



# Helicity quark distributions from DIS and SIDIS measured in COMPASS

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On behalf of the COMPASS collaboration

*XVI International Workshop  
on Deep-Inelastic Scattering  
and Related Subjects*

London, April 7-11, 2008

$$\frac{1}{2} = \frac{1}{2} \Delta \Sigma + \Delta G + L_z$$

$\Delta \Sigma = \Delta u + \Delta \bar{u} + \Delta d + \Delta \bar{d} + \Delta s + \Delta \bar{s}$

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<sup>a</sup>on leave from JINR, Dubna

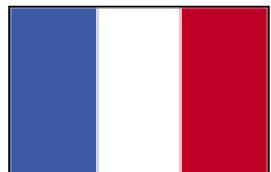
## Overview

- COMPASS experiment
- Inclusive asymmetry  $A_1^d$  and structure function  $g_1^d$   
V.Yu.Alexakhin et al., PLB 647 (2007) 8-17; PLB 647 (2007) 330-340.
- Valence quark distributions from hadron asymmetry  $A_d^{h^+ - h^-}$   
M.Alekseev et al., PLB 660 (2008) 458-465.
- Projection of the statistical precision for the data collected on  ${}^6\text{LiD}$  target in 2006 and on  $\text{NH}_3$  target in 2007
- Summary and outlook

## More than 240 physicists from 29 institutes



*Prague(CU,CUT,  
TUL)*



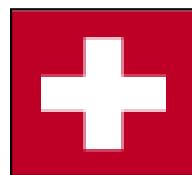
*Saclay*



*Bielefeld  
Bochum  
Bonn(ISKP&PI)  
Erlangen  
Freiburg  
Heidelberg  
Mainz  
Munchen(LMU,TU)*



*Burdwan  
Calcutta*



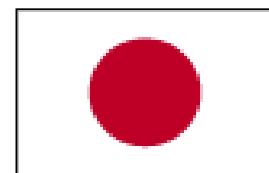
*CERN*



*TelAviv*



*Torino  
(University & INFN)  
Trieste  
(University & INFN)*



*Yamagata*



*Warsaw  
(SINS, TU,  
& WU)*

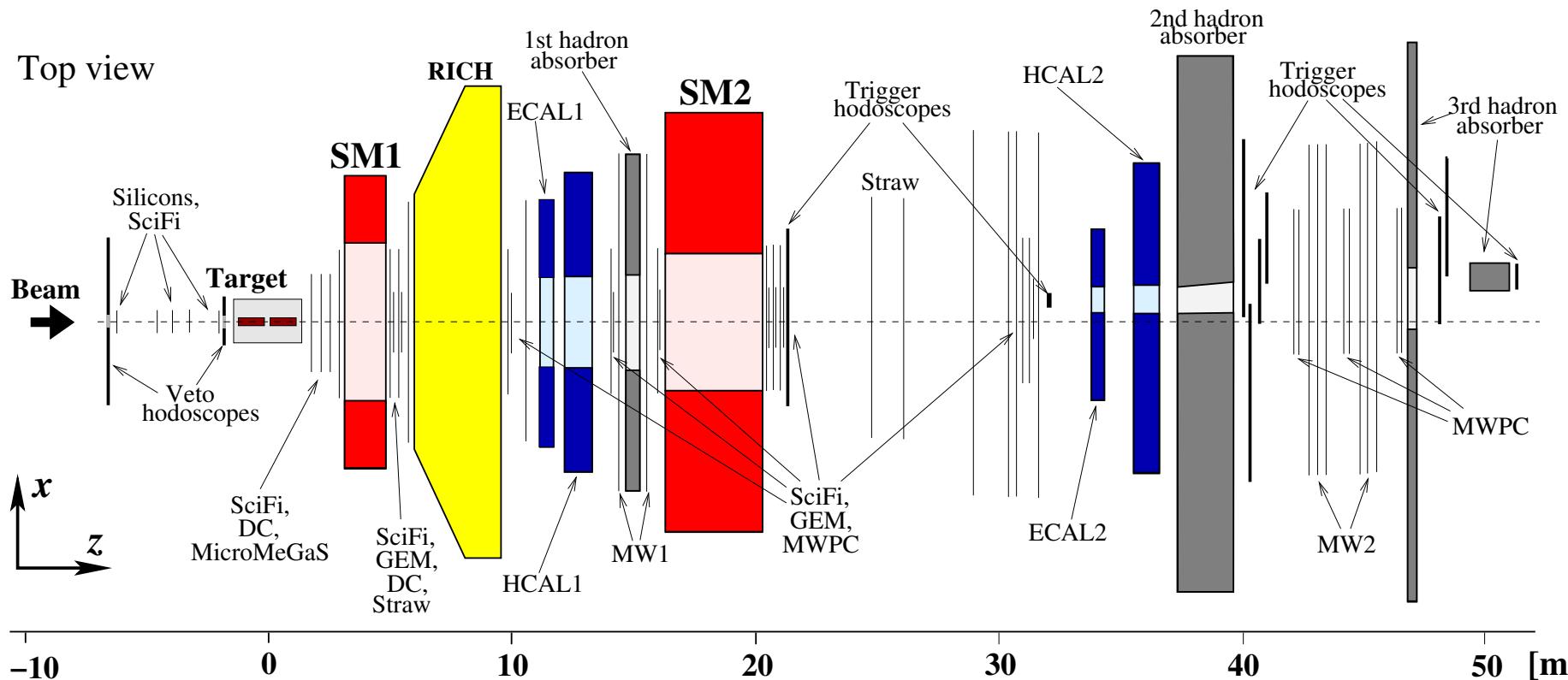


*Lisbon*



*Dubna  
Moscow(INR,LPI,  
State University)  
Protvino*

## Experimental setup



- Polarized beam  $\mu^+$  (-80%),  $E_b=160$  GeV
- 2/3 cells polarized target  ${}^6\text{LiD}$  (50%) and  $\text{NH}_3$  (90%)
- Two stages spectrometer
- Tracking detectors of different types
- Identification: HCALS, ECALS, RICH, muon walls

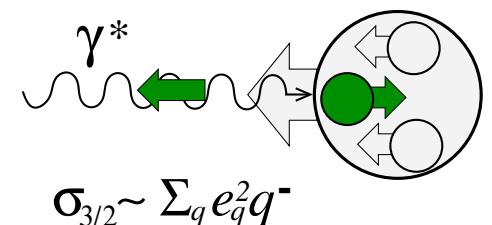
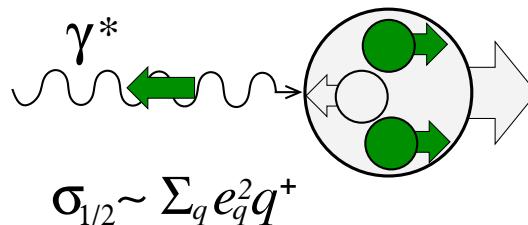
# Inclusive asymmetry $A_1^d$ --- & structure function $g_1^d$ ---

## Deep-inelastic scattering

- Quark densities in QPM:

$$q(x) = q^+(x) + q^-(x)$$

$$\Delta q(x) = q^+(x) - q^-(x)$$



- Longitudinal double-spin asymmetry:  $A^{\gamma N} \equiv A_1 = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}} = \frac{\sum_q e_q^2 \Delta q}{\sum_q e_q^2 q}$

- Spin (in)dependent cross-sections:

$$\sigma = \bar{\sigma} \pm \Delta\sigma$$

- Longitudinal spin asymmetry  $\mu N$ :

$$A^{\mu N} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} = \frac{\Delta\sigma}{\bar{\sigma}} \simeq D A_1$$

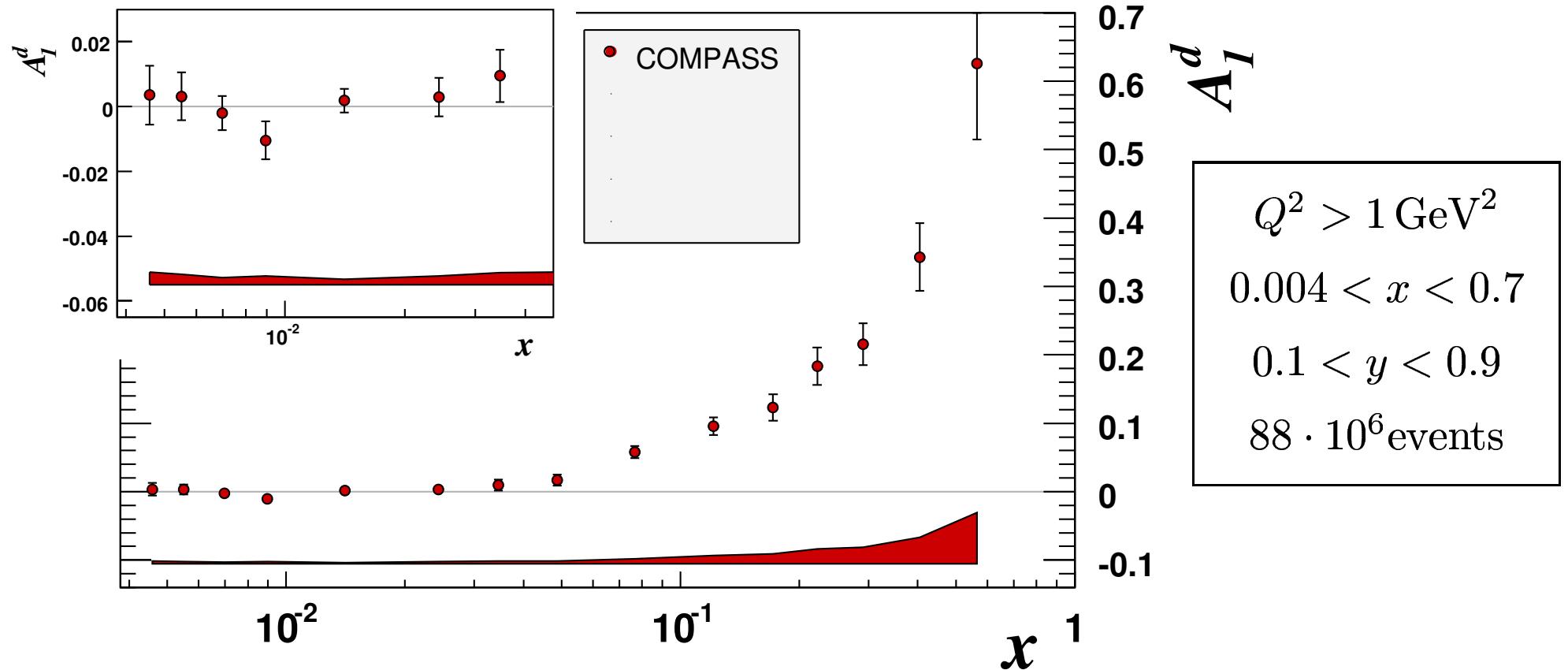
$D$  – depolarization factor of  $\gamma$

- Structure functions & quark distributions:

$$F_1 = \frac{1}{2} \sum_q e_q^2 (q + \bar{q}), \quad g_1 = \frac{1}{2} \sum_q e_q^2 (\Delta q + \Delta \bar{q})$$

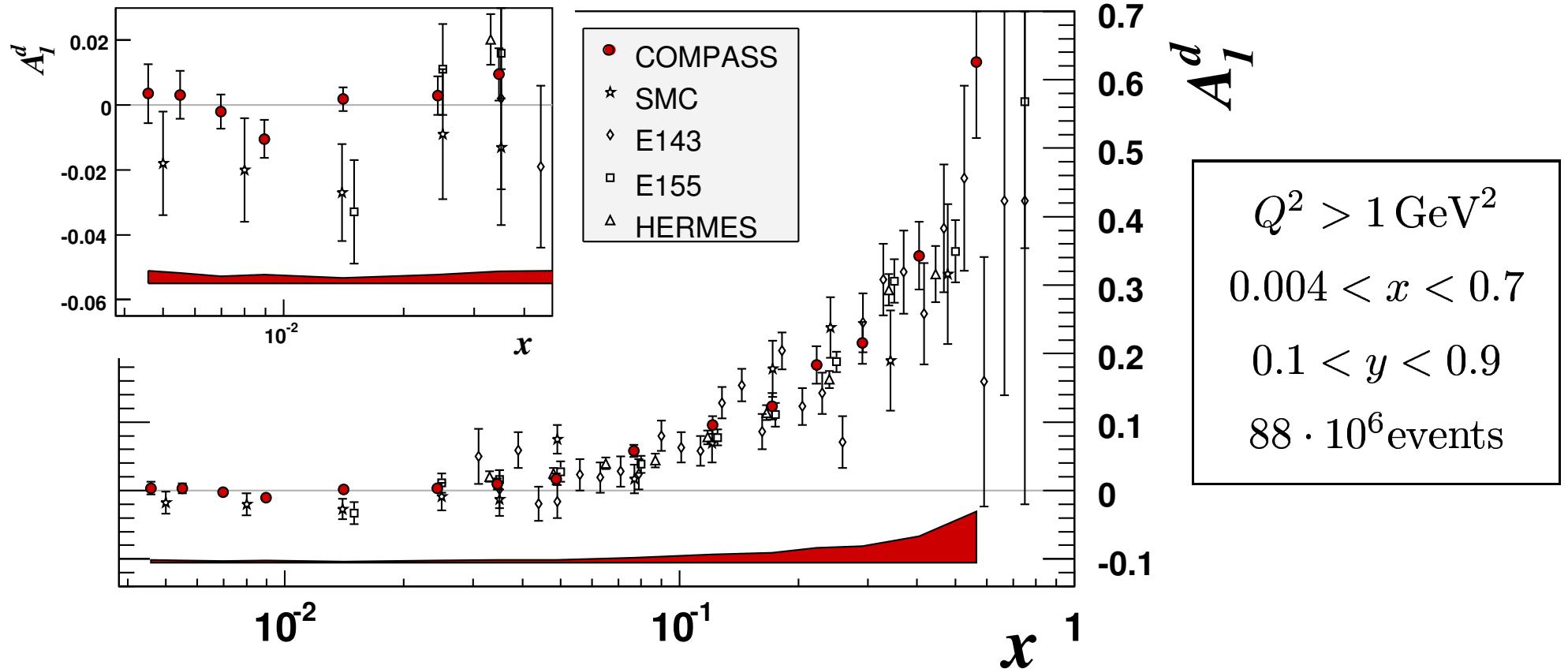
- Asymmetry  $A_1$  gives access to  $g_1$ :  $g_1 \simeq A_1 \cdot F_1$

## Results on Inclusive Asymmetry $A_1^d$



- Good agreement in the region  $x > 0.03$
- For  $x < 0.03$  statistical error is reduced by factor 4
- Results show no tendency toward negative values at  $x < 0.03$

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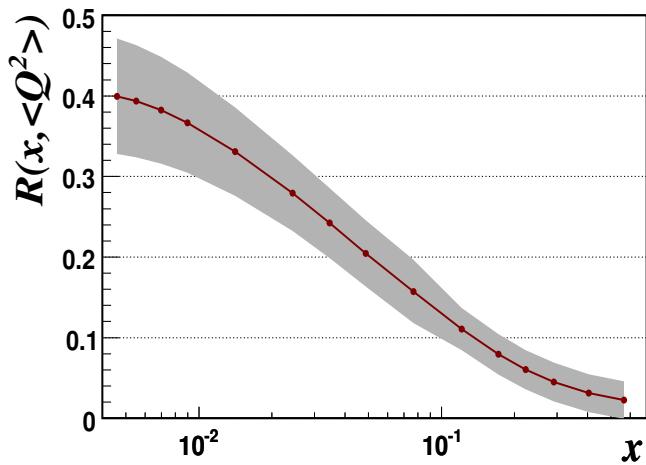
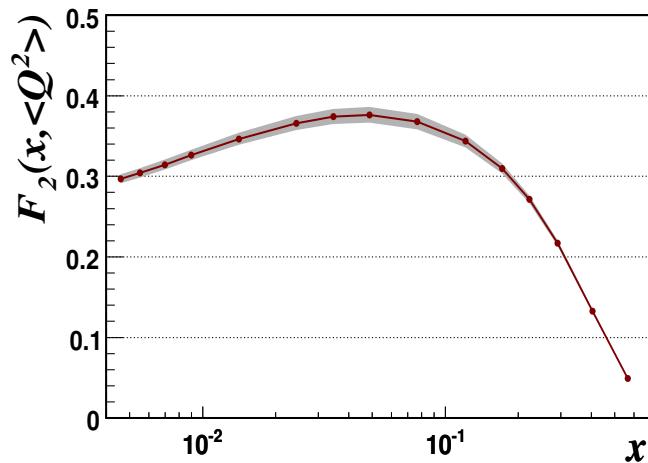


- Good agreement in the region  $x > 0.03$
- For  $x < 0.03$  statistical error is reduced by factor 4
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## Results on Structure Function $g_1^d$

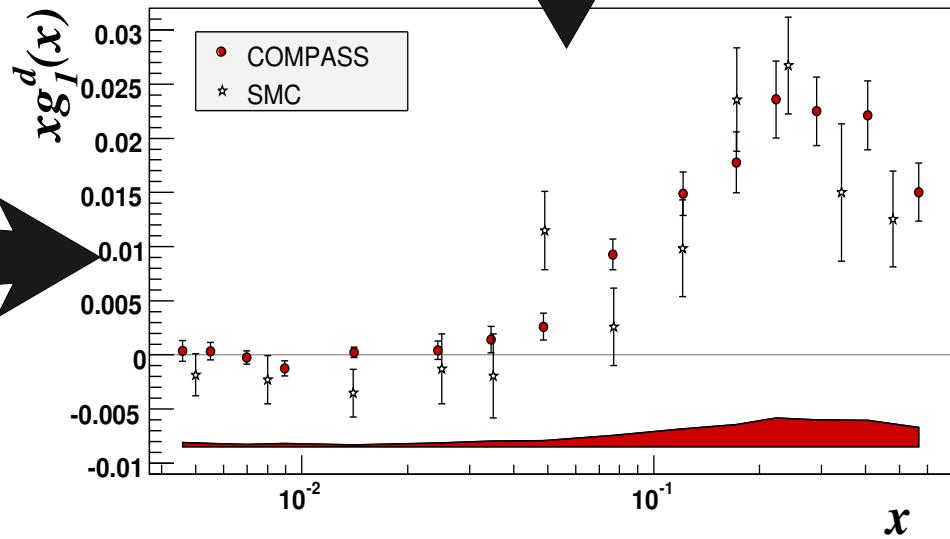
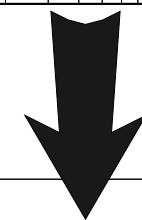
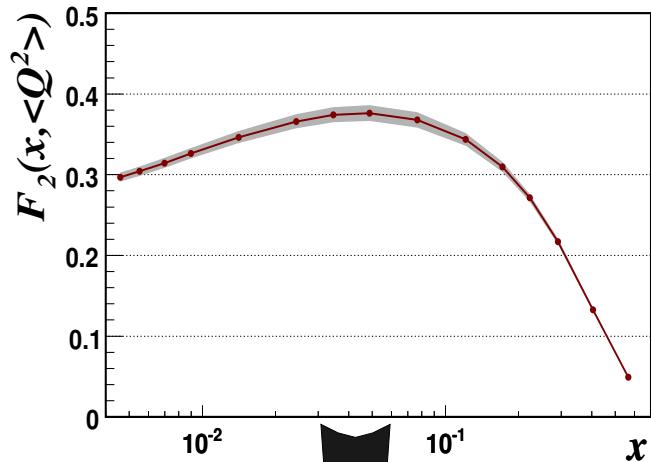
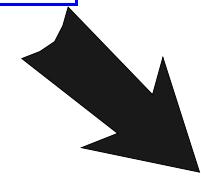
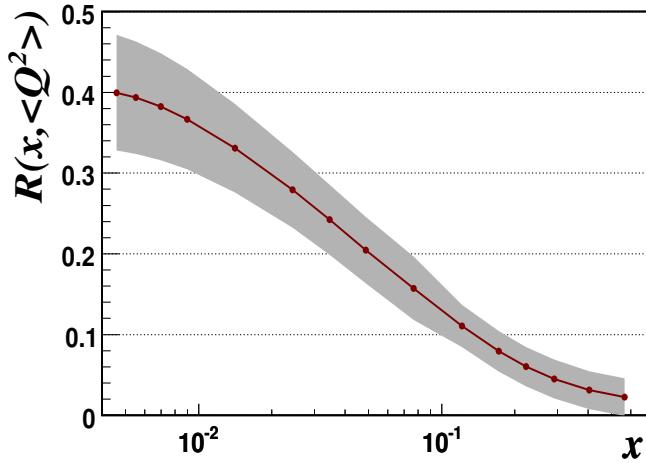
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$$\begin{aligned} g_1^d &= g_1^N \cdot \left(1 - \frac{3}{2}\omega_D\right) \\ &= \frac{F_2^d}{2x(1+R)} A_1^d \end{aligned}$$



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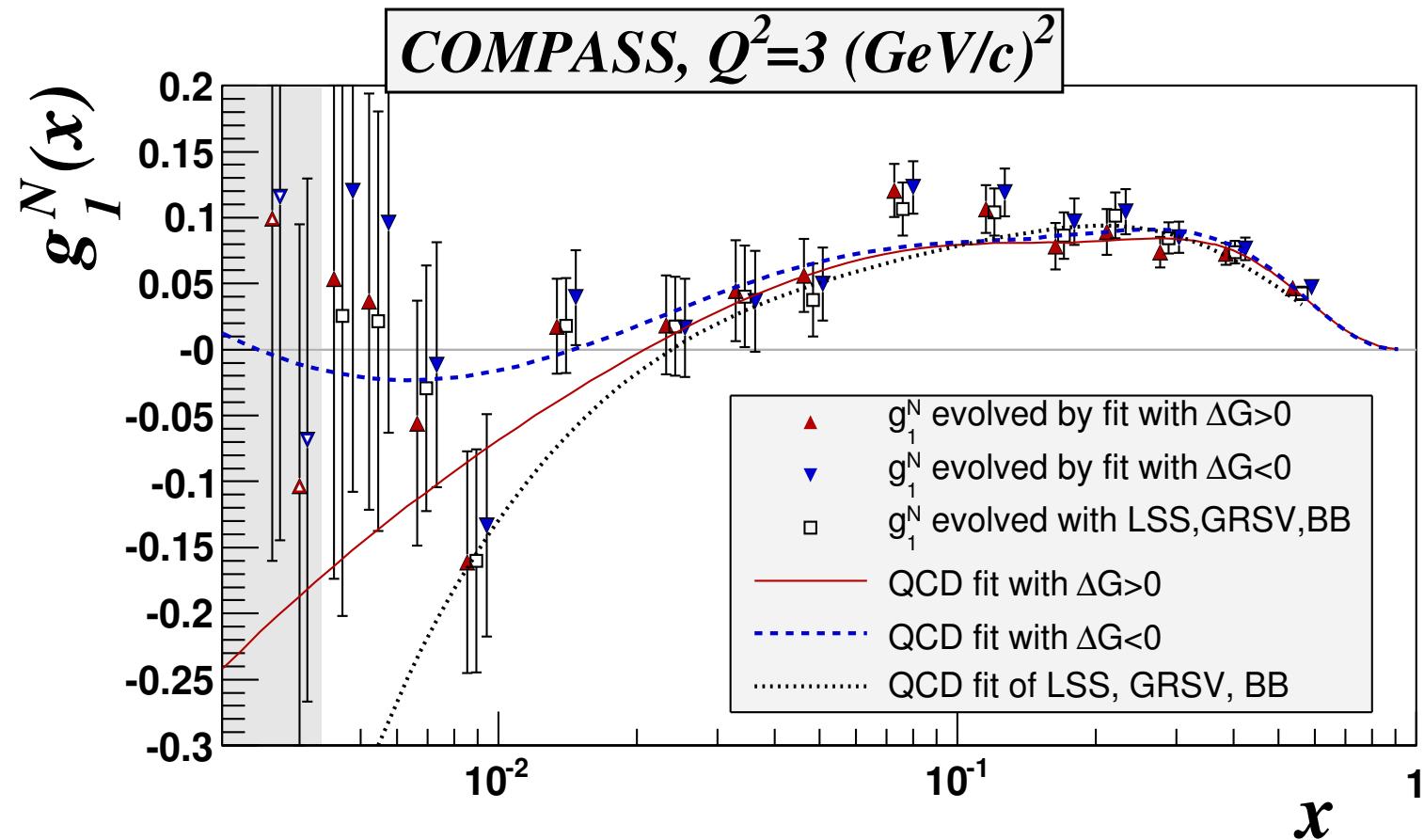
## NLO QCD analysis

- Measured structure functions  $g_1^{p,d,n}$  (different  $x, Q^2$ )

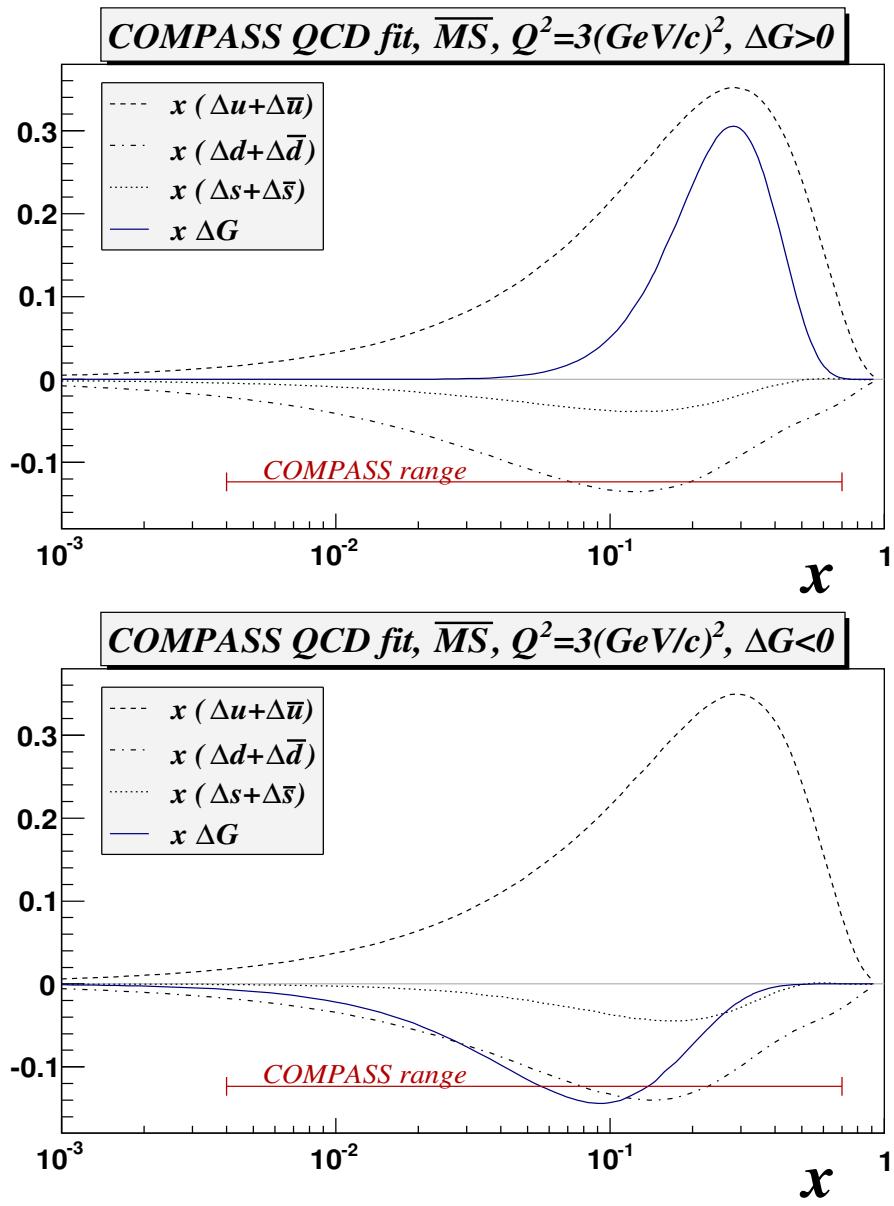
$$g_1(x, Q^2) = \frac{1}{2} \langle e^2 \rangle \left[ C_q^S \otimes \Delta\Sigma + C_q^{NS} \otimes \Delta q^{NS} + 2n_f C_G \otimes \Delta G \right]$$

- Two programs have been used:
  1. Numerical integration in  $(x, Q^2)$  space (Phys.Rev.D58(1998)112002)
  2. Solution of DGLAP in space of moments (Phys.Rev.D70(2004)074032)
- NLO calculation in  $\overline{MS}$  scheme
- Initial parametrization ( $x$ -dependence at fixed  $Q^2$ )
 
$$\Delta\Sigma = \eta \frac{x^\alpha (1-x)^\beta (1+\gamma x)}{\int_0^1 x^\alpha (1-x)^\beta (1+\gamma x) dx}, \quad (\Delta q_3, \Delta q_8, \Delta G) = \eta \frac{x^\alpha (1-x)^\beta}{\int_0^1 x^\alpha (1-x)^\beta dx}$$
- World data fit: 9 experiments, 230 experimental points
- **2 solutions have been found** which describe data equally well and correspond to  $\Delta G > 0$  and  $\Delta G < 0$

## Comparison with published fits ( $Q^2=3 \text{ GeV}^2$ )



- Disagreement of data with previous QCD fits (BB, GRSV, LSS05) at low  $x$
- Updated fits after COMPASS publication: LSS07, DSSV08



- Quark distributions are quite similar for two solutions
- No significant difference between results of two QCD-fit programs and the difference for two solutions ( $\eta_G > 0$  and  $< 0$ ) is also very small

$$\eta_\Sigma = 0.30 \pm 0.01(\text{stat}) \pm 0.02(\text{evol})$$

- Indirect determination the gluon function (via evolution equations)
- Solutions with  $\eta_G > 0$ :  $\eta_G^{\text{prog}\,1} = 0.26^{+0.04}_{-0.06}$ ,  $\eta_G^{\text{prog}\,2} = 0.19^{+0.01}_{-0.10}$
- Solutions with  $\eta_G < 0$ :  $\eta_G^{\text{prog}\,1} = -0.31^{+0.1}_{-0.1}$ ,  $\eta_G^{\text{prog}\,2} = -0.18^{+0.04}_{-0.03}$

$$|\eta_G| \simeq 0.2 - 0.3$$

## Quark polarization with COMPASS data only

- The first moment of  $g_1^d$  at  $Q^2=3\text{ GeV}^2$ :

$$\Gamma_1^N = \int_0^1 g_1^N(x, Q^2) dx = 0.0502 \pm 0.0028(\text{stat}) \pm 0.0020(\text{evol}) \pm 0.0051(\text{syst})$$

- $a_0$  can be extracted from the first moment of  $g_1^N$

$$\Gamma_1^N(Q^2) \Big|_{NLO} = \frac{1}{9} \left( 1 - \frac{\alpha_s(Q^2)}{\pi} + \mathcal{O}(\alpha_s^2) \right) \times \left( a_0(Q^2) + \frac{1}{4} a_8 \right)$$

- From hyperon  $\beta$  decays assuming  $SU(3)_f$ :

$$a_8 = 0.585 \pm 0.025$$

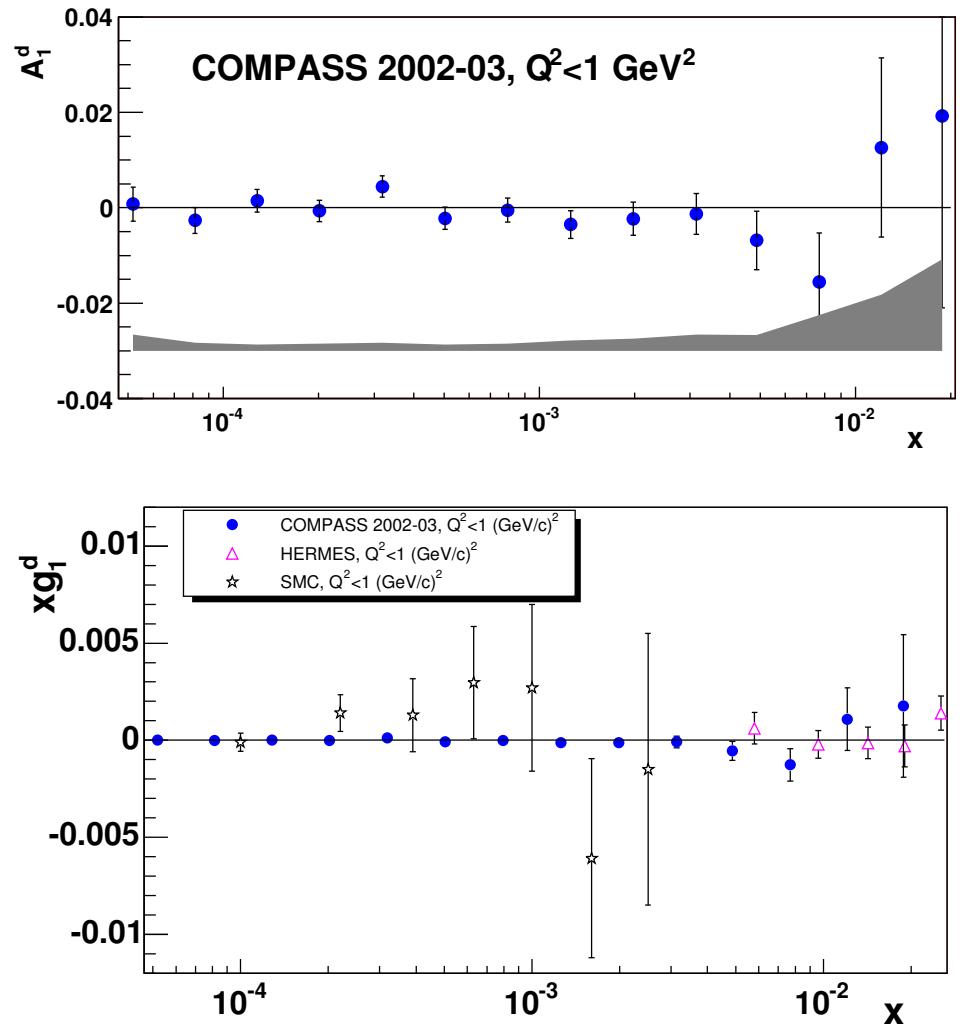
- Contribution to  $\Gamma_1^N$  from unmeasured  $x$ -range is  $\approx 4\%$
- Quark polarization at  $Q^2=3\text{ GeV}^2$ :

$$a_0 = 0.35 \pm 0.03(\text{stat}) \pm 0.05(\text{syst})$$

$$\eta_\Sigma = 0.30 \pm 0.01(\text{stat}) \pm 0.02(\text{evol})$$

## $g_1^d$ at low $x$ and $Q^2 < 1 \text{ GeV}^2$

- Results from 2002-2003
- Statistics:  $300 \cdot 10^6$  events
- Compatible with 0 in the whole  $x$  interval
- Good agreement with results of previous experiments
- Factor 10–20 improvement in statistical precision as compared to SMC
- Parton saturation and non-perturbative models (Regge, VMD)



# Hadron asymmetries

## Hadron asymmetries

Semi-inclusive asymmetries

$$A^{h+} = \frac{\sigma_{\uparrow\downarrow}^{h+} - \sigma_{\uparrow\uparrow}^{h+}}{\sigma_{\uparrow\downarrow}^{h+} + \sigma_{\uparrow\uparrow}^{h+}} \quad A^{h-} = \frac{\sigma_{\uparrow\downarrow}^{h-} - \sigma_{\uparrow\uparrow}^{h-}}{\sigma_{\uparrow\downarrow}^{h-} + \sigma_{\uparrow\uparrow}^{h-}}$$

$$A_1^h(x) = \frac{\sum_q e_q^2 (\Delta q(x) D_q^h + \Delta \bar{q}(x) D_{\bar{q}}^h)}{\sum_q e_q^2 (q(x) D_q^h + \bar{q}(x) D_{\bar{q}}^h)}$$

Difference asymmetry

$$A^{h^+ - h^-} = \frac{(\sigma_{\uparrow\downarrow}^{h+} - \sigma_{\uparrow\downarrow}^{h-}) - (\sigma_{\uparrow\uparrow}^{h+} - \sigma_{\uparrow\uparrow}^{h-})}{(\sigma_{\uparrow\downarrow}^{h+} - \sigma_{\uparrow\downarrow}^{h-}) + (\sigma_{\uparrow\uparrow}^{h+} - \sigma_{\uparrow\uparrow}^{h-})}$$

$$A_d^{\pi^+ - \pi^-}(x) = A_d^{K^+ - K^-}(x) = \frac{\Delta u_v(x) + \Delta d_v(x)}{u_v(x) + d_v(x)}$$

- Some fragmentation functions  $D_q^h = \int D_q^h(z) dz$  are poorly known
- Difference asymmetry originally was proposed in:  
L.Frankfurt *et al.*, Phys. Lett. B230 (1989) 141
- First was used in SMC: B. Adeva *et al.*, Phys. Lett. B369 (1996) 93.
- Meaningful physics results for the deuteron target in LO QCD even without hadron identification

## Single hadron asymmetries $A^{h+}$ and $A^{h-}$

- Deuteron data 2002-2004 are used
- Kinematic cuts (DIS region):

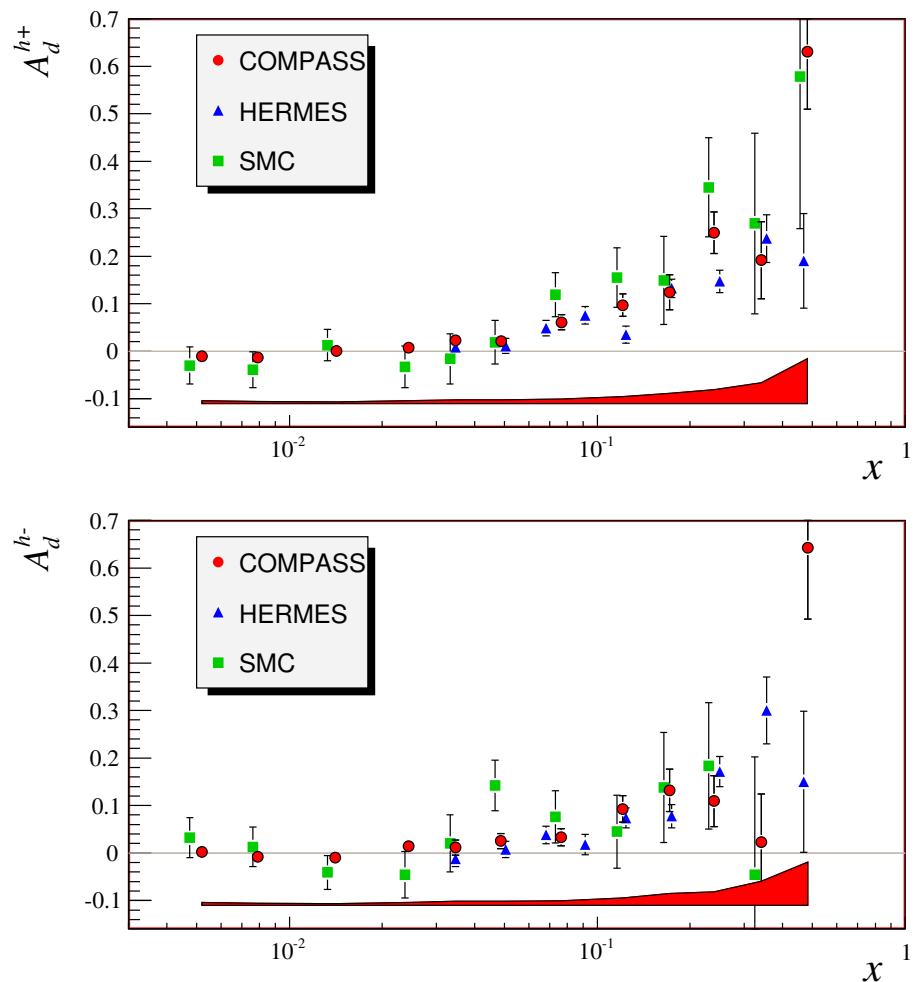
$$Q^2 > 1 \text{ GeV}^2, \quad 0.1 < y < 0.9$$

- No hadron identification
- Current fragmentation region:  $z > 0.2$
- To avoid ambiguity between secondary  $\mu$  and the scattered  $\mu$ , and suppress contribution from diffractive events:

$$z < 0.85$$

- Final statistics:

$$N^+ = 30 \cdot 10^6, \quad N^- = 25 \cdot 10^6, \quad \text{cor}(N^+, N^-) \approx 20\%$$



## Difference asymmetry

- $A^{h+}$  and  $A^{h-}$  are used to obtain  $A^{h^+-h^-}$

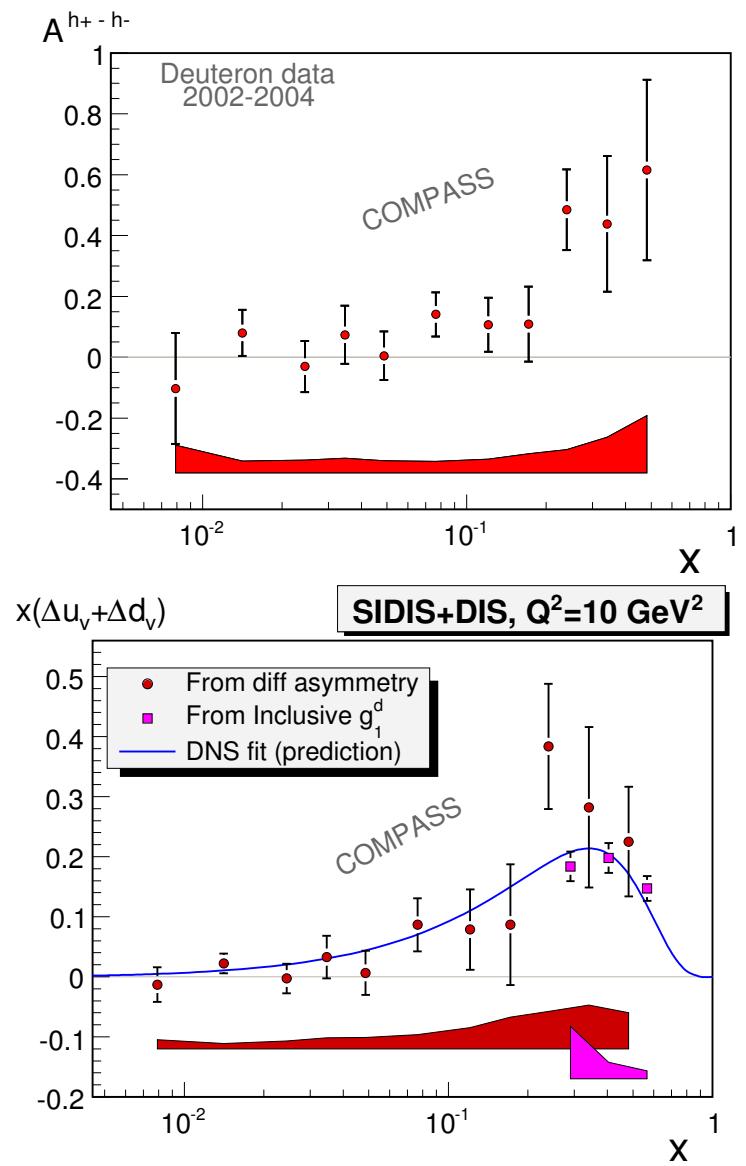
$$A^{h^+-h^-} = \frac{1}{1-r} (A^{h+} - r A^{h-}), \quad r = \frac{\sigma^{h-}}{\sigma^{h+}}.$$

- $r$  is obtained from hadron numbers  $N^\pm$  corrected for their acceptances  $a^\pm$ :

$$r = \frac{\sigma^{h-}}{\sigma^{h+}} = \frac{N^-/a^-}{N^+/a^+}.$$

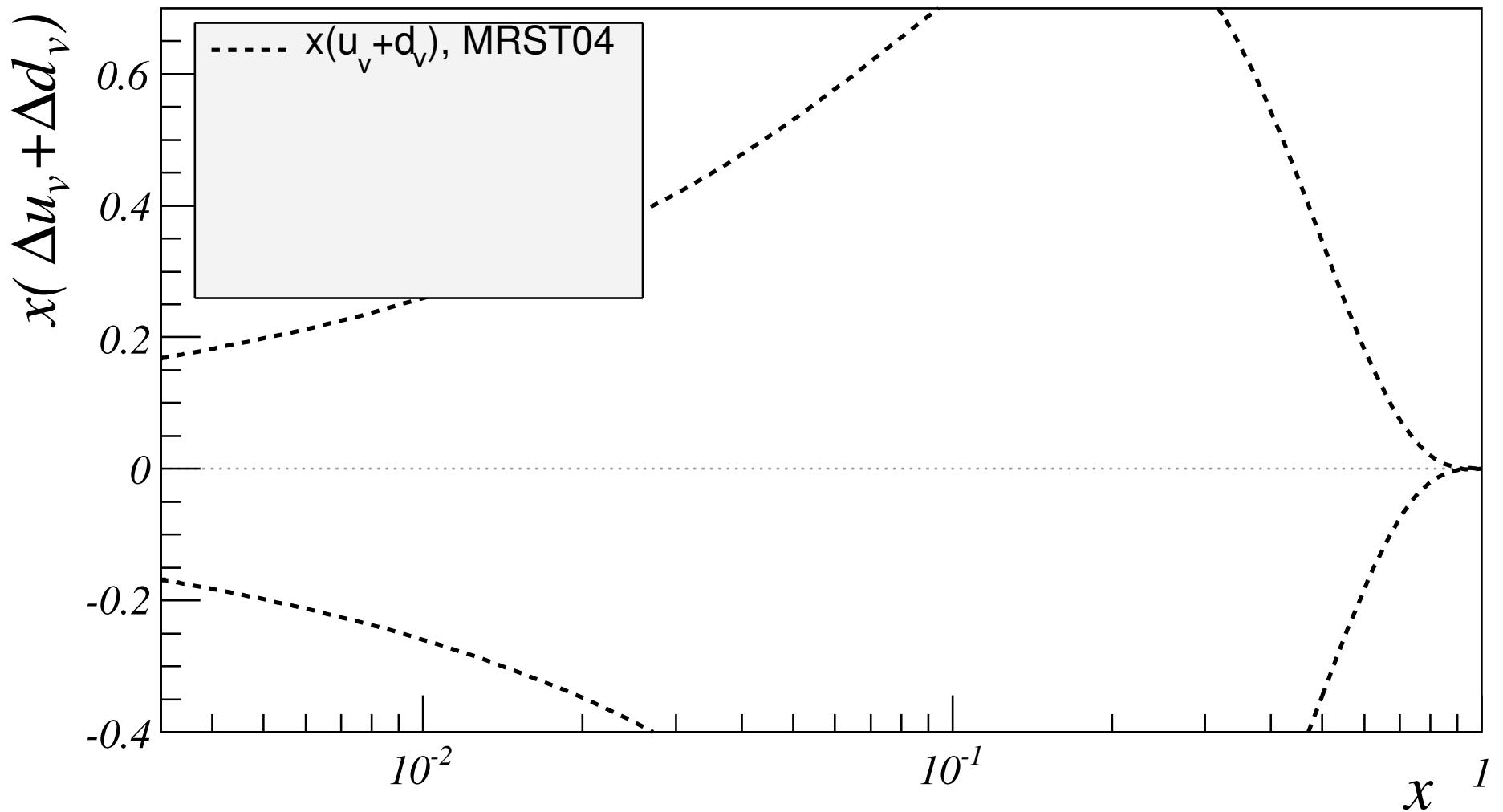
- For unpolarized PDF LO MRST04 was chosen
- Constraint as in SMC & HERMES analyzes:  $\Delta\bar{u} = \Delta\bar{d} = \Delta s = 0$  at  $x > 0.3$

$$\Delta u_v + \Delta d_v \simeq \frac{36}{5} \frac{g_1^d(x, Q^2)}{(1 - 1.5\omega_D)}$$



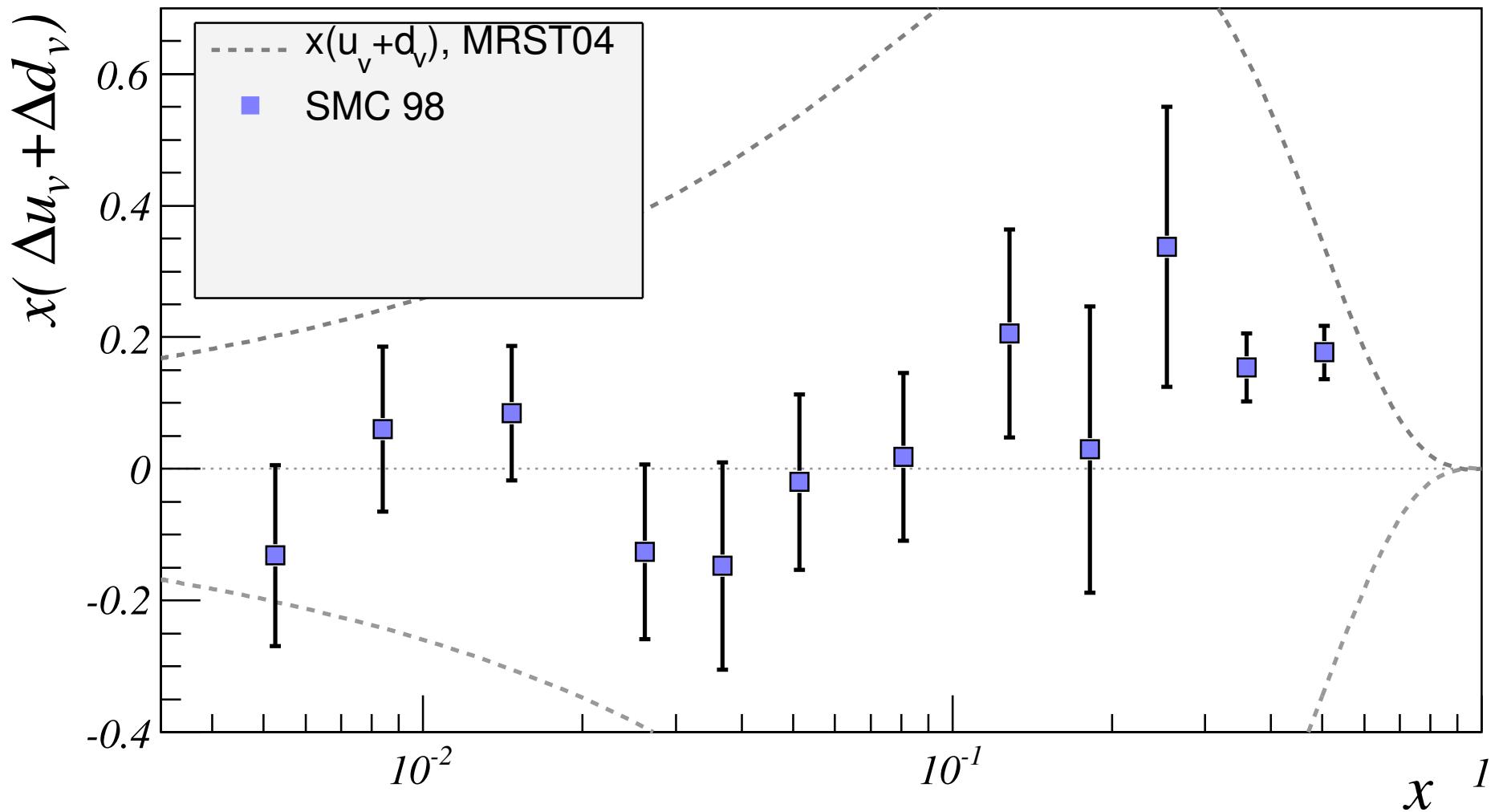
## Comparison with other experiments

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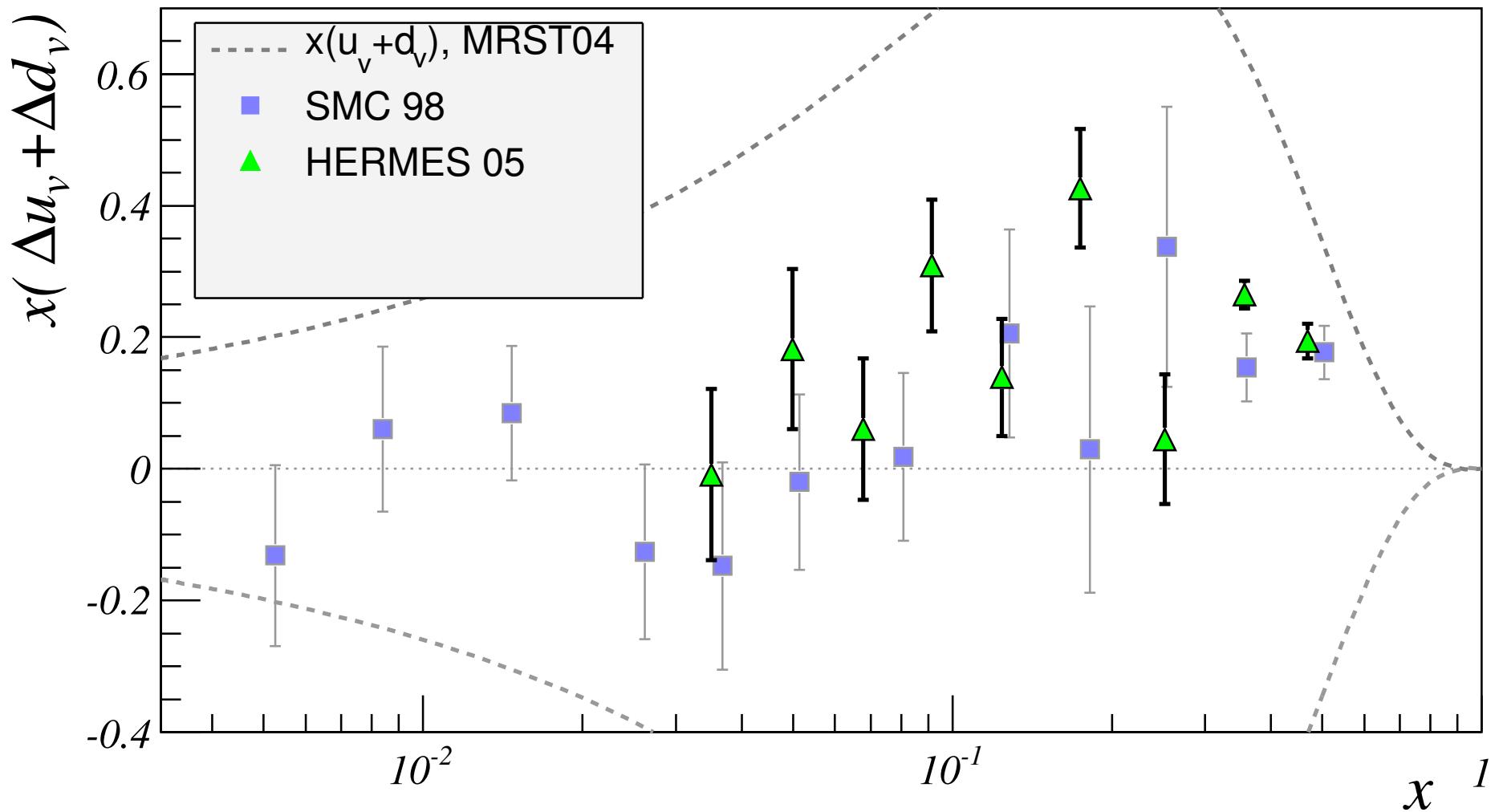


## Comparison with other experiments

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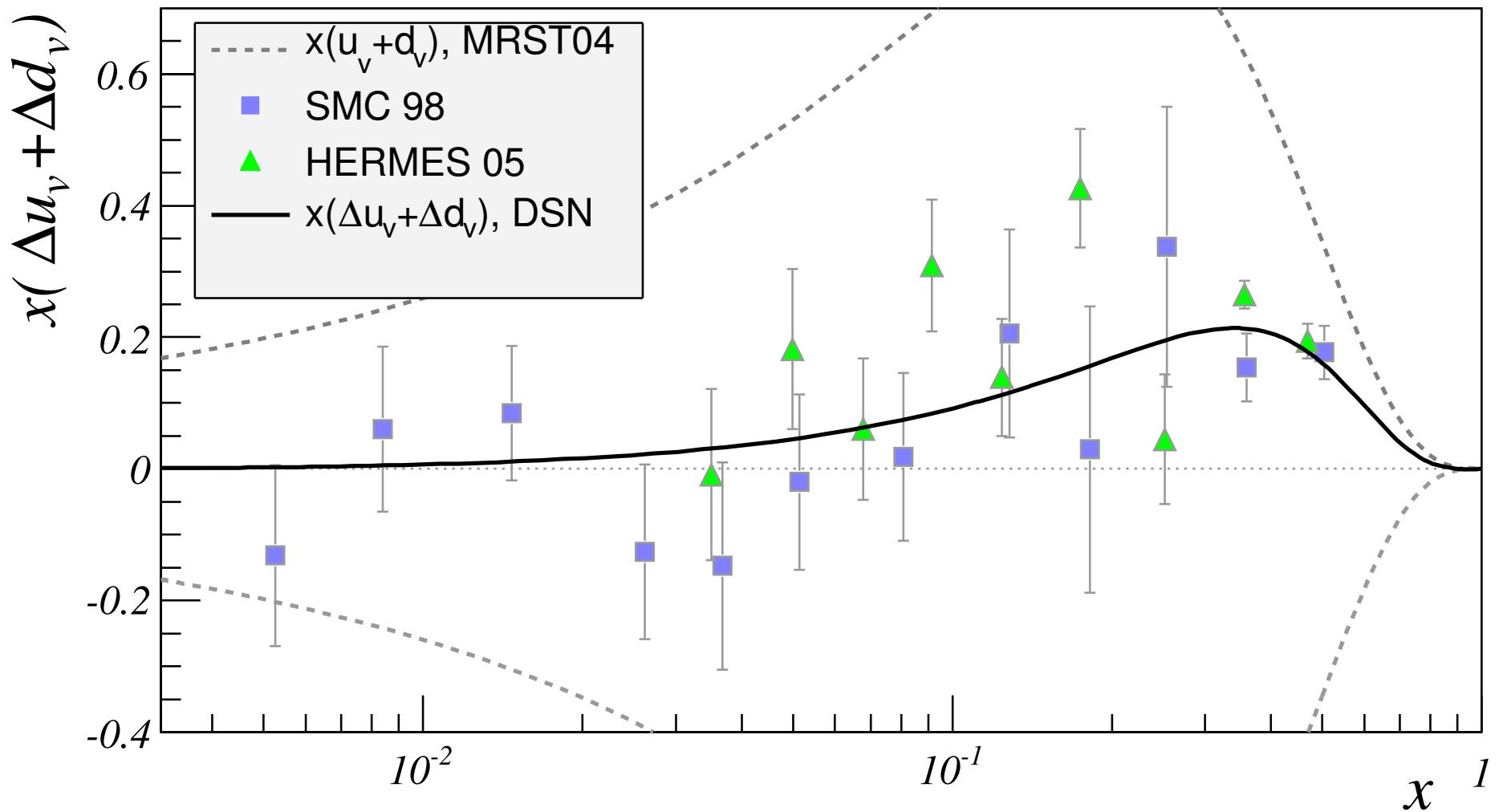


## Comparison with other experiments



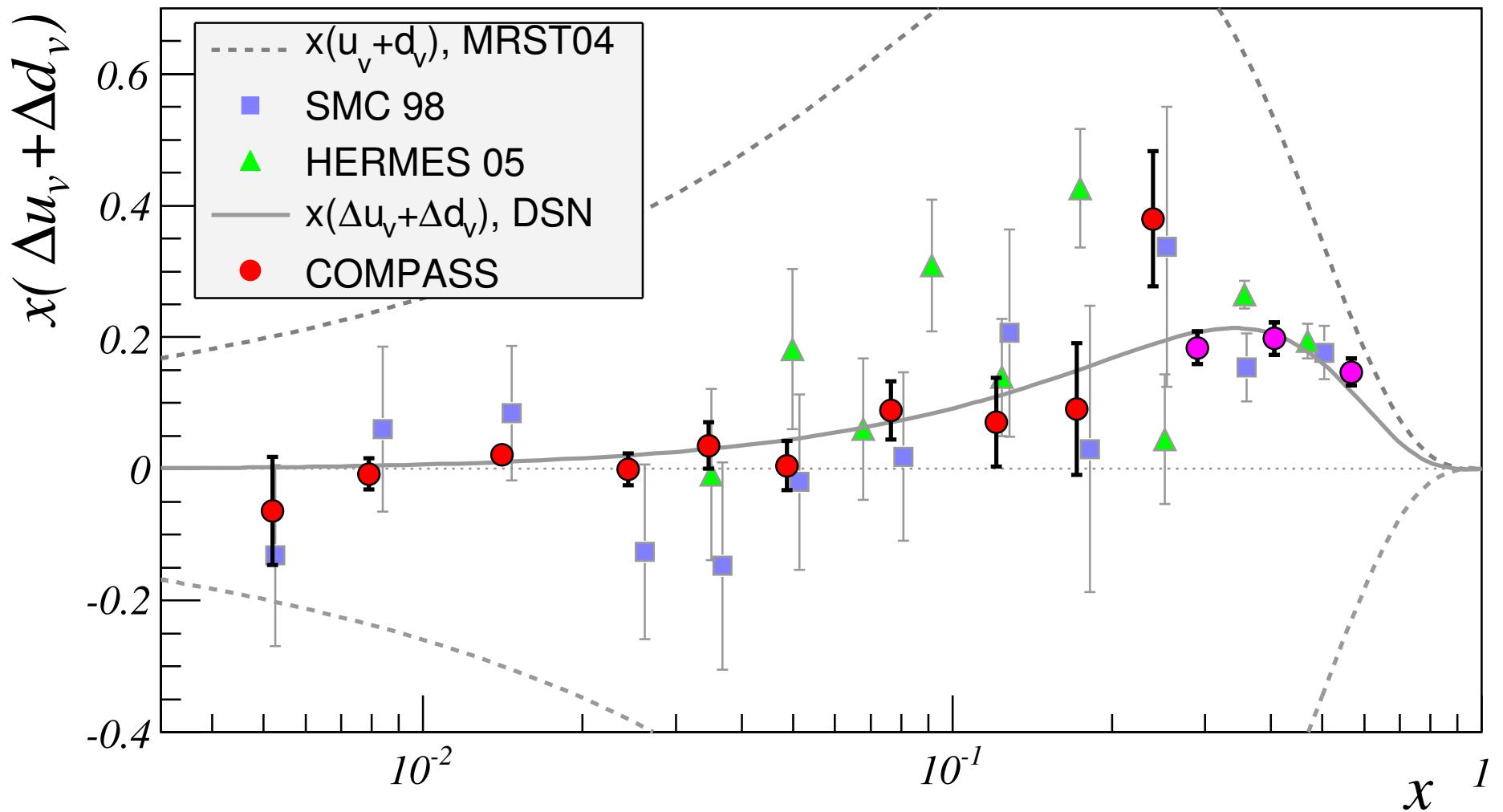
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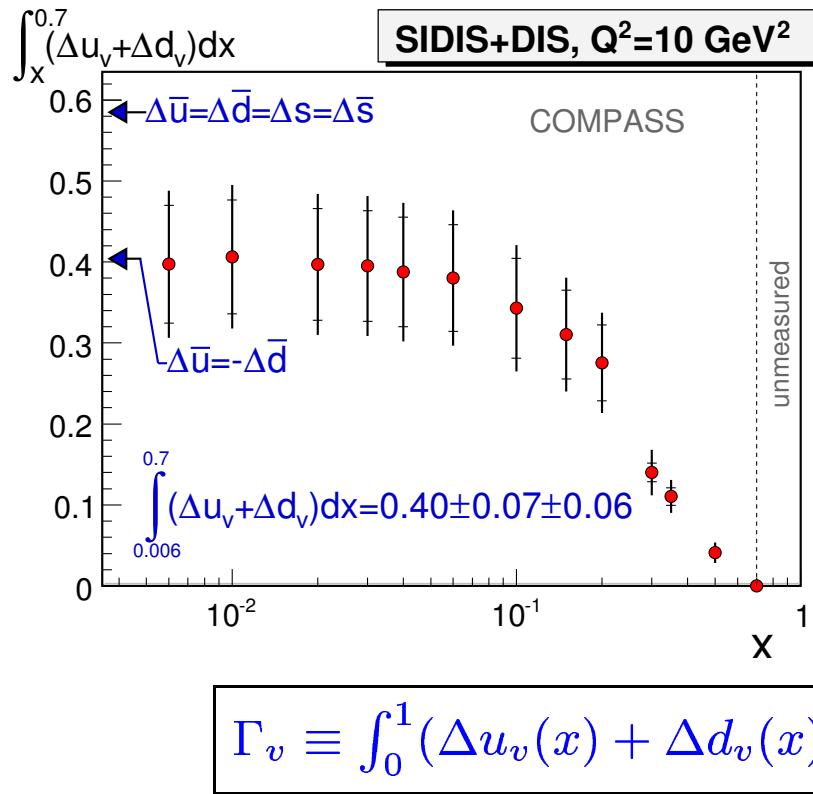


## Comparison with other experiments

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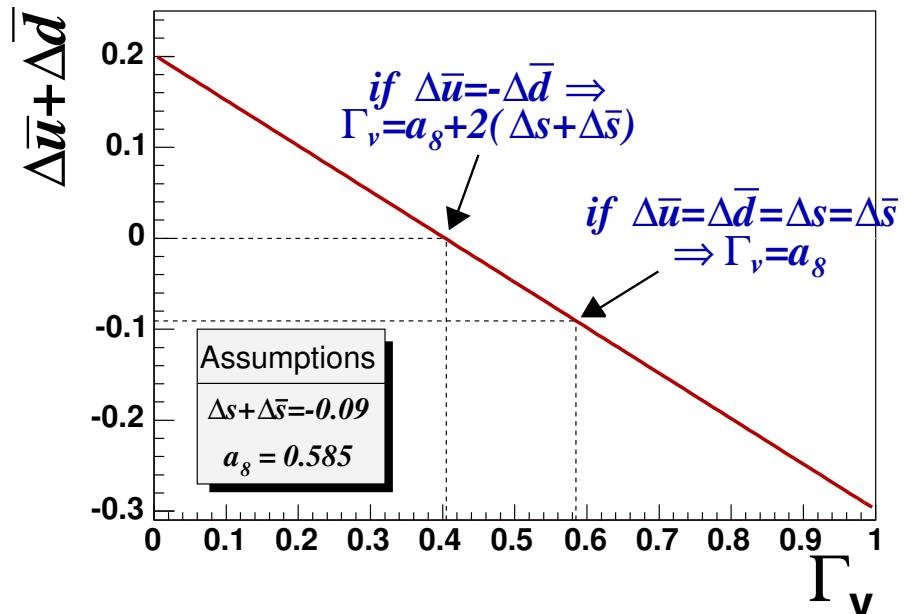


## Estimate for the first moments (LO)



- Contribution from unmeasured high  $x$  region (DNS fit):

$$\int_{0.7}^1 (\Delta u_v + \Delta d_v) dx = 0.004$$



- Combining with axial charge  $a_8$
- $$\begin{aligned} \Delta \bar{u} + \Delta \bar{d} &= (\Delta s + \Delta \bar{s}) + \frac{1}{2}(a_8 - \Gamma_v) \\ &= 0.0 \pm 0.04 \pm 0.03 \end{aligned}$$
- The estimate of  $\Gamma_v$  is  $2\sigma$  away from the flavor symmetric sea scenario

Projection of the stat.

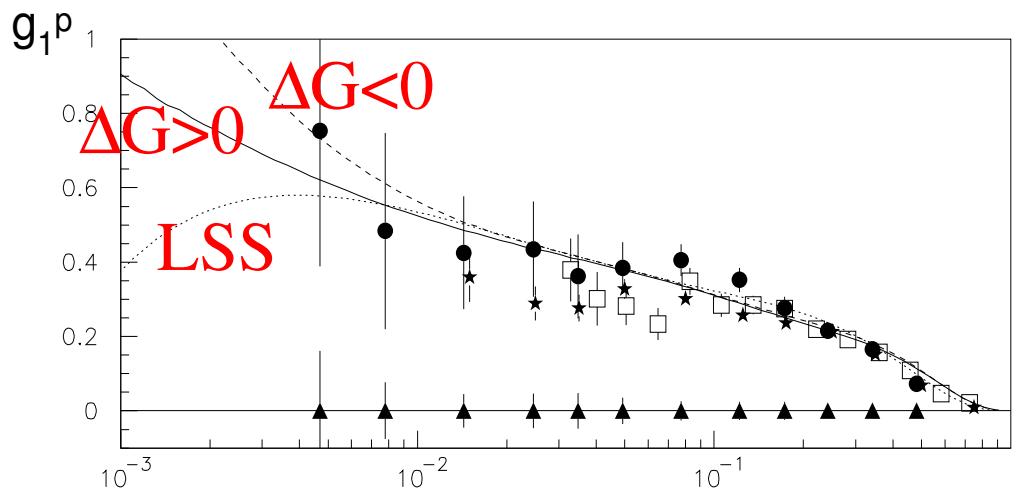
precision for data 2006, 2007

## Upgrade of setup in 2006/2007

- New target magnet
  - ◊ Angular acceptance is increased by a factor 2 (70 mrad → 180 mrad)
  - ◊ 3 cells ⇒ reduction of false asymmetries
- Detectors upgrade (RICH, ECAL, trackers)

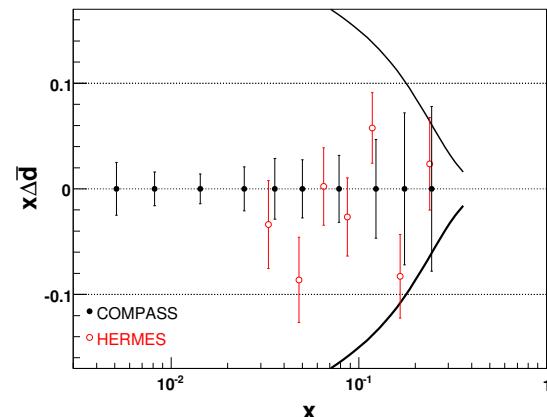
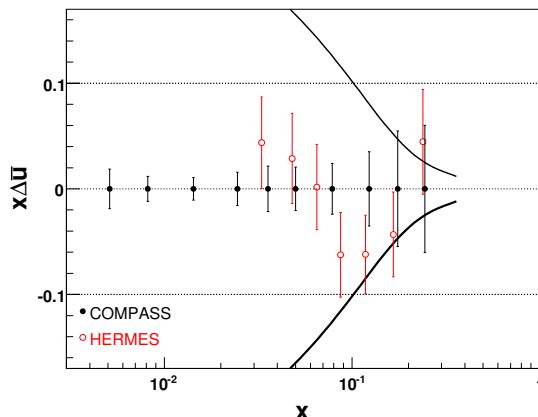
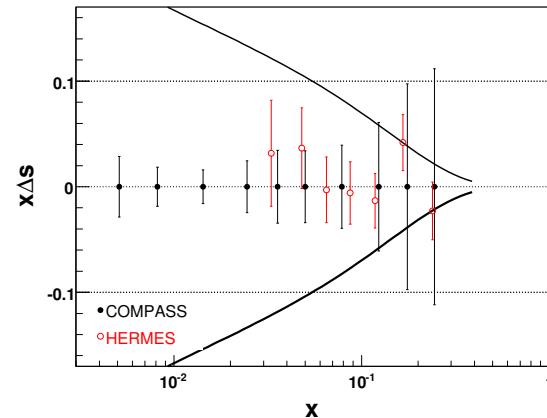
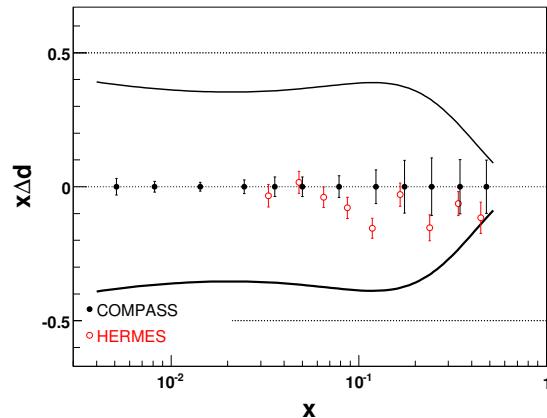
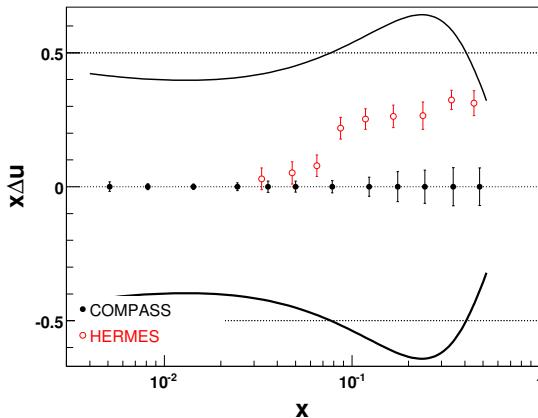
## Analysis

- Deuteron data 2006 ( ${}^6\text{LiD}$  target)
- Proton data 2007 ( $\text{NH}_3$  target)
  - ◊ Crosscheck of low  $x$  points of  $g_1^d$  (so far measured by SMC only)
  - ◊ Full flavor separation



## Flavor separation (prediction for stat. error)

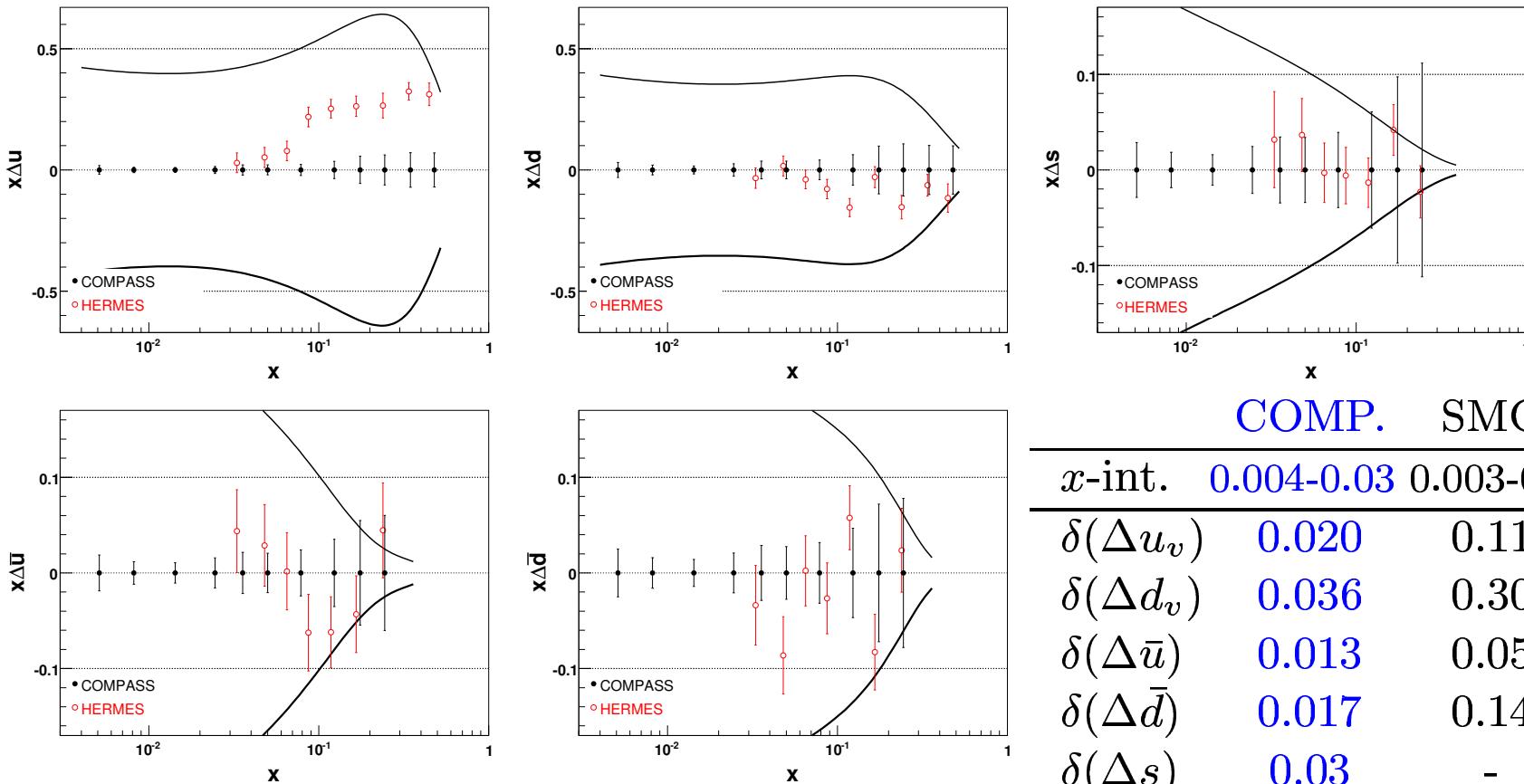
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	COMP.	SMC	HERMES
$x$ -int.	<b>0.004-0.7</b>	0.003-0.7	0.023-0.6
$\delta(\Delta u_v)$	<b>0.07</b>	0.11	0.07
$\delta(\Delta d_v)$	<b>0.11</b>	0.30	0.07
$\delta(\Delta \bar{u})$	<b>0.04</b>	0.05	0.04
$\delta(\Delta \bar{d})$	<b>0.05</b>	0.14	0.03
$\delta(\Delta s)$	<b>0.09</b>	-	0.03

## Flavor separation (prediction for stat. error)

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	COMP.	SMC	HERMES
<i>x</i> -int.	<b>0.004-0.03</b>	0.003-0.7	0.023-0.6
$\delta(\Delta u_v)$	<b>0.020</b>	0.11	0.07
$\delta(\Delta d_v)$	<b>0.036</b>	0.30	0.07
$\delta(\Delta \bar{u})$	<b>0.013</b>	0.05	0.04
$\delta(\Delta \bar{d})$	<b>0.017</b>	0.14	0.03
$\delta(\Delta s)$	<b>0.03</b>	-	0.03

## Summary and Outlook

- Analysis of deuteron data 2002 – 2004 have been presented
  - ◊ Inclusive asymmetry  $A_1^d$  and structure function  $g_1^d$
  - ◊ Valence quark distributions  $\Delta u_v + \Delta d_v$  from hadron asymmetry  $A_d^{h^+ - h^-}$
  - ◊ Strong increase in the precision at low  $x$  as compared to SMC results
- Data of 2006 have been processed  $\Rightarrow$  update on  $A_1^d$ ,  $A_d^{h^\pm}$  soon
- Hadron asymmetries  $A_d^{\pi^\pm}$ ,  $A_d^{K^\pm}$  are coming
- Processing of 2007 data (longitudinal polarization) is in progress