



Quark Helicity Distributions from
Longitudinal Spin Asymmetries
in Muon-Proton and Muon-Deuteron
Scattering measured by COMPASS at CERN

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On behalf of the COMPASS Collaboration

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- Reference *arXiv:1007.4061v1[hep-ex]* (to be published in *Phys.Lett.B*)

**A short review of COMPASS
DIS and SIDIS results**

2007	$g_1^d(x), \int g_1^d(x) dx$	$\Delta\Sigma = \sum(\Delta q + \Delta\bar{q})$
2008	$A_{1,d}^{h^+ - h^-}$	$\Delta u_v + \Delta d_v$
2009	$A_{1,d}, A_{1,d}^{\pi^{+,-}}, A_{1,d}^{K^{+,-}}$	$\Delta u_v + \Delta d_v, \Delta\bar{u} + \Delta\bar{d}, \Delta s (= \Delta\bar{s})$
2010	$g_1^p(x), \int g_1^{NS}(x) dx$	$ g_A/g_V $
2010	$A_{1,d}, A_{1,d}^{\pi^{+,-}}, A_{1,d}^{K^{+,-}},$ $A_{1,p}, A_{1,p}^{\pi^{+,-}}, A_{1,p}^{K^{+,-}}$	$\Delta u, \Delta d, \Delta\bar{u}, \Delta\bar{d},$ $\Delta s, \Delta\bar{s}$

COMPASS longitudinal SIDIS data

	2002 – 2006 ${}^6\text{LiD}$ target	2007 NH_3 target
E_μ	160 GeV	160 GeV
P_μ	≈ -0.80	≈ -0.80
$ P_T $	≈ 0.50	≈ 0.90
Dilution factor f	≈ 0.37	≈ 0.14
$f P_T $	$\approx \mathbf{0.20}$	$\approx \mathbf{0.13}$

Selection criteria

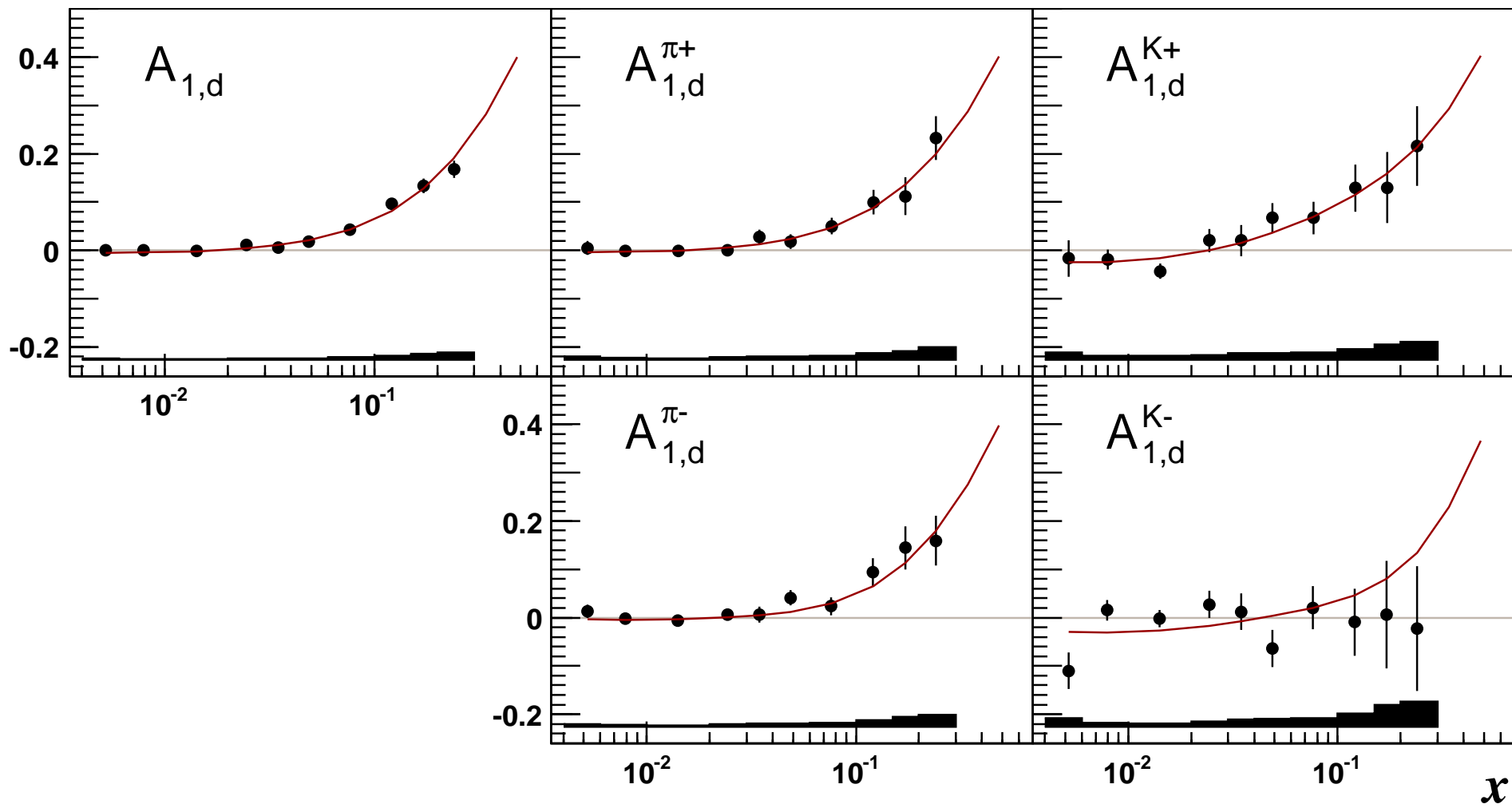
Events	Hadrons
$Q^2 > 1 \text{ (GeV/c)}^2$	$0.2 < z < 0.85$
$0.1 < y < 0.9$	$10 < P < 50 \text{ GeV/c}$
$0.004 < x < 0.7$	(RICH IDENT)

COMPASS longitudinal SIDIS data

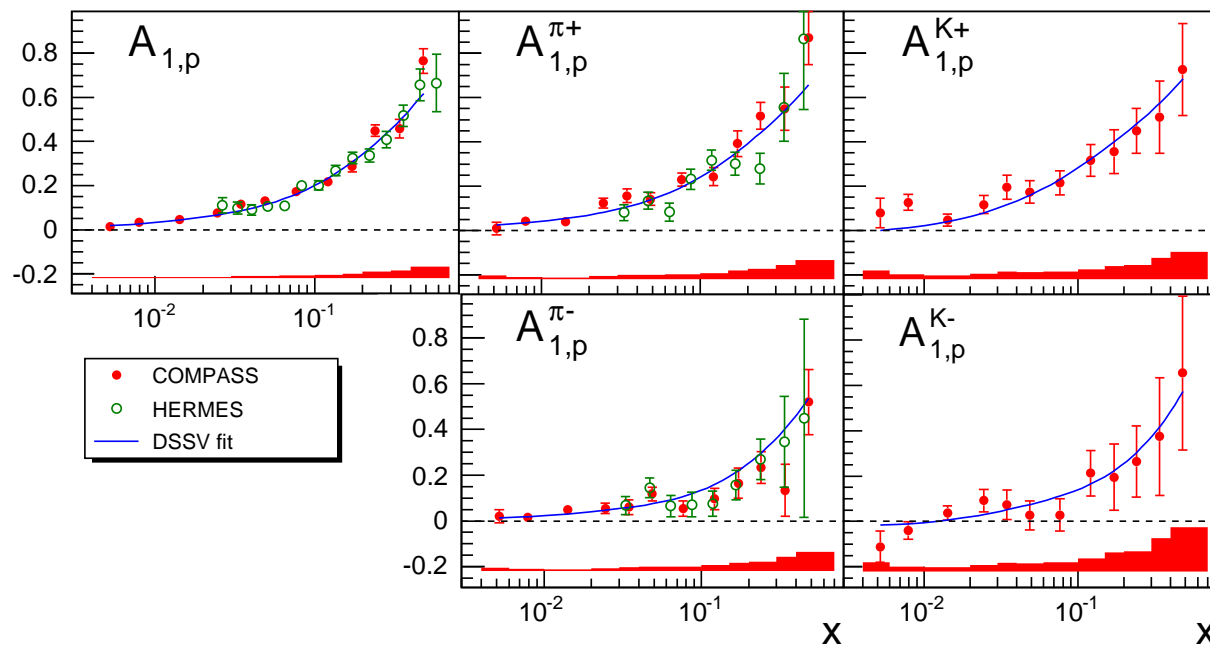
Purity of hadron samples

	${}^6\text{LiD}$ target	NH_3 target
π^+	≥ 0.98	≥ 0.98
π^-	≥ 0.98	≥ 0.98
K^+	$0.80 \Rightarrow 0.93$	$0.73 \Rightarrow 0.93$
K^-	$0.80 \Rightarrow 0.91$	$0.73 \Rightarrow 0.91$

COMPASS asymmetries on deuteron (2009)
Curves = DSSV fit



COMPASS asymmetries on proton Comparison with HERMES and DSSV fit



- **Correlated statistical errors** in a given x interval:

$$\Rightarrow \rho(A_{1,p}^{\pi^+}, A_{1,p}) \approx (0.30 - 0.45).$$

- **Unfolding** of A^K, A^π
 $\Rightarrow \rho < 0$ if same sign
 (≈ -0.16 at small x).

Systematic errors on COMPASS asymmetries

	${}^6\text{LiD}$ target	NH_3 target
P_B	5%	5%
P_T	5%	2%
f	2%	1%
$R = \sigma_L/\sigma_T$	2 – 3%	$\leq 3\%$
”False asym.”	$\leq 0.4 \sigma_{\text{stat.}}$	$\leq 0.56 \sigma_{\text{stat.}}$

Corrections to asymmetries

- **QED** radiative corrections applied to all asymmetries (≤ 0.019).
- **Proton** asymmetries corrected for ${}^{14}\text{N}$ polarisation (≤ 0.015).
- **Deuteron** asymmetries corrected for ${}^7\text{Li}$ and ${}^1\text{H}$ admixture in target material (≤ 0.020). **NOT applied in the 2008 analysis.**

LO extraction of polarised PDFs

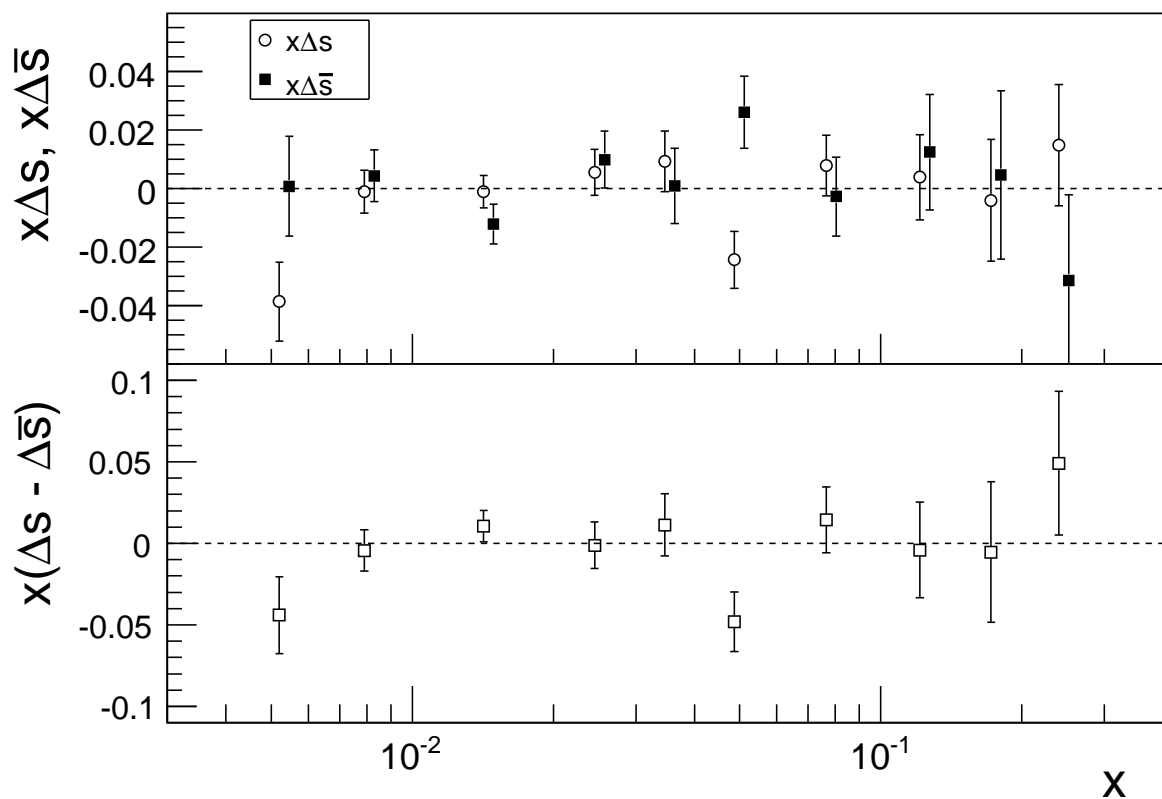
$$A^h(x, z) = \frac{\sum_q e_q^2 \left[\Delta q(x) D_q^h(z) + \Delta \bar{q}(x) D_{\bar{q}}^h(z) \right]}{\sum_q e_q^2 \left[q(x) D_q^h(z) + \bar{q}(x) D_{\bar{q}}^h(z) \right]}$$

- **Inputs:** 10 asymmetries for each interval of x

$$\begin{array}{ccccc} A_{1,p} & A_{1,p}^{\pi+} & A_{1,p}^{\pi-} & A_{1,p}^{K+} & A_{1,p}^{K-} \\ A_{1,d} & A_{1,d}^{\pi+} & A_{1,d}^{\pi-} & A_{1,d}^{K+} & A_{1,d}^{K-} \end{array}$$

- **Unknowns:** 6 polarised PDFs $\Delta u, \Delta d, \Delta \bar{u}, \Delta \bar{d}, \Delta s, \Delta \bar{s}$
 \implies (reduced to 5 if $\Delta s = \Delta \bar{s}$ is assumed)
- **Q^2 dependence** of asymmetries neglected $\implies Q^2 = 3 \text{ (GeV/c)}^2$
- $q(x), \bar{q}(x)$ from MRST2004LO, corrected by $(1 + R(x, Q^2))$
- $D_q^h, D_{\bar{q}}^h$ fragmentation functions (FF) from DSS fit at LO

Δ_s and $\Delta_{\bar{s}}$ from COMPASS asymmetries and the Difference $\Delta_s - \Delta_{\bar{s}}$

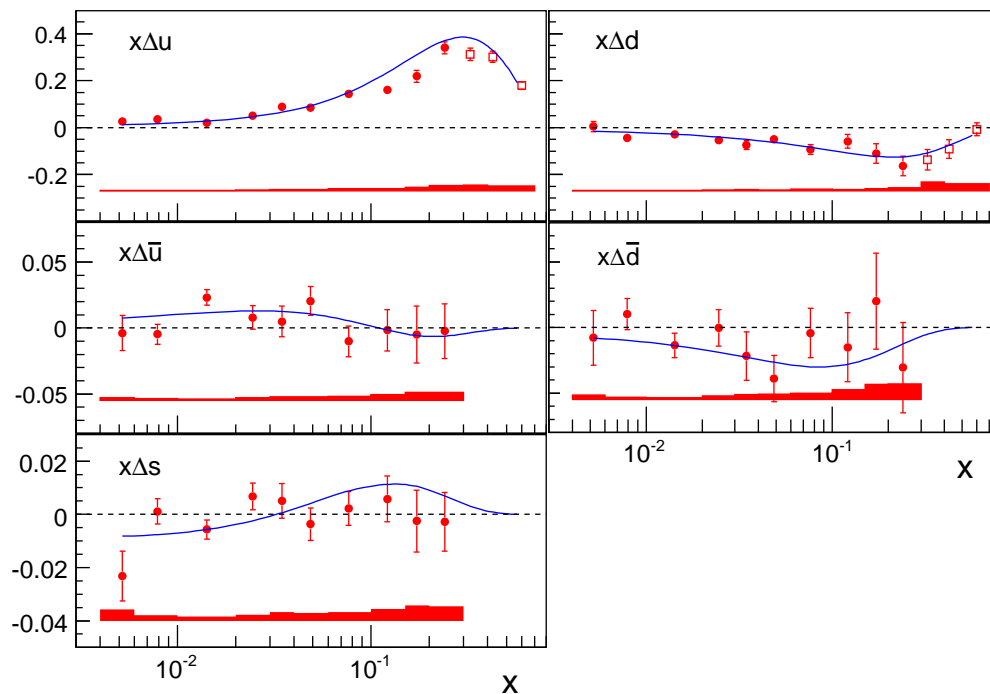


- Fixed $Q^2 = 3 \text{ (GeV}/c)^2$
- FF from DSS
- No significant difference: one point at 2.7σ
- Stable for changes in $s(x)$, $\bar{s}(x)$ or FFs
- $\Delta_s = \Delta_{\bar{s}}$ assumed for subsequent analysis

Extraction of PDFs
assuming $\Delta s = \Delta \bar{s}$

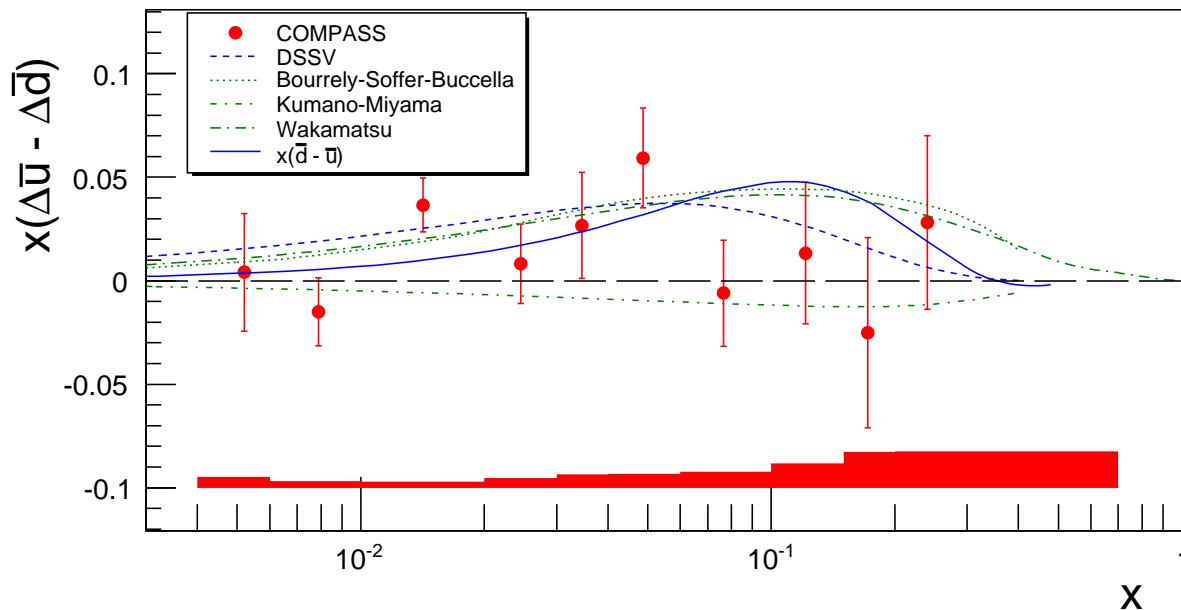
- Least square fit in each interval of x ($0.004 < x < 0.3$):
10 asymmetries, 5 unknowns
- Data compatible with LO formula:
 $1.8/5 < (\chi^2/ND) < 8.5/5$
- Errors reduced at least by factor 1.5

LO PDFs at $Q^2 = 3 \text{ (GeV}/c)^2$ from COMPASS asymmetries
Curves = DSSV fit (NLO)



- **Valence quarks**
 - $\Delta u > 0, \Delta d < 0 \Rightarrow$ dominant
 - 3 points at $x > 0.3$ derived assuming $\Delta \bar{q} = 0$
 - shapes \approx DSSV curves
 - Syst.error mainly from P_μ (5%)
- **Sea quarks**
 - All compatible with zero
 - Slight indication for $\Delta \bar{d} < 0$
 - No indication for $\Delta s < 0$ or changing sign
 - Syst.error mainly from "false asymmetries"

The flavour asymmetry of the sea $\Delta\bar{u} - \Delta\bar{d}$



- $\Delta\bar{u} - \Delta\bar{d} \geq 0$ and $\Delta\bar{u} - \Delta\bar{d} \leq \bar{d} - \bar{u}$
- **First moment:**
 $\Gamma_{0.004}^{0.7} = 0.06 \pm 0.04 \pm 0.02$
- Consistent with *statistical model (BSB)* and *CQSM (Wakamatsu)* (≥ 0)
- Within errors also consistent with *meson cloud model (KM)* (< 0)
- **Need reduction of error by factor ≥ 2 to discriminate between models**

**First moments of polarised PDFs
at $Q^2 = 3 \text{ (GeV}/c)^2$**

- $0.004 < x < 0.3$ COMPASS, LO fit of asymmetries
- $0.3 < x < 0.7$ COMPASS, $g_1^d(x)$, $g_1^p(x)$, $\Delta\bar{q} = 0$ assumed
- $0.7 < x < 1$ Data extrapolation (negligible)
- $0 < x < 0.004$ 2 options:
 - Linear extrapolation $\Delta\bar{q} \approx 0$
 - DSSV fit $\Delta\bar{d} < 0$, $\Delta\bar{s} < 0$

First moments (continued)

$$Q^2 = 3 \text{ (GeV}/c)^2$$

	$0.004 < x < 0.7$	$0 < x < 1$ (Extrap.)	$0 < x < 1$ (DSSV)
Δu	$0.69 \pm 0.02 \pm 0.03$	$0.71 \pm 0.02 \pm 0.03$	$0.71 \pm 0.02 \pm 0.03$
Δd	$-0.33 \pm 0.04 \pm 0.03$	$-0.34 \pm 0.04 \pm 0.03$	$-0.35 \pm 0.04 \pm 0.03$
$\Delta \bar{u}$	$0.02 \pm 0.02 \pm 0.01$	$0.02 \pm 0.02 \pm 0.01$	$0.03 \pm 0.02 \pm 0.01$
$\Delta \bar{d}$	$-0.05 \pm 0.03 \pm 0.02$	$-0.05 \pm 0.03 \pm 0.02$	$-0.07 \pm 0.03 \pm 0.02$
$\Delta s(\Delta \bar{s})$	$-0.01 \pm 0.01 \pm 0.01$	$-0.01 \pm 0.01 \pm 0.01$	$-0.05 \pm 0.01 \pm 0.01$
Δu_v	$0.67 \pm 0.03 \pm 0.03$	$0.68 \pm 0.03 \pm 0.03$	$0.68 \pm 0.03 \pm 0.03$
Δd_v	$-0.28 \pm 0.06 \pm 0.03$	$-0.29 \pm 0.06 \pm 0.03$	$-0.28 \pm 0.06 \pm 0.03$
$\Delta \Sigma$	$0.31 \pm 0.03 \pm 0.03$	$0.32 \pm 0.03 \pm 0.03$	$0.22 \pm 0.03 \pm 0.03$

First Moments (continued)

$$Q^2 = 3 \text{ (GeV}/c)^2$$

Consistency with previous COMPASS results

- $\Delta\Sigma = 0.32 \pm 0.03 \pm 0.03$

$$a_0 = 0.33 \pm 0.03 \pm 0.05 \text{ (NLO)}$$

from $\int g_1^d(x)dx$, with a_8 from hyperon decays ($= 0.585 \pm 0.025$)

COMPASS, Phys. Lett.B647 (2007) 8

- $\Delta u_v + \Delta d_v = 0.39 \pm 0.03 \pm 0.04$

$$\Delta u_v + \Delta d_v = 0.41 \pm 0.07 \pm 0.06$$

from $A^{h^+ - h^-}$ (at $Q^2 = 10 \text{ (GeV}/c)^2$)

COMPASS, Phys. Lett.B660 (2008) 458

Dependence of moments of PDFs on fragmentation functions

- $D_{q,\bar{q}}^\pi$ better constrained by data than $D_{q,\bar{q}}^K$
- Relation **asymmetries** \Leftrightarrow **PDFs** depends on two ratios of FFs into kaons:
"unfavoured to favoured" R_{UF} and *"strange to favoured"* R_{SF}

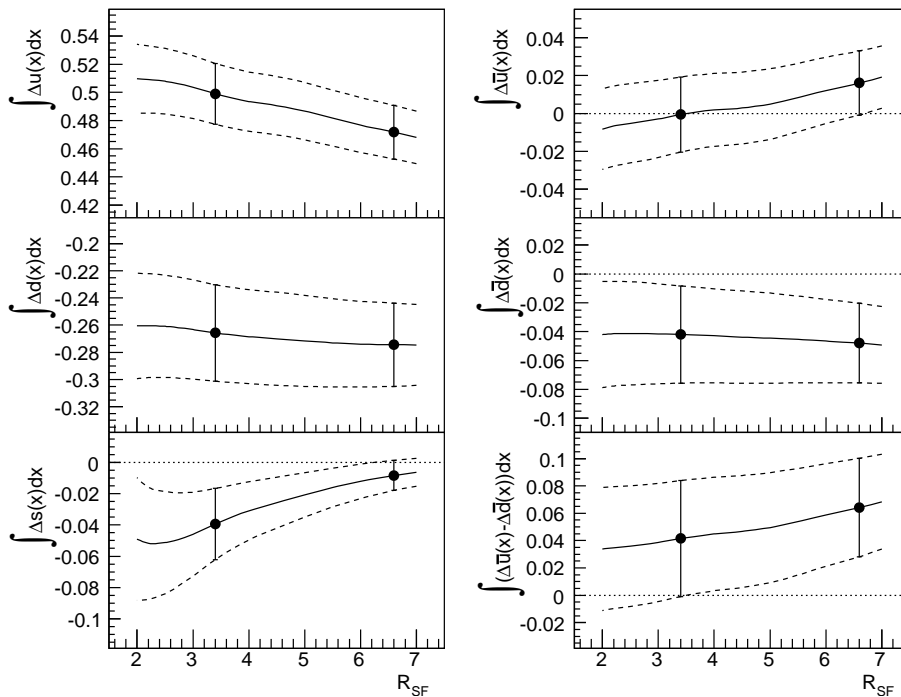
$$R_{UF} = \frac{\int D_d^{K^+}(z) dz}{\int D_u^{K^+}(z) dz} \quad \Leftrightarrow \quad R_{SF} = \frac{\int D_s^{K^+}(z) dz}{\int D_u^{K^+}(z) dz}$$

- At $Q^2 = 3 \text{ (GeV/c)}^2$:

	DSS	EMC
R_{UF}	0.14	0.35
R_{SF}	6.6	3.4

- Move simultaneously R_{SF} and R_{UF} from DSS to EMC values and check variation of moments $\Delta q, \Delta \bar{q}$

Moments of PDFs vs. fragmentation functions (decrease of R_{SF} and increase of R_{UF} from DSS to EMC values)



- Increase of Δu by $\approx 1.0 \sigma_{\text{stat}}$.
- Decrease of $\Delta \bar{u}$ by $\approx 1.0 \sigma_{\text{stat}}$.
- Negligible effect on Δd and $\Delta \bar{d}$
- Decrease of $\Delta \bar{u} - \Delta \bar{d}$ by $0.5 \sigma_{\text{stat}}$.
- Decrease of Δs to -0.04 with two times larger statistical error
- *Limited effect on K^+ and K^- rates*

The Δs puzzle (DIS vs. SIDIS)

- Δs from DIS: $\Gamma_1^N = \frac{1}{2} \int (g_1^p(x) + g_1^n(x)) dx$

- LO relations

$$\Gamma_1^N = \frac{1}{9}(a_0 + \frac{1}{4}a_8)$$

$$\Delta s + \Delta \bar{s} = \frac{1}{3}(a_0 - a_8)$$

$$\Delta s + \Delta \bar{s} = 3\Gamma_1^N - \frac{5}{12}a_8$$

- $\Gamma_1^N \approx 0.05$ (COMPASS, $Q^2 = 3$ (GeV/c)²)

- $a_8 = 0.585 \pm 0.025$ (Hyperon decays, assuming SU(3)_f symmetry)

- Hence $\Delta s + \Delta \bar{s} < 0$ (≈ -0.09)

- Δs from SIDIS: $\Delta s(x)$ measured in limited range of x

- HERMES ($x > 0.02$): No indication for $\Delta s(x) < 0$

- COMPASS ($x > 0.004$): No indication for $\Delta s(x) < 0$

- νp elastic data and PV $\vec{e}p$ asymmetries $\Rightarrow \Delta s < 0$ (*S. Pate, this conference*)

The Δs puzzle (DIS vs. SIDIS)

Possible ways out

- (1) **Uncertainty on FFs \Rightarrow SIDIS results questionable (?)**
Would need strong reduction of R_{SF} (to ≈ 3 vs. 6.6 in DSS fit)
- (2) **SIDIS data cover a limited range in x**
Large negative contribution to Δs in unmeasured region at low $x \Rightarrow$
$$\int_{\text{SIDIS}} \Delta s(x) dx = \int_{\text{DIS}} \Delta s(x) dx$$
 - DSSV fit (2008)
 - LSS10 fit, including COMPASS data (*cf. A. Sidorov, this conference*)
- (3) **Assume $a_8 < 0.585$ due to $SU(3)_f$ violation**
 $a_8 \rightarrow (a_8 - \epsilon)$ implies $a_0 \rightarrow (a_0 + \epsilon/4)$ to keep Γ_1^N constant and
 $\Delta s + \Delta \bar{s} \rightarrow \Delta s + \Delta \bar{s} + (5/12)\epsilon$
Cloudy bag model calculations $\Rightarrow a_8 \approx 0.42$ and $\Delta s + \Delta \bar{s} \approx -0.02$
cf. S.D.Bass and A.W.Thomas, Phys.Lett. B684(2010)216

Present fixed target data may improve on (1) but cannot discriminate (2) vs.(3).

Conclusions and prospects

- **New evaluation of polarised PDFs at LO**
 - Δq , $\Delta\bar{q}$ from COMPASS DIS and SIDIS $K^{+,-}$ and $\pi^{+,-}$ asymmetries on ${}^6\text{LiD}$ and NH_3 targets
 - $\Delta\bar{q}$ distributions are small over measured range of x ($0.004 < x < 0.3$)
 - No significant difference between $\Delta s(x)$ and $\Delta\bar{s}(x)$
 - $(\Delta\bar{u} - \Delta\bar{d}) > 0$ (at $1.5 \sigma_{\text{stat}}$ but not larger than $\bar{d} - \bar{u}$)
 - Moments of Δu , $\Delta\bar{u}$ and Δs found to vary with choice of kaon FFs.
Variation is critical for Δs (becomes negative with large error for $R_{SF} \leq 4$)
- **Future**
 - 2011 COMPASS data on NH_3 target will improve precision on $(\Delta\bar{u} - \Delta\bar{d})$ and help discriminate between models
 - Ongoing investigations on FFs from COMPASS K^+ and K^- rates will at least clarify (if not solve) the Δs puzzle