



Spin structure of the nucleon studied with muon and electron beams

G. K. Mallot
CERN/PH

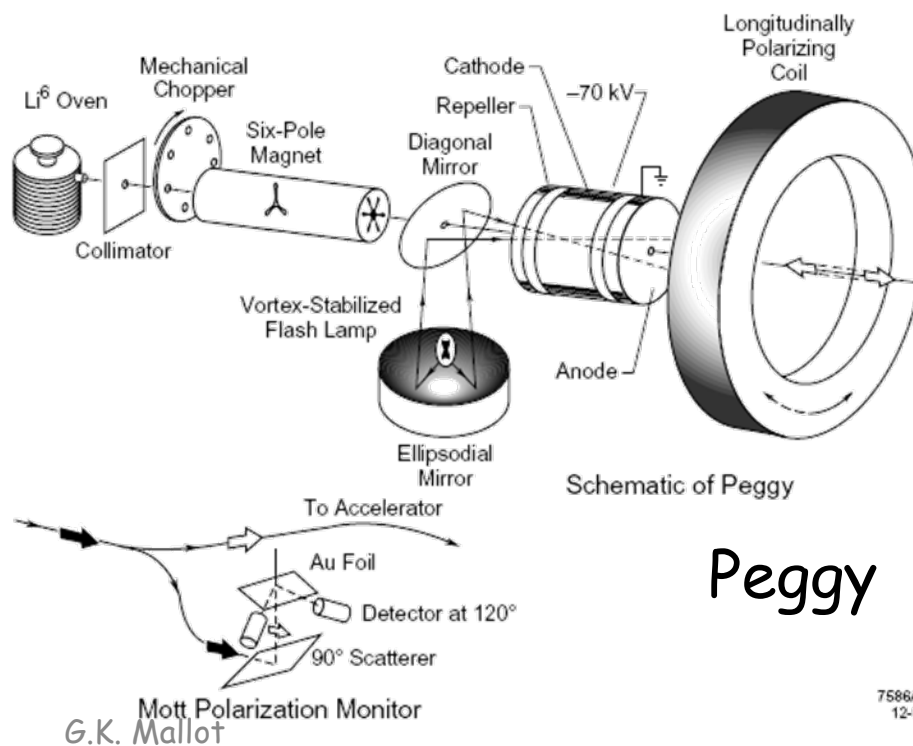
JPS Autumn Meeting,
Yamagata, Japan, September 23 , 2008



The early days

SLAC-Yale E80 (1975):

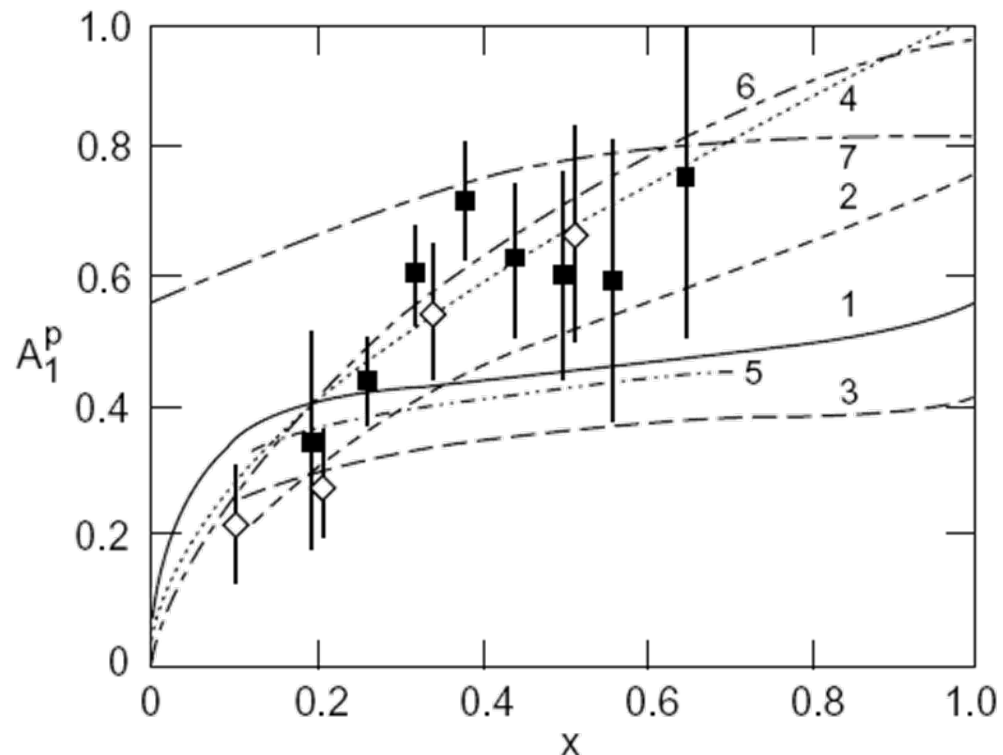
- beam:
10-16 GeV e^- ,
85% pol from pol. ${}^6\text{Li}$
- target:
butanol 60% pol



Support for the QPM

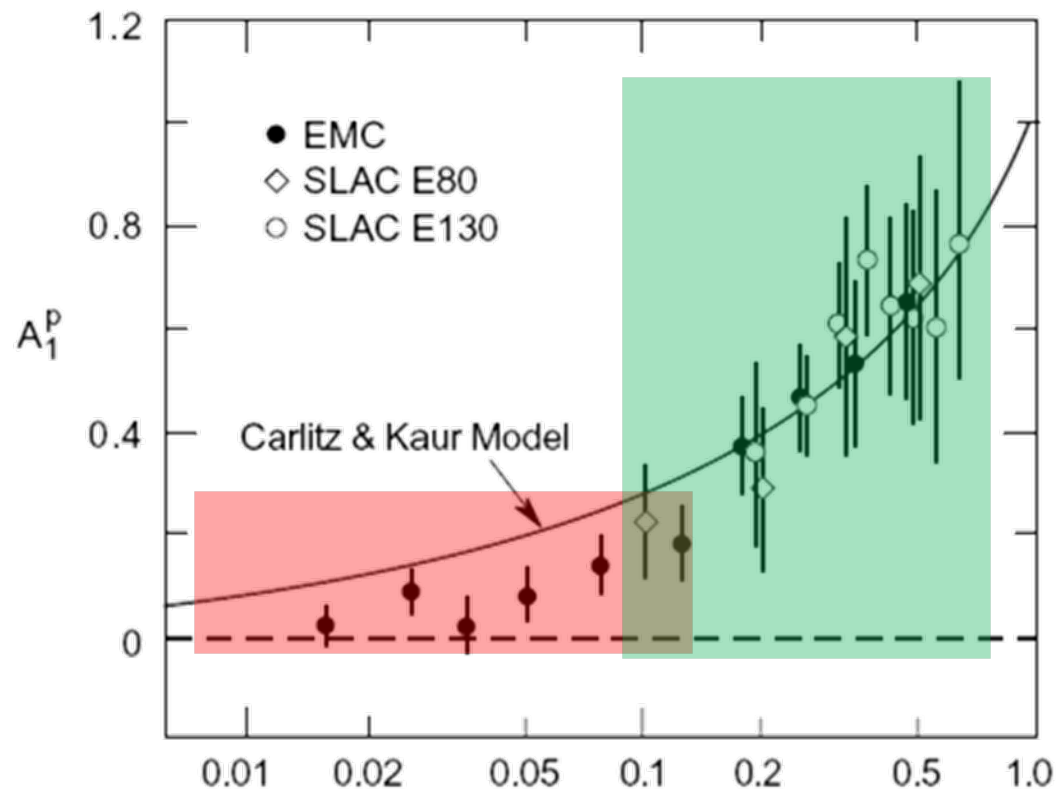
- large longitudinal double spin asymmetries at large x_{Bj}
- predicted by Bjorken from the Quark Parton Model

E80 (\diamond)
E130 (\blacksquare)

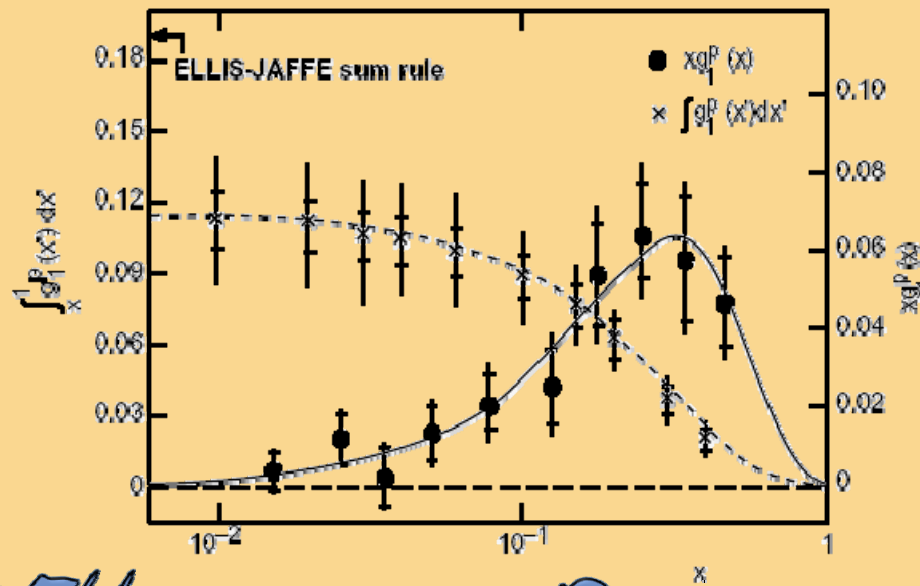


The shock 1987/88

- European Muon Collaboration (EMC) at CERN
- beam: 100 - 280 GeV, muons, pol. 80%
- target: ammonia, 80% pol.
- models wrong below $x < 0.1$
- unmeasured by E80 & E130



EMC 1987/88



20TH ANNIVERSARY

Implications of the EMC result

- The **Ellis-Jaffe sum rule** for the proton is violated
- The fundamental **Bjorken sum rule** can only be valid, if the EJ sum rule for the neutron is violated by the same amount

$$\Gamma_1^p - \Gamma_1^n = \frac{1}{6}g_a$$

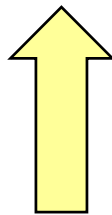
“if wrong, QCD is wrong”

- The strange quark polarization Δs does not vanish
- The quark spins **contribute little** to the proton spin

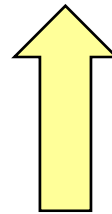
Where, oh where is the proton spin?

Elliot Leader

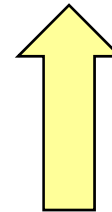
$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_z$$



small



poorly known
certainly not 6



unknown

Theory Input 1988

CHIRAL SYMMETRY AND THE SPIN OF THE PROTON ☆

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PLB 206 (1988) 309

A crisis in the parton model: where, oh where is the proton's spin?

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Received 18 March 1988

ZPC 41 (1988) 239

E2-88-287

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SPIN STRUCTURE OF THE NUCLEON AND TRIANGLE ANOMALY

THE ANOMALOUS GLUON CONTRIBUTION TO POLARIZED LEPTOPRODUCTION

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Received 29 June 1988

PLB 212 (1988) 391

Considered Options

- Skyrmions: model,
all orbital angl. mom. (BEK) maybe
- Bjorken sum rule broken?
Measurement wrong? (LA) no!
- Large $\Delta G \sim 2-3-6$ at EMC Q^2 could mask
quark spin via axial anomaly (ET, AR) measure
gluon pol!

requires fine tuning of cancelation of ΔG and orbital
angular momentum (orb. ang. mom. is generated at
gluon emission)

Lepton-Photon 1989

To summarise, let us return to the fit of Fig. 7 and 8. At $Q^2=10\text{GeV}^2$ this corresponds to $\Delta g=6.3$ and so the proton helicity is given by

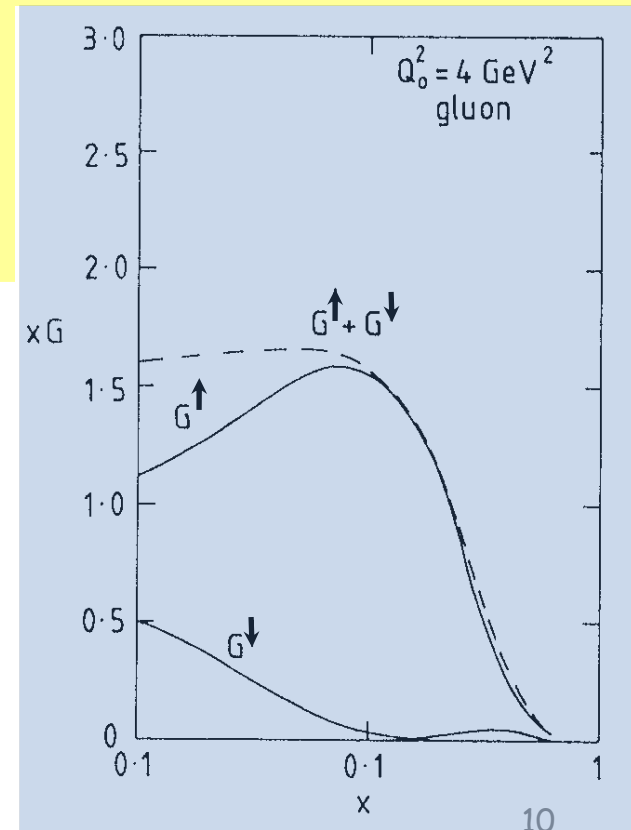
$$\begin{aligned}\frac{1}{2} &= \frac{1}{2}\Delta\Sigma + \Delta g + L_z \\ &= 0.35 + 6.3 - 6.15\end{aligned}$$

G. Ross 1989

possible scenario:

$$\Delta G \approx 6 \quad (Q^2=10 \text{ GeV}^2)$$

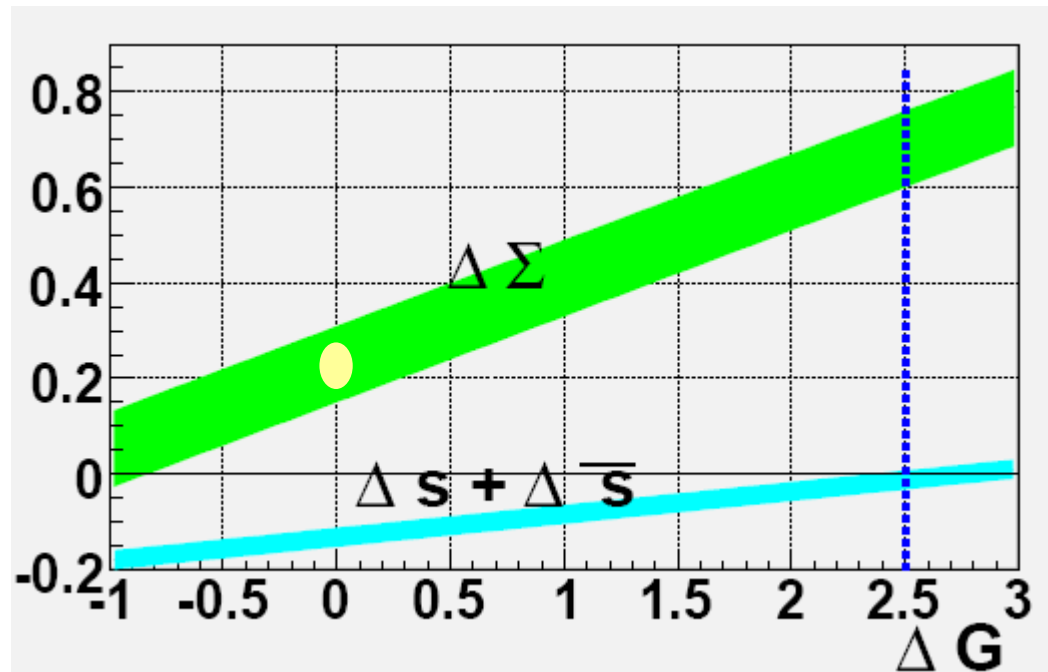
$$\Delta g/g(x) = 1 \quad \text{for } x_g > 0.1$$



ΔG and $\Delta \Sigma$ in AB/jet scheme

$$\Delta \Sigma \leftarrow a_0 + \frac{3\alpha_s}{2\pi} \Delta G \quad \alpha_s \text{ strong coupling constant}$$

$$\Delta s \leftarrow \Delta s + \frac{3\alpha_s}{2\pi} \Delta G$$



Now:
 $a_0 \simeq 0.3$

Need:
 $\Delta G \simeq 2.5$

Priorities in 1988



Vernon W Hughes,
1921 - 2003,
E80, E130,
EMC, SMC

- **repeat** EMC meas. with higher precision and
- **measure BJ sum rule** (neutron experiment)
- **gluon polarization** (longer term)

Third generation experiments:

- **SMC @CERN**
- **Hermes @ DESY** (delayed)
- **E142/43, E154/155, E155x at SLAC**

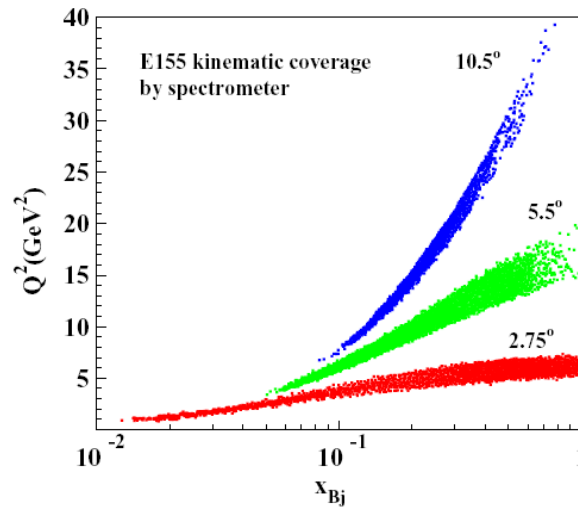
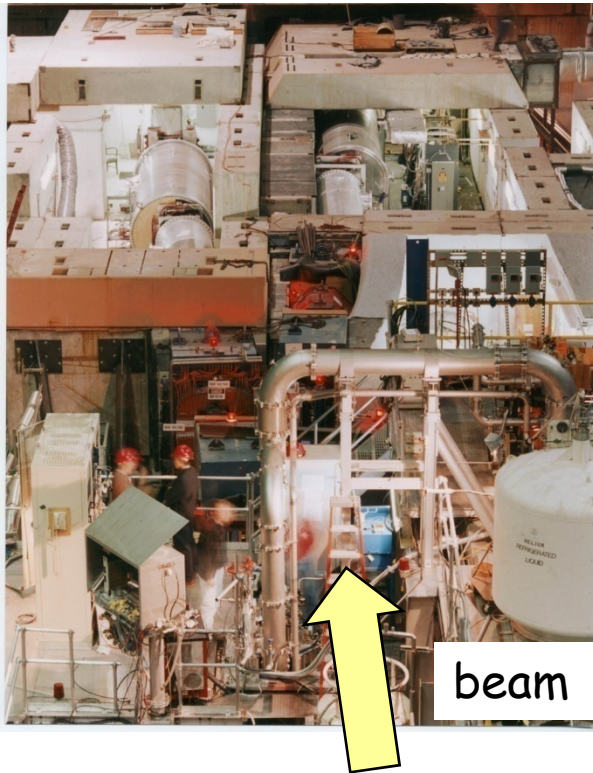
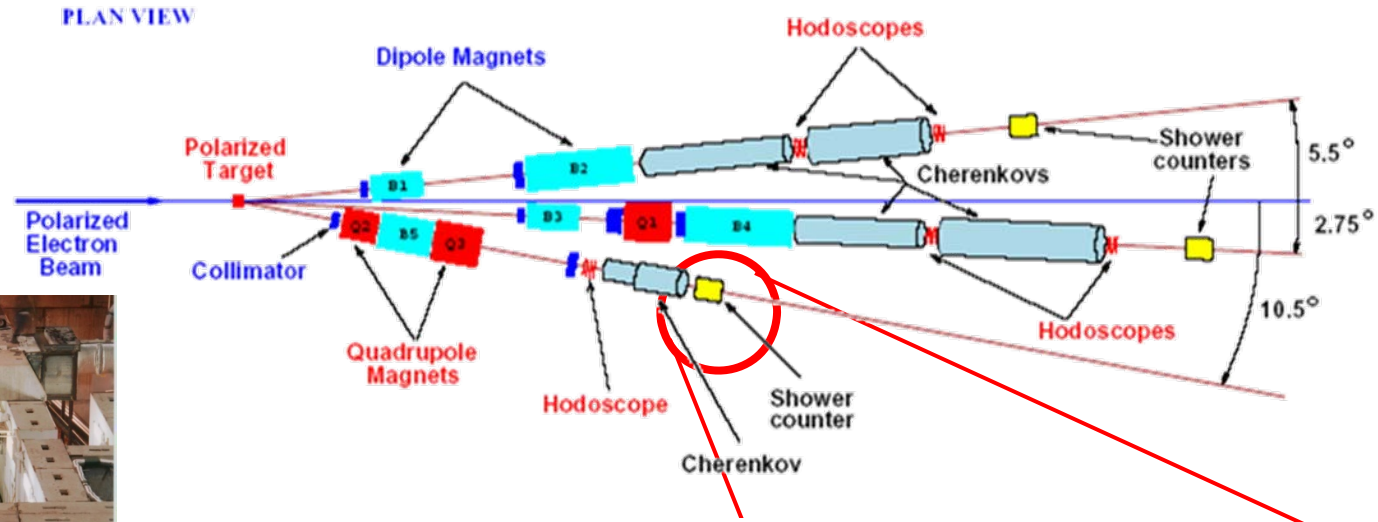


Forth generation experiments:

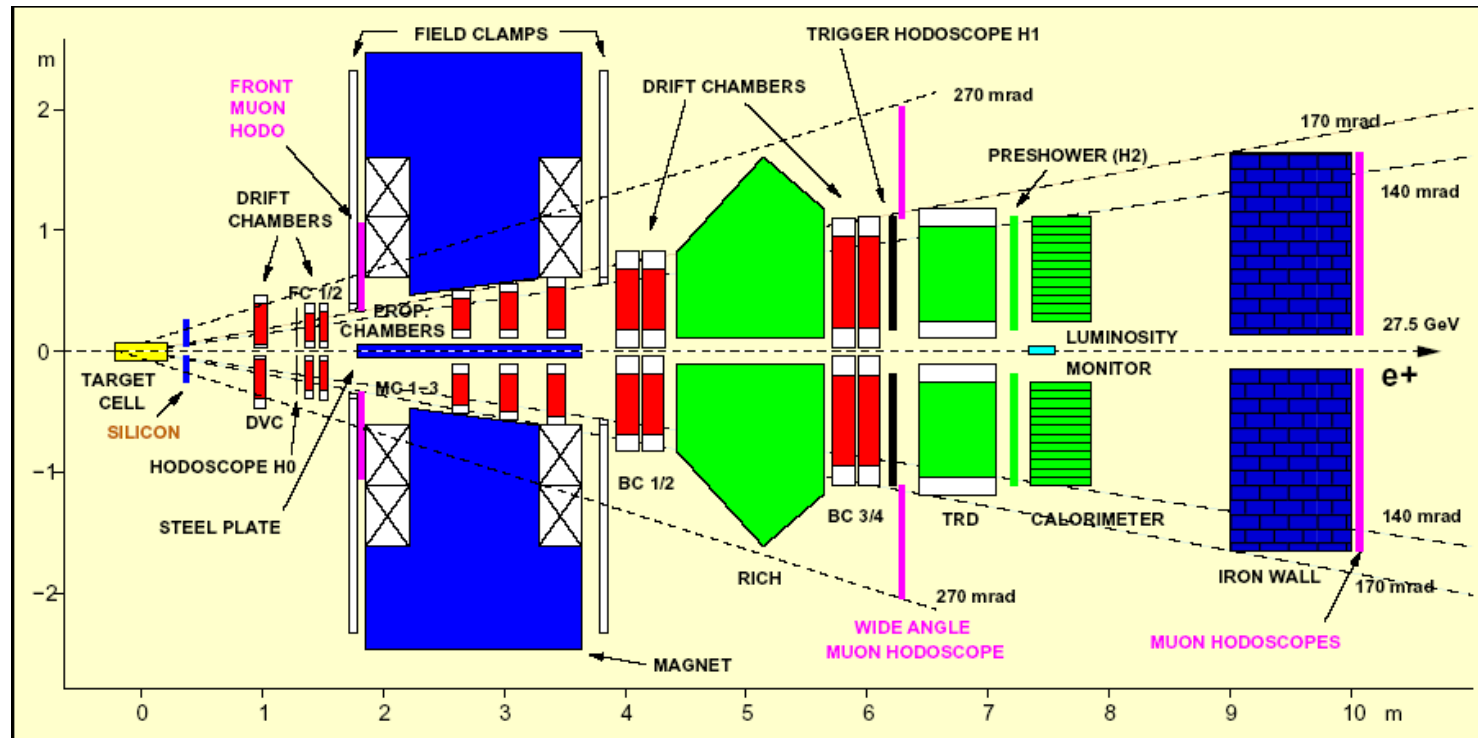
- **COMPASS @CERN**
- **E99-117, ... Jefferson Lab**
- **PHENIX & STAR @ RHIC**



SLAC E155 Spectrometer



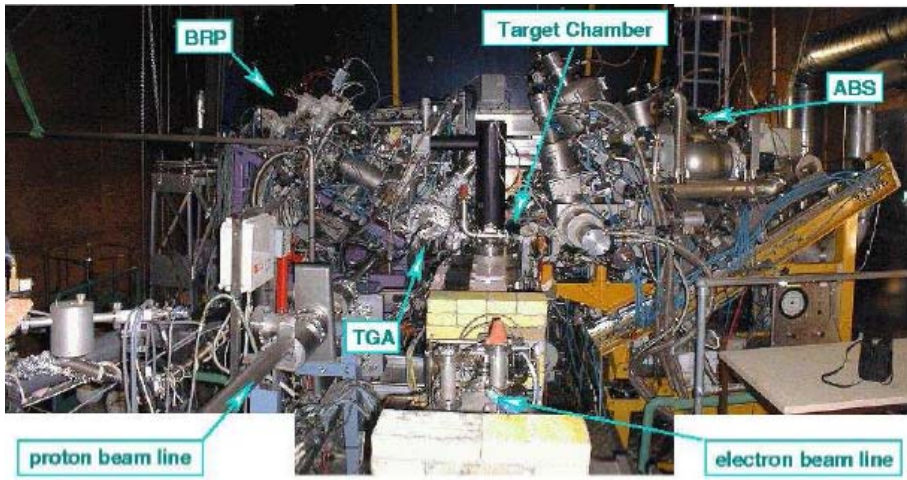
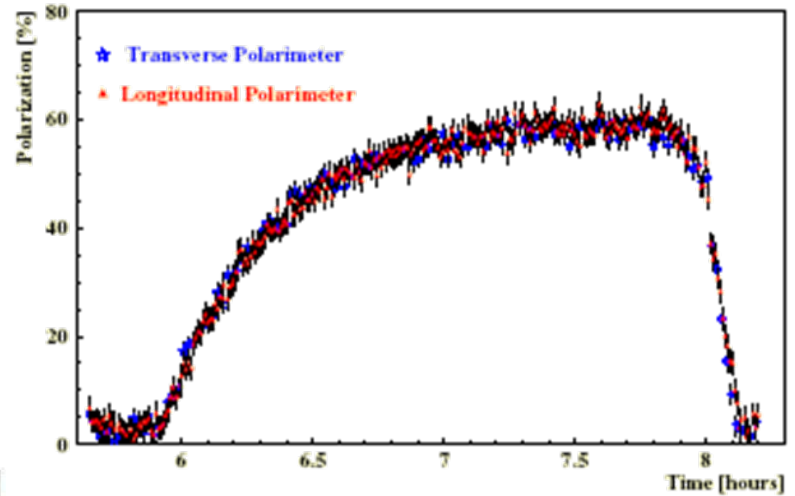
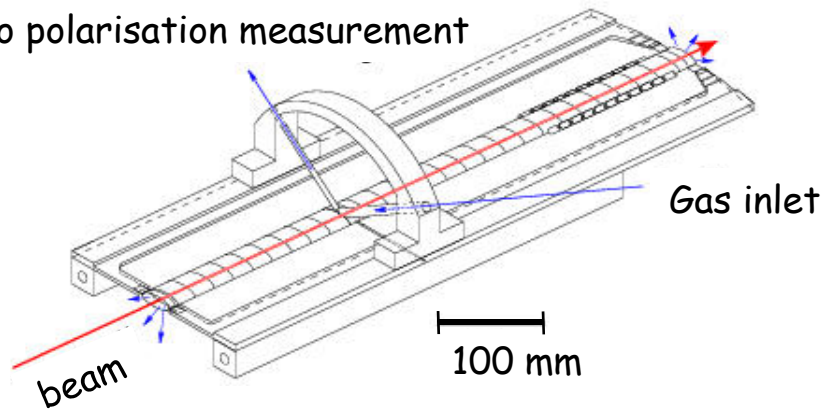
HERMES



HERMES

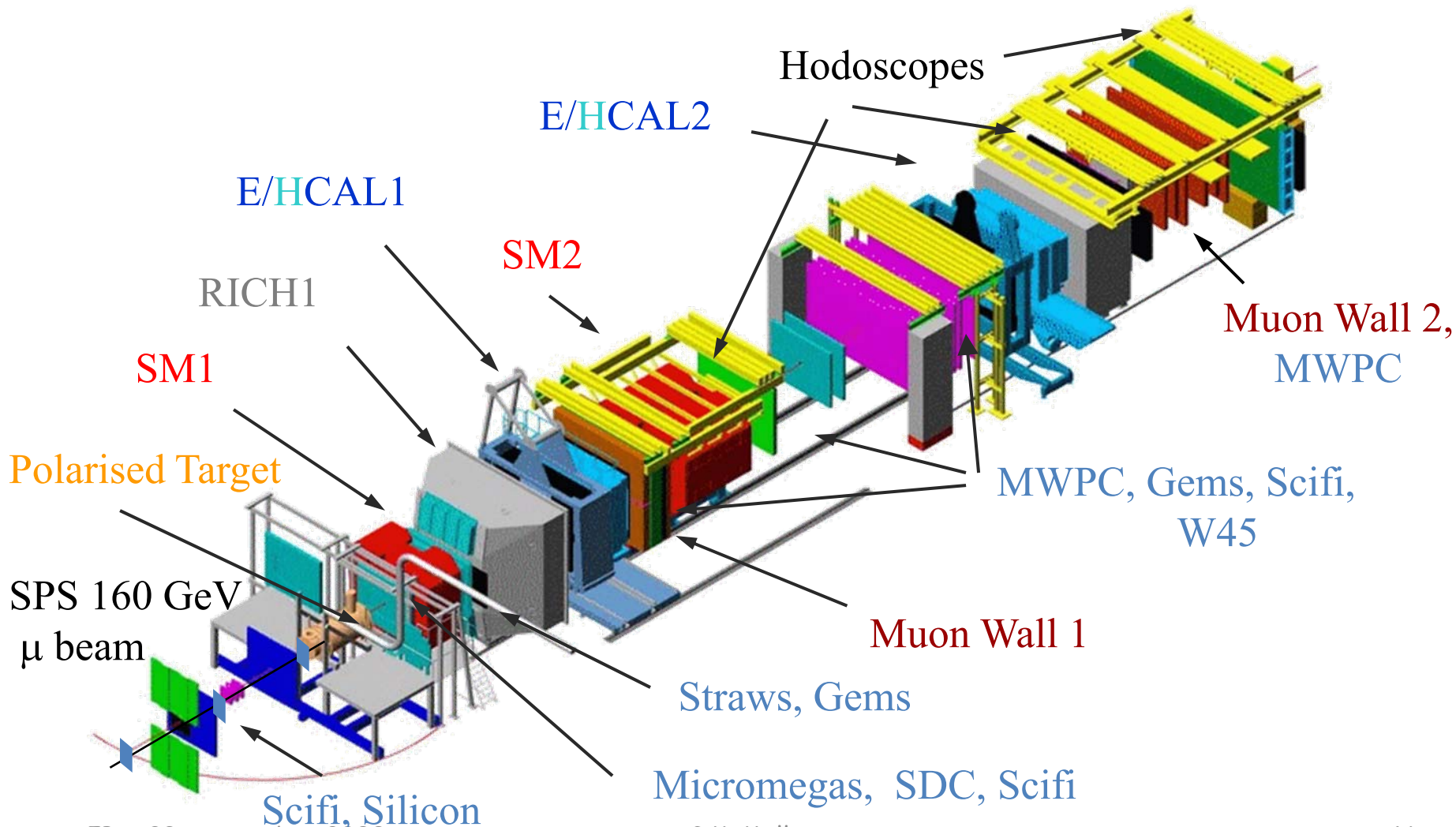
Target cell

Gas to polarisation measurement



beam polarisation
built-up

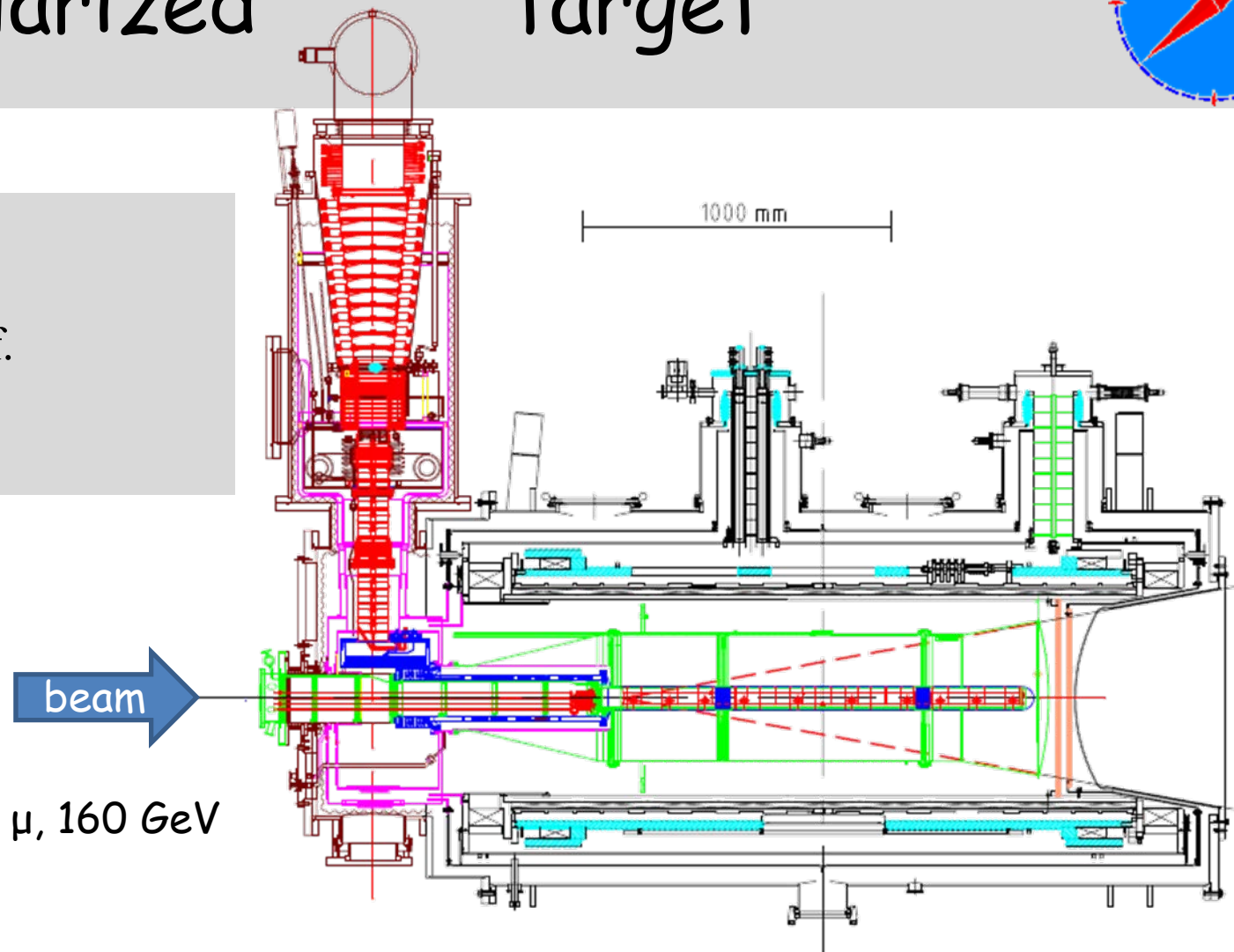
The COMPASS Spectrometer



Polarized target



- ${}^6\text{LiD}/\text{NH}_3$
- 50/90% pol.
- 40/16% dil. f.
- 2.5 T
- 50 mK

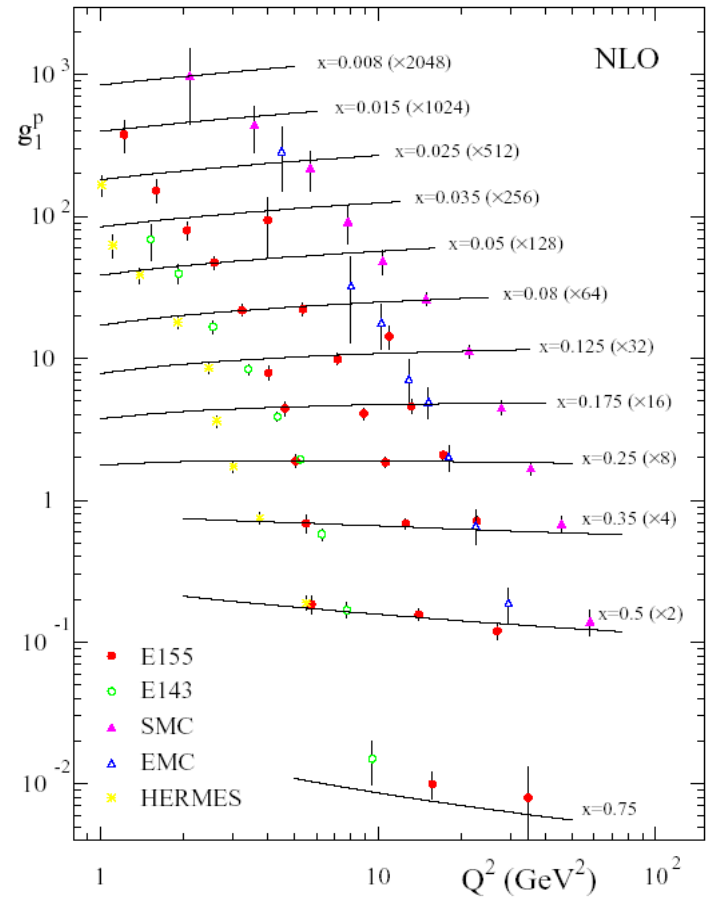
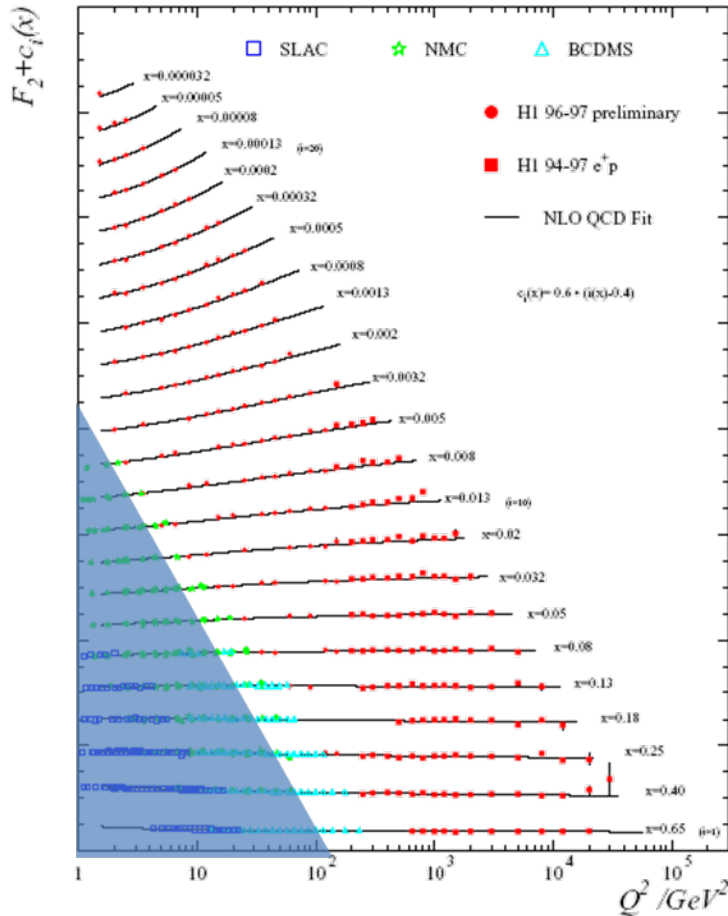


Structure Functions

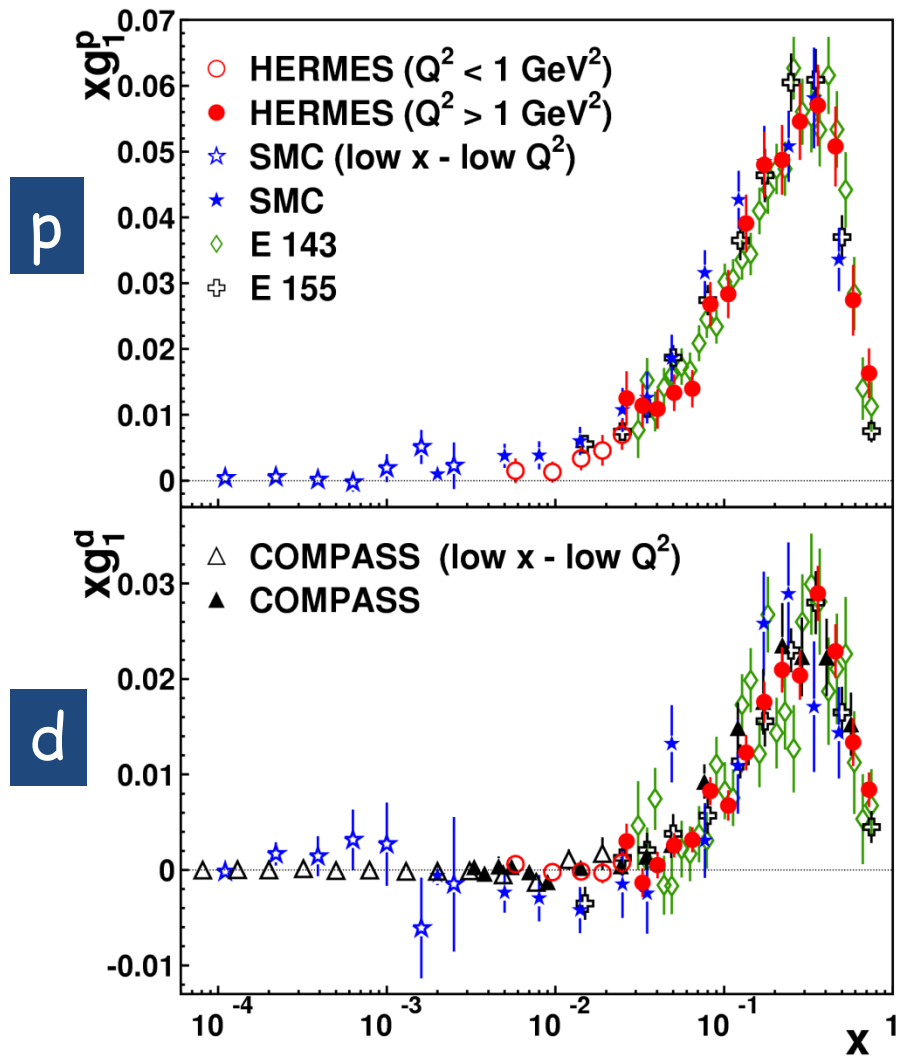
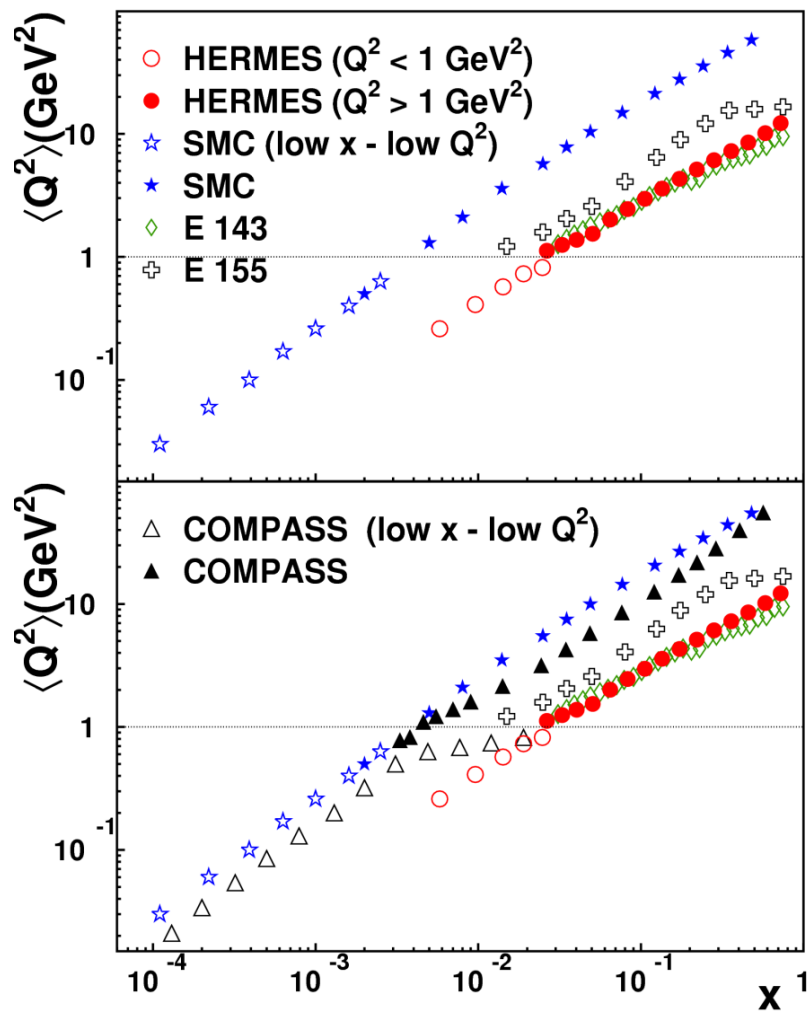
$$F_2(x, Q^2)$$

proton

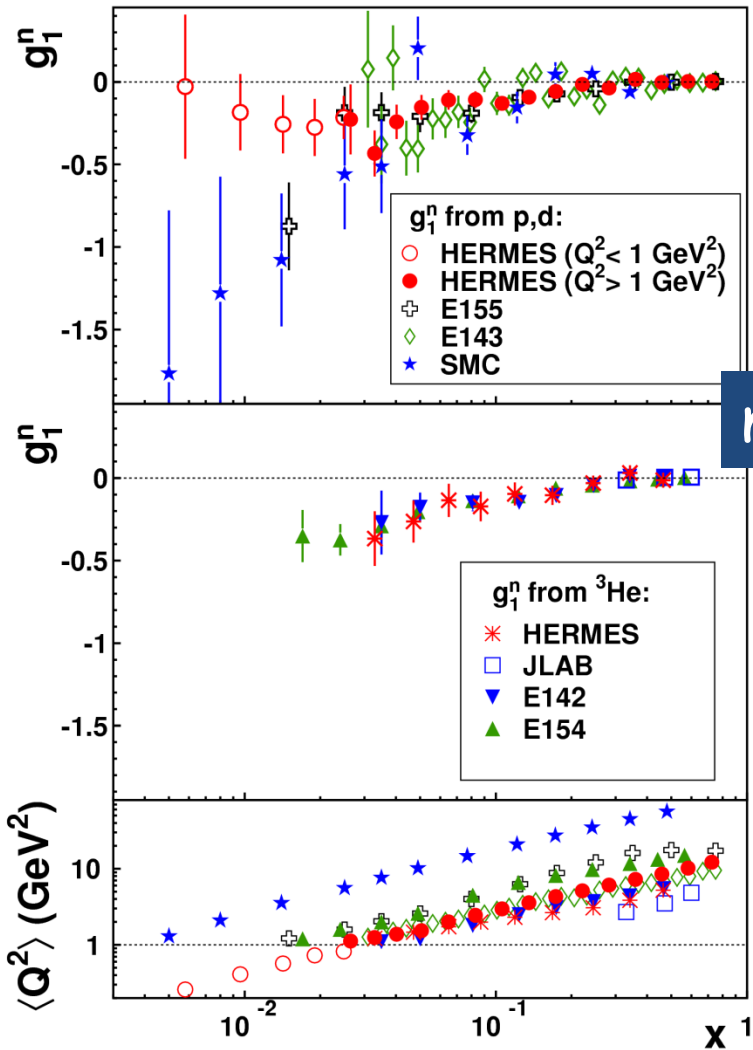
$$g_1(x, Q^2)$$



World data on $xg_1(x, Q^2)$



World data on neutron g_1^n



from p and d

$$g_1^n = \frac{2}{1 - \frac{3}{2}\omega_D} g_1^d - g_1^p$$

from ^3He

Scaling violations: QCD fits

NLO DGLAP:

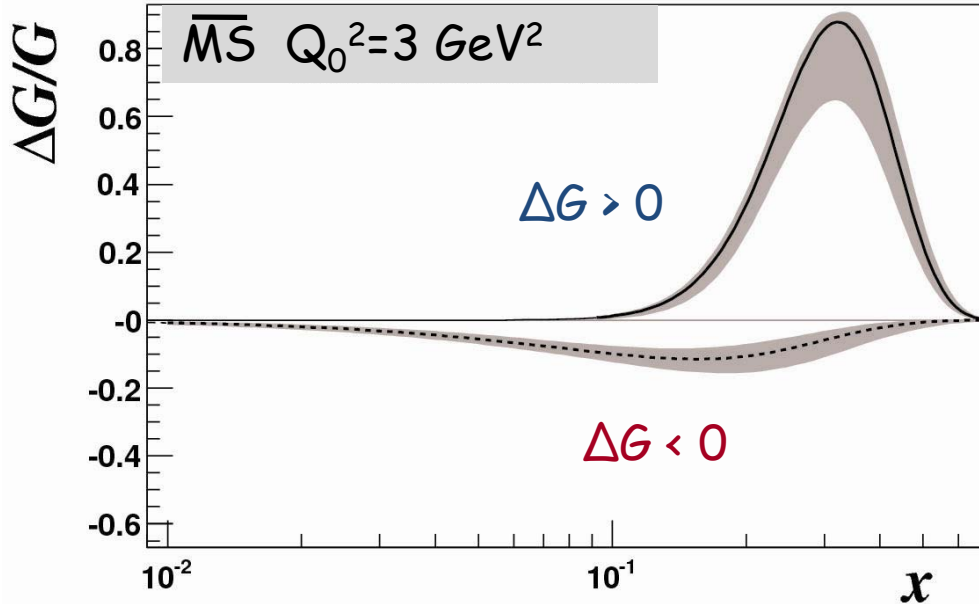
$$\frac{d}{d \ln Q^2} \Delta q^{ns} = \Delta \mathcal{P}_{qq}^{ns} \otimes \Delta q^{ns}$$
$$\frac{d}{d \ln Q^2} \begin{pmatrix} \Delta q^s \\ \Delta g \end{pmatrix} = \begin{pmatrix} \Delta \mathcal{P}_{qq}^s & \Delta \mathcal{P}_{qg}^s \\ \Delta \mathcal{P}_{gq}^s & \Delta \mathcal{P}_{gg}^s \end{pmatrix} \otimes \begin{pmatrix} \Delta q^s \\ \Delta g \end{pmatrix}$$

- choose scheme (\overline{MS} , AB, jet) and Q_0^2
- optionally fix ns moments from hyperon decays (a_3, a_8)
- fit PDFs for quark non-singlet and singlet and gluon to g_1 data
- functional form of PDFs biases error band
- extra problems in polarized case:
 - no positivity condition, no momentum sum rule
- higher twist, ...

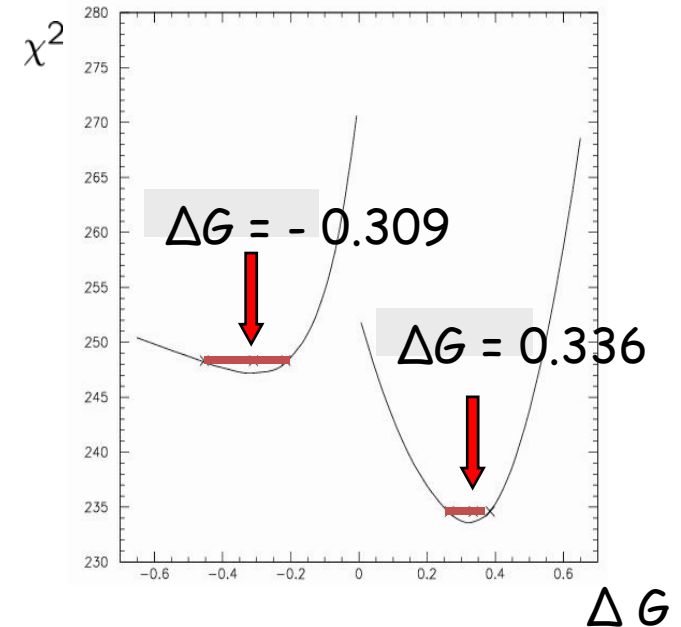


COMPASS QCD Fit

- two solutions with $\Delta G > 0$ and $\Delta G < 0$
- uncertainty due to parametrization **not included**

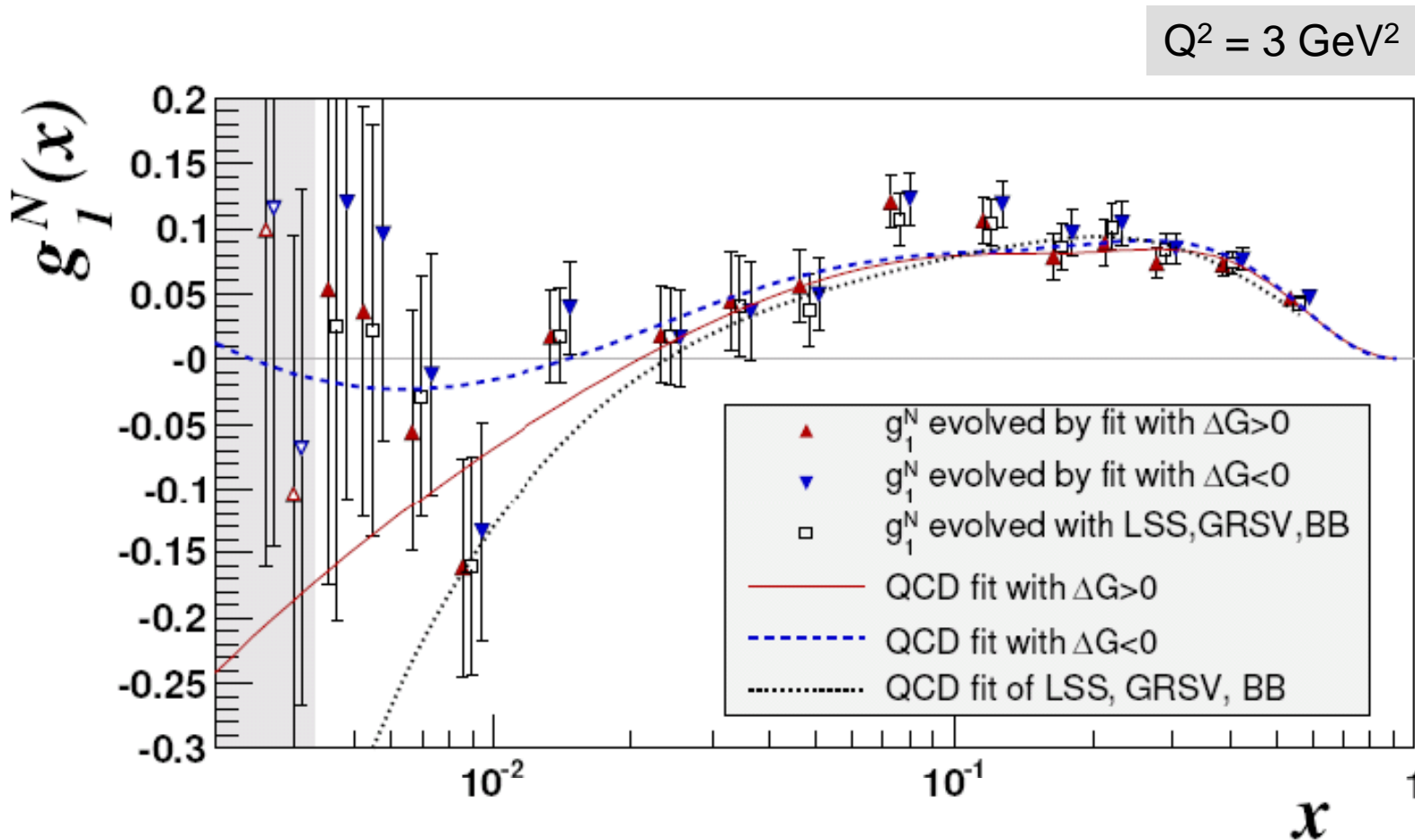


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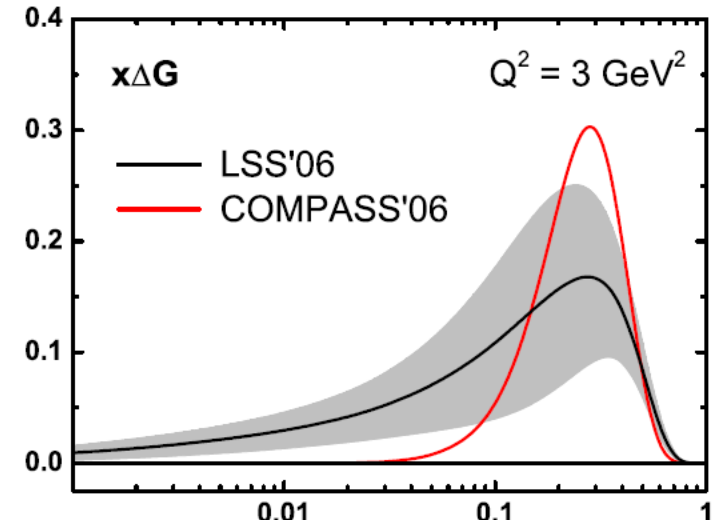


COMPASS deuteron g_1

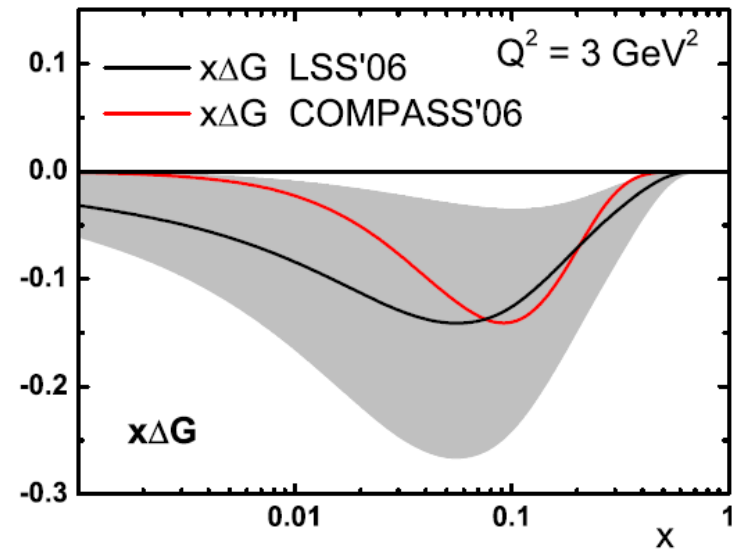


QCD Fit: LSS06 / COMPASS06

- LSS06 also finds two solutions with small $\Delta G > 0$ and $\Delta G < 0$
- includes HT and Clas data
- How to tell sign of ΔG ?



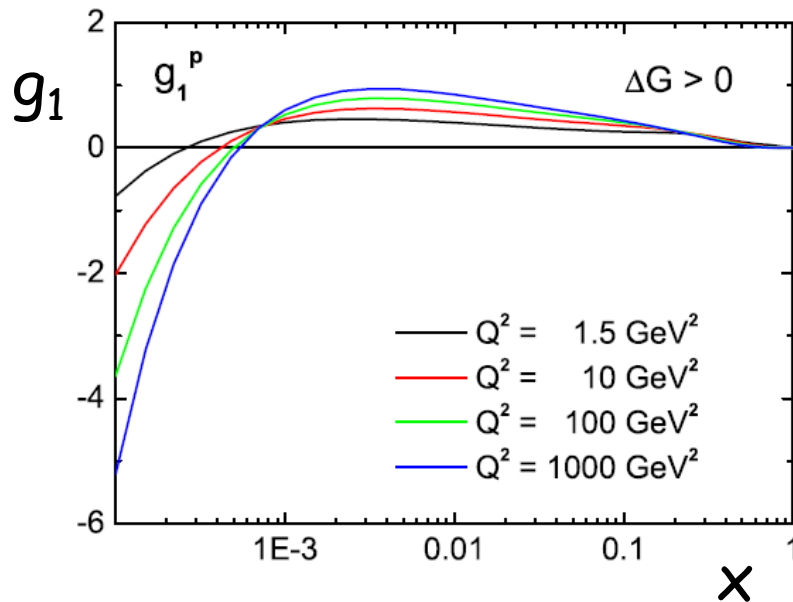
$\Delta G > 0$



$\Delta G < 0$

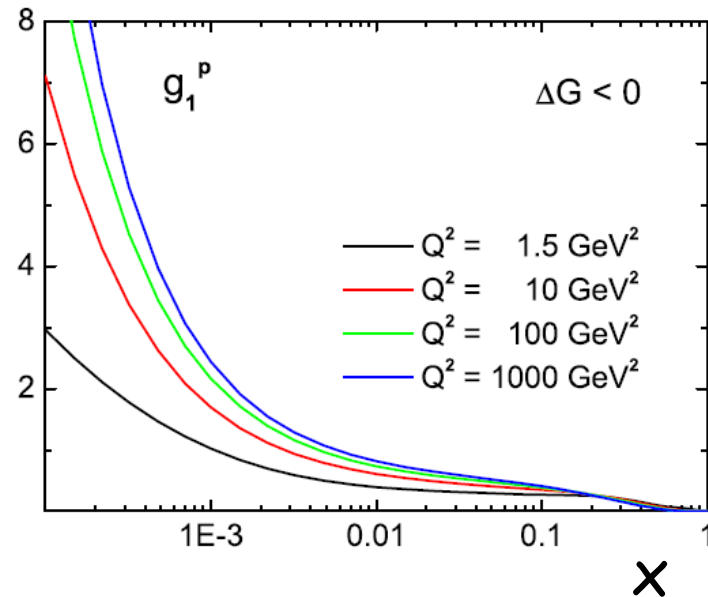
Sign of ΔG and low g_1 at small x

$\Delta G > 0$



$\Delta G < 0$

p

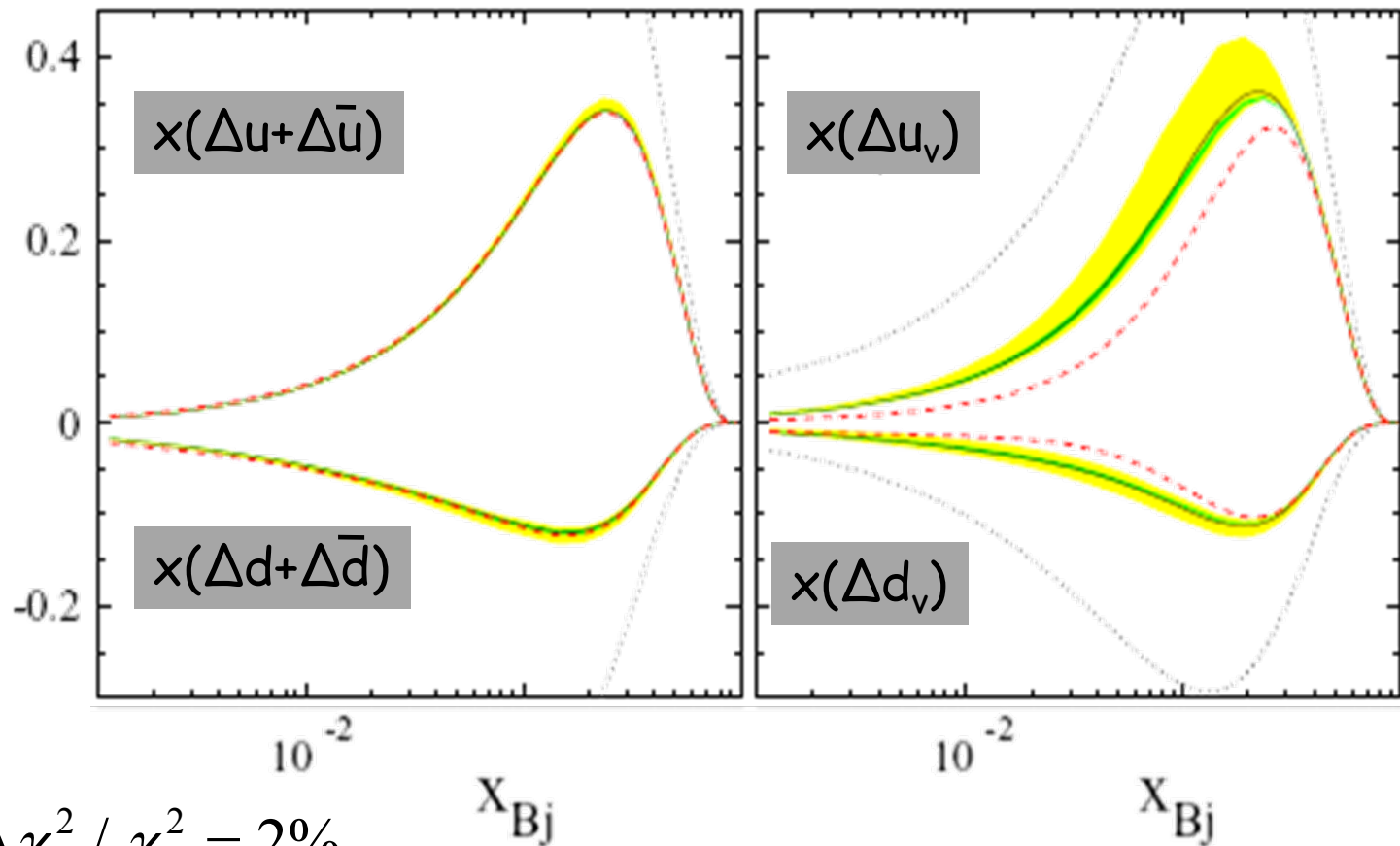


LSS06

measurable at a polarized ep collider (EIC)

Leader, DIS2008

QCD Fit: DNS05/DSSV08

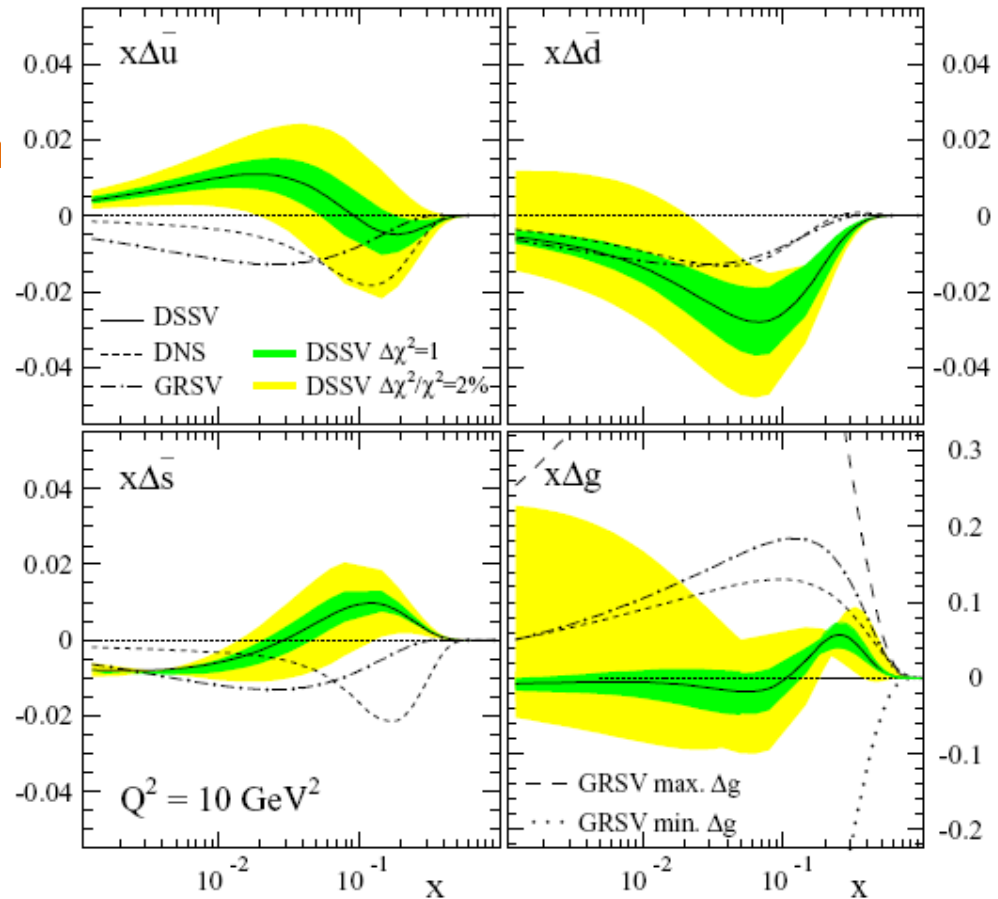


$\Delta\chi^2 / \chi^2 = 2\%$
 $\Delta\chi^2 = 1$

$Q^2 = 10 \text{ GeV}^2$

QCD Fit: DSSV08

- include semi-inclusive data
- includes pp data from Phenix and Star
- Δg might have a node
- $\Delta s < 0$ for $x < 0.02$
 $\Delta s > 0$ for $x < 0.02$
 forced by HERMES semi-inclusive data



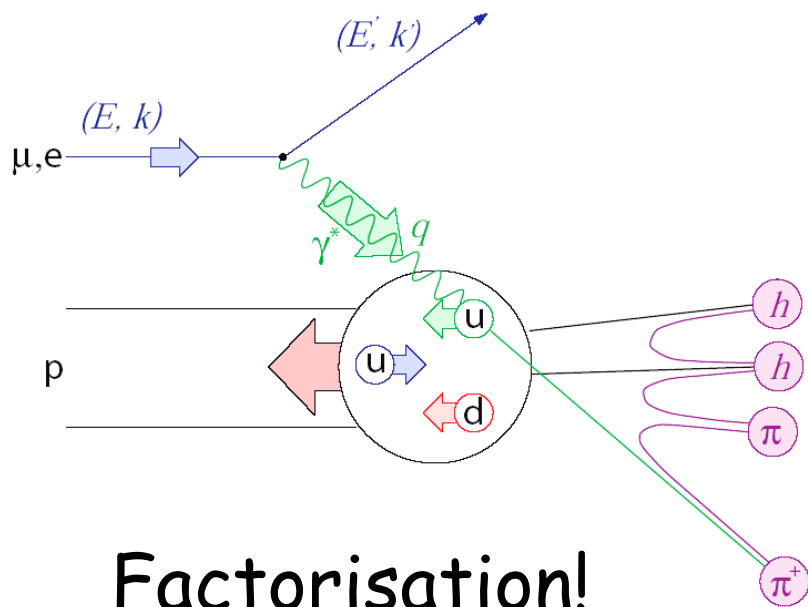
de Florian, Sassot, Stratmann, Vogelsang
 PRL101:072001

DSSV08

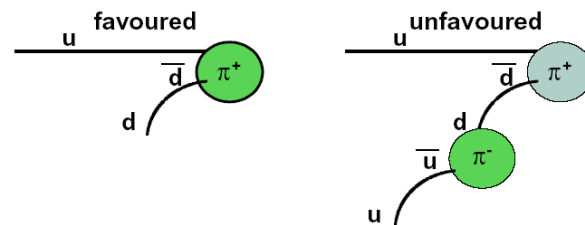
	$x_{\min} = 0$	$x_{\min} = 0.001$	
	best fit	$\Delta\chi^2 = 1$	$\Delta\chi^2/\chi^2 = 2\%$
$\Delta u + \Delta \bar{u}$	0.813	0.793 $^{+0.011}_{-0.012}$	0.793 $^{+0.028}_{-0.034}$
$\Delta d + \Delta \bar{d}$	-0.458	-0.416 $^{+0.011}_{-0.009}$	-0.416 $^{+0.035}_{-0.025}$
$\Delta \bar{u}$	0.036	0.028 $^{+0.021}_{-0.020}$	0.028 $^{+0.059}_{-0.059}$
$\Delta \bar{d}$	-0.115	-0.089 $^{+0.029}_{-0.029}$	-0.089 $^{+0.090}_{-0.080}$
$\Delta \bar{s}$	-0.057	-0.006 $^{+0.010}_{-0.012}$	-0.006 $^{+0.028}_{-0.031}$
Δg	-0.084	0.013 $^{+0.106}_{-0.120}$	0.013 $^{+0.702}_{-0.314}$
$\Delta \Sigma$	0.242	0.366 $^{+0.015}_{-0.018}$	0.366 $^{+0.042}_{-0.062}$

at $Q^2 = 10 \text{ GeV}^2$

Semi-inclusive DIS



D_q^h from quark q into hadron h
 $z = \frac{E_h}{\nu}$ energy fraction carried by h



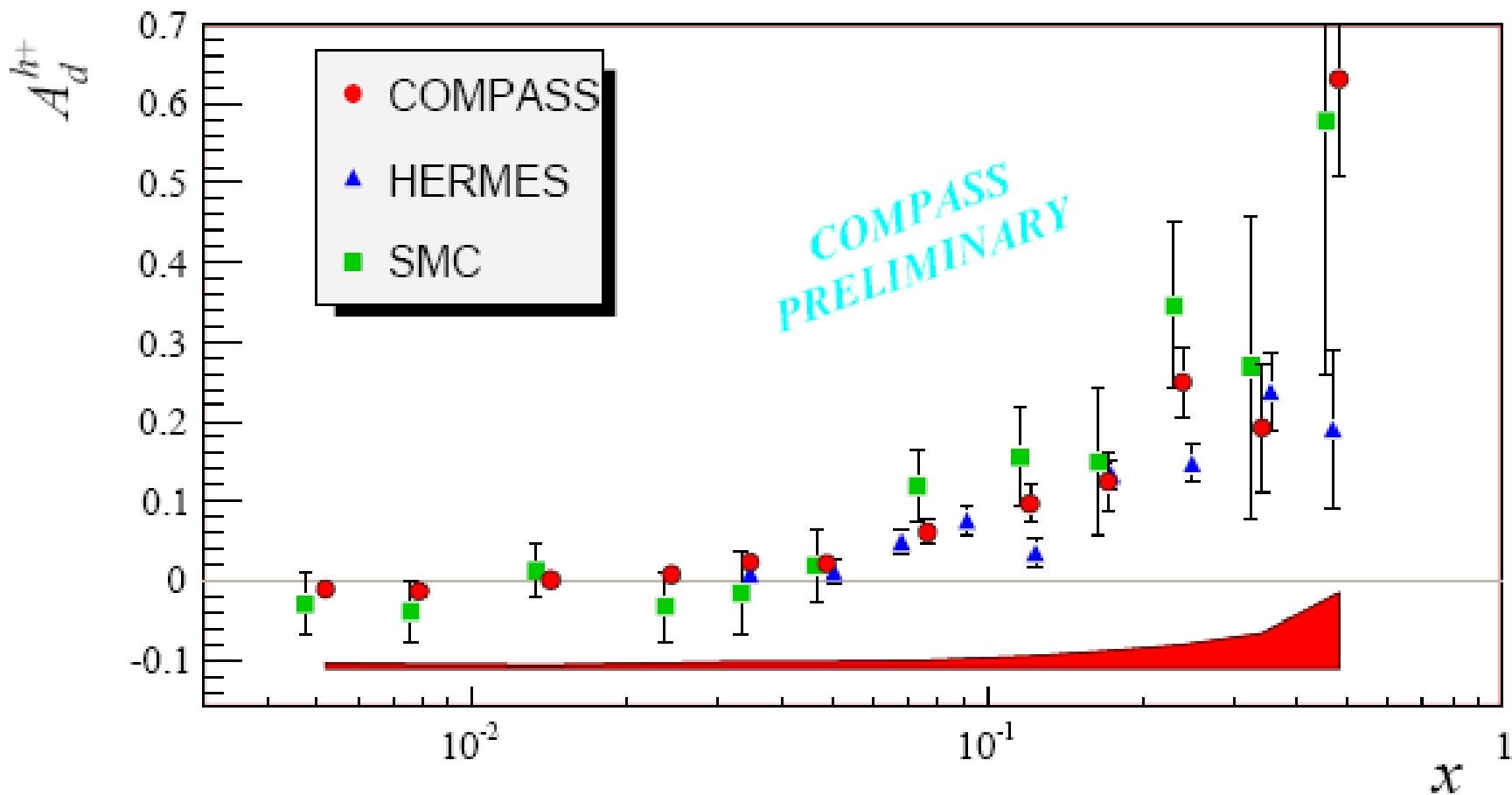
$$\begin{array}{ccccccc}
 D_u^{\pi^+} & = & D_{\bar{u}}^{\pi^-} & = & D_{\bar{d}}^{\pi^+} & = & D_d^{\pi^-} \\
 D_d^{\pi^+} & = & D_{\bar{d}}^{\pi^-} & = & D_u^{\pi^+} & = & D_u^{\pi^-}
 \end{array}$$

CC IS CC

$$\frac{1}{\sigma_0} \frac{d\sigma^h}{dz} = \frac{\sum_f e_f^2 q_f(\mathbf{x}, Q^2) \cdot D_f^h(z, Q^2)}{\sum_f e_f^2 q_f(\mathbf{x}, Q^2)}$$



Semi-inclusive asymmetries



Flavour separated polarization

Asymmetries can in LO be related to Δq by

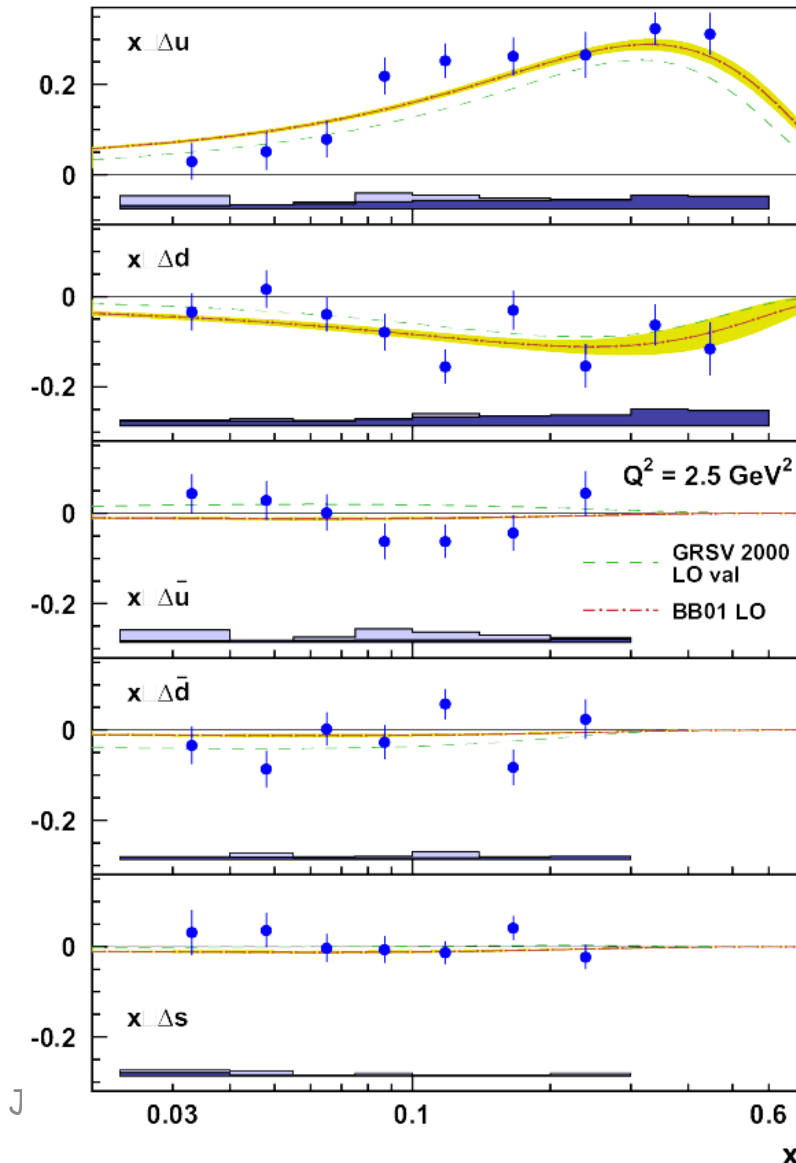
$$\vec{A} = \mathcal{P} \vec{Q}$$

where

$$\vec{A} = (A_{1,t}^h, \dots)$$

$$\vec{Q} = (\Delta q_f, \dots)$$

$$\mathcal{P}_f^h = \frac{e_f^2 q_f(x) \int dz D_f^h}{\sum_i e_i^2 q_i(x) \int dz D_i^h(z)}$$



Alternative: difference asymmetries

Semi-inclusive asymmetries

$$A^+ = \frac{\sigma_{\uparrow\downarrow}^{h+} - \sigma_{\uparrow\uparrow}^{h+}}{\sigma_{\uparrow\downarrow}^{h+} + \sigma_{\uparrow\uparrow}^{h+}} \quad A^- = \frac{\sigma_{\uparrow\downarrow}^{h-} - \sigma_{\uparrow\uparrow}^{h-}}{\sigma_{\uparrow\downarrow}^{h-} + \sigma_{\uparrow\uparrow}^{h-}}$$

$$A_1^h(x) = \frac{\sum_q e_q^2 (\Delta q(x) D_q^h + \Delta \bar{q}(x) D_{\bar{q}}^h)}{\sum_q e_q^2 (q(x) D_q^h + \bar{q}(x) D_{\bar{q}}^h)}$$

Difference asymmetry

$$A^{+-} = \frac{(\sigma_{\uparrow\downarrow}^{h+} - \sigma_{\uparrow\downarrow}^{h-}) - (\sigma_{\uparrow\uparrow}^{h+} - \sigma_{\uparrow\uparrow}^{h-})}{(\sigma_{\uparrow\downarrow}^{h+} - \sigma_{\uparrow\downarrow}^{h-}) + (\sigma_{\uparrow\uparrow}^{h+} - \sigma_{\uparrow\uparrow}^{h-})}$$

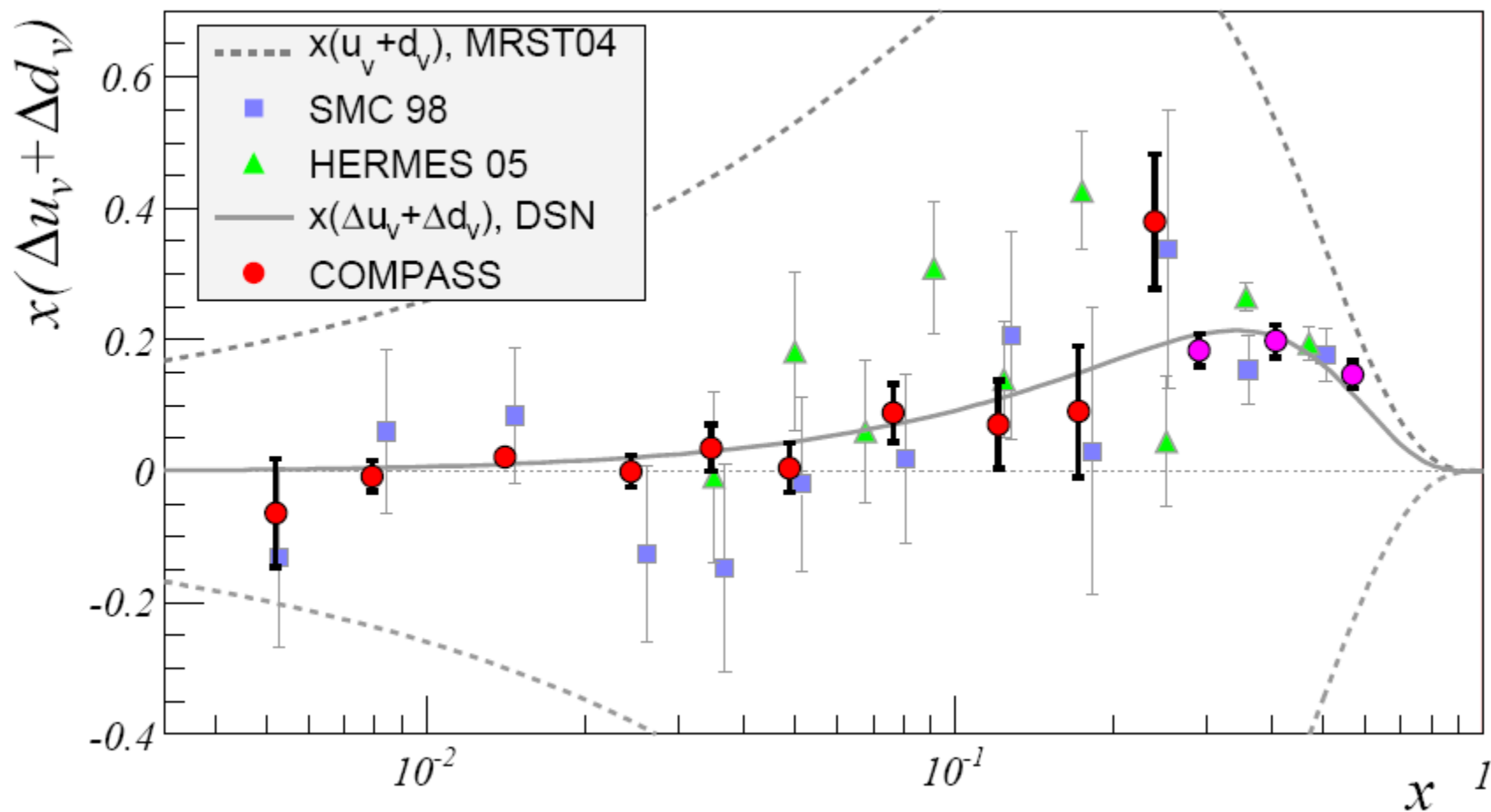
$$A_d^{\pi^+-\pi^-}(x) = A_d^{K^+-K^-}(x) = \frac{\Delta u_v(x) + \Delta d_v(x)}{u_v(x) + d_v(x)}$$

Valence quark polarisation without
fragmentations function

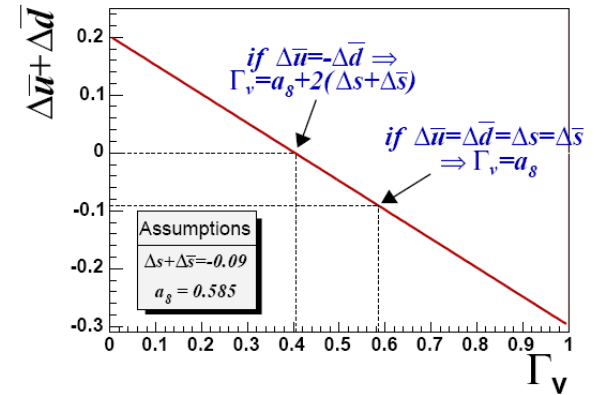
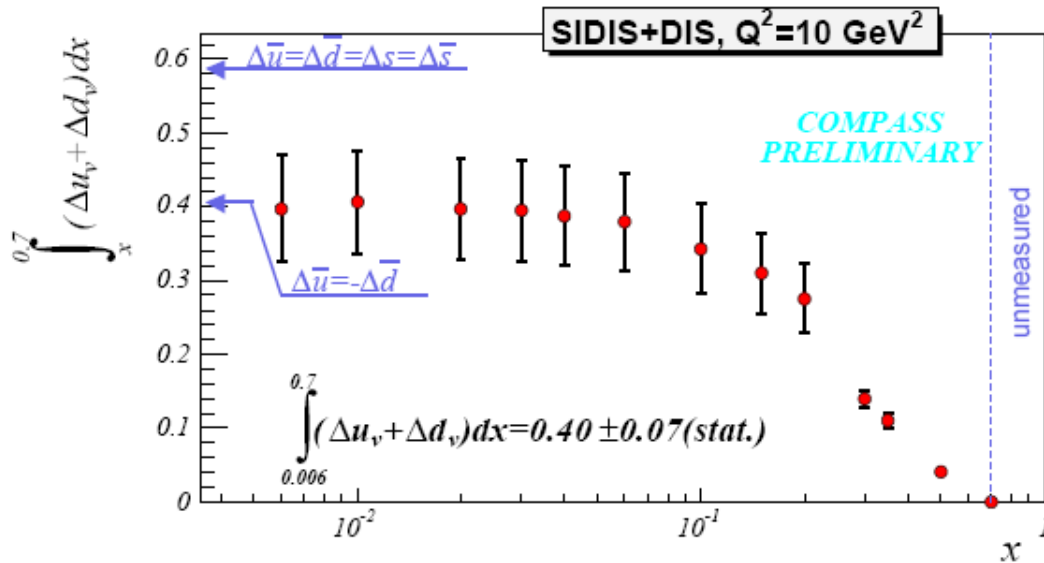




Valence polarization



Valence quark polarisation

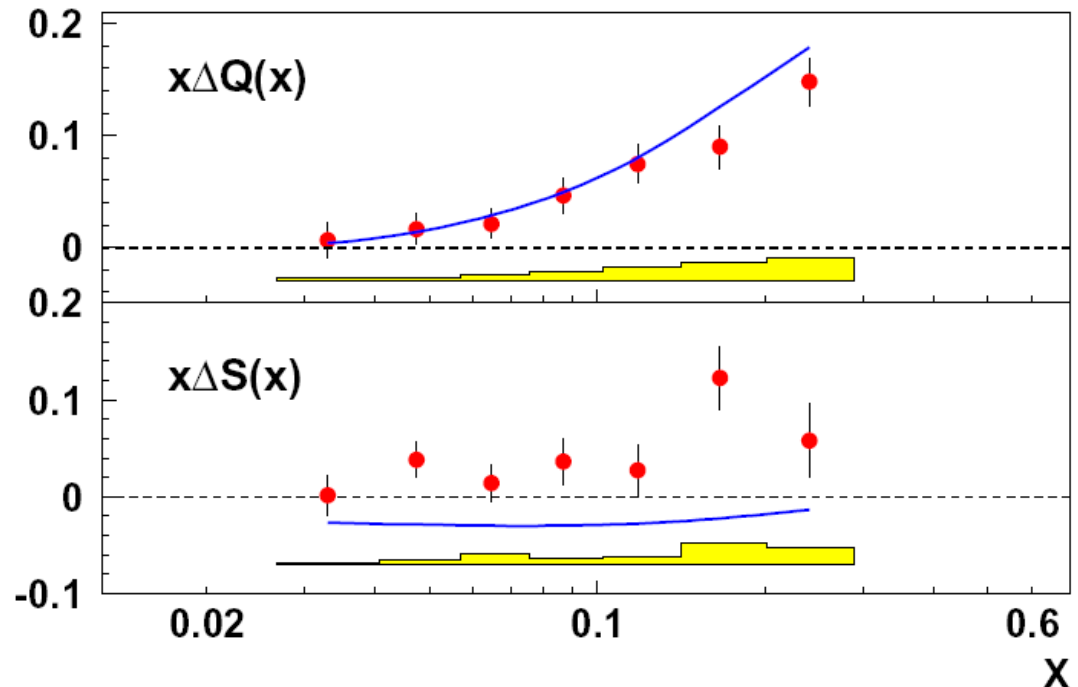


	x-range	Q^2 GeV ²	$\Delta u_v + \Delta d_v$		$\Delta \bar{u} + \Delta \bar{d}$	
			measur.	DNS	measur.	DNS
SMC 98	0.003–0.7	10	$0.26 \pm 0.21 \pm 0.11$	0.386	$0.02 \pm 0.08 \pm 0.06$	-0.009
HERMES 05	0.023–0.6	2.5	$0.43 \pm 0.07 \pm 0.06$	0.363	$-0.06 \pm 0.04 \pm 0.03$	-0.005
COMPASS	0.006–0.7	10	$0.40 \pm 0.07 \pm 0.05$	0.385	$0.0 \pm 0.04 \pm 0.03$	-0.007

Strange quark sea

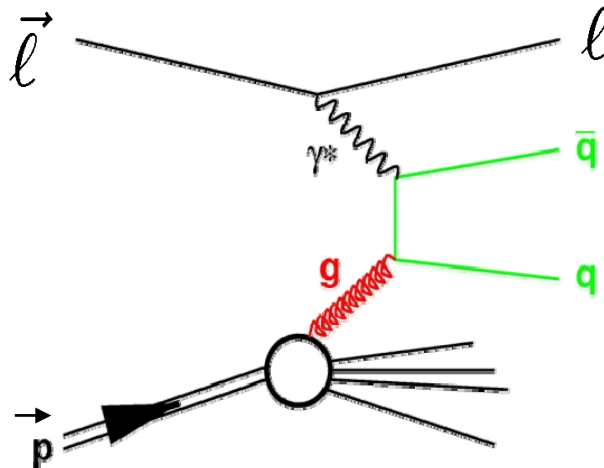
- semi-inclusive data incl. kaon $A_{||,d}^{K^\pm}(x)$
- $\Delta Q = \Delta q + \Delta \bar{q}$
- $\Delta S = 0.037 \pm 0.019 \pm 0.027$
- $\Delta S < 0$ expected from incl. data
- results from COMPASS at Spin 2008

$Q^2 = 2.5 \text{ GeV}^2$



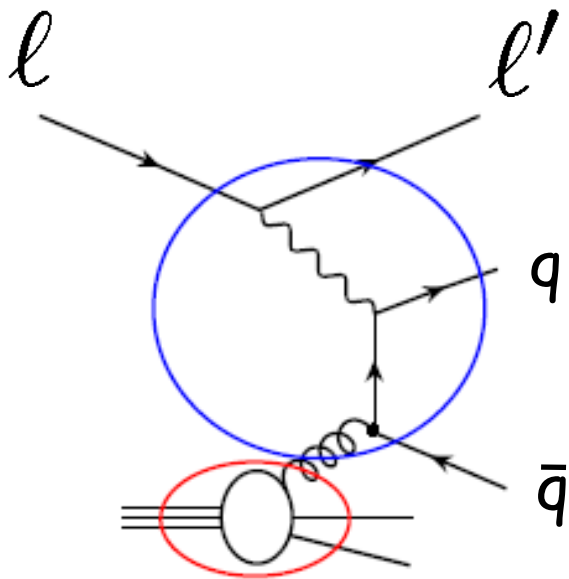
$\Delta g/g$ from hadron production

Photon-gluon fusion



Hadron production in DIS via PGF

Principle: Gluon polarization enters via photon-gluon fusion (PGF)



$$A_{||} = R_{pgf} \langle \hat{a}_{pdf} \rangle \left\langle \frac{\Delta g}{g} \right\rangle$$

- measure $A_{||}$
- calculate R_{pgf} , $\langle \hat{a}_{pgf} \rangle$ and background by Monte Carlo

Analyzed channels for $\Delta g/g$

analysed data sets:

– high- p_T hadron pairs (no ID, pions/kaons)

- $Q^2 > 1 \text{ GeV}^2$

LEPTO



- $Q^2 < 1 \text{ GeV}^2$ or unmeasured
"untagged"

PYTHIA



– high- p_T single hadron

- small Q^2 or unmeasured
"untagged"

PYTHIA



– single charmed meson

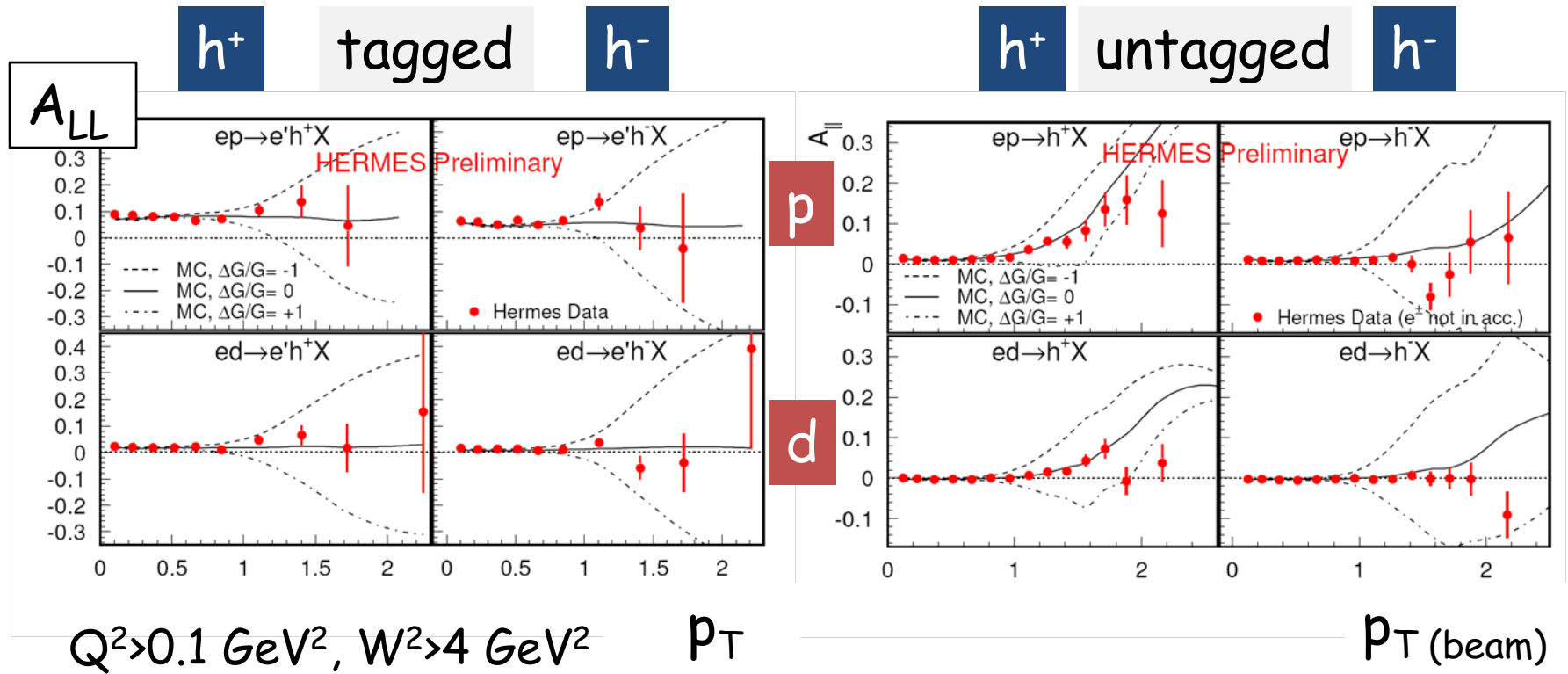
- quasi-real photons

AROMA, RAPGAP



All analyses in LO till now (plus parton showers)

A_{LL} for single hadrons



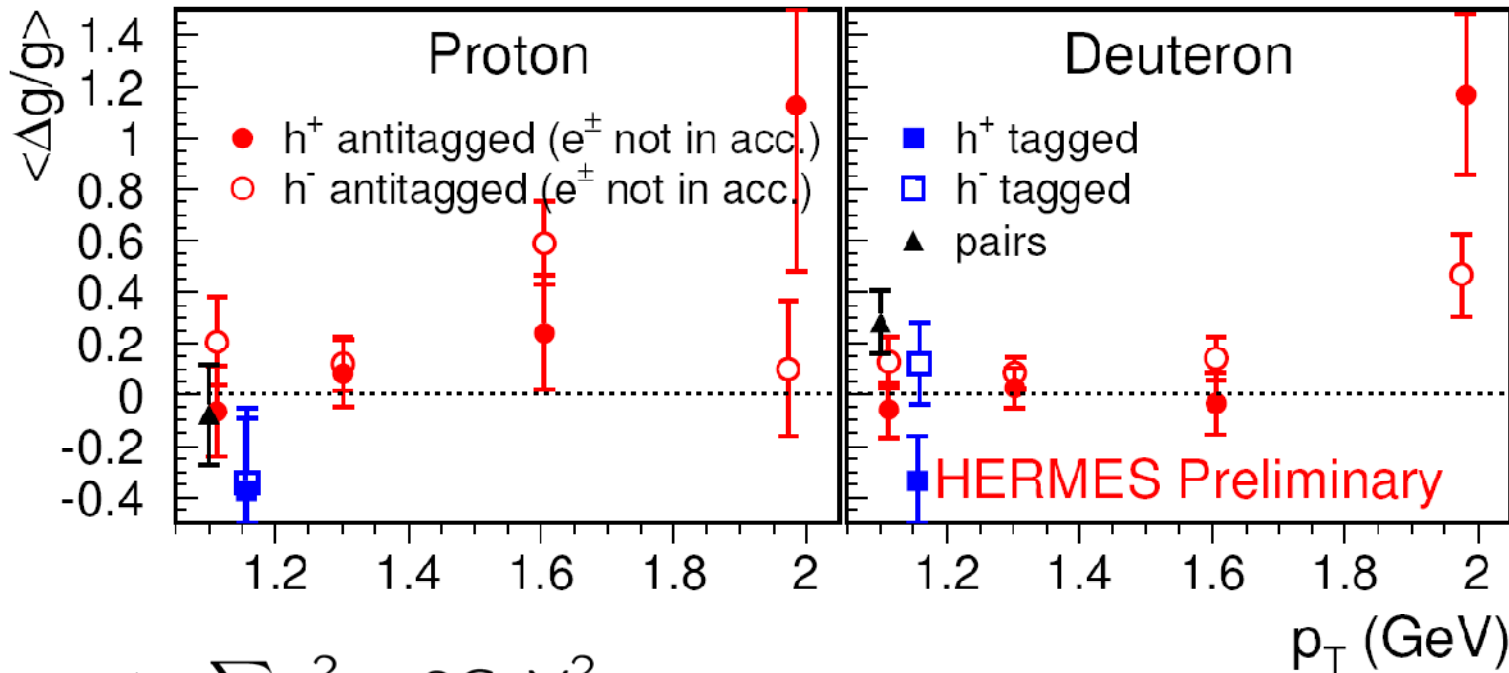
MC plus asymmetry model with $\Delta g/g(x) = -1, 0, 1$ for upper, middle and lower curve

Direct Method (I)

$$\left\langle \frac{\Delta g}{g} \right\rangle = \frac{1}{R_{sig} \langle \hat{a} \rangle} \left\{ A_{||}^{meas} - R_{bg} A_{bg} \right\}$$

from Monte Carlo

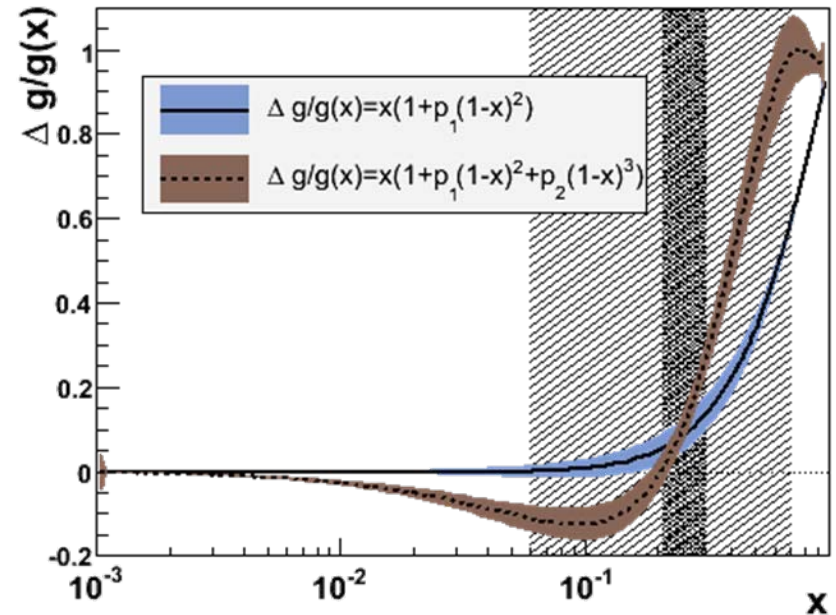
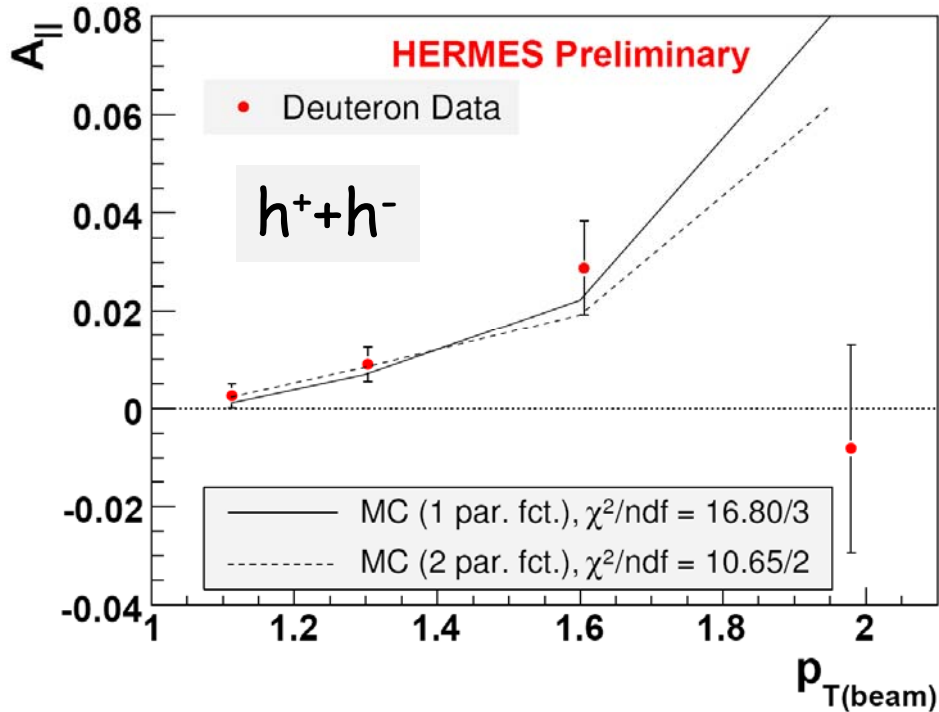
statistical errors only



▲ pairs: $\sum p_T^2 > 2\text{GeV}^2$

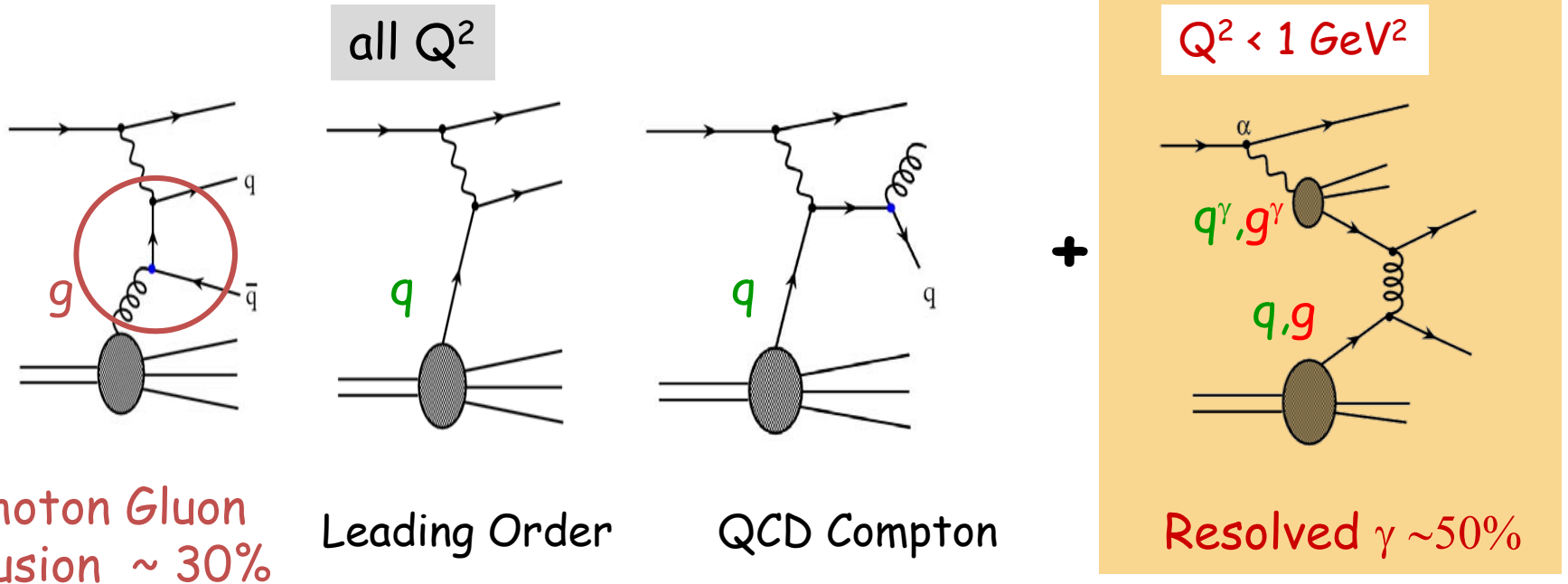
Indirect Method (II)

Fit parameters of polynomial function to A_{\parallel} using MC





$\Delta G/G$ from high- p_T pairs



$$A_{LL}^{2h} = R_{pgf} a_{LL}^{pgf} \frac{\Delta g}{g}(x_g) + R_{LO} D A_1^{LO}(x_{Bj}) + R_C a_{LL}^C A_1^{LO}(x_C)$$

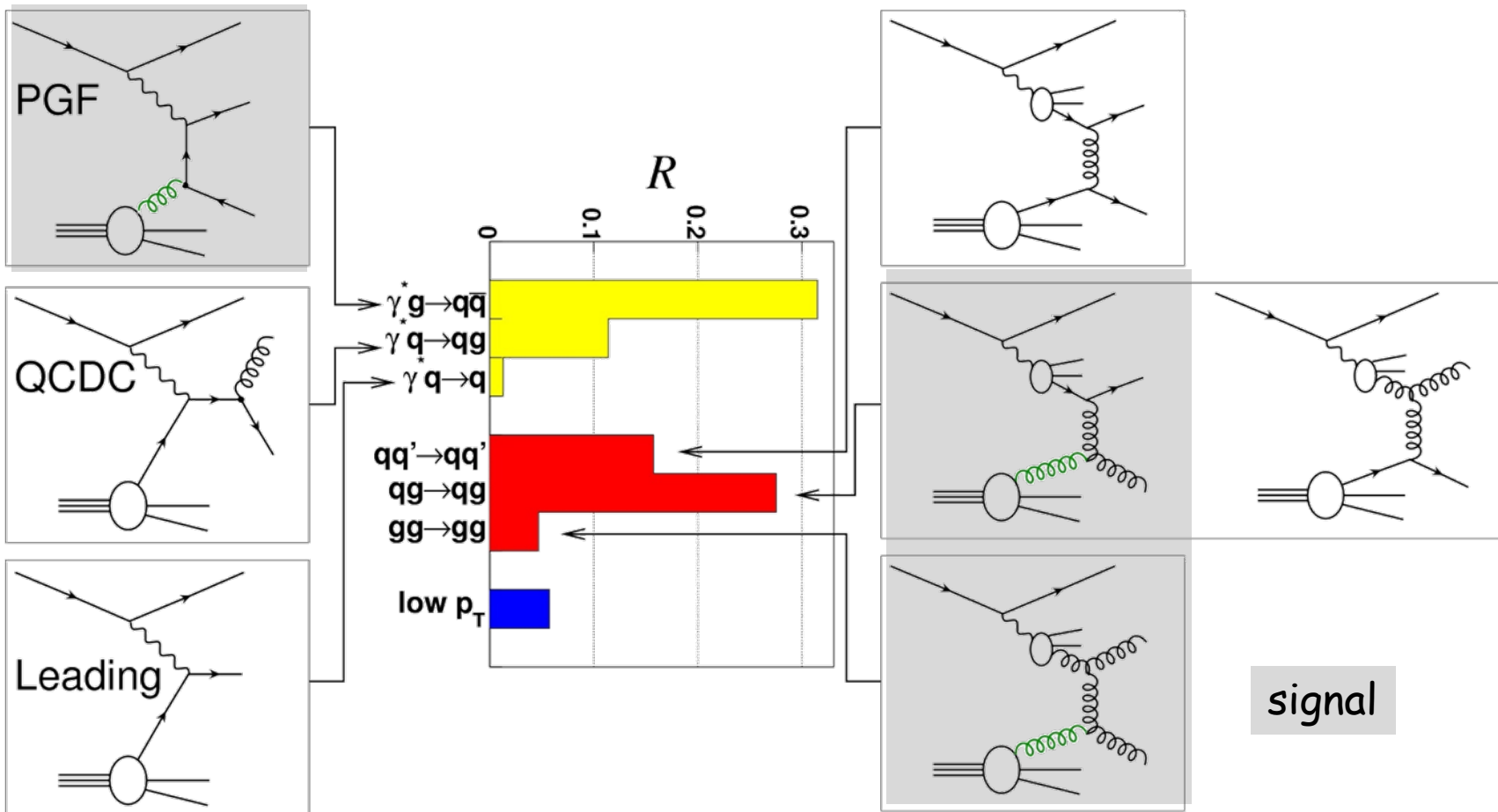
use also inclusive A_{LL}



High- p_T pairs, low Q^2

Ratios for hadron pairs with for $Q^2 < 1$

Resolved photons





High- p_T pairs, $Q^2 > 1 \text{ GeV}^2$

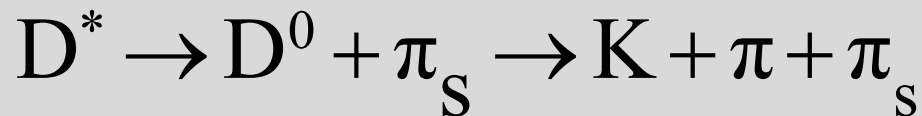
$$A_{LL}^{2h} = R_{pgf} a_{LL}^{pgf} \frac{\Delta g}{g}(x_g) + R_{LOD} A_1^{LO}(x_{Bj}) + R_C a_{LL}^C A_1^{LO}(x_C)$$

- tune MC (Lepto) to reproduce data
- estimate relative fractions R on event-by-event basis using NN trained with MC events (kin. variables)
- use in NN output as event weight
- looser cuts possible
 - $Q^2 > 1 \text{ GeV}^2$
 - $p_{T1,2} > 0.7 \text{ GeV}$
 - $x_F > 0$, inv. mass $2h > 1.5 \text{ GeV}^2$



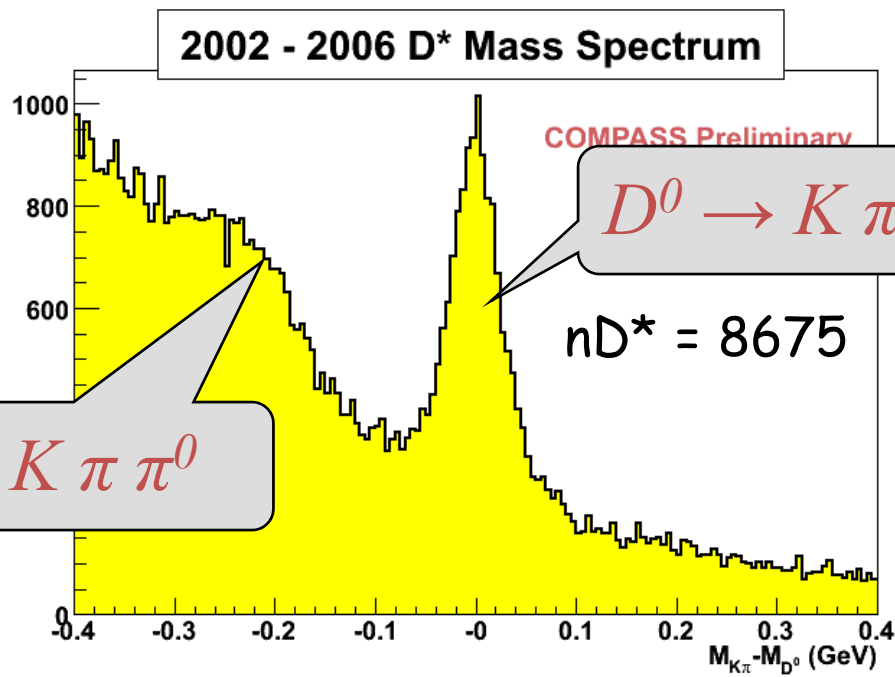
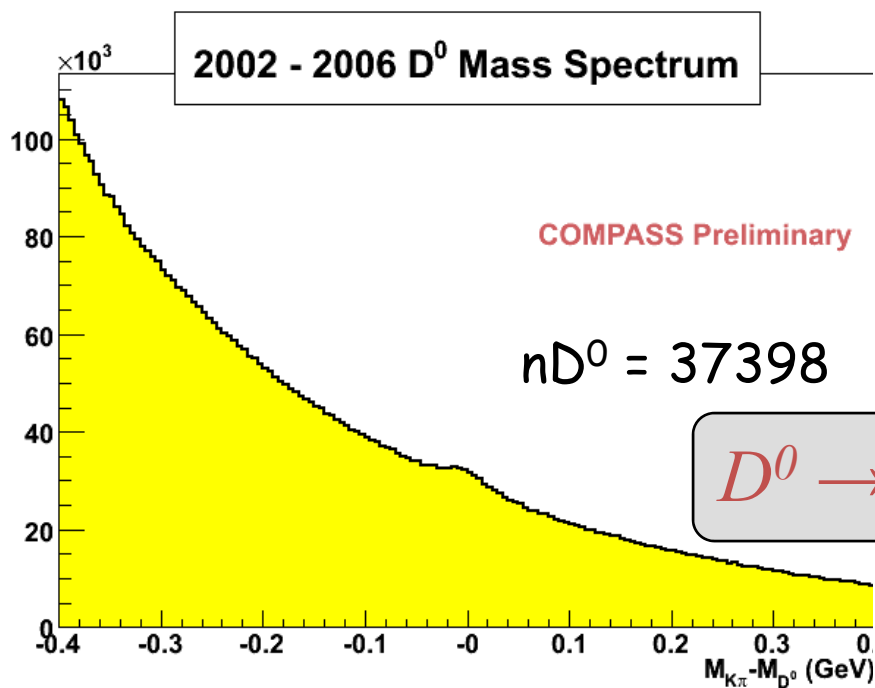
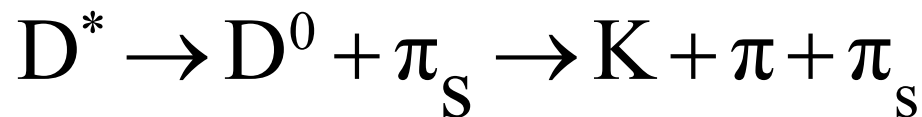
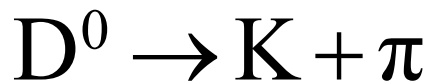
$\Delta g/g$ from open charm

- cleanest process (“golden channel”)
 - no or little physics background (LO, QCDC)
- observe asymmetry in D meson production
 - strongly statistics limited
 - only one D meson via $D \rightarrow \pi K$ (BR $\sim 4\%$)
 - combinatorial background large
 - drastically reduced when looking to D^* decay in coincidence with slow pion



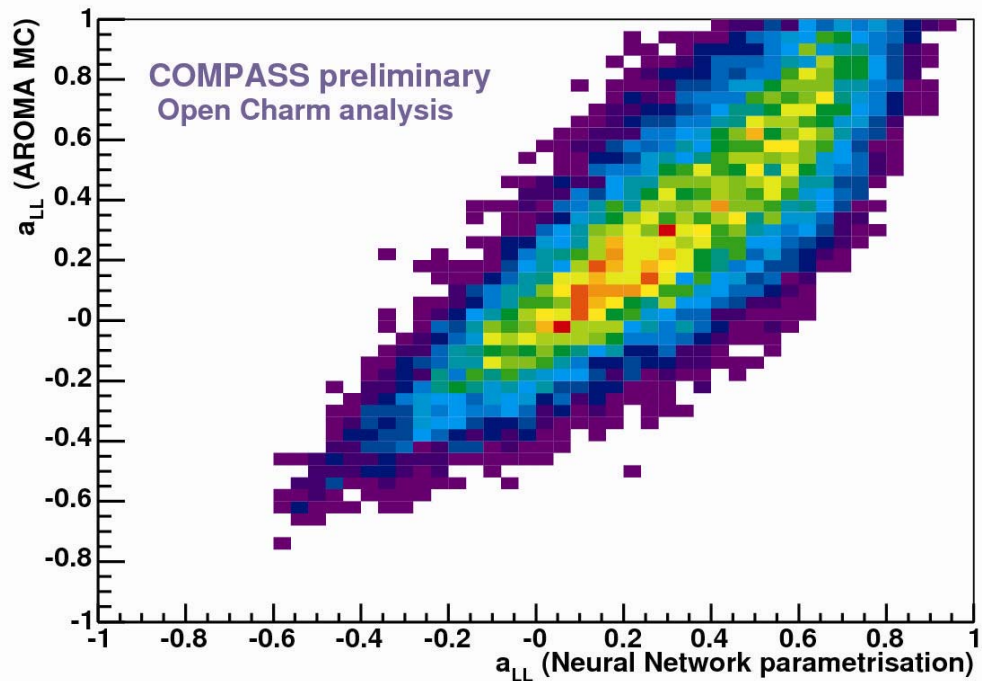
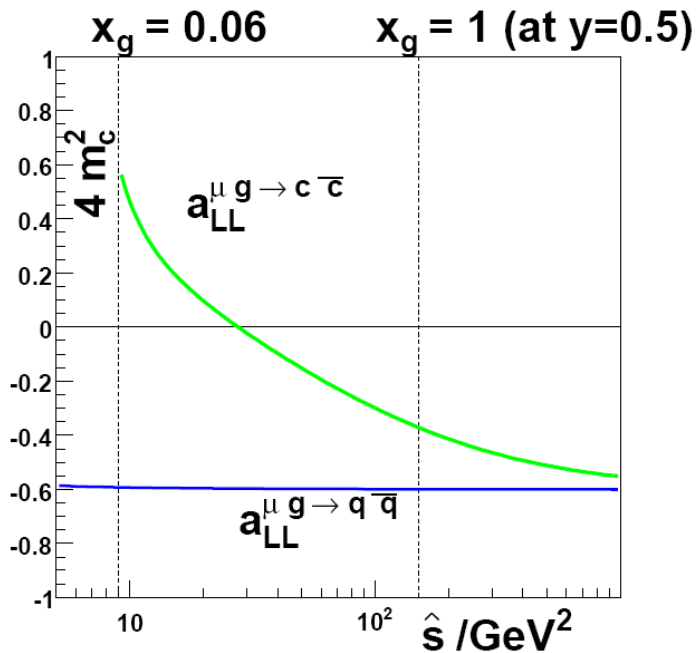


D mass spectra

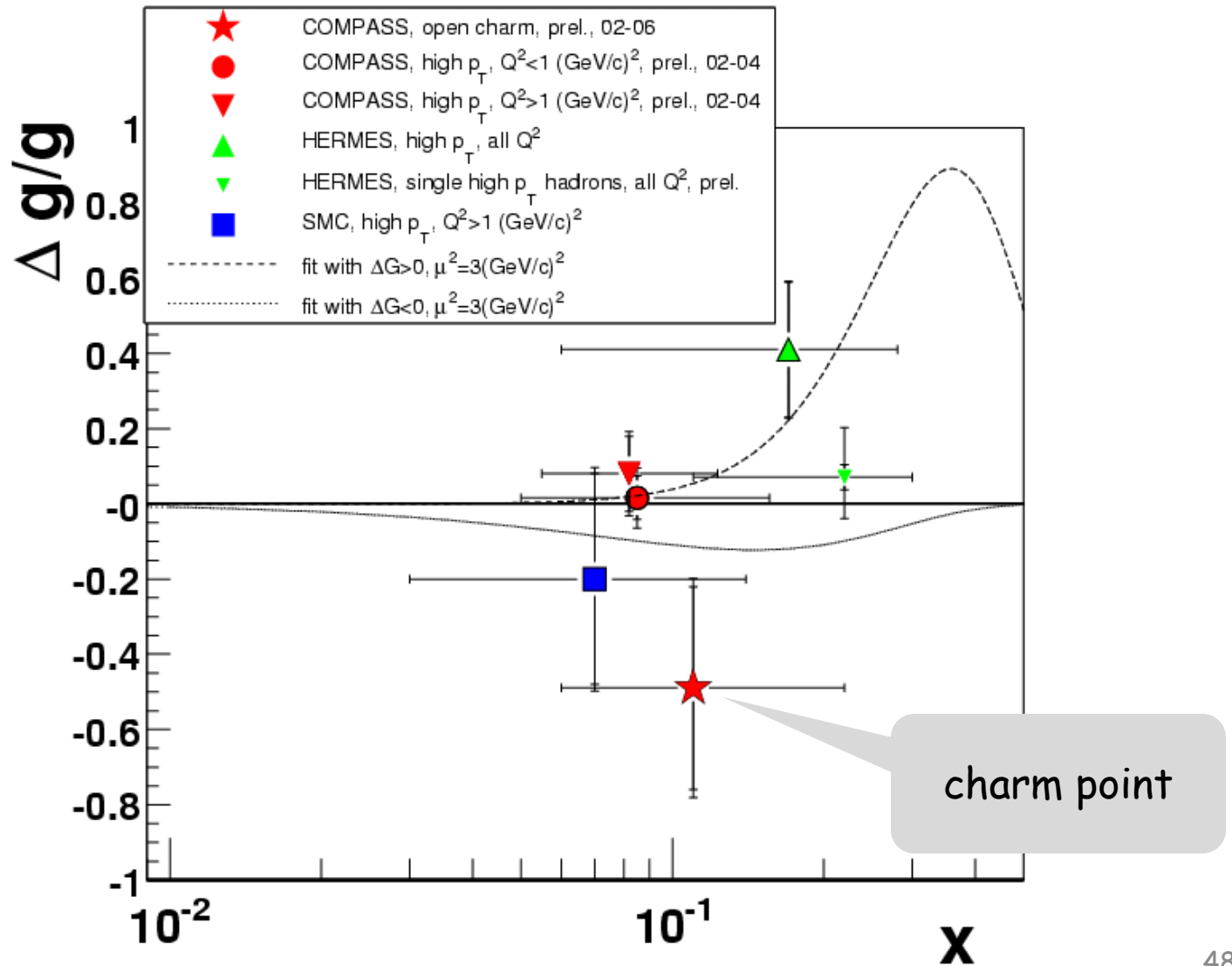




a_{LL} variation



Summary of results on $\Delta g/g$

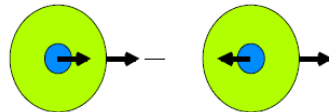


Transversity

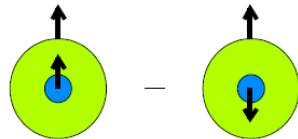
q, g



$\Delta q, \Delta g$



$\Delta_T q$

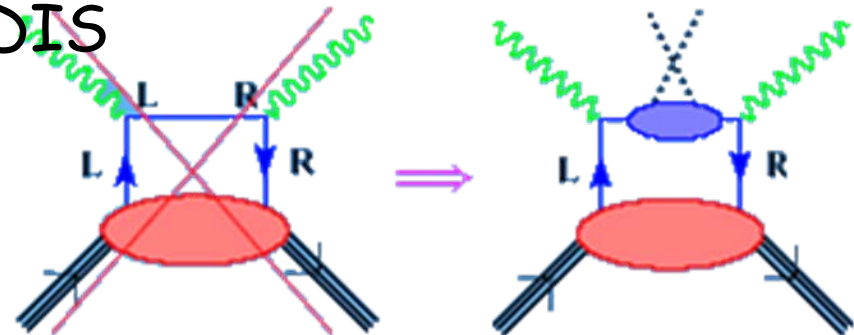


momentum

helicity

transversity (alias h_1)

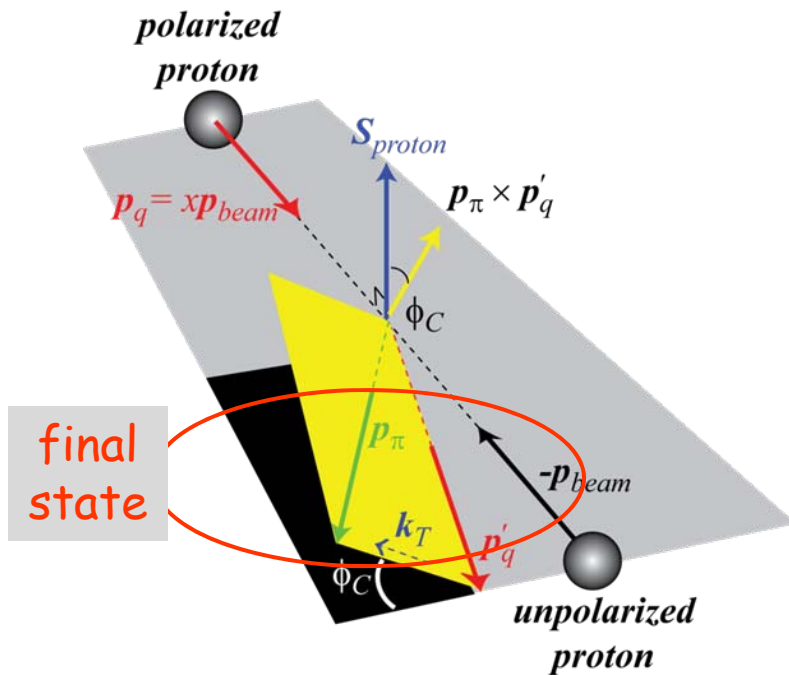
- 3 fundamental twist-2 PDFs, new transversity $\Delta_T q(x)$
- non-relativistic $\Delta_T q = g_1$
- **chiral-odd** PDF \rightarrow not seen in DIS
- semi-inclusive DIS allowed if coupled to a **chiral-odd** FF
- Soffer bound: $2|\Delta_T q| \leq q + \Delta q$



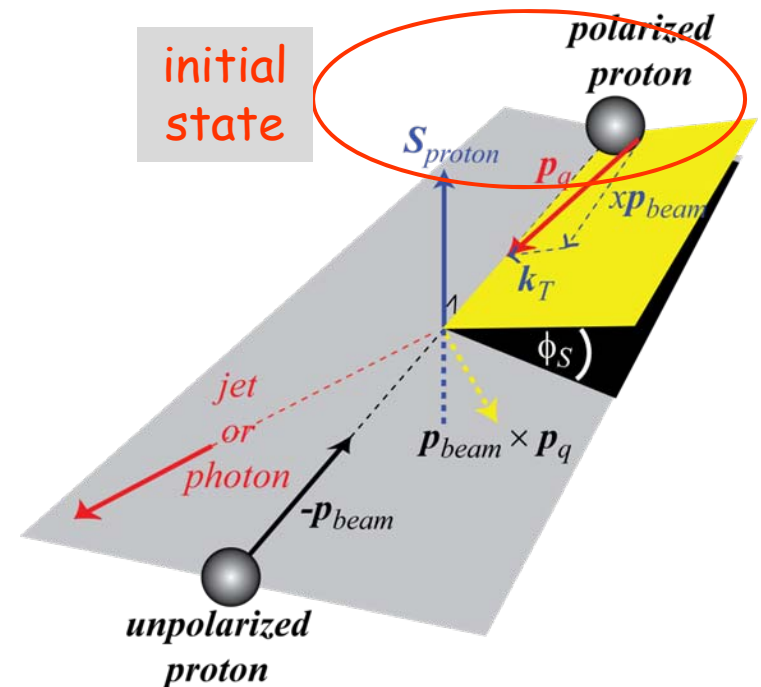
Origin of single-spin asymmetries

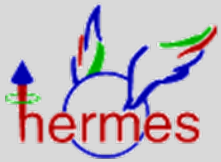
from L. Bland

Collins/Heppelmann mechanism requires *transverse quark polarization* and *spin-dependent fragmentation*

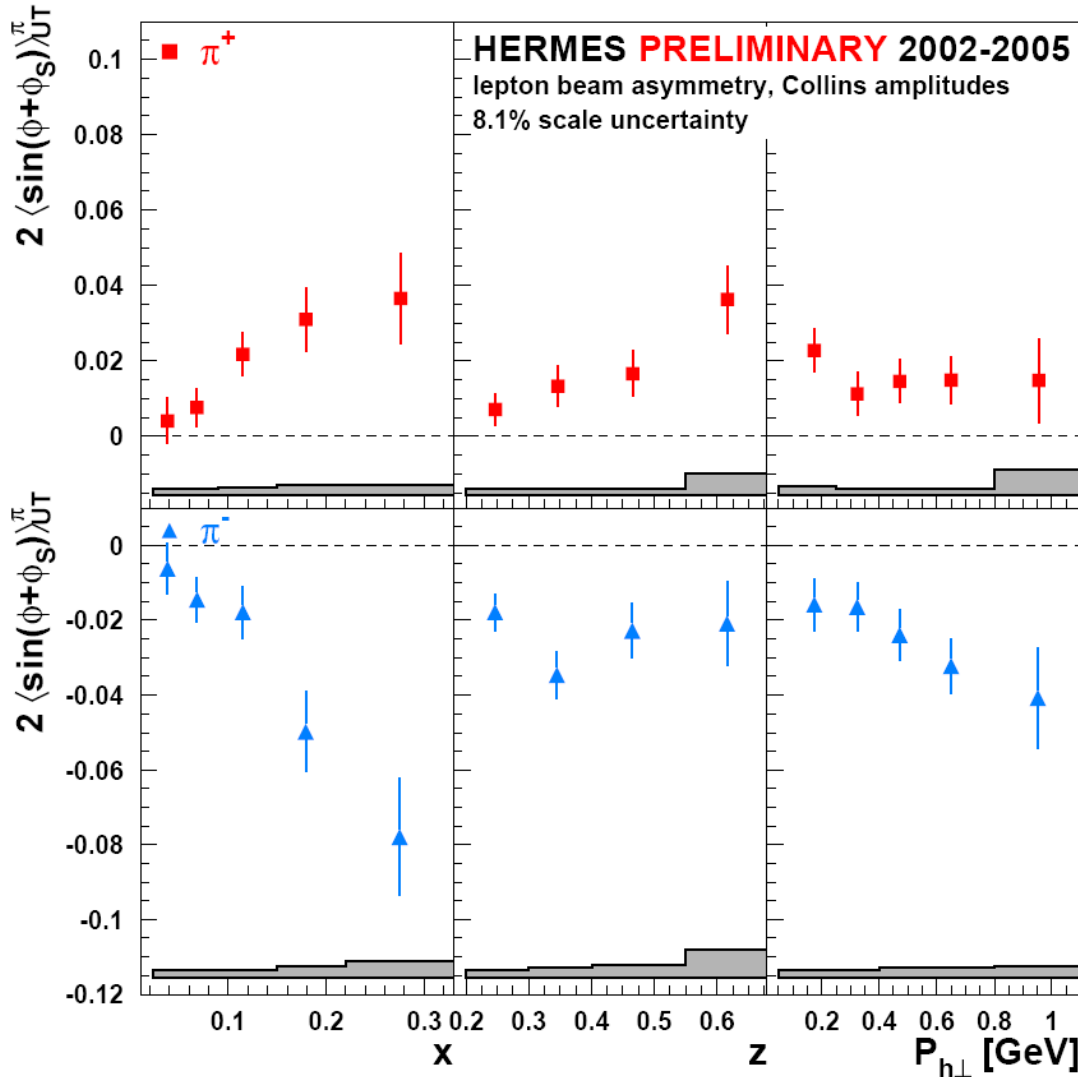


Sivers mechanism requires *spin-correlated transverse momentum k_T* in the proton (orbital motion).

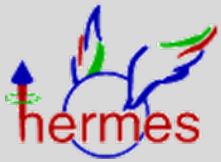




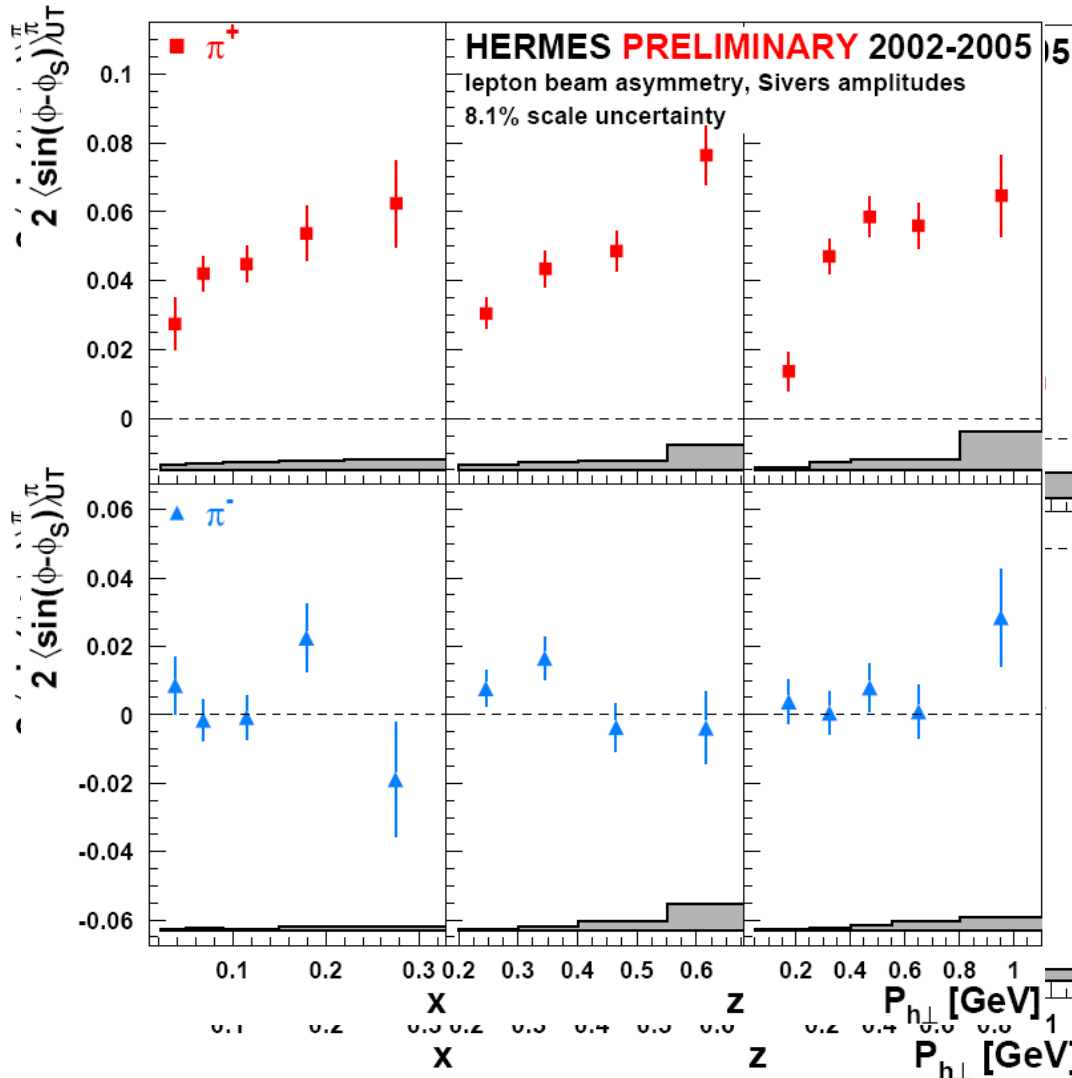
Collins asymmetry (proton)



- at large x :
- large and positive for π^+
- large and negative for π^-



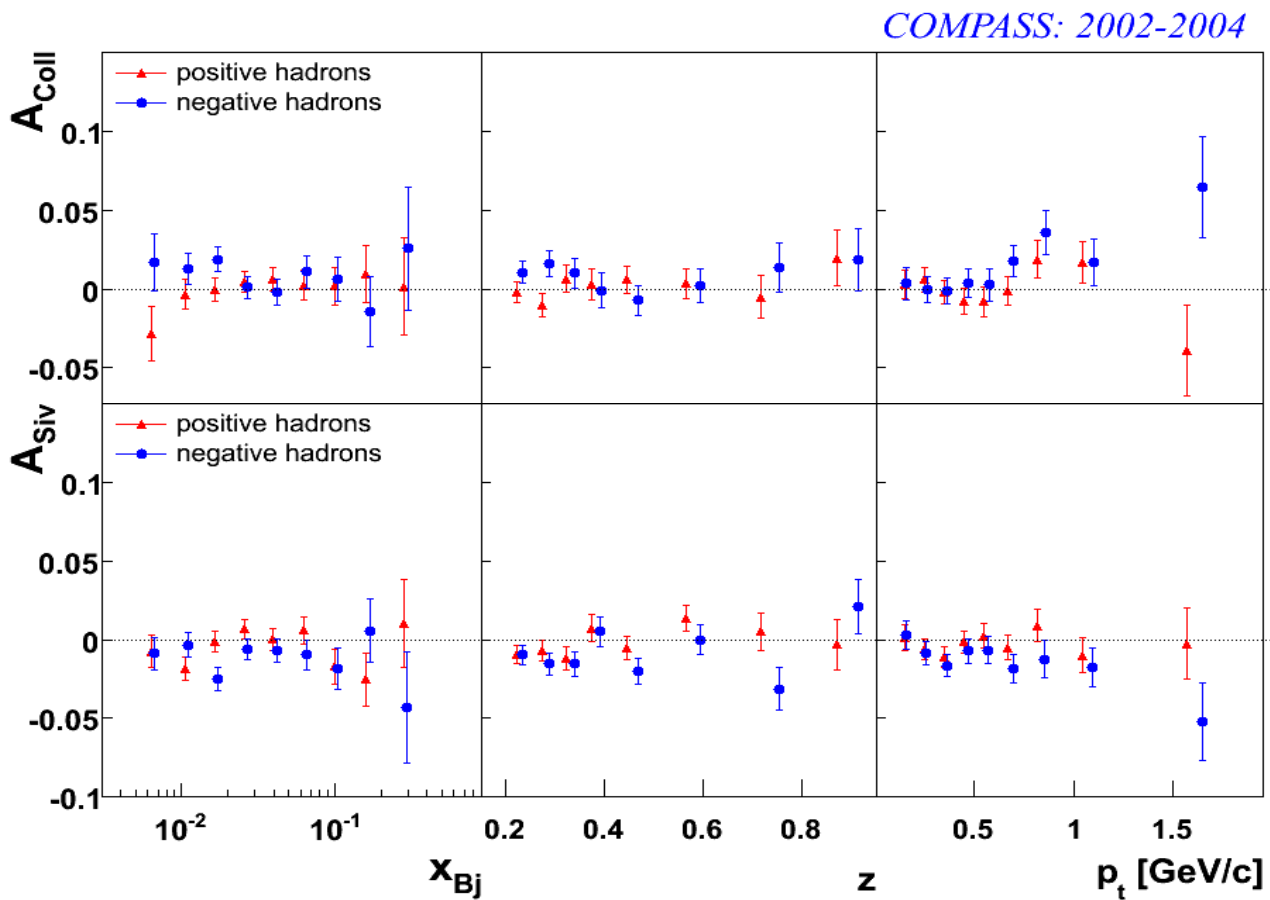
Sivers asymmetry (proton)



- large and positive for π^+
- small for π^-



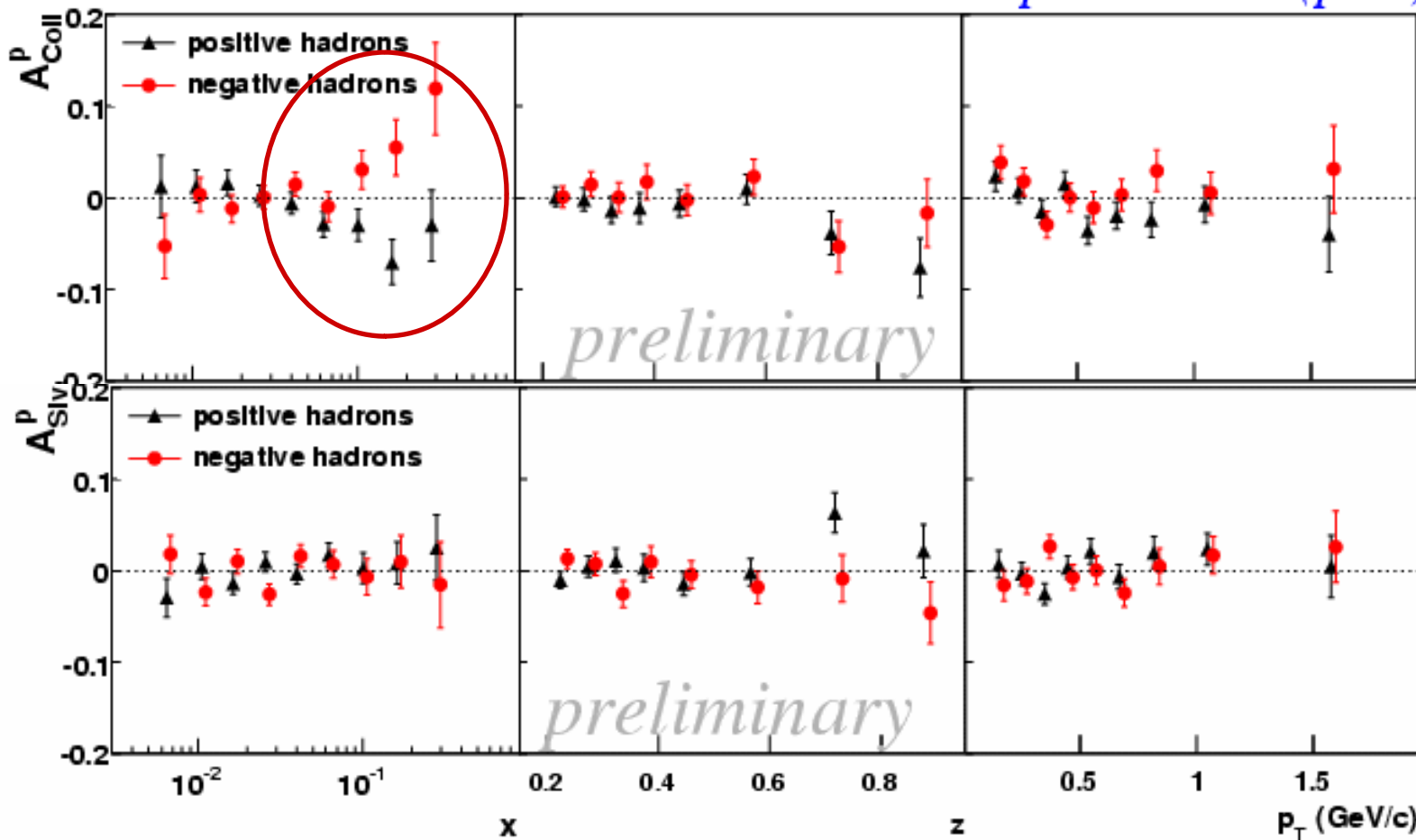
Collins & Sivers asymmetries (deut.)





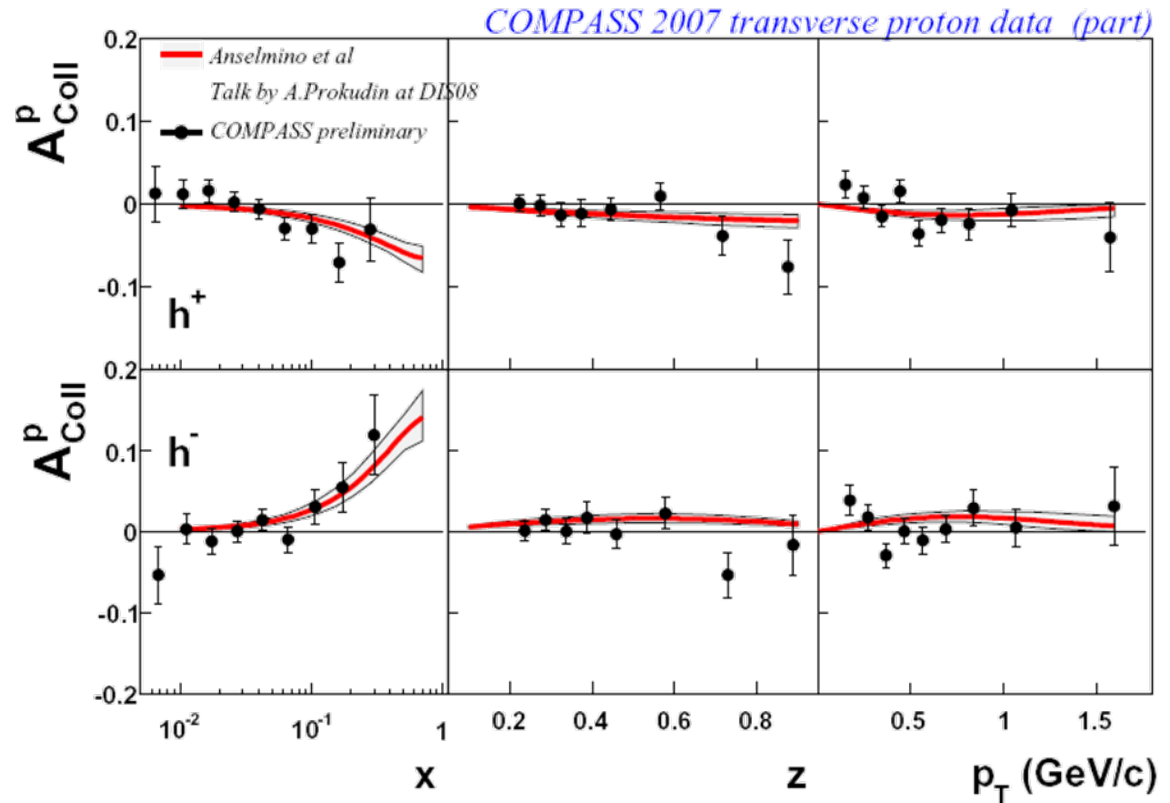
Collins & Sivers asym (proton)

COMPASS 2007 proton data (part)



Towards a global fit

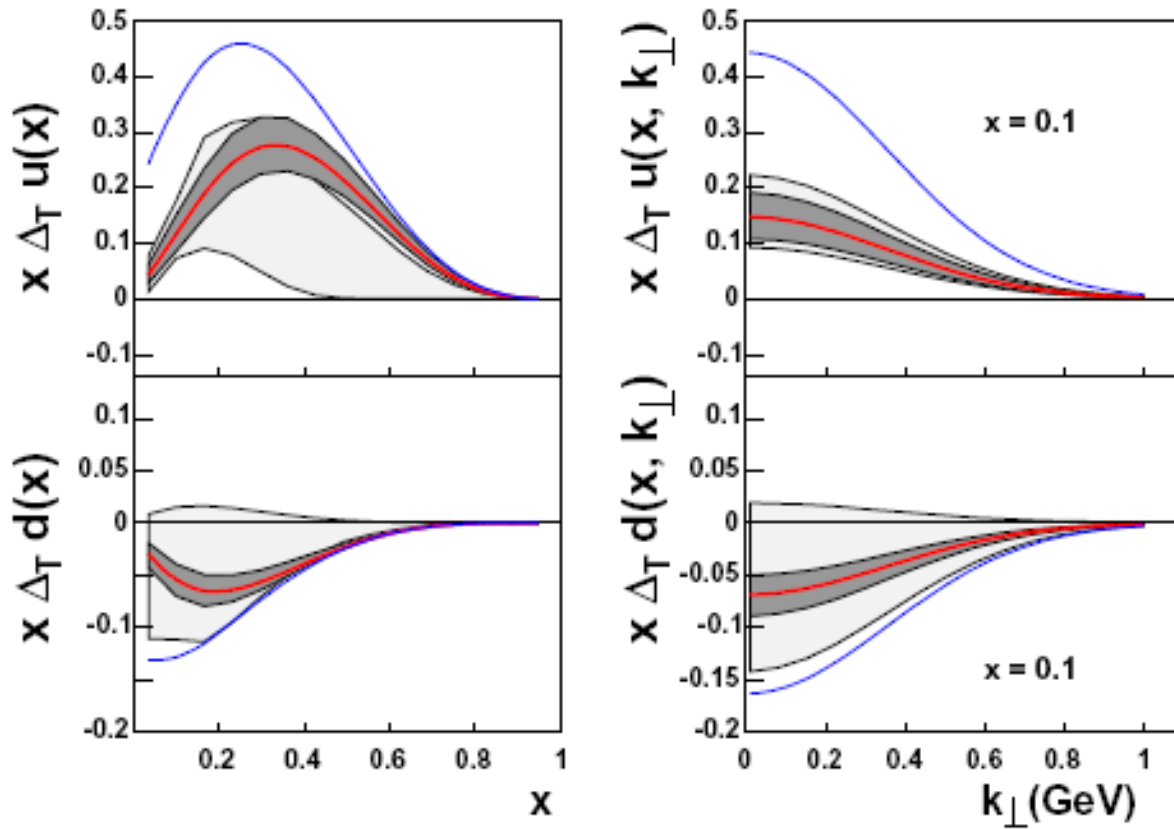
- Data
 - Hermes p
 - COMPASS p,d
 - Belle fragm.



Prokudin et al., DIS2008

A glimpse of transversity

- towards a global analysis



Anselmino et al., DIS2008

Summary & Outlook

Exciting times behind AND ahead of us:

- Bjorken sum rule confirmed at 10%
- quark polarization are well measured
- anti-quark still need improvement
- first handles on $\Delta g/g$, axial anomaly
will not restore quark spin contribution of 0.6
- GPD will be the topic of the next decade