

# Recent Results on Nucleon Spin Structure

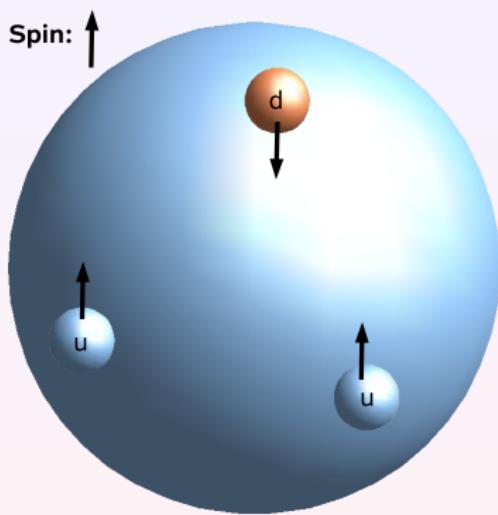
Jörg Pretz

Physikalisches Institut, Universität Bonn



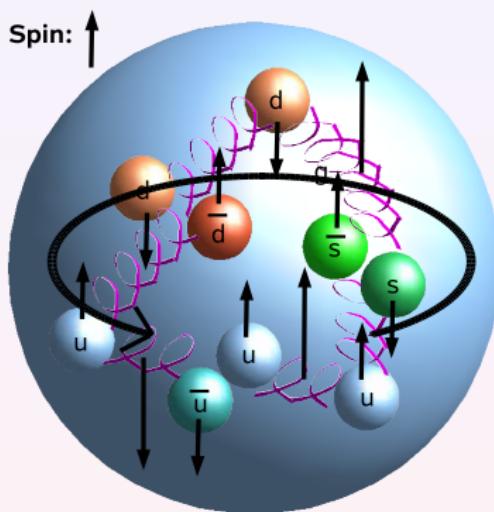
Int. Workshop on Gross Properties of Nuclei and Nuclear  
Excitations, Jan. 2011, Hirschegg, Austria

# Proton Structure ...



- ... looks simple in static quark model

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- ... looks simple in static quark model
- ... much more complicated in QCD

# Outline

- Motivation

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- Helicity Distribution  $\Delta q$  and  $\Delta G$

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- Future Projects:  
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- Summary & Outlook

# Motivation

# Motivation

## Motivation I:

Where does the Nucleon  
Spin come from?

$$\frac{1}{2} = \frac{1}{2} \Delta \Sigma + \Delta G + L_q + L_G$$

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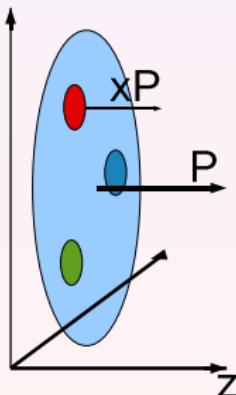
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## Motivation II:

Parton Distribution Functions:

- unpolarized  $q(x), g(x)$



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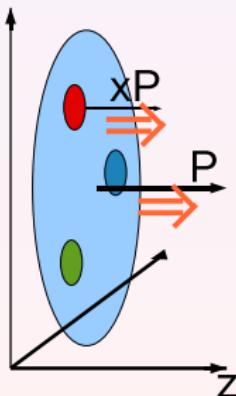
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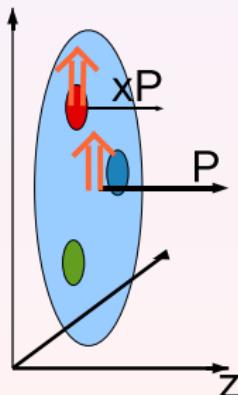
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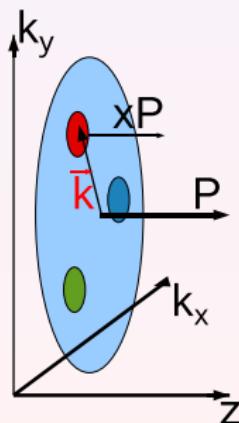
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- Transverse Momentum dependent (TMD) distributions



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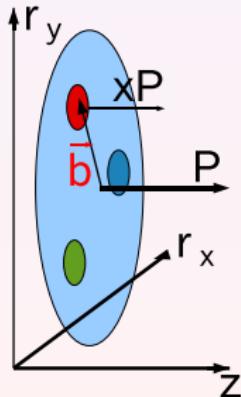
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• Transverse Momentum dependent (TMD) distributions

• Generalized Parton distributions (GPDs)

$$\Delta \Sigma = \int_0^1 \Delta u(x) + \Delta \bar{u}(x) + \Delta d(x) + \Delta \bar{d}(x) + \Delta s(x) + \Delta \bar{s}(x) dx$$

$$\Delta G = \int_0^1 \Delta g(x) dx$$

$L_q$  related to TMDs

$\Delta \Sigma + L_q$  related to GPDs

Focus in this talk:

Helicity Distributions of quarks and gluons and quarks:  $\Delta q, \Delta g$

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**Helicity** Distributions of quarks and gluons and quarks:  $\Delta q, \Delta g$

Other presentation in the workshop related to the field:

M. Boglione      Transverse Spin Structure of the Nucleon

M. Guidal      Deep Virtual Compton Scattering: from Data to GPDs

W. Vogelsang      QCD Spin Physics

A. Deshpande      Electron Ion Colliders

A. Schäfer      Nucleon Structure from the Lattice

# Helicity Distributions

# What do we know?

- $\Delta\Sigma \approx 30\%$   
But how do the different  $\Delta q(x)$ ,  $q = u, d, s, \bar{u}, \bar{d}, \bar{s}$  look like?
- $\Delta G = \int_0^1 \Delta g(x) dx$  small?  
But how small? How does  $\Delta g(x)$  look like?

# Helicity distributions

How can they be measured?

Find a process where one probes interaction  
with quark/gluon of a given polarisation  
with respect to the parent nucleon.

Can be done in two ways, using

- ① double polarisation

in Deep Inelastic Scattering:  $\vec{\ell} + \vec{N} \rightarrow \ell' + \text{hadrons} + X$

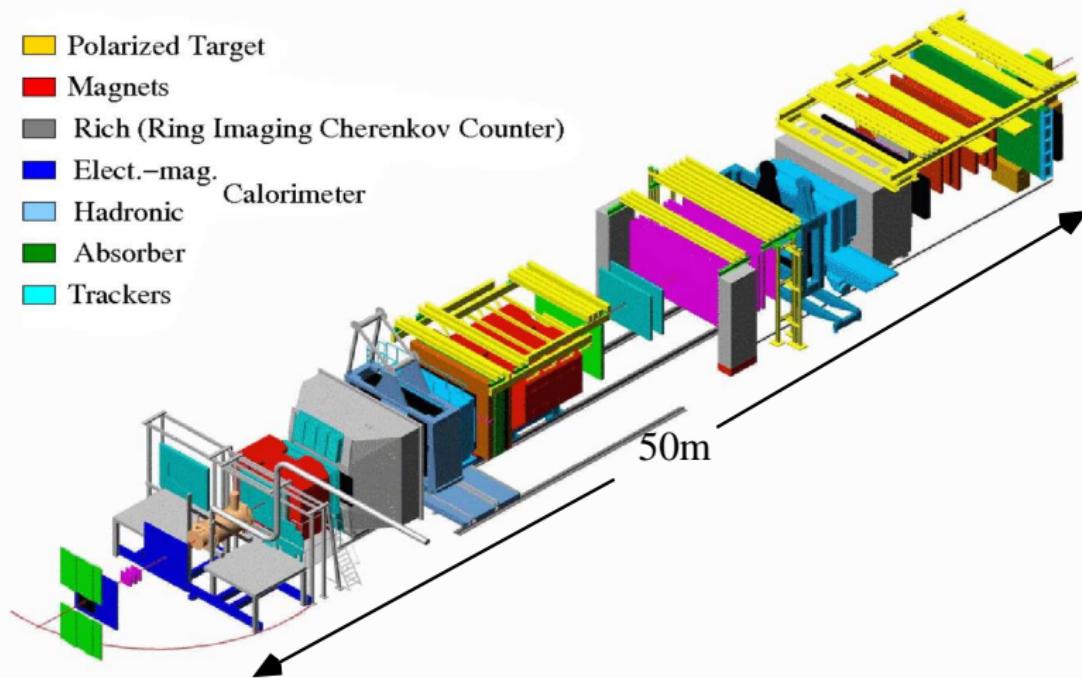
Proton-Proton Scattering:  $\vec{p} + \vec{p} \rightarrow \text{Jet}/\gamma/\text{Hadrons} + X$

- ② single polarisation & weak interaction

$\vec{p} + p \rightarrow W^\pm \rightarrow e^\pm + \nu$

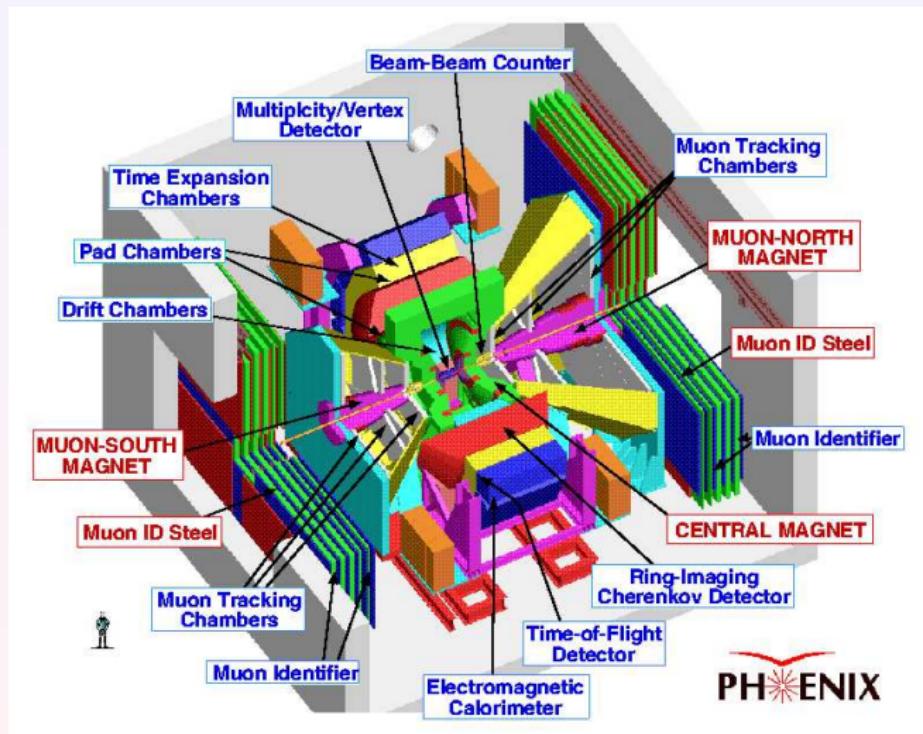
# COMPASS Experiment at CERN

- [Yellow Box] Polarized Target
- [Red Box] Magnets
- [Grey Box] Rich (Ring Imaging Cherenkov Counter)
- [Blue Box] Elect.-mag. Calorimeter
- [Light Blue Box] Hadronic
- [Dark Green Box] Absorber
- [Cyan Box] Trackers



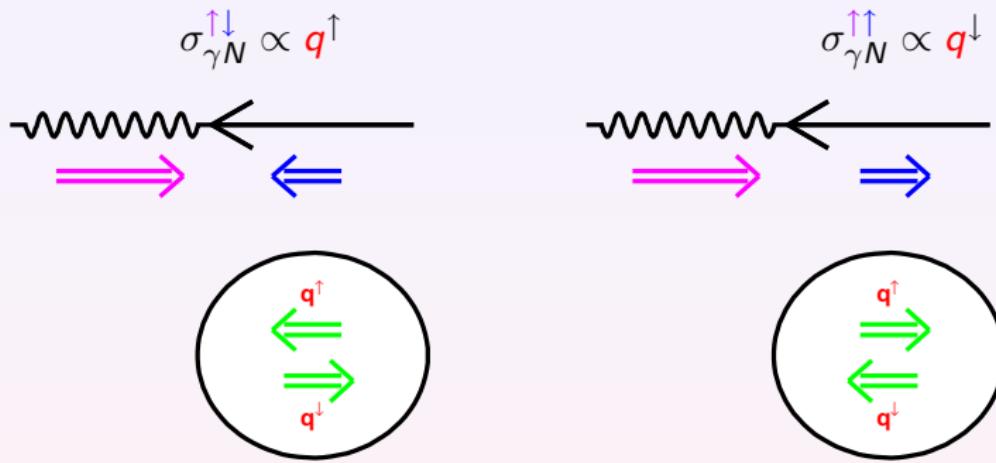
$\mu N$  scattering at  $E_\mu = 160$  GeV ( $\sqrt{s} = 18$  GeV)

# PHENIX Experiment at BNL



$pp$  collisions at  $\sqrt{s} = 200, 500$  GeV

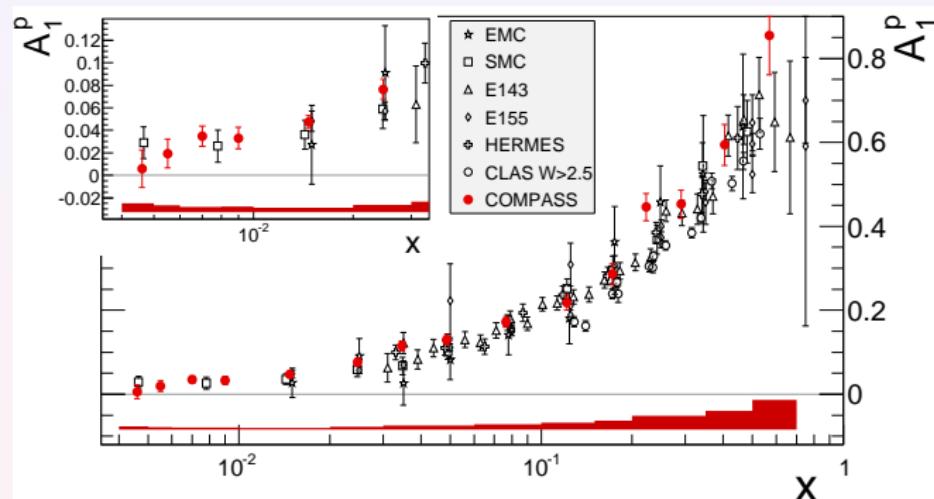
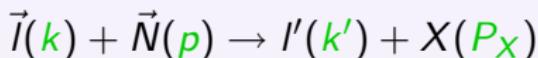
# Polarized Inclusive DIS: $\vec{\ell} + \vec{N} \rightarrow \ell' + X$



Measure double spin asymmetry:

$$A_1 = \frac{g_1}{F_1} = \frac{\sigma_{\gamma N}^{updown} - \sigma_{\gamma N}^{upup}}{\sigma_{\gamma N}^{updown} + \sigma_{\gamma N}^{upup}} = \frac{\sum_q e_q^2 (q^{\uparrow} - q^{\downarrow})}{\sum_q e_q^2 (q^{\uparrow} + q^{\downarrow})} = \frac{\sum_q e_q^2 \Delta q}{\sum_q e_q^2 q}$$

# Proton Asymmetry



$$Q^2 = -(\textcolor{red}{k} - \textcolor{blue}{k})^2$$

$$Q^2 > 1 \text{ GeV}^2$$

$$x = \frac{Q^2}{2\textcolor{blue}{p}\cdot(\textcolor{red}{k}-\textcolor{blue}{k}')} \quad \text{where } \textcolor{blue}{p} = \textcolor{red}{k} + \textcolor{blue}{k}'$$

$$A_1^p = \frac{g_1^p}{F_1^p} = \frac{4(\Delta u + \Delta \bar{u}) + (\Delta d + \Delta \bar{d}) + (\Delta s + \Delta \bar{s})}{4(u + \bar{u}) + (d + \bar{d}) + (s + \bar{s})}$$

# Results

using proton, deuteron asymmetries and weak hyperon decay constants  $F$  and  $D$ :

$$\begin{aligned}\Delta\Sigma &= 0.254 \pm 0.042 \\ \Delta s + \Delta\bar{s} &= -0.110 \pm 0.012\end{aligned}\text{at } Q^2 = 4 \text{ GeV}^2$$

E. Leader, A. V. Sidorov and D. B. Stamenov, arXiv:1010.0574 [hep-ph]

Provides only information about  $\Delta q + \Delta\bar{q}$ , because  $e_q^2 = e_{\bar{q}}^2$

# Helicity distributions

How to measure helicity distributions for different flavors?

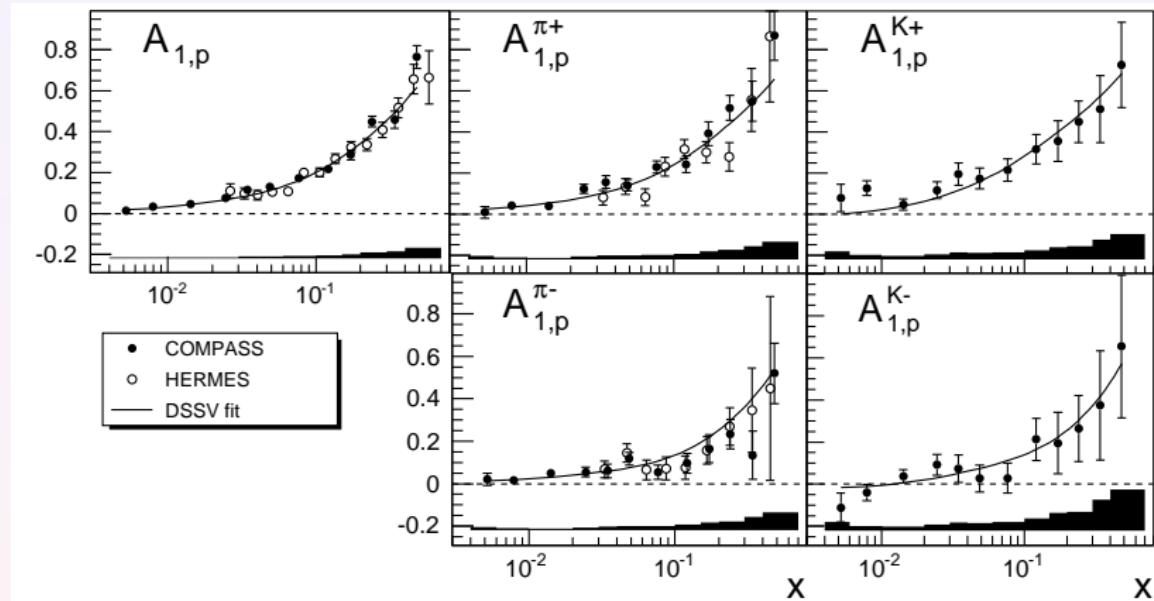
Principle:

Measure double spin asymmetries of various hadronic final states  $h$   
 in  $\vec{\ell} + \vec{N} \rightarrow \ell' + X + \text{hadrons}$

$$A^h = \frac{N_h^{\uparrow\downarrow} - N_h^{\uparrow\uparrow}}{N_h^{\uparrow\downarrow} + N_h^{\uparrow\uparrow}} \propto \frac{\sum_q e_q^2 (\Delta q(x) D_q^h(z) + \Delta \bar{q}(x) D_{\bar{q}}^h(z))}{\sum_q e_q^2 (q(x) D_q^h(z) + \bar{q}(x) D_{\bar{q}}^h(z))}$$

- $D_q^h$ : fragmentation function
- $D_q^h(z)dz$  = number of hadrons of type  $h$  produced from a quark  $q$  with energy fraction in  $[z, z + dz]$
- $D_u^{\pi^+} > D_{\bar{u}}^{\pi^+}$
- Kaon asymmetries are for example sensitive to  $\Delta s$

# Semi-Inclusive Asymmetries



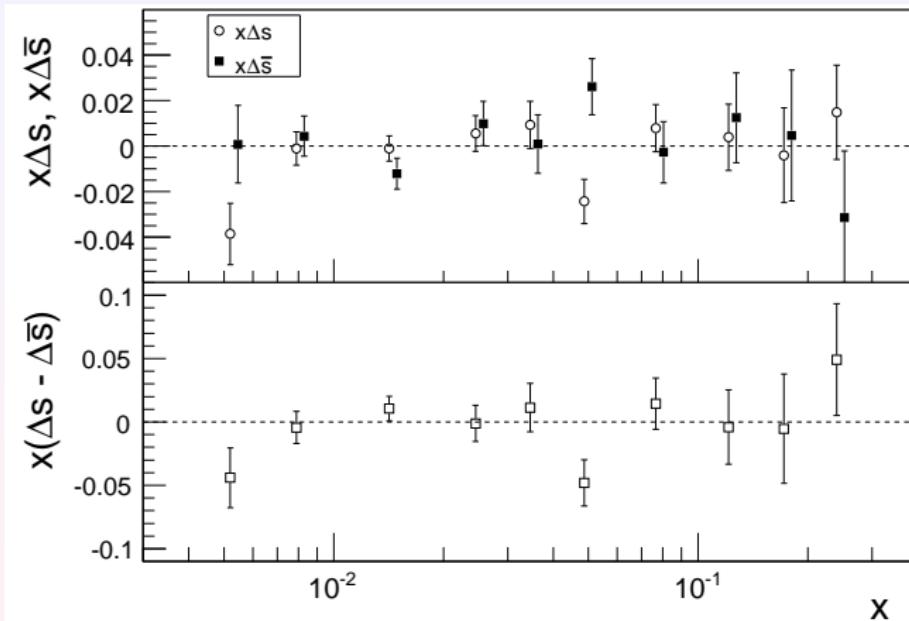
# Asymmetries $\rightarrow \Delta q$

Solve:

$$\vec{A} = B \Delta \vec{q}$$

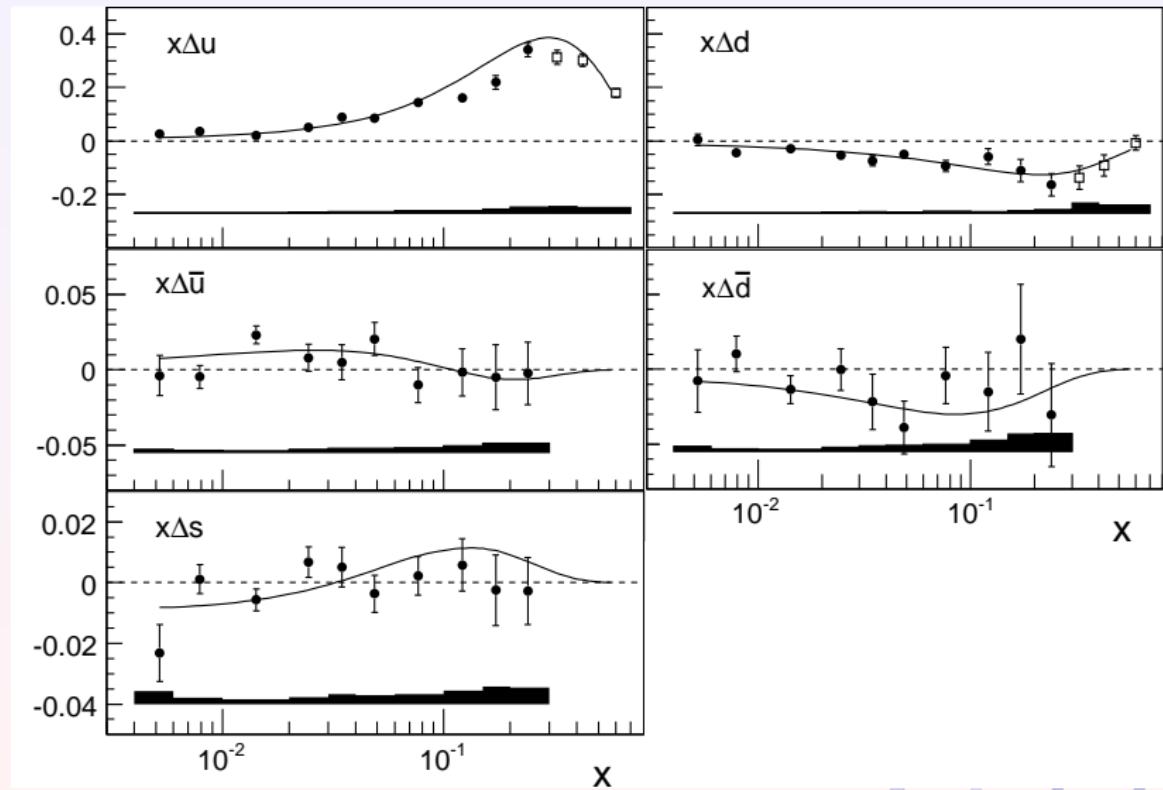
- $\vec{A} = (A_{1,p}, A_{1,p}^{\pi^+}, A_{1,p}^{K^+}, \dots, A_{1,d}, \dots, A_{1,p}^{K^-})$
- $\Delta \vec{q} = (\Delta u, \Delta d, \Delta s, \Delta \bar{u}, \Delta \bar{d}, \Delta \bar{s})$
- $B(q, \int D_q^h dz)$

# $\Delta s(x)$ and $\Delta \bar{s}(x)$ from COMPASS Data

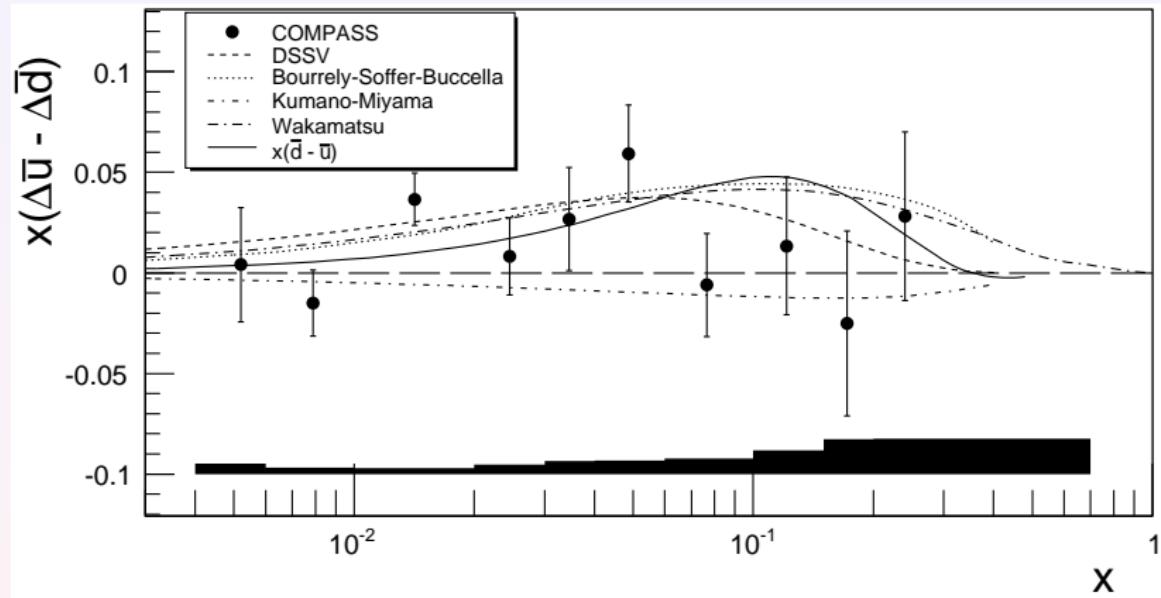


⇒ In the following assume  $\Delta s = \Delta \bar{s}$

$$\Delta u(x), \Delta d(x), \Delta s(x), \Delta \bar{u}(x), \Delta \bar{d}(x), \Delta s(x)$$



# $\Delta\bar{u}(x)$ and $\Delta\bar{d}(x)$



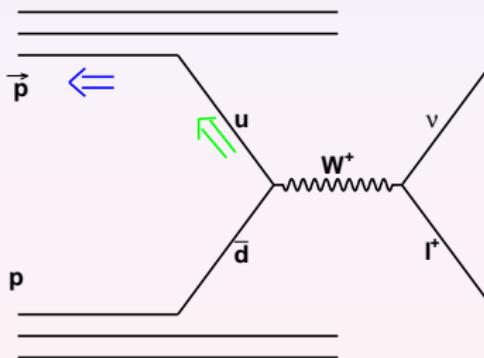
$$\int_{0.004}^{0.3} \Delta\bar{u}(x) - \Delta\bar{d}(x) dx = 0.06 \pm 0.04 \pm 0.02$$

# Summary $\Delta q$

- Statistics allowed for the first time to determine all 6 quark flavors from COMPASS data alone
- $\Delta \bar{u} - \Delta \bar{d} > 0$ ? More data will decide
- $\Delta \Sigma = 0.32 \pm 0.03$  consistent with inclusive result
- No difference found between  $\Delta s$  and  $\Delta \bar{s}$
- $\int_{0.004}^{0.3} (\Delta s + \Delta \bar{s}) dx = -0.02 \pm 0.02 \pm 0.02$  in contrast to  $\int_0^1 (\Delta s + \Delta \bar{s}) dx = -0.11 \pm 0.01$  from inclusive data & Hyperon decay constants
- Result (mainly  $\Delta s$ ) depend on fragmentation functions

# Helicity distributions from $\vec{p}p$ at RHIC

- Instead of measuring double spin asymmetries, one can measure single spin asymmetries and use weak interaction
- Done at RHIC ( $\vec{p} + p \rightarrow W^\pm \rightarrow e^\pm + \nu$  at  $\sqrt{s} = 500$  GeV)

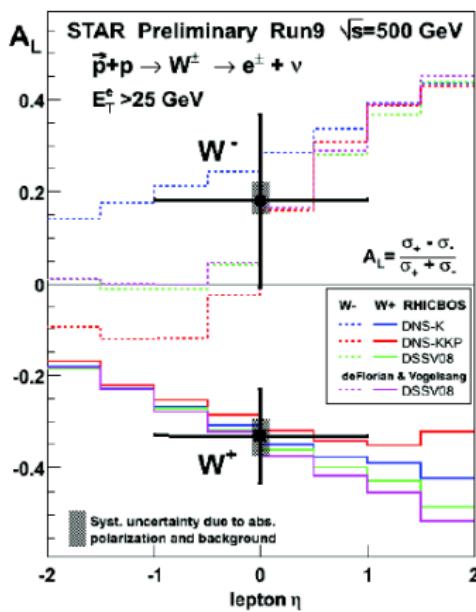


$$A_L^{W^+} = \frac{\Delta \bar{d}(x_1)u(x_2) - \Delta u(x_1)\bar{d}(x_2)}{u(x_1)\bar{d}(x_2) + \bar{d}(x_1)u(x_2)}$$

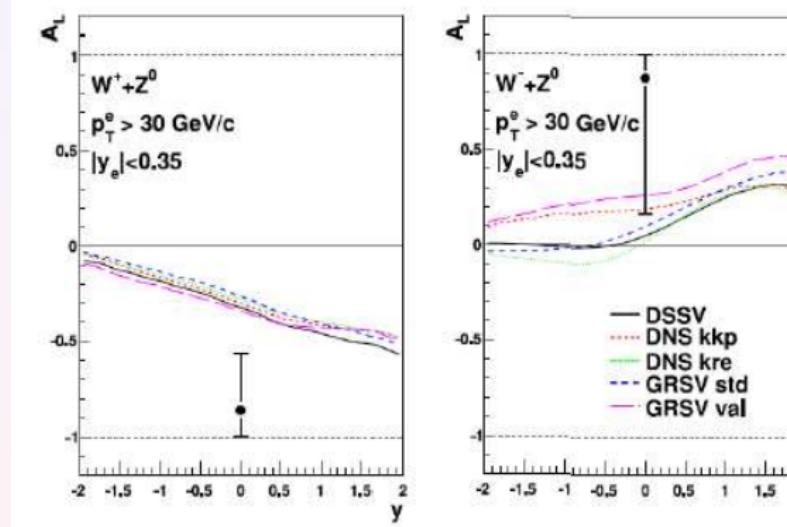
$$A_L^{W^-} = (u \leftrightarrow d)$$

# Results

## STAR



## PHENIX

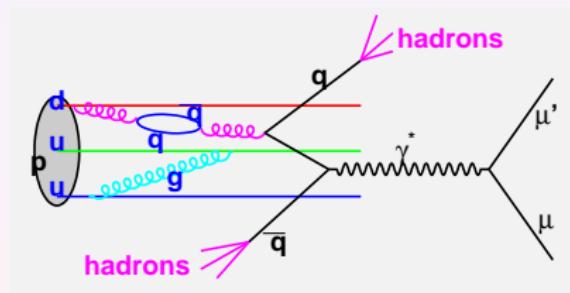


# Gluon Helicity

# How to measure $\Delta G$ ?

Use hadronic final state in DIS to tag gluon!

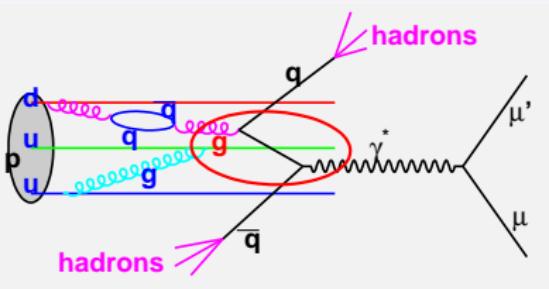
$$\vec{\mu} + \vec{N} \rightarrow \mu' + \text{hadrons} + X$$



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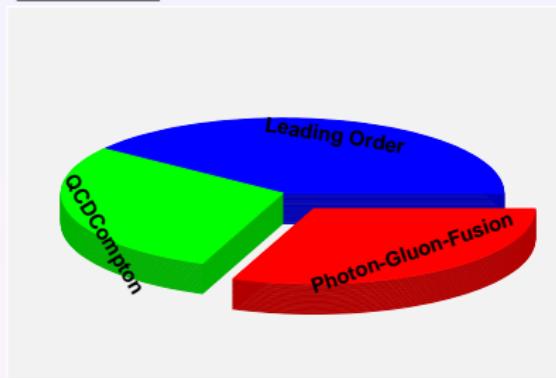
$$\vec{\mu} + \vec{N} \rightarrow \mu' + \text{hadrons} + X$$



How to tag Photon -Gluon- Fusion sub-process

$$\gamma^* g \rightarrow q\bar{q} ?$$

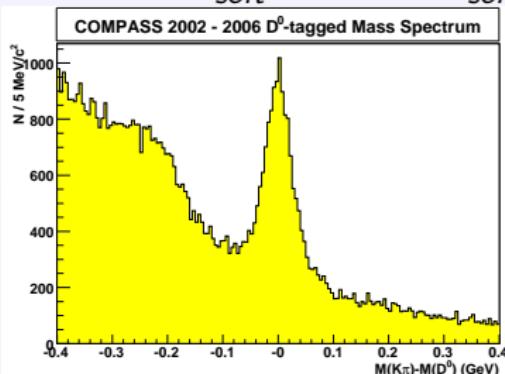
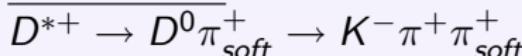
- ① open charm:  $\gamma^* g \rightarrow c\bar{c} \rightarrow D^0 + X$
- ② high  $p_T$ :  $\gamma^* g \rightarrow q\bar{q} \rightarrow \text{hadrons with large } p_T$

High  $p_T$ 

$$R = \frac{\sigma_{PGF}}{\sigma_{PGF} + \sigma_{bgd}} \approx 0.3$$

from LEPTO MC for  $Q^2 > 1 \text{ GeV}^2$   
 PYTHIA MC for  $Q^2 < 1 \text{ GeV}^2$

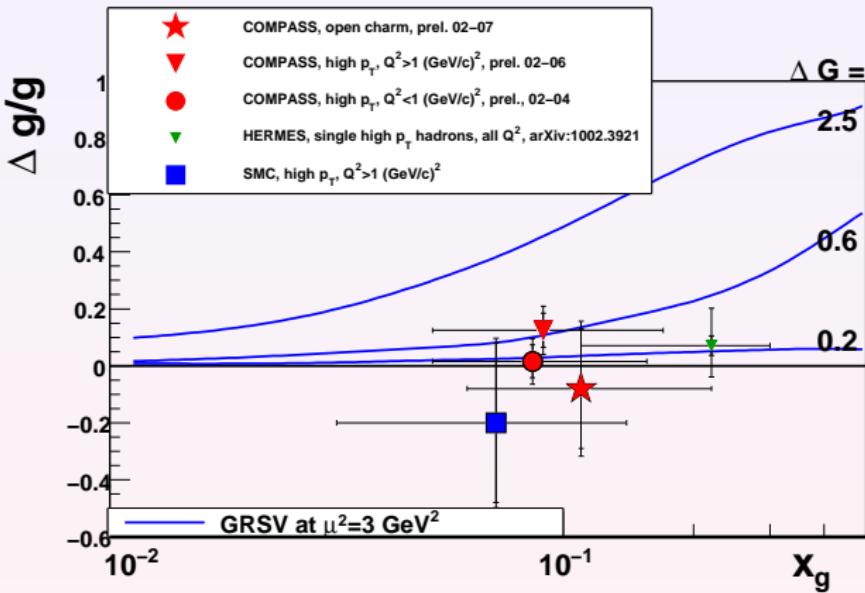
## Open Charm



$$R = \frac{\sigma_{PGF}}{\sigma_{PGF} + \sigma_{bgd}} \approx 0.5$$

from data

# Results on $\Delta G$ from DIS

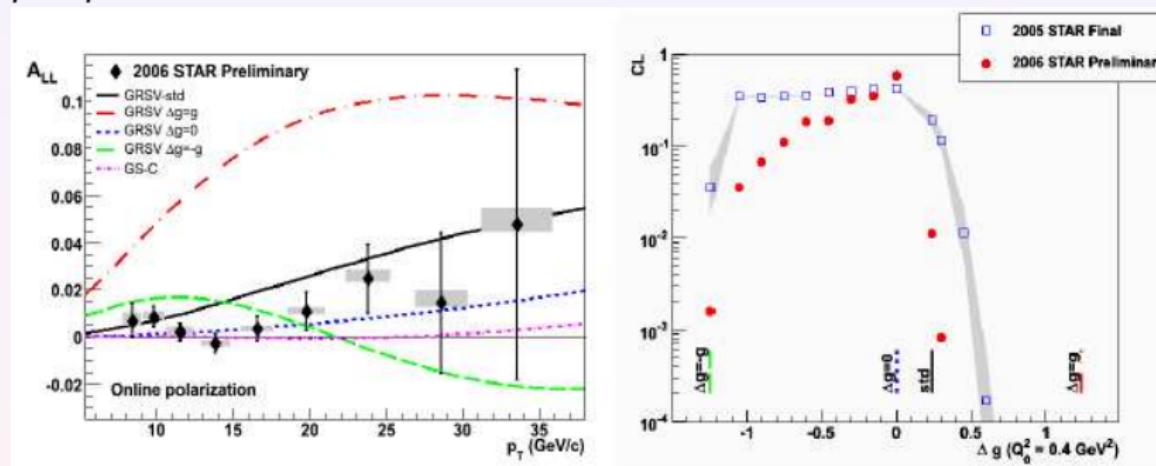


- Data show small values of  $\Delta g/g$  at  $x_g \approx 0.1$

# Results on $\Delta G$ from $\vec{p}\vec{p}$

STAR:

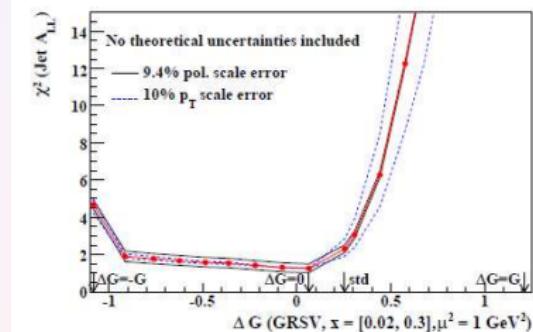
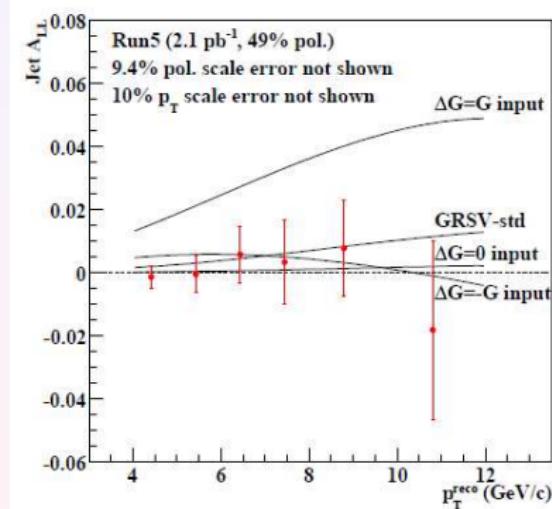
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# Results on $\Delta G$ from $\vec{p} \vec{p}$

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# Summary $\Delta G$

- $\Delta G = \int_0^1 \Delta g(x) dx \approx 0 \pm \frac{1}{2}$   
certainly small compared to large values  $\Delta G \approx 2 - 3$   
proposed to explain small of  $\Delta \Sigma \approx 30\%$ ,  
**not** small compared to the total spin of the proton of  $\frac{1}{2}!$
- $x$ -dependence not very well determined
- Note: RHIC results are in NLO QCD, (most) DIS results in LO QCD

# Future Projects

# The ENC@FAIR project

- add a 3 GeV  $e^+/e^-$  accelerator to the already planned 15 GeV HESR (High Energy Storage Ring) for  $\bar{p}$ ,  $p$
- $e^-$  and  $p$  polarized ( $P \approx 80\%$ )
- $\mathcal{L} \approx 10^{32}/\text{cm}^2/\text{s}$
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Experiment	JLab(12 GeV)	HERMES	ENC	COMPASS
$s/\text{GeV}^2$	23	50	180	300
$\mathcal{L}/(1/\text{cm}^2/\text{s})$	$\approx 10^{38}$	$\approx 10^{32}$	$\approx 10^{32}$	$\approx 10^{32}$

# Luminosity → FOM

More interesting: FOM for polarisation measurements:

$$\text{FOM} = (\text{diluting factors})^2 \mathcal{L}$$

diluting factors:	beam polarization	$P_B$
	target polarization	$P_T$
	target dilution factor	$f$
	reconstruction efficiency and purity	$r$

# Diluting Factors

	COMPASS	collider
$P_T$	0.5	0.8
$f$	0.4	1
$P_B$	0.8	0.8

COMPASS uses a solid target ( ${}^6\text{LiD}$  or  $\text{NH}_3$ )  
dilution factor  $\approx \frac{\text{nb. of polarisable nucleons}}{\text{nb. of all nucleons}} = \frac{4}{8}$  for  ${}^6\text{LiD}$

# Diluting Factors

	diluting factor COMPASS	diluting factor ENC	ratio
double spin asymmetries $(P_T f P_B)^2$	0.026	0.41	16
reconstruction of hadronic final state			$\approx 10$
mass resolution	:(	:)	
displaced vertices	:(	:)	
more $D^0$ decay ch.	:(	:)	
determination of $x_g$ due to reconstruction of $D$ and $\bar{D}$	:(	:)	

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Huge potential for polarization observables!

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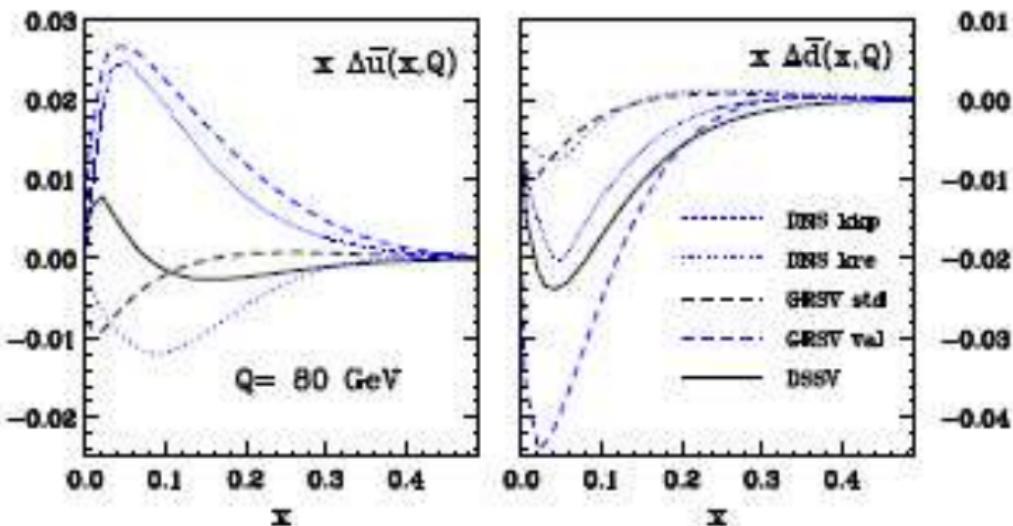
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**Generalized Parton Distributions** (GPDs) and **Transverse Momentum Distributions** (TMDs)
- An **polarized electron nucleon collider** would offer high potential for polarisation measurements

Spare

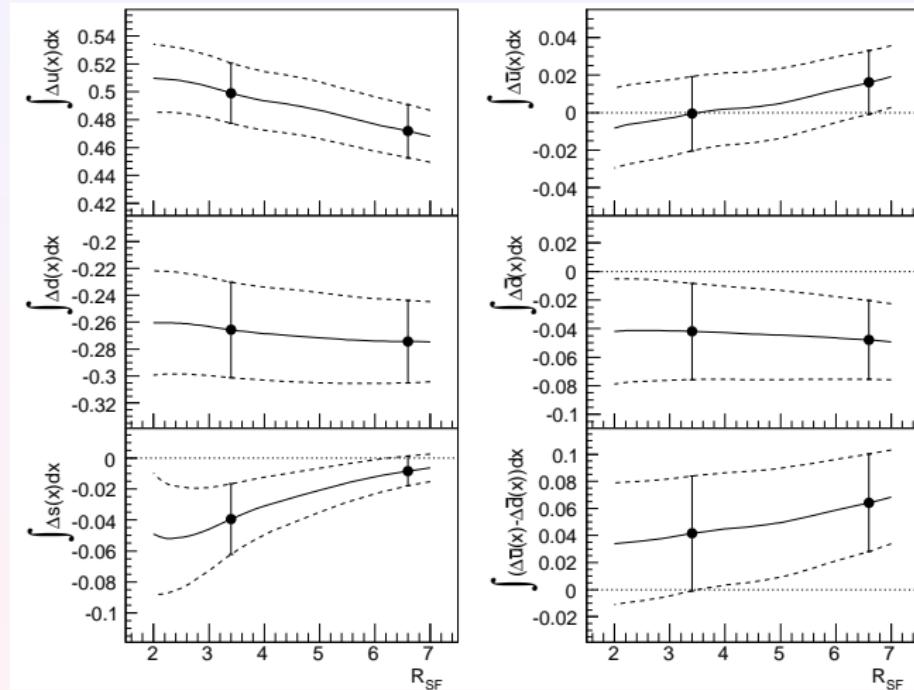
# $\Delta\bar{u}$ and $\Delta\bar{d}$

for different curves shown in  $A_{LL}^W$  plot.



D. de Florian, W. Vogelsang arXiv 1003.4533

# Dependence of SIDIS results on FF



$$R_{SF} = \frac{\int D_{\bar{s}}^{K^+}(z) dz}{\int D_u^{K^+}(z) dz}$$

# Unpol. PDFs at $Q^2 = 10 \text{ GeV}^2$

