



# Measurement of the longitudinal spin structure of proton by COMPASS

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on behalf of the COMPASS collaboration

August 31, 2009

1. COMPASS experiment
2. DIS and SIDIS asymmetries with deuteron (2002-2006) proton (2007) data
3. Non-singlet structure function  $g_1^{NS}$  and Bjorken sum rule
4. Full flavor separation analysis with LO QCD fit

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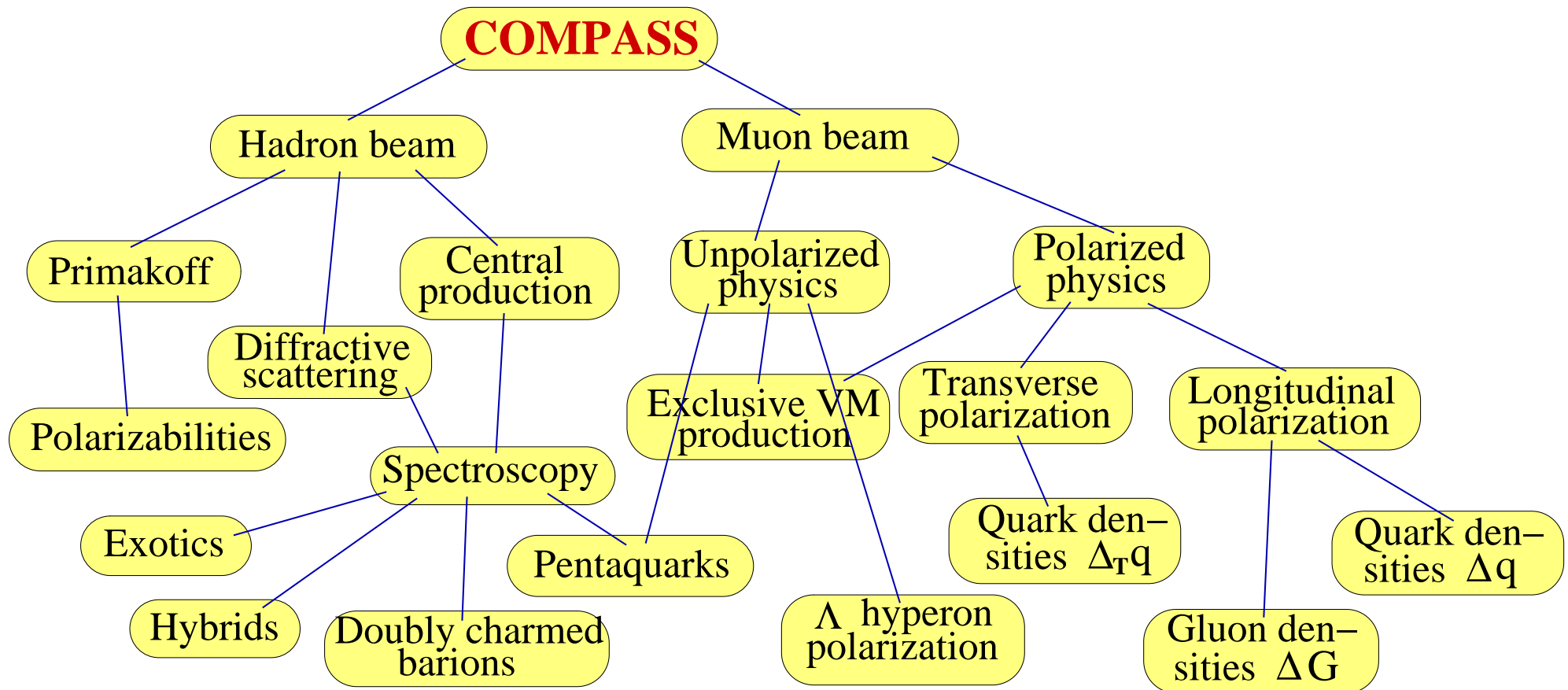
<sup>a</sup>on leave from JINR, Dubna

# COMPASS experiment

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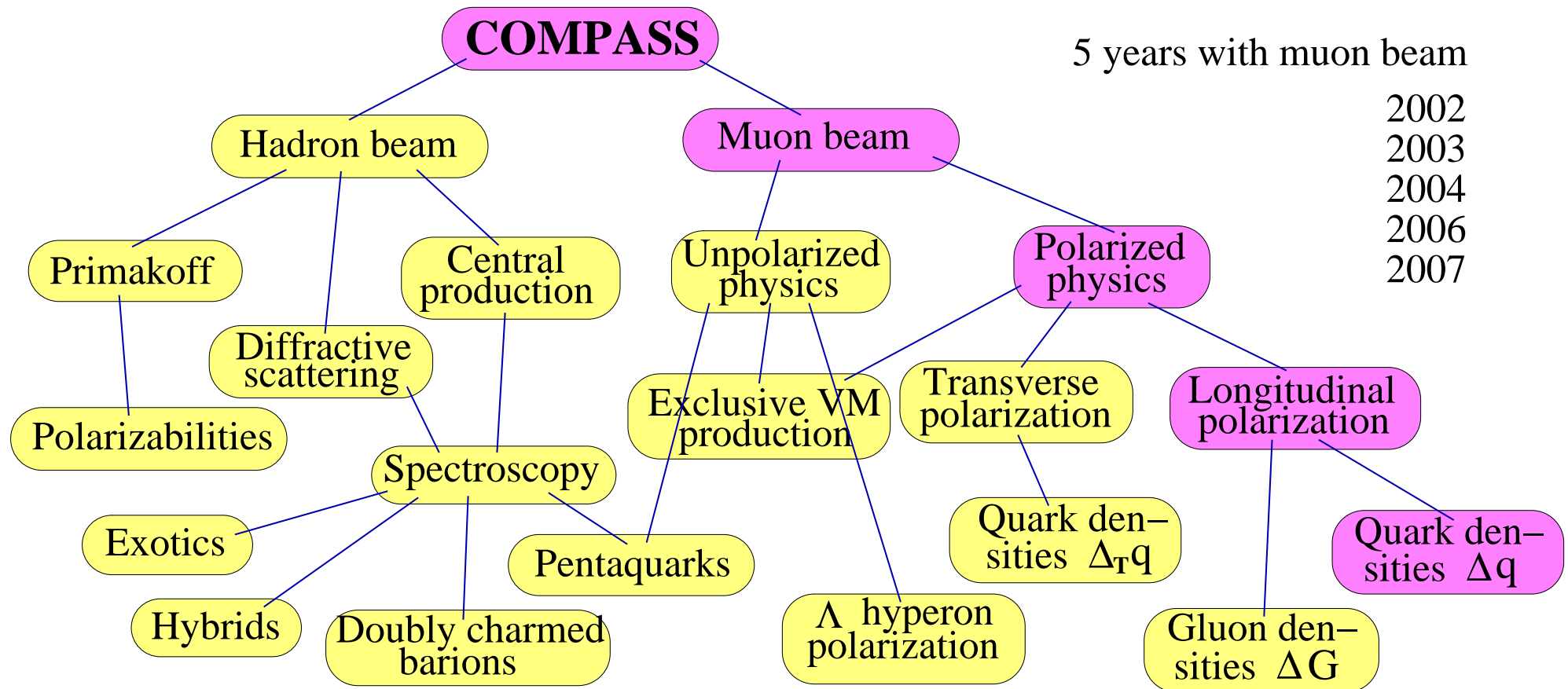
# COmmon Muon and Proton Apparatus for Structure and Spectroscopy

More than 220 physicists from 30 institutes

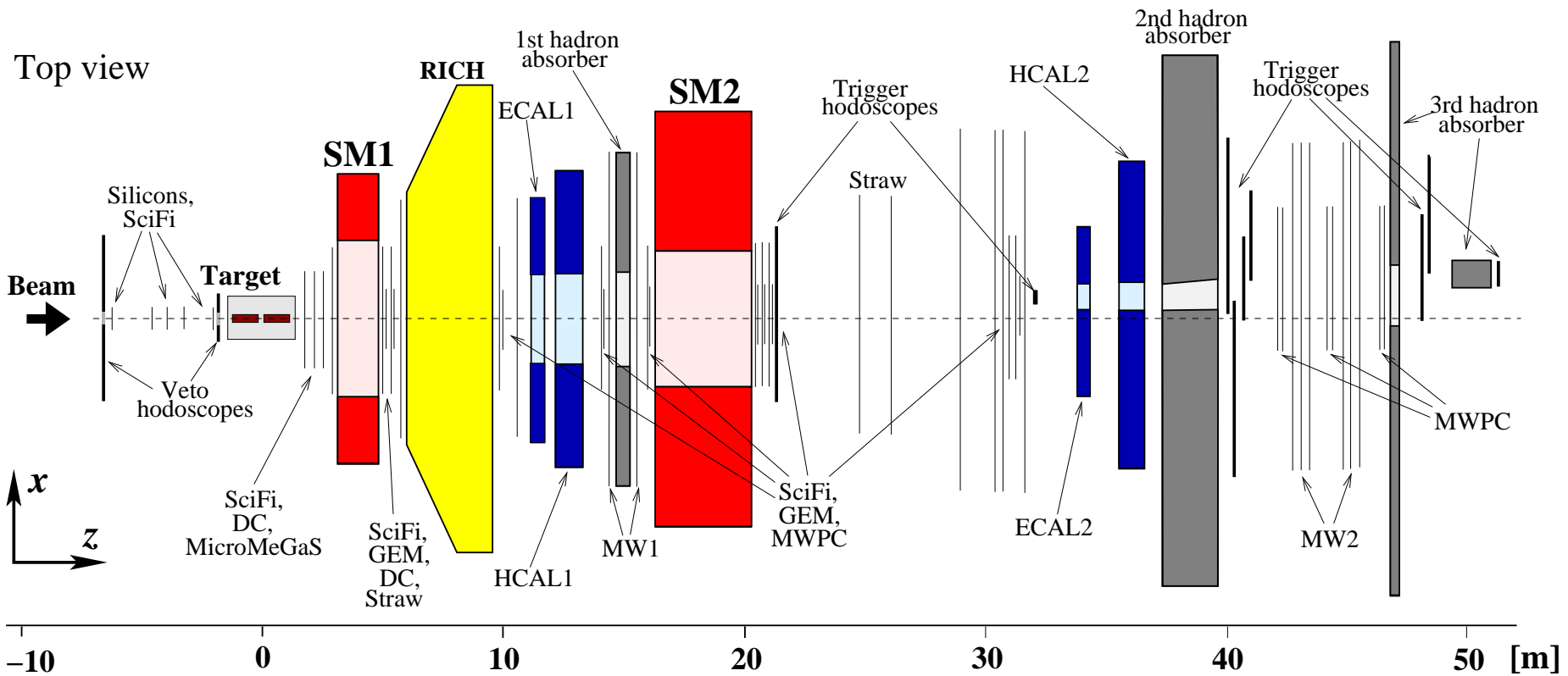


# COmmon Muon and Proton Apparatus for Structure and Spectroscopy

More than 220 physicists from 30 institutes



## Experimental setup



- Polarized beam  $\mu^+$  (-80%),  $E_b=160$  GeV
- 2(3) cells polarized target  ${}^6\text{LiD}$  (50%) and  $\text{NH}_3$  (90%)
- Two stages spectrometer
- Tracking detectors of different types
- Identification: HCALs, ECALs, RICH, muon walls

# Double-spin asymmetries from DIS and SIDIS reactions

## Introduction

- Naive view: 3 valence quarks with spin  $1/2 \Rightarrow$  nucleon spin is  $1/2$ .
- Decomposition of nucleon spin:

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + (L_q + L_G), \quad \text{Jaffe \& Manohar}$$

$$\frac{1}{2} = \left(\frac{1}{2}\Delta\Sigma + L_q\right) + J_G, \quad \text{Ji}$$

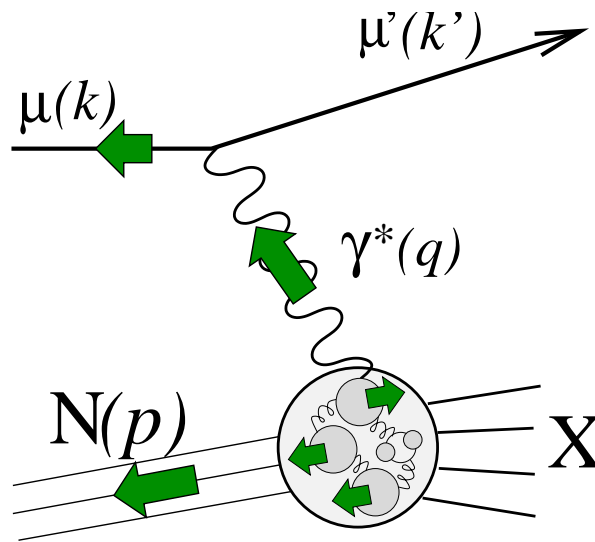
$$\frac{1}{2} = \dots \quad \text{other decompositions}$$

- Non-relativistic  $SU(6) = SU_f(3) \times SU_S(2)$  quark model
  - ◇ classification of  $J^P = \frac{1}{2}^+$  octet of baryons
  - ◇ successful to predict magnetic moments of baryons
  - ◇  $\Delta\Sigma = 0.58 \pm 0.03$ , where  $\Delta s \equiv 0$
- Relativistic models of constituent quarks ( $m_{u,d} \approx 330$  MeV)

$$\Delta\Sigma \approx 0.6 \quad L_q \approx 0.4$$

- Measurement of EMC (1988):  $\Delta\Sigma = 0.12 \pm 0.09 \pm 0.04 \Rightarrow$  “spin crisis”
- Recent evaluation from COMPASS (2007):  $\Delta\Sigma = 0.30 \pm 0.01 \pm 0.02$

## Deep-Inelastic Scattering (1)



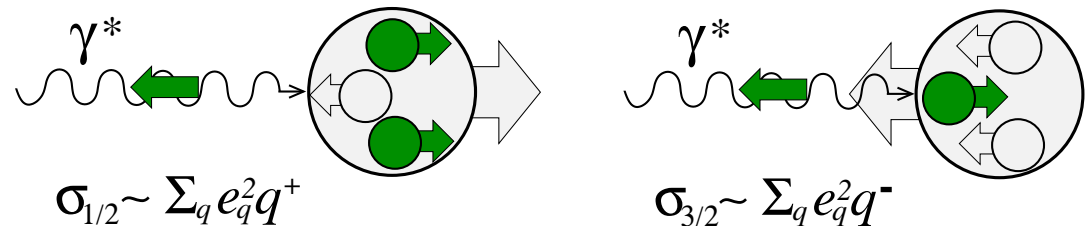
$k = (E, \vec{k})$	4-momentum of beam $\mu$
$k' = (E', \vec{k}')$	4-momentum of scattered $\mu$
$p = (M, \vec{0})$	4-momentum of nucleon
$q = k - k'$	4-momentum of $\gamma^*$
$-Q^2 = q^2$	Virtuality of $\gamma^*$
$\nu = E - E'$	Energy of $\gamma^*$ in lab. system
$y = \nu/E$	Fraction of energy of the beam $\mu$ taken by $\gamma^*$
$x = \frac{Q^2}{2M\nu}$	Bjorken scaling variable

### Quark-parton model

- Quark densities:

$$q(x) = q^+(x) + q^-(x)$$

$$\Delta q(x) = q^+(x) - q^-(x)$$



- Double-spin asymmetry:  $A^{\gamma N} \equiv A_1 = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}} = \frac{\sum_q e_q^2 \Delta q}{\sum_q e_q^2 q}$



## Deep-Inelastic Scattering (2)

- DIS cross-section in approximation of one photon exchange:

$$\sigma = \bar{\sigma} \pm \Delta\sigma$$

- Structure functions  $F_{1,2}$  and  $g_{1,2}$

$$\bar{\sigma}(x, Q^2) = aF_1(x, Q^2) + bF_2(x, Q^2)$$

$$\Delta\sigma(x, Q^2) = \alpha g_1(x, Q^2) + \beta g_2(x, Q^2)$$

- Double-spin asymmetry  $\mu N$ :

$$A^{\mu N} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} = \frac{\Delta\sigma}{\bar{\sigma}} \simeq DA_1$$

$D$  – depolarization factor

- Relation of structure functions to parton densities in QPM and/or LO QCD:

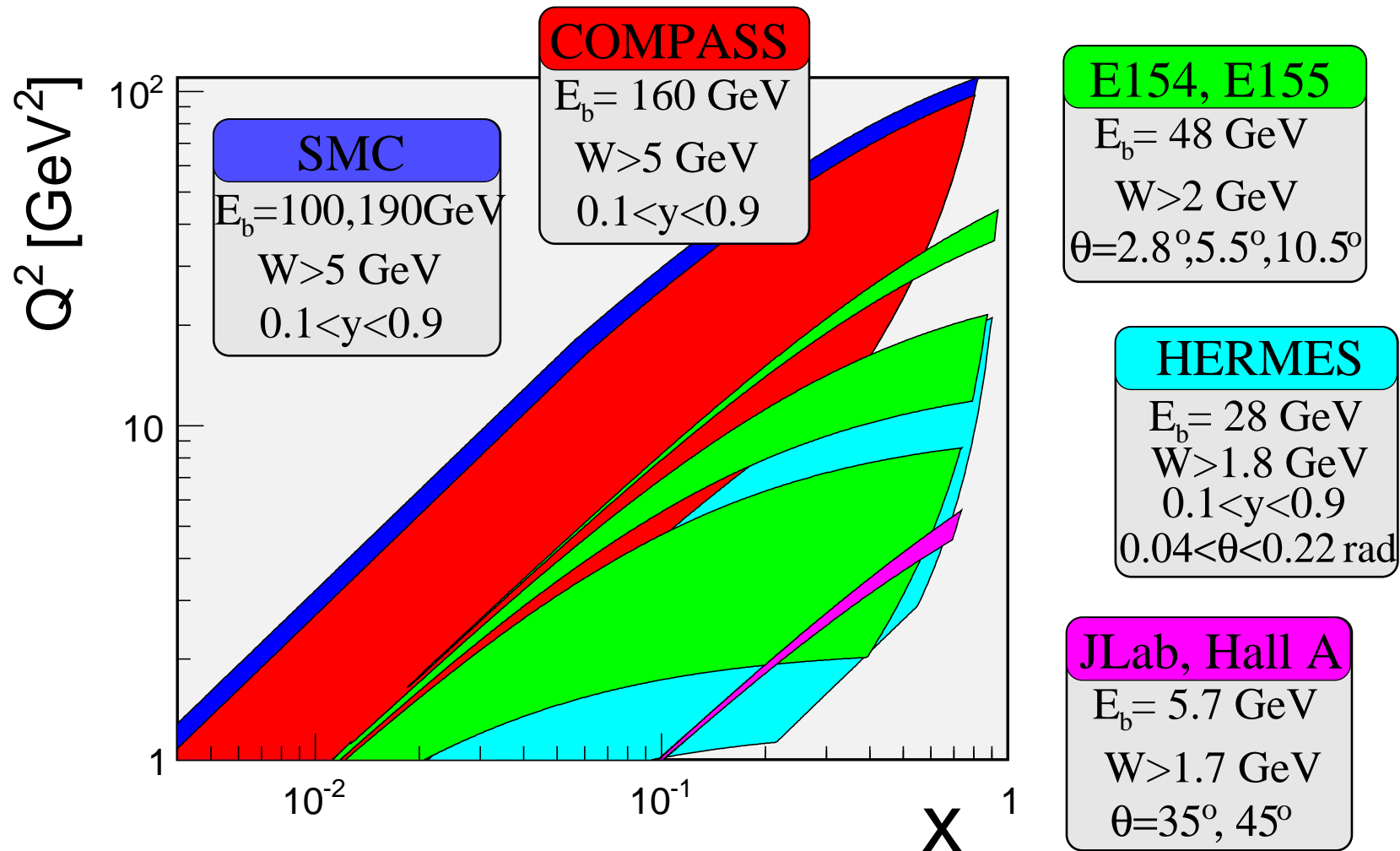
$$F_1 = \frac{1}{2} \sum_q e_q^2 (q + \bar{q})$$

$$g_1 = \frac{1}{2} \sum_q e_q^2 (\Delta q + \Delta \bar{q})$$

- Spin-independent  $F_{1,2}$  are well measured in a wide range of  $(x, Q^2)$
- Objective of study:

$$g_1 \simeq A_1 \cdot F_1$$

# Kinematic acceptance of typical pDIS experiments



**Advantage of COMPASS: access to low  $x$ !**

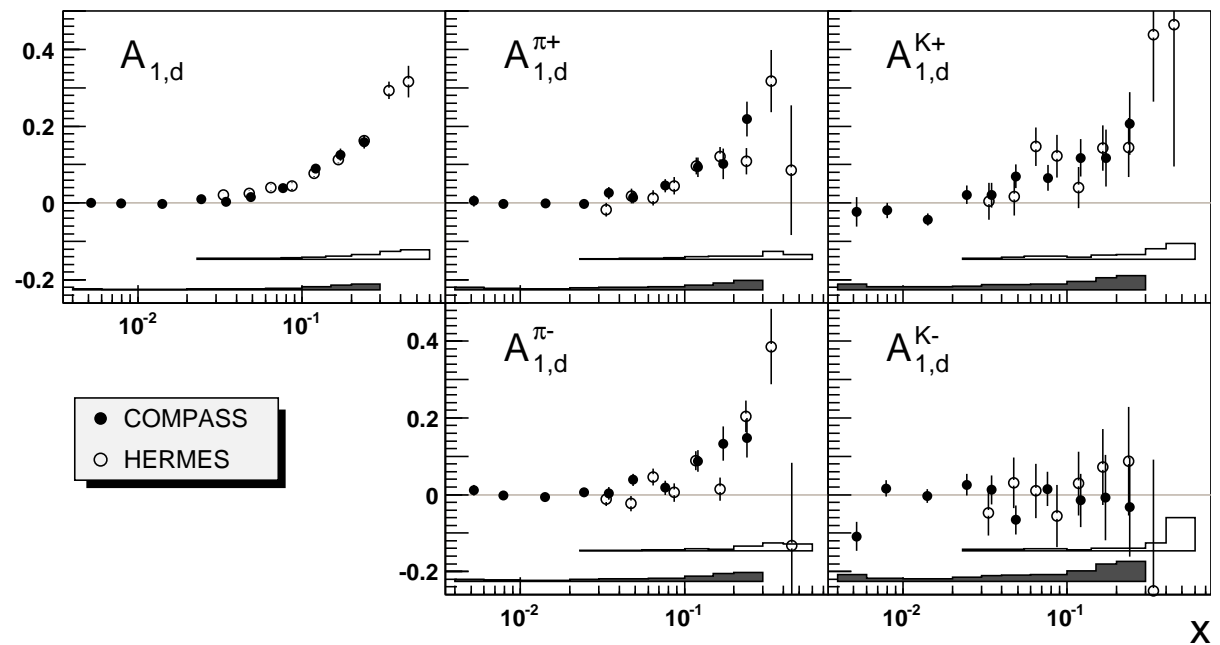
## Proton and deuteron asymmetries of COMPASS

- Kinematic domain:

$$Q^2 > 1 \text{ GeV}^2$$

$$0.1 < y < 0.9$$

$$0.004 < x < 0.7$$



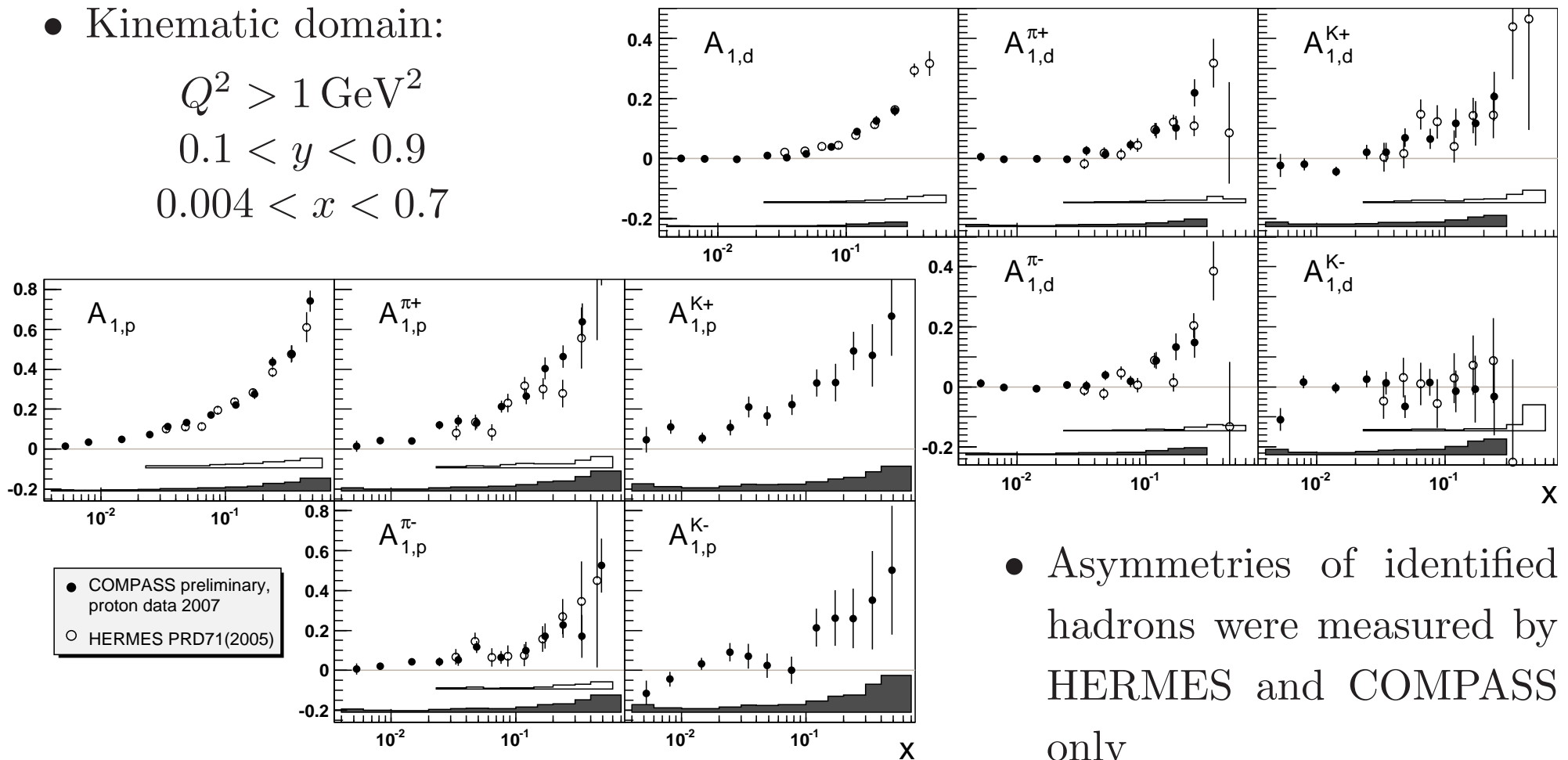
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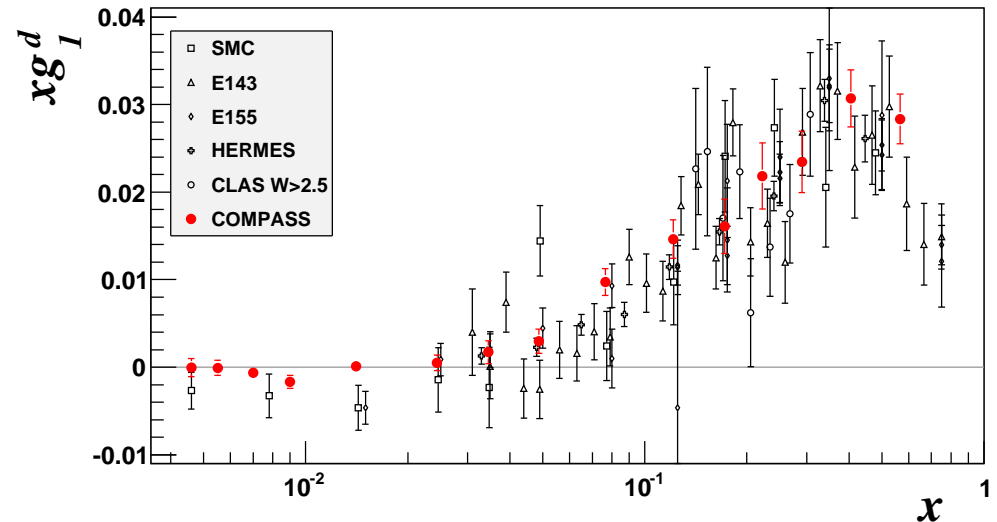
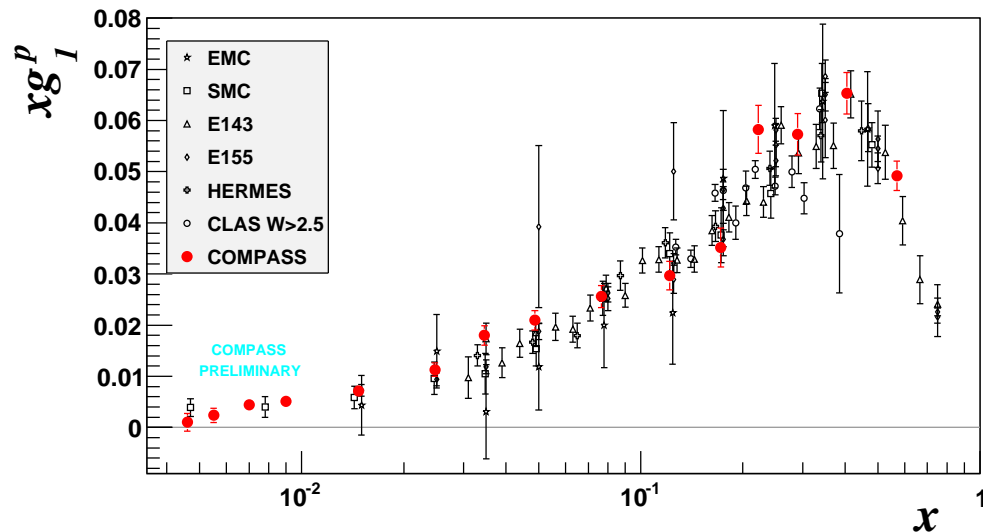
$$0.004 < x < 0.7$$



- Asymmetries of identified hadrons were measured by HERMES and COMPASS only

# Non-singlet structure function $g_1^{NS}$ and Bjorken sum rule

# Structure functions $g_1^p$ and $g_1^d$



- The non-singlet spin structure function  $g_1^{NS}(x)$  can be evaluated

$$g_1^{NS}(x) = g_1^p(x) - g_1^n(x) = 2 \left[ g_1^p(x) - \frac{g_1^d(x)}{1 - 3/2\omega_D} \right],$$

- First moments provide a test of the Bjorken sum rule, a fundamental result of QCD derived using current algebra:

$$\int_0^1 g_1^{NS}(x) dx = \frac{1}{6} \left| \frac{g_A}{g_V} \right| C^{NS} \quad \text{or} \quad \Delta u - \Delta d = \left| \frac{g_A}{g_V} \right|$$

## Fit of COMPASS data alone

- Evolution of non-singlet distribution is decoupled from  $\Delta\Sigma$  and  $\Delta G$

$$\frac{d}{dt} \begin{pmatrix} \Delta q^{NS} \\ \Delta\Sigma \\ \Delta G \end{pmatrix} = \frac{\alpha_s(t)}{2\pi} \begin{pmatrix} P_{qq}^{NS} & & \\ & P_{qq}^S & 2n_f P_{qG}^S \\ & P_{Gq}^S & P_{GG}^S \end{pmatrix} \otimes \begin{pmatrix} \Delta q^{NS} \\ \Delta\Sigma \\ \Delta G \end{pmatrix}, \quad t = \log\left(\frac{Q^2}{\Lambda^2}\right)$$

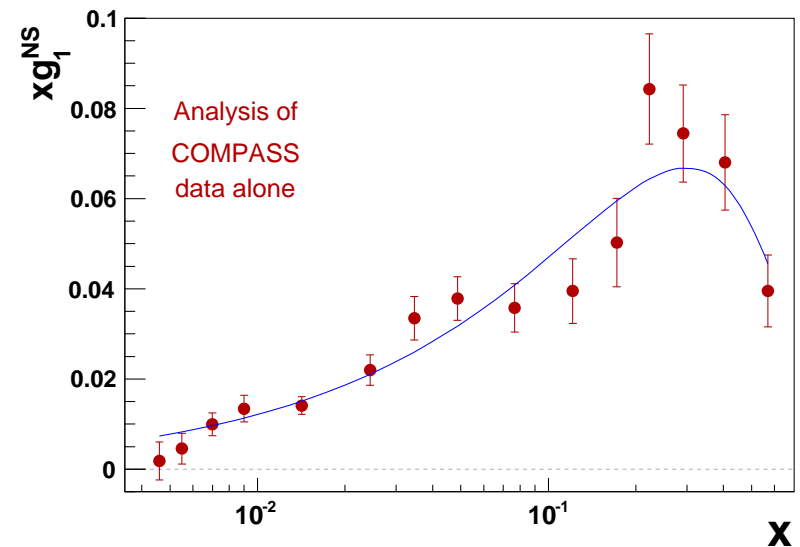
- Parametrization of  $\Delta q_3(x)$ :  $\Delta q_3(x) = \left| \frac{g_A}{g_V} \right| x^\alpha (1-x)^\beta$

$g_A/g_V$	$\alpha$	$\beta$
$1.30 \pm 0.07$	$-0.24 \pm 0.07$	$2.3 \pm 0.4$

### Systematic error

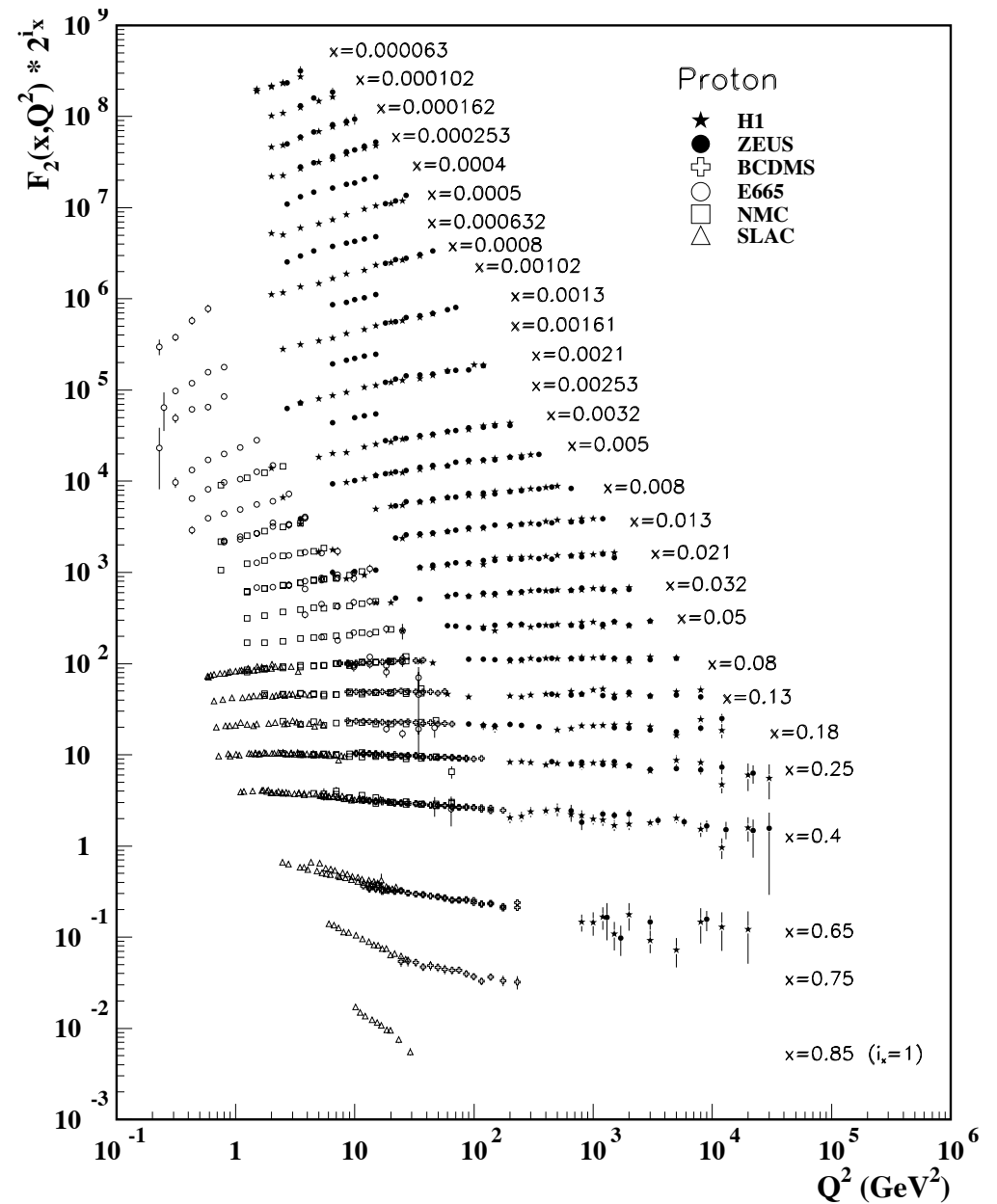
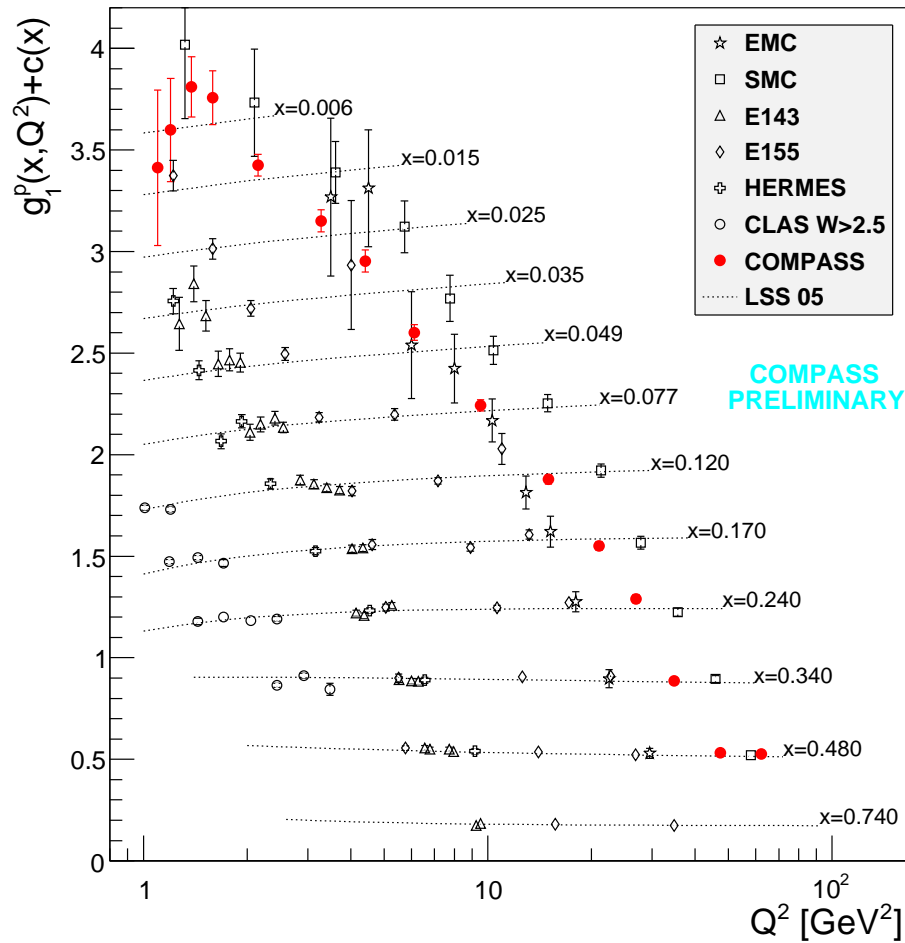
- ◇  $\delta(P_b)$  is the dominant error: 5%  $\Rightarrow \pm 0.065$
- ◇  ${}^6\text{LiD}$ : 7% due to  $f$  and  $P_t$ :  $\Rightarrow \pm 0.041$
- ◇  $\text{NH}_3$ : 3% due to  $f$  and  $P_t$ :  $\Rightarrow \pm 0.056$

$g_A/g_V = 1.30 \pm 0.07(\text{stat}) \pm 0.10(\text{syst})$



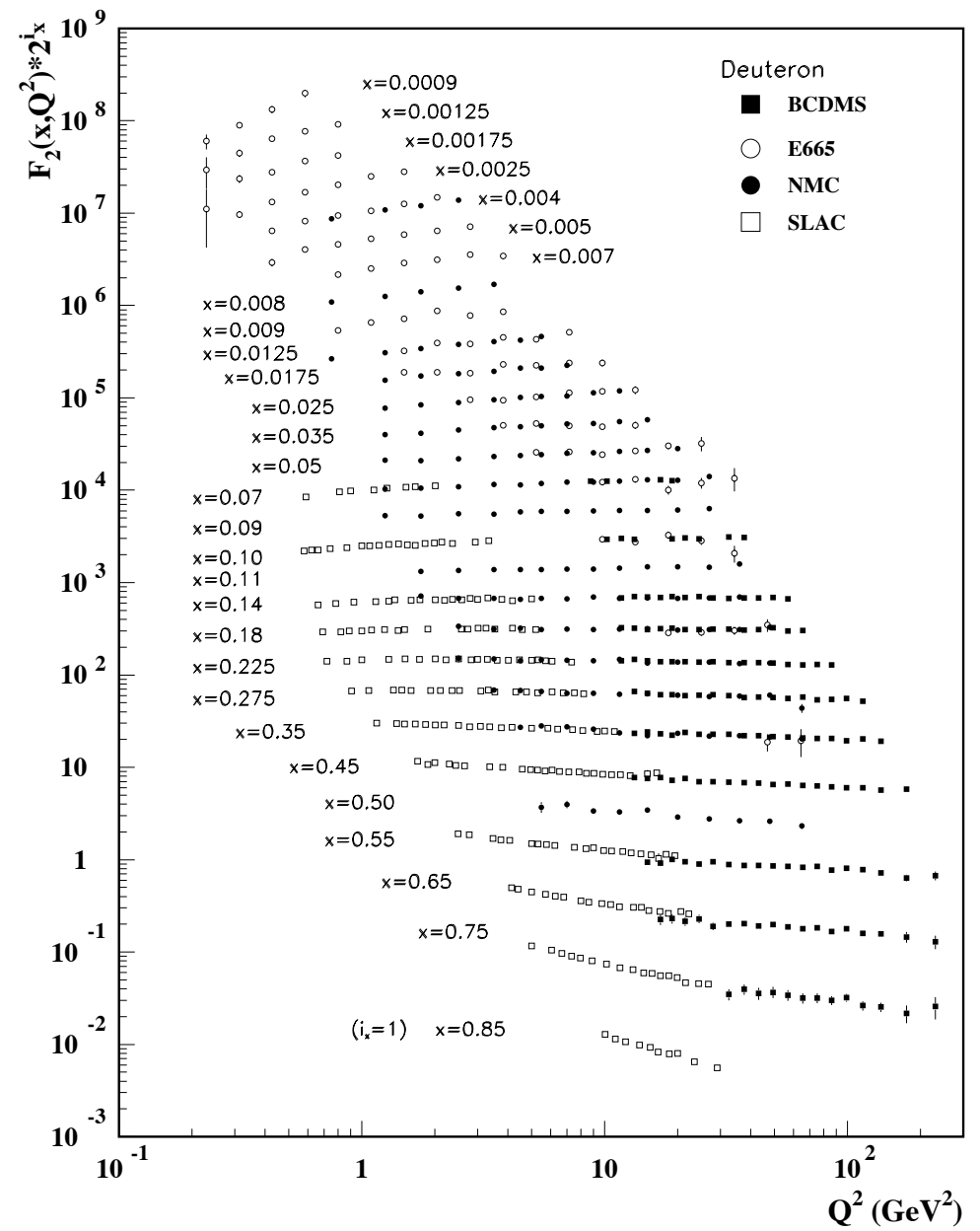
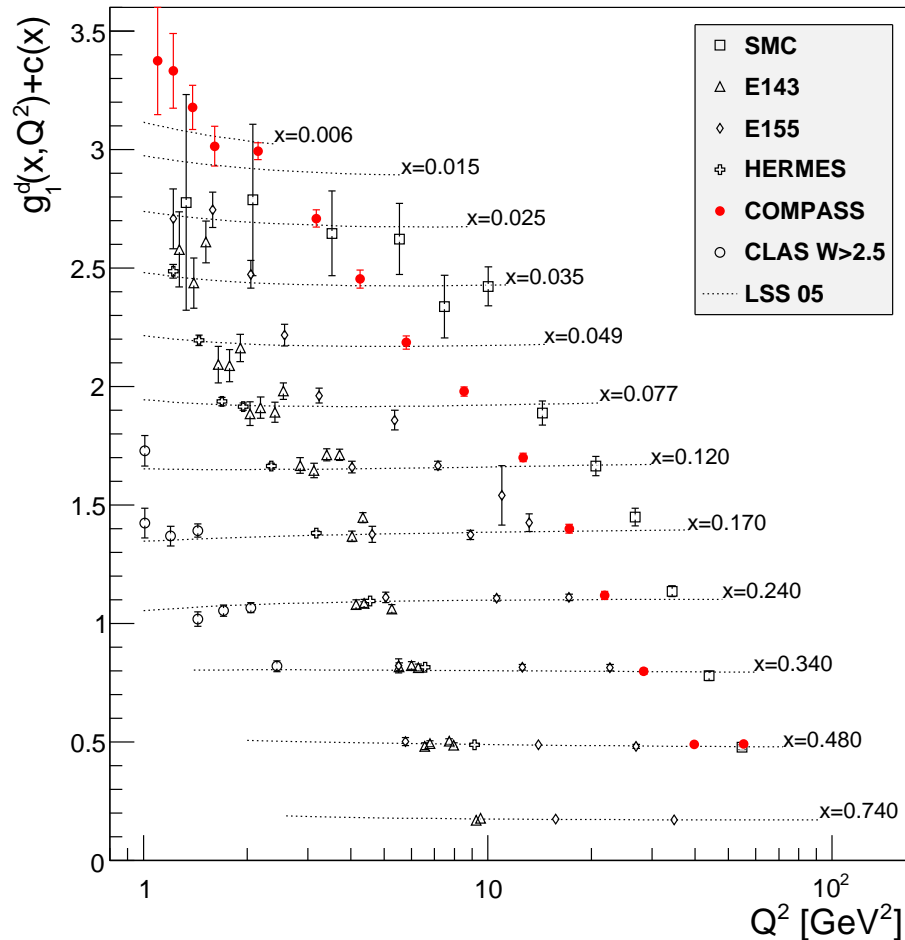
$g_A/g_V^{PDG} = 1.269 \pm 0.003$

# Polarized and unpolarized proton World's data





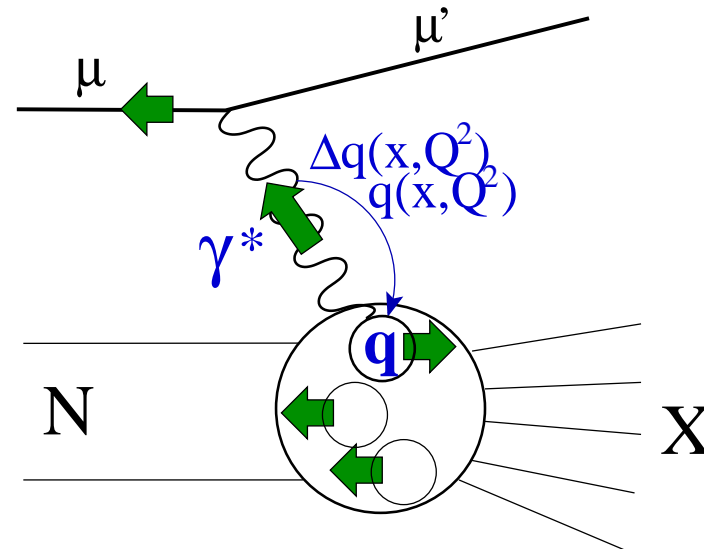
# Polarized and unpolarized deuteron World's data



# Full flavor separation analysis with LO QCD fit

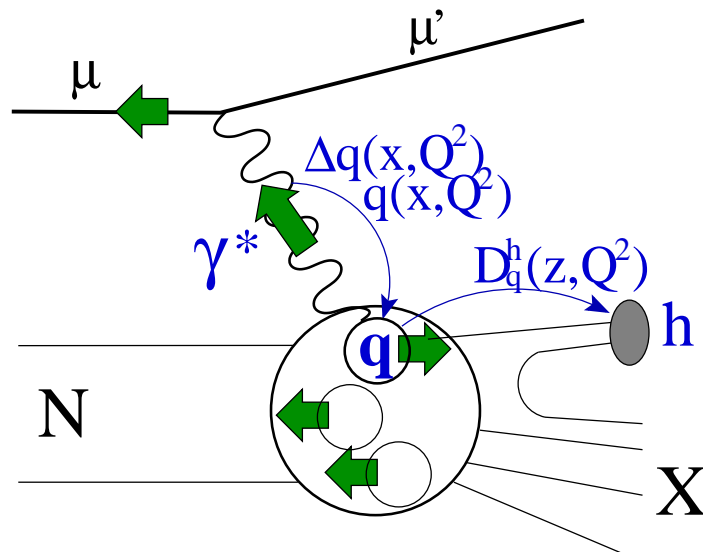
## Inclusive DIS

- Detected particle:  $\mu, \mu'$
- $A_1 = \frac{\sum_q e_q^2 (\Delta q(x) + \Delta \bar{q}(x))}{\sum_q e_q^2 (q(x) + \bar{q}(x))}$
- only  $\Delta q + \Delta \bar{q}$  can be measured



## Semi-Inclusive DIS

- Detected particle:  $\mu, \mu', h, \dots$
- $A_1^h = \frac{\sum_q e_q^2 (\Delta q(x) \int D_q^h dz + \Delta \bar{q}(x) \int D_{\bar{q}}^h dz)}{\sum_q e_q^2 (q(x) \int D_q^h dz + \bar{q}(x) \int D_{\bar{q}}^h dz)}$
- $D_q^h \neq D_{\bar{q}}^h \Rightarrow$  quarks and anti-quarks separation



## Extraction of parton densities

- LO QCD analysis (independent quark fragmentation)

$$A_{1,d} = \frac{5(\Delta\mathbf{u} + \Delta\mathbf{d}) + 5(\Delta\bar{\mathbf{u}} + \Delta\bar{\mathbf{d}}) + 4\Delta\mathbf{s}}{5(u+d) + 5(\bar{u} + \bar{d}) + 2(s + \bar{s})}$$

$$A_d^h = \frac{(4D_u^h + D_d^h)(\Delta\mathbf{u} + \Delta\mathbf{d}) + (4D_{\bar{u}}^h + D_{\bar{d}}^h)(\Delta\bar{\mathbf{u}} + \Delta\bar{\mathbf{d}}) + 2(D_s^h + D_{\bar{s}}^h)\Delta\mathbf{s}}{(4D_u^h + D_d^h)(u+d) + (4D_{\bar{u}}^h + D_{\bar{d}}^h)(\bar{u} + \bar{d}) + 2(D_s^h + D_{\bar{s}}^h)(s + \bar{s})}$$

$$A_{1,p} = \frac{4(\Delta\mathbf{u} + \Delta\bar{\mathbf{u}}) + (\Delta\mathbf{d} + \Delta\bar{\mathbf{d}}) + 2\Delta\mathbf{s}}{4(u + \bar{u}) + (d + \bar{d}) + (s + \bar{s})}$$

$$A_{1,p}^h = \frac{4(D_u^h \Delta\mathbf{u} + D_{\bar{u}}^h \Delta\bar{\mathbf{u}}) + (D_d^h \Delta\mathbf{d} + D_{\bar{d}}^h \Delta\bar{\mathbf{d}}) + (D_s^h + D_{\bar{s}}^h)\Delta\mathbf{s}}{4(D_u^h u + D_{\bar{u}}^h \bar{u}) + (D_d^h d + D_{\bar{d}}^h \bar{d}) + (D_s^h s + D_{\bar{s}}^h \bar{s})}$$

- Matrix form. 10 equations with 5 unknowns

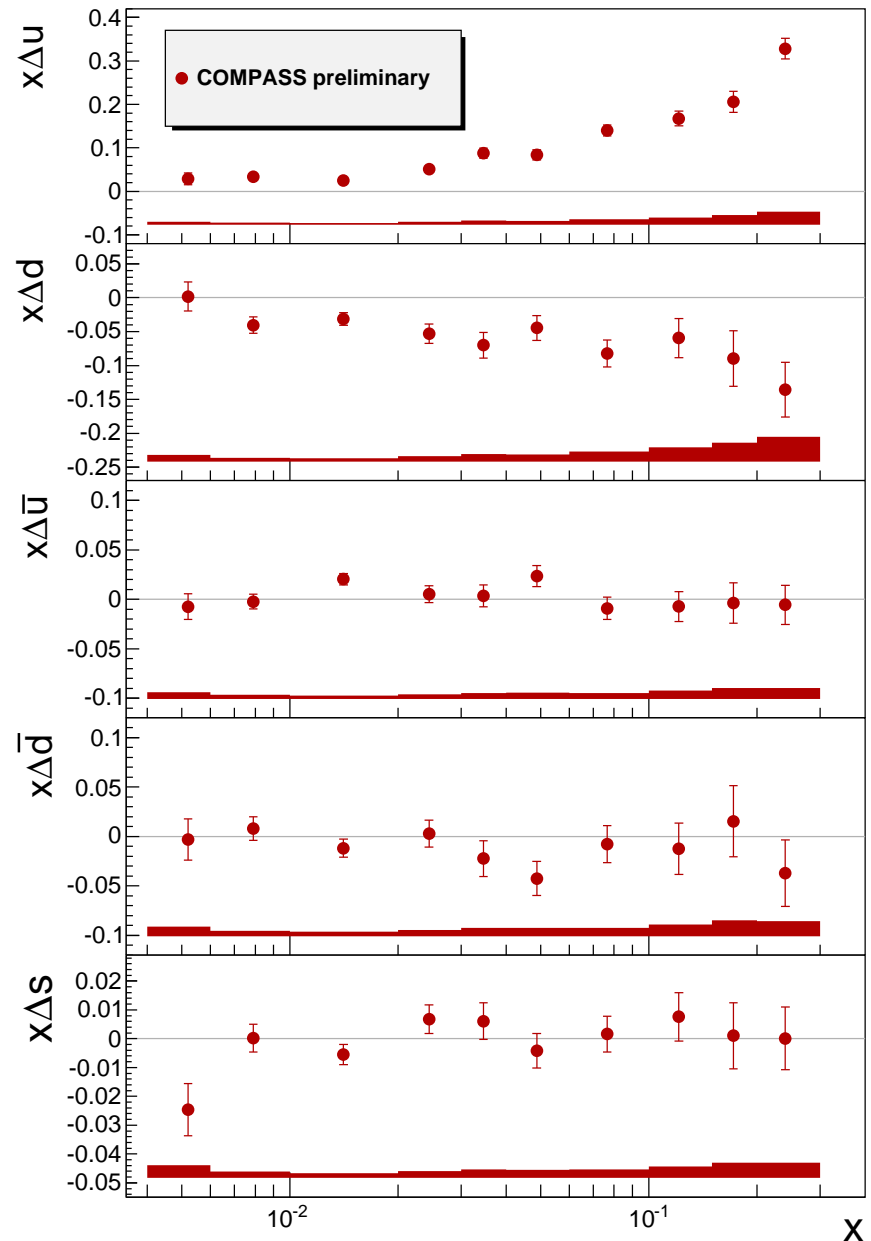
$$\vec{A} = \mathbf{B} \Delta\vec{q}, \quad \text{where} \quad \begin{cases} \vec{A} = (A_1^d, A_d^{\pi^+}, A_d^{\pi^-}, A_d^{K^+}, A_d^{K^-}, A_1^p, A_p^{\pi^+}, A_p^{\pi^-}, A_p^{K^+}, A_p^{K^-}) \\ \Delta\vec{q} = (\Delta u, \Delta d, \Delta\bar{u}, \Delta\bar{d}, \Delta s), \quad \Delta s \equiv \Delta\bar{s} \end{cases}$$

- LS estimation: uniqueness, unbiasedness and minimum variance of the solution

$$\chi^2 = (\vec{A} - \mathbf{B}\Delta\vec{q})^T \text{Cov}_A^{-1} (\vec{A} - \mathbf{B}\Delta\vec{q}).$$

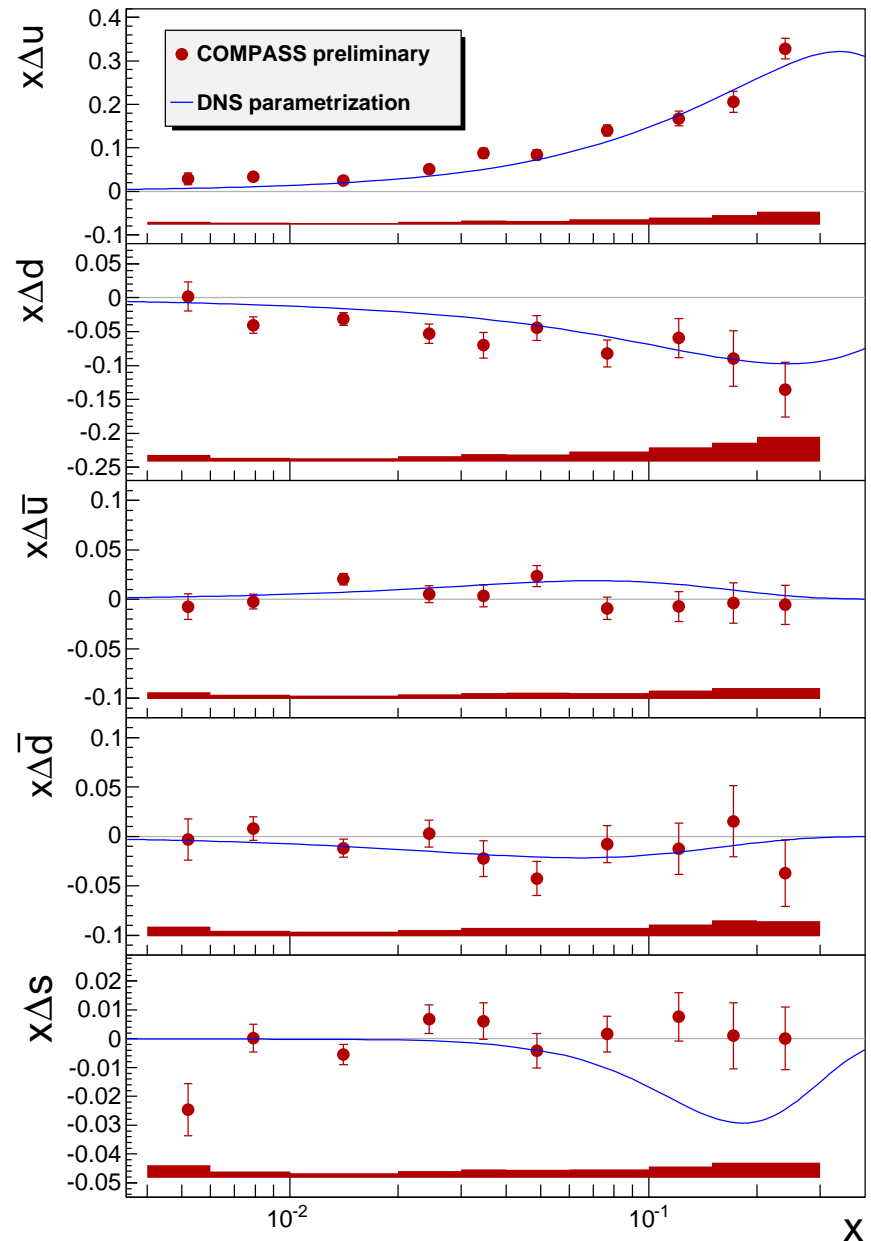
## Results of the fit ( $Q^2=3 \text{ GeV}^2$ )

- MRST04 parametrization is used for unpolarized PDFs
- DSS parametrization is used for FFs: pQCD analysis of electron-positron annihilation, lepton-nucleon DIS and **SIDIS**, hadron-hadron collision data
- All sea-quark distributions are compatible with zero
- Good agreement of  $\Delta u$ ,  $\Delta \bar{u}$ ,  $\Delta d$ ,  $\Delta \bar{d}$  with global fit
- Typical  $x\Delta s(x)$  distribution obtained from QCD fits of  $g_1(x, Q^2)$  data has minimum at  $x \approx 0.2 \Rightarrow$  significant discrepancy is observed



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## Flavor symmetry breaking of the light sea

- Asymmetry between the unpolarized  $\bar{u}$  and  $\bar{d}$  distrib. is well established experimental fact

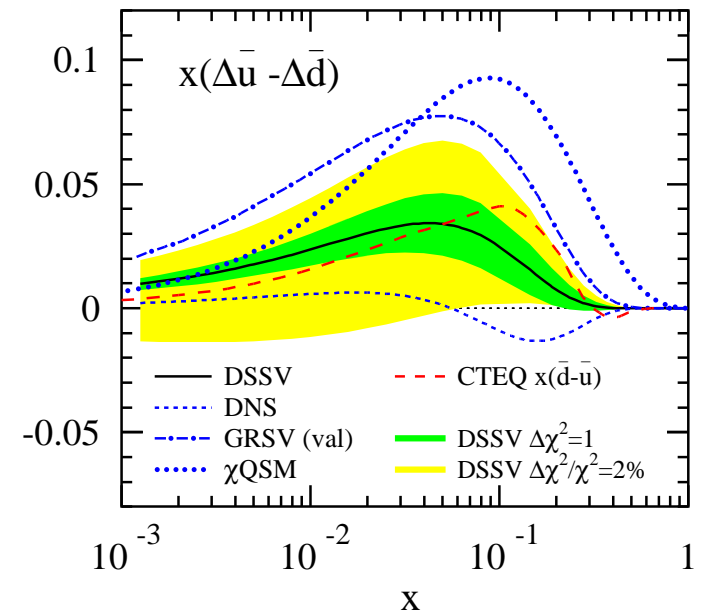
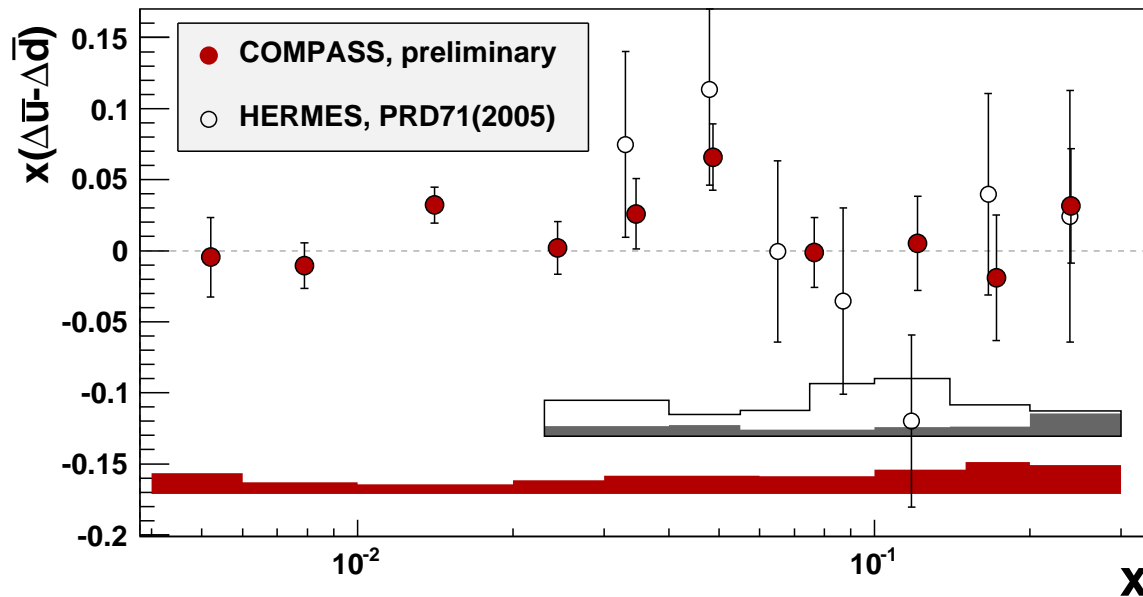
Experiment	$\langle Q^2 \rangle$ [GeV <sup>2</sup> ]	$\int_0^1 [\bar{u} - \bar{d}] dx$	Reference
NMC/DIS	4	$0.147 \pm 0.039$	M.Arneodo et al., Phys.Rev.D55(1994)R1
HERMES/SIDIS	2.3	$0.16 \pm 0.03$	K.Ackerstaff et al., Phys.Rev.Lett.81(1998)5519
FNAL E866/DY	54	$0.118 \pm 0.012$	R.S.Towell et al., Phys.Rev.D64(2001)052002

- Many non-perturbative models predicts a sizable asymmetry of the helicity densities

	Model	$\int_0^1 [\Delta\bar{u} - \Delta\bar{d}] dx$	Reference
	$\pi$ -meson	0	A.W.Thomas, Phys.Lett.B126(1983)97
	$\rho$ -meson	$\simeq -0.0007$ to $-0.027$	R.J.Fries,A.Schafer, Phys.Lett.B443(1998)40
Meson cloud	$\pi$ - $\rho$ interf.	$= -6 \int_0^1 g^p(x) dx \simeq -0.7$	K.G.Boreskov, A.B.Kaidalov, Eur.Phys.J.C10(1999)143
	$\rho$ and $\pi$ - $\rho$ interf.	$\simeq -0.004$ to $-0.033$	F.G.Cao, A.I.Signal, Eur.Phys.J.C21(2001)105
	$\rho$ -meson	$< 0$	S.Kumano, M.Miyama, Phys.Rev.D65(2002)034012
	$\pi$ - $\sigma$ interf.	$\simeq 0.12$	R.J.Fries,A.Schafer,C.Weiss, hep-ph/0204060
Pauli-blocking	bag model	$\simeq 0.09$	F.G.Cao, A.I.Signal, Eur.Phys.J.C21(2001)105
	ansatz	$\simeq 0.3$	M.Gluck et al., Phys.Rev.D63(2001)094005
		$= \frac{5}{3} \int_0^1 [\bar{d} - \bar{u}] dx \simeq 0.2$	F.M.Steffens, Phys.Lett.B541(2002)346
Chiral-quark soliton		0.31	B.Dressler et al., hep-ph/9809487
		$\simeq \int_0^1 2x^{0.12} [\bar{d} - \bar{u}] dx$	M.Wakamatsu, T.Watabe, Phys.Rev.D62(2000)017506
Instanton		$\frac{5}{3} \int_0^1 [\bar{d} - \bar{u}] dx \simeq 0.2$	Dorokhov, hep-ph/0112332
Statistical		$\simeq \int_0^1 [\bar{d} - \bar{u}] dx \simeq 0.12$	C.Bourrely,J.Soffer,F.Buccella, Eur.Ph.J.C23(2002)487
		$> \int_0^1 [\bar{d} - \bar{u}] dx > 0.12$	R.S.Bhalerao, Phys.Rev.C63(2001)025208

taken from J.C.Peng “Flavor Structure of the nucleon sea”, hep-ph/0301053

## Flavor symmetry breaking of the light sea



- Presently  $\Delta\bar{u} - \Delta\bar{d}$  is accessible only via SIDIS processes

HERMES( $Q^2 = 2.5 \text{ GeV}^2$ ) :  $\int_{0.023}^{0.3} (\Delta\bar{u} - \Delta\bar{d}) dx = 0.048 \pm 0.057(\text{stat}) \pm 0.028(\text{syst})$

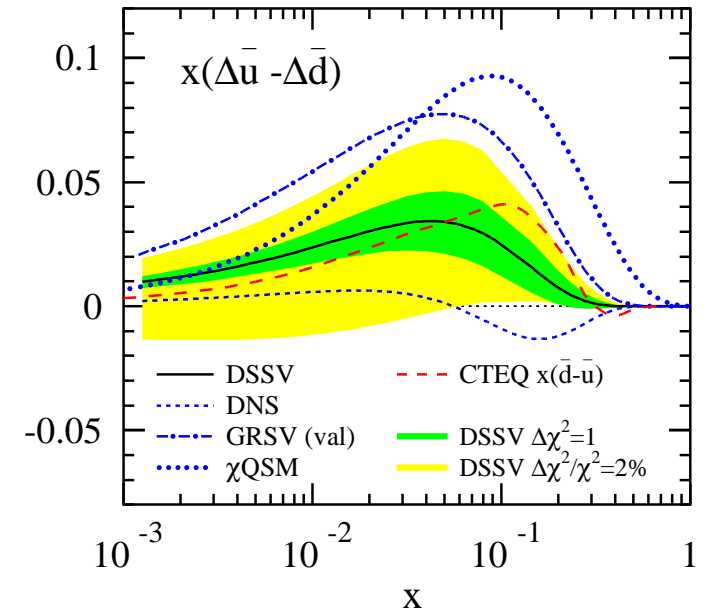
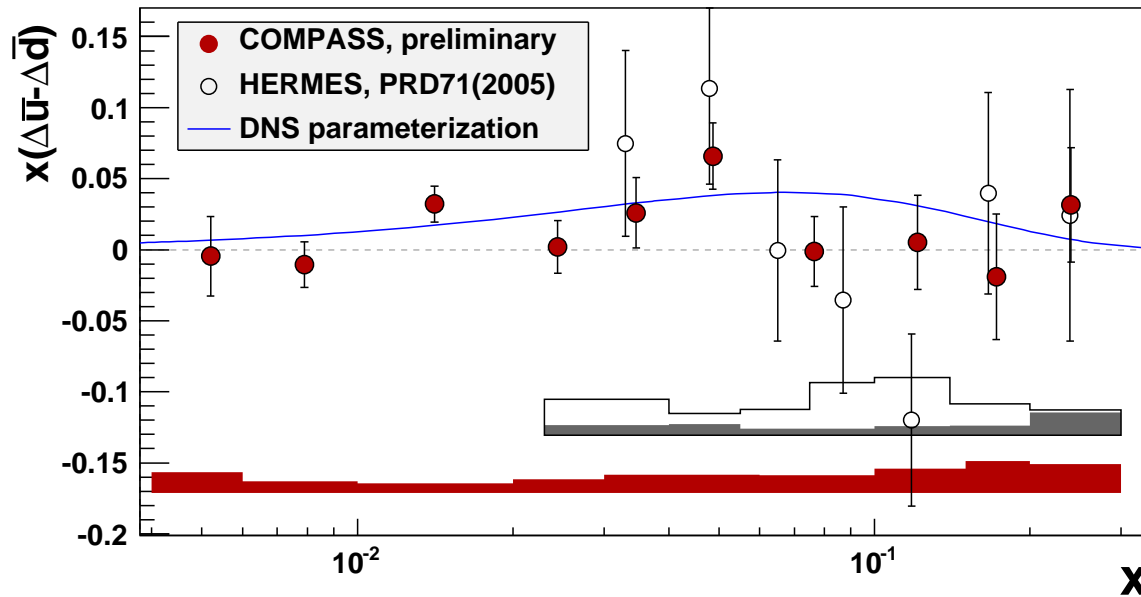
COMPASS( $Q^2 = 3 \text{ GeV}^2$ ) :  $\int_{0.004}^{0.3} (\Delta\bar{u} - \Delta\bar{d}) dx = 0.052 \pm 0.035(\text{stat}) \pm 0.013(\text{syst})$

- Present analysis: no estimation of systematics coming from uncertainties of FF
- Strength of the effect is comparable to the one observed in unpolarized case

$$\int_0^1 (\bar{u} - \bar{d}) dx = 0.118 \pm 0.012$$



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$$\int_0^1 (\bar{u} - \bar{d}) dx = 0.118 \pm 0.012$$

## Summary

- All COMPASS data with deuteron (2002-2006) and proton (2007) targets have been processed and analyzed
- Combined analysis of proton and deuteron data
  - ◇ Non-singlet structure function  $g_1^{NS}$  and Bjorken sum rule

$$g_A/g_V = 1.30 \pm 0.07(stat) \pm 0.10(syst)$$

- ◇ Full flavor separation analysis with LO QCD fit
  - \* Good agreement of non-strange PDFs with results of previous QCD fits
  - \* Shape of  $\Delta s(x)$  disagrees significantly with previous fits
  - \* Flavor asymmetry of the light sea quarks have been observed  $\Delta\bar{u} \gtrsim \Delta\bar{d}$
- Proposal for a one more year (2011) with longitudinally polarized proton target has been submitted for SPSC