



TMDs at COMPASS

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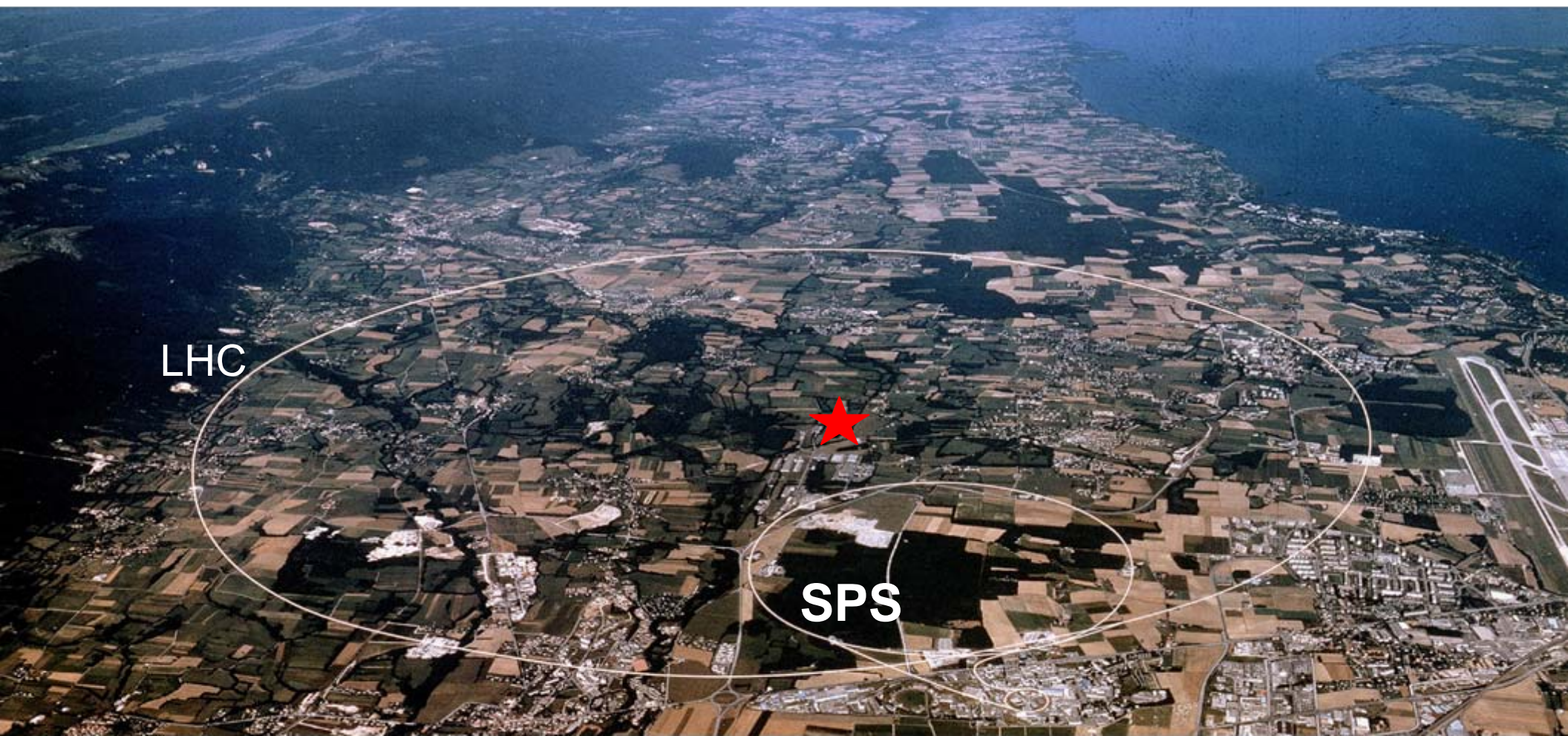
**on behalf of
the COMPASS Collaboration**

OUTLINE

- **the COMPASS experiment**
- **results on azimuthal asymmetries**
 - unpolarised d target
 - longitudinally polarised d target
 - transversely polarised d and p targets
 - Collins asymmetry, 2h asymmetry, Λ polarisation
 - Sivers asymmetry
- **future measurements**



the **Common**
Muon and
Proton
Apparatus for
Structure and
Spectroscopy **Experiment**



LHC

SPS



the COMPASS Experiment

broad physics program – data taking started in 2002

- hadron spectroscopy (hadron beams)
(2004) 2008 2009 runs
- nucleon spin structure with high energy muon beam

2002	} polarised deuteron (${}^6\text{LiD}$) target	— L & T (20%)
2003		
2004		
2006	polarised deuteron (${}^6\text{LiD}$) target	— L only
2007	polarised proton (NH_3) target	— L & T (50%)
2010	polarised proton (NH_3) target	— T only
2011	polarised proton (NH_3) target	— L only

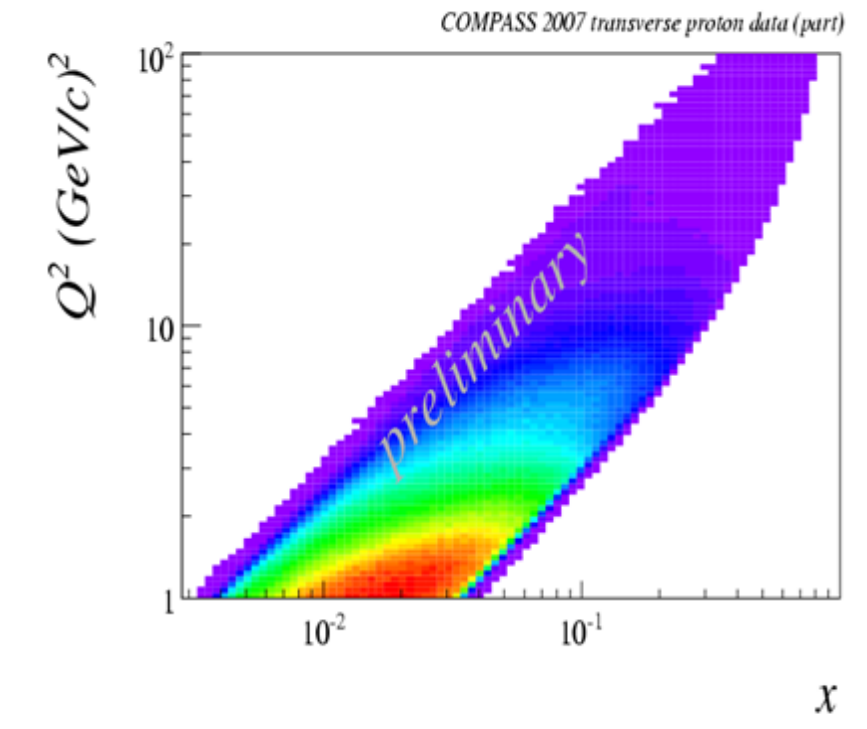
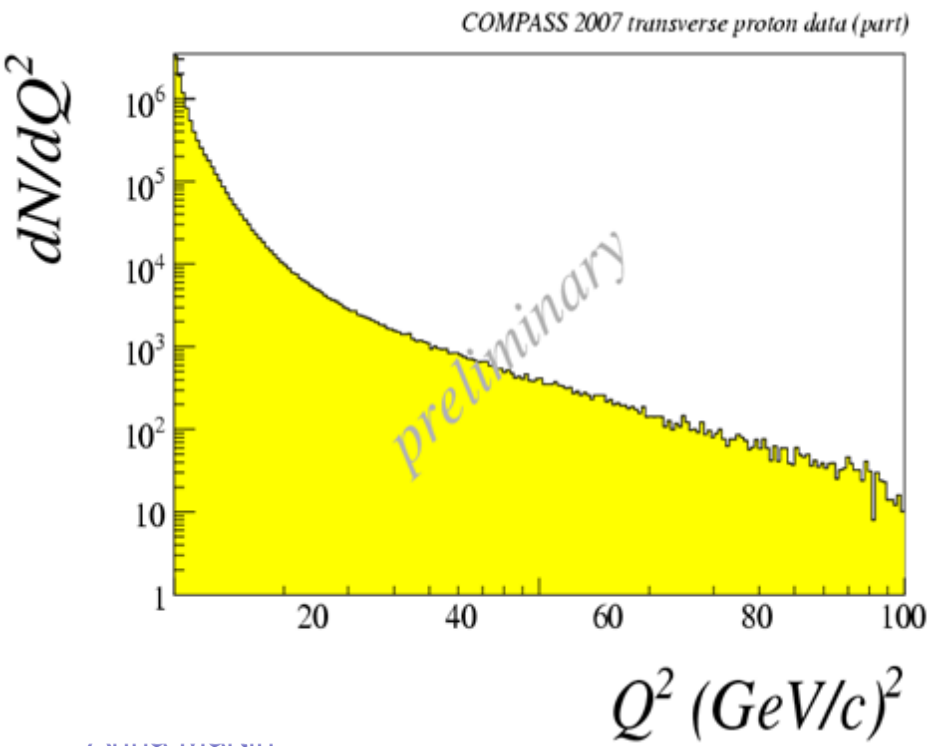
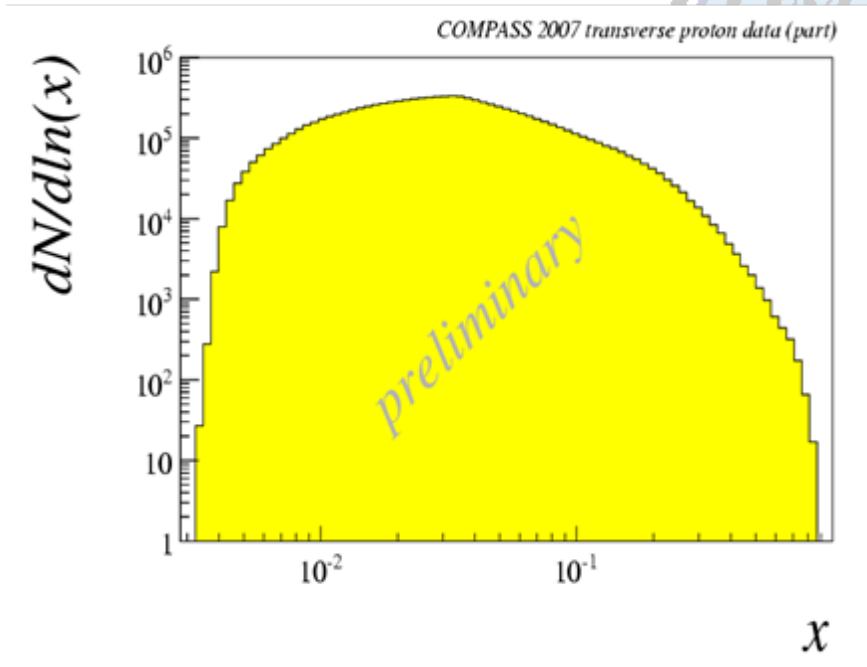
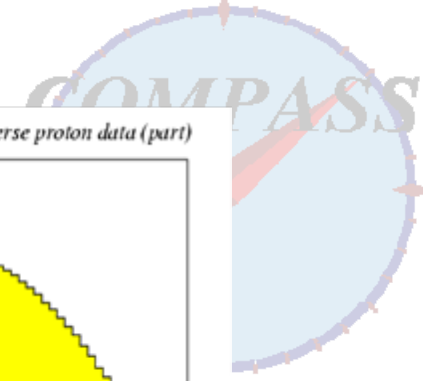
muon beam: 160 GeV/c

longitudinal polarisation -80%

intensity $2 \cdot 10^8 \mu^+/\text{spill}$ (4.8s/16.2s)

SIDIS event selection

DIS cuts: $Q^2 > 1 \text{ (GeV/c)}^2$
 $0.1 < y < 0.9$
 $W > 5 \text{ GeV/c}^2$

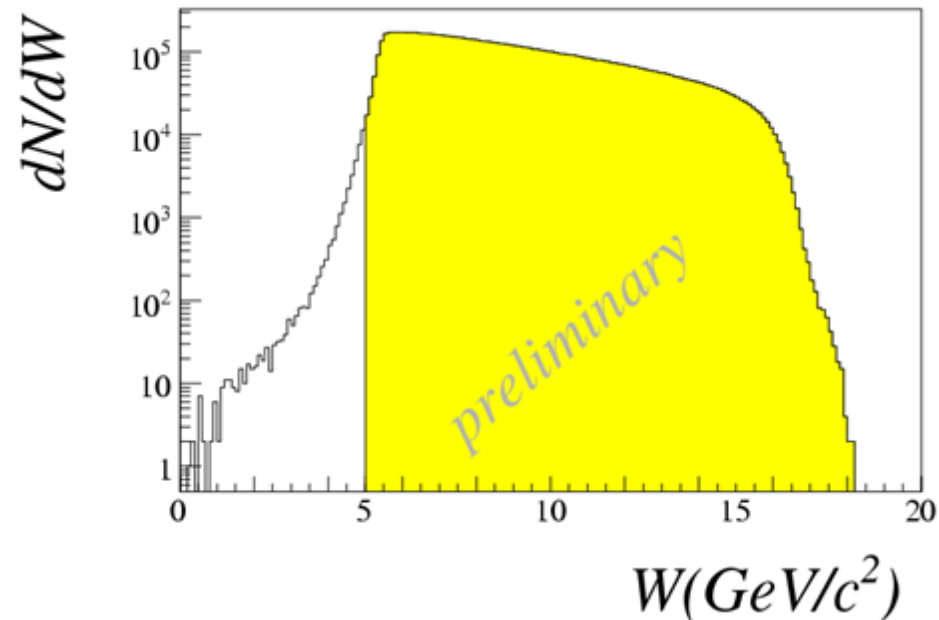


SIDIS event selection

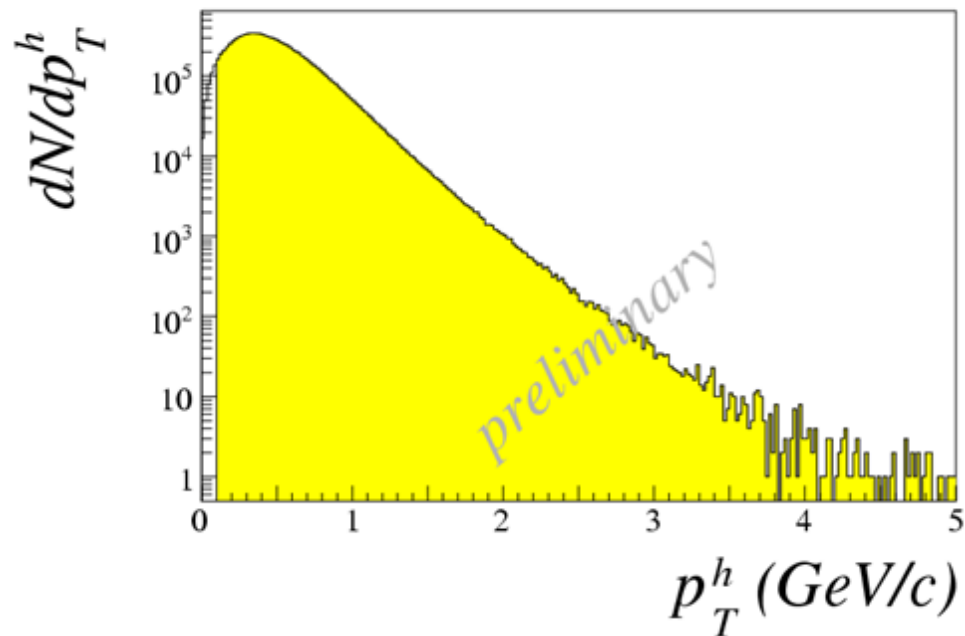
DIS cuts: $Q^2 > 1 \text{ (GeV/c)}^2$
 $0.1 < y < 0.9$
 $W > 5 \text{ GeV/c}^2$

hadron selection: $p^h > 1.5 \text{ GeV/c}$,
 $p_T^h > 0.1 \text{ GeV/c}$,
 $z > 0.2$

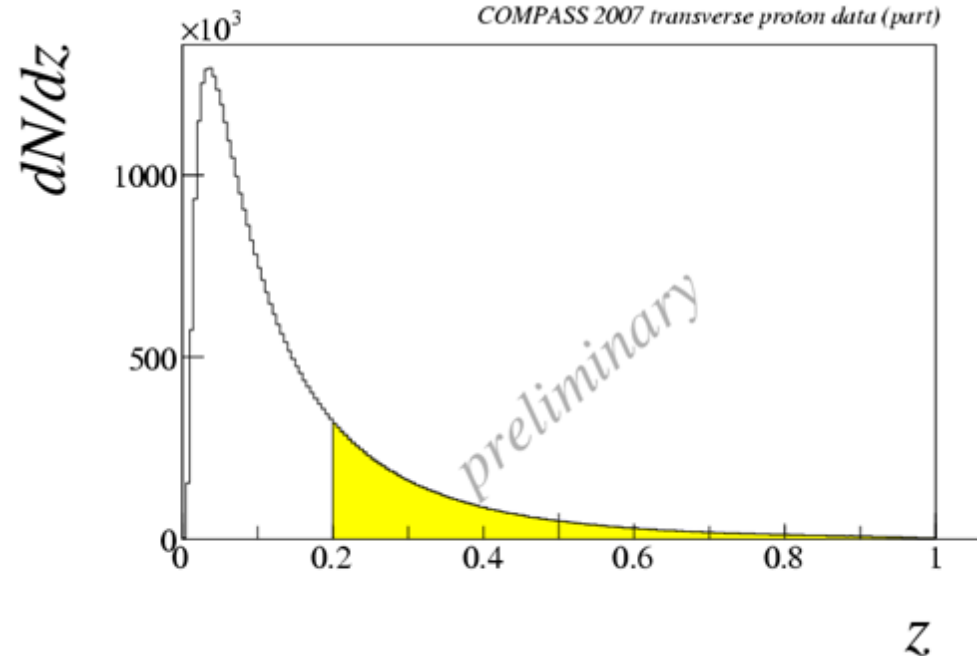
COMPASS 2007 transverse proton data (part)



COMPASS 2007 transverse proton data (part)



COMPASS 2007 transverse proton data (part)



results

SIDIS cross-section

18 structure functions

$$\begin{aligned}
 \frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = & \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right. \\
 & + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \\
 & + S_{\parallel} \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[\sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right] \\
 & + |S_{\perp}| \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\
 & + \left. \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \\
 & + |S_{\perp}| \lambda_e \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\
 & \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \left. \right\},
 \end{aligned}$$

3 modulations
with **unpol** target

3 modulations
with **L pol** target

8 modulations
(4 LO)
with **T pol** target

$$\gamma = \frac{2Mx}{Q}$$

$$\varepsilon = \frac{1 - y - \frac{1}{4}\gamma^2 y^2}{1 - y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}$$

$\phi_h (S)$ hadron (nucleon spin)
azimuthal angle in GNS

The Structure of the Nucleon
















three distribution functions are necessary to describe the quark structure of the nucleon at LO in the collinear case

taking into account the quark intrinsic transverse momentum k_T ,
at leading order 8 PDFs are needed for a full description

“TMDs”

nucleon polarisation

quark polarisation

	U	L	T	
U	f_1  <i>number density</i> q		f_{1T}^\perp  - 	$\Delta_0^T q$ <i>Sivers function</i>
L		g_1  -  <i>helicity</i> Δq	g_{1T}  - 	
T	h_1^\perp  - 	h_{1L}^\perp  - 	h_1  -  <i>transversity</i> h_{1T}^\perp  - 	$\Delta_T q$

SIDIS gives access to all of them

SIDIS cross-section

18 structure functions

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right.$$

$$+ \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h}$$

$$+ S_{\parallel} \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[\sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right]$$

$$+ |S_{\perp}| \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right.$$

$$+ \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)}$$

$$+ \left. \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \right.$$

$$+ |S_{\perp}| \lambda_e \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right.$$

$$\left. \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\},$$

3 modulations
with **unpol** target

3 modulations
with **L pol** target

8 modulations
(4 LO)
with **T pol** target

all measured
at **COMPASS**

$$\gamma = \frac{2Mx}{Q}$$

$$\varepsilon = \frac{1 - y - \frac{1}{4}\gamma^2 y^2}{1 - y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}$$

$\phi_h(S)$ hadron (nucleon spin)
azimuthal angle in GNS

SIDIS cross-section: unpolarised target

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right. \\ \left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \right\} + \dots$$

twist3

3 independent azimuthal modulations

Boer-Mulders DF

Cahn effect

$$F_{UU}^{\cos\phi_h} = \frac{2M}{Q} C \left[-\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} \left(xh H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{D}^\perp}{z} \right) - \frac{\hat{h} \cdot \mathbf{p}_T}{M} \left(x f^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{H}}{z} \right) \right]$$

$$xh = x\tilde{h} + \frac{p_T^2}{M^2} h_1^\perp$$

$$x f^\perp = x\tilde{f}^\perp + f_1 \quad F_{UU}^{\cos\phi_h} \approx \frac{2M}{Q} C \left[-\frac{\hat{h} \cdot \mathbf{p}_T}{M} f_1 D_1 \right]$$

$$F_{UU}^{\cos 2\phi_h} = C \left[-\frac{2(\hat{h} \cdot \mathbf{k}_T)(\hat{h} \cdot \mathbf{p}_T) - k_T \cdot \mathbf{p}_T}{M M_h} h_1^\perp H_1^\perp \right]$$

Boer-Mulders DF x Collins FF
+ Cahn effect (twist 4, $1/Q^2$)

SIDIS cross-section: unpolarised target

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right. \\ \left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \right. + \dots$$

measurable from the data collected with polarised target

- both target orientation configurations are used to cancel possible polarisation effects

to extract the asymmetries the azimuthal distributions have to be corrected by the apparatus acceptance

→ MC simulations

the final azimuthal distributions are fitted with the function:

$$N_{\text{corr}}(\phi_h) = N_0 (1 + A_{\sin\phi_h} \sin\phi_h + A_{\cos\phi_h} \cos\phi_h + A_{\cos 2\phi_h} \cos 2\phi_h)$$

preliminary results from data collected with L and T polarisation of the ${}^6\text{LiD}$ (~d) target



summary of results for d

(Transversity 2008)

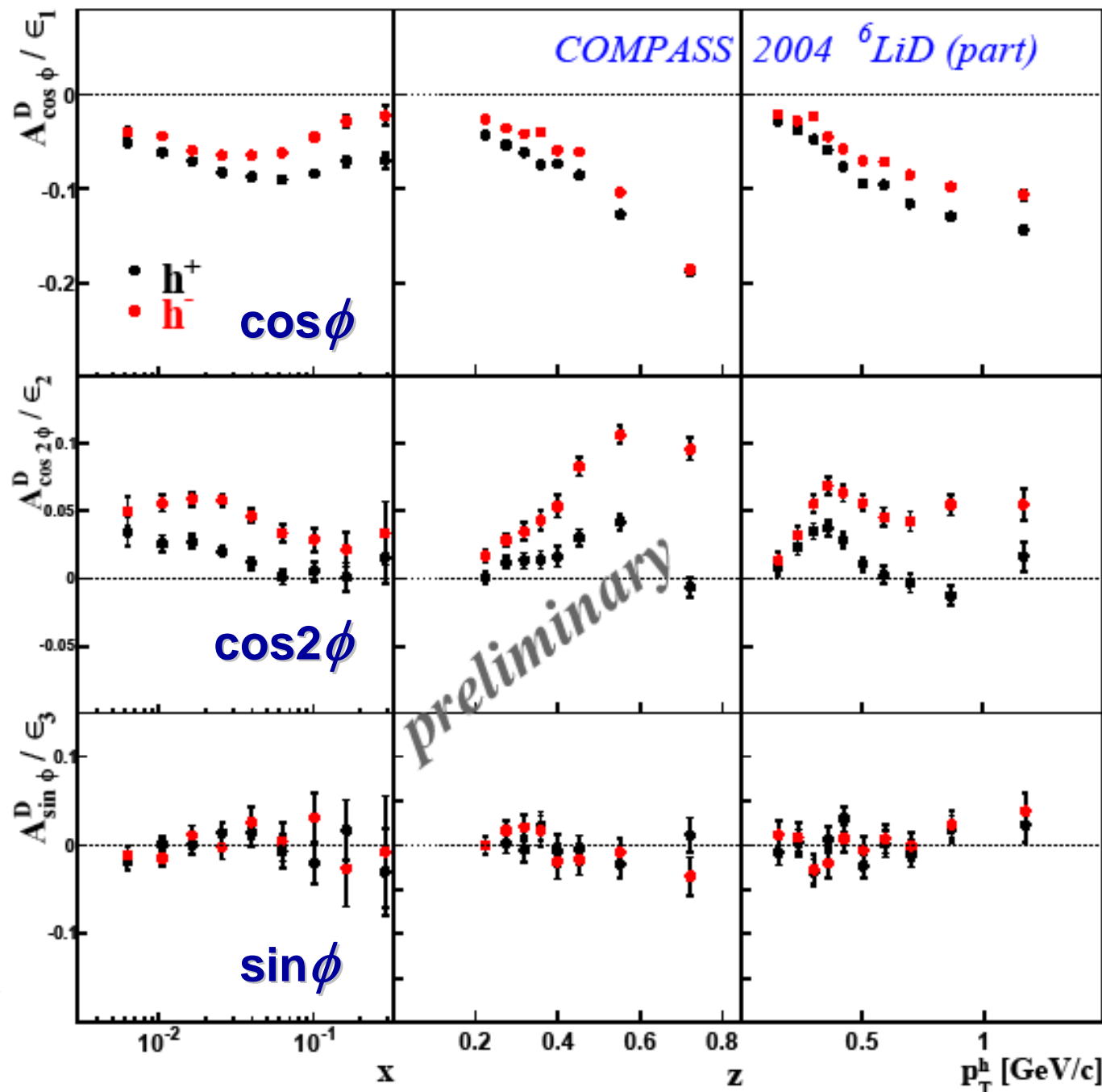
clear signal,
different for h^+ and h^- :
 non negligible contribution
 of BM term, different $\langle k_T \rangle$
 for u and d quarks...

clear signal,
different for h^+ and h^- :
 important contribution
 of BM term

error bars:
 statistical errors only

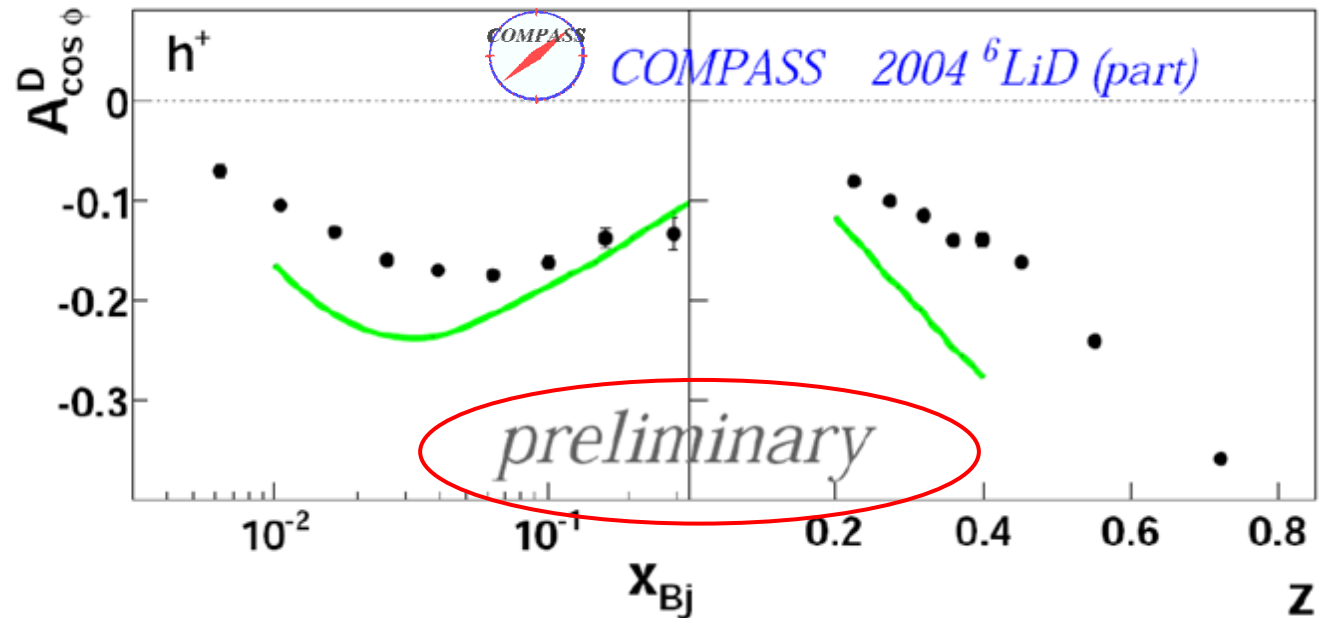
$$\varepsilon_c = \frac{2(2-y)\sqrt{1-y}}{1+(1-y)^2} \quad \varepsilon_{c2} = \frac{2(2-y)}{1+(1-y)^2} \quad \varepsilon_s = \frac{2y\sqrt{1-y}}{1+(1-y)^2}$$

Anna Martin



comparison with theory

$\cos\phi$ amplitude



final results soon
presently, indication
that the $\cos\phi$
amplitude will
somewhat change



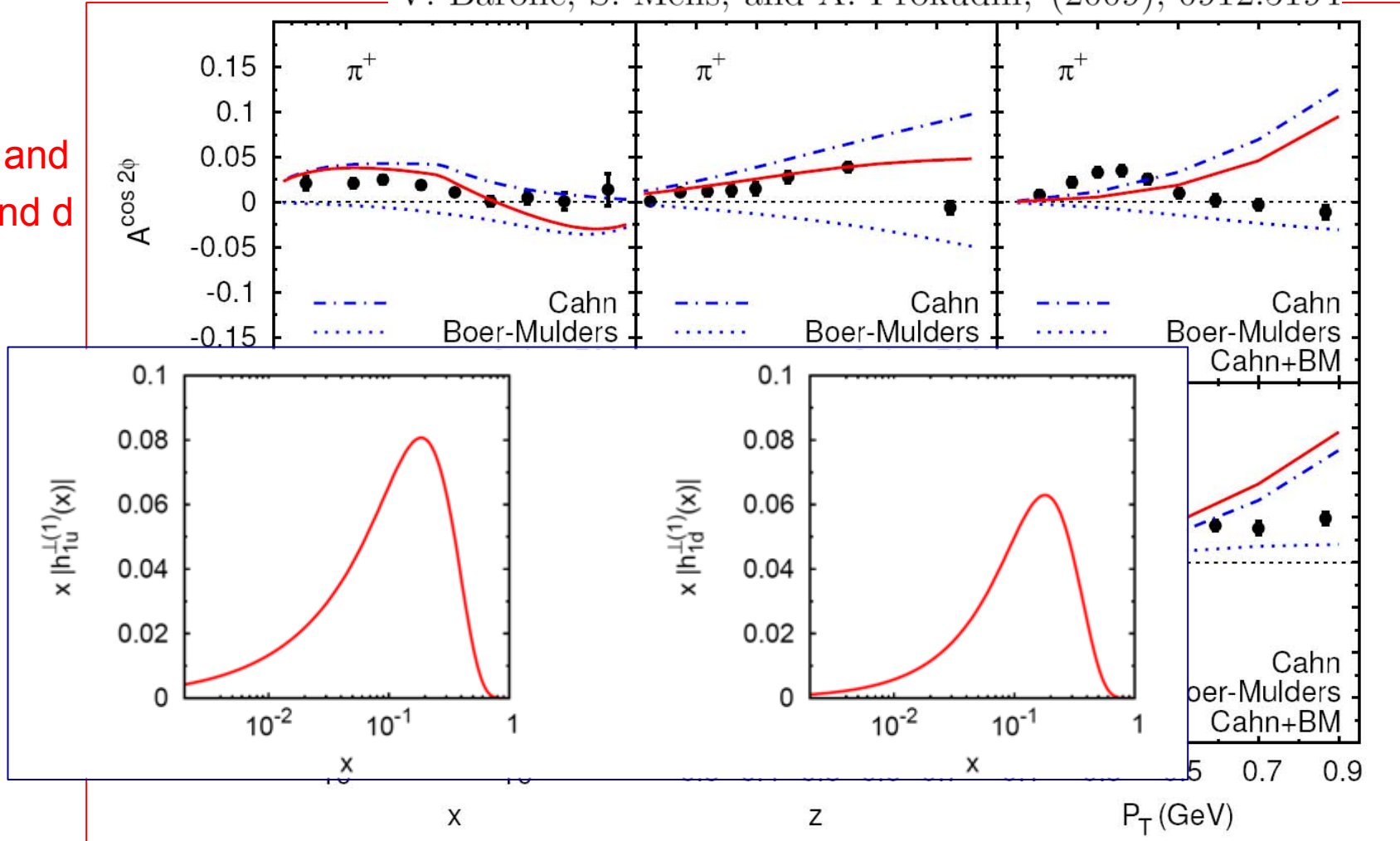
M. Anselmino, M. Boglione, A. Prokudin, C. Türk
Eur. Phys. J. A 31, 373-381 (2007)
does not include Boer – Mulders contribution

comparison with theory

cos 2φ amplitude

V. Barone, S. Melis, and A. Prokudin, (2009), 0912.5194

fit to
COMPASS d and
HERMES p and d
data
→ S. Melis



$$H_1^{\perp q}(z, p_T^2) = \rho_q^C(z) \eta^C(p_T) D_1(z, p_T^2) \quad \text{M. Anselmino et al., Nucl. Phys. Proc. Suppl. } \mathbf{191}, 98 \text{ (2009), 0812.4366}$$

$$h_1^{\perp q} = \lambda_q f_{1T}^{\perp q} \quad \text{M. Anselmino et al., Eur. Phys. J. } \mathbf{A39}, 89 \text{ (2009), 0805.2677}$$

$$\langle k_T^2 \rangle = 0.25 \text{ GeV}^2, \quad \langle p_T^2 \rangle = 0.20 \text{ GeV}^2 \quad \text{M. Anselmino et al., Phys. Rev. } \mathbf{D71}, 074006 \text{ (2005)}$$



unpolarised azimuthal Asymmetries

- **deuteron**: final results soon
- **proton**: COMPASS II proposal

longitudinal Spin Asymmetries

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \dots$$

$$+ S_{\parallel} \lambda_e \left[\sqrt{1 - \varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1 - \varepsilon)} \cos \phi_h F_{LL}^{\cos \phi_h} \right]$$

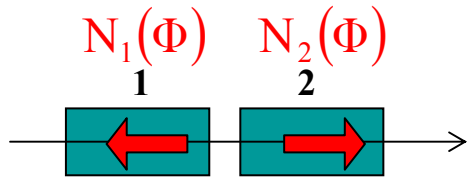
$$+ S_{\parallel} \left[\sqrt{2\varepsilon(1 + \varepsilon)} \sin \phi_h F_{UL}^{\sin \phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + \dots$$

$$\frac{d\sigma^{\leftarrow\Rightarrow} - d\sigma^{\leftarrow\Leftarrow}}{|S_{\parallel}|(d\sigma^{\leftarrow\Rightarrow} + d\sigma^{\leftarrow\Leftarrow})}$$

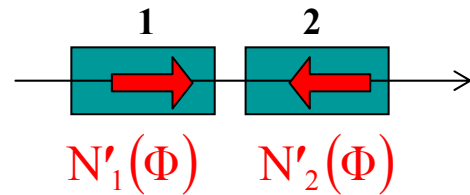
extraction of the L Spin Asymmetries



“standard” COMPASS method of the “ratio products”



$$F(\phi_h) = \frac{N_1(\phi_h)}{N'_1(\phi_h)} \cdot \frac{N'_2(\phi_h)}{N_2(\phi_h)}$$



$$a(\phi_h) = \frac{1}{S_{\parallel,1} + S_{\parallel,2} + S'_{\parallel,1} + S'_{\parallel,2}} \cdot \{F(\phi_h) - 1\} \cong \frac{\sigma_L(\phi_h)}{\sigma_U(\phi_h)}$$

$$a(\phi_h) = a^{\text{const}} + a^{\sin \phi_h} \sin \phi_h + a^{\sin 2 \phi_h} \sin 2 \phi_h + a^{\sin 3 \phi_h} \sin 3 \phi_h + a^{\cos \phi_h} \cos \phi_h$$

$$\downarrow$$

$$F_{LL}$$

helicity $g_{1L}D_1$

$$\downarrow$$

$$F_{UL}^{\sin \phi_h}$$

(twist 3)

$$\downarrow$$

$$F_{UL}^{\sin 2 \phi_h}$$

worm-gear $h_{1L}^\perp H_1^\perp$



pretzelosity $h_{1T}^\perp H_1^\perp$

$$F_{UT}^{\sin(3\phi_h - \phi_S)}$$

$$\downarrow$$

$$F_{LL}^{\cos \phi_h}$$

(twist 3)

$$\sin \theta_\gamma \sim \frac{M}{Q}$$

Sivers $f_{1T}^\perp D_1$

$$F_{UT,T}^{\sin(\phi_h - \phi_S)}$$

transversity $h_1 H_1^\perp$

$$F_{UT}^{\sin(\phi_h + \phi_S)}$$

worm-gear $g_{1T}D_1$

$$F_{LT}^{\cos(\phi_h - \phi_S)}$$

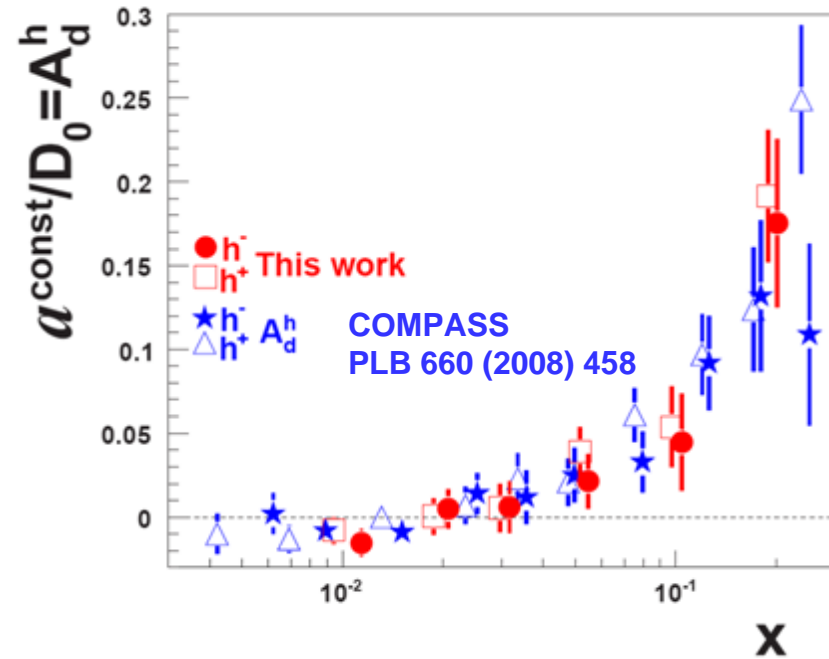
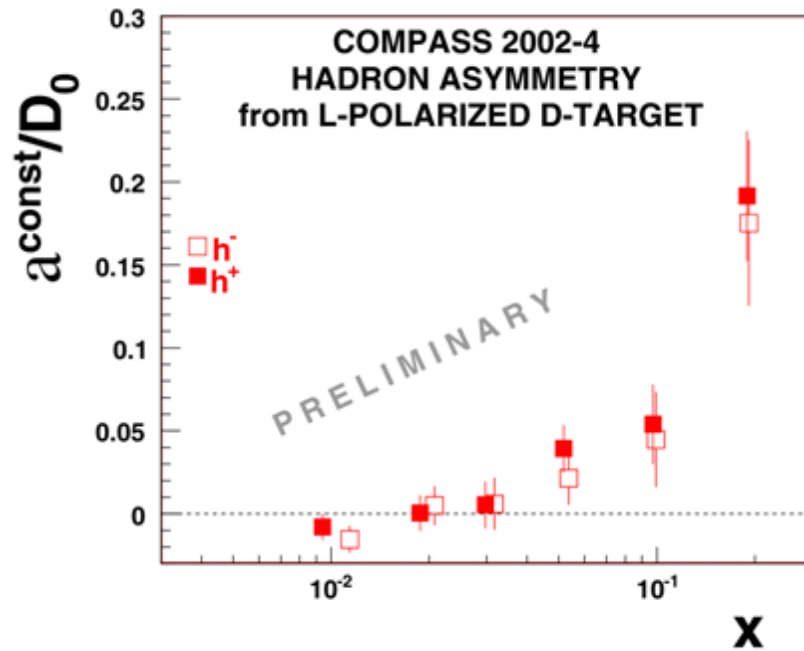
preliminary results from the 2002-2004 d data (Dubna-Spin 2009)

deuteron results

a^{const}

F_{LL}
helicity $g_{1L}D_1$

$$\frac{a^{\text{const}}(x)}{D_0} = A_d^h(x) \quad D_0 = |P_\mu| \sqrt{1-\epsilon^2}$$



good agreement \rightarrow internal consistency of the COMPASS results

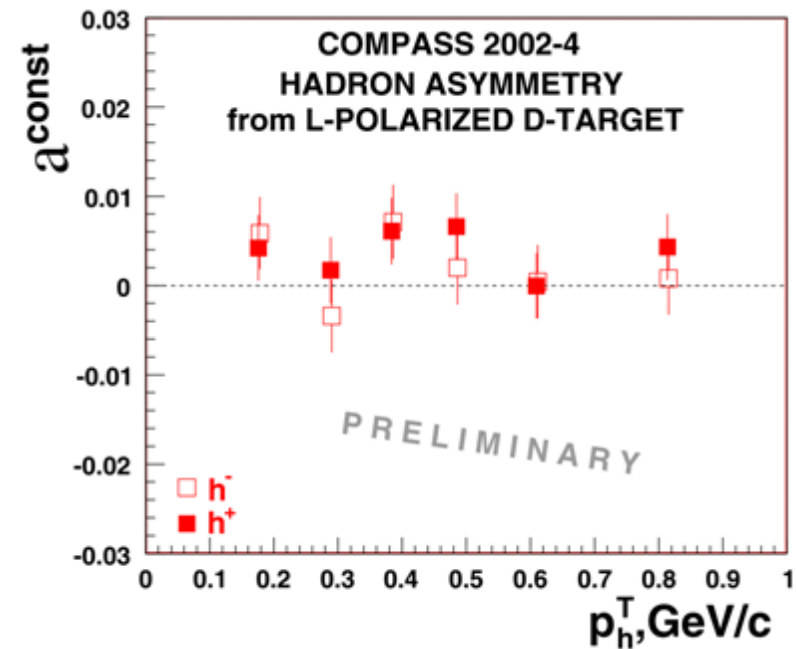
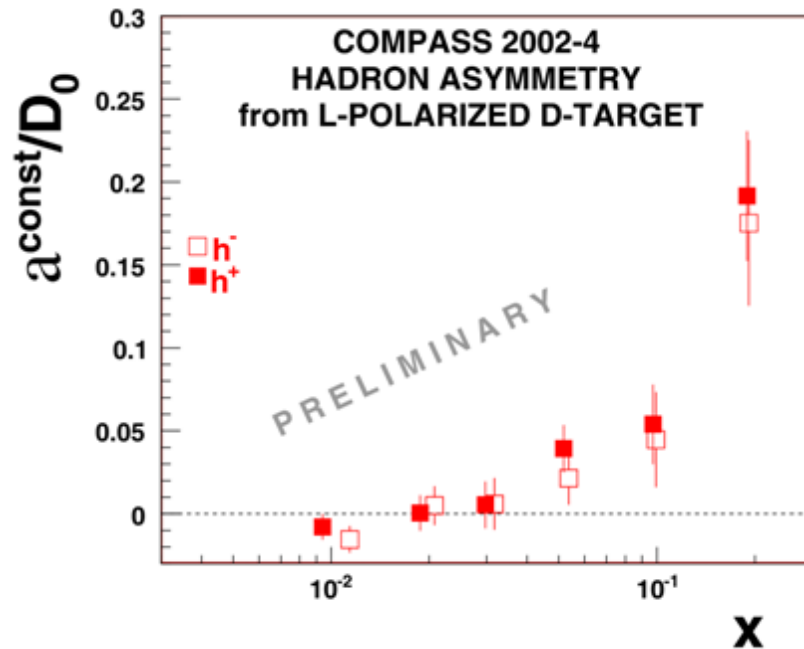


deuteron results

a^{const}

F_{LL}
helicity $g_{1L}D_1$

$$\frac{a^{\text{const}}(x)}{D_0} = A_d^h(x) \quad D_0 = |P_\mu| \sqrt{1-\epsilon^2}$$



good agreement \rightarrow internal consistency of the COMPASS results

no strong z or p_h^T dependence

deuteron results

$$a^{\sin\phi_h}$$

$$\overline{F_{UL}^{\sin\phi_h}}$$

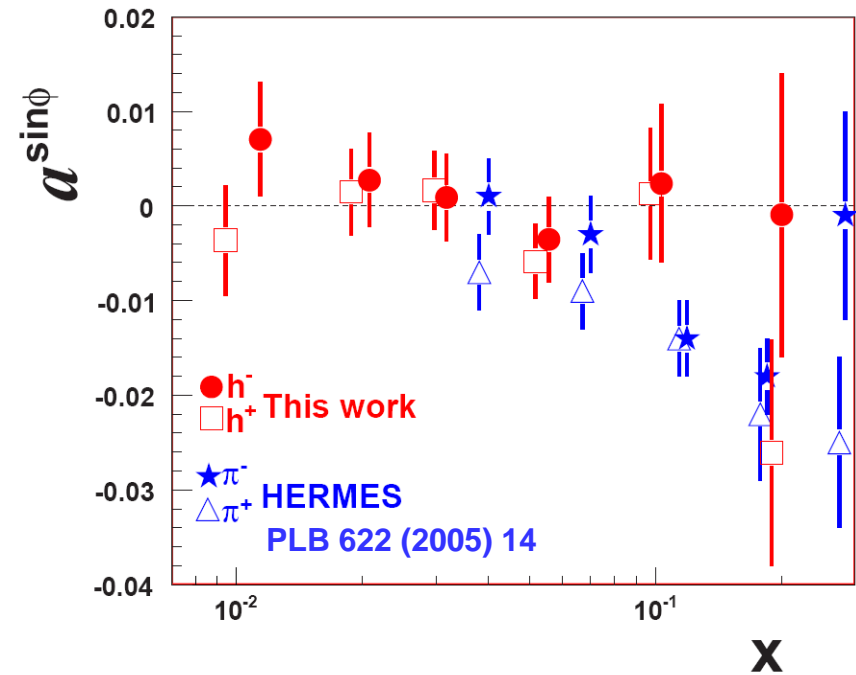
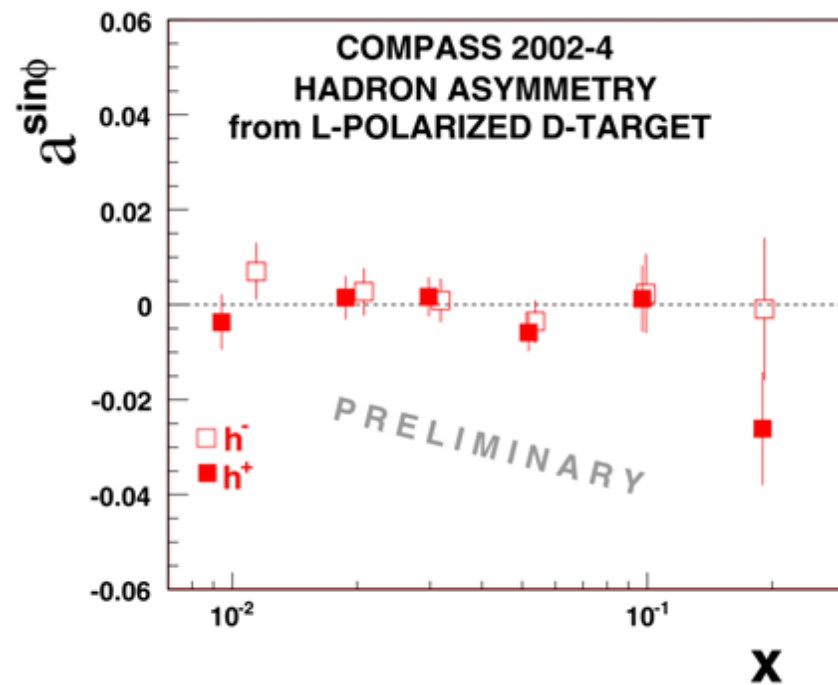
(twist 3)

$$F_{UT,T}^{\sin(\phi_h - \phi_S)}$$

Sivers $f_{1T}^\perp D_1$

$$F_{UT}^{\sin(\phi_h + \phi_S)}$$

transversity $h_1 H_1^\perp$



no evident x dependence

different kinematics

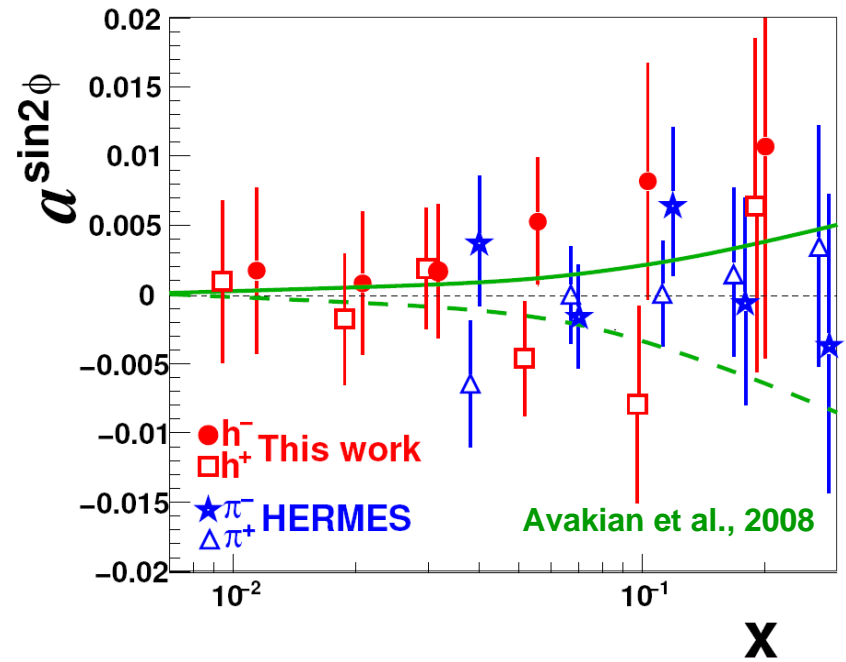
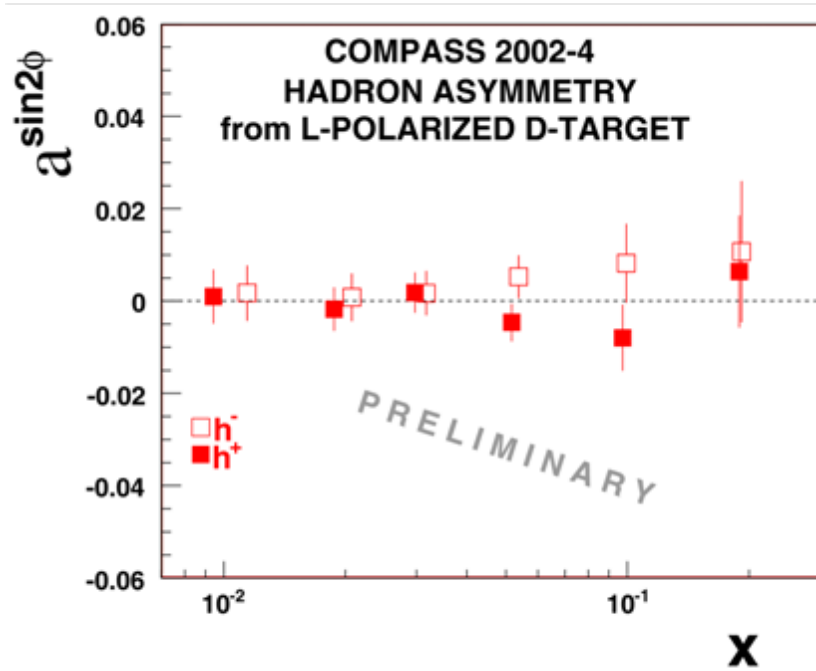


deuteron results

$$a^{\sin 2\phi_h}$$

$$F_{UL}^{\sin 2\phi_h}$$

worm-gear $h_{1L}^\perp H_1^\perp$



small, consistent with zero within the errors



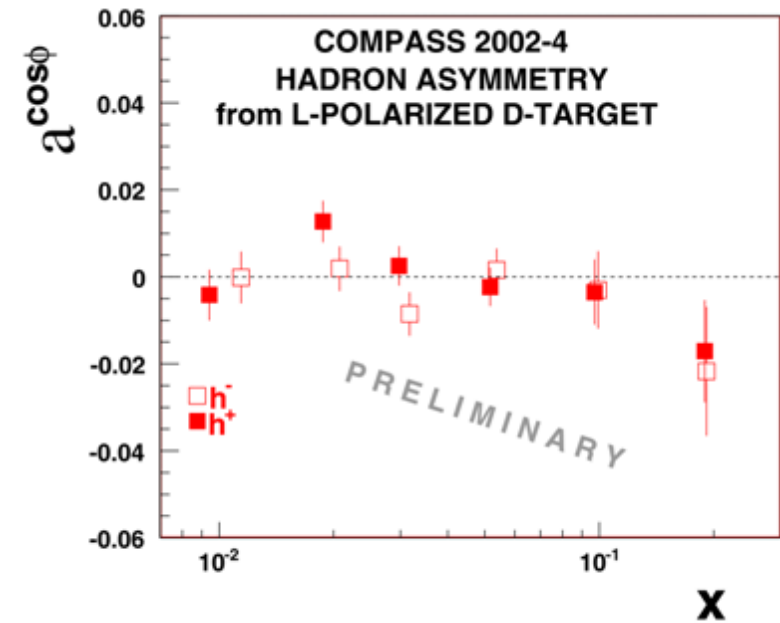
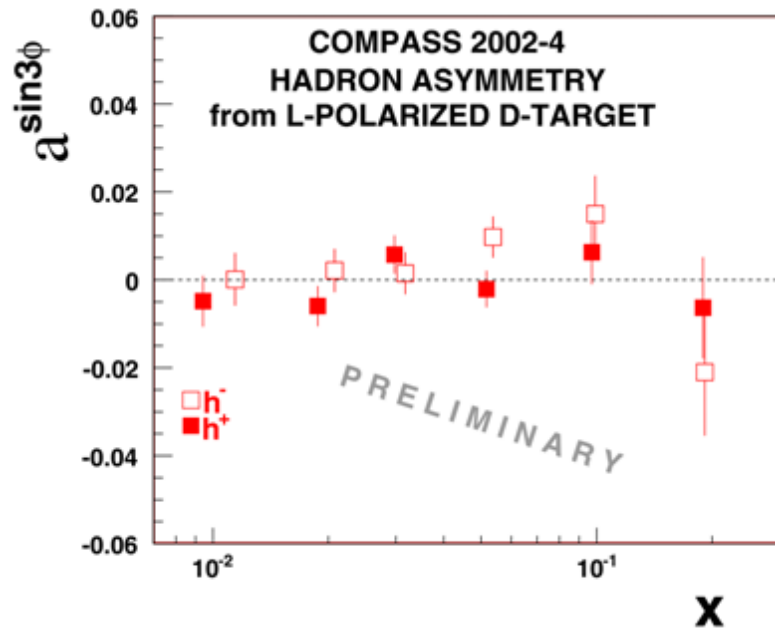
deuteron results

$$a^{\sin 3\phi_h} \quad F_{UT}^{\sin(3\phi_h - \phi_S)}$$

pretzelocity $h_{1T}^\perp H_1^\perp$

$$a^{\cos\phi_h} \quad F_{LL}^{\cos\phi_h} \quad F_{LT}^{\cos(\phi_h - \phi_S)}$$

(twist 3) worm-gear $g_{1T} D_1$



compatible with zero, in agreement with the COMPASS measurements with the T polarised d target

next: extract the same asymmetries from the 2007 p data



transverse Spin Asymmetries

8 modulations
(4 LO)

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \dots$$

Collins asymmetry

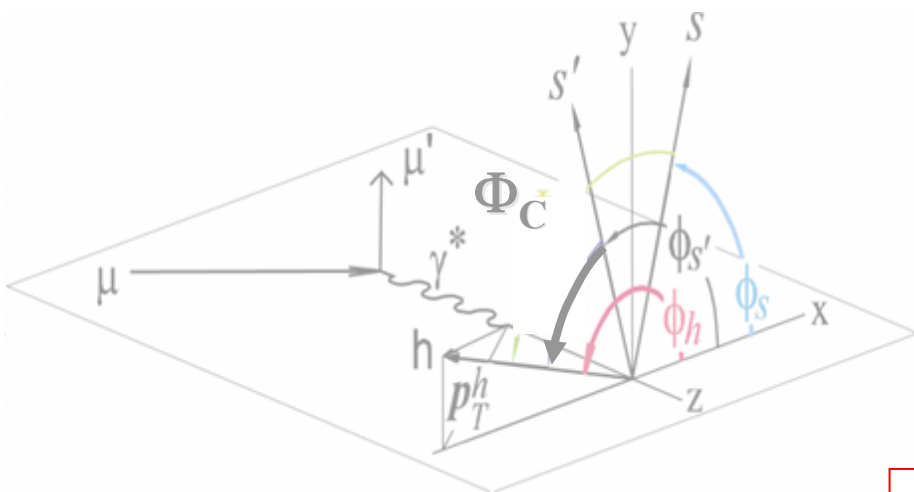
$$\begin{aligned}
 & + |\mathbf{S}_\perp| \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\
 & \left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \\
 & + |\mathbf{S}_\perp| \lambda_e \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\
 & \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \Bigg\},
 \end{aligned}$$

Collins asymmetry

if transversity PDFs and Collins FFs different from zero

modulation in the azimuthal distribution of the final state hadrons

$$N_h^\pm(\Phi_C) = N_h^0 \cdot \left[1 \pm P_T \cdot D_{NN} \cdot A_{Coll} \cdot \sin \Phi_C \right]$$



$$\Phi_C = \phi_h + \phi_S - \pi$$



ϕ_h azimuthal angle of the hadron,

ϕ_S azimuthal angle of the spin of the nucleon

transversity

“Collins FF”

$$A_{Coll} \approx \frac{\sum_q e_q^2 \Delta_T q \otimes \Delta_T^0 D_q^h}{\sum_q e_q^2 q \otimes D_q^h}$$

first measured by HERMES (proton target) and COMPASS (deuteron target)

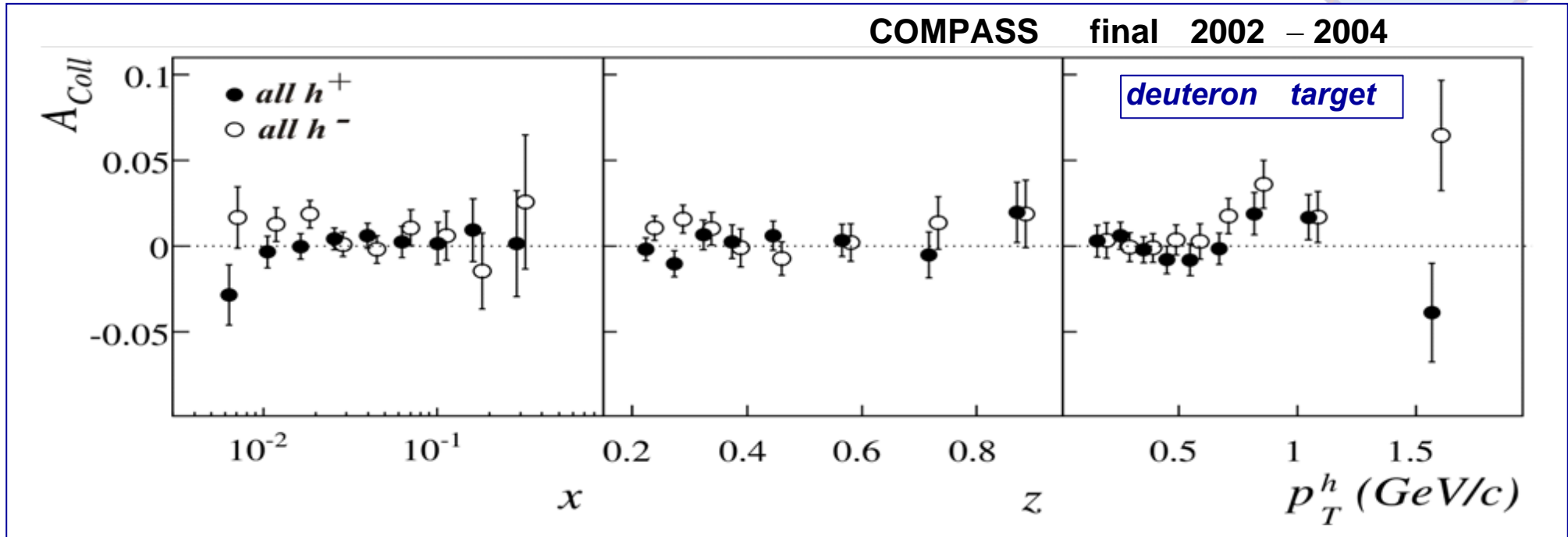
different from zero

compatible with zero

Collins asymmetry



COMPASS d results: *PRL 94 (2005) 202002, NPB 765 (2007) 31, PLB 673 (2009) 127*



understood as u – d cancellation

the COMPASS d, HERMES p, and BELLE $e^+e^- \rightarrow \pi^+\pi^- X$ data

are well described in global fits [M. Anselmino et al.]

→ first extractions of the Collins FFs and the transversity PDFs, and tensor charge

energy dependence?

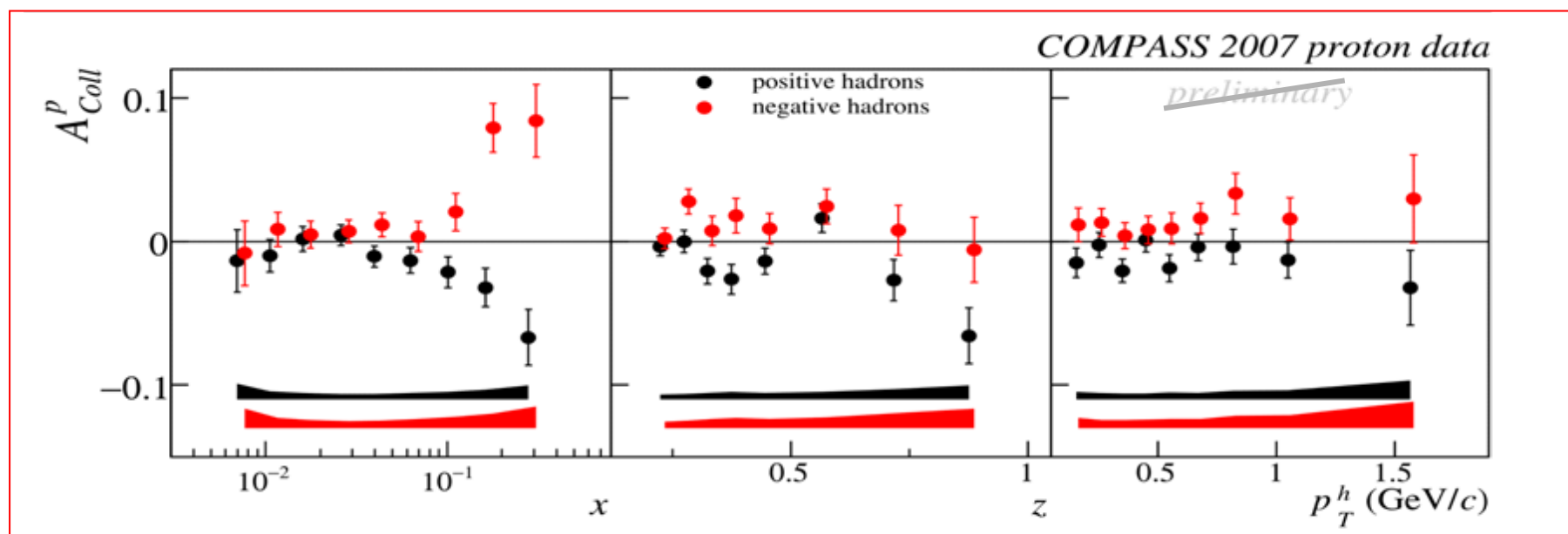
Collins asymmetry - proton



the analysis of the 2007 proton run is over

the paper has been submitted CERN-PH-EP-2010-013, May 2010, arXiv:1005.5609 [hep-ex]

final results very much the same as presented at DIS 2009



- at small x , the asymmetries are **compatible with zero**
- **large signal in the valence region** of opposite sign for positive and negative hadrons

same sign and ~ strength as HERMES: not obvious!

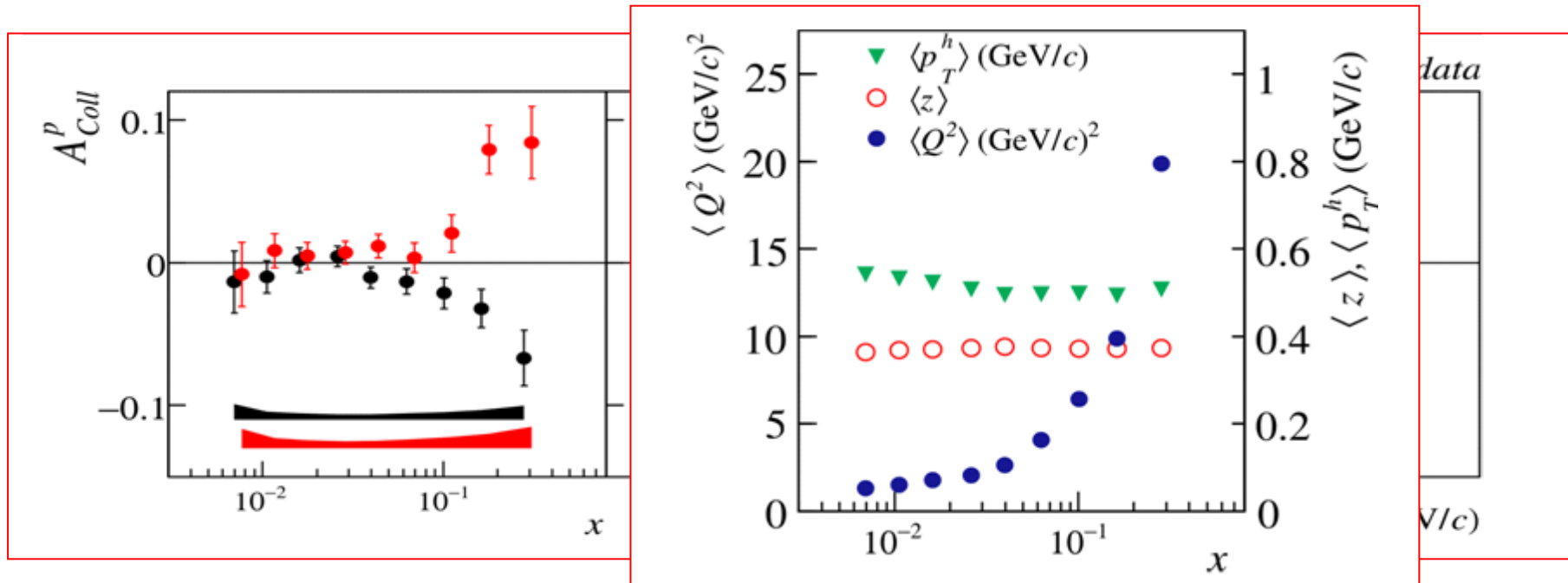
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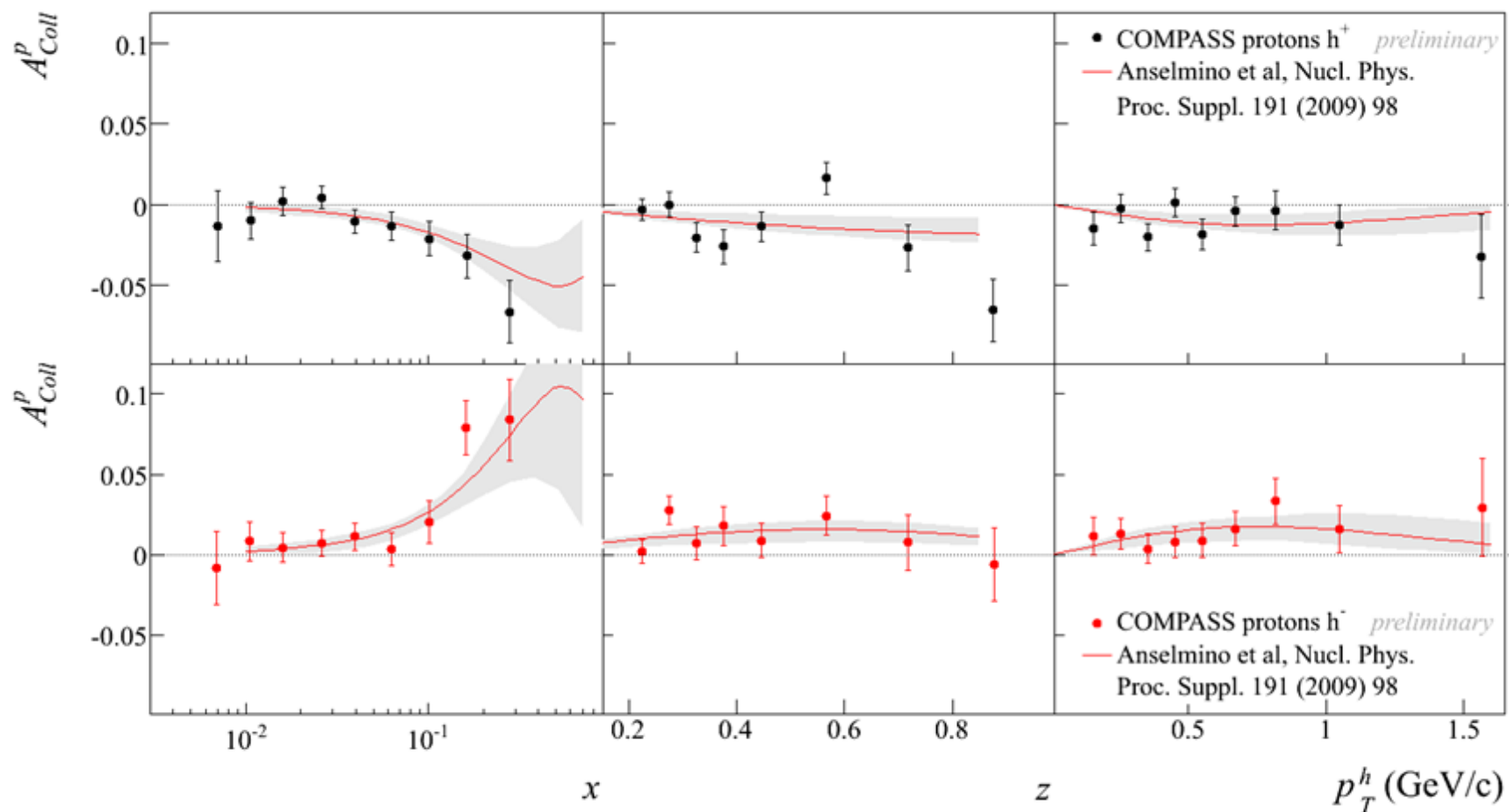


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Collins asymmetry - proton

comparison with predictions from fit to the
HERMES proton, COMPASS deuteron, BELLE data



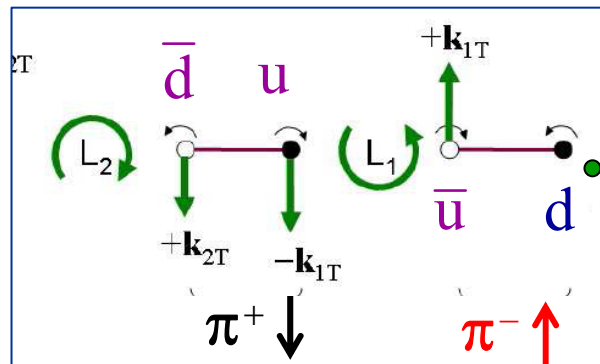
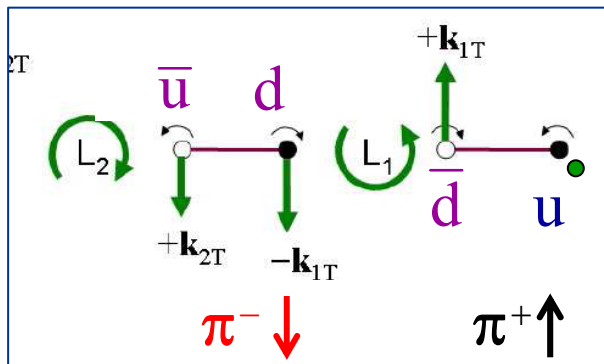
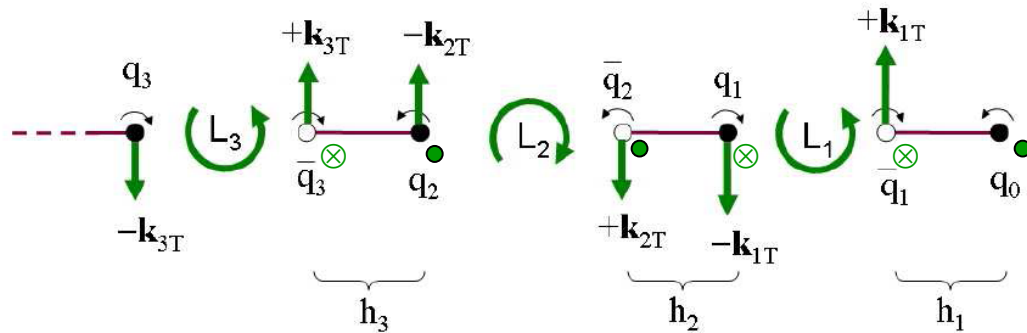
our data support the assumption of a weak Q^2 dependence
in the present energy range

Collins asymmetry - proton

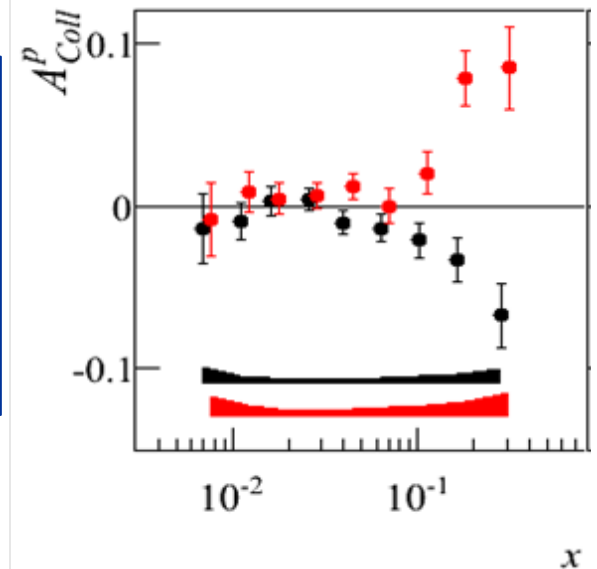
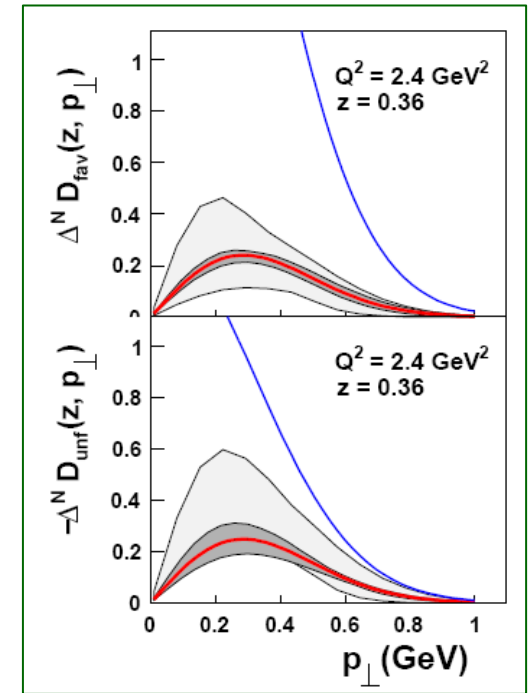
SIGN in agreement with the

“recursive fragmentation model with quark spin”

[X. Artru, arXiv:1001.1061] 3P_0



Collins FFs: favored ~ - unfavored
 transversity PDFs: substantially different for u and d



Transversity PDF

can be measured in SIDIS off transversely polarised targets via
“quark polarimetry”

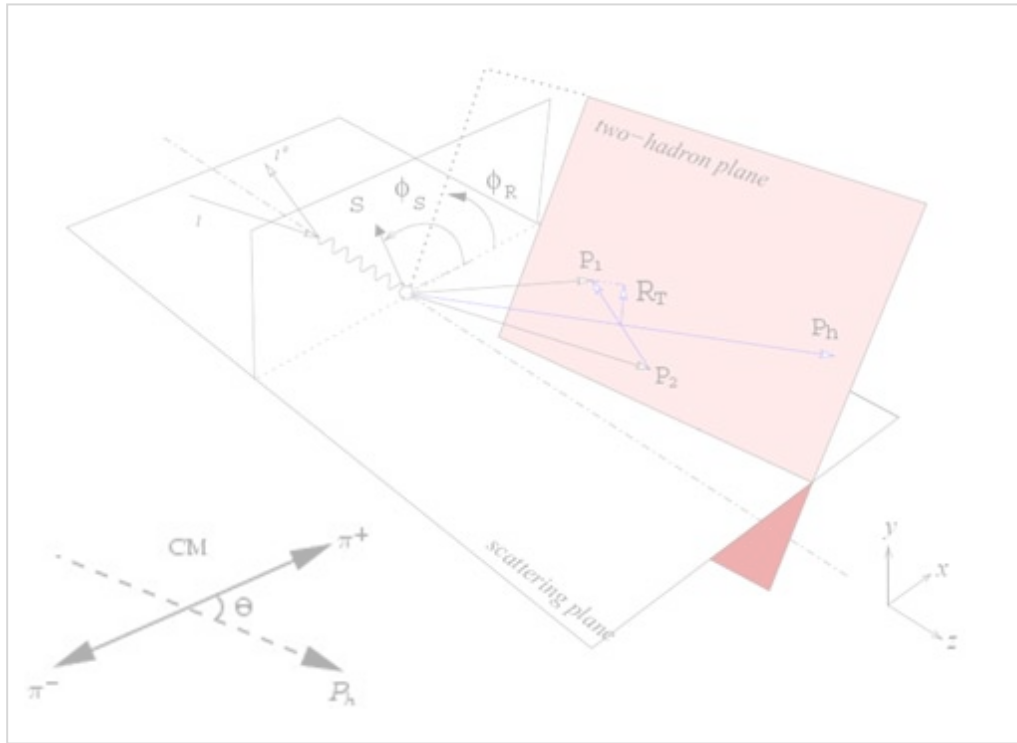
$l N^\uparrow \rightarrow l' h X$ “Collins” asymmetry
“Collins” Fragmentation Function

$l N^\uparrow \rightarrow l' h h X$ “two-hadron” asymmetry
“Interference” Fragmentation Function

$l N^\uparrow \rightarrow l' \Lambda X$ Λ polarisation
Fragmentation Function of $q^\uparrow \rightarrow \Lambda$

all explored in COMPASS

Two Hadron Asymmetry



azimuthal asymmetry in

$$\phi_{RS} = \phi_{R\perp} - \phi_S,$$

$\phi_{R\perp}$ is the azimuthal angle of the plane defined by the two hadrons

$$R = (z_1 p_2 - z_2 p_1) / (z_1 + z_2)$$

$$N^\pm(\Phi_{RS}) = N^0 \cdot \{ 1 \pm A \cdot \sin \Phi_{RS} \}$$

Interference Fragmentation Function

BELLE

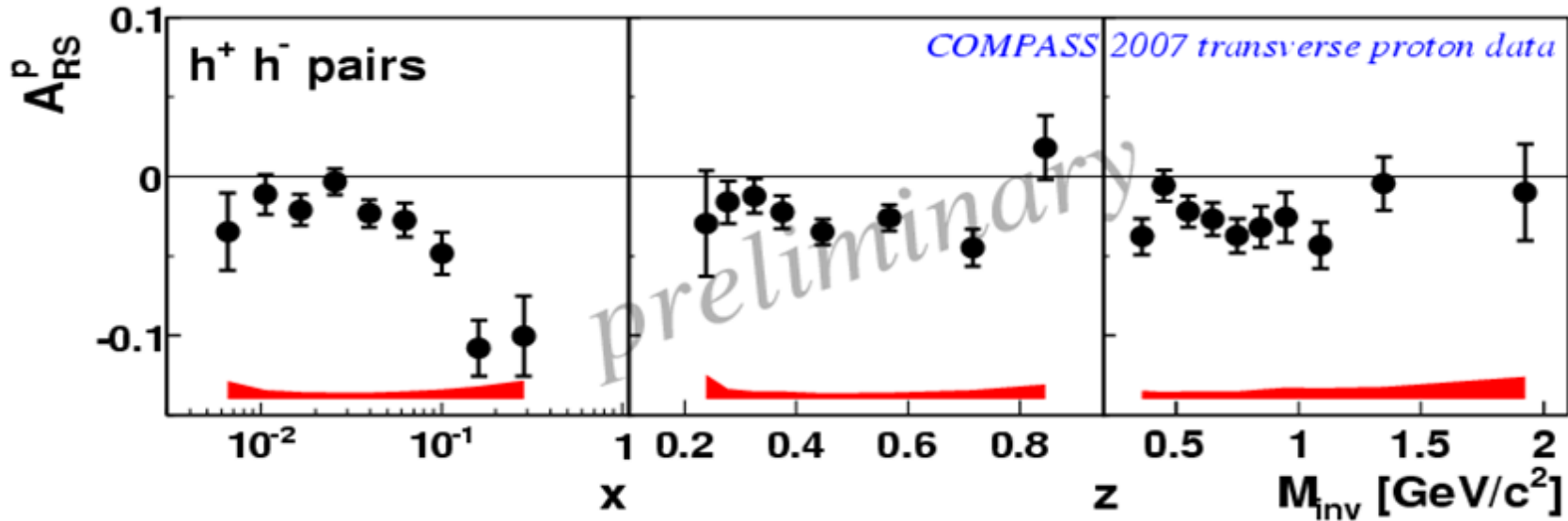
$$A_{RS} = \frac{1}{f \cdot P_T \cdot D_{NN}} \cdot A = \frac{\sum_q e_q^2 \cdot \Delta_T q(x) \cdot H_q^{2h}(z, M_h^2)}{\sum_q e_q^2 \cdot q(x) \cdot D_q^{2h}(z, M_h^2)}$$

Two Hadron Asymmetry



deuteron: compatible with zero at all x , for all the combinations we have tested

proton preliminary results (DIS2009)



$x_F > 0.1$
 $z_{1,2} > 0.1$
 $Z = z_1 + z_2 < 0.9$
 $R_T > 0.07 GeV/c$

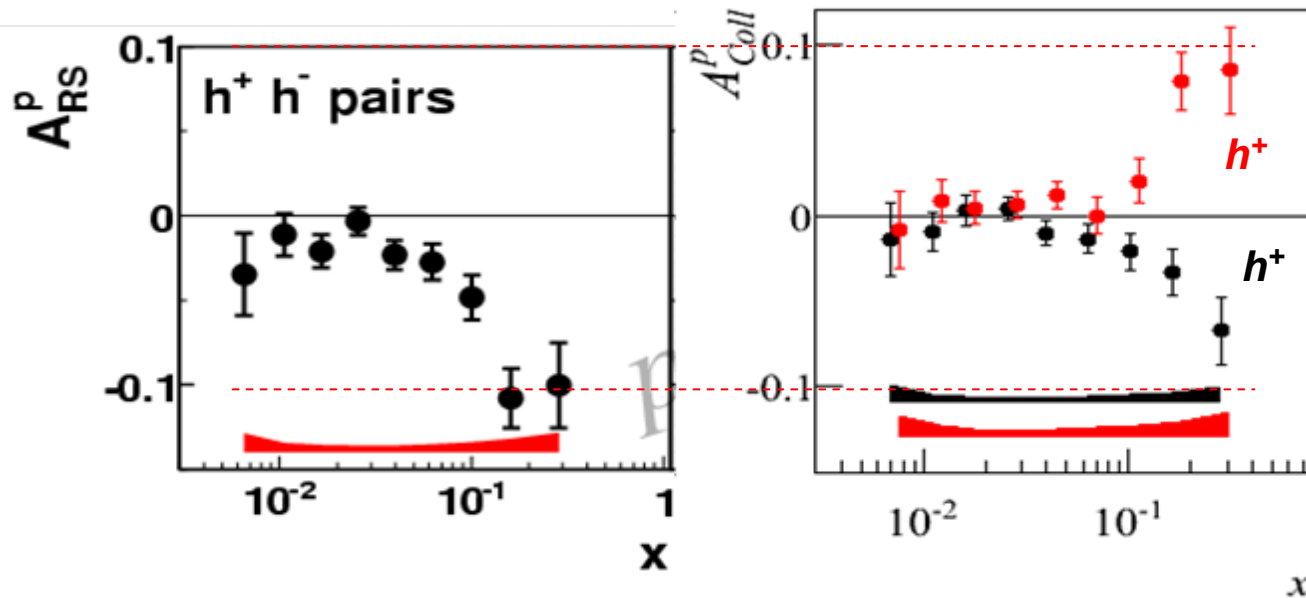
large signal in the valence region, no particular trend in z and M_{inv}

Two Hadron Asymmetry



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large signal in the valence region, no particular trend in z and M_{inv}
sign in agreement with the Collins asymmetry,
strength \sim larger than the Collins asymmetry

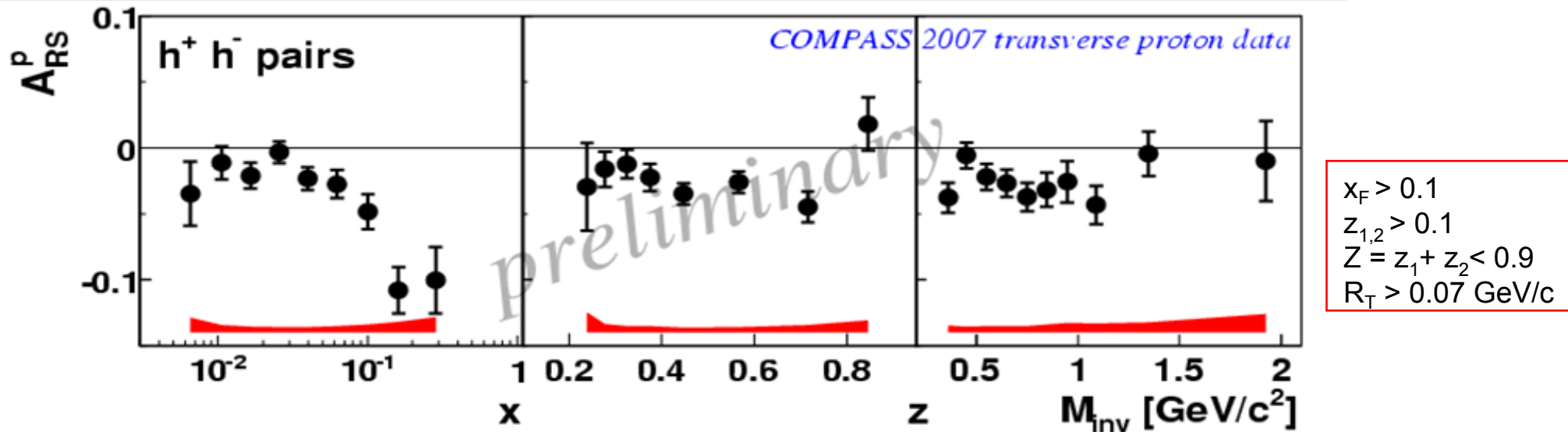
in qualitative agreement with the "recursive model" if $\Delta_T u \sim -\Delta_T d$

Two Hadron Asymmetry



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 sign in agreement with the Collins asymmetry,
 strength \sim larger than the Collins asymmetry

in qualitative agreement with the “recursive model” if $\Delta_T u \sim -\Delta_T d$

larger than measured by HERMES

difficult to describe both sets of results at the same time

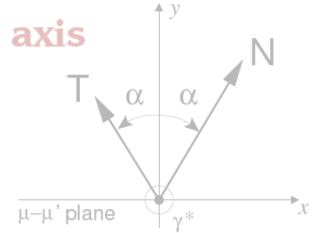
[Bacchetta et al., Mah et al.]

Λ polarisation



$$P_{T,exp}^\Lambda = f P_N D(y) \frac{\sum_q e_q^2 \Delta_{Tq}(x) \Delta_T D_{\Lambda/q}(z)}{\sum_q e_q^2 q(x) D_{\Lambda/q}(z)}$$

Λ polarization axis



2007 proton data

$p_T > 23$ MeV/c to exclude e^+e^- pairs

p and pion momenta > 1 GeV/c

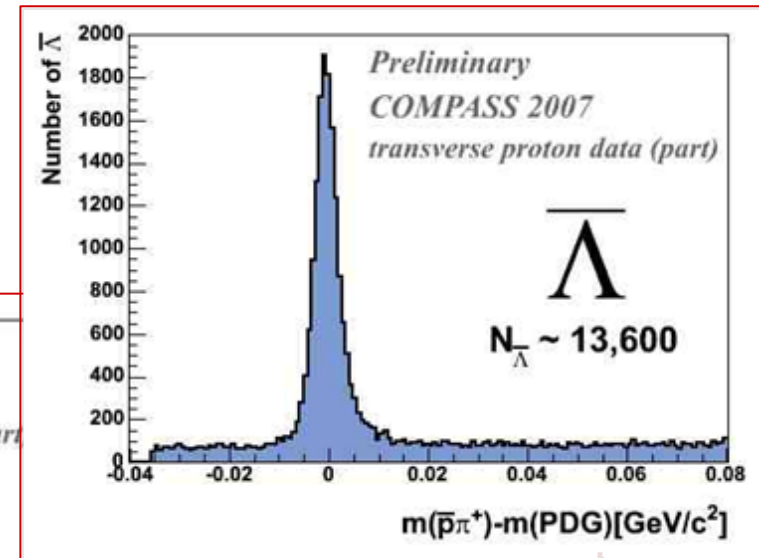
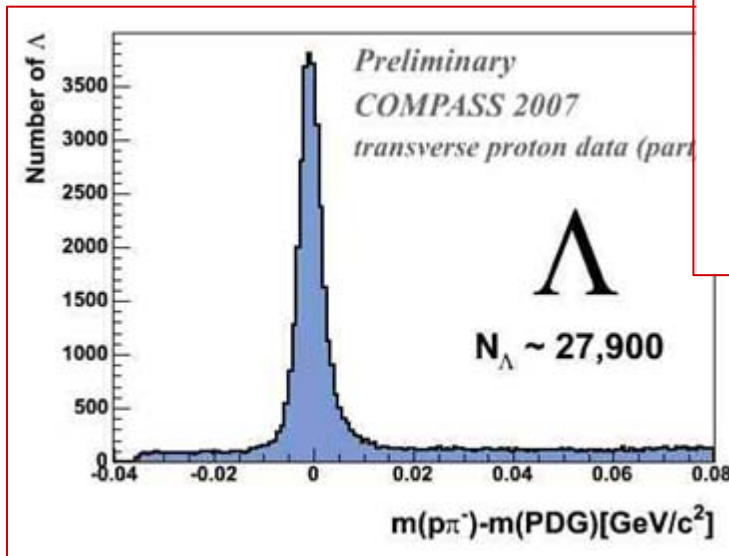
$Q^2 > 1$ (GeV/c)²

$0.1 < y < 0.9$

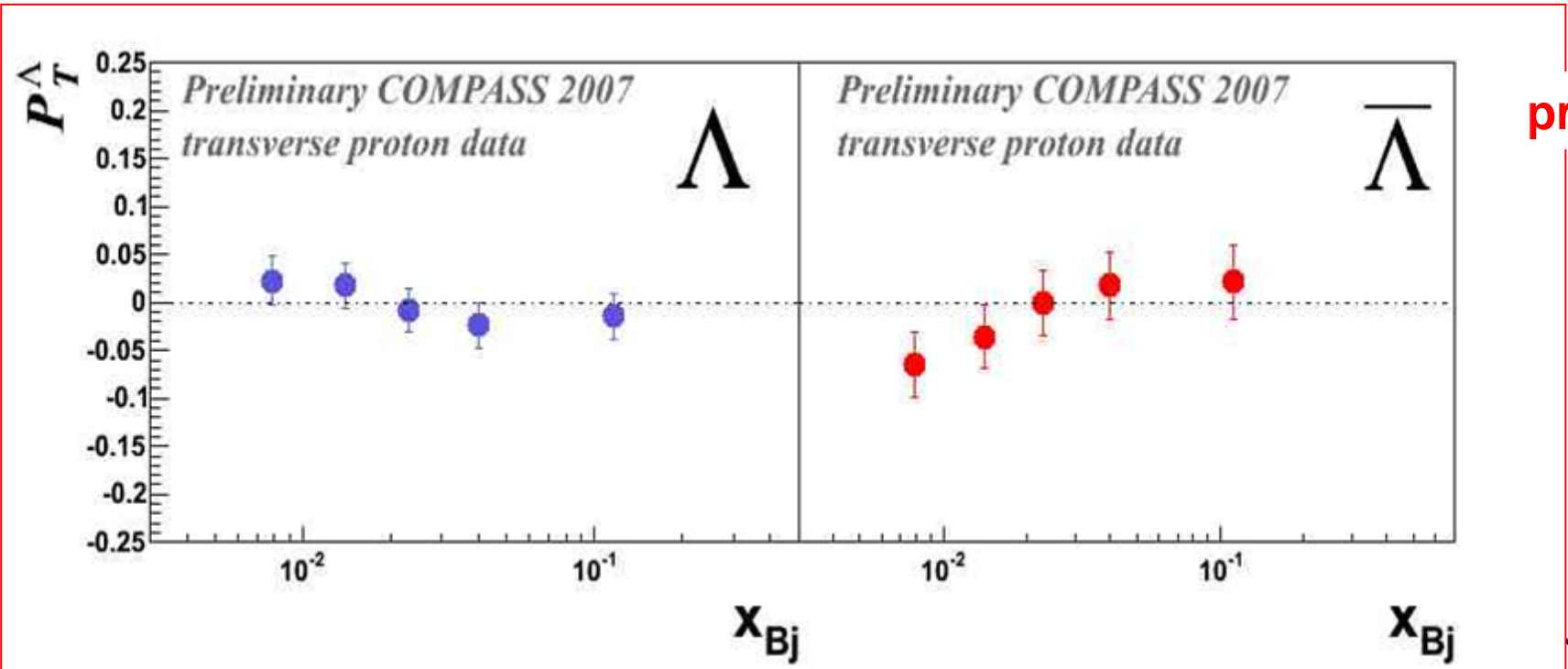
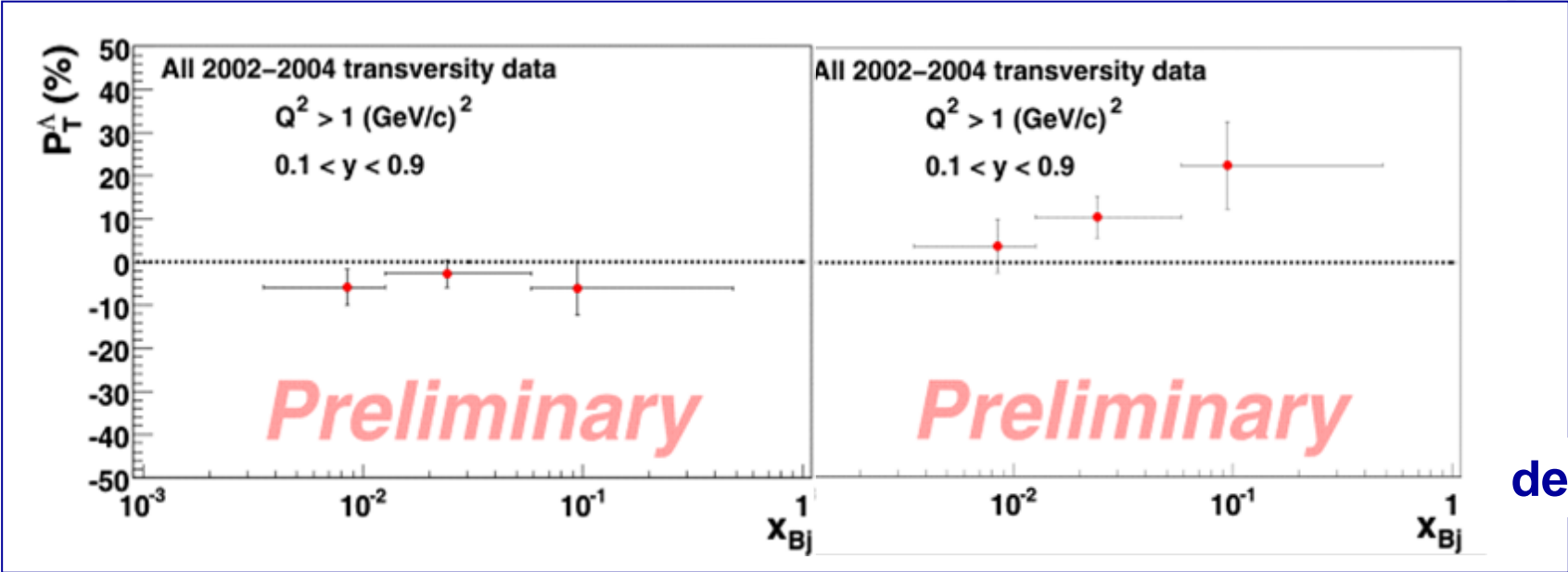
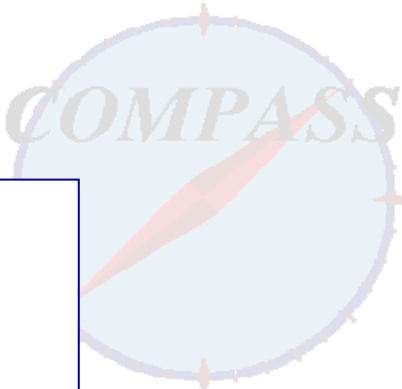
Use of RICH (2007 data)

Λ decay distance $D_\Lambda > 7 \sigma_D$

Collinearity < 10 mrad



Λ polarisation



transverse Spin Asymmetries

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \dots$$

Sivers asymmetry

$$+ |\mathbf{S}_\perp| \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right]$$

Collins asymmetry

$$+ \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)}$$


$$+ \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right]$$

$$+ |\mathbf{S}_\perp| \lambda_e \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right]$$

$$+ \left. \left[\sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\},$$

Sivers asymmetry

$$A_{Siv} \approx \frac{\sum_q e_q^2 f_{1T}^{\perp q} \otimes D_1^q}{\sum_q e_q^2 f_1 \otimes D_1^q}$$

- strong signal seen by HERMES for π^+ and K^+ on protons
- no signal seen by COMPASS on deuterons  interpreted as u - and d -quark cancellation (as for the Collins asymmetry)
- first extractions of the Sivers function from HERMES (and COMPASS) data
good description of the experimental results

no energy dependence expected

first COMPASS results on p

from part of the 2007 data presented at Transversity 2008:

compatible with zero

now the analysis of the 2007 data is over

new final results (DIS2010)

more statistics, further data taking periods

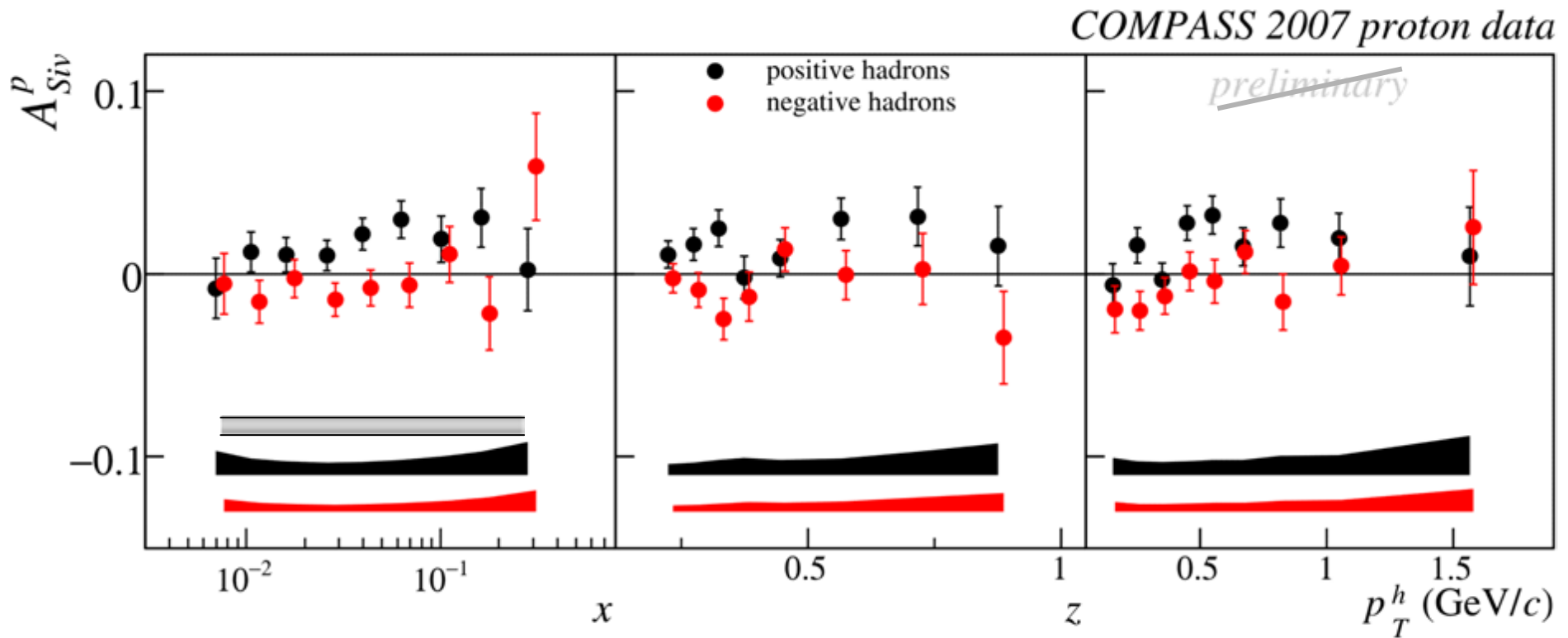
paper sent for publication CERN-PH-EP-2010-013, arXiv:1005.5609 [hep-ex]

Sivers asymmetry - proton



new final results

CERN-PH-EP-2010-013



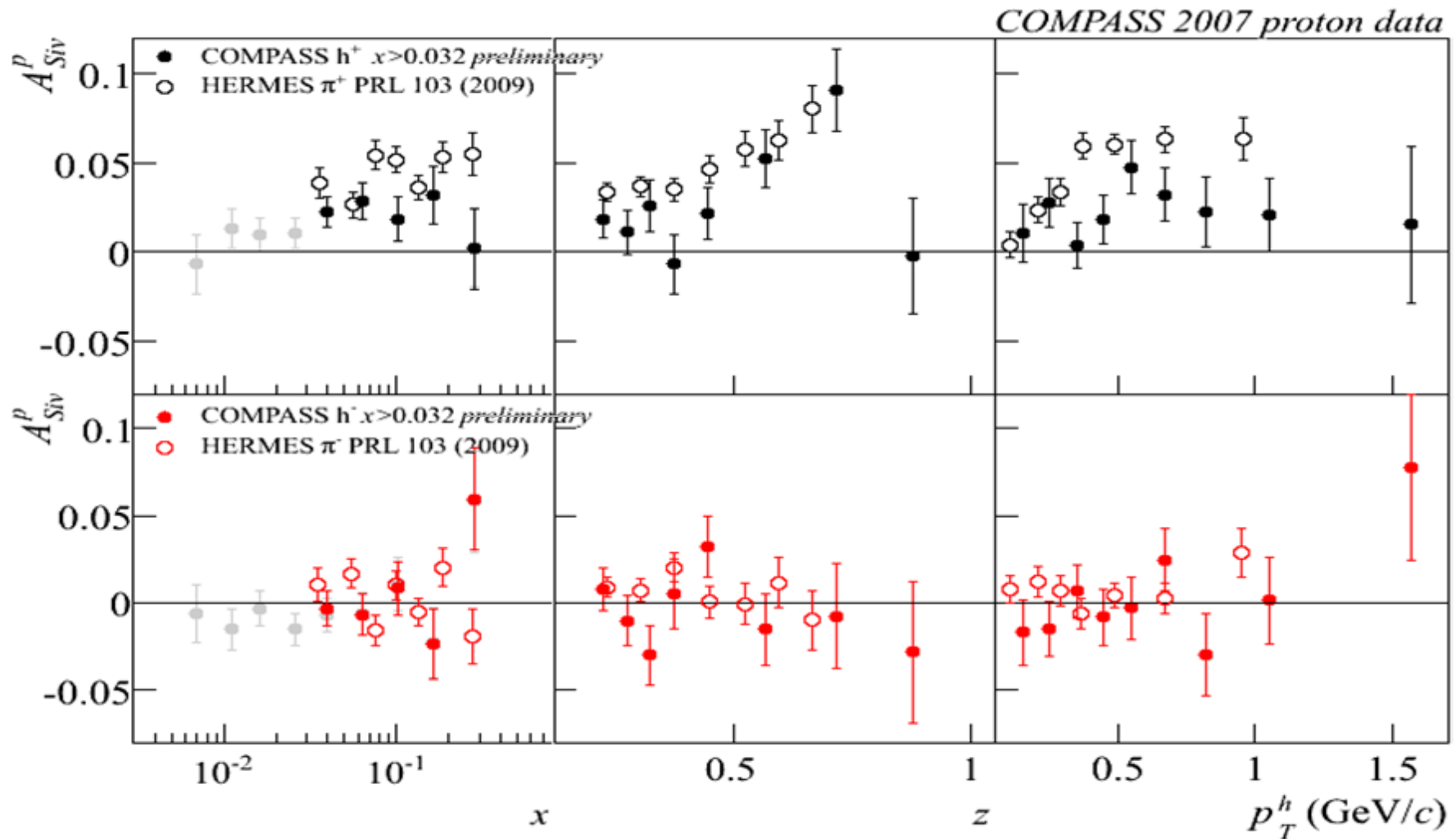
evidence for a positive signal for h^+ ,
which extends to small x , in the region not measured before

systematic errors $h^- \sim 0.5 \sigma_{stat}$
 $h^+ \sim 0.8 \sigma_{stat}$ plus a scale (abs) uncertainty of ± 0.01

Sivers asymmetry - proton



comparison with the **HERMES** 2002-2005 final results

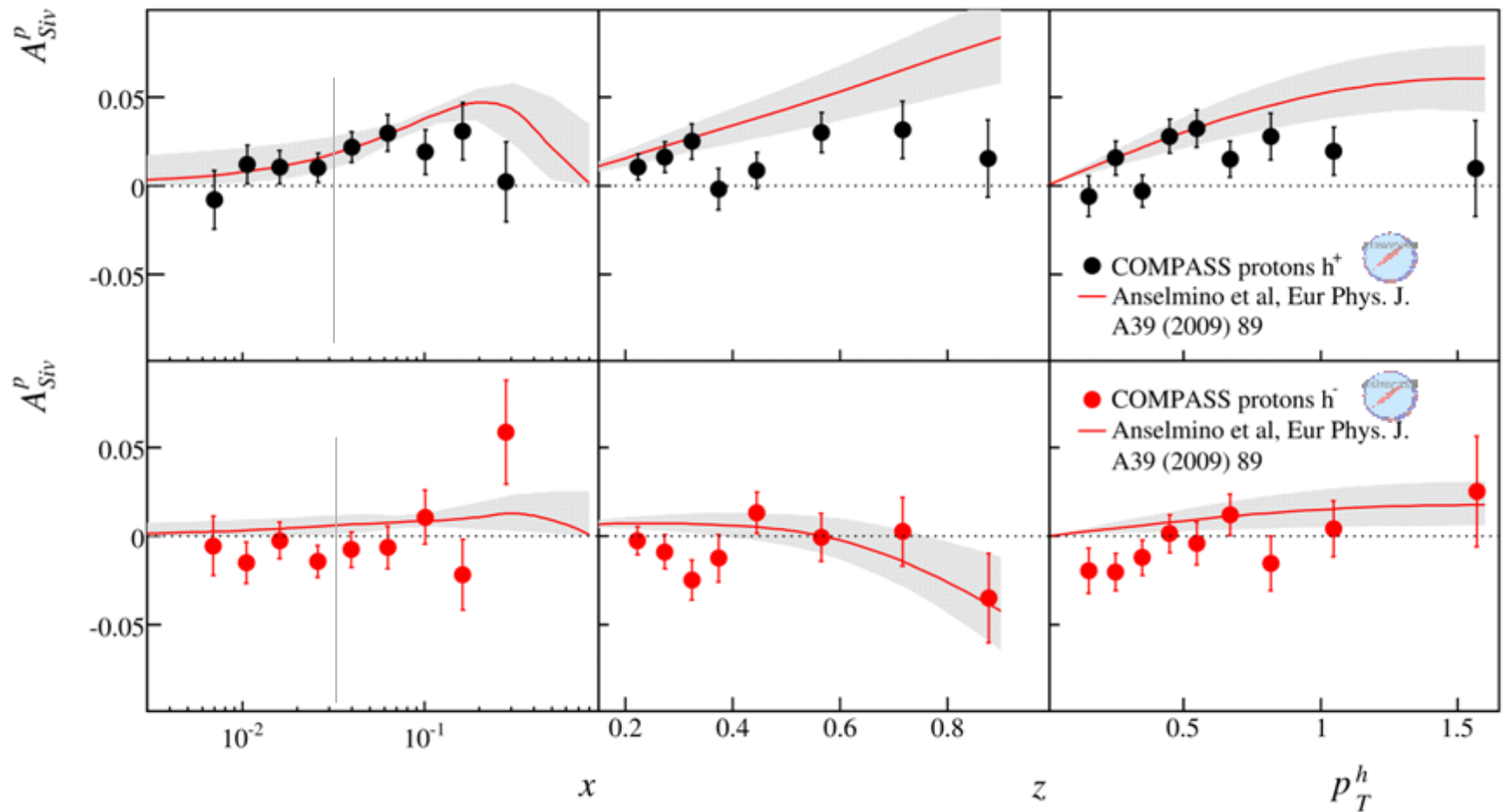


h^+ COMPASS asymmetry: same sign
smaller by a factor ~ 2

Sivers asymmetry - proton

comparison with theory

- ... most recent predictions from *M. Anselmino et al.*
based on the fit of HERMES proton and COMPASS deuteron data

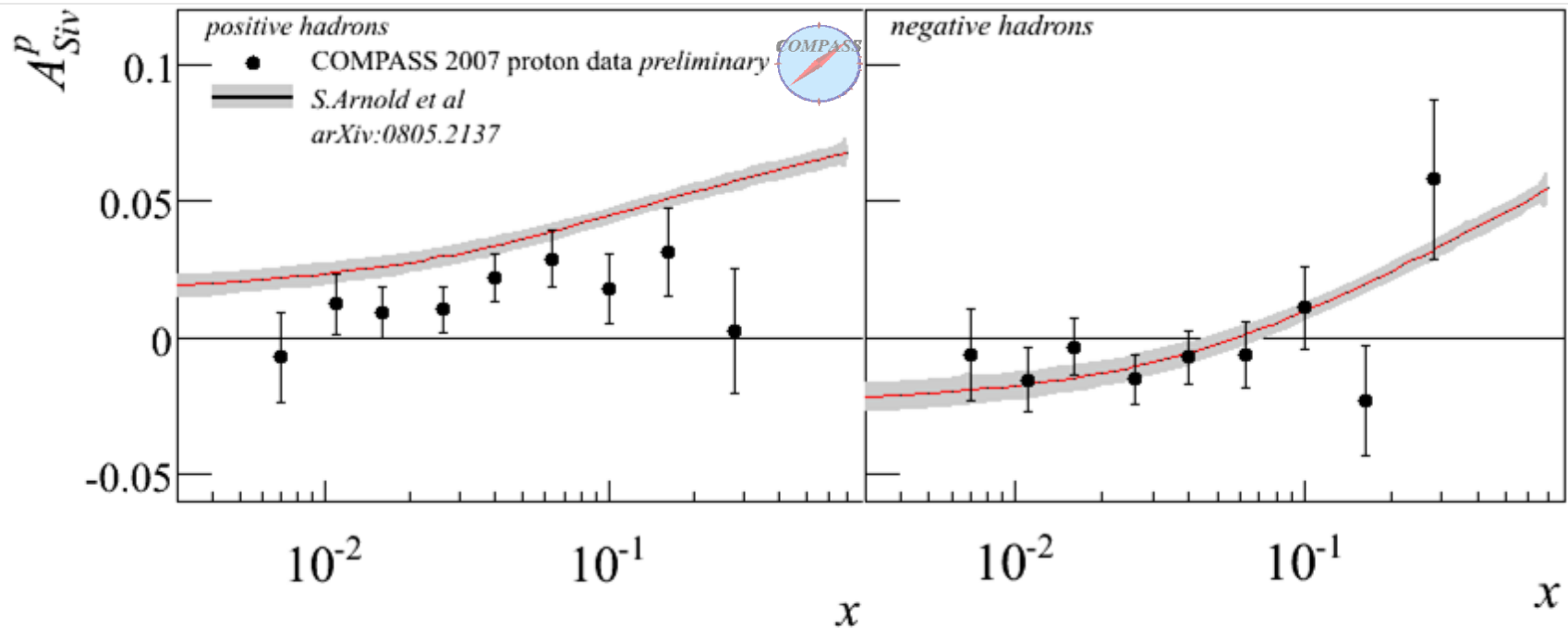


Sivers asymmetry - proton

comparison with theory

... calculations from *S.Arnold et al.*

in agreement with HERMES preliminary results



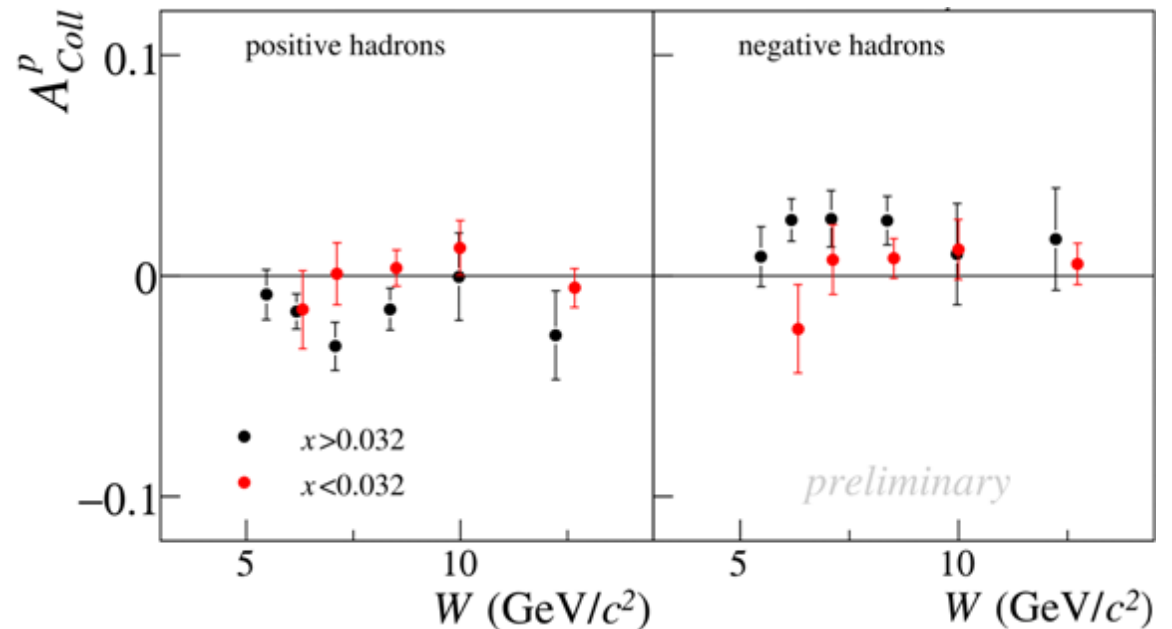
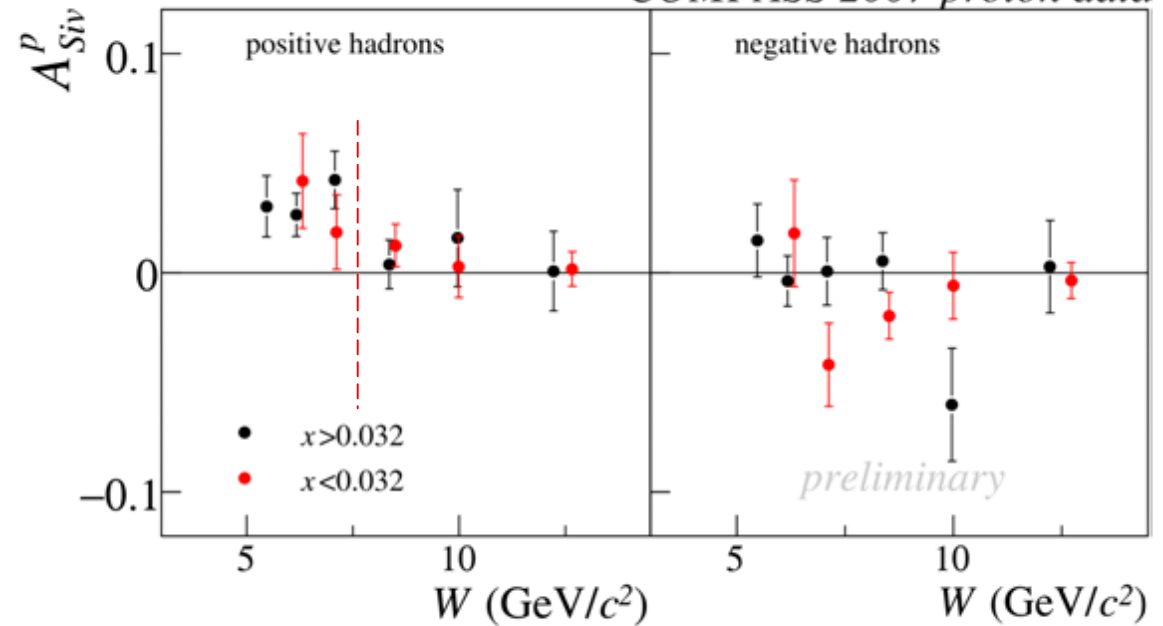
Sivers asymmetry - proton

a lot of investigations to understand the results (systematic effects)

hints for a possible W dependence of the h^+ Sivers asymmetry

no evidence of dependence of the Collins asymmetry on W

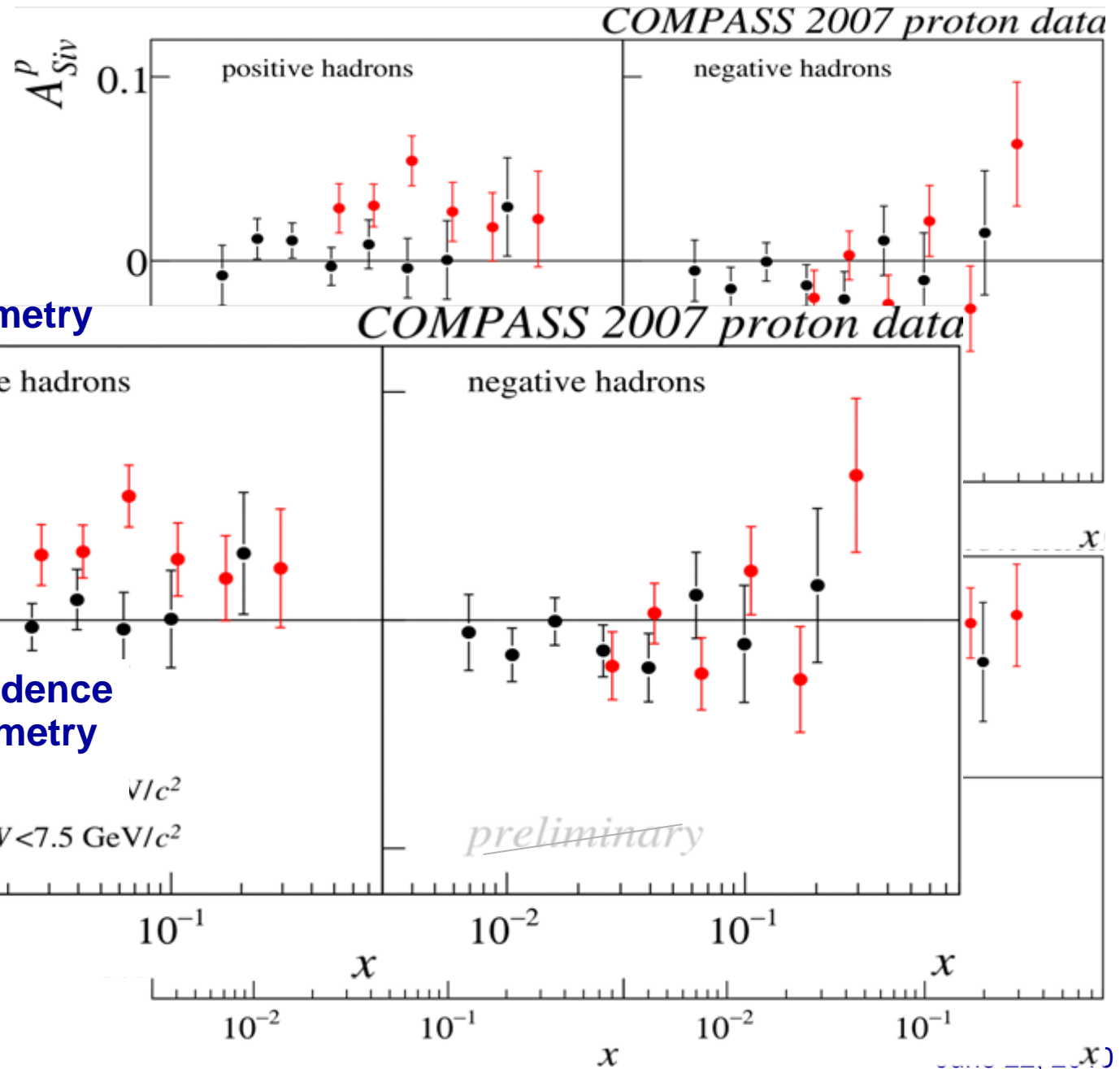
COMPASS 2007 proton data



Sivers asymmetry - proton

hints for a possible
W dependence of
the h^+ Sivers asymmetry

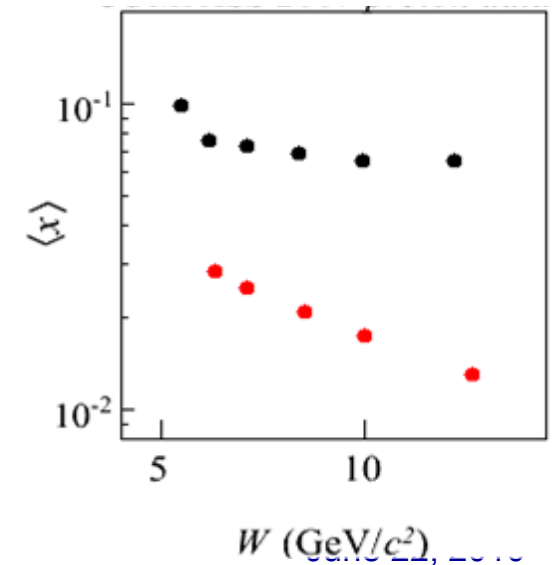
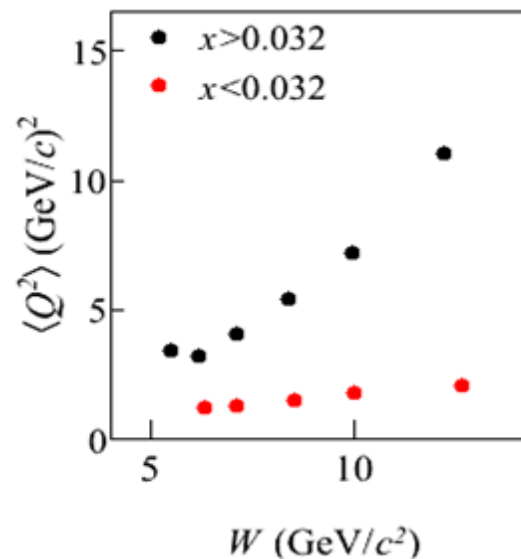
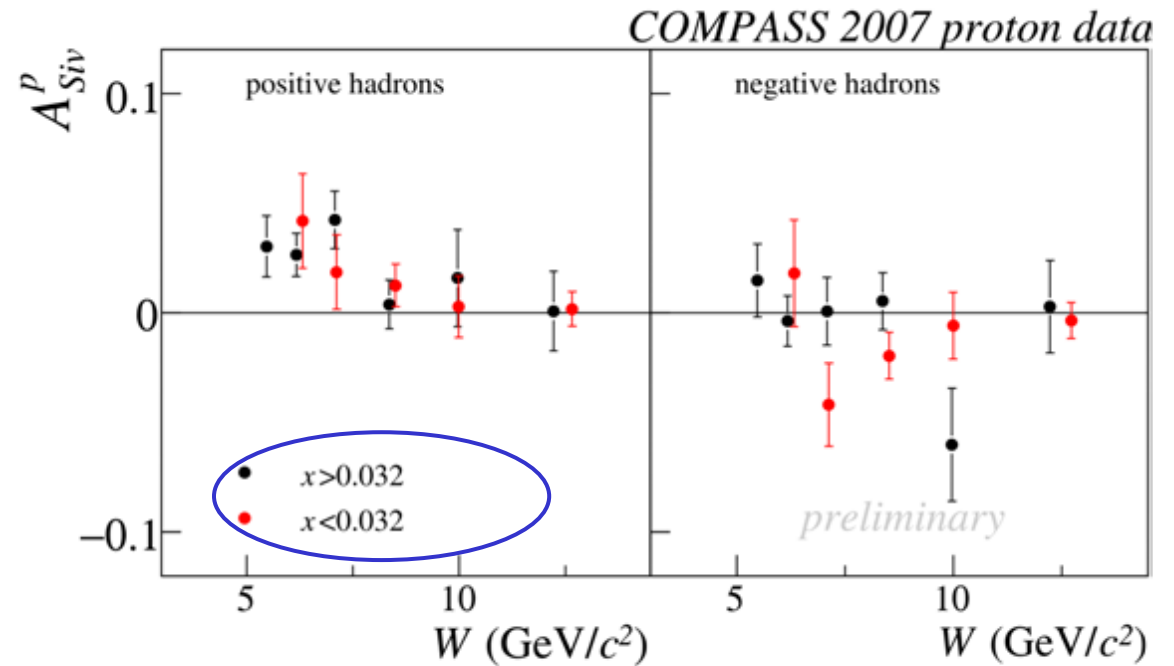
no evidence of dependence
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on W



Sivers asymmetry - proton

hints for a possible
W dependence of
the h^+ Sivers asymmetry

not due to
different $\langle x \rangle$ vs W



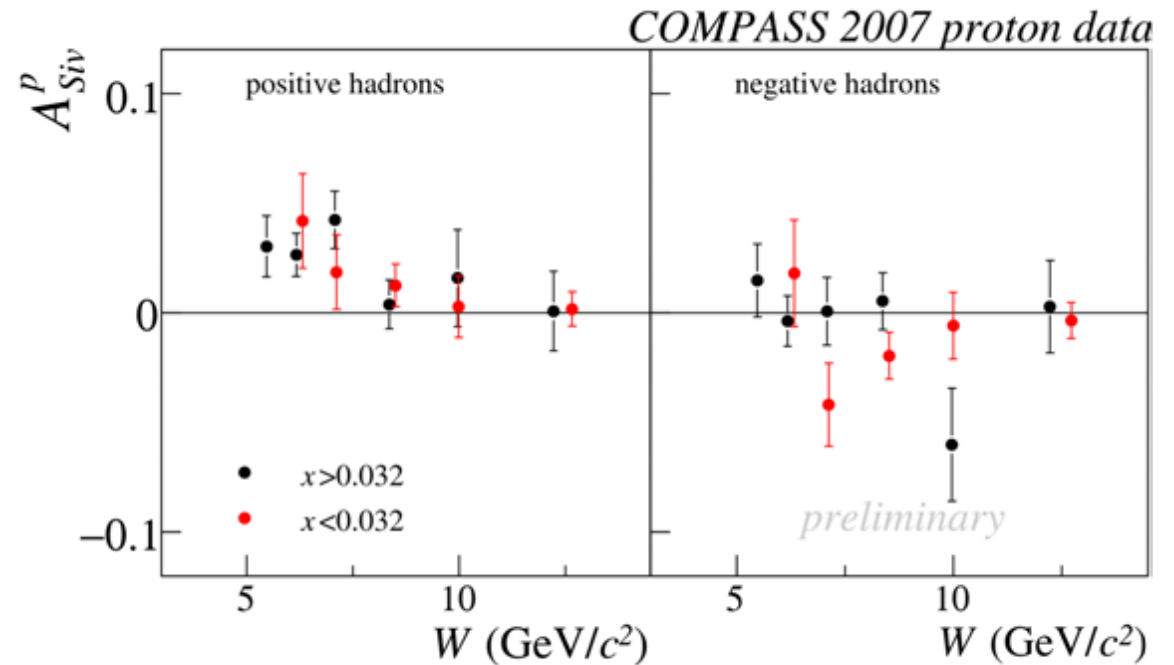
Sivers asymmetry - proton

hints for a possible
W dependence of
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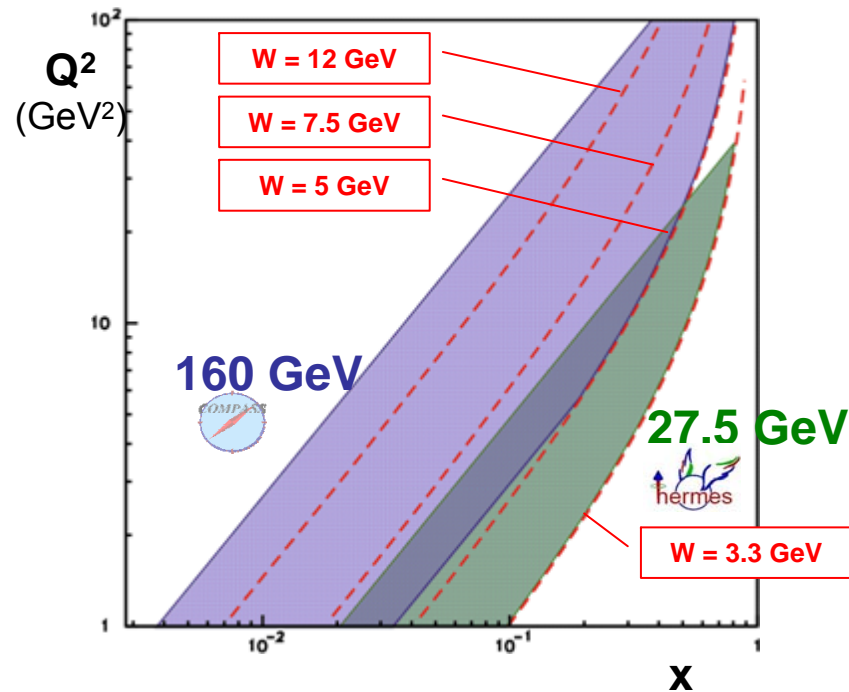
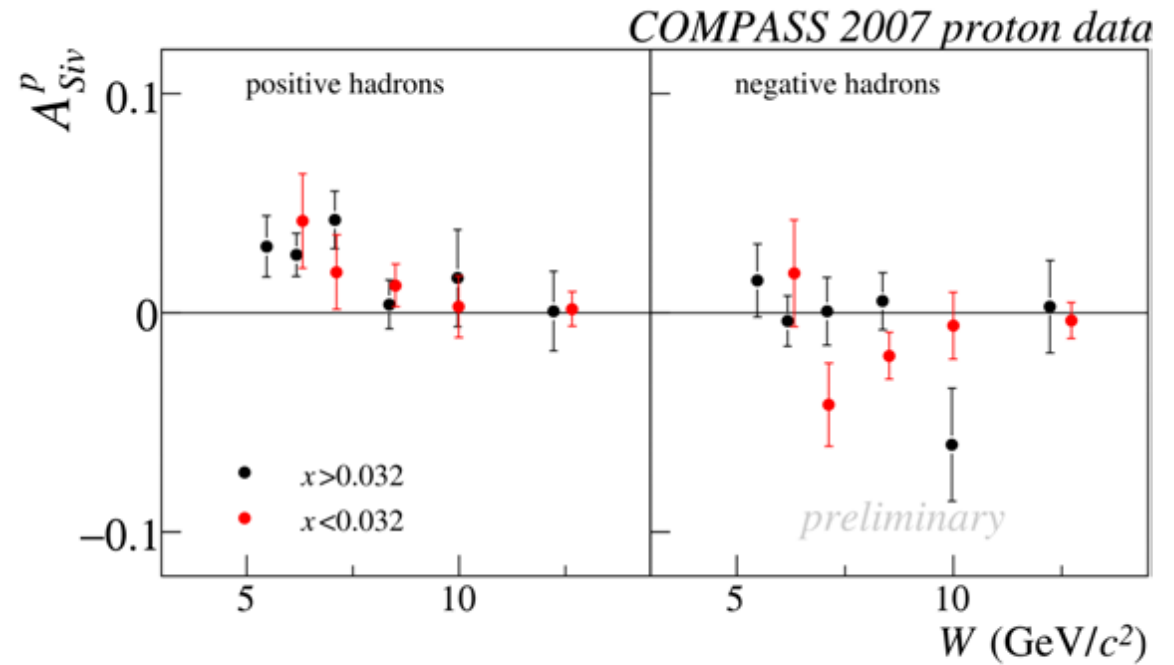
unexpected ...

*but W and z cuts sometimes are applied to
select the current fragmentation region*



Sivers asymmetry - proton

hints for a possible
W dependence of
the h^+ Sivers asymmetry



no definite conclusion with the
present accuracy:
higher precision
measurements needed

→ 2010 data

transverse Spin Asymmetries

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \dots$$

further two twist 2 asymmetries

four twist 3 asymmetries

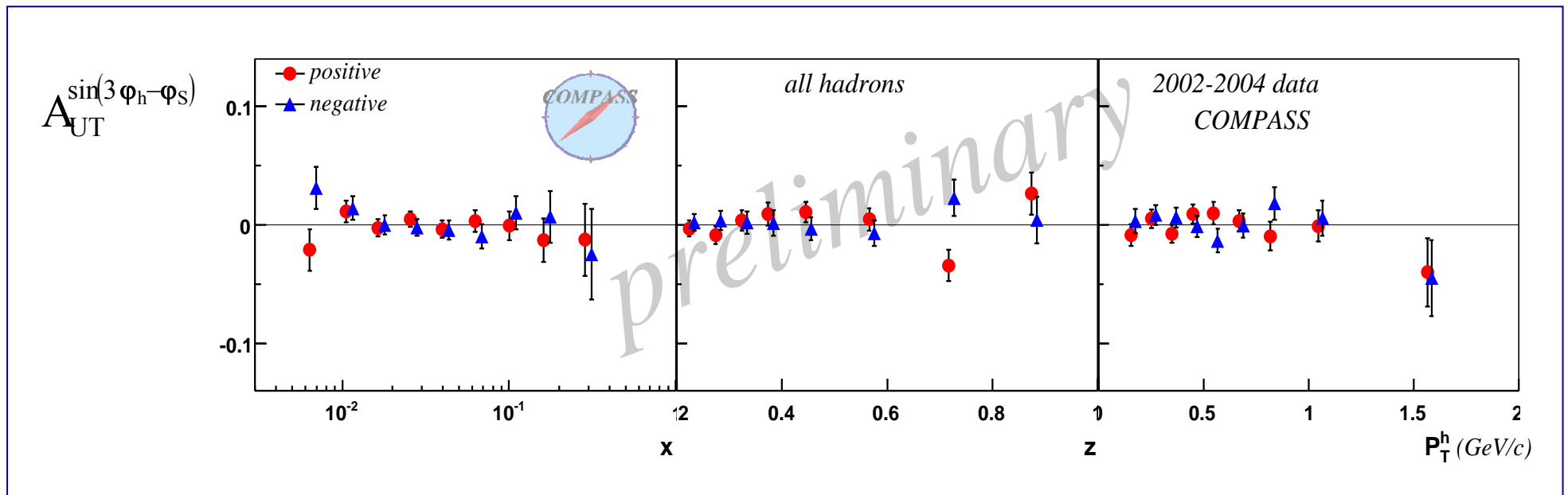
$$\begin{aligned}
 & + |\mathbf{S}_\perp| \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\
 & \left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \\
 & + |\mathbf{S}_\perp| \lambda_e \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\
 & \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \Bigg\},
 \end{aligned}$$

all measured by COMPASS on d (DIS2007): an example

other T SAs - deuteron data

$$F_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$


 "pretzelosity" \otimes Collins FF



on deuteron asymmetries compatible with zero :
 again because of cancellation between u and d quark contributions?

COMPASS results: summary



deuteron data:

- **unpolarised azimuthal asymmetries:** large effects, different for h^+ and h^-
finalised soon
- **all spin asymmetries (T&L)** compatible with zero
Collins and Sivers asymmetries: constrain for d quark PDFs
final results already published

proton, 2007 data:

final results for Collins and Sivers at high energy

- Q^2 and W ranges extended at large values
- x range extended to considerably smaller values

Collins asymmetry:

- clear signal both for positive and negative hadrons in the valence region
- SIDIS as appropriate tool to investigate the transversity PDF

Sivers asymmetry:

- signal for positive hadrons, also at small x values
- indication for a possible (and unexpected) W dependence

more statistic needed asap

next from the 2007 p data: PID for Collins, Sivers and the other T SSA
LR asymmetries

from the d data: unpolarised SIDIS differential cross-sections

future

2010: transversely polarised NH₃ target and 160 GeV muon beam
data taking started on June 12

→ higher precision measurements of the Collins, the Sivers,
and the other T spin asymmetries
0.004 < x < 0.3, in valence region Q² up to 20 GeV²

2011: longitudinally polarised NH₃ target and the 190 GeV muon beam
→ higher precision measurements of the L spin asymmetries



COMPASS II Proposal: submitted in May 2010

- Primakoff
- DY on transversely polarised target → *O. Denissov*
- DVCS on LH2 → **unpolarised azimuthal asymmetries and cross-sections**

high energy SIDIS: a special tool to investigate transversity and TMDs
complementary to JLab experiments

future:

- **fixed target with higher intensity high energy beams**
- **high energy colliders**

thank you!