

Review on exclusive meson production

recent experimental results

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● Introduction

● Exclusive and proton-dissociative production of VM at small $|t|$

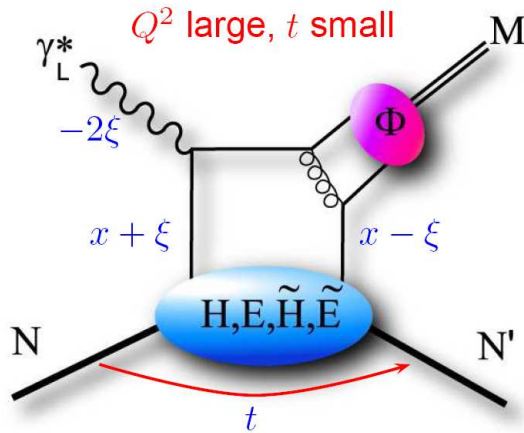
● Helicity amplitudes for VM production on unpolarised nucleons

● Production of pseudoscalar mesons

● Meson production on transversely polarised nucleons

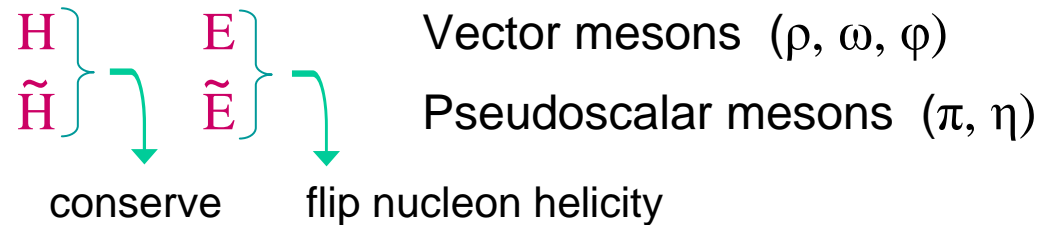
● Conclusions

GPDs and Hard Exclusive Meson Production



- 4 Generalised Parton Distributions (GPDs) for each quark flavour and for gluons
- factorisation proven only for σ_L
 σ_T suppressed by $1/Q^2$
- applicable at DIS region, $|t| \ll Q^2$ and **any** x_B

- allows separation $(H,E) \leftrightarrow (\tilde{H},\tilde{E})$ and wrt quark flavours



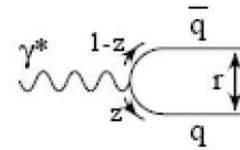
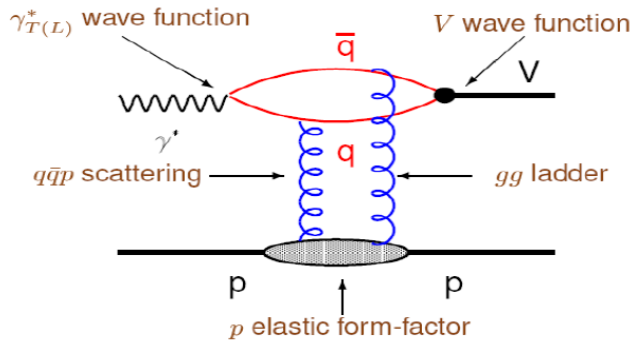
Flavour sensitivity of HEMP on the proton

π^0	$2\Delta u + \Delta d$
η	$2\Delta u - \Delta d$
ρ^0	$2u + d, 9g/4$
ω	$2u - d, 3g/4$
ϕ	s, g
ρ^+	$u - d$
J/ψ	g

- quarks and gluons enter at the same order of α_s
- at $Q^2 \approx \text{few GeV}^2$ **power corrections/higher order pQCD terms** are essential
- wave function of meson (DA Φ)
additional nonperturbative component

Colour dipole models

an alternative description of VM production at small x
 applicable at **small x** both for **photoproduction and DIS** region



$$\langle r \rangle \approx k / \sqrt{\mu^2}$$

$$\mu^2 \approx z(1-z)(Q^2 + M_V^2)$$

for heavy mesons or γ_L^* $z \approx 1/2$
 and $\mu^2 = (Q^2 + M_V^2) / 4$

$$\Psi^\gamma(z, \vec{r}) \otimes \sigma^{q\bar{q}-p}(x_B, \vec{r}; t) \otimes \Psi^V(z, \vec{r})$$

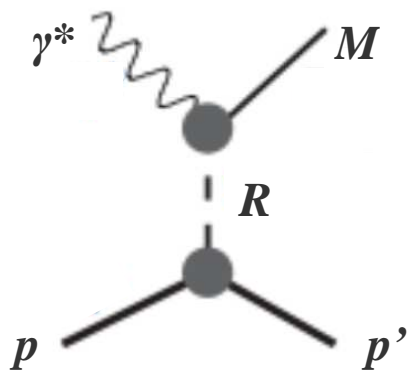
- at small x sensitivity mostly to gluons → universal dipole-nucleon cross section
 dipole-nucleon cross section related to inclusive photo- and DIS production
 the link exploited in certain colour dipole models
- cross section for VM production $\sim |g(x_B)|^2$ (at LO)
 hardening of the gluon distribution $g(x_B) \sim x_B^{-\lambda}$ at large Q^2 → strong W -dep.

dipole transv. size	W-dep.	t-dep.
large	weak	steep
small	strong	shallow

Regge models

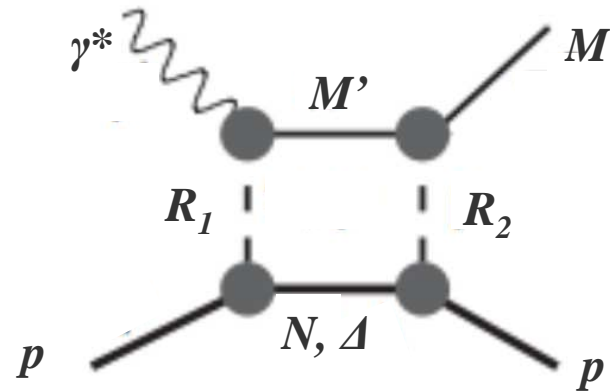
another alternative description of meson photo- and electroproduction based on general properties of amplitudes analyticity at $|t| \ll s$ (W) applicable from photoproduction to moderate Q^2

t-channel exchange of Reggeon(s) R (R_1, R_2): $\mathcal{P}, \rho, \omega, \sigma, f_2, \pi, b_1 \dots$



Regge poles

+



Regge cuts

M	R
ρ^0	\mathcal{P}, σ, f_2
ω	\mathcal{P}, π^0
ϕ	\mathcal{P}
ρ^+	π^+, ρ^+
π^0	ω, ρ^0, b_1

factorisation of vertices for a Regge pole exchange;
 $g_{RNN}(t)$ at nucleon vtx. and meson form factor

energy dependence determined by the Reggeon trajectory:

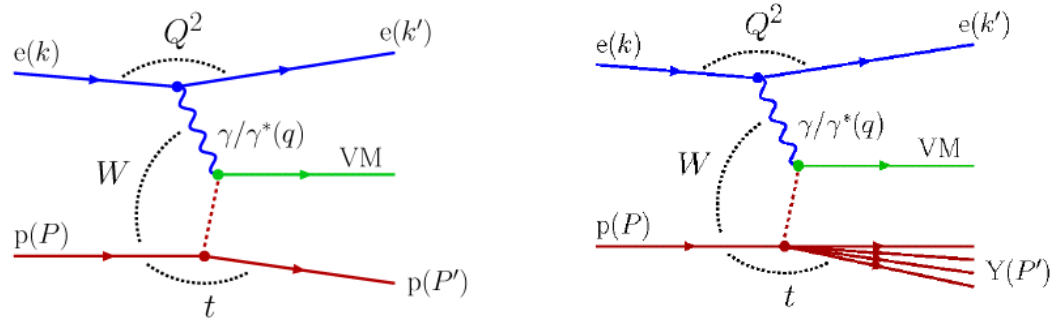
$$\frac{d\sigma}{dt}(W; R) = F(t)(W / W_0)^{2[\alpha_R(t)-2]}$$

$$\alpha_R(t) \approx \alpha_R(0) + \alpha'_R t$$

except \mathcal{P} , contributions of other Reggeons decrease with W

Elastic and proton-dissociative small $|t|$ VM production at HERA

VM: $\rho^0, \omega, \phi, J/\psi, \psi(2s), \Upsilon$



VM measured in central detectors

no other activity, apart from forward detectors

$$10^{-4} \leq x_B \leq 10^{-2}$$

$$0 \leq Q^2 < 160 \text{ GeV}^2$$

$$30 < W < 180 \text{ GeV}$$

$$|t| < 3 \text{ GeV}^2$$

elastic sample - scattered proton inside the beam pipe;
'no-tag events'

proton-dissociative sample - remnants of the proton hit
forward detectors; 'tag events'

Main sources of background:

cross-contaminations between tag and no-tag samples $\approx 10\%$

diffractive ρ' production with not all decay particles being measured - several %

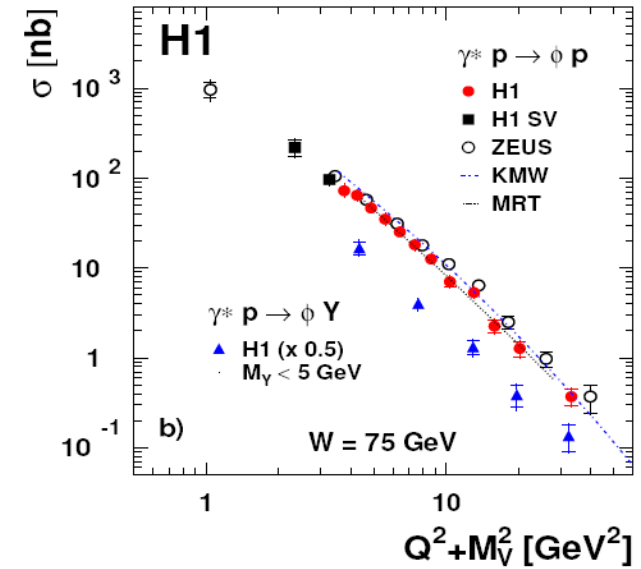
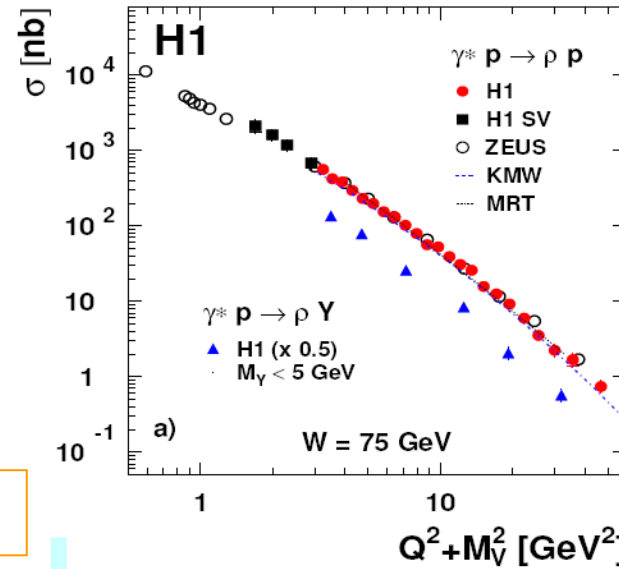
$\pi^+\pi^-$ background in ϕ samples $\approx 5\%$

semi-inclusive events suppressed by large rapidity gap between VM and forward detectors

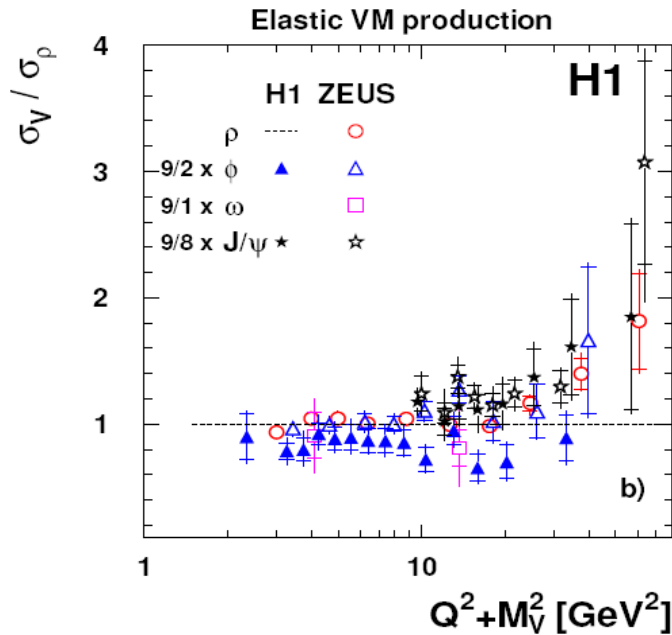
➤ Q^2 dependence

KMW (Kowalski, Motyka, Watt)
dipole approach

MRT (Martin, Ryskin, Teubner)
parton-hadron duality



➤ SU(4) universality (?)



for the ratios σ_V rescaled according
to quark charge content

- shape similar for ρ & ϕ and for elastic & dissociation
power law fits $1/(Q^2+M_V^2)^n$ with $n \approx 2.4$
- shape reasonably well described by models
- normalization; some (< 20%) differences between experiments
similar level of agreement with models
- universality qualitative (within 20%)
scaling factors from VM electronic decay widths
expected to encompass wave function and soft effects

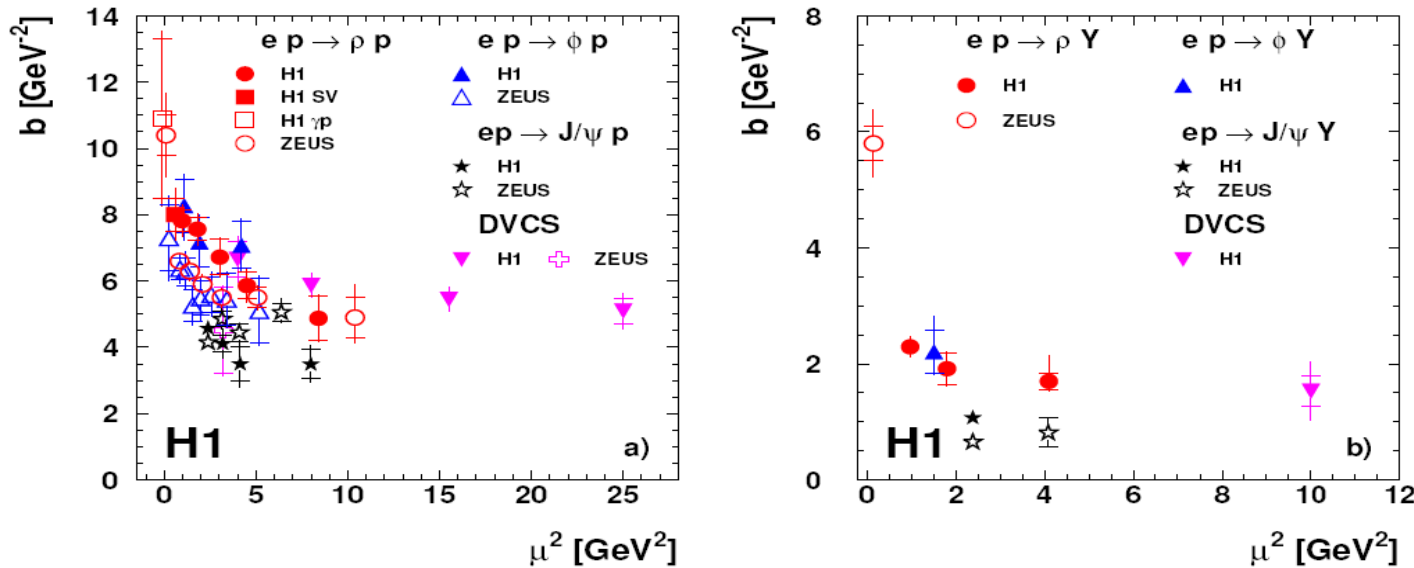
➤ t dependence

$$\frac{d\sigma}{dt} \propto e^{-b|t|} \quad \text{for elastic } (|t| < 0.5(1.0) \text{ GeV}^2) \text{ and dissoc. } (|t| < 3 \text{ GeV}^2)$$

$$b = b_Y + b_{qq} + b_P (+ b_V ?)$$

related to 'transverse imaging' of the proton

b_P expected small and Q^2 independent



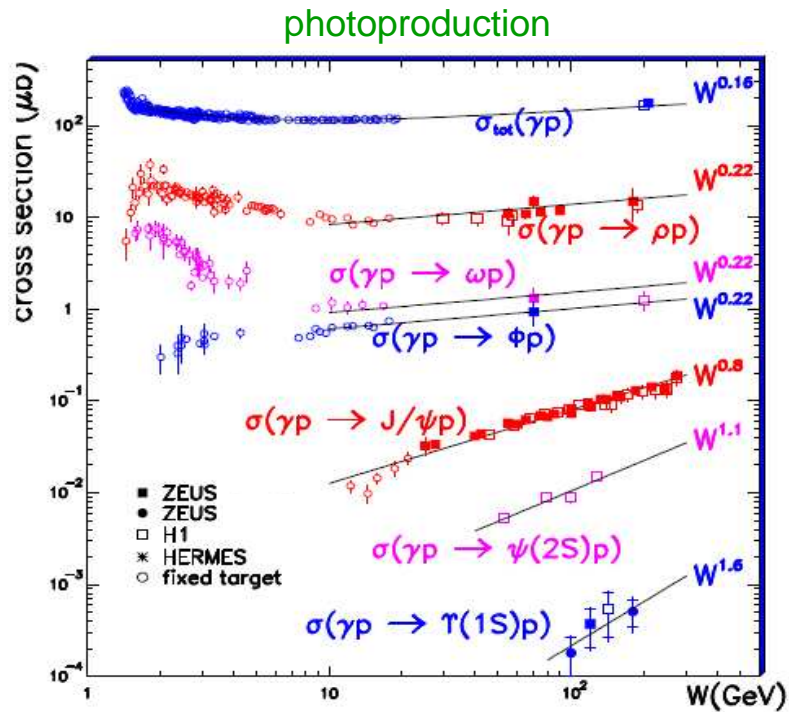
$$\mu^2 = (Q^2 + M_V^2)/4$$

(= Q^2 for DVCS)

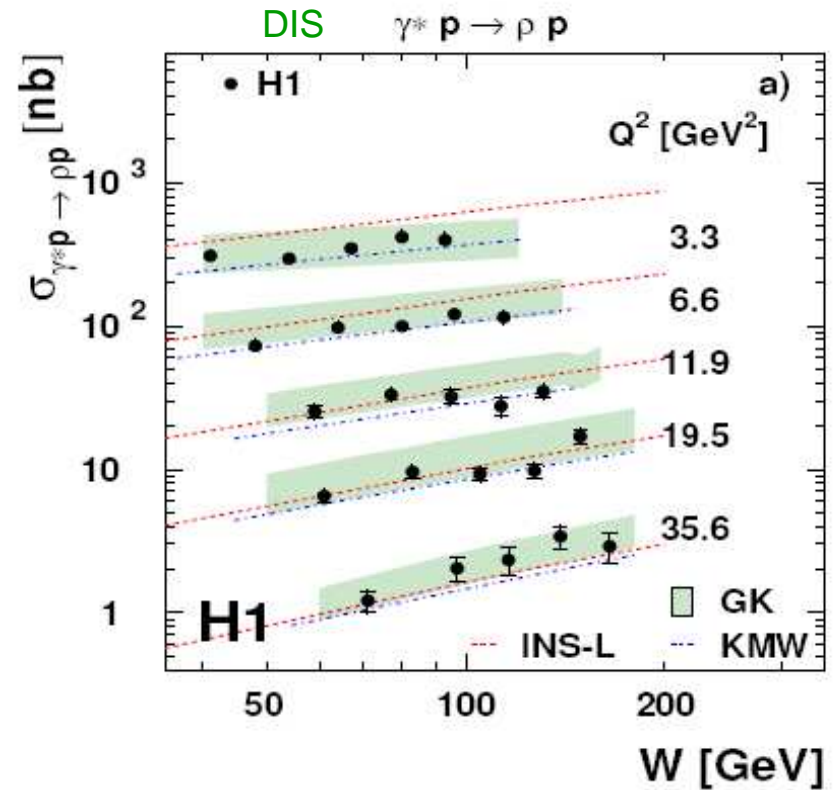
- some discrepancy between experiments, due to subtraction of dissoc. background
- significant decrease from photoproduction already at $\mu^2 \approx 0.5 \text{ GeV}^2$ and levelling at $\mu^2 \approx 5 \text{ GeV}^2$
decrease of dipole transverse size with increasing scale
- light mesons slightly above J/ψ (effect of VM form factors ?)
- slopes in diffractive dissociation significantly smaller

➤ W dependence

$$\sigma \propto W^\delta$$



GK - (Goloskokov, Kroll) GPD model
 KMW
 INS-L - (Ivanov, Nikolaev, Savin) dipole model with large meson wave function



- faster growth at large mass or large Q^2

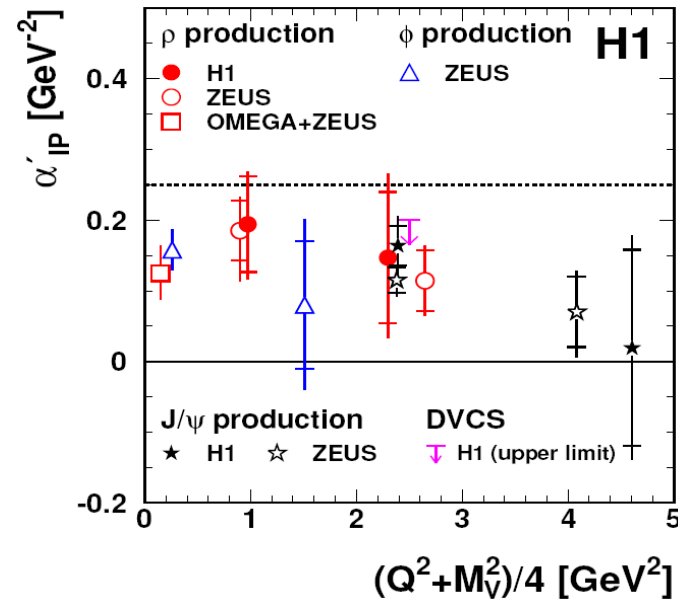
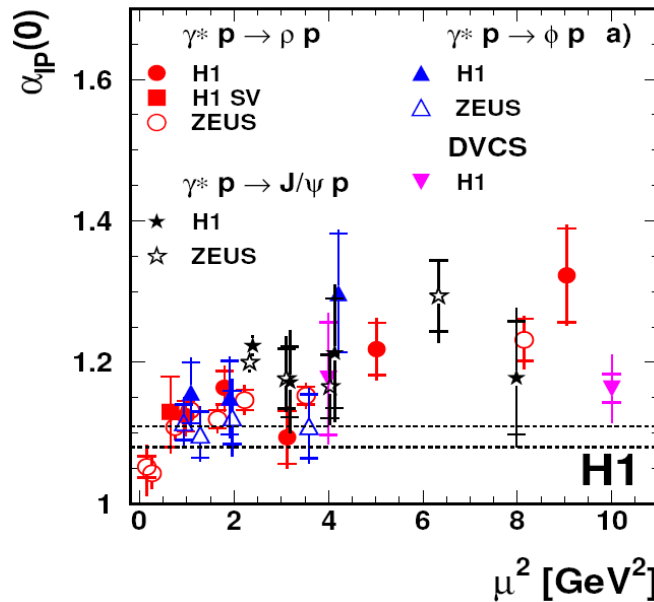
hardening of the gluon distribution $g(x_B) \sim x_B^{-\lambda}$

- pQCD models reproduce W dependence well, sensitivity to assumed gluon PDFs

➤ Interplay between W and t dependences

$$\frac{d\sigma}{dt}(W) = \frac{d\sigma}{dt}(W_0) (W/W_0)^{\delta(t)} \propto e^{b_0 t} (W/W_0)^{4(\alpha_P(0) + \alpha'_P t - 1)} \quad \longrightarrow \quad b = b_0 + 4\alpha'_P \ln \frac{W}{W_0}$$

effective Pomeron trajectory determined either by measuring W evolution of t -slope b or t evolution of W^δ (more accurate)



- increase of $\alpha_P(0)$ with the scale due to hardening of gluon distribution
- at large μ^2 scales W dependence ($\alpha_P(0)$) significantly stronger than in soft hadronic diffraction
- α'_P smaller than for 'soft Pomeron', even at $Q^2 \approx 0$
- a hint that α'_P may vanish at very large Q^2 , as expected for BFKL dynamics

Exclusive VM production at CLAS

VM: $\rho^0, \omega, \phi, \rho^+$

preliminary, first results ever

- S. Morrow et al. EPJ A39, 5 (2009)
- L. Morand et al. EPJ A24, 445 (2005)
- J.P. Santoro et al. PR C78, 025210 (2008)

ρ^0 : $e p \rightarrow e p \pi^+ \pi^-$

ω : $e p \rightarrow e p \pi^+ \pi^- \pi^0$ or $e p \rightarrow e p \pi^+ \pi^- \pi^0$

ϕ : $e p \rightarrow e p K^+ K^-$

ρ^+ : $e p \rightarrow e n \pi^+ \pi^0$

'Typical' kinematic domain

$$0.16 \leq x_B \leq 0.7$$

$$1.6 \leq Q^2 < 5.6 \text{ GeV}^2$$

$$1.8 < W < 2.8 \text{ GeV}$$

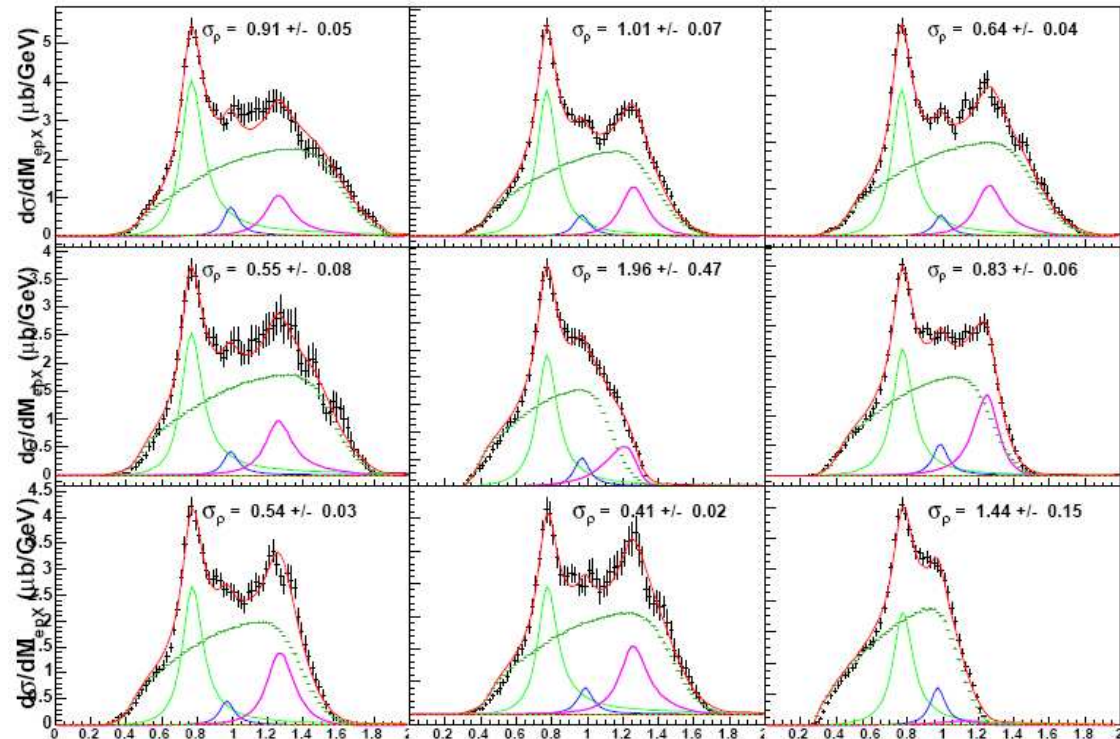
$$0.1 < |t| < 4.3 \text{ GeV}^2$$

missing mass used to ensure exclusivity

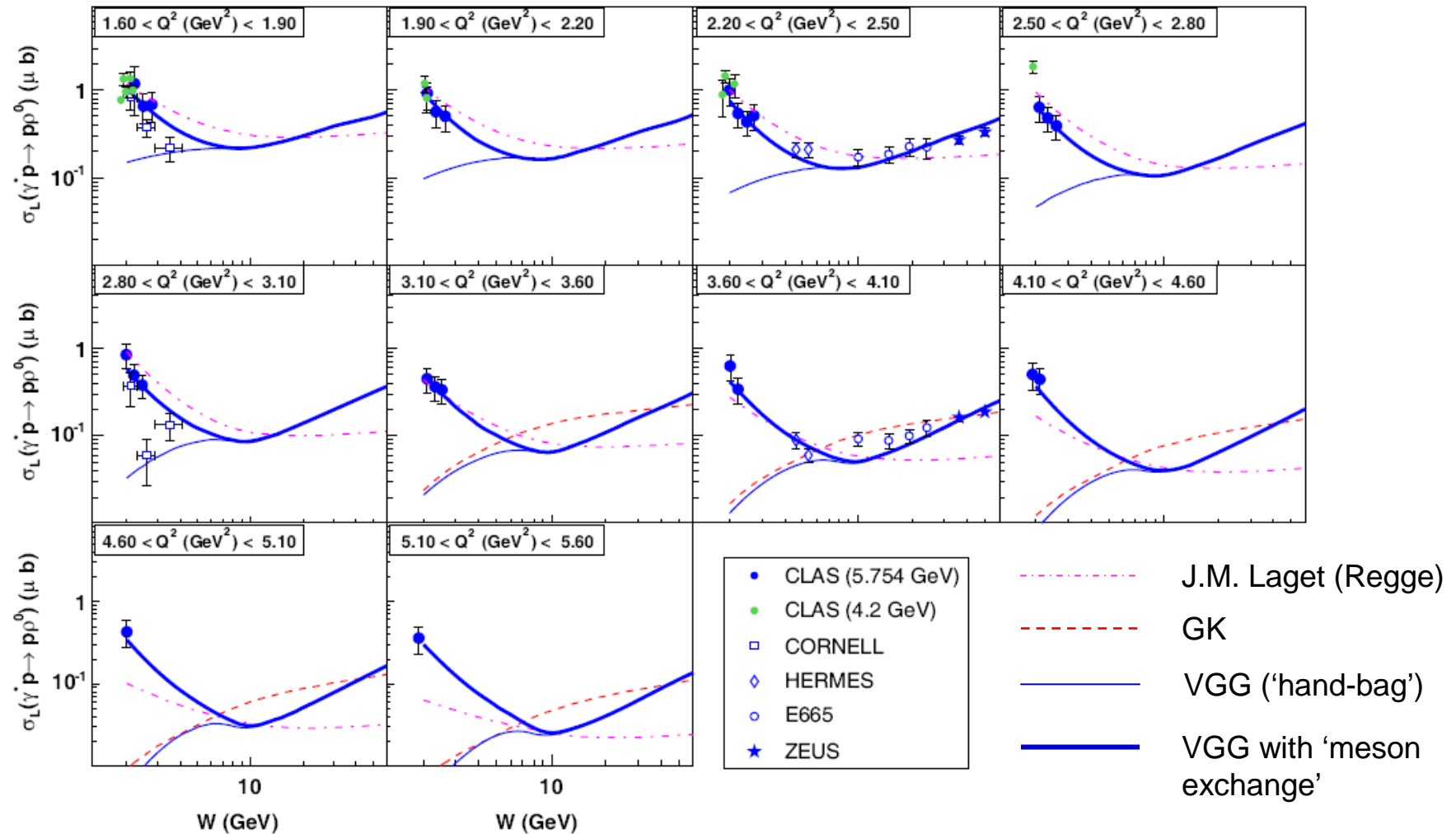
ρ^0

missing mass $M_X[epX]$
for selected (Q^2, x_B) bins

fitted sum of ρ^0, f_0, f_2
and nonresonant $\pi^+ \pi^-$



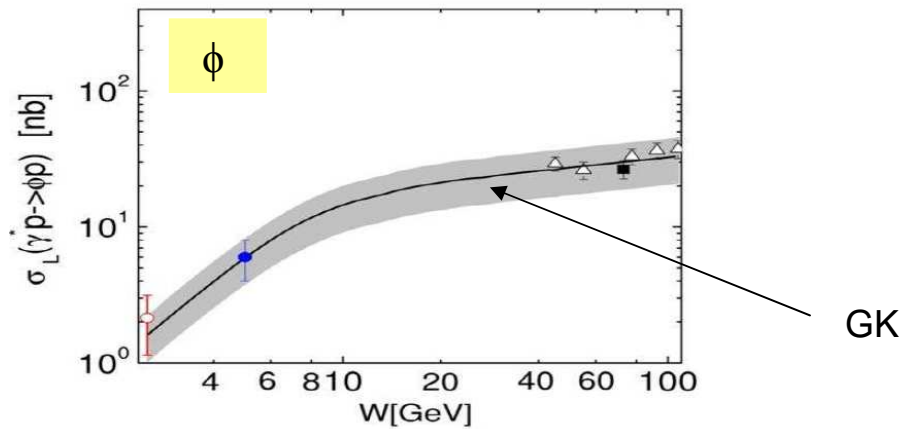
➤ W dependence of $\sigma(\gamma^* p \rightarrow \rho^0 p_L)$



- Laget (Regge) able to describe data up to $Q^2 \approx 4 \text{ GeV}^2$
- GPD models using 'hand-bag' mechanism + power corrections OK at $W \geq 5 \text{ GeV}$
fail by an order of magnitude at the lowest W
- at small W (large x_B) in the framework of GPDs important contrib. of $q\bar{q}$ exchange

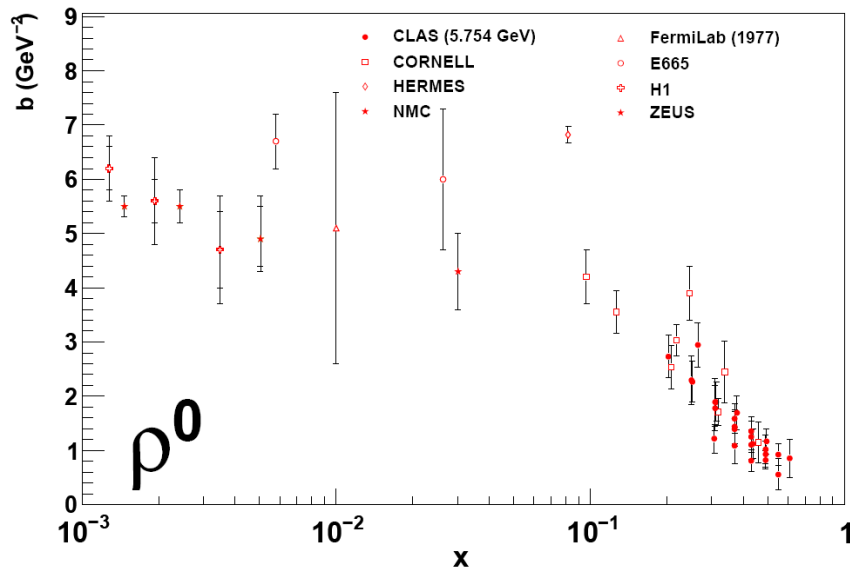
➤ W dependence for ρ^+_{\perp} and ϕ_{\perp}

- for ρ^+ (not shown) qualitatively similar trends as for ρ^0



- for ϕ GPD model describes data well in all W range
 ϕ production through gluon and sea quark exchanges (Pomeron in Regge formalism)
 in contrast, for other mesons at small W also valence quark exchanges important
 (subleading Reggeons)

➤ b slope



← courtesy of M. Guidal

- probing more compact object at large x_B

Spin Density Matrix Elements for VM production on unpolarised nucleons

VM angular distributions $W(\cos\theta, \varphi, \Phi)$ depend on the **spin density matrix elements** (SDME)

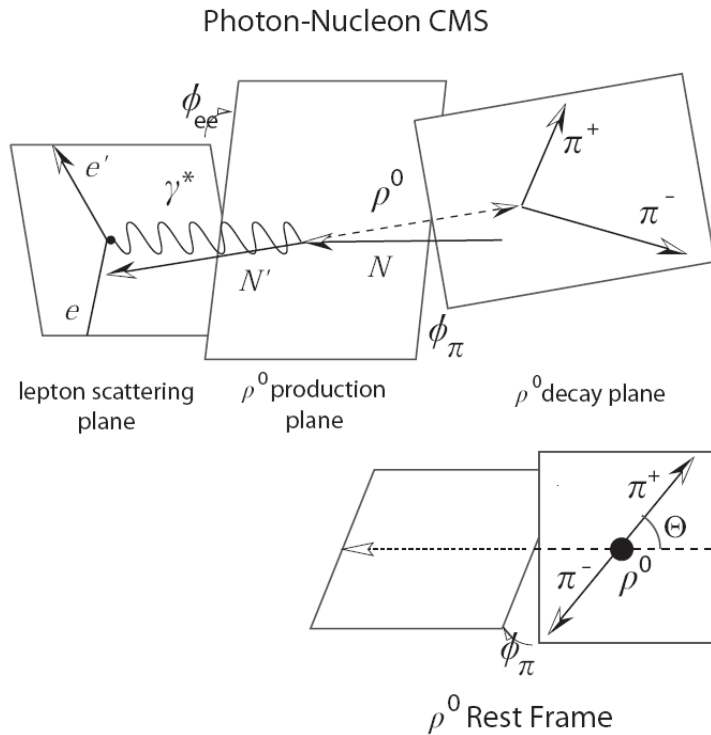
⇒ 23 (15) observables with polarized (unpolarized) beam

SDMEs are bilinear combinations of the helicity amplitudes

$$F_{\lambda m \lambda N'; \lambda \gamma \lambda N}(\gamma^* N \rightarrow m N')$$

$$F = T + U \quad (\text{natural} + \text{unnatural PE})$$

convention $T_{\lambda m \lambda \gamma}, U_{\lambda m \lambda \gamma}$ implies $\lambda_{N'} = \lambda_N = +1/2$



❖ determine hierarchy of $T_{\lambda m \lambda \gamma}, U_{\lambda m \lambda \gamma}$ amplitudes

❖ check s-channel helicity conservation

for SCHS the only non-vanishing are T_{00}, T_{11}, U_{11}

❖ describe parity of t-channel exchange

NPE vs. UPE

❖ impact on GPD studies – determination of σ_L

$$\text{SDMEs} \longrightarrow R = \frac{\sigma_L}{\sigma_T}$$

• in Regge formalism - NPE: $\mathbb{P}, \rho, \omega, f_2, a_2$; UPE: π, a_1, b_1 exchanges

• in GPD formalism - NPE: H, E ; UPE: \tilde{H}, \tilde{E} GPDs

at leading order only SCHC & NPE

➤ SDMEs from HERMES for ρ^0 production on protons and deuterons

comprehensive measurement and analysis of 15(8) unpolarised (polarised) SDMEs !

A. Airapetian et al. EPJ C 62, 659 (2009)

similar results (not shown here) also for ϕ

$$\begin{aligned}
 &1 < Q^2 < 7 \text{ GeV}^2 \\
 &3.0 < W < 6.3 \text{ GeV} \\
 &|t'| < 0.4 \text{ GeV}^2 \text{ (**)}
 \end{aligned}$$

$$\begin{aligned}
 \Delta E &= (M_X^2 - M_p^2) / 2 < M_p \\
 t' &= t - t_0
 \end{aligned}$$

selections and background

$$0.6 < M_{\pi\pi} < 1.0 \text{ GeV} \text{ (*)}$$

$$-1.0 < \Delta E < 0.6 \text{ GeV} \text{ (**)}$$

(*) non-resonant $\pi^+\pi^-$ background 4-8% (unsubtracted)

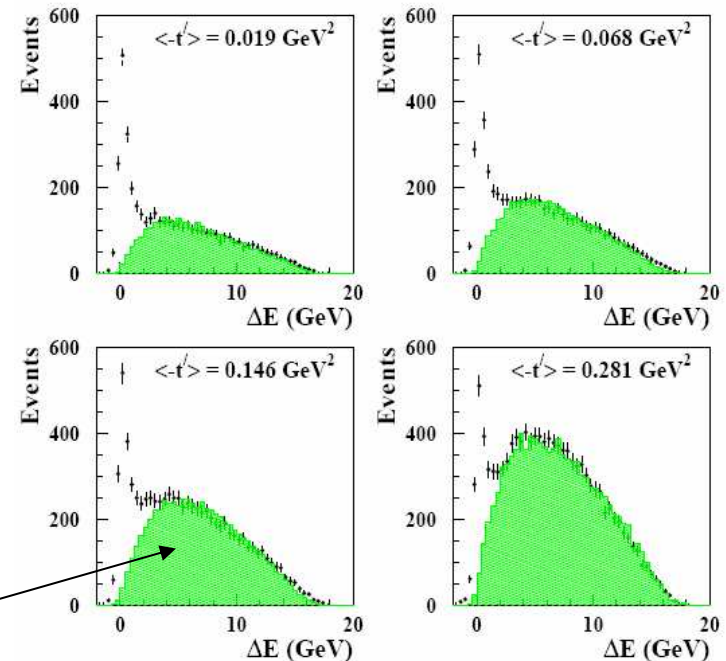
(**) { SIDIS background 3-12% (subtracted bin-by-bin)
 proton-dissociative background \approx 4% (unsubtracted)

Main sources of systematic errors:

background subtraction

uncertainties of parameters in exclusive MC

PYTHIA



➤ SDMEs

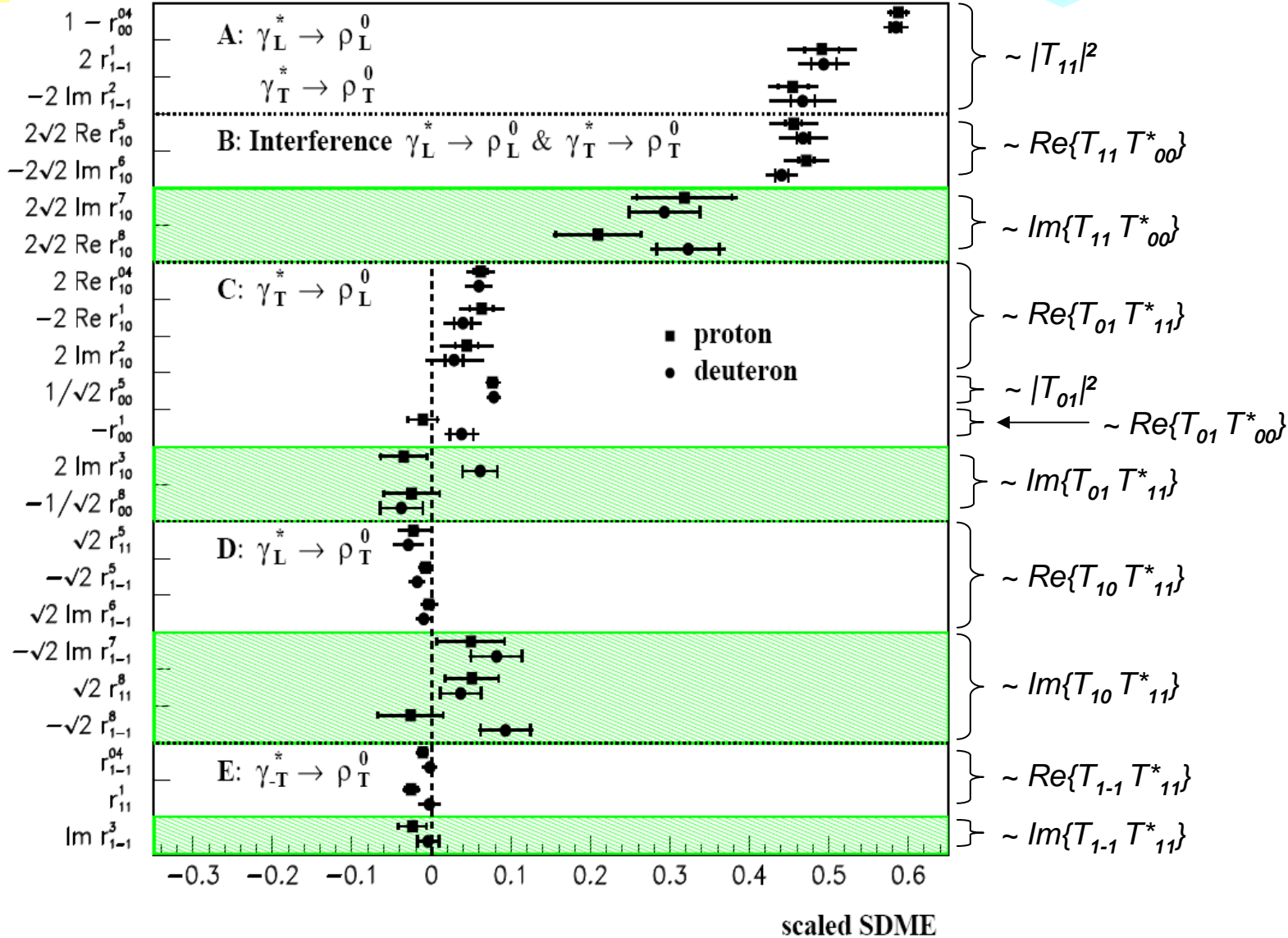
combined 1996-2005 data over whole kinematic range

EPJ C 62, 659 (2009)

ρ^0

$\langle x_B \rangle = 0.08, \langle Q^2 \rangle = 1.95 \text{ GeV}^2, \langle -t' \rangle = 0.13 \text{ GeV}^2$

leading contributions



observed hierarchy of NPE amplitudes: $|T_{00}| \sim |T_{11}| \gg |T_{01}| > |T_{10}| \approx |T_{1-1}|$

➤ selected results on helicity amplitudes from HERMES

- phase difference between T_{11} and T_{00} : $\delta = +26.4^\circ \pm 2.3 \pm 4.9$ (p); $+29.3^\circ \pm 1.6 \pm 3.6$ (d)
increases ($20^\circ \rightarrow 38^\circ$) with Q^2 ($1 \rightarrow 7 \text{ GeV}^2$)

- relative magnitude of SCHC non-conserving amplitudes $\tau_{ij} = \frac{|T_{ij}|}{\sqrt{\mathcal{N}}}$ $\mathcal{N} = \mathcal{N}_T + \epsilon \mathcal{N}_L$

HERMES	τ_{01}	τ_{10}	τ_{1-1}
proton	$0.114 \pm 0.007 \pm 0.010$	$0.075 \pm 0.030 \pm 0.003$	$0.051 \pm 0.029 \pm 0.010$
deuteron	$0.122 \pm 0.007 \pm 0.006$	$0.090 \pm 0.022 \pm 0.011$	$0.007 \pm 0.025 \pm 0.015$

- relative contributions to cross section, τ^2_T and τ^2_{UPE} , of NPE SCHC non-conserving and UPE amplitudes

$$\tau^2_T = 0.025 \pm 0.003 \pm 0.003 \text{ (p); } 0.028 \pm 0.002 \pm 0.002 \text{ (d)}$$

$$\tau^2_{\text{UPE}} = 0.063 \pm 0.011 \pm 0.025 \text{ (p); } 0.046 \pm 0.008 \pm 0.023 \text{ (d)}$$

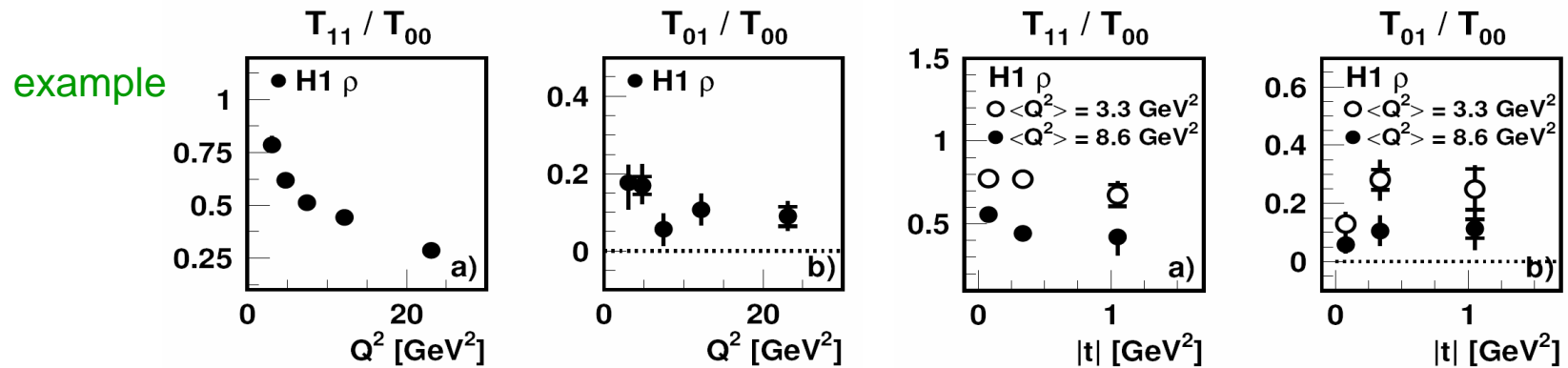
- for ρ^0 small ($\approx 10\%$) but statistically significant SCHS violating amplitudes T_{01} and T_{10}
- small contribution of unnatural-parity exchanges for ρ^0
- for ϕ no s-channel helicity violation and no UPE
- for proton and deuteron SDMEs (mostly) the same

➤ selected results on helicity amplitudes from H1 and ZEUS

❖ among SCHS non-conserving SDMEs **significantly $\neq 0$** $r^5_{00} \sim Re(T_{01} T_{00}^*)$
 smaller $Re r^{04}_{11}, Re r^1_{10}, Im r^2_{10} \sim Re(T_{01} T_{11}^*)$

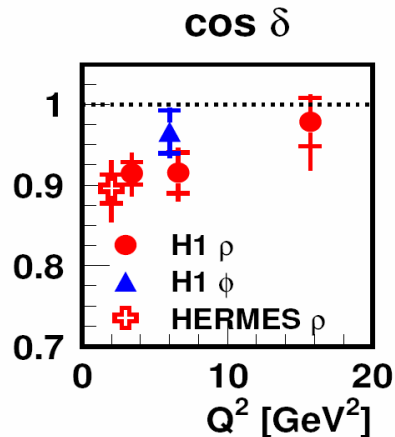
❖ UPE consistent with 0 (checked for transverse photons)

❖ extracted ratios of helicity amplitudes $T_{11}/T_{00}, T_{01}/T_{00}, T_{10}/T_{00}, T_{1-1}/T_{00}$ vs. Q^2 and t

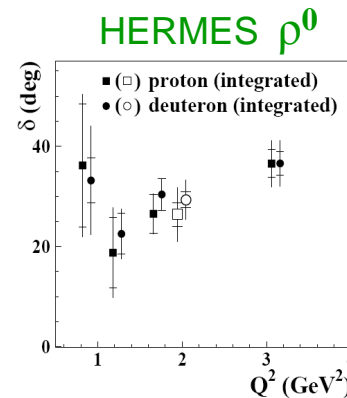


observed hierarchy of amplitudes $|T_{00}| > |T_{11}| \gg |T_{01}| > |T_{10}| \approx |T_{1-1}|$

❖ phase difference δ between T_{11} and T_{00}



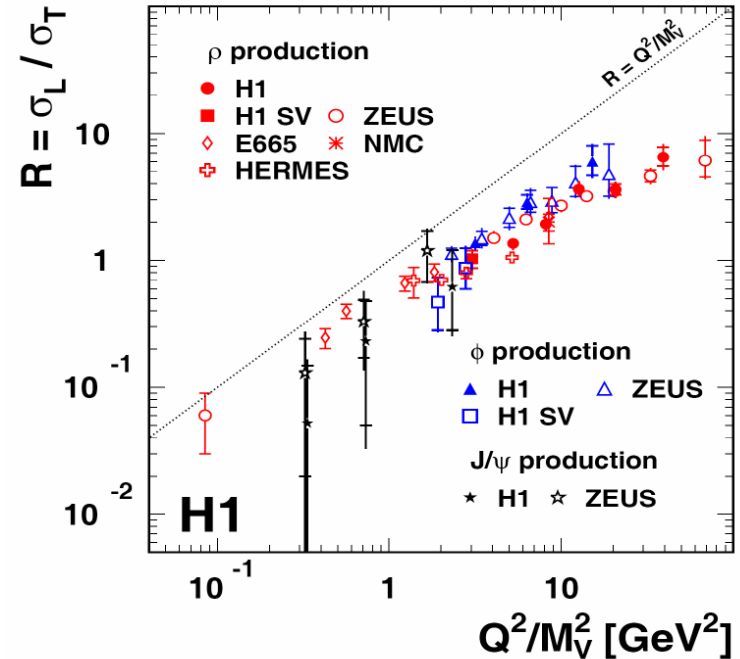
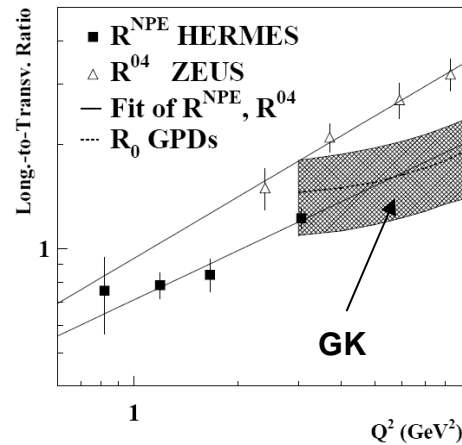
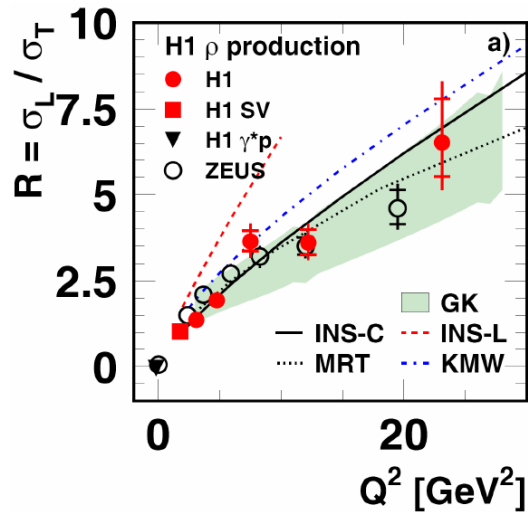
however opposite trend for HERMES only



reflection of possible x_B dependence ?

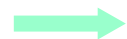
(due to Q^2 - x_B correlation in HERMES data)

$$R = \sigma_L / \sigma_T$$



- several models able to describe the data well
- qualitative universality of R vs. Q^2/M_V^2
- no significant W -dependence of R within single experiment

an indication of moderate increase between low energies (HERMES) and HERA

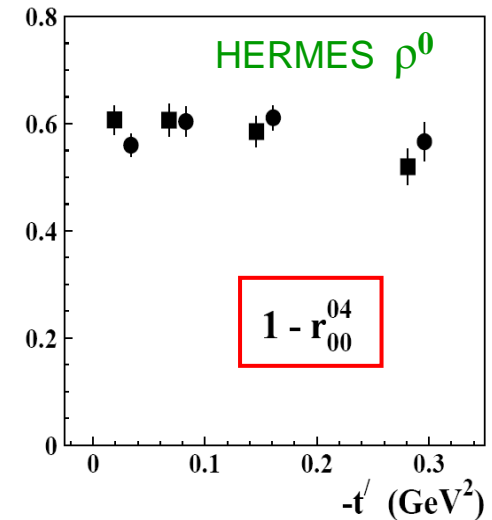
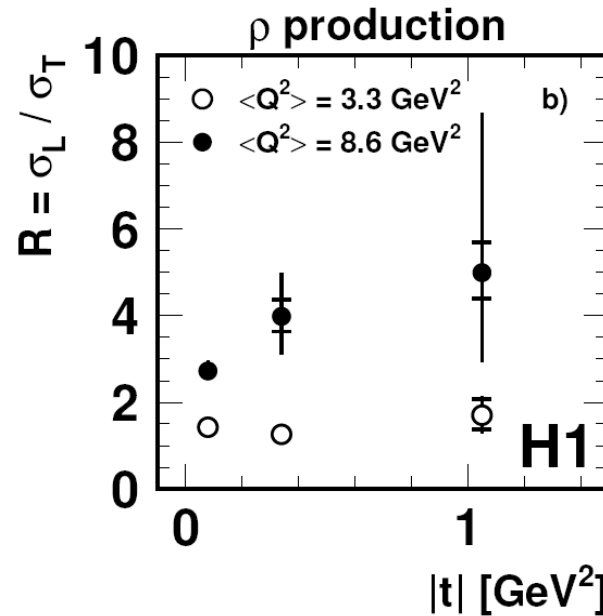
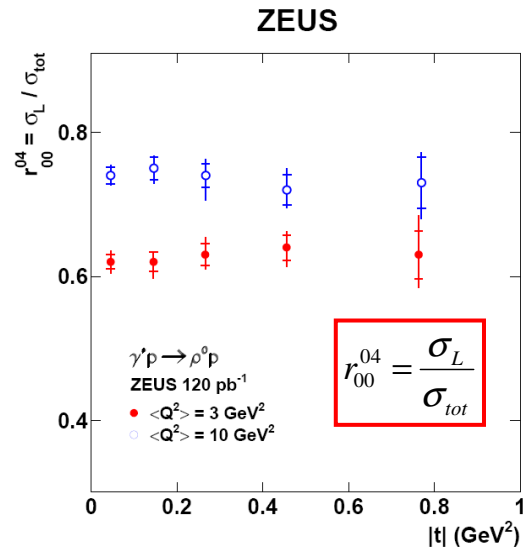


S. Goloskokov, more comparison of GK model vs. data

➤ t -dependence of R (or r_{00}^{04})

$$R(t) \propto e^{(b_L - b_T)t}$$

t -dependence of R would indicate different transverse sizes probed by γ_L^* and γ_T^*



- no significant t -dependence of R within total (statistical + systematic) errors

however from another H1 estimate of R using ratios of helicity amplitudes

3 σ from 0

$\langle Q^2 \rangle$ (GeV ²)	$b_L - b_T$ (GeV ⁻²)
ρ production	
3.3	$-0.06 \pm 0.22^{+0.24}_{-0.11}$
8.6	$-0.53 \pm 0.10^{+0.14}_{-0.57}$
ϕ production	
5.3	$-0.70 \pm 0.23^{+0.58}_{-0.63}$

Surprising !

needed to check by ZEUS and sensitivity to assumptions

Exclusive pseudoscalar meson production

π^+ (HERMES, Hall C), π^0 (Hall A, CLAS), η (CLAS)
 challenging at higher energies – small cross section

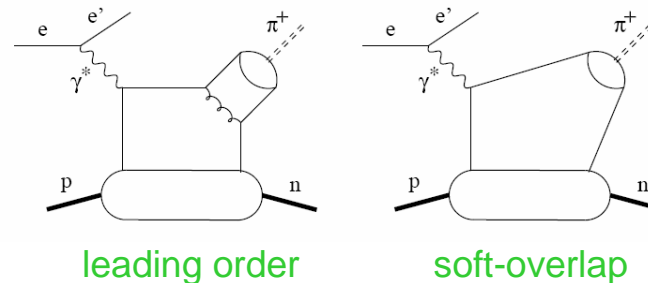
- for γ_L^* at leading order sensitivity to GPDs \tilde{H}, \tilde{E}

- flavour separation

π^+	$\Delta u - \Delta d$
π^0	$2\Delta u + \Delta d$
η	$2\Delta u - \Delta d$

- for π^+ important contribution to \tilde{E} of pion-pole exchange in t-channel dominates σ_L at small t
- no pion-pole exchange for π^0 ;
 π^0 from the pion cloud cannot couple directly to γ^*
- expected sizeable higher twist corrections:

- transverse momenta of partons
- soft overlap diagrams



➤ Exclusive π^+ production from HERMES

A. Airapetian et al. PL B 659, 486 (2008)

$$e p \rightarrow e n \pi^+$$

data collected in 1996-2005 from unpolarised and polarised proton target

$$0.02 \leq x_B \leq 0.55$$

$$1 < Q^2 < 11 \text{ GeV}^2$$

$$|t| \lesssim 2 \text{ GeV}^2$$

$$\langle W \rangle = 4 \text{ GeV}$$

L - T separation not possible

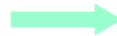
to ensure good efficiency and purity of pion identification

$$7 < p_\pi < 15 \text{ GeV}$$

selection of exclusive π^+ sample:

'double subtraction method'

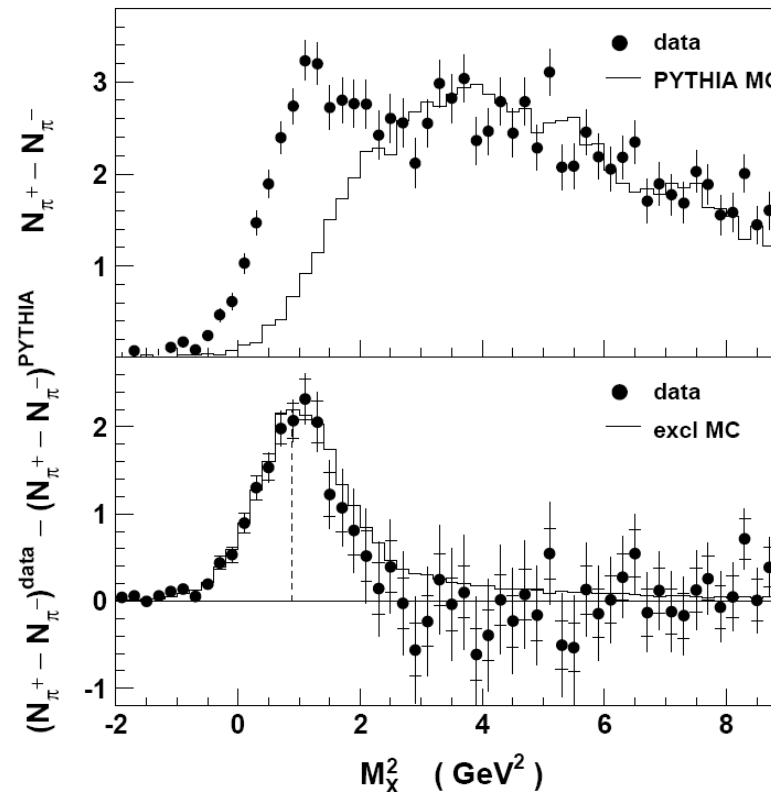
$$\text{cut: } M_X^2 < = 1.2 \text{ GeV}^2$$



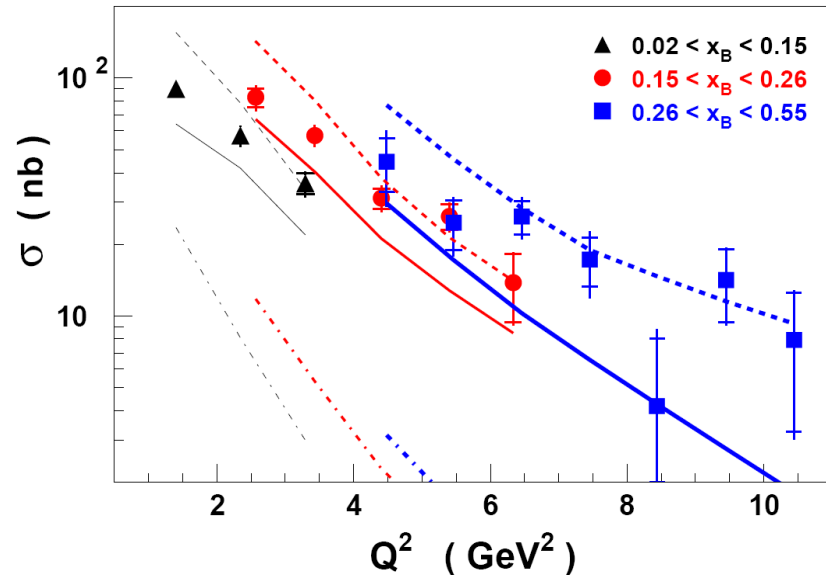
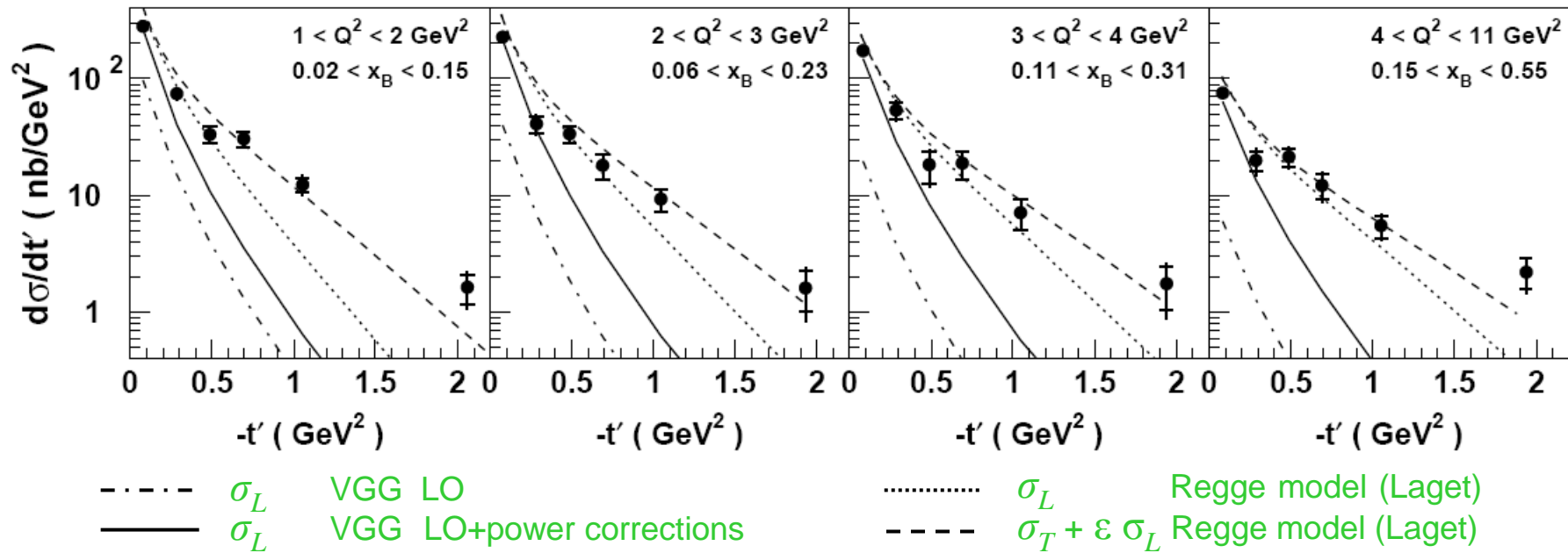
Main sources of systematic errors:

background subtraction

estimate of detection probability



HERMES π^+



- GPD LO calculations underestimate the data
- data support the order of the magnitude of the power corrections at low $-t'$ region
- Regge calculations for unseparated xsec. provides good description of magnitude and t' and Q^2 dependences

➤ Exclusive π^+ production at Hall C

$$e p \rightarrow e n \pi^+$$

$$\begin{aligned} \langle Q^2 \rangle &= 1.60, 2.45 \text{ GeV}^2 [*] \\ &= 2.15, 3.91 \text{ GeV}^2 [**] \\ \langle W \rangle &\approx 2.2 \text{ GeV} \end{aligned}$$

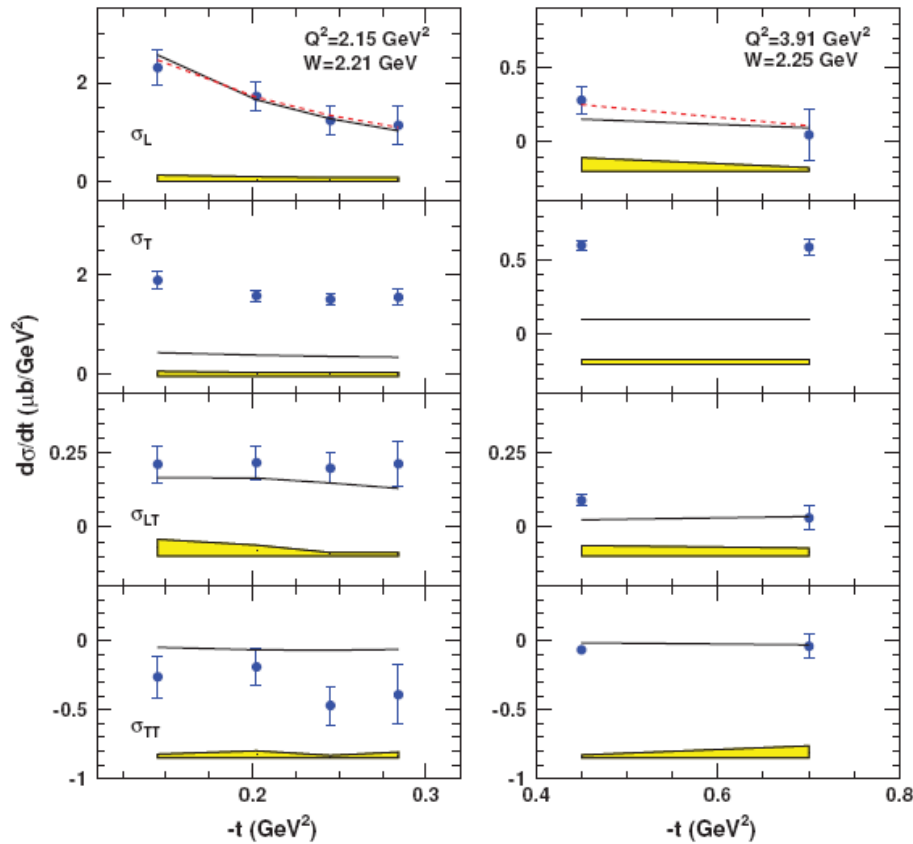
experiments $F_\pi - 2$ [*] and $\pi - \text{CT}$ [**]

T. Horn et al. PRL 97, 192001 (2006)

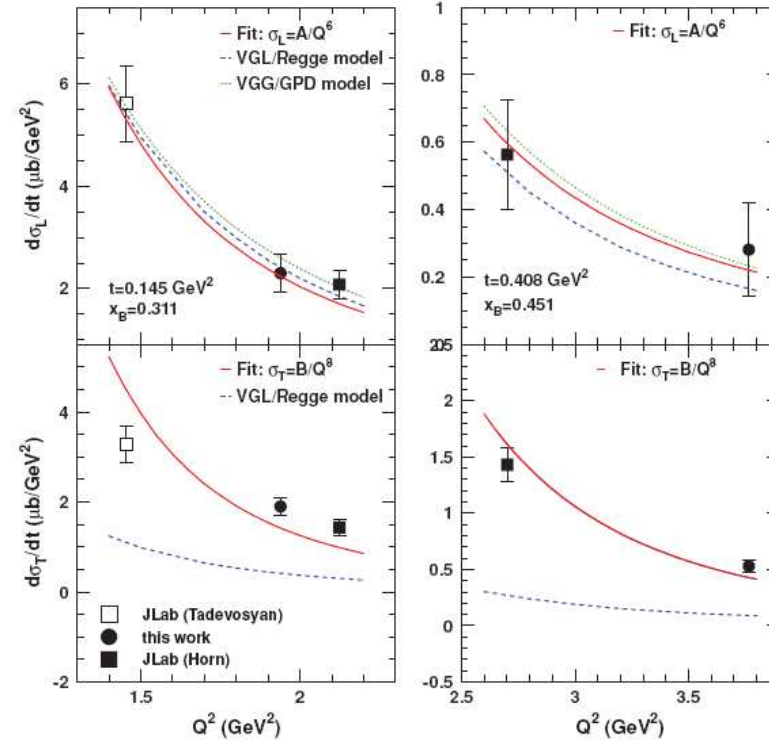
T. Horn et al. PR C78, 058201 (2008)

Rosenbluth separation of σ_L and σ_T

$$\frac{d^2\sigma_{\gamma^* p \rightarrow p\pi^+}}{dt d\phi} = \frac{1}{2\pi} \left(\frac{d\sigma_T}{dt} + \varepsilon \frac{d\sigma_L}{dt} + \varepsilon \cos 2\phi \frac{d\sigma_{TT}}{dt} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi \frac{d\sigma_{TL}}{dt} \right)$$



— VGL(Regge)
 - - - VGG(GPD with power corrections)

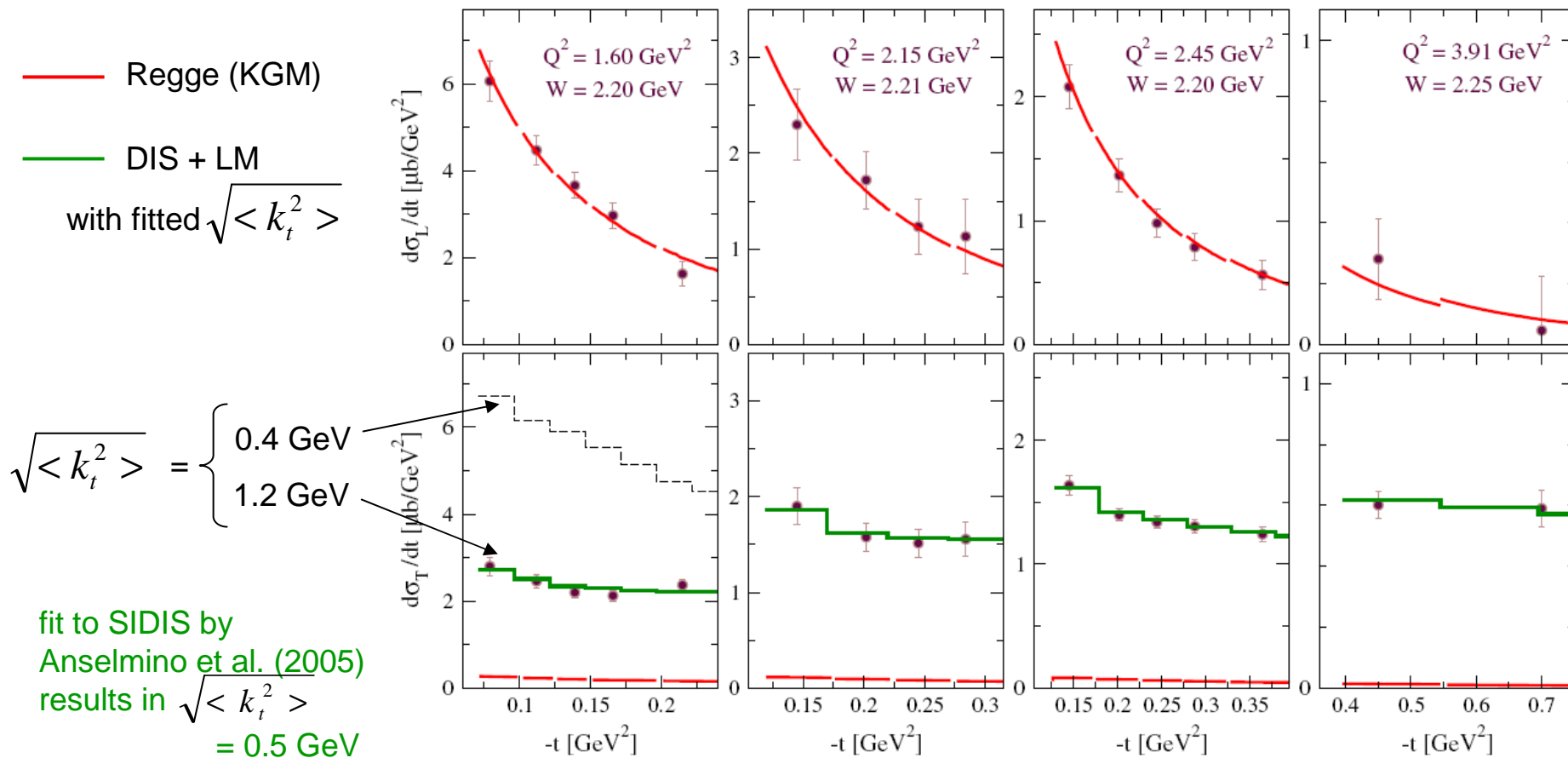


- GPD model describes σ_L well
- Regge calculations also reproduce σ_L well
 σ_T underestimated by factor $\sim 3 - 6$
- Q^2 dependence of σ_T significantly softer than $\sim Q^{-8}$

combined description of longitudinal and transverse components:

σ_L dominated by hadronic exchanges (Regge) and pion form factor

σ_T at moderate and large Q^2 mostly hard scattering process (DIS) $\gamma^* q \rightarrow q$
followed by fragmentation into $\pi^+ n$

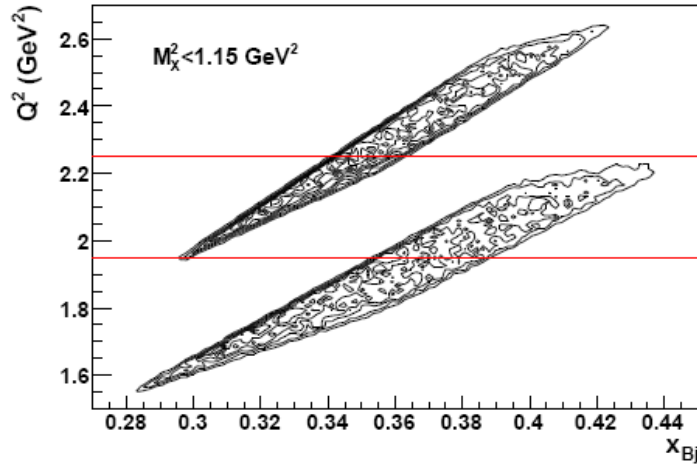


➤ Exclusive π^0 production at Hall A

preliminary

$$e p \rightarrow e p \pi^0 \rightarrow e p \gamma \gamma$$

kinematic domain



$$|t'| < 0.22 \text{ GeV}^2$$

missing mass $M_X[e\pi^0X]$ resolution

exclusivity cut $M_X^2 < 1.0 \text{ GeV}^2$

Main sources of systematic errors ($\approx 3.4\%$):

- HRS acceptance
- beam polarisation
- radiative corrections

at 5.75 GeV electron energy

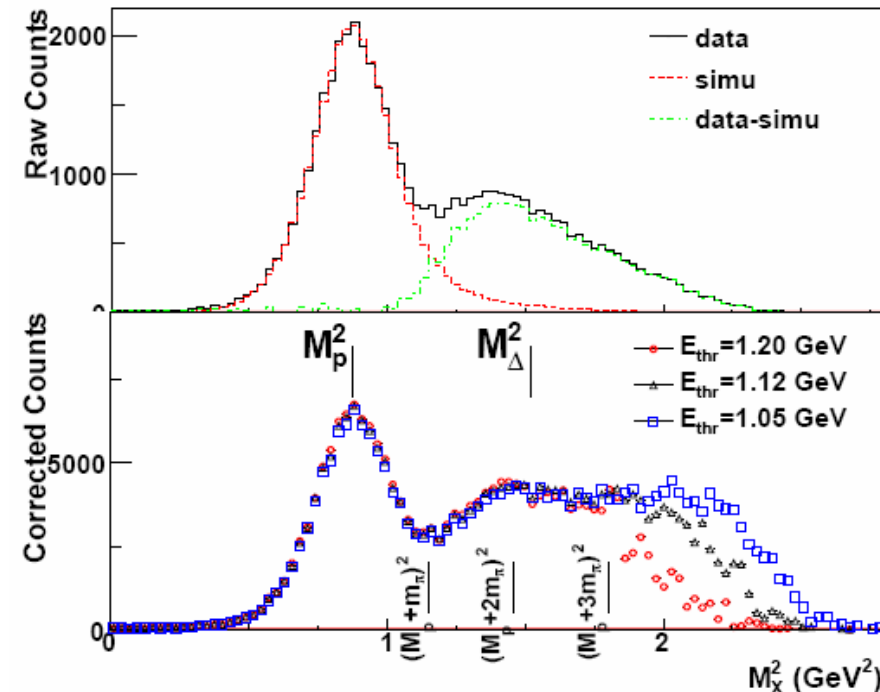
high resolution spectrometer + PbF_2 calorimeter

$$E_\gamma > 1 \text{ GeV}$$

results given for:

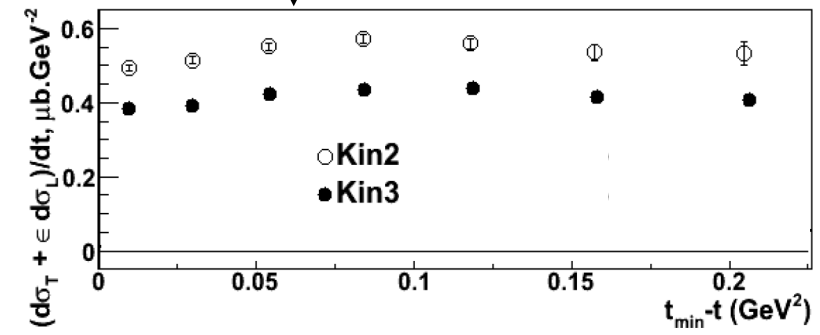
two values of Q^2 ($= 1.9, 2.3 \text{ GeV}^2$) at fixed $x_B = 0.36$

two values of x_B ($= 0.40, 0.33$) at fixed $Q^2 = 2.1 \text{ GeV}^2$

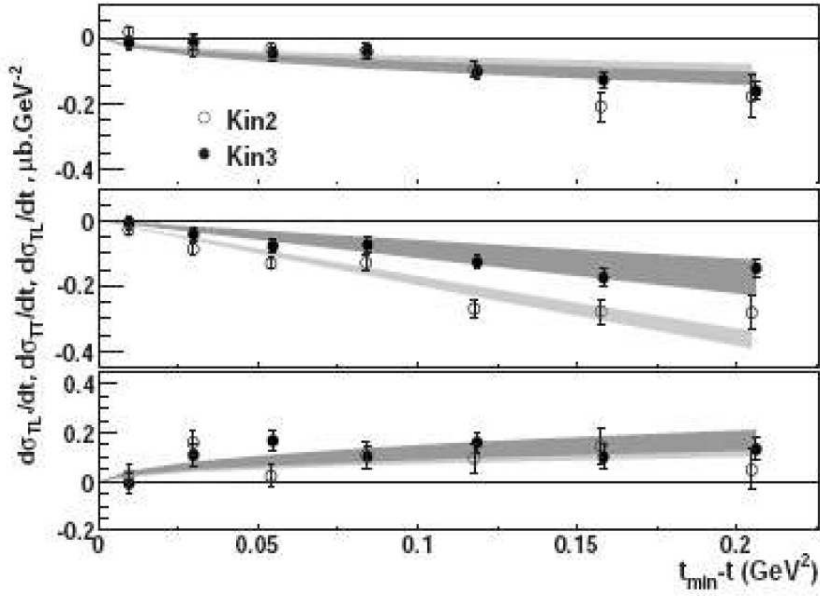


Hall A π^0

$$\frac{d\sigma}{dt} = \underbrace{\frac{d\sigma_T}{dt} + \epsilon_L \frac{d\sigma_L}{dt}}_{\epsilon (\epsilon_L) \text{ degree of linear (longitudinal) polarisation of } \gamma^*} + \sqrt{2\epsilon_L(1+\epsilon)} \frac{d\sigma_{TL}}{dt} \cos\phi_\pi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi_\pi + h\sqrt{2\epsilon_L(1-\epsilon)} \frac{d\sigma_{TL'}}{dt} \sin\phi_\pi$$



Kin2: $Q^2 = 1.9 \text{ GeV}^2, x_B = 0.36$
 Kin3: $Q^2 = 2.3 \text{ GeV}^2, x_B = 0.36$

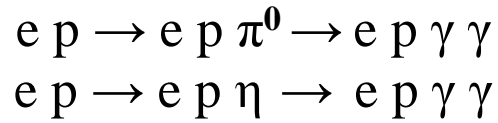


bands show fits $\sim \sin\theta_{\pi}^{CM}, \sin^2\theta_{\pi}^{CM}, \sin\theta_{\pi}^{CM}$
 for components $\sigma_{TL}, \sigma_{TT}, \sigma_{TL'}$ respectively

- no depletion at $t'=0$
 and no significant t -dependence of $\sigma_T + \epsilon \sigma_L$
- slow Q^2 -dependence of $\sigma_T + \epsilon \sigma_L \sim (Q^2)^{-1.35 \pm 0.10}$
 far from the QCD leading twist prediction
 for $\sigma_L \sim (Q^2)^{-3}$
- reasonable agreement (within $\approx 15\%$) between
 Regge model (Laget) and $\sigma_T + \epsilon \sigma_L$
 no agreement for interference terms
- need $\sigma_L - \sigma_T$ separation
 E07-007 taking data now

➤ Exclusive π^0 and η production at CLAS

preliminary



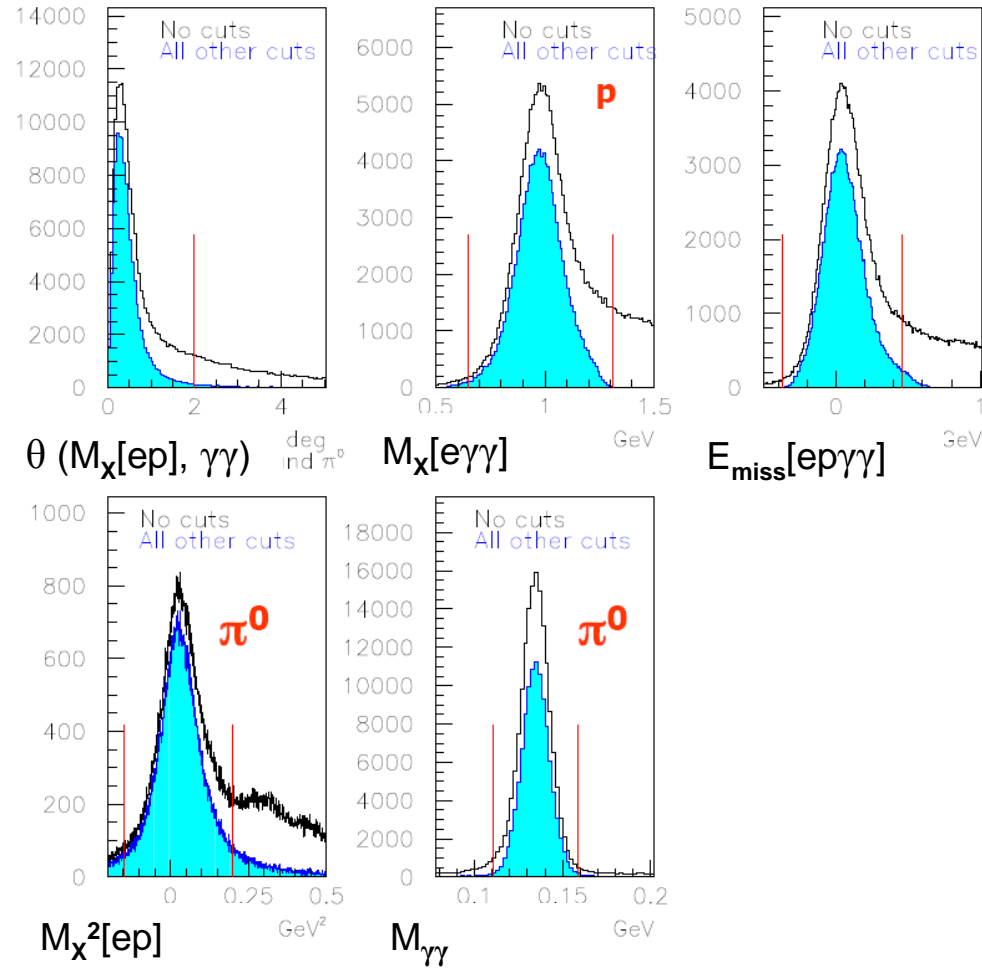
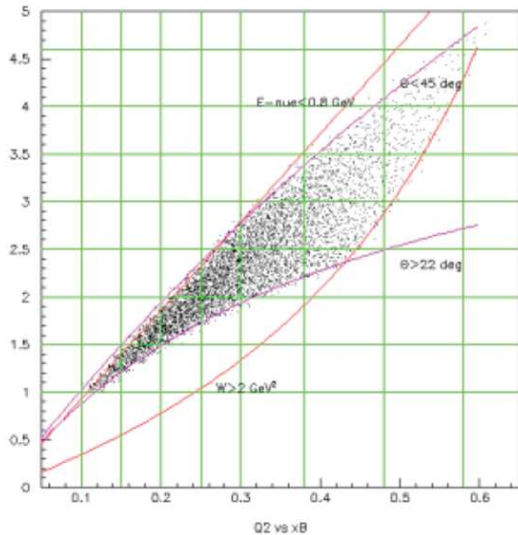
at 5.78 GeV electron energy

various cuts to ensure exclusivity ☺

$$1 \leq Q^2 < 4.5 \text{ GeV}^2$$

$$0.1 < x_B < 0.58$$

$$0.09 < |t| < 2.0 \text{ GeV}^2$$

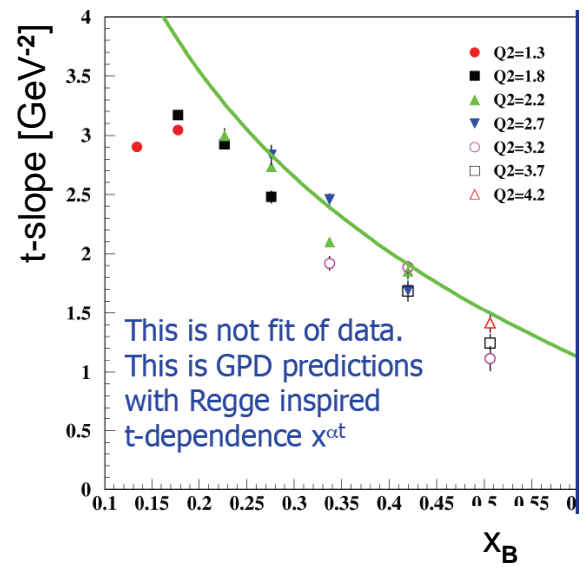
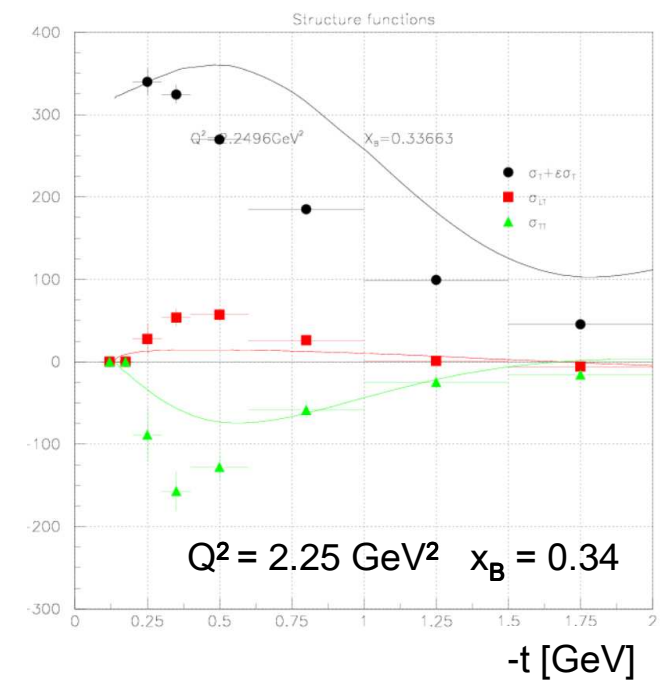
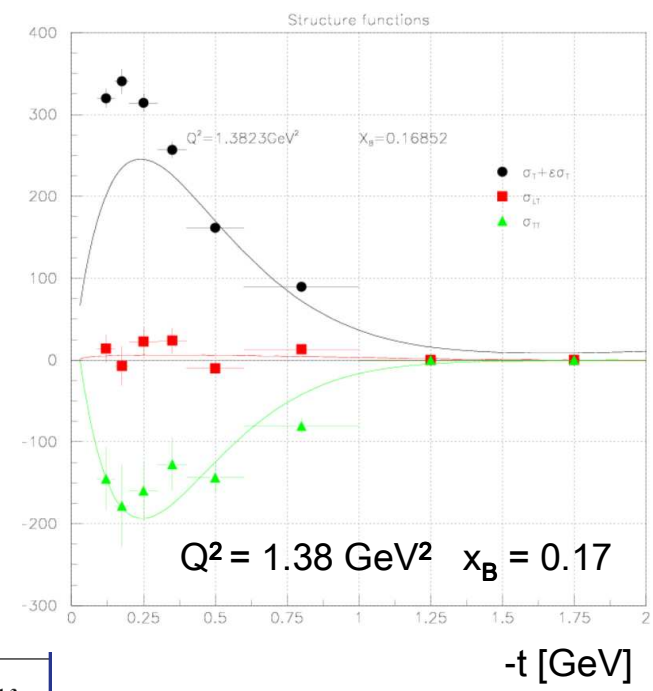


CLAS π^0

$$\frac{d^2\sigma_{\gamma^*p \rightarrow p\pi^0}}{dt d\phi} = \frac{1}{2\pi} \left(\underbrace{\frac{d\sigma_T}{dt} + \varepsilon \frac{d\sigma_L}{dt}}_{\bullet} + \varepsilon \cos 2\phi \underbrace{\frac{d\sigma_{TT}}{dt}}_{\blacktriangle} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi \underbrace{\frac{d\sigma_{LT}}{dt}}_{\blacksquare} \right)$$

example: \rightarrow
2 out of 25 (Q^2, x_B) bins

compared to
Regge model (Laget)



- Regge model exhibits similar trends as the data but quantitative differences, in particular at $|t| (< 0.5 \text{ GeV}^2)$
- t-slope almost independent of Q^2 , decreases with x_B
- ratio $\sigma_{\eta}/\sigma_{\pi} = 0.2 - 0.4$, very weak dependence on Q^2 and x_B increases with $|t|$

\rightarrow V. Kubarovsky

Exclusive meson production on transversely polarised targets

at leading twist cross section sensitive to GPD E and \tilde{E}

transverse target
spin dependent
cross section

$$\begin{aligned} \frac{1}{2} \left(\frac{d\sigma_{00}^{\uparrow\uparrow}}{dt} - \frac{d\sigma_{00}^{\downarrow\downarrow}}{dt} \right) &= -\text{Im} \frac{d\sigma_{00}^{+-}}{dt} = \Gamma' \sqrt{1-\xi^2} \frac{\sqrt{t_0-t}}{M_p} \text{Im}(E_M^* H_M) && \text{for vector mesons} \\ &= -\Gamma' \sqrt{1-\xi^2} \frac{\sqrt{t_0-t}}{M_p} \xi \text{Im}(\tilde{E}_M^* \tilde{H}_M) && \text{for pseudoscalar mesons} \\ \Gamma' &= \frac{\alpha_{\text{em}}}{Q^6} \frac{x_B^2}{1-x_B} && \xi = \frac{x_B}{2-x_B}, \quad -t_0 = \frac{4\xi^2 M_p^2}{1-\xi^2} \end{aligned}$$

$H_M, E_M (\tilde{H}_M, \tilde{E}_M)$

are weighted sums of convolutions of hard scattering kernels ,
corresponding GPDs of quarks and gluons, and meson DAs

weights depend on contributions of various quark flavours and of
gluons to the production of meson M

access to 'elusive' GPD E and the orbital angular momentum of quarks

so far GPD E poorly constrained by data (mostly by Pauli form factors)

$$\frac{1}{2} \int_{-1}^1 dx x [H_q(x, \xi, t) + E_q(x, \xi, t)] \stackrel{t \rightarrow 0}{=} J_q = \frac{1}{2} \Delta \Sigma + L_q$$

Ji's sum rule

➤ exclusive ρ^0 production on p^\uparrow at HERMES

A. Airapetian et al. PL B 679, 100 (2009)

Transversely polarised
proton target, $P_T \approx 73\%$
2002-2005 data

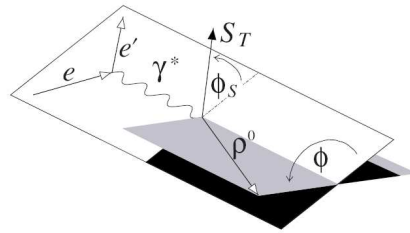
$$\begin{aligned} Q^2 &> 1 \text{ GeV}^2 \\ W &> 2 \text{ GeV}^2 \\ |t'| &< 0.4 \text{ GeV}^2 \end{aligned}$$

30 new SDMEs determined for the first time !

$$\begin{aligned} n_{\mu\mu'}^{\nu\nu'} \text{ and } s_{\mu\mu'}^{\nu\nu'} \text{ from } W_{UT}(\phi, \phi_s, \vartheta) \\ (\text{similarly } u_{\mu\mu'}^{\nu\nu'} \text{ from } W_{UU}(\phi, \varphi, \vartheta)) \end{aligned}$$

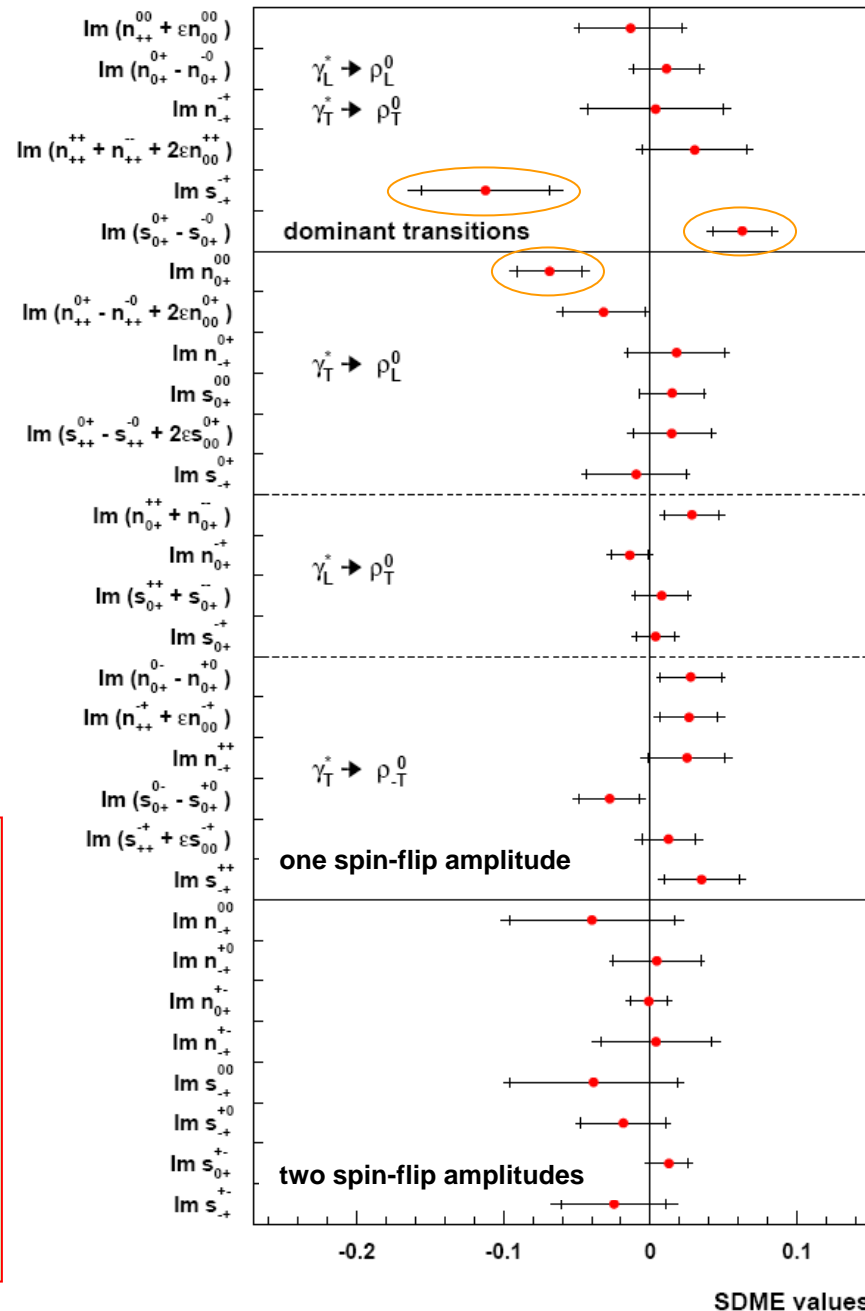
Diehl's convention:

$\mu, \mu' (v, v')$ helicities of $\gamma^* (\rho^0)$.
For amplitudes $T(U)_{\mu\alpha}^{\nu\beta}$
 $\alpha (\beta)$ correspond to helicity
of initial (final) proton



- $\text{Im } s_{-+}^{-+}, \text{Im}(s_{0+}^{0+} - s_{0+}^{-0}) > 2.5\sigma$ from 0
 $\text{Im } s_{-+}^{-+} \sim T_{-+}^{-+}(U_{+-}^{++})^* \quad \text{Im } s_{0+}^{0+} \sim T_{0+}^{0+}(U_{+-}^{++})^*$
 signal of UPE; related to \tilde{H}, \tilde{E}
- $\text{Im } n_{0+}^{00} > 2.5\sigma$ from 0
 another indication of SCHC violation
 in $\gamma_T^* \rightarrow \rho_L$

$$\langle x_B \rangle = 0.08, \langle Q^2 \rangle = 1.95 \text{ GeV}^2, \langle -t' \rangle = 0.13 \text{ GeV}^2$$



HERMES ρ^0 off p^\uparrow

for ρ^0_L

$$A_{UT}^{LL, \sin(\phi - \phi_S)} = \frac{\text{Im}(n_{++}^{00} + \varepsilon n_{00}^{00})}{u_{++}^{00} + \varepsilon u_{00}^{00}}$$

$$u_{++}^{00} + \varepsilon u_{00}^{00} = \frac{\sigma(\rho_L^0)}{\sigma(\rho_T^0) + \varepsilon \sigma(\rho_L^0)} \quad (\equiv r_{00}^{04})$$

(in Schilling-Wolf notation)

for ρ^0_T

$$A_{UT}^{TT, \sin(\phi - \phi_S)} = \frac{\text{Im}(n_{++}^{++} + n_{++}^{--} + 2\varepsilon n_{00}^{++})}{1 - (u_{++}^{00} + \varepsilon u_{00}^{00})}$$

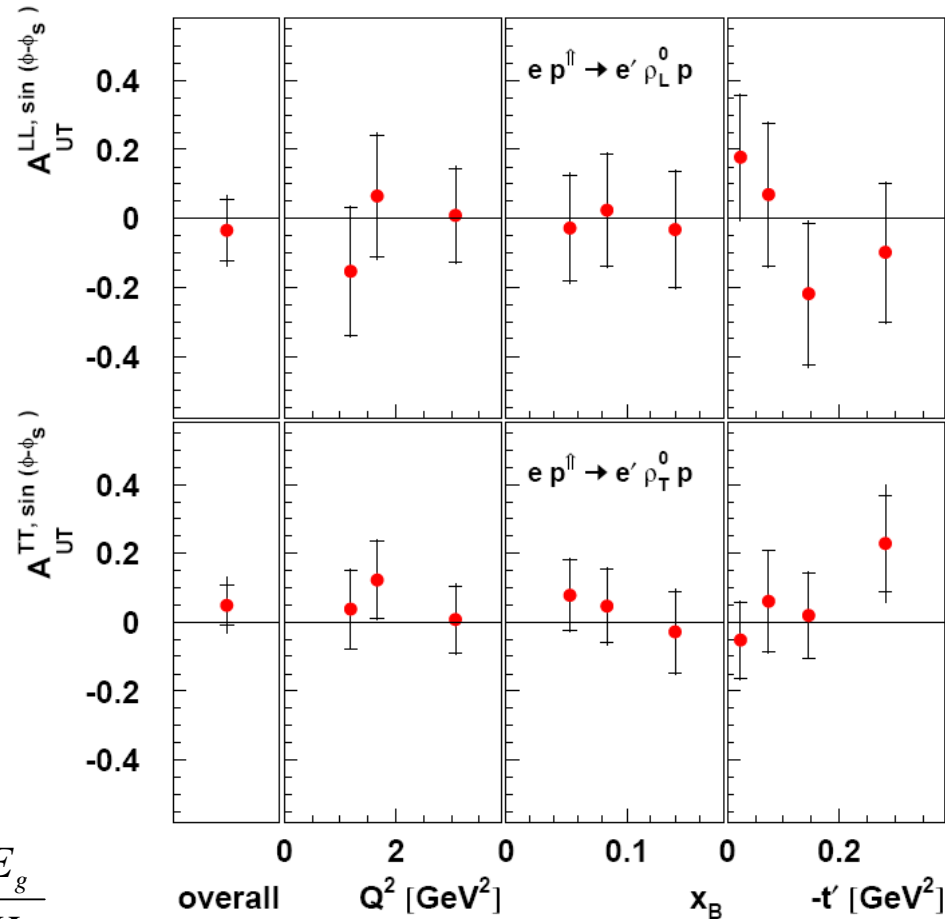
if SCHC $A_{UT}^{LL, \sin(\phi - \phi_S)} \cong \frac{\text{Im} n_{00}^{00}}{u_{00}^{00}} \propto \frac{E_M}{H_M} \propto \frac{E_q + E_g}{H_q + H_g}$

a few GPD model calculations for $A_{UT}^{\sin(\phi - \phi_S)}$ for ρ^0

Goeke, Polyakov, Vanderhaegen (2001)

Ellinghaus, Nowak, Vinnikov, Ye (2006)

E_q parameterised in terms of J^u and J^d
ENVY includes also E_g



$$A_{UT}^{LL, \sin(\phi - \phi_S)} = -0.035 \pm 0.103$$

- J^u in the range 0.2 - 0.4 and $J^d = 0$ consistent with ρ^0 data, although within large errors

➤ exclusive ρ^0 production on p^\uparrow and d^\uparrow at COMPASS

preliminary

Transversely polarised **deuteron** target (${}^6\text{LiD}$), $P_T \approx 50\%$, 2002-2004 data

Transversely polarised **proton** target (NH_3), $P_T \approx 90\%$, 2007 data

Target segmented in 2 (3 in 2007) cells with opposite polarisations

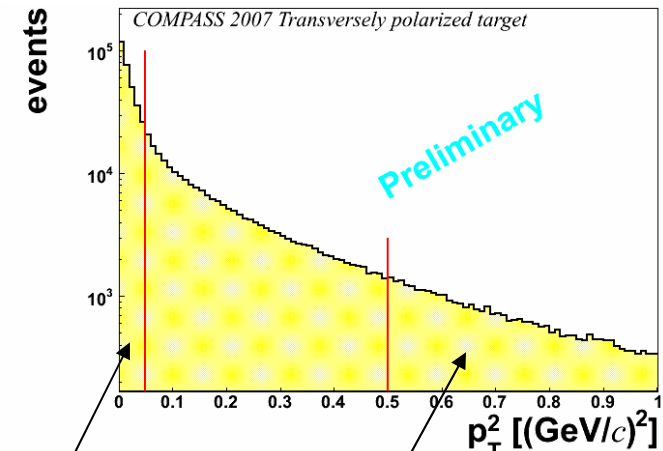
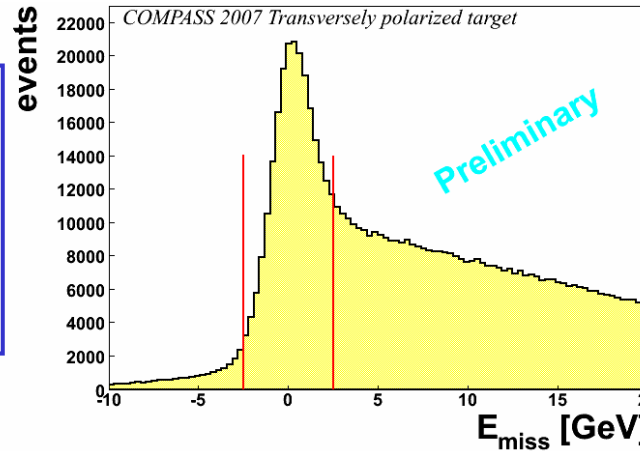
Spins reversed regularly by DNP

Kinematic domain

$$\begin{aligned}
 & Q^2 > 1 \text{ GeV}^2 \\
 & W > 5 \text{ GeV} \\
 & 0.005 < x_{\text{Bj}} < 0.1 \\
 & 0.05 < p_t^2 < 0.5 \text{ GeV}^2 \quad [\text{NH}_3] \\
 & 0.01 < p_t^2 < 0.5 \text{ GeV}^2 \quad [{}^6\text{LiD}]
 \end{aligned}$$

$$-0.3 < M_{\pi\pi} - M_{\rho(\text{PDG})} < 0.3 \text{ GeV}/c^2$$

$$E_{\text{miss}} = \frac{M_X^2 - M_{\text{proton}}^2}{2M_{\text{proton}}} \in [-2.5, 2.5] \text{ GeV}$$



dominant coherent on N

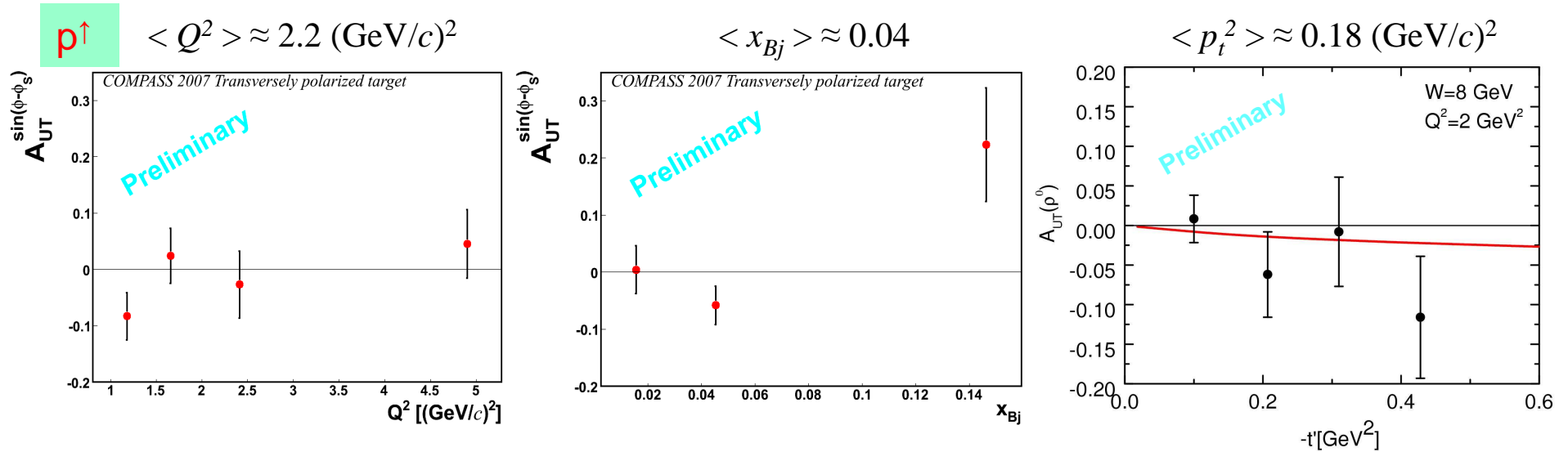
dominant non-exclusive bkg.

A_{UT} extracted with the **double ratio (DR) method**;

in $\text{DR}(\phi - \phi_s)$ counts from different cells for the data before and after spin reversal combined such that in the ratio muon **flux**, **numbers of target nucleons** and unpolarised cross section σ_0 cancel also **acceptance** cancels provided no changes between spin reversals

$$\text{fit to DR}(\phi - \phi_s) \longrightarrow A_{UT}^{\sin(\phi - \phi_s)} = -\frac{\text{Im}(\sigma_{++}^{+-} + \varepsilon \sigma_{00}^{+-})}{\sigma_0} \quad \sigma_0 = \frac{1}{2}(\sigma_{++}^{++} + \sigma_{++}^{--}) + \varepsilon \sigma_{00}^{++} \equiv \sigma_T + \varepsilon \sigma_L$$

COMPASS ρ^0 off p^\uparrow and d^\uparrow



- $A_{UT}^{\sin(\phi-\phi_s)}$ for transversely polarised protons compatible with 0
- compatible with predictions of the GPD model of GK for protons
- for the proton target errors $\approx 2x$ smaller than for HERMES
- for transversely polarised deuterons $A_{UT}^{\sin(\phi-\phi_s)}$ also compatible with 0

in progress: L/T ρ^0 separation

coherent/incoherent separation for deuteron data

estimate effects of the non-exclusive background

in 2010 data with transverse polarisation with NH_3 target \rightarrow 3-fold increase of statistics

➤ exclusive π^+ production on p^\uparrow at HERMES

determined for the first time !

A. Airapetian et al. PL B 682, 345 (2010)

Transversely polarised **proton** target

$P_T \approx 73\%$, 2002-2005 data

$$0.03 \leq x_B \leq 0.35$$

$$1 < Q^2 < 10 \text{ GeV}^2$$

$$|t| \leq 0.7 \text{ GeV}^2$$

$\langle W \rangle = 4 \text{ GeV}$

selection of exclusive π^+ sample:

$7 < p_\pi < 15 \text{ GeV}$

'double subtraction method'

$-1.2 < M_X^2 < = 1.2 \text{ GeV}^2$

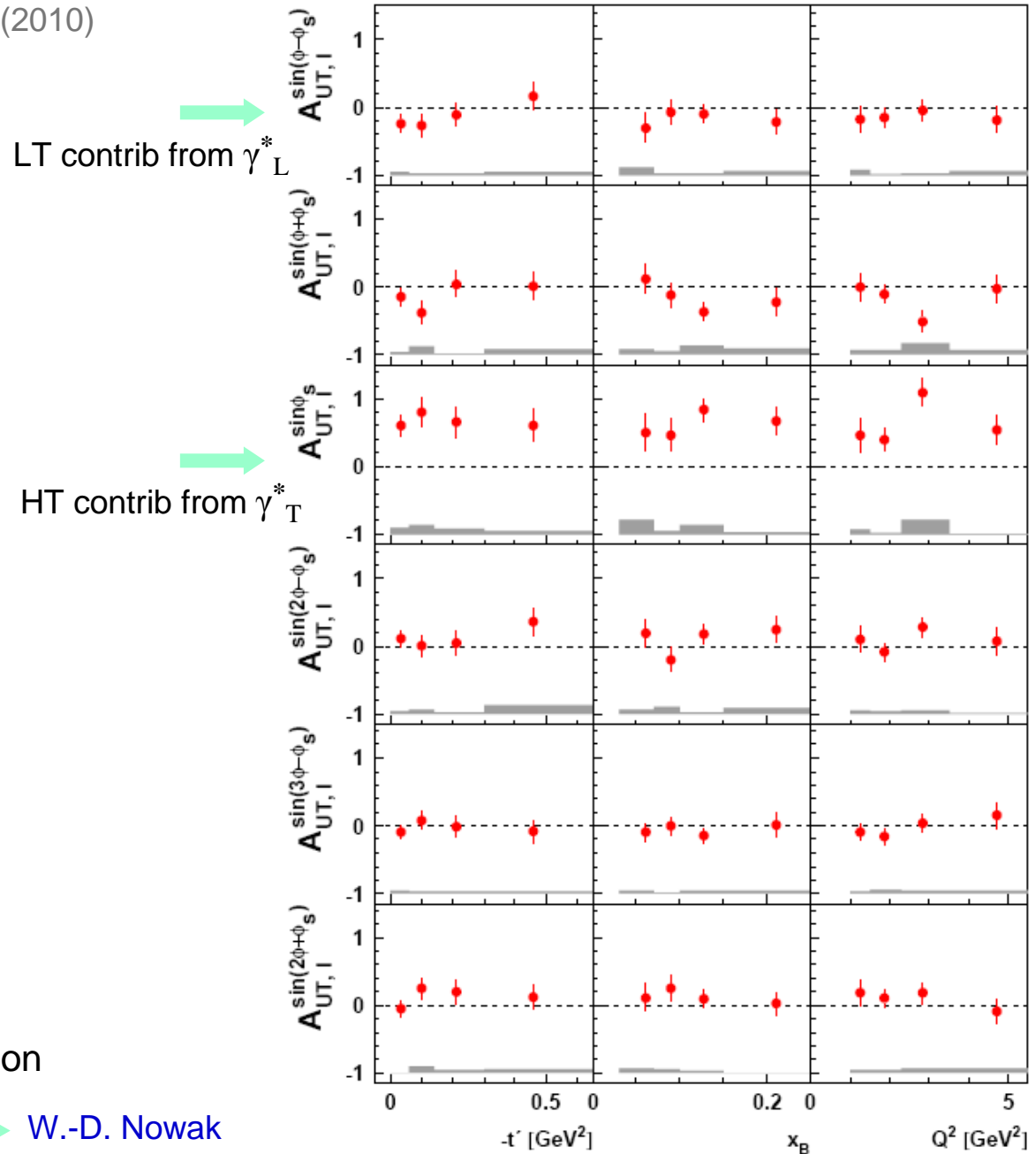
Main systematic errors

background subtraction

estimate of detection probability

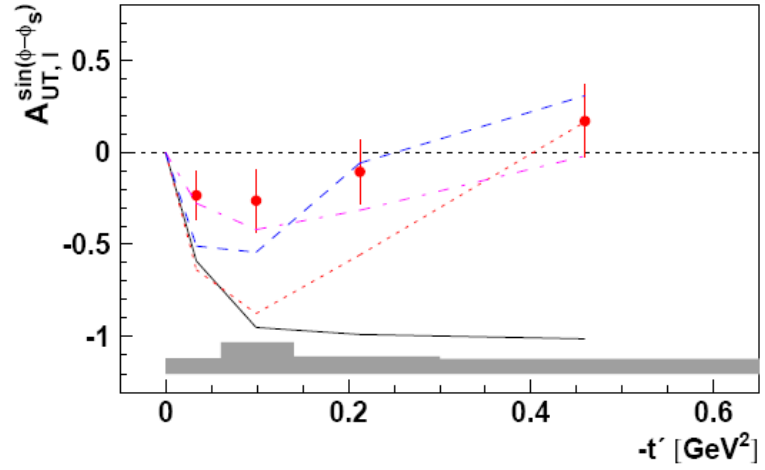
determination of target polarisation

➡ W.-D. Nowak



HERMES π^+ off $p \uparrow$

$$A_{UT,l}^{\sin(\phi-\phi_s)} = -\frac{\sqrt{-t'}}{M_p} \times \frac{\xi \sqrt{1-\xi^2} \text{Im}(\tilde{\mathcal{E}}^* \tilde{\mathcal{H}})}{(1-\xi^2)\tilde{\mathcal{H}}^2 - \frac{t\xi^2}{4M_p^2} \tilde{\mathcal{E}}^2 - 2\xi^2 \text{Re}(\tilde{\mathcal{E}}^* \tilde{\mathcal{H}})}$$



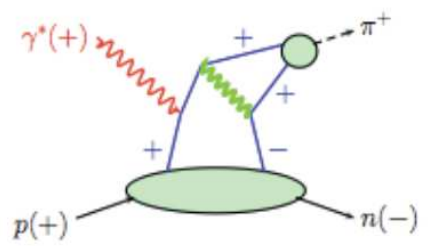
- } C. Bechler, D. Müller } pion pole dominates \tilde{E}
- ⋯ } more t-channel exchanges
- · - K. Kumericki, D. Müller
- - - S. Goloskokov, P. Kroll

$$A_{UT,l}^{\sin \phi_s} \propto \mathcal{M}_{0+++}^* + \mathcal{M}_{0+0-} + \mathcal{M}_{0-++}^* + \mathcal{M}_{0-0-}$$

$\begin{matrix} \nearrow & \nearrow & \nearrow & \nwarrow \\ \pi & n & \gamma^* & p \end{matrix}$

in LT $\mathcal{M}_{0-++}^* \sim \sqrt{-t'}$

higher twist contributions involving H_T and \tilde{H}_T doesn't have to vanish



$$H_T(x,0,0) = h_I(x)$$

- $A_{UT,l}^{\sin(\phi-\phi_s)}$ consistent with zero within errors excluding pure pion-pole contribution to GPD \tilde{E}
- $A_{UT,l}^{\sin(\phi_s)}$ signal of $\gamma_T^* \rightarrow \pi^+$ transitions interesting link to transversity and chiral odd GPDs

Conclusions

- Significant progress on meas. of cross sections, SDME's and spin asymmetries provide more stringent constraints on the models for DVMP
- Description of the present data on DVMP in terms of GPDs more complex than LT handbag approach:
power corrections, higher order pQCD terms,
quark-antiquark exchanges, semiinclusive-like contribution etc.
- For DVMP program at future facilities: **JLAB12, COMPASS-II, EIC**
essential experimental requirements for further progress:
high luminosity, hermetic detector (or recoil detector), $\gamma_L^* - \gamma_T^*$ separation