

**“Inclusive spin-dependent  
asymmetry  
 $A_1$  from COMPASS”**

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*JINR, Dubna*

**on behalf of the COMPASS collaboration**

*Hadron Structure and QCD: from low to high energies  
Gatchina, Russia, 30 June-4 July 2008*

# Overview:

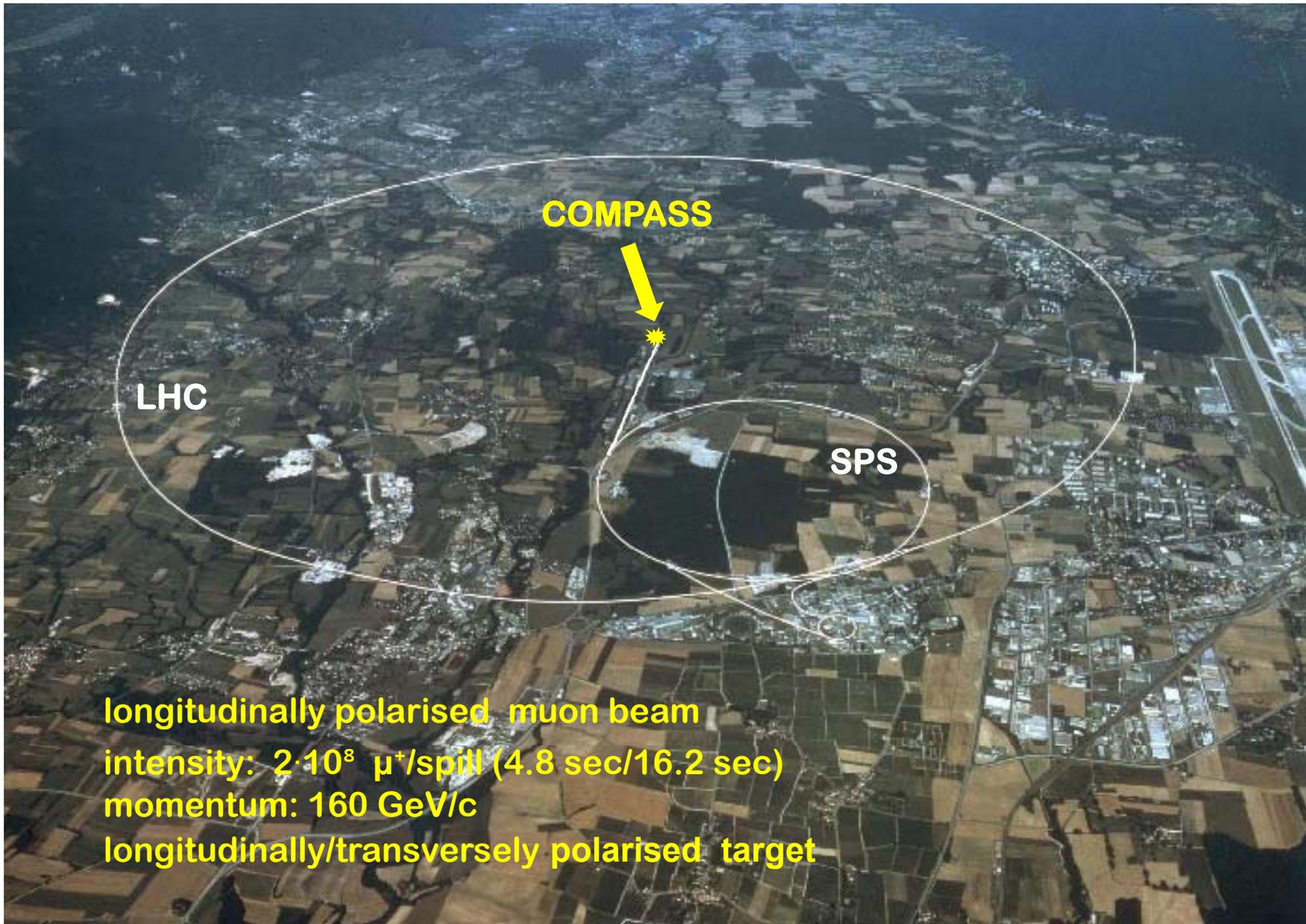
- **COMPASS experiment**
- **Spin of the nucleon and deep-inelastic scattering**
- **Inclusive asymmetry  $A_1$  and structure function  $g_1$**
- **QCD analysis**
- **Summary and outlook**



**CO**mmon  
**M**uon and  
**P**roton  
**A**pparatus for  
**S**tructure and  
**S**pectroscopy

***28 Institutes: Bielefeld, Bochum, Bonn, Calcutta, CERN,  
Dubna, Erlangen, Freiburg, Lisbon, Mainz,  
Moscow, Munich, Prague, Protvino, Saclay,  
Tel Aviv, Torino, Trieste, Yamagata, Warsaw***

***~ 230 physicists***



**longitudinally polarised muon beam**  
**intensity:  $2 \cdot 10^8 \mu^+/\text{spill}$  (4.8 sec/16.2 sec)**  
**momentum: 160 GeV/c**  
**longitudinally/transversely polarised target**

# Physics program of COMPASS

## With $\mu$ beam

*Spin dependent structure functions*

*Polarized quark distributions*

*Gluon polarization*

*Transversity*

*Lambda polarization*

*Vector meson production*

## With hadron beam

*Pion and Kaon polarizabilities*

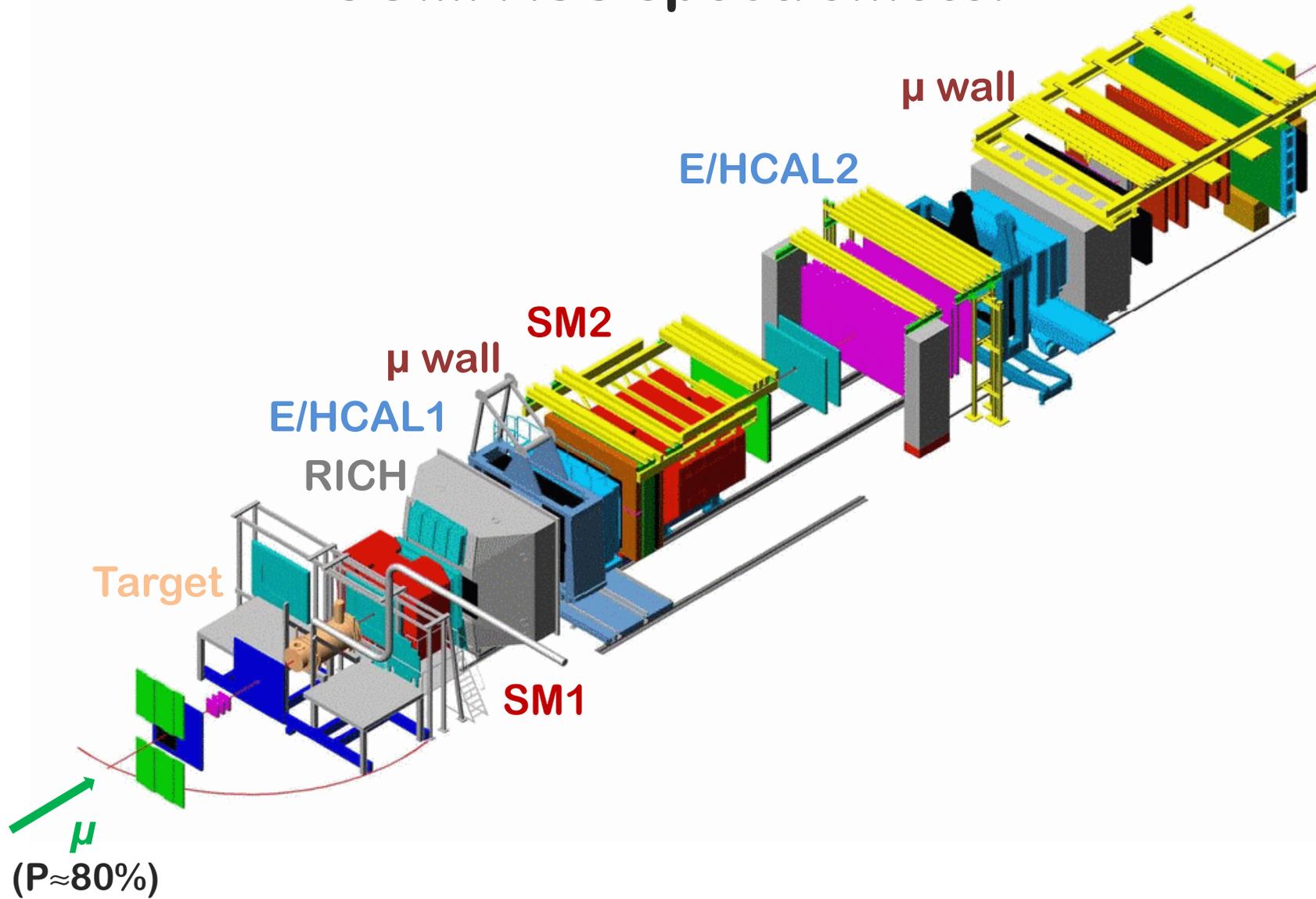
*Diffraction production of exotic states*

*Search for glueball*

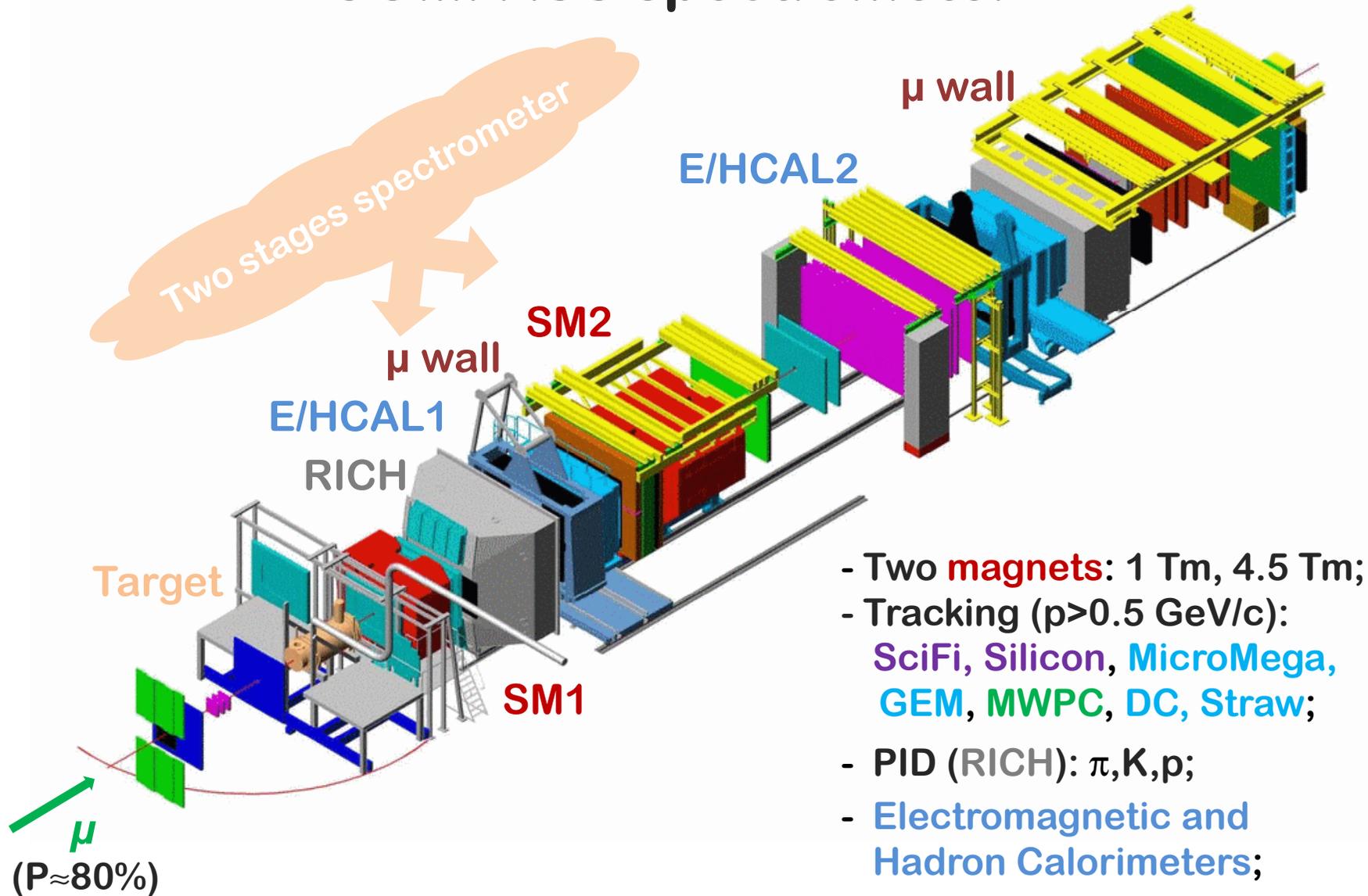
*Light meson spectroscopy*

*Production of double charmed baryons*

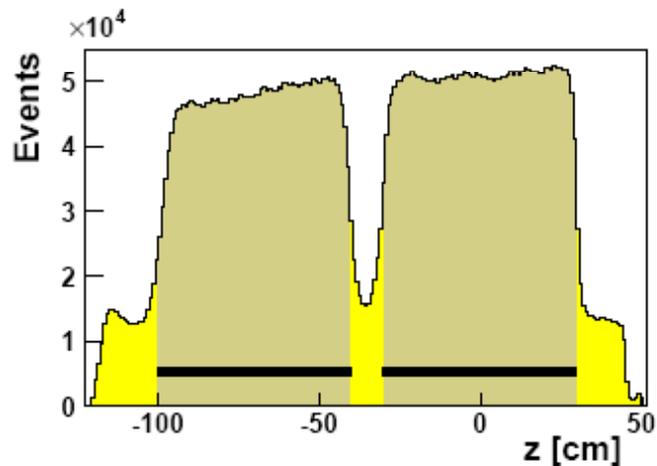
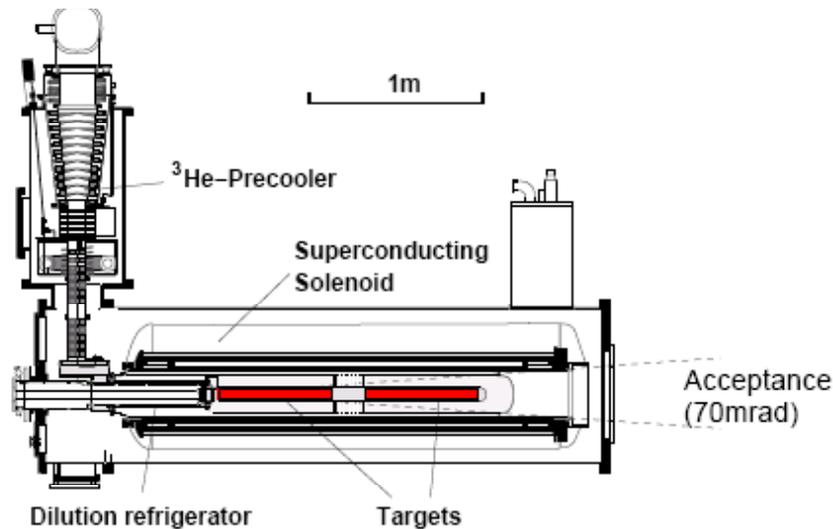
# COMPASS spectrometer



# COMPASS spectrometer



# COMPASS polarized target 2002-2004

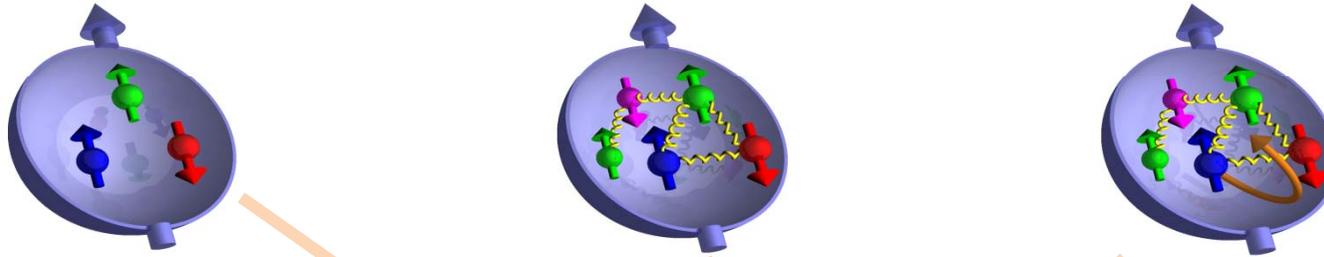


2 cells polarized target  
<sup>6</sup>LiD (50%)

- polarization:  $P > 50\%$
- dilution factor:  $\sim 0.4$
- **D**ynamic **N**uclear **P**olarization
- solenoid field: 2.5T
- acceptance: 70mrad
- <sup>3</sup>He/ <sup>4</sup>He:  $t_{\min} \approx 50\text{mK}$
- two 60cm long target cells with opposite polarization
- regular spin reversal

# Spin of the nucleon & Deep-inelastic scattering

# Spin of the nucleon



$$\mathbf{S}_N = \frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + \underbrace{L_q + L_g}$$

**Constituent parton model:**

$$\Delta\Sigma = \Delta u_v + \Delta d_v = 1$$

**Complete description :**

- $\Delta\Sigma = \Delta u + \Delta d + \Delta s$  (for  $q$  and  $\bar{q}$ )
- $\Delta G$
- orbital angular momenta

# Deep inelastic scattering

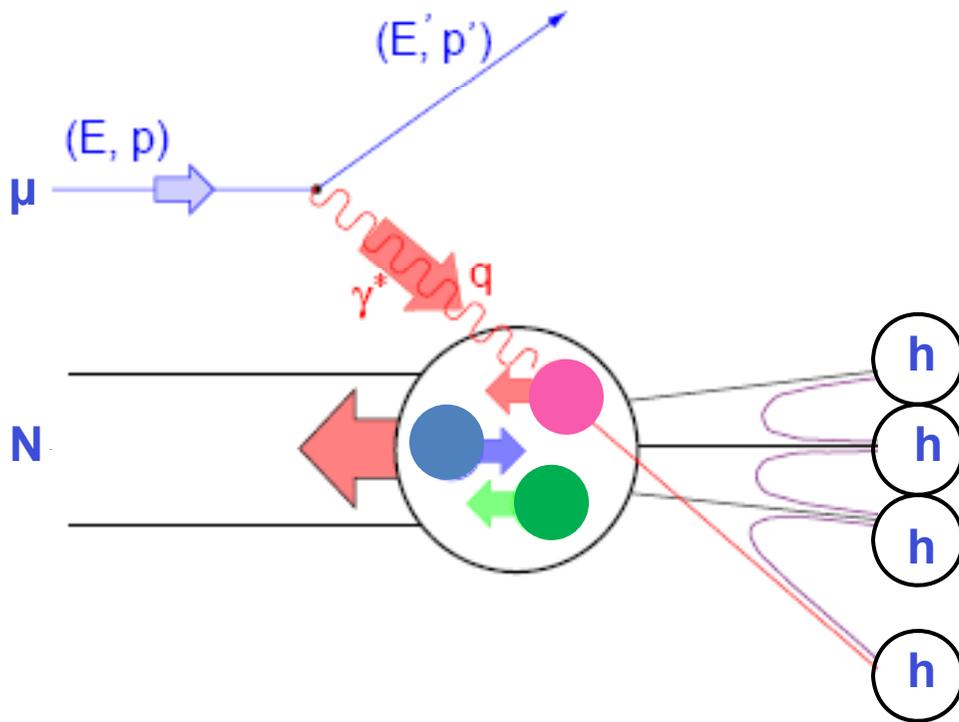
Kinematical variables:

$$Q^2 = -q^2$$

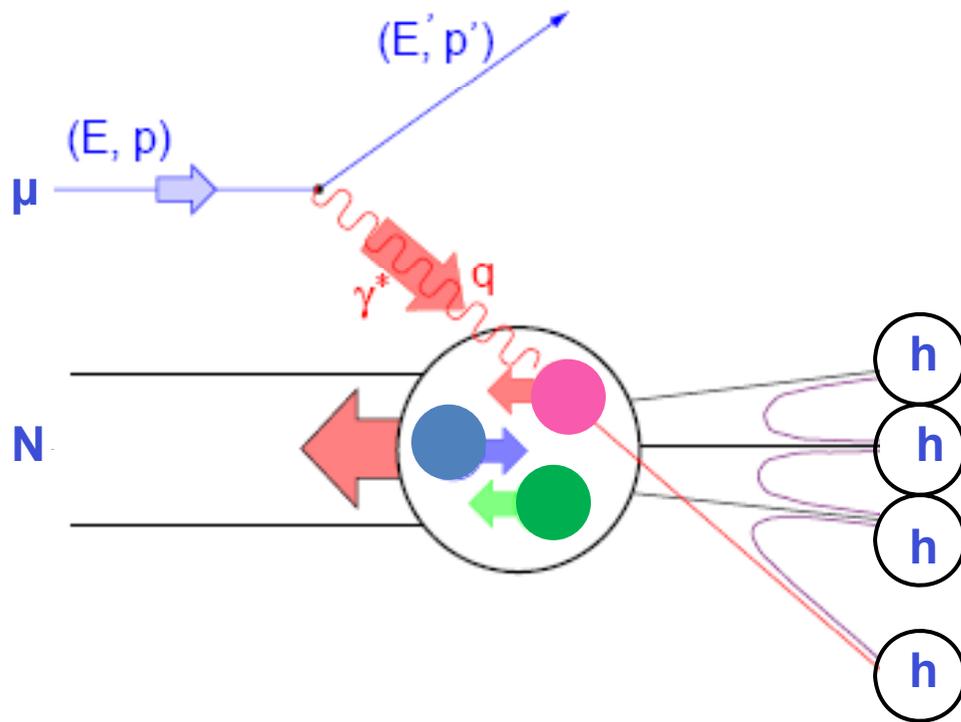
$$x = Q^2/2Mv$$

$$v = E - E'$$

$$y = v/E$$



# Deep inelastic scattering



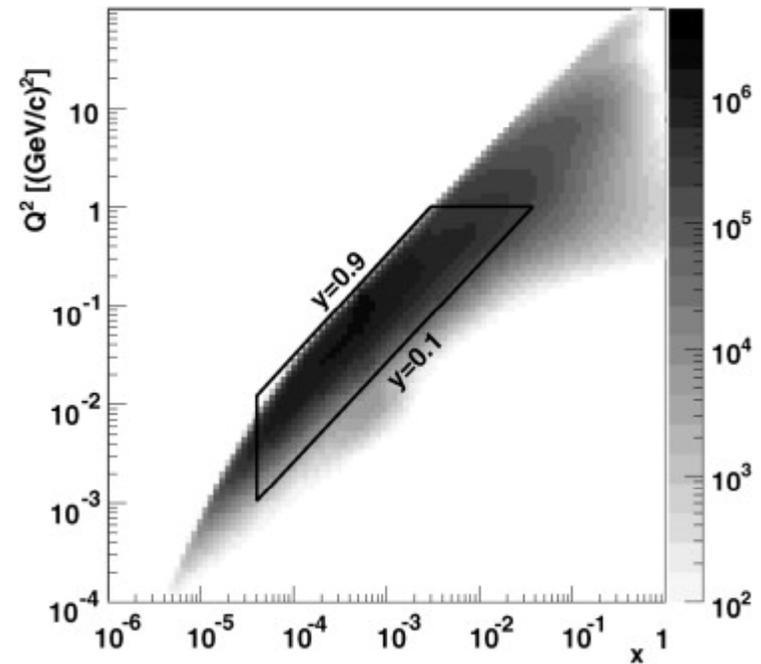
Kinematical variables:

$$Q^2 = -q^2$$

$$x = Q^2/2Mv$$

$$v = E - E'$$

$$y = v/E$$



# Deep inelastic scattering

- quark densities in QPM:

$$q(x) = q^+(x) + q^-(x)$$

$$\Delta q(x) = q^+(x) - q^-(x)$$

- Longitudinal double-spin asymmetry:

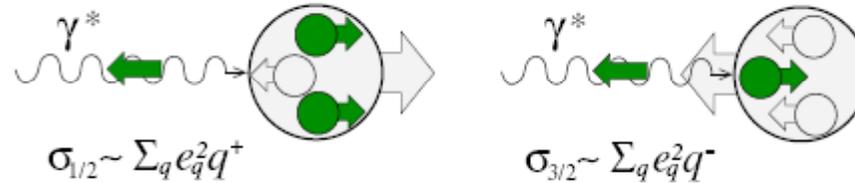
- Cross-sections

and

Structure functions:

$$\bar{\sigma}(x, Q^2) = aF_1(x, Q^2) + bF_2(x, Q^2)$$

$$\Delta\sigma(x, Q^2) = \alpha g_1(x, Q^2) + \beta g_2(x, Q^2)$$



$$A^{\gamma N} \equiv A_1 = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}} = \frac{\sum_q e_q^2 \Delta q}{\sum_q e_q^2 q}$$

- Longitudinal spin asymmetry  $\mu N$ :

$$A^{\mu N} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} = \frac{\Delta\sigma}{\bar{\sigma}} \simeq DA_1$$

$D$  – depolarization factor of  $\gamma$

- Structure functions and PDF:

$$F_1 = \frac{1}{2} \sum_q e_q^2 (q + \bar{q}), \quad g_1 = \frac{1}{2} \sum_q e_q^2 (\Delta q + \Delta \bar{q})$$

- Asymmetry  $A_1$  and structure function  $g_1$ :  $g_1 \approx A_1 \cdot F_1$

# Method

- to be measured:  $A_{\parallel} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}}$

- measured values:  $N_u, N_d, N'_u, N'_d$

- flux normalization:  $\frac{\Phi_u}{\Phi_d} = 1$

- acceptance: (constant ratio)  $\frac{x'_d}{x'_u} = 1$

- double ratio method:  $\delta = \frac{N_u \cdot N'_d}{N'_u \cdot N_d}$

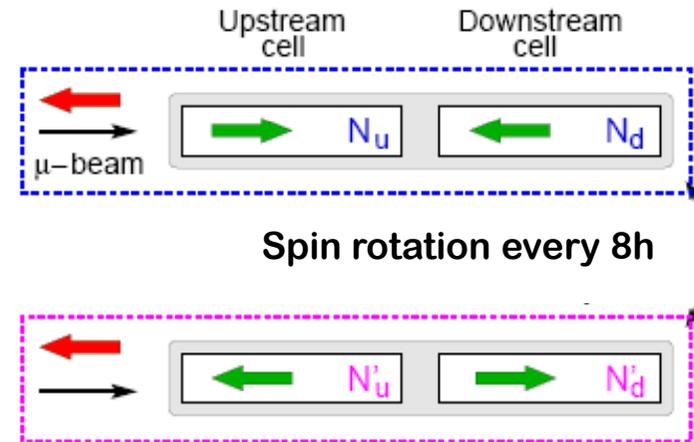
⇒ solve for  $A_{\text{exp}}$  (2<sup>nd</sup> order equation)

⇒ minimization of bias

- experimental asymmetry:  $A_{\text{exp}} = \rho_{\mu} \rho_T f A_{\parallel}$

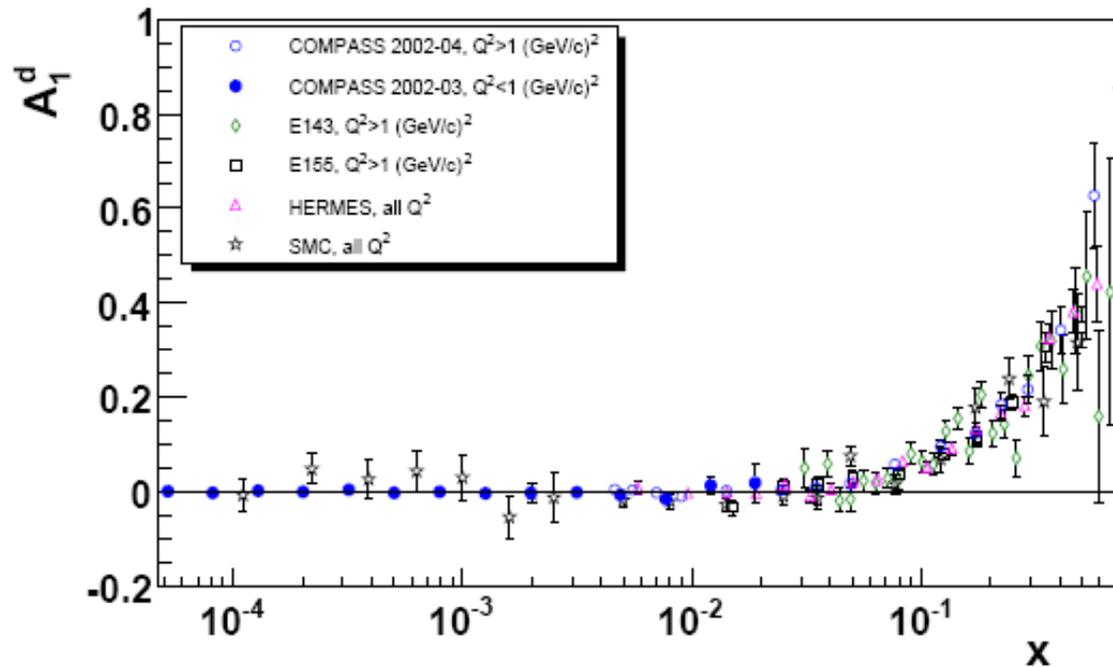
$\rho_{\mu}, \rho_T$  - beam and target polarization

$f$  - dilution factor



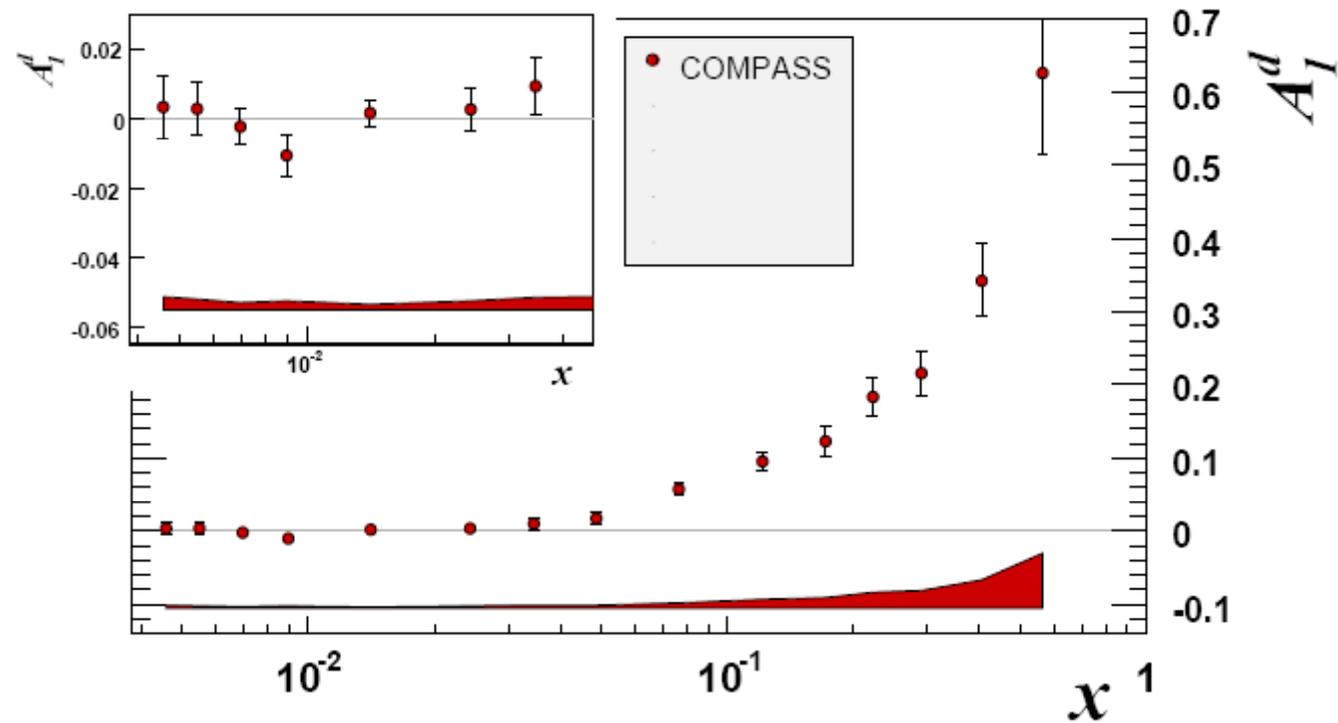
# Inclusive asymmetry $A_1$

# Inclusive asymmetry for $Q^2 < 1 \text{ (GeV/c)}^2$



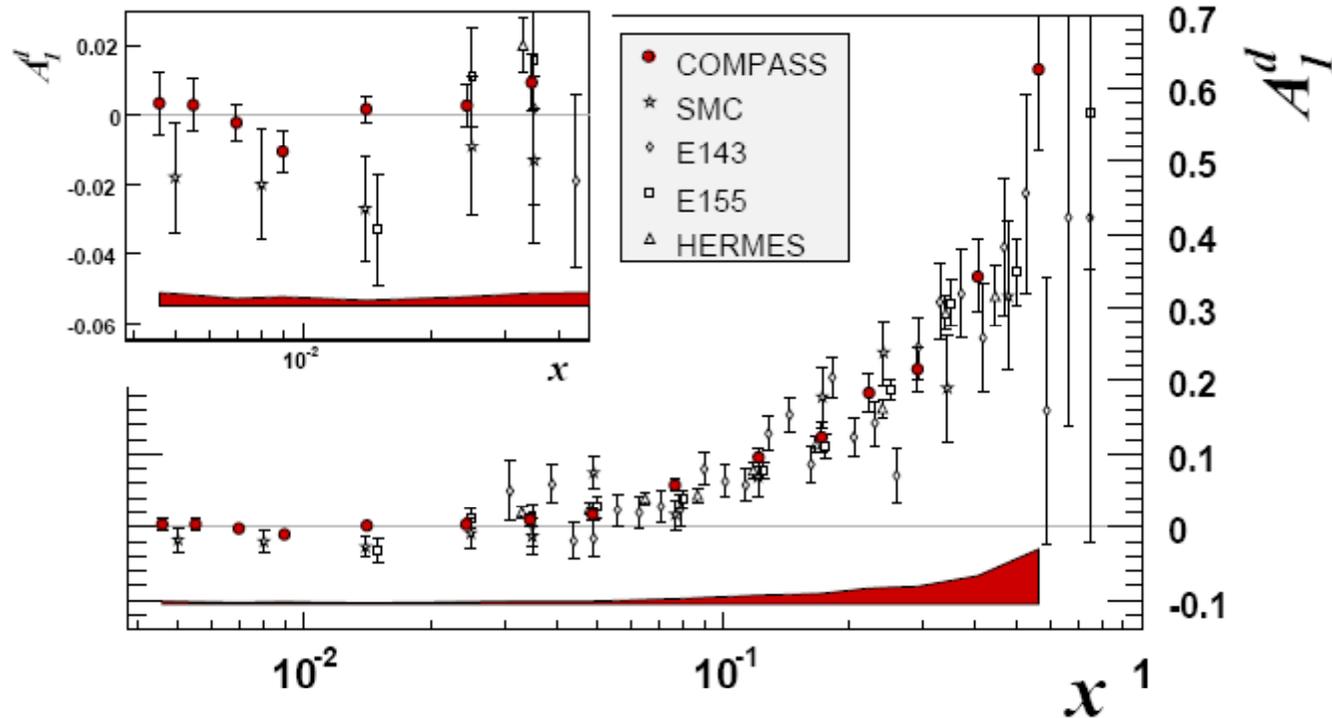
- Results are published in PLB 647(2007)330
- Systematic error mainly due to false asymmetries
- $A_1^d$  is compatible with **0** at small  $x$
- **$3 \cdot 10^8$**  events: factor 10-20 improvement in statistical errors compared to SMC

# Inclusive asymmetry for $Q^2 > 1 \text{ (GeV/c)}^2$



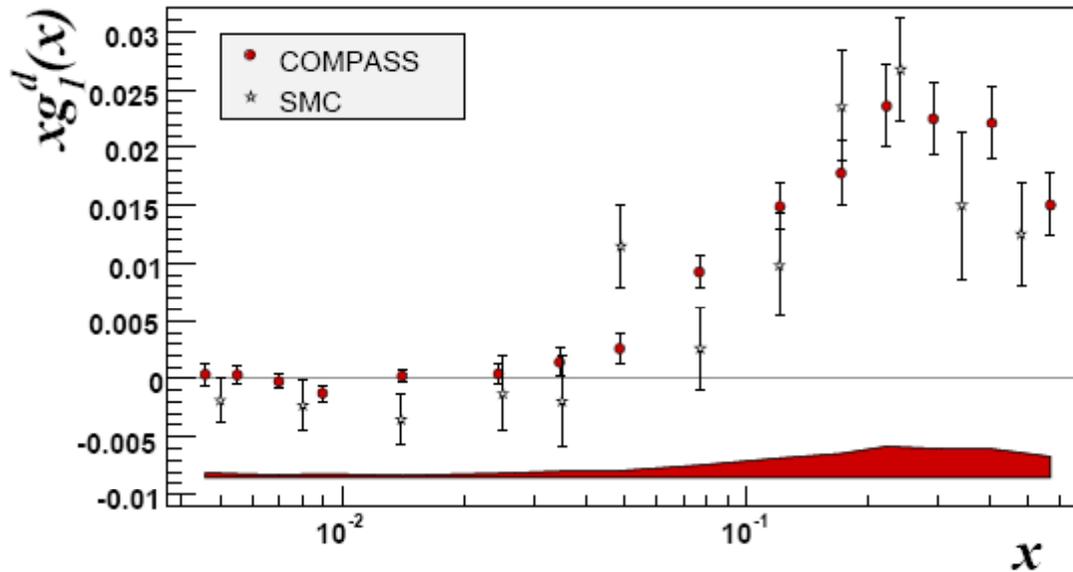
- Results are published in PLB 647(2007) 8
- Systematic errors:  $p_\mu$  (5%),  $p_T$  (5%),  $f$  (2÷3%),  $D$  (6%)  $\rightarrow \delta A_1 \approx 0.1 A_1$
- **$88 \cdot 10^6$**  events for  $0.7 > x > 0.004$ ,  $0.1 < y < 0.9$

# Inclusive asymmetry for $Q^2 > 1 \text{ (GeV/c)}^2$

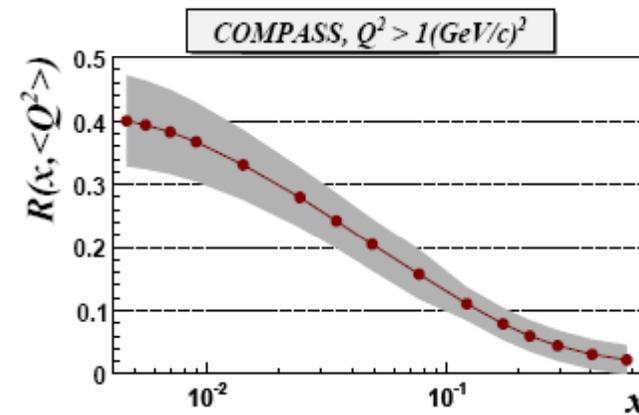
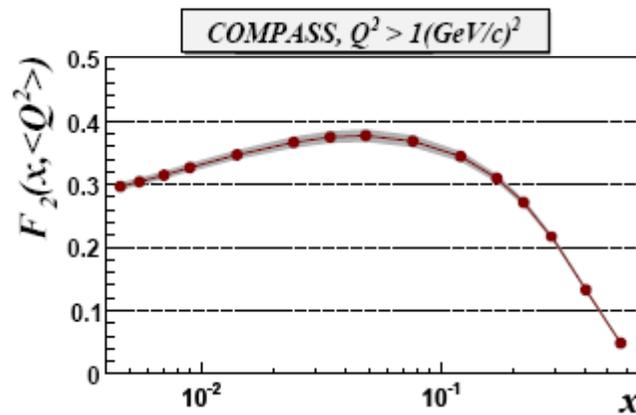


- Results are published in PLB 647(2007) 8
- $A_1^d$  is compatible with 0 for  $x < 0.05$
- good agreement with previous experiments

# Structure function $g_1(x)$ at measured $Q^2$



$$g_1 = A_1 \cdot \frac{F_2}{2x(1 + R)}$$



# First moment of $g_1$

- COMPASS data only

$$\Gamma_1^N(Q^2 = 3(\text{GeV}/c)^2) = \int_0^1 g_1^N(x) dx$$

$$= 0.0502 \pm 0.0028(\text{stat}) \pm 0.0020(\text{evol.}) \pm 0.0051(\text{syst.})$$

- data for  $0.004 < x < 0.7$ , QCD fit used for extrapolation
- contribution of unmeasured region about 3%

- using  $\Gamma_1^N = \frac{1}{9}(1 - \frac{\alpha_s(Q^2)}{\pi} + O(\alpha + s^2))(a_0(Q^2) + \frac{1}{4}a_8)$

$$a_0(Q^2 = 3(\text{GeV}/c)^2) = 0.35 \pm 0.03(\text{stat}) \pm 0.05(\text{syst})$$

- extrapolation  $Q^2 \rightarrow \infty$ :  $\hat{a}_0 = 0.33 \pm 0.03(\text{stat.}) \pm 0.05(\text{syst.}) = \Delta\Sigma$

$$(\Delta s + \Delta \bar{s}) = \frac{1}{3}(\hat{a}_0 + a_8) = -0.08 \pm 0.01(\text{stat.}) \pm 0.02(\text{syst.})$$

- negative strange sea polarization

# QCD analysis

# QCD analysis

- Measured structure functions  $g_1^{p,n,d}$ (different  $x, Q^2$ )

$$g_1(x, Q^2) = \frac{1}{2} \langle e^2 \rangle \left[ C_q^S \otimes \Delta\Sigma + C_q^{NS} \otimes \Delta q^{NS} + 2n_f C_G \otimes \Delta G \right]$$

- Two programs have been used:
  1. Numerical integration in  $x - Q^2$  space (Phys.Rev.D58(1998)112002)
  2. Solution of DGLAP in space of moments (Phys.Rev.D70(2004)074032)

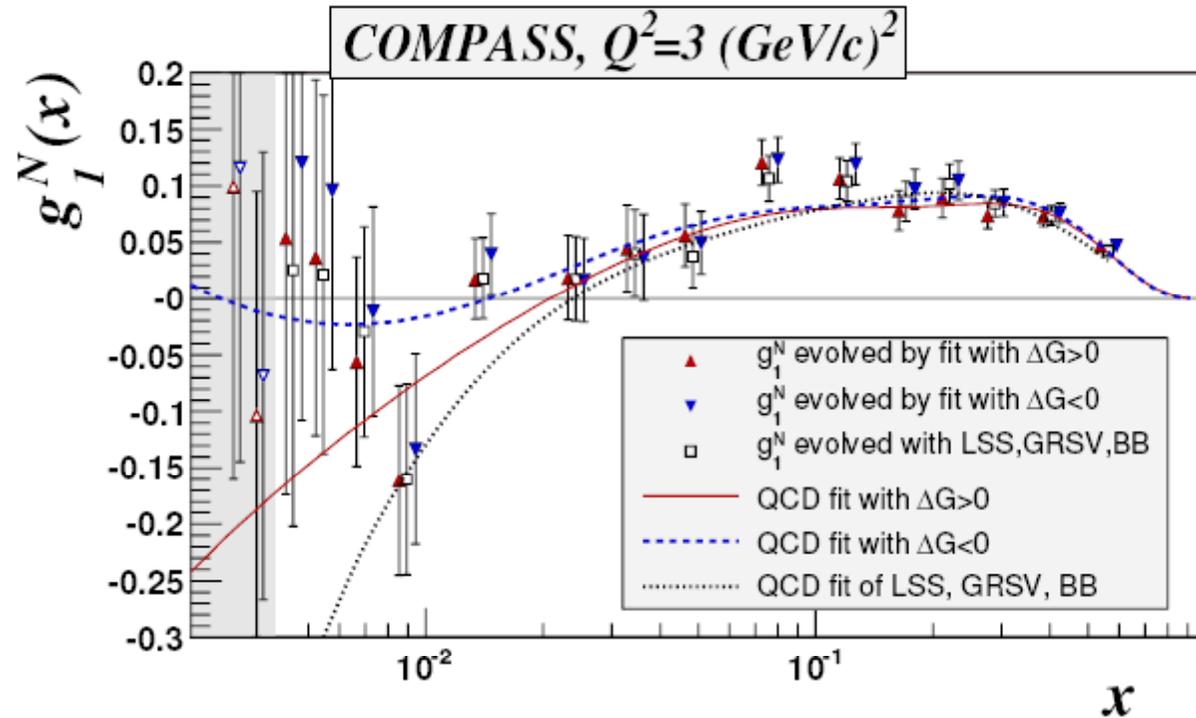
- NLO calculation in  $\overline{\text{MS}}$  scheme

- Initial parametrization ( $x$ -dependence at fixed  $Q^2$ )

$$\Delta\Sigma = \eta \frac{x^\alpha (1-x)^\beta (1+\gamma x)}{\int_0^1 x^\alpha (1-x)^\beta (1+\gamma x) dx}, \quad (\Delta q_3, \Delta q_8, \Delta G) = \eta \frac{x^\alpha (1-x)^\beta}{\int_0^1 x^\alpha (1-x)^\beta dx}$$

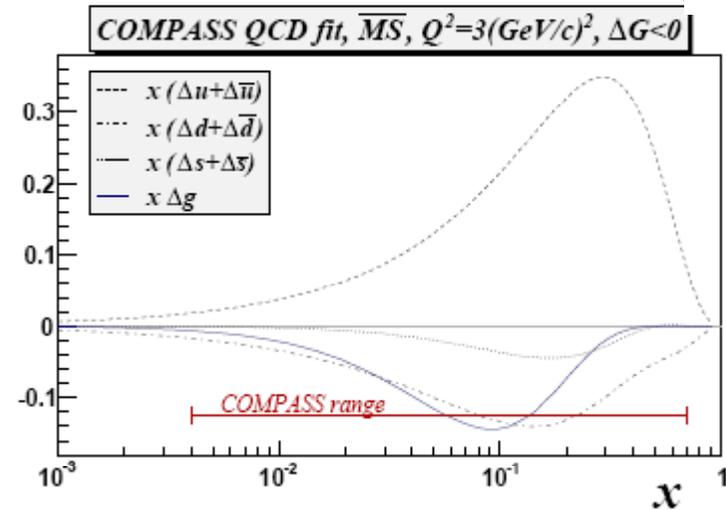
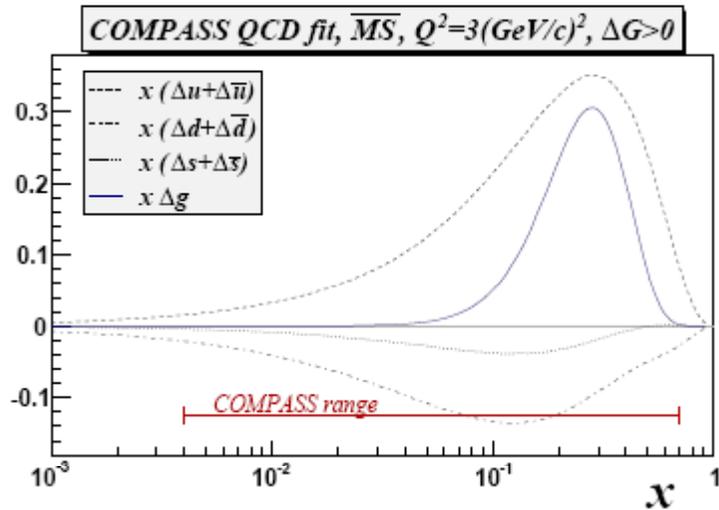
- World data fit: 230 experimental points from 9 experiments
- Two solutions have been found: describe data equally well and correspond to  $\Delta G > 0$  and  $\Delta G < 0$

# QCD analysis



Fit of world data (except final  $g_1^d$  from HERMES)

# Polarized parton distribution

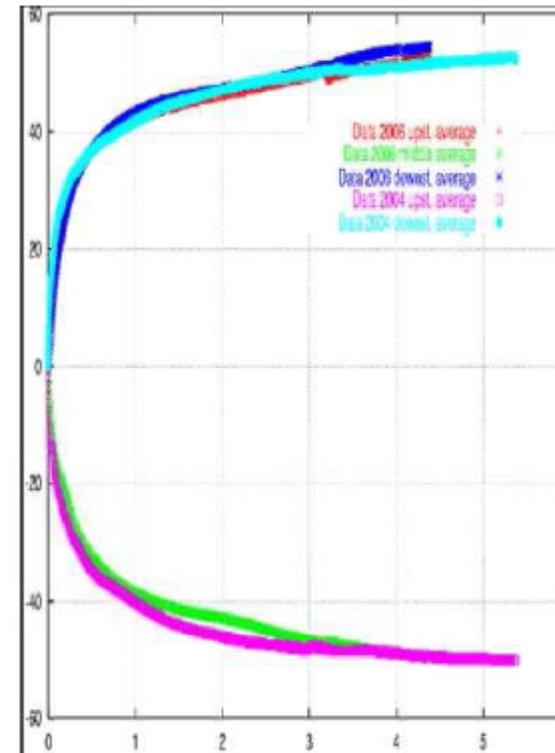
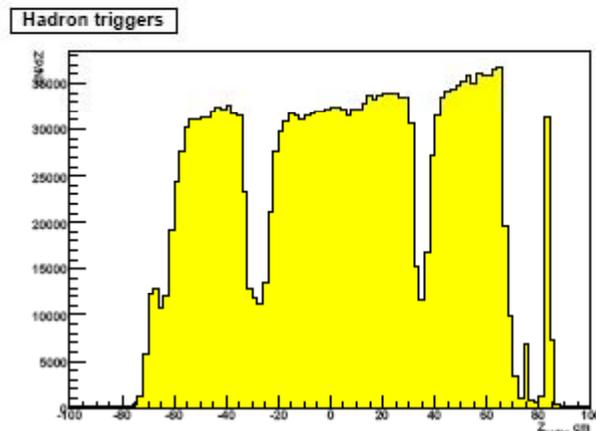


- $\Delta\Sigma = 0.30 \pm 0.01(\text{stat.}) \pm 0.02(\text{evol.})$
- **Small sensitivity to the gluon polarization**
- **Gluon polarization  $|\Delta G| \approx 0.2 \div 0.3$**

# 2006-2007 data

# Data taking 2006

- target material:  ${}^6\text{LiD}$
- longitudinal polarization
- increase statistics by about 40%
- larger increase at high  $x$  and  $Q^2$  (acceptance)
- reconstruction finished

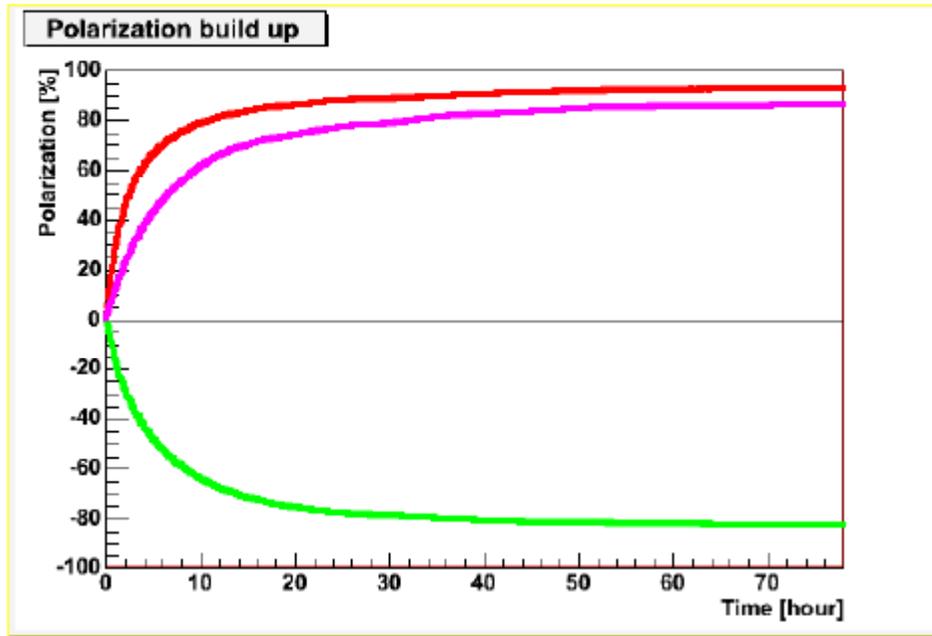


Polarization of  ${}^6\text{LiD}$  in 2006:  
53.5%    -52%    56.2%

Higher and faster than in 2004

# Data taking 2007

- longitudinal and transverse polarizations
- new trigger with use of ECAL1
- integrated beam flux about 30% of 2002-2006



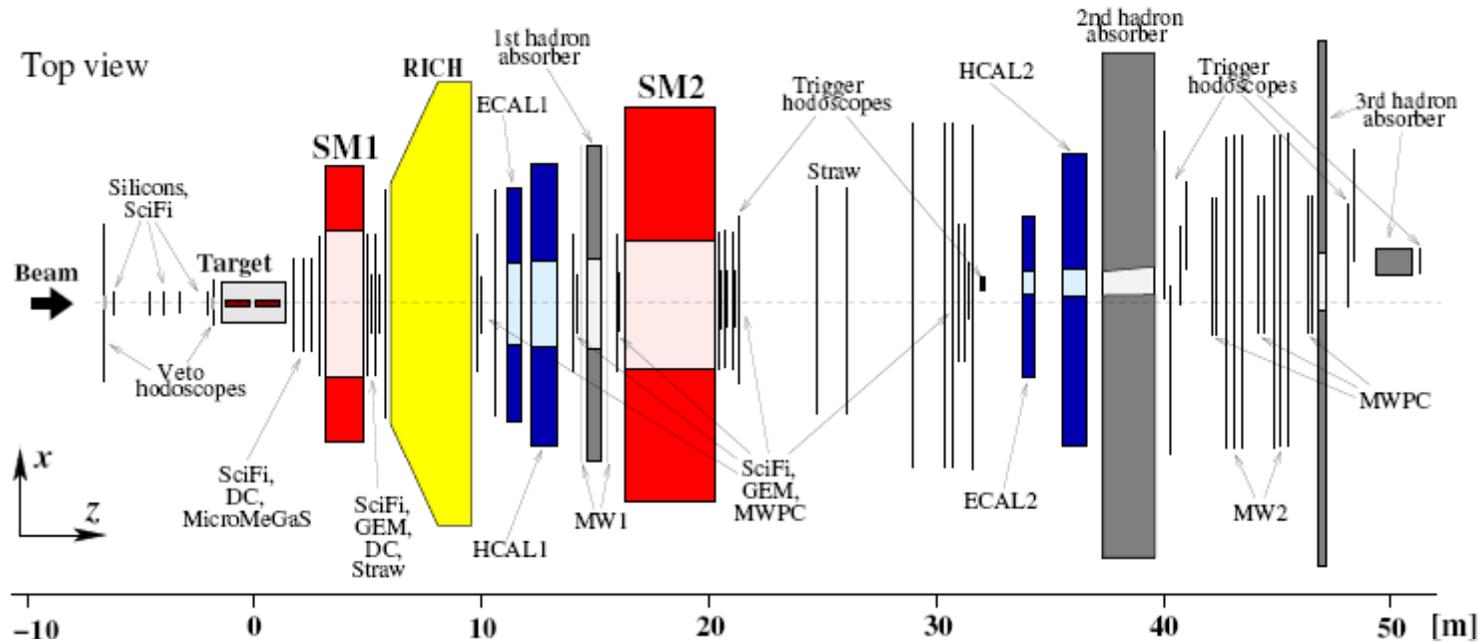
- target material:  $\text{NH}_3$
- high polarization
- very good relaxation time ( $\sim 4000\text{h}$ )
- field rotation without loss of polarization

Polarization in 2007:  
+92%   -83%   +88%

# Summary

- Analysis of deuteron data 2002-2004 have been presented:
  - Inclusive asymmetry  $A_1^d$  and structure function  $g_1^d$
  - First moment of  $g_1^d$  and QCD analysis
- Data of 2006 have been processed, update of  $A_1^d$  expected to be soon
- Processing of 2007 data (longitudinal polarization) is in progress

*Spare slides*



- Polarized beam  $\mu^+$  (-80%),  $E_b=160$  GeV
- 2/3 cells polarized target  ${}^6\text{LiD}$  (50%) and  $\text{NH}_3$  (90%)
- Two stages spectrometer
- Tracking detectors of different types
- Identification: HCALs, ECALs, RICH, muon walls

# Expectation from 2006-2007

**3<sup>6</sup> =**

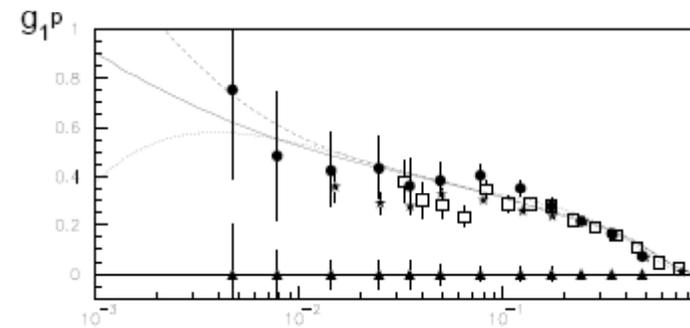
- longitudinal target polarisation:

**flavour separation** of PDFs

sign of **strange** sea polarisation  
at low  $x$

**shape of  $g_1^P$**  at low  $x$

$g_1^P$  at low  $x$



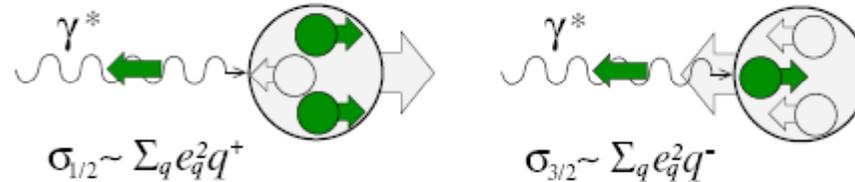
Significant improvement in QCD evolution is possible

# Deep inelastic scattering

- Quark densities in QPM:

$$q(x) = q^+(x) + q^-(x)$$

$$\Delta q(x) = q^+(x) - q^-(x)$$



- Longitudinal double-spin asymmetry:  $A^{\gamma N} \equiv A_1 = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}} = \frac{\sum_q e_q^2 \Delta q}{\sum_q e_q^2 q}$

- Spin (in)dependent cross-sections:

$$\sigma = \bar{\sigma} \pm \Delta\sigma$$

- Longitudinal spin asymmetry  $\mu N$ :

$$A^{\mu N} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} = \frac{\Delta\sigma}{\bar{\sigma}} \simeq DA_1$$

$D$  – depolarization factor of  $\gamma$

- Structure functions  $F_{1,2}$  and  $g_{1,2}$

$$\bar{\sigma}(x, Q^2) = aF_1(x, Q^2) + bF_2(x, Q^2)$$

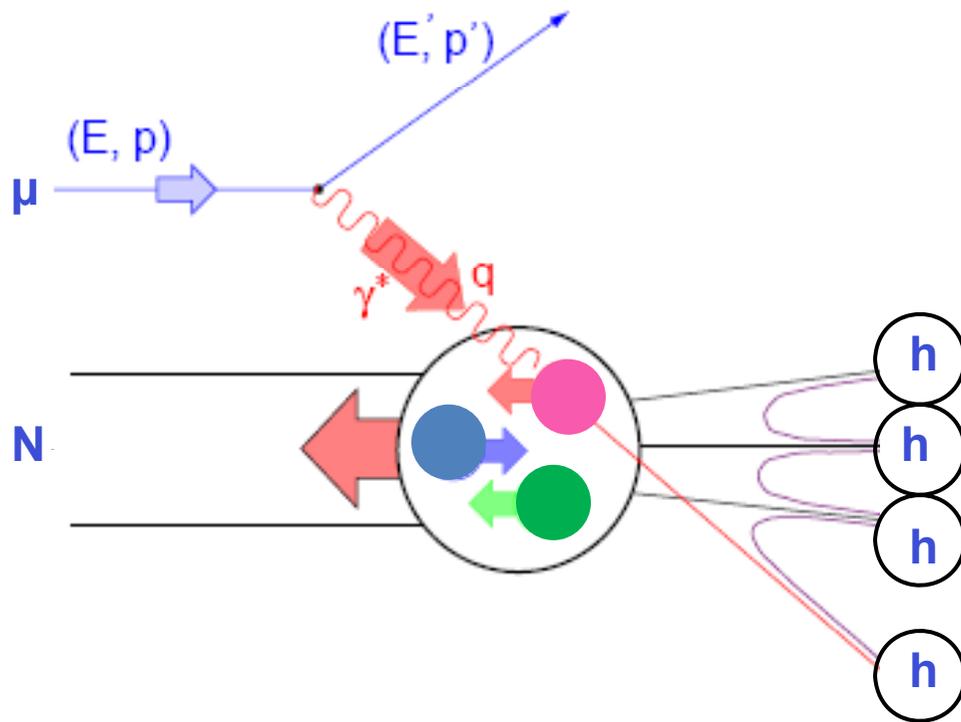
$$\Delta\sigma(x, Q^2) = \alpha g_1(x, Q^2) + \beta g_2(x, Q^2)$$

- Structure functions & quark distributions:

$$F_1 = \frac{1}{2} \sum_q e_q^2 (q + \bar{q}), \quad g_1 = \frac{1}{2} \sum_q e_q^2 (\Delta q + \Delta \bar{q})$$

- Asymmetry  $A_1$  gives access to  $g_1$ :  $g_1 \simeq A_1 \cdot F_1$

# Deep inelastic scattering



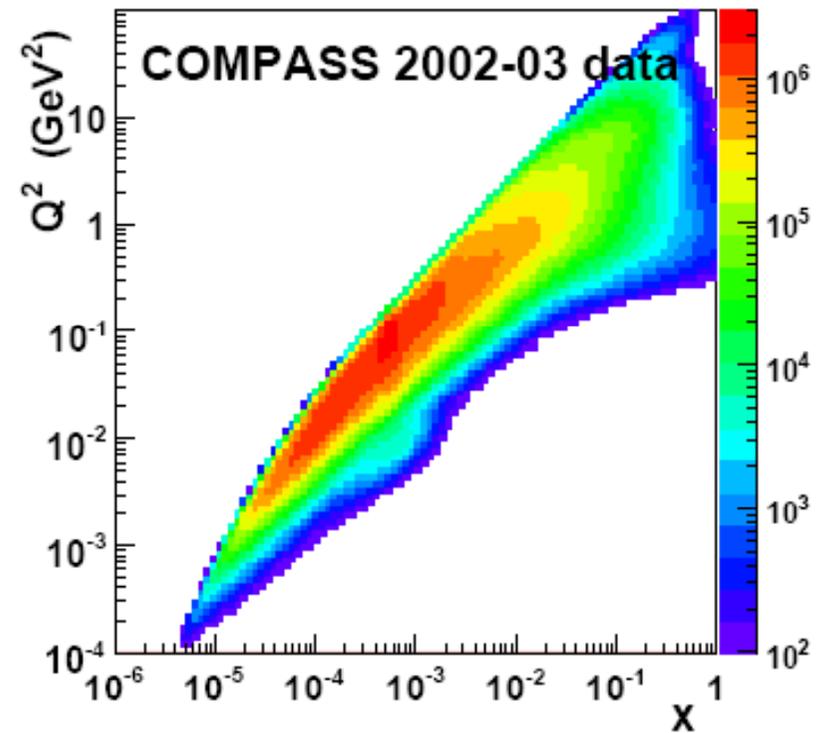
Kinematical variables:

$$Q^2 = -q^2$$

$$x = Q^2/2Mv$$

$$v = E - E'$$

$$y = v/E$$



# QCD analysis

- Measured structure functions  $g_1^{p,d,n}$  (different  $x$ ,  $Q^2$ )

$$g_1(x, Q^2) = \frac{1}{2} \langle e^2 \rangle \left[ C_q^S \otimes \Delta\Sigma + C_q^{NS} \otimes \Delta q^{NS} + 2n_f C_G \otimes \Delta G \right]$$

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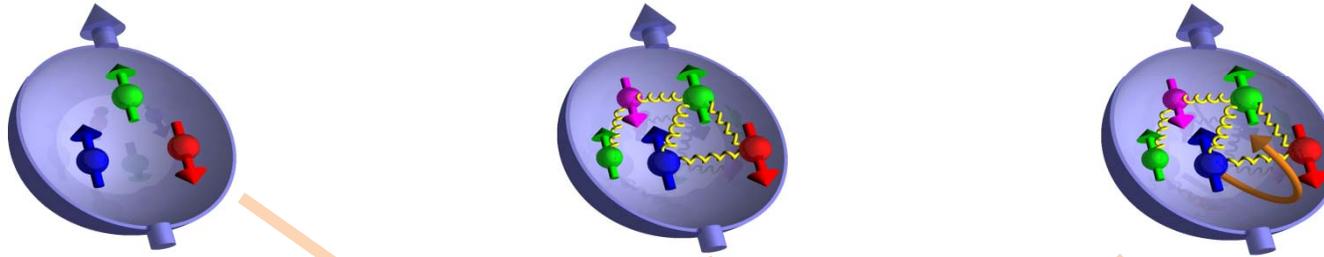
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- Initial parametrization ( $x$ -dependence at fixed  $Q^2$ )

$$\Delta\Sigma = \eta \frac{x^\alpha (1-x)^\beta (1+\gamma x)}{\int_0^1 x^\alpha (1-x)^\beta (1+\gamma x) dx}, \quad (\Delta q_3, \Delta q_8, \Delta G) = \eta \frac{x^\alpha (1-x)^\beta}{\int_0^1 x^\alpha (1-x)^\beta dx}$$

- World data fit: 9 experiments, 230 experimental points
- **Two solutions have been found:** describe data equally well and correspond to  **$\Delta G > 0$  and  $\Delta G < 0$**

# Spin of the nucleon



$$\mathbf{S}_N = \frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + \underbrace{\mathbf{L}_q + \mathbf{L}_g}$$

**Naïve parton model:**

$$\Delta\Sigma = \Delta u_v + \Delta d_v = 1$$

$$\Delta\Sigma = 0.23 \pm 0.07 \pm 0.19 \text{ (E155)}$$

**Complete description :**

- $\Delta\Sigma = \Delta u + \Delta d + \Delta s$  (for  $q$  and  $\bar{q}$ )
- $\Delta G$
- orbital angular momenta

# Deep inelastic scattering

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$$\Delta q(x) = q^+(x) - q^-(x)$$

- Longitudinal double-spin asymmetry:

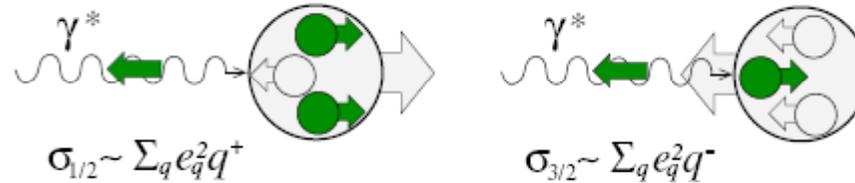
- Cross-sections:

$$\sigma = \bar{\sigma} \pm \Delta\sigma$$

- Structure functions:

$$\bar{\sigma}(x, Q^2) = aF_1(x, Q^2) + bF_2(x, Q^2)$$

$$\Delta\sigma(x, Q^2) = \alpha g_1(x, Q^2) + \beta g_2(x, Q^2)$$



$$A^{\gamma N} \equiv A_1 = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}} = \frac{\sum_q e_q^2 \Delta q}{\sum_q e_q^2 q}$$

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$$A^{\mu N} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} = \frac{\Delta\sigma}{\bar{\sigma}} \simeq DA_1$$

$D$  – depolarization factor of  $\gamma$

- Structure functions and QDF:

$$F_1 = \frac{1}{2} \sum_q e_q^2 (q + \bar{q}), \quad g_1 = \frac{1}{2} \sum_q e_q^2 (\Delta q + \Delta \bar{q})$$

- Asymmetry  $A_1$  and structure function  $g_1$ :  $g_1 \approx A_1 \cdot F_1$