

COMPASS results on the gluon polarisation in the nucleon

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on behalf of the COMPASS collaboration

SYMMETRIES AND SPIN (Spin-Praha-2009)
Prague July 28, 2009

Overview

- The Spin Puzzle
- The COMPASS experiment
- Direct gluon polarisation measurements
 - Open Charm analysis
 - High p_T hadron pairs analysis
- Results
- Summary and Outlook

The Spin Puzzle 20 years later

$$\frac{\hbar}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L_z$$

Definitions:

$$\Delta\Sigma = \Delta u + \Delta d + \Delta s$$

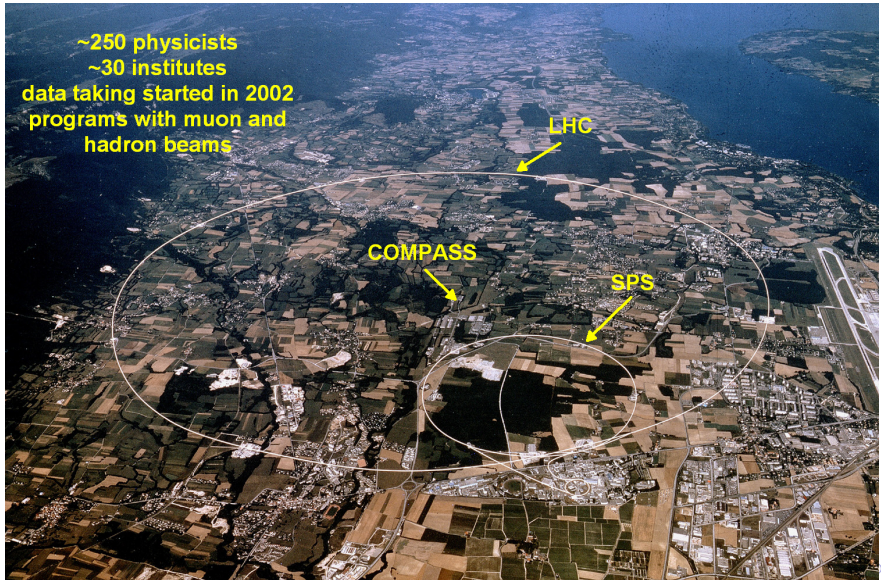
$$\Delta q = \int \Delta q(x) dx$$

$$\Delta G = \int \Delta g(x) dx$$

- In the naive QPM: $\Delta\Sigma = 1$
- Taking into account relativistic corrections and $\Delta s = 0$: $\Delta\Sigma \approx 0.6$
- The EMC: $\Delta\Sigma = 0.12 \pm 0.17$ [*Nucl. Phys. B* **328** (1989) 1]
- COMPASS NLO QCD fit to the world data:
 $\Delta\Sigma = 0.30 \pm 0.01(\text{stat.}) \pm 0.02(\text{evol.})$ [*PLB* **647** (2007) 8-17]
- Direct measurements can answer what is the contribution of ΔG to the nucleon spin...

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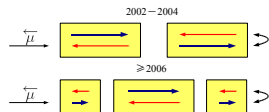
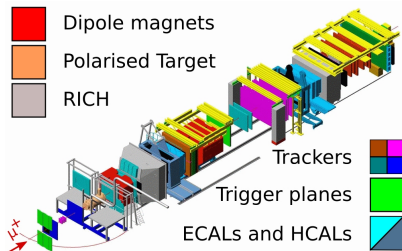
COmmon MUon and P-roton Apparatus for S-tructure and S-pectroscopy



The COMPASS setup

- Two stages: LAS and SAS
- Tracking ($p > 0.5$ GeV):
Scifis, GEMs, Micromegas, Straws
- Particle identification:
 π , K, p separation
(above 2, 9 and 18 GeV)
with RICH, ECAL, HCAL, μ Filter
- Beam: 160 GeV μ^+ , $2 \cdot 10^8 \mu/5s$,
naturally polarised $\sim 80\%$
- Target (${}^6\text{LiD}$): 2 (3) cells oppositely
polarised $\sim 50\% \Rightarrow$
observables \equiv cross-section **asymmetries!**

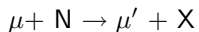
[NIMA 577 (2007) 455]



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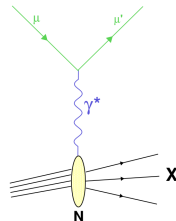
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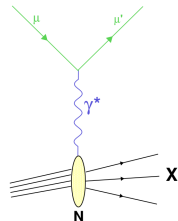
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$$\gamma^* + g \rightarrow q \bar{q}$$



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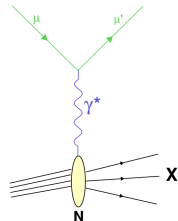
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- Tag PGF through special hadrons in the final state:

- charmed mesons
 - hadrons with high transverse momenta (w.r.t. γ^*)



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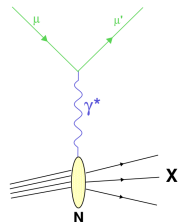
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- Measure double spin asymmetries:

$$A^{exp} = \frac{N^{\uparrow\downarrow} - N^{\uparrow\uparrow}}{N^{\uparrow\downarrow} + N^{\uparrow\uparrow}} \propto \frac{\Delta g}{g}$$



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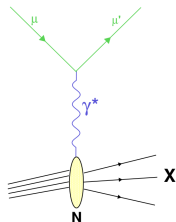
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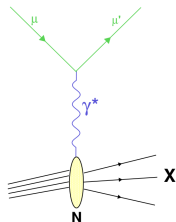
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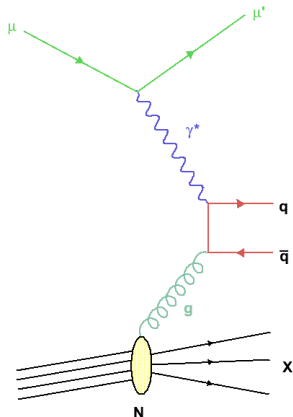
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$$\Delta g \equiv \Delta g(x, \mu^2)$$

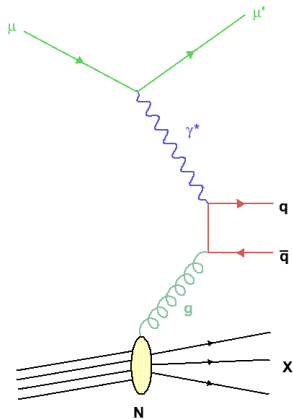
$$g \equiv g(x, \mu^2)$$

Tagging PGF process: charmed mesons



- $q \equiv c \Rightarrow$ D mesons in the final state
- clean channel:
 - intrinsic charm and charm in string fragmentation – suppressed
 - resolved photon – negligible
- perturbative scale: $4(m_c^2 + p_T^2)$
- difficult measurement:
 - low statistics
 - huge combinatorial background
- NLO effects may be important

Tagging PGF process: high p_T hadron pairs, $Q^2 > 1$ (GeV/c)²



- $q \equiv$ **light quarks** \Rightarrow a pair of hadrons with high transverse momenta in the final state
- perturbative scale: Q^2
- simple measurement: large statistics
- QCD background processes
- strong dependence on the MC simulations

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Interpretation of the charmed double spin asymmetry

In the LO approximation:

$$A^{exp} = \frac{N^{\uparrow\downarrow} - N^{\uparrow\uparrow}}{N^{\uparrow\downarrow} + N^{\uparrow\uparrow}} = P_t P_b f a_{LL} \frac{S}{S+B} \frac{\Delta g}{g} + A^{bgd}$$

P_t target polarisation: 50%

P_b beam polarisation: 80%

f target dilution factor: ≈ 0.4 for ${}^6\text{LiD}$

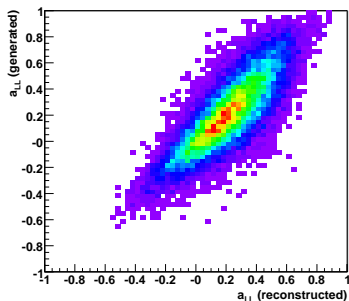
a_{LL} partonic cross-section asymmetry (analysing power)

$\frac{S}{S+B}$ fraction of the signal

A^{bgd} extracted simultaneously with A^{exp}

Partonic cross-section asymmetry a_{LL}

- $a_{LL} \equiv \frac{\Delta\hat{\sigma}}{\hat{\sigma}}$: partonic cross-section asymmetry, not accessible in the measurement
- it is determined from Monte Carlo (AROMA LO) and parameterised using Neural Network
- the trained NN is applied to data \Rightarrow obtain a_{LL} on the event-by-event basis



Data samples (2002 – 2006)

- standard channels: [PLB 676 (2009) 31-38]

- $D^0 \rightarrow K\pi$
(D^* -non-tagged; 37000 events)

Data selection:

- K, π identified using RICH
- $0.4 \text{ GeV}/c^2 < M_{K\pi} - M_{D^0} < 0.4 \text{ GeV}/c^2$

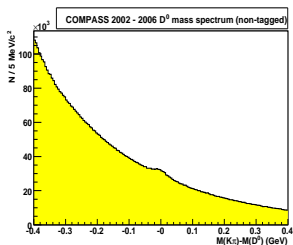
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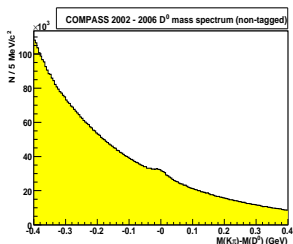
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- $D^* \rightarrow D^0 \pi_{slow} \rightarrow K\pi\pi_{slow}$
(D^* -tagged; 8700 events)

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- electrons rejected (avoid fake π_{slow})



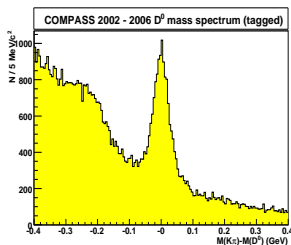
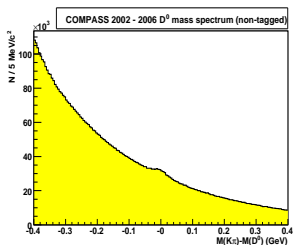
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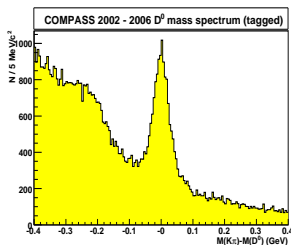
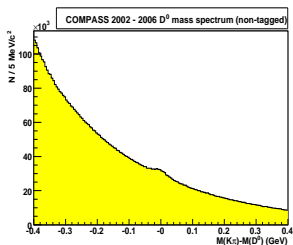
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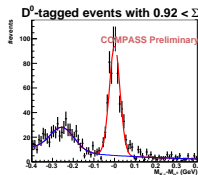
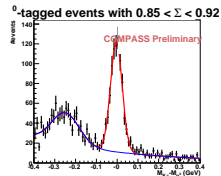
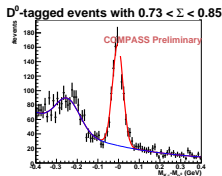
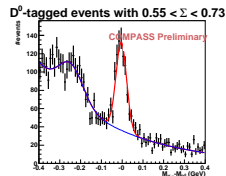
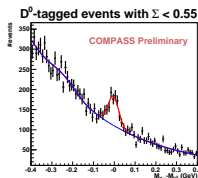
- new channels:

- $D^* \rightarrow D^0\pi_{slow} \rightarrow K\pi(\pi^0)\pi_{slow}$ (D^* -tagged; 6200 events)
- $D^* \rightarrow D^0\pi_{slow} \rightarrow K_{sub}\pi\pi_{slow}$ (D^* -tagged; 1800 events)

Event weight

To select the signal in more efficient way:

- each event is weighted with the full weight: $fP_{b\text{all}} \frac{S}{S+B}$
- at the same time event is weighted with the background weight ($\dots \frac{B}{S+B}$)
 \Rightarrow simultaneous extraction of signal and background asymmetries
- $\Sigma \equiv \frac{S}{S+B}$ is parameterised event-by-event basis as a function of many variables (e.g. m_{D^0} , $p_{T_{D^0}}$, RICH likelihoods,...)



Open charm results (2002–2006)

sample	$\langle \Delta g/g \rangle_x$
D*-tagged and non-tagged [PLB 676 (2009) 31-38]	-0.47 ± 0.27 (stat.) ± 0.11 (sys.)
new! D* with additional π^0	-0.15 ± 0.63 (stat.)
new! D* with RICH-subthreshold kaons	$+0.57 \pm 1.02$ (stat.)

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$$\left\langle \frac{\Delta g}{g} \right\rangle_x = -0.39 \pm 0.24 \text{ (stat.) } \pm 0.11 \text{ (syst.)}$$

at $\langle x_g \rangle = 0.11_{-0.05}^{+0.11}$, $\langle \mu^2 \rangle = 13 \text{ (GeV}/c)^2$

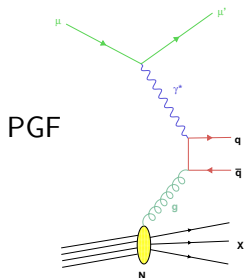
SYSTEMATICS:

source	$\delta(\langle \Delta g/g \rangle_x) D^0(D^*)$	source	$\delta(\langle \Delta g/g \rangle_x) D^0(D^*)$
false asymmetry	0.05(0.05)	P_b	0.025
S/(S+B)	0.07(0.01)	P_t	0.025
a _{LL}	0.05(0.03)	f	0.025
Total:	0.11(0.07)		

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Interpretation of the high p_T hadron asymmetry, A^{2h}

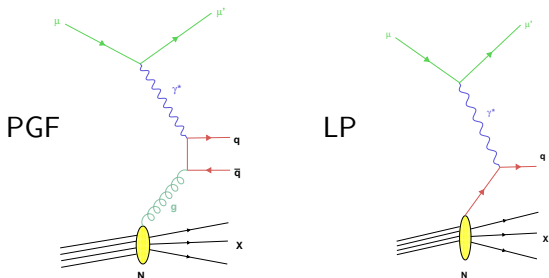
In the LO approximation:



- R_i – fraction of sub-processes (PGF, LP, QCD-C)
- a_{LL}^i – analysing powers for PGF, LP and QCD-C
- D – a depolarisation factor
- $A_1^{LO} = \sum e_i^2 \Delta q_i / \sum e_i^2 q_i$

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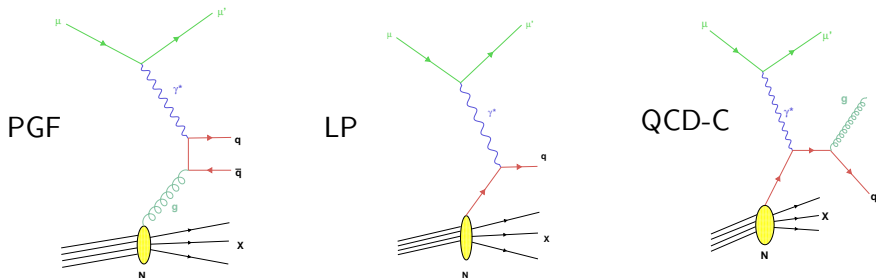
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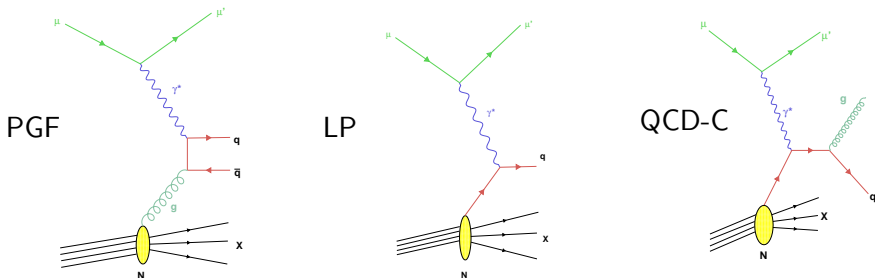
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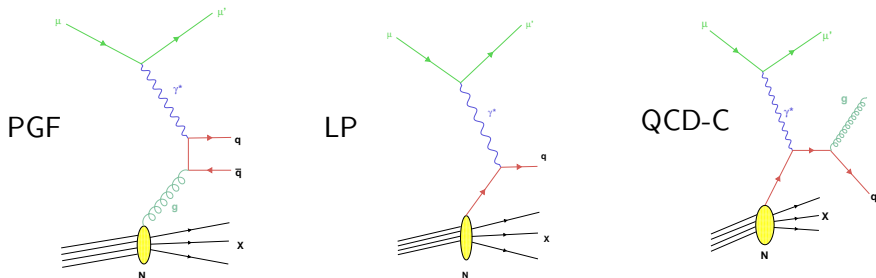


$$A^{2h} \sim \frac{\Delta g}{g}(x_g) a_{LL}^{PGF} R_{PGF} + A_1^{LO}(x_{Bj}) DR_{LO} + A_1^{LO}(x_c) a_{LL}^{QCDC} R_{QCDC}$$

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$\Delta g/g$ extraction

$$\langle \frac{\Delta g}{g} \rangle_x = \frac{A^{2h} + A^{corr}}{\beta}$$

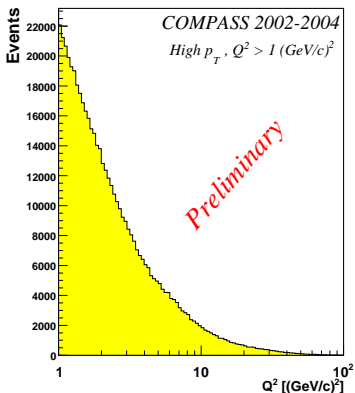
- $A^{2h} = A^{exp} / P_t P_b f$ – directly from data
- A^{corr} – combination of inclusive asymmetry A_1 , R_i and a_{LL}^i
- β factor – a function of R_i and a_{LL}^i
- R_i and a_{LL}^i have to be obtained from MC simulation (**LEPTO**) for both inclusive and hight p_T samples
 ⇐ good agreement between data and MC is crucial!

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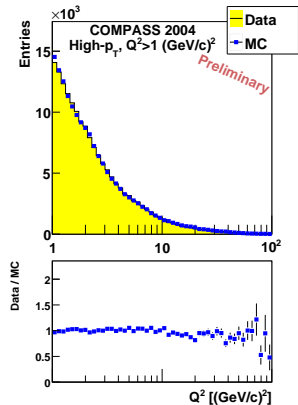
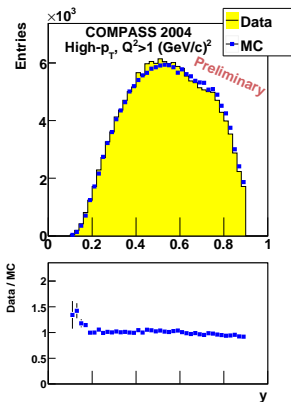
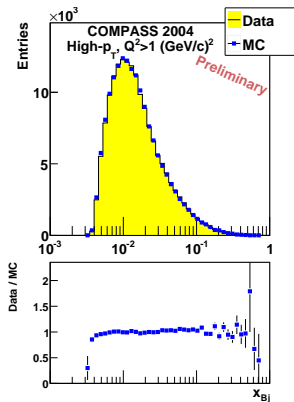
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- R_i and a_{LL}^i have to be obtained from MC simulation (**LEPTO**) for both inclusive and high p_T samples
 ⇐ good agreement between data and MC is crucial!
- Event weight: $fDP_b\beta$
- Parameterisation on the event-by-event basis: Neural Network

High p_T sample

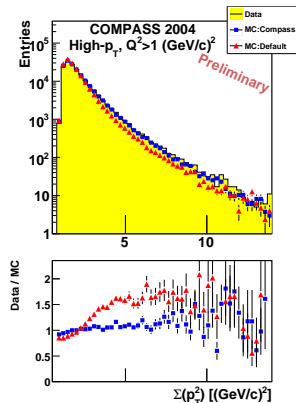
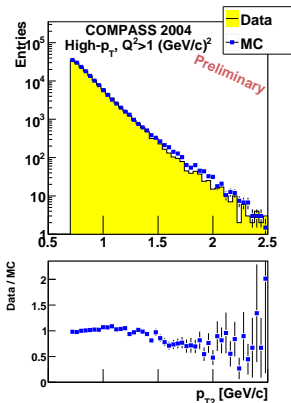
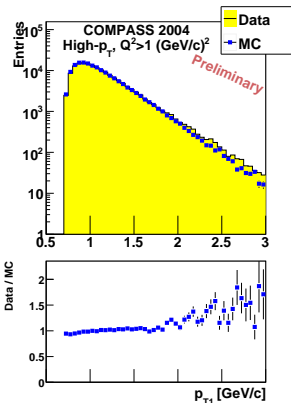


Data selection:

- $Q^2 > 1$ (GeV/c)² (cuts 90% of the statistics)
- $p_{T_1} > 0.7$ GeV/c and $p_{T_2} > 0.7$ GeV/c
- 2002 – 2004: 500k events

Data and MC comparison: x_{Bj} , y , Q^2 

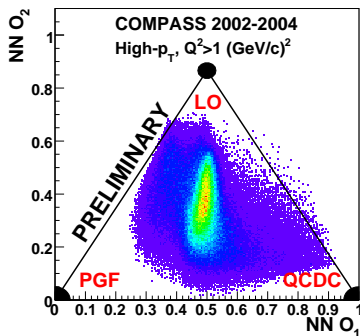
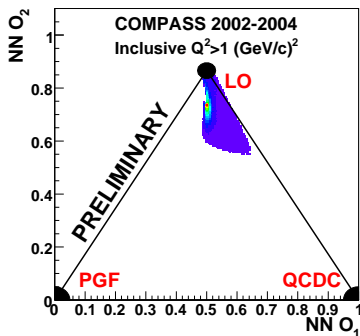
Data (2002-2004) and MC comparison: p_{T1} , p_{T2} , Σp_{T2}



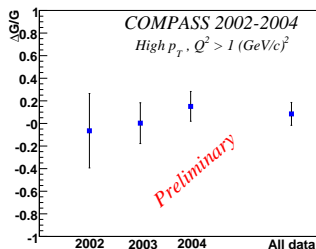
LEPTO tuning: k_T and parameters of fragmentation

NN parameterisation of R_i

The event probability to be PGF, LP or QCDC is evaluated from a NN parametrising R_i (R_i sum up to 1):



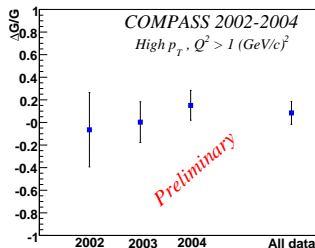
$$R_{PGF} = 1 - O_1 - \frac{1}{\sqrt{3}} O_2 \quad R_{QCDC} = O_1 - \frac{1}{\sqrt{3}} O_2 \quad R_{LP} = \frac{2}{\sqrt{3}} O_2$$

High p_T hadron pairs results
 $Q^2 > 1 \text{ (GeV}/c)^2 \text{ (2002 - 2004):}$


SYSTEMATICS:

source	$\delta(\langle \Delta g/g \rangle_x)$
NN	0.006
MC	0.040
$fP_b P_t$	0.006
false asymmetry	0.011
A_1	0.008
formula	0.013
Total	0.045

$$\left\langle \frac{\Delta g}{g} \right\rangle_x = 0.08 \pm 0.10 \text{ (stat.)} \pm 0.05 \text{ (sys.)} \quad \langle x_g \rangle = 0.082^{+0.041}_{-0.027}, \quad \langle \mu^2 \rangle = 3 \text{ (GeV}/c)^2$$

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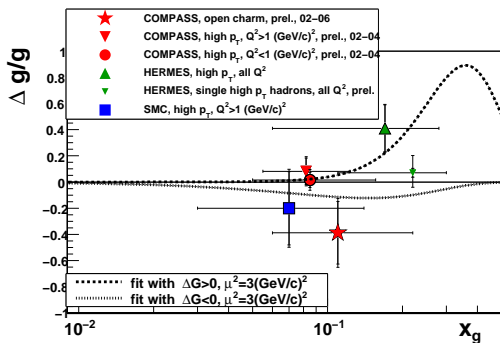
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$$Q^2 < 1 \text{ (GeV}/c)^2 \text{ (2002 - 2003):} \quad \left\langle \frac{\Delta g}{g} \right\rangle_x = 0.024 \pm 0.089 \pm 0.057 \text{ [PLB 633 (2006) 25-32]}$$

$$Q^2 < 1 \text{ (GeV}/c)^2 \text{ (2002 - 2004):} \quad \left\langle \frac{\Delta g}{g} \right\rangle_x = 0.016 \pm 0.058 \pm 0.054 \text{ preliminary}$$

- The Spin Puzzle
- The COMPASS experiment
- Direct gluon polarisation measurements
 - Open Charm analysis
 - High p_T hadron pairs analysis
- Results
- Summary and Outlook

COMPASS results on $\Delta g/g$ 

- Direct COMPASS measurements on gluon polarisation: $\langle \Delta g/g \rangle_x$ compatible with 0 at $x_g \approx 0.1$
- The curves: COMPASS NLO QCD fits to world data on $g_1^d \Rightarrow$ fits with negative and positive ΔG describe data equally well

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 - High p_T , $Q^2 < 1$ (GeV/c)²: $\langle \Delta g/g \rangle_x = 0.016 \pm 0.058 \pm 0.054$ ($\mu^2 = 3$ (GeV/c)²)
- The results indicate $\langle \Delta g/g \rangle_x$ consistent with 0 at $x_g \approx 0.1$

OUTLOOK

- Open Charm:
 - NLO analysis is going on
 - add 2007 data
- High p_T pairs:
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COMPASS has presented recently to the SPSC the addendum to its original proposal and got positive feed-back.

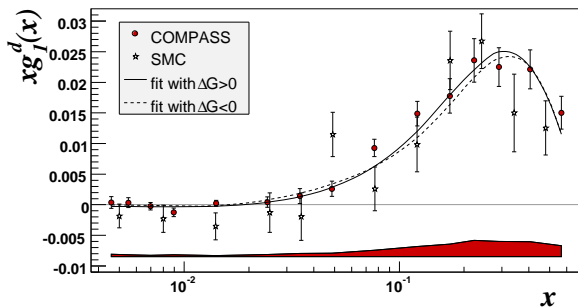
It will run both longitudinal and transverse programs beyond 2009.

SPARES

Indirect $\Delta g/g$ Determination:

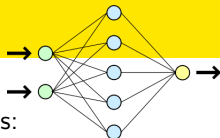
- World data: 9 experiments, 230 data points (43 from COMPASS)
- Both solutions: $\Delta G > 0$ and $\Delta G < 0$ describe data equally well

[PLB 647 (2007) 330–340]



ΔG from COMPASS data only: $\approx 0.2 - 0.3$

SPARES: Artificial Neural Network



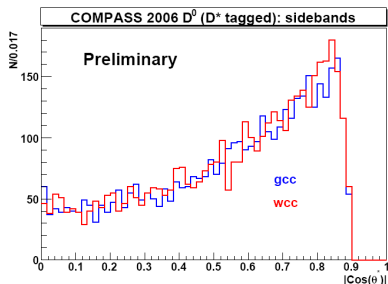
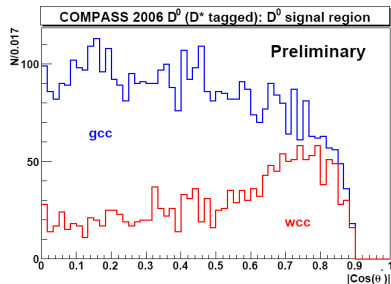
- a multidimensional structure of the interconnected neurons:
 - input layer: vector of variables on which the parameterisation will be built
 - hidden layers with the possibility to change the number of neurons
 - output layer: usually 1 exit neuron contained the desired output (e.g. a_{LL}^{par})
- the desired output is provided on the event-by-event basis (supervised learning)
- the connections are weighted
- the training process: the iterative procedure of weights adaptation
- the training goal: to minimise the difference between the desired and obtained NN output
- the training results are simultaneously checked using the testing set
- once the net is trained – frozen structure and weights – it can be applied to solve the problem for the new input sets!

SPARES: Neural Network qualification of events

the slide from C. Franco DIS 2009, Madrid, Spain

- **Two real data samples** (*with same cuts*) are compared by the **Neural Network** (*giving as input some kinematic variables as a learning vector*):
 - **Signal model** \rightarrow **gcc** = $K^+ \pi^- \pi_s^- + K^- \pi^+ \pi_s^+$ (D^0 spectrum: signal + bg.)
 - **Background model** \rightarrow **wcc** = $K^+ \pi^+ \pi_s^- + K^- \pi^- \pi_s^+$ (*no D^0 is allowed*)
- **If the background model is good enough:** Net is able to distinguish the signal from the combinatorial background on a event by event basis (*inside gcc*)

Example of a good learning variable



SPARES: The full formula for open-charm analysis

the slide from C. Franco DIS 2009, Madrid, Spain

- The number of events comes from the asymmetries in the following way:

$$N_{u,d} = a \phi n (S+B) \left(1 + P_T P_\mu f \left(a_{LL} \frac{S}{S+B} \frac{\Delta G}{G} + a_{LL}^B \frac{B}{S+B} A_B \right) \right)$$

a = acceptance, ϕ = muon flux, n = number of target nucleons

- We have 4 cell configurations (*2 cells oppositely polarised + field reversal for acceptance normalization*):

- Weight the 4 $N_{u,d}$ equations by ω_s and by $\omega_B = P_\mu \cdot f \cdot D(y) \cdot (B/S+B)$:

$$\langle \sum_{k=1}^{N_{\text{cell}}} \omega_i^k \rangle = \hat{a}_{\text{cell},i} \left(1 + (\langle \beta_{\text{cell},S} \rangle \omega_i) A_S + (\langle \beta_{\text{cell},B} \rangle \omega_i) A_B \right) = f_{\text{cell},i}$$

(cell = u , d , u' , d')
(ΔG/G)
(i = S , B)

$$\hat{a} = a \phi n \sigma = a \phi n (\sigma_{pGF} + \sigma_B) = a \phi n (S+B)$$

$$\beta_S = P_B P_T f a_{LL} \frac{S}{S+B} \quad \beta_B = P_B P_T f D \frac{B}{S+B}$$

8 eq. with 10 unknowns

SPARES: Monte Carlo in high p_T analysis

- 2 MC samples were used: high p_T and inclusive
- the MC chain: LEPTO generator (PDFs: MRST2004LO) and the full simulation of the detector response and of the reconstruction
- the part of the NLO corrections taken into account: gluon radiations in final and initial states
- to improve data/MC agreement – LEPTO was tuned: k_T (transverse momentum of the $q\bar{q}$ pairs) and parameters of fragmentation (default parameters were used in the systematics studies)

	PARJ21	PARJ23	PARJ24	PARJ41	PARJ42
Default	0.36	0.01	2.0	0.3	0.58
COMPASS	0.3	0.02	3.5	0.6	0.1

SPARES: the full formula for high p_T analysis

the slide from K.Kurek SPIN 2008, Charlottesville, USA

$$\frac{\Delta G}{G}(x_G) = \frac{A_{LL}^{2h}(x_{Bj}) + A^{corr}}{\beta}$$

Note that inclusive sample also contains PGF and QCDC as well as LO process

$$\beta = a_{LL}^{PGF} R_{PGF} - a_{LL}^{PGF,incl} R_{PGF}^{incl} \left(\frac{R_L}{R_L^{incl}} + \frac{R_C}{R_L^{incl}} \frac{a_{LL}^C}{D} \right)$$

$$A^{corr} = -A_1(x_{Bj})D \frac{R_L}{R_L^{incl}} - A_1(x_C)\beta_1 + A_1(x'_C)\beta_2$$

$$\beta_1 = \frac{1}{R_L^{incl}} (a_{LL}^C R_C - a_{LL}^{C,incl} R_C^{incl} \frac{R_L}{R_L^{incl}}) \quad \beta_2 = a_{LL}^{C,incl} \frac{R_C R_C^{incl}}{(R_L^{incl})^2} \frac{a_{LL}^C}{D}$$