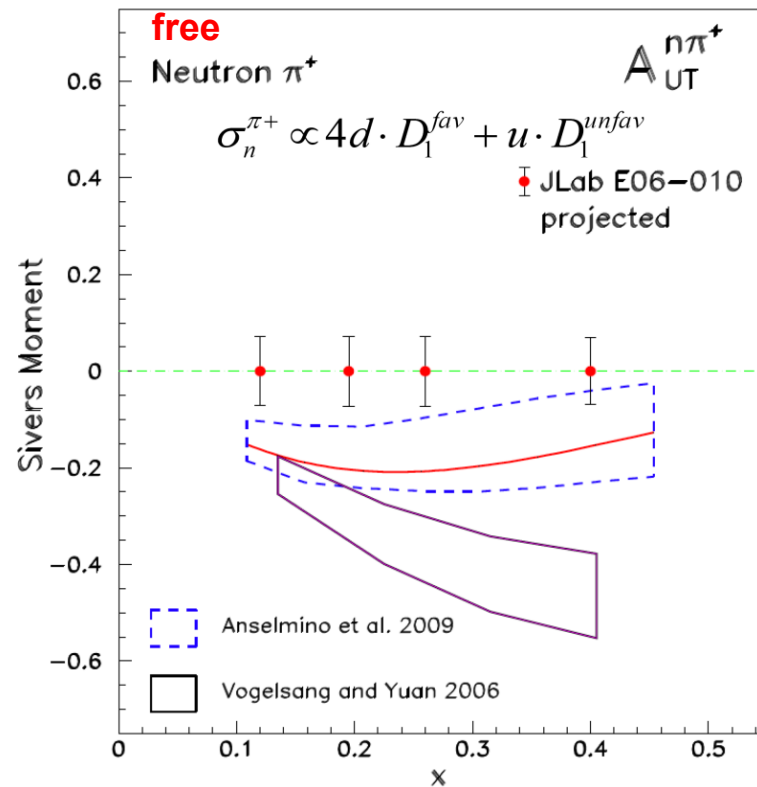
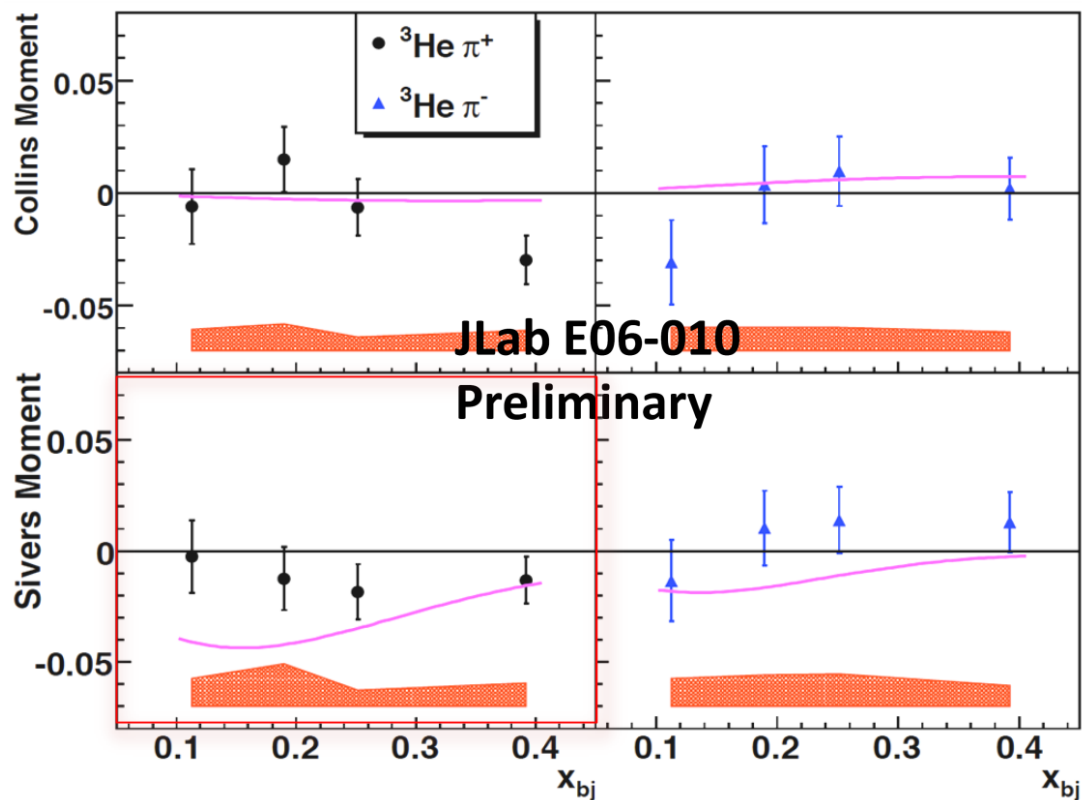


# Sivers asymmetry

## JLab E06-010 experiment

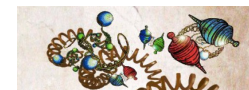
To extract information on neutron,  
one would assume :

$${}^3\text{He}^\uparrow = 0.865 \cdot n^\uparrow - 2 \times 0.028 \cdot p^\uparrow$$



${}^3\text{He}$  Collins SSA are not large (as expected).

${}^3\text{He}$  Sivers SSA are smaller than expected (vs Vogelsong and Yuan 2006), follow the trend of Anselmino et al. 2009.



# azimuthal asymmetries

## transverse target polarisation

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \dots$$

Sivers asymmetry

$$+ |\mathbf{S}_\perp| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right]$$

Collins asymmetry

$$+ \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)}$$

$$+ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)}$$

$$+ |\mathbf{S}_\perp| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right]$$

$$+ \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \left. \vphantom{\sqrt{2\varepsilon(1-\varepsilon)}} \right\}$$

$h_{IT}^\perp H_L^\perp$

$g_{IT} D_L$

# azimuthal asymmetries transverse target polarisation

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \dots$$

$$+ |\mathbf{S}_\perp| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon \right. \right.$$

$$\left. + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \right.$$

$$\left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right]$$

$$+ |\mathbf{S}_\perp| \lambda_\sigma \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{TT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{TT}^{\cos\phi_S} \right]$$



preliminary results

all the other 6 are small,  
compatible with zero both on p and d

$F_{LT}^{\cos(\phi_h - \phi_S)}$  positive for  $\pi^-$  on  $^3\text{He}$   
at JLab E06-010



$F_{UT}^{\sin\phi_S}$  different from zero

$h_\perp^\perp H_\perp^\perp$

$g_{IT} D_\perp$

# azimuthal asymmetries

## longitudinal target polarisation

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \dots$$

$$+ S_{\parallel} \lambda_e \left[ \sqrt{1 - \varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1 - \varepsilon)} \cos \phi_h \underbrace{F_{LL}^{\cos \phi_h}}_{\text{twist 3}} \right]$$

$$+ S_{\parallel} \left[ \sqrt{2\varepsilon(1 + \varepsilon)} \sin \phi_h \underbrace{F_{UL}^{\sin \phi_h}}_{\text{twist 3}} + \varepsilon \sin(2\phi_h) \underbrace{F_{UL}^{\sin 2\phi_h}}_{\substack{h_{iL}^{\perp} H_i^{\perp} \\ \text{worm-gear}}} \right]$$



**no clear signal** (on deuteron)

EPJC 70 (2010) 39

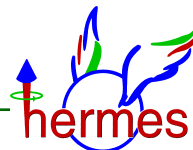
$F_{UL}^{\sin 2\phi_h}$

**from CLAS**

arXiv:1003.4549

$F_{UL}^{\sin \phi_h}$

**from HERMES**



...  
PLB 562(2003)182  
PLB 622(2005)14



# azimuthal asymmetries

## unpolarised target

### 3 independent azimuthal modulations

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right.$$

$$\left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} + \dots \right\}$$

**twist-3**





# azimuthal asymmetries unpolarised target

## 3 independent azimuthal modulations

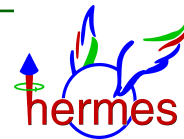
$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right. \\ \left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} + \dots \right\}$$

**twist-3**

*preliminary results*



**positive**  
**for positive hadrons (d)**



**positive for**  
**positive pions (p,d)**

**CLAS: positive for**  
**positive pions (p)**



# azimuthal asymmetries unpolarised target

## 3 independent azimuthal modulations

**Cahn effect** **Boer - Mulders**  
× Collins FF

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right.$$

$$\left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} + \dots \right\}$$

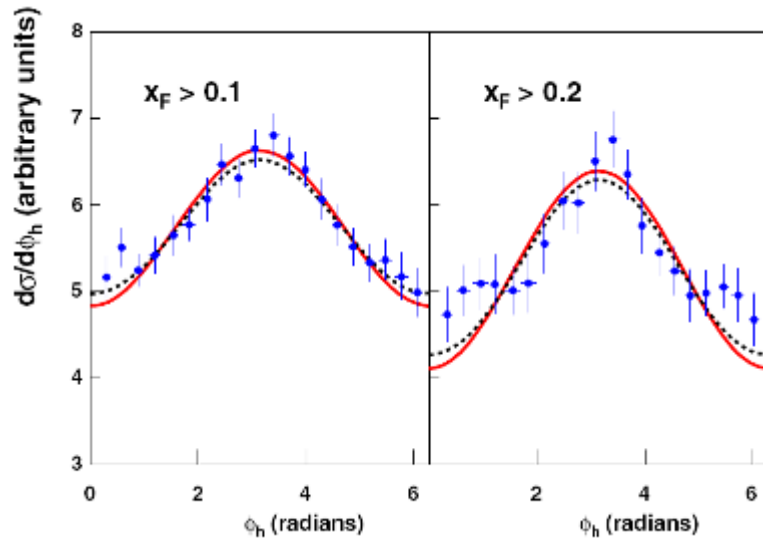
$$\propto h_1^\perp \otimes H_1^\perp + \frac{1}{Q^2} f_1 \otimes D_1$$

**Boer - Mulders** **Cahn effect**  
× Collins FF



# cos $\phi$ modulation

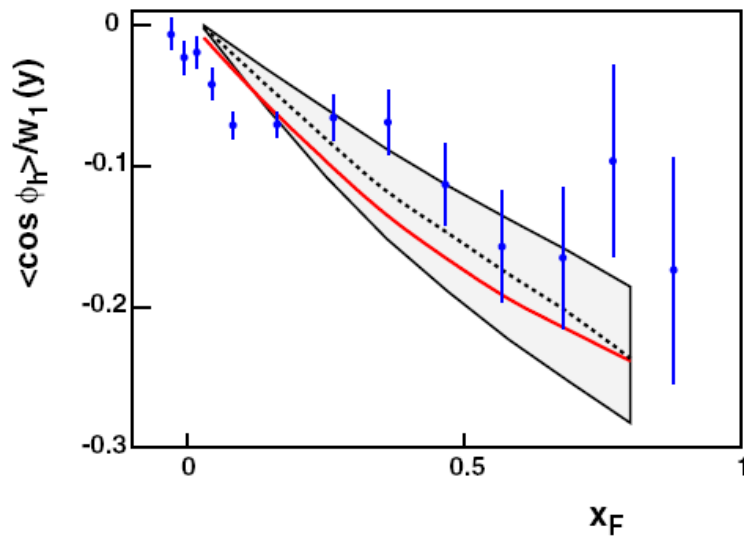
EMC 1987



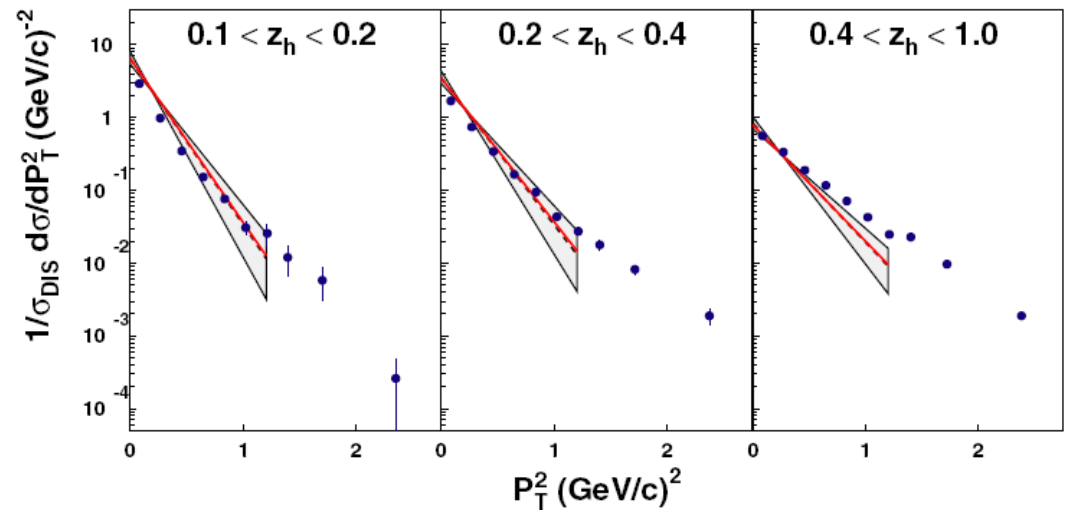
large effects  
for  $h^+ + h^-$  asymmetries

used to extract  $\langle k_T^2 \rangle$

M. Anselmino et al., PRD 71 (2005) 074006

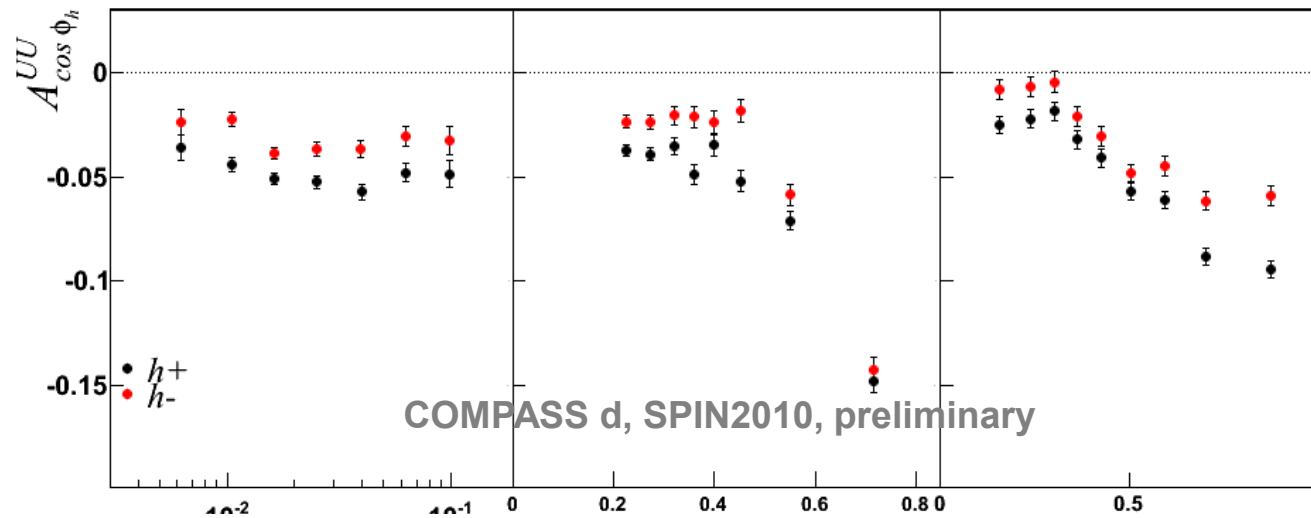


EMC 1991



# cos $\phi$ and cos $2\phi$ modulations

first results for  $h^+$  and  $h^-$  from COMPASS in 2008



## cos $\phi$

large signals over all the  $x$  range

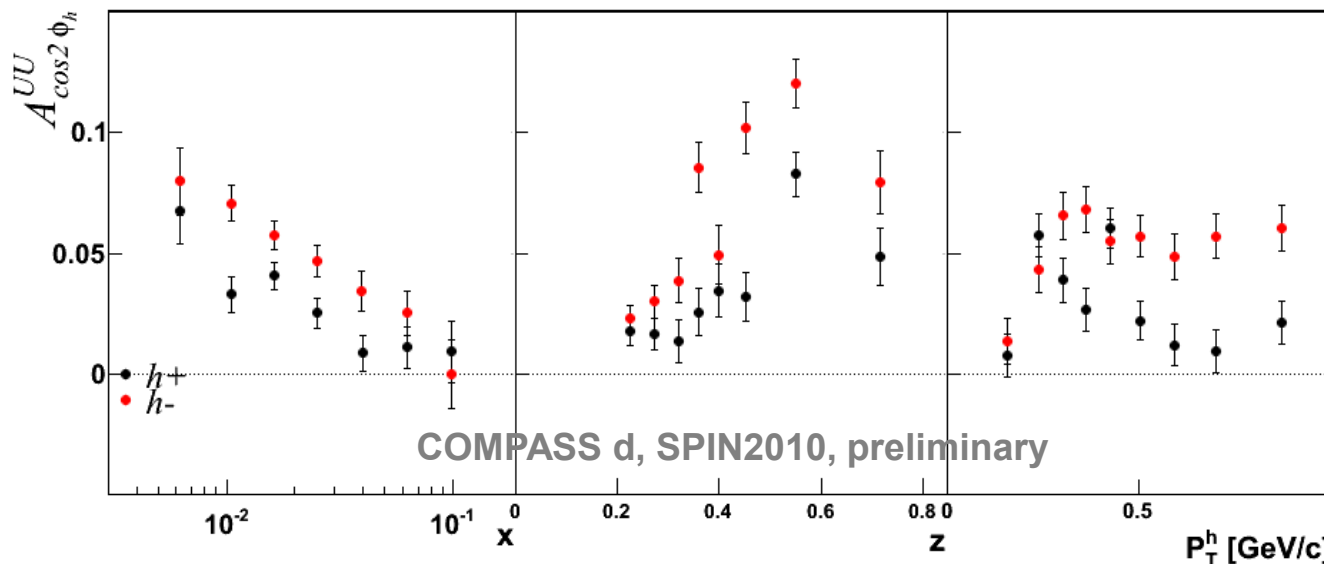
strong dependence

on  $x, z, P_T^h$

surprising,

different for  $h^+$  and  $h^-$

*Boer-Mulders contribution?*



## cos $2\phi$

large signals

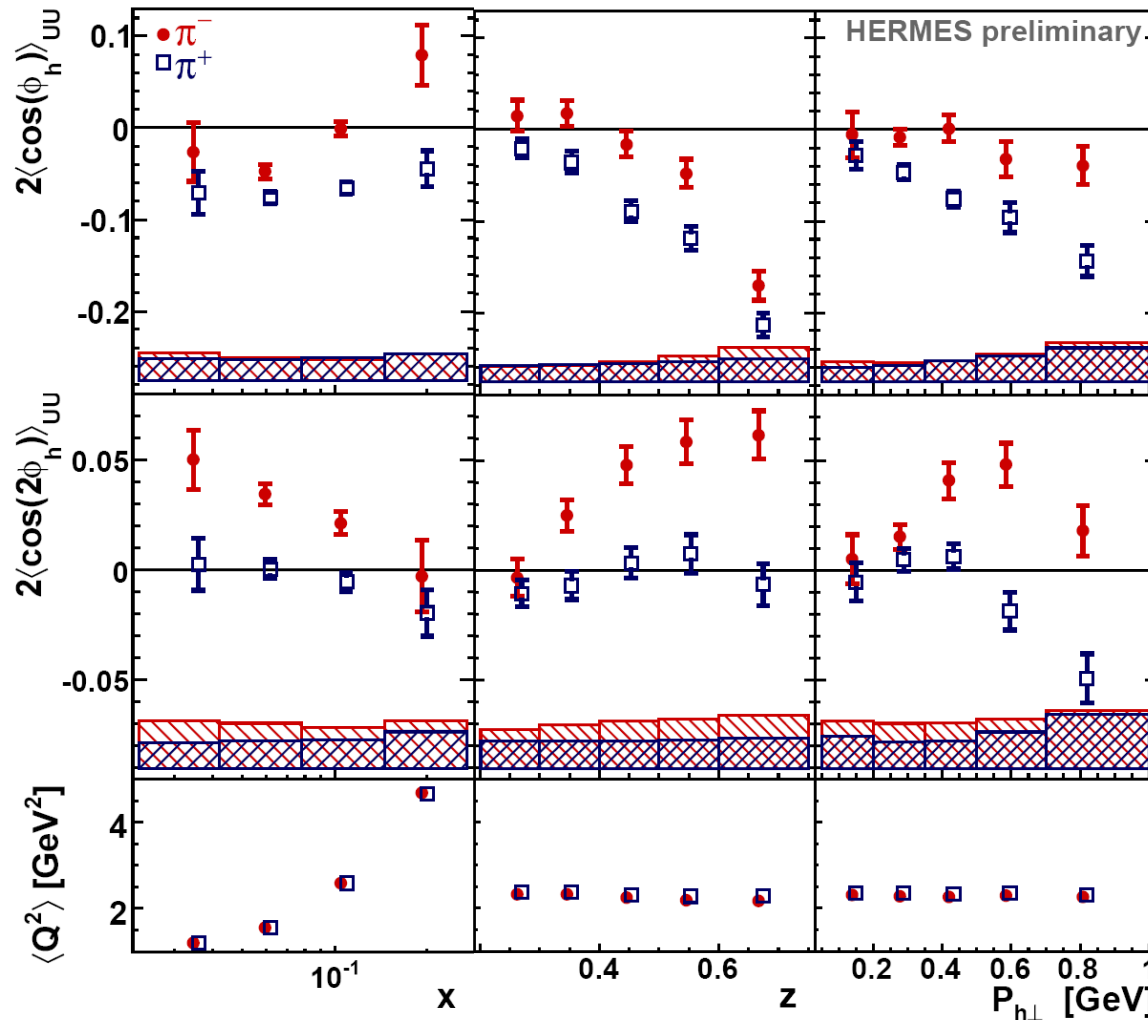
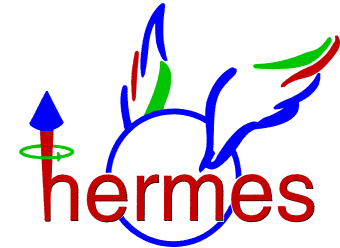
at small  $x$

strong dependence

on  $x, z, P_T^h$

different for  $h^+$  and  $h^-$

# cos $\phi$ and cos 2 $\phi$ modulations



large signals

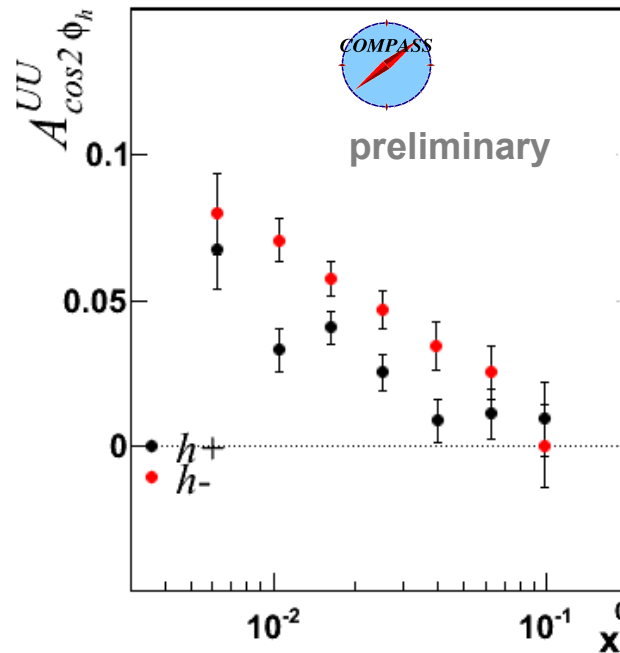
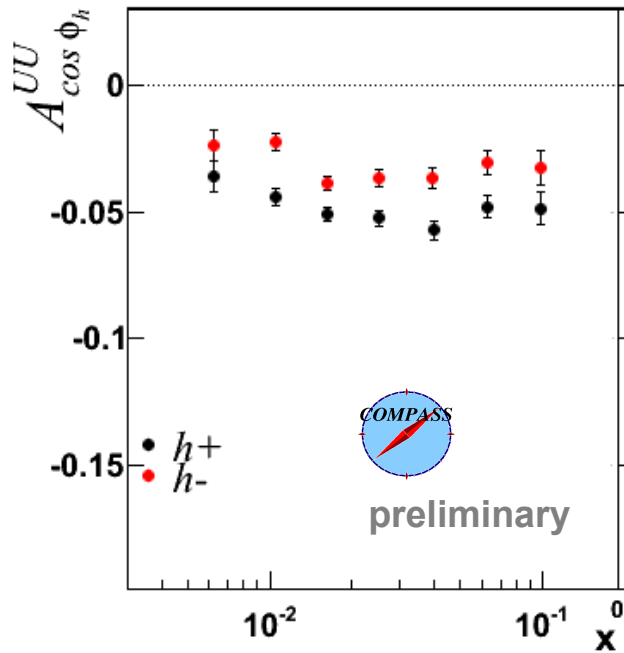
strong dependence  
on  $x, z, P_T^h$

different values  
for  $\pi^+$  and  $\pi^-$

deuteron (very similar for proton)



# cos $\phi$ and cos $2\phi$ modulations

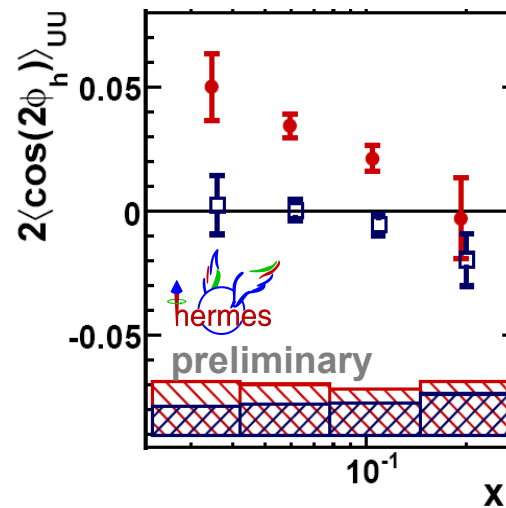
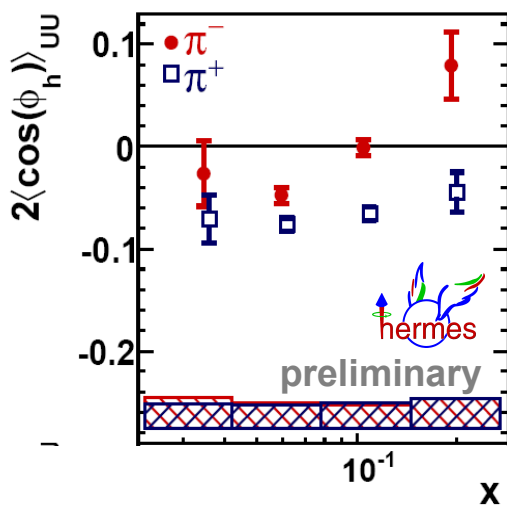


different contributions of the Boer-Mulders term at HERMES and COMPASS?

from first fits to extract the B-M function (Barone et al.)

- difficult to fit all the data

- Cahn contribution not negligible

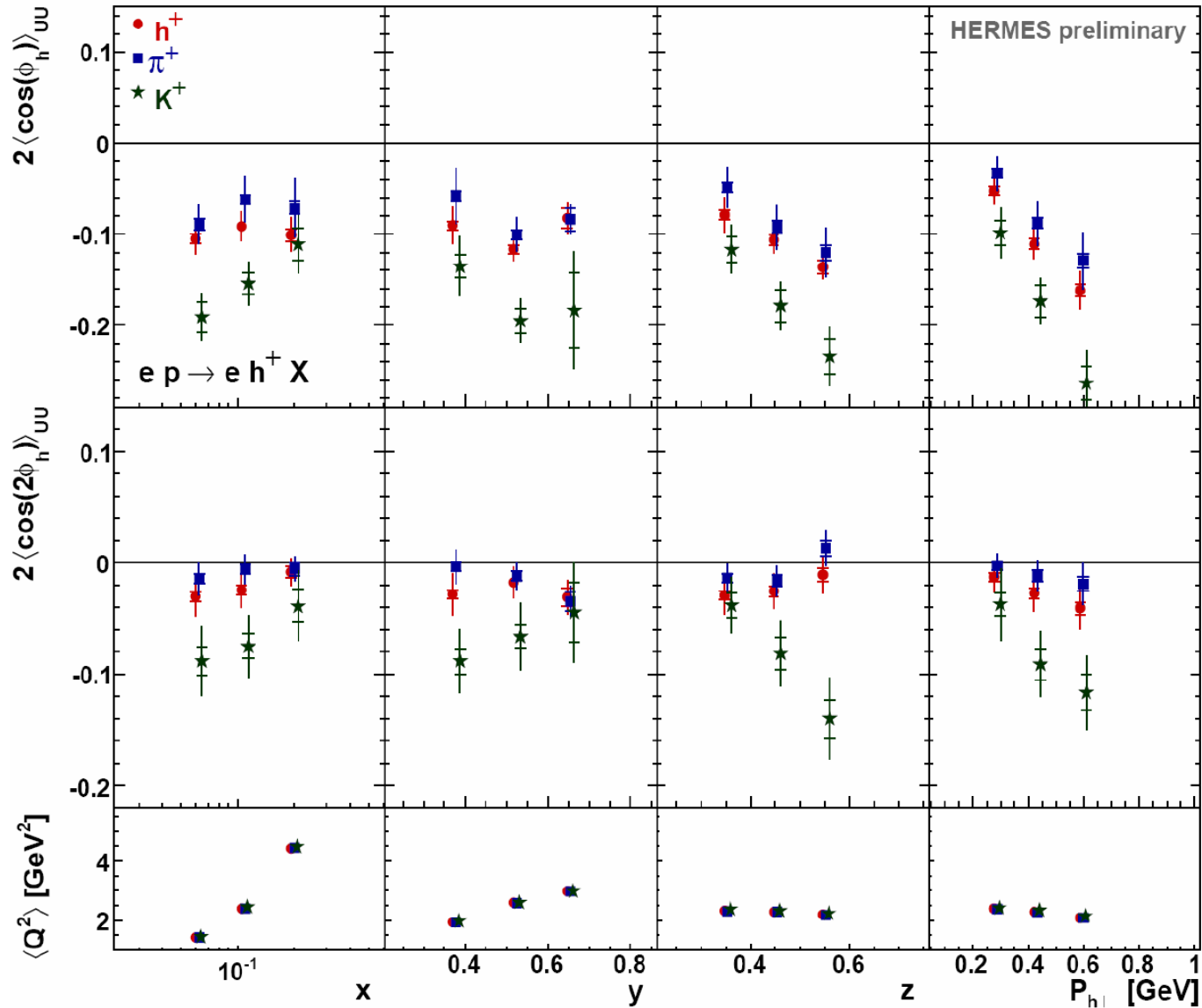
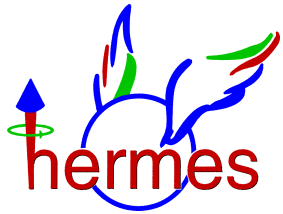


deuteron data



# cos $\phi$ and cos $2\phi$ modulations

surprising ...!



# unpolarised target SIDIS differential cross-section

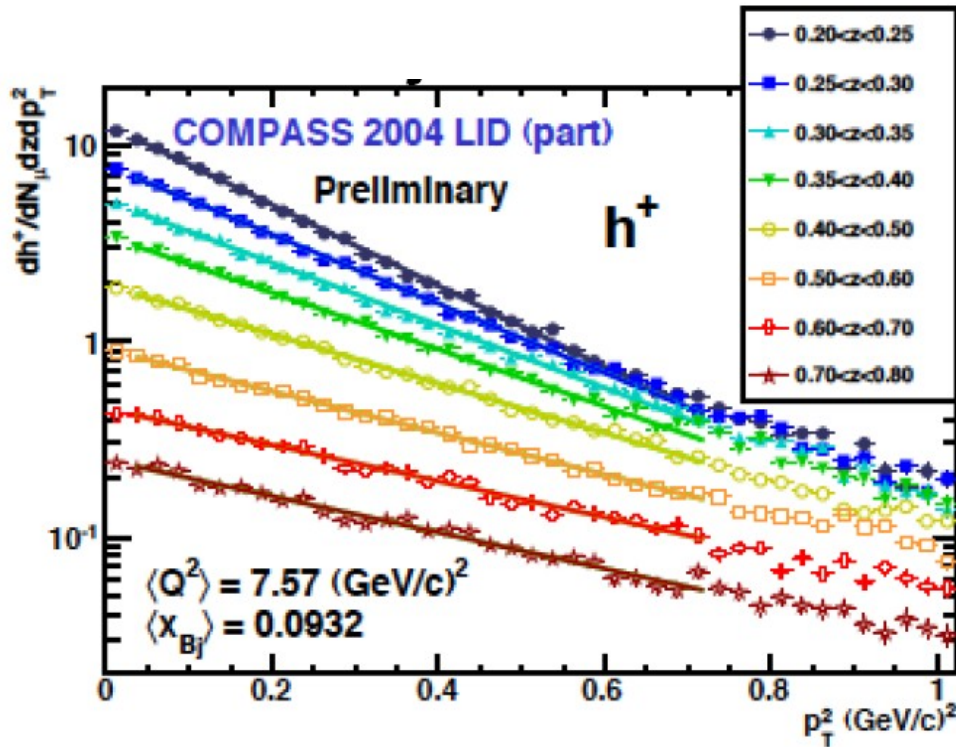




# unpolarised target SIDIS differential cross-section

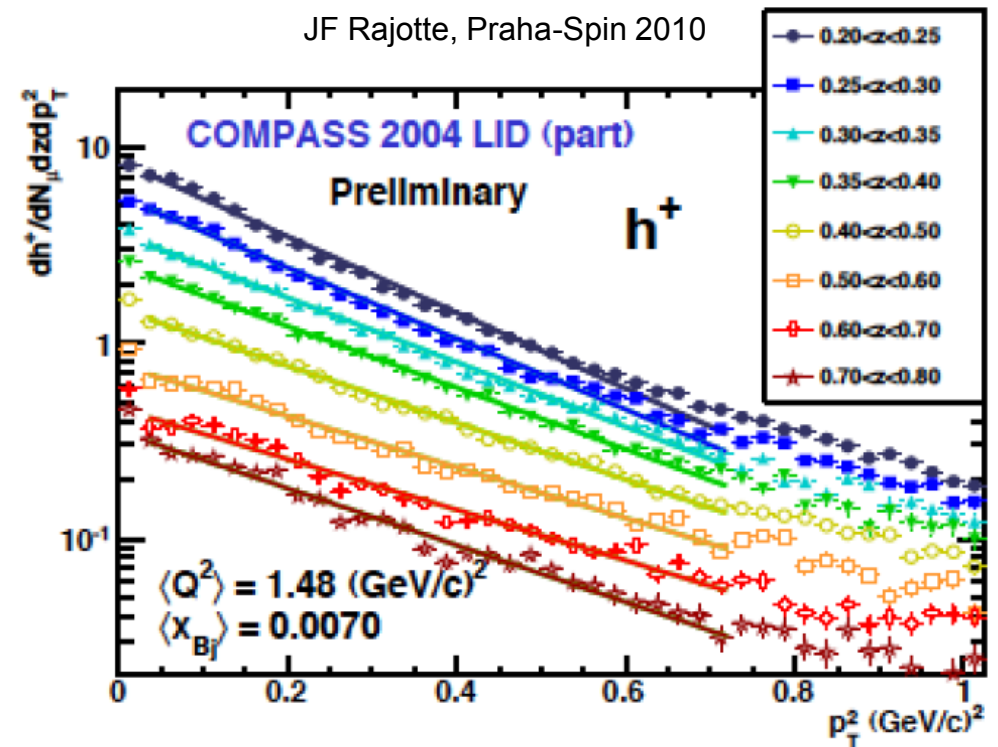


deuteron



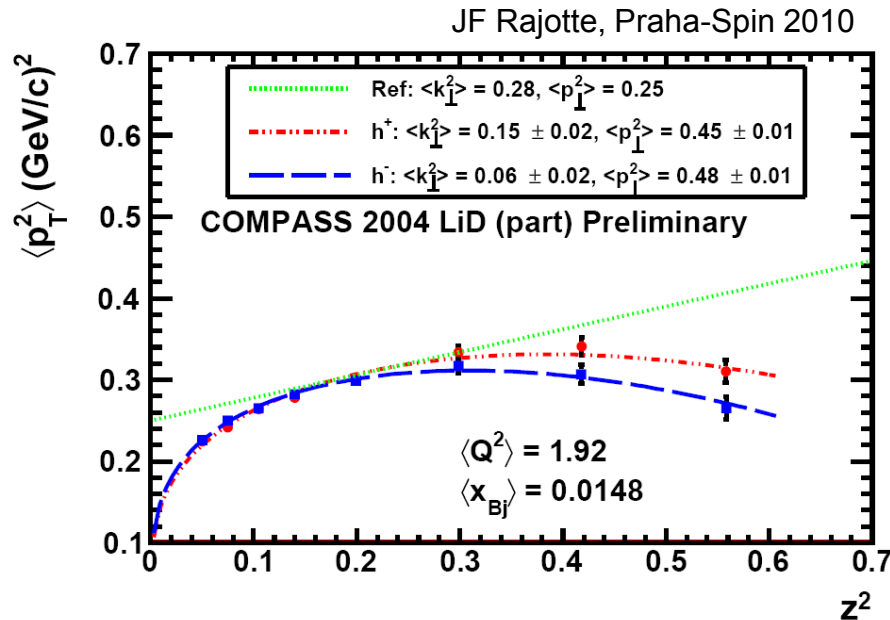
hadron multiplicity  
vs transverse momentum of  
the final state hadrons

JF Rajotte, Praha-Spin 2010



as well as the  $\cos \phi_h$  asymmetry,  
these data can be used to extract  
the intrinsic transverse momentum

# unpolarised target SIDIS differential cross-section



the expected behaviour

$$\langle p_T^2 \rangle = \langle p_{\perp}^2 \rangle + z^2 \langle k_{\perp}^2 \rangle$$

final state hadron  $\uparrow$  FF PDF

does not reproduce the data  
as already known

using

$$\langle p_T^2 \rangle = z^{\alpha} (1 - z)^{\beta} \langle p_{\perp}^2 \rangle + z^2 \langle k_{\perp}^2 \rangle$$

the extracted  $\langle k_{\perp}^2 \rangle$  is

- smaller than in previous extractions
- different for h<sup>+</sup> and h<sup>-</sup>
- Q<sup>2</sup> dependent

a lot of interpretation work on the transverse momentum is ongoing:  
news soon ?

# summary

a lot of SIDIS results have been produced since 2005

very interesting, with some surprises

- solid evidence for: transversity PDF to be different from zero  
Sivers function to be different from zero

still, important points to be clarified

and the existing experiments will contribute

*new results will come soon from COMPASS 2010 data,  
and from JLab experiments*

- several allowed TMD asymmetries seem not to be measurable in SIDIS  
*global fits / calculations, using data from different experiments and all  
the measured SIDIS azimuthal asymmetries ?*

SIDIS is an excellent tool to study the transverse structure of the nucleon

→ short term: high energy SIDIS off unpolarised p target at COMPASS II  
JLab 12 GeV

→ longer time scale: ep collider

to know more: Transverity 2011  
<http://www.ecsac.ictp.it>

