

# COMPASS results on the spin

## structure function $g_1^d$

*On behalf of the COMPASS collaboration*

**Dubna-Spin05**

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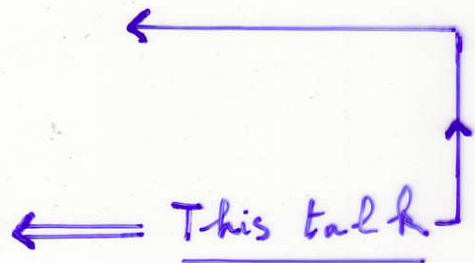
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# COMPASS at CERN

- Approved 1997
- Data taking started in 2002
- One of the few fixed target exp. running at CERN
- Extended muon and hadron program

## Spin physics with $\mu$ beam and polarised target

- Transverse  $P_T$
- Longitudinal  $P_T$ 
  - Main topic:  $\Delta G$
  - Exclusive channels
  - Semi-inclusive channels
  - Inclusive  $\mu$  interactions:  $A_1^d, g_1^d$



## Reference:

COMPASS, E.S. Ageev et al., Phys. Lett. B 612 (2005) 154-164

- Experimental layout
- DIS data
- Extraction of  $A_1^d$ , systematic errors
- $A_1^d$  at low  $x$ , COMPASS vs. SMC
- $g_1^d$  from COMPASS
- QCD analysis of world  $g_1$  data

# The COMPASS spectrometer

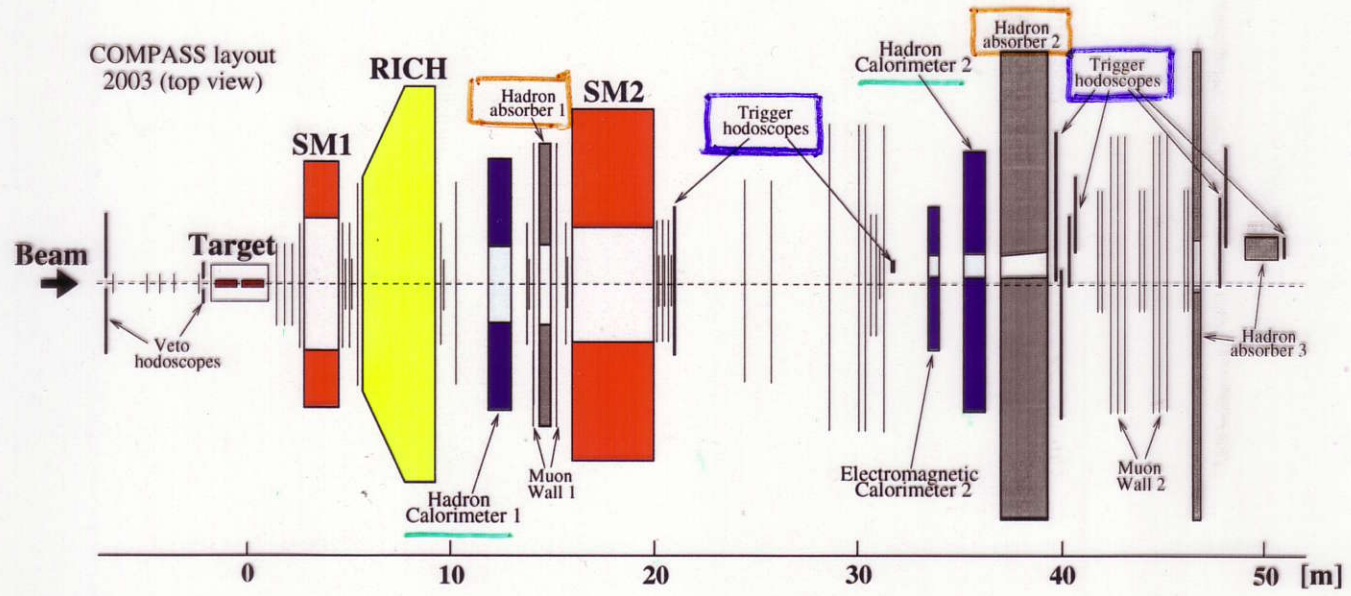


Figure 1: The COMPASS spectrometer.

Beam:  $\mu^+$   $E = 160 \text{ GeV}$   $\langle P_L \rangle = -0.70$

$I = 2 \cdot 10^8 \mu / \text{spill}$  (4 spills/min.)

Polarised target:  ${}^6\text{LiD}$   $|P_T| \approx 0.50$

2 cells:  $l = 60 \text{ cm}$   $\Phi = 3 \text{ cm}$

Spectrometer: 2 stages

2 dipole magnets: SM1  $\left\{ \begin{array}{l} \int B \cdot dl = 1 \text{ Tm} \\ P > 0.4 \text{ GeV}/c \end{array} \right.$

SM2  $\left\{ \begin{array}{l} \int B \cdot dl = 4.4 \text{ Tm} \\ P > 4 \text{ GeV}/c \end{array} \right.$

$\mu\text{ID}$ : 2 hadron absorbers

Hadron detection: 2 calorimeters

Large variety of trackers (adapted to part. route)



# The COMPASS trigger system

## \* 3 types of triggers:

- Inclusive triggers: direction of scattered  $\mu$  behind SM2  
(from coincidence signals in hodoscopes)

- Semi-inclusive triggers:

$\mu$  energy loss (from trigger hodoscopes)

+

hadron signal in HCAL

- Calorimeter trigger: (Not <sup>installed</sup> used in 2002)

Hadron signal in calorimeter

(No condition on scattered  $\mu$ )

## \* Software requirements:

- in all cases: beam  $\mu$  + scattered  $\mu$  +  
interaction point inside target cells

- for semi-incl. and calor<sup>imeter</sup> triggers:

in addition, at least one hadron at  
interaction point

\*\* Setup mainly for quasi-real photon interactions

Only a small fraction of triggers for DIS

DIS data

2002 + 2003

$$Q^2 > 1 \text{ GeV}^2$$

$$0.1 < y < 0.9$$

$$140 < P_{\mu} < 180 \text{ GeV}/c$$

34.  $10^6$  events

(2/3 from 2003)

2004 data

Not analysed yet for DIS events

Expect  $\approx$  same statistics as (2002 + 2003)

# Fraction of various trigger types

in DIS sample vs.  $x$  and  $Q^2$

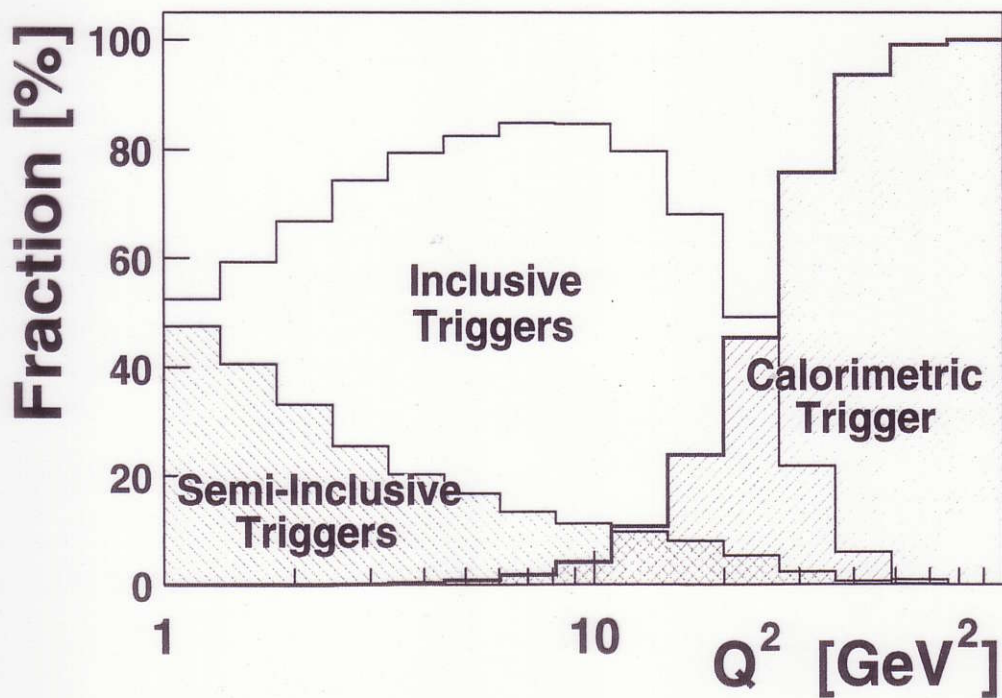
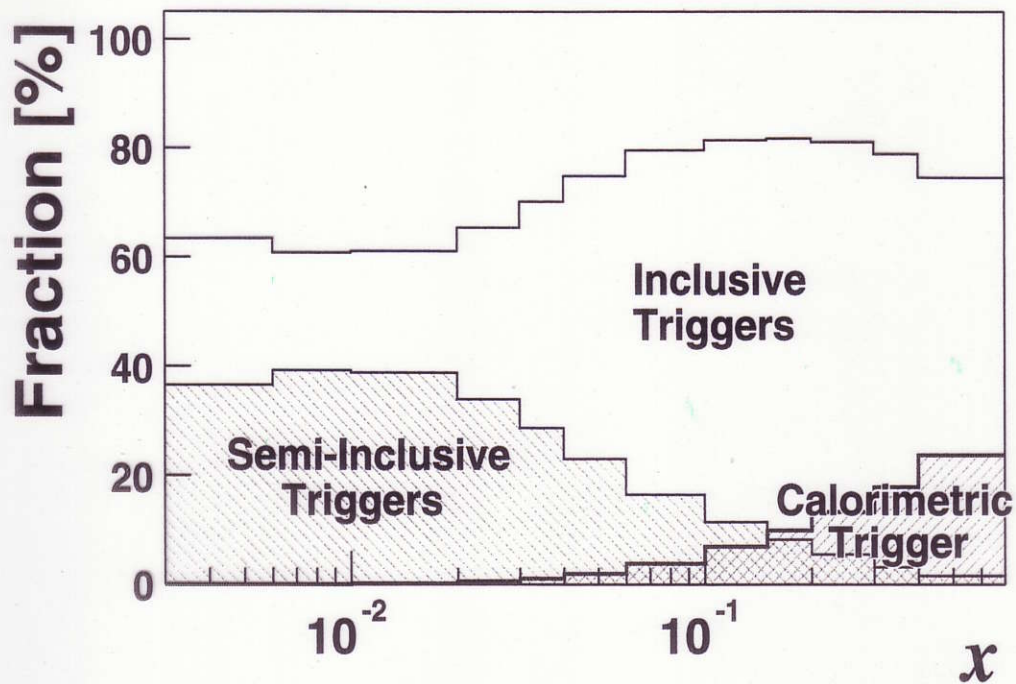


Figure 1: Fraction of inclusive, semi-inclusive and calorimetric triggers in the final data sample (2002–2003) as a function of  $x$  and  $Q^2$ . Events are counted with the weight they carry in the asymmetry calculation.



# Asymmetries and spin-structure function

## \* Cross-section asymmetry

$$A^d = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}}$$

## \* Longitudinal $\gamma^*$ -electron asymmetry

$$A_1^d = \frac{\sigma_0^T - \sigma_2^T}{2\sigma^T}$$

$\sigma_J^T = \begin{cases} \text{transverse cross-section} \\ \text{total spin proj}^n \text{ on } \hat{y} \cdot \hat{w}^n = J \end{cases}$

with  $\sigma^T = \frac{1}{3} (\sigma_0^T + \sigma_1^T + \sigma_2^T)$

## \* $A_1^d$ vs. $A^d$

$$A^d = D (A_1^d + \eta A_2^d)$$

$\eta, D \rightarrow$  event kinematics  
(+  $R = \sigma_L / \sigma_T$  for  $D$ )

Compare kinematics:  $\eta, A_2^d$  small

$\Rightarrow$

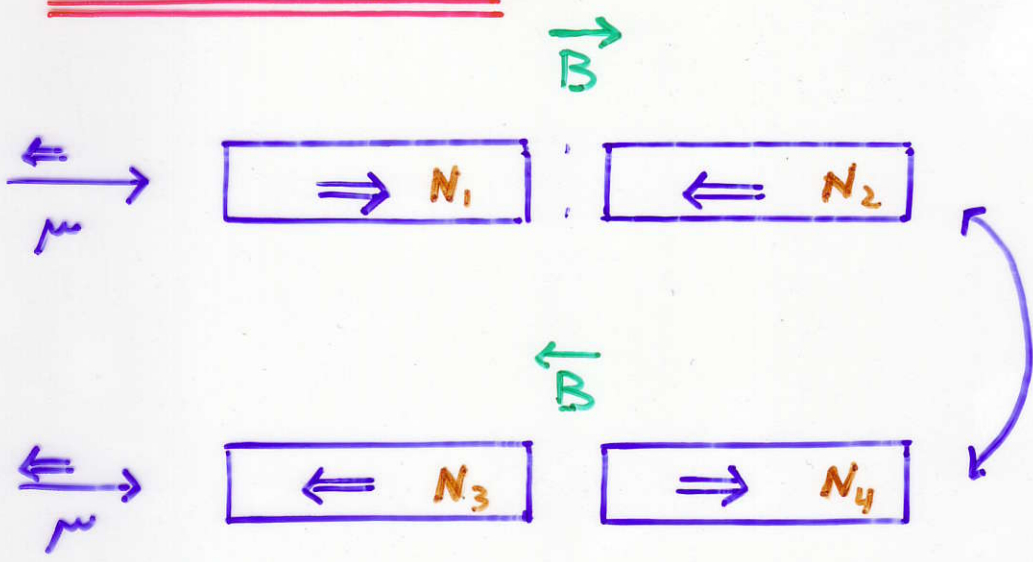
$$A_1^d \approx A^d / D$$

$$g_1^d = \frac{F_2^d}{2x(1+R)} A_1^d$$

$A_1^d$  derived separately for nucl./hadronic events  
 $\Rightarrow$  compared and merged



# Evaluation of $A_1^d$



Spin reversal  
by field rotation

$$N_i = a_i \varphi_i n_i \bar{\sigma} (1 + P_B P_T f D A_1^d)$$

- $a_i$  = acceptance
- $\varphi_i$  = neutron flux
- $n_i$  = Nr. target nucleons/surf.
- $f$  = target dilution factor

\* Same flux for the 2 cells:  $\varphi_1 = \varphi_2$  and  $\varphi_3 = \varphi_4$

$$\frac{N_1 N_4}{N_2 N_3} = 2^{ol} \text{-order eq. in } A_1^{ol}$$

System. error  
↓

Acceptances cancel out if  $(a_1/a_2) = (a_3/a_4)$

\* Statistical error minimized by using weighted events:

$$N_i \rightarrow \sum_i w_i \quad \text{with} \quad w = f P_B D$$

The polarised target dilution factor



Naive expectation  $f({}^6\text{LiD}) \approx 0.5$

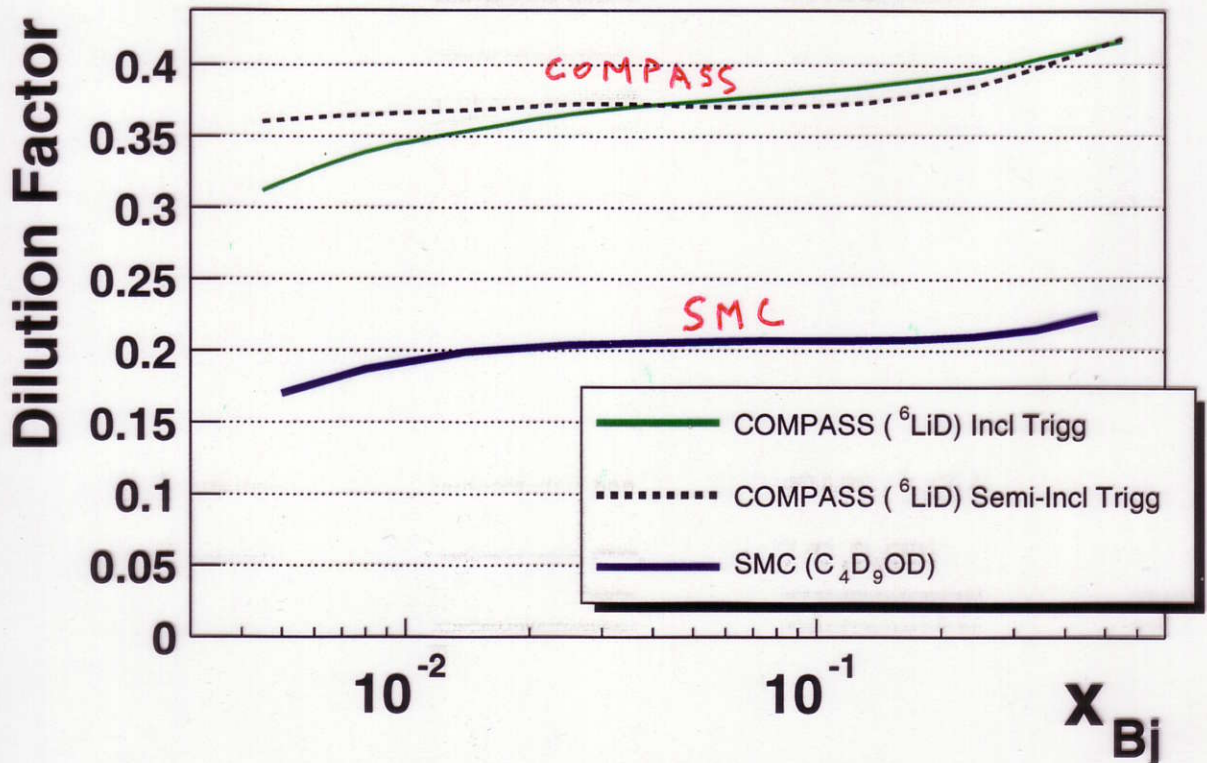


Figure 1: The dilution factor (including radiative effects on the deuteron) as a function of  $x$ .

- \* Ratio of  $\sigma$ 's on nucleons bound in nuclei
- \* correction for polarisation of D bound in  ${}^6\text{Li}$
- \* correction for radiative effects in deuteron

$$A_1 = \frac{\Delta\sigma^{(1\gamma)}}{\bar{\sigma}^{(1\gamma)}} = \underbrace{\frac{\Delta\sigma^{(t,t)}}{\bar{\sigma}^{(t,t)}} \left( \frac{\bar{\sigma}^{(1\gamma)}}{\bar{\sigma}^{(t,t)}} \right)}_{\text{Unpol. RC}} + \underbrace{\frac{\Delta\sigma^{(1\gamma)} - \Delta\sigma^{(t,t)}}{\bar{\sigma}^{(1\gamma)}}}_{\text{Pol. RC}}$$

} included in  $f$   
} different incl./semi-incl.

2



# Systematic errors on $A_1^d, g_1^d$

1-  $A_1$  from incl./semi-incl. triggers  $\rightarrow$  No effect

Also tested by MC  $\Rightarrow$   $\left\{ \begin{array}{l} \text{deuteron target} \\ \text{OK within exp. conditions} \end{array} \right.$

## 2- External sources:

- $\left\{ \begin{array}{l} P_B, P_T \rightarrow 6.5\% \text{ scale error} \\ f \rightarrow 6\% \\ R \rightarrow 4-5\% \\ F_2^d \rightarrow (\text{in } g_1^d) \\ \vdots (A_2, R.C. (Pol.)) \rightarrow \text{smaller effects} \end{array} \right.$

## 3- False asymmetries due to time variation of $(a_{u,d})$

- Divide data into 100 subsamples taken within  $\sim 16$  hours

$$\frac{\times 2}{200}$$

- Distributions of  $(A_i - \bar{A})/\sigma_i$   $\Rightarrow$   $N(0, 1)$   
in every x bin

$$\sigma(\bar{A}) = \frac{1}{\sqrt{400}} = 0.05$$

$\Rightarrow$  No indication for broadening due to time dependent effects

$$\sqrt{\sigma_{stat}^2 + \sigma_{syst}^2} \leq 1.10 \sigma_{stat}$$

$\Downarrow$

 $\sigma_{syst.} < 0.5 \sigma_{stat.}$   
(conservative limit)



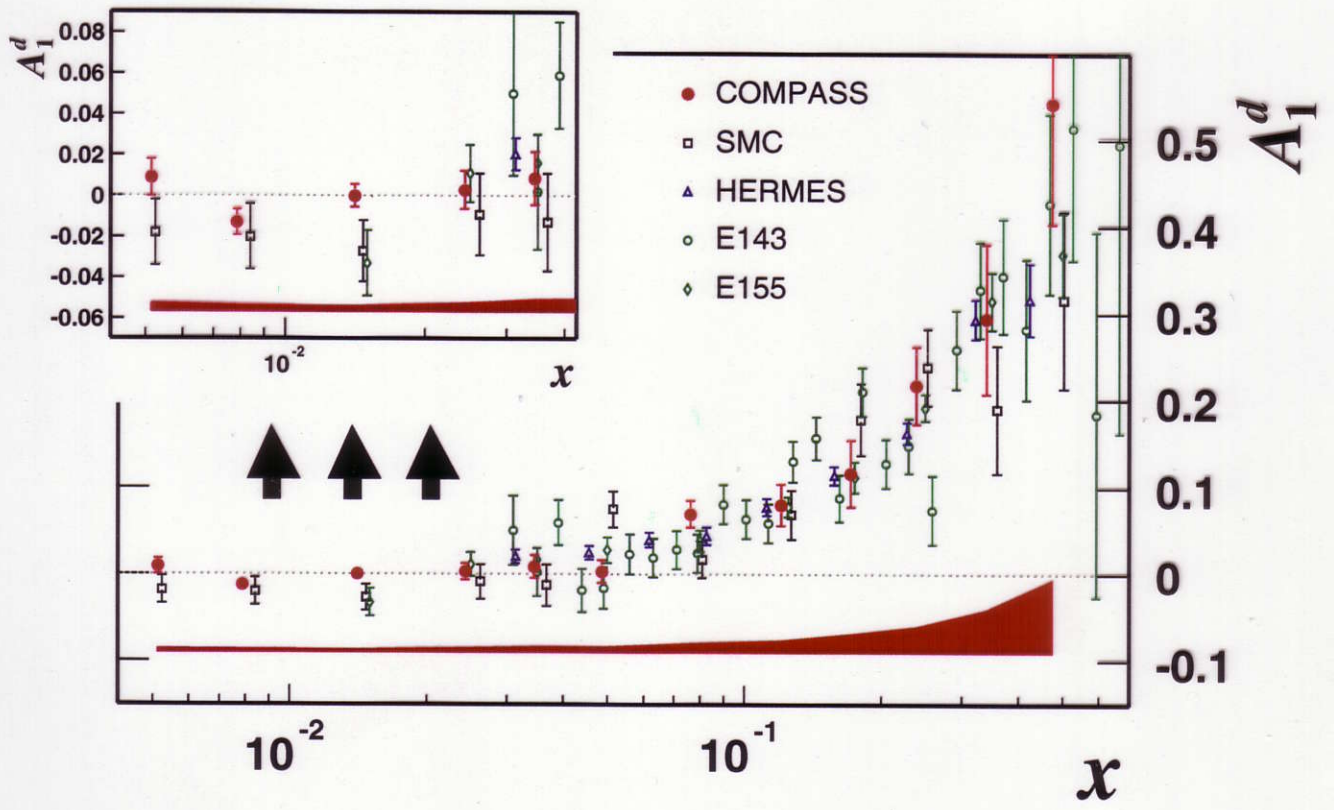


Figure 1: The asymmetry  $A_1^d(x)$  as measured in COMPASS and previous results from SMC, HERMES, SLAC E143 and E155 at  $Q^2 > 1 \text{ GeV}^2$ .

$A_1^d(x, Q^2)$  almost independent of  $Q^2$

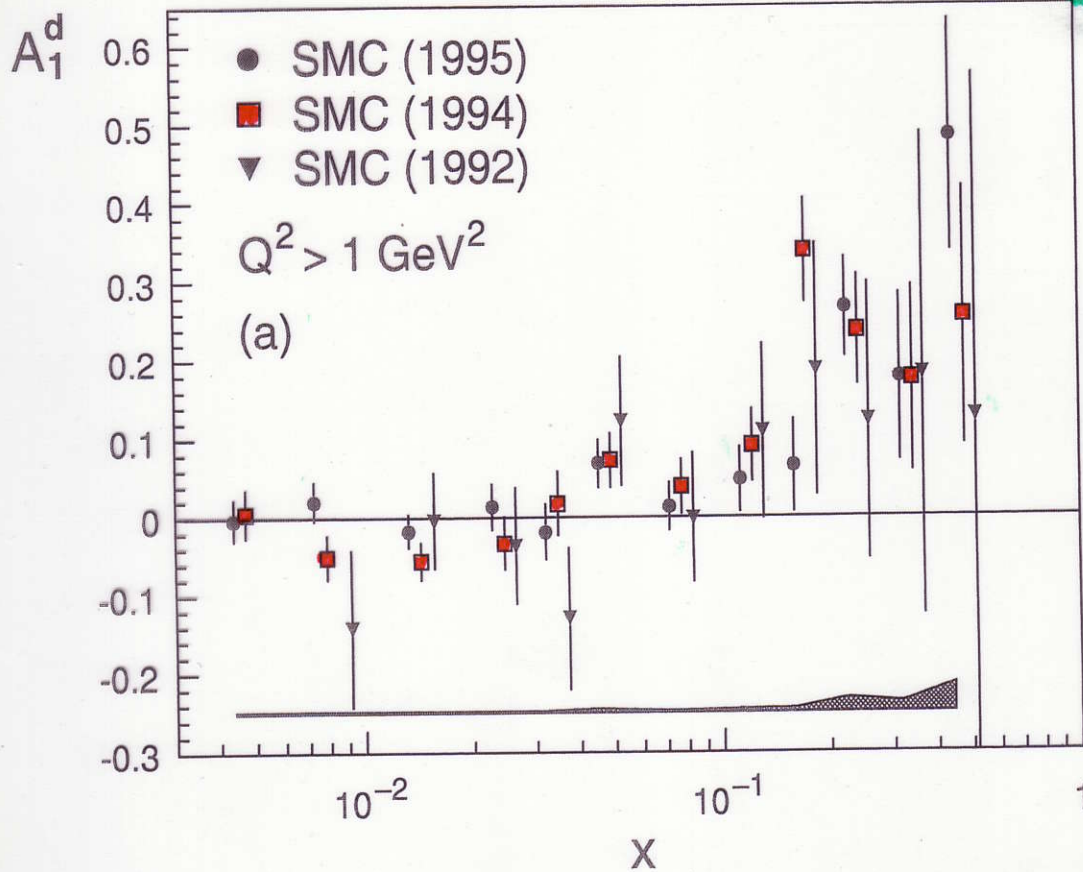


Data at same  $x \approx$  equal for all experiments

# $A_1^d$ at low $x$ - Historical aspects

$(x < 0.04)$

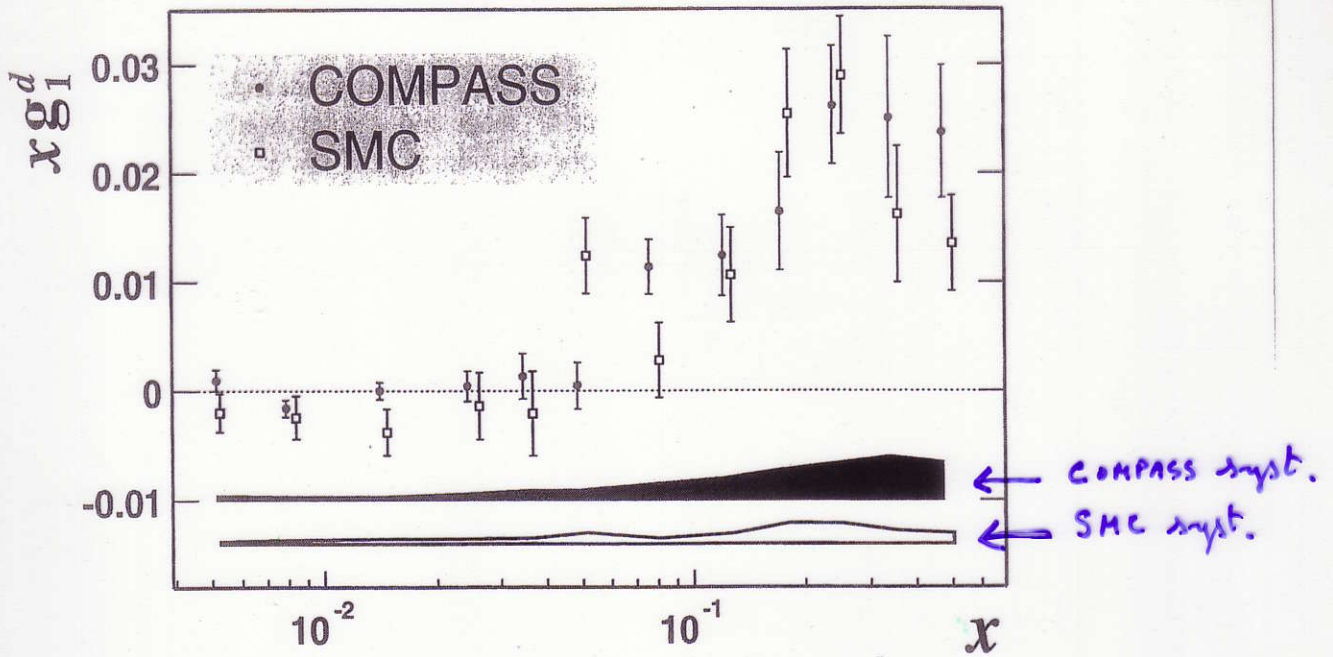
Ph. Lett. B 398 (1997) 338



<u>SMC</u>	1992	2 points $< 0$	Large errors, $E = 100 \text{ GeV}$	
	1994	3 points $< 0$		$2.5 \sigma$
	1995 This plot	→ { Reanalysed 94 data New data - Combined		$\sim 2.5 \sigma$
				No effect } Merged
	1998	Final analysis		$\sim 1.5 \sigma$ ←
		$\sim 2 \sigma$ ( <u>Not discussed</u> ) $A_1^d < 0$		
<u>Compass</u>	2002-2003	This analysis	No effect	



COMPASS vs. SMC (at  $Q^2$  of COMPASS points)



\*  $\sigma_{stat.} (COMPASS) \lesssim \sigma_{stat.} (SMC) / 2$  for  $x < 0.06$

Precision improved at low x

\* For  $x \geq 0.2$   $\sigma_{stat.} (COMPASS) > \sigma_{stat.} (SMC)$

(due to incomplete trigger system in 2002)

$\Gamma_1^d (?)$

SMC :  $\int_{0.003}^{0.7} g_1^d(x, Q_0^2) dx \rightarrow \sigma_{stat.} = 0.006$

COMPASS : (0.4  $\rightarrow$  0.7)  $\rightarrow \sigma \approx 0.004$   
 (last bin)

SUM RULES  $\Rightarrow$  Needs 2004 data



# QCD fits of world data of $f_1^{p,d,u}$

(with and without COMPASS data)

\* Data sets: all  $g_1$  data at  $Q^2 > 1 \text{ GeV}^2$

SLAC: E142 - E143 - E154 - E155

DESY: HERMES

JLAB: Hall A

CERN: EMC - SMC - COMPASS

} 200 data points

\* Fitting program:

(SMC program) } NLO fit  $\overline{\text{MS}}$  scheme  
( $x, Q^2$ ) space

\* PDF's parametrisations: at  $Q_0^2 = 3 \text{ GeV}^2$

$$\left\{ \begin{aligned} \Delta \Sigma &= \eta_\Sigma N_\Sigma^{-1}(\alpha, \beta, \gamma) x^\alpha (1-x)^\beta (1+\gamma x) \\ \Delta q &= \eta_q N_q^{-1}(\alpha, \beta) x^\alpha (1-x)^\beta \\ \Delta q_{3,8} &= \underbrace{K_{3,8}}_{\text{fixed (F,D)}} N_{3,8}^{-1} x^\alpha (1-x)^\beta \end{aligned} \right.$$

Nr. parameters:  $4 + 3 + 2 + 2 = 11$   
(+1 floating normalisation for one data set)

\* Require  $|\Delta \rightarrow(x, Q_0^2)| \leq \rightarrow(x, Q_0^2)$  Positivity limit  
 $\uparrow \frac{1}{3} (\Delta \Sigma - \Delta q_8)$

$x \cdot g_1^d(x)$  COMPASS - SMC data vs. fit

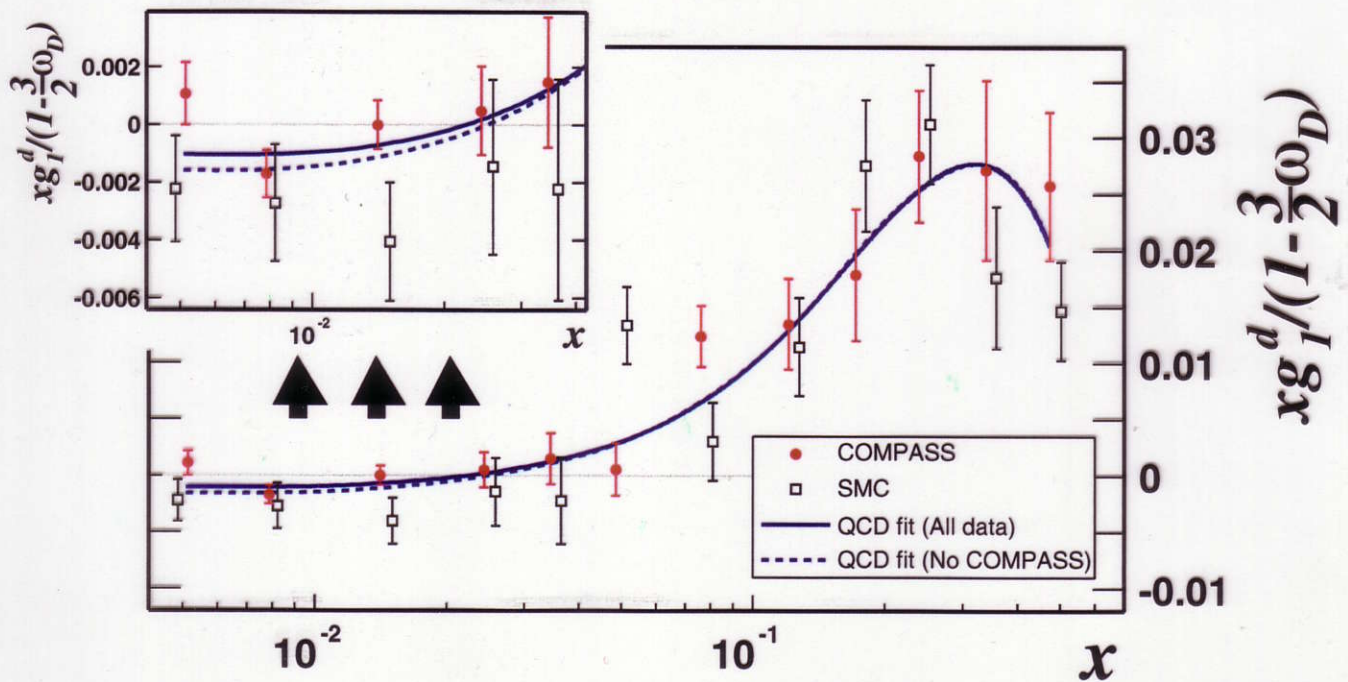


Figure 1: Values of  $x \cdot g_1^d(x)$  measured by COMPASS and SMC with the result of fits to world data. The data points are corrected for the deuteron D-wave probability.

$$\int_{0.004}^{0.03} g_1^d(x) dx = \begin{cases} (-0.3 \pm 1.0) \cdot 10^{-3} & \text{COMPASS} \\ (-5.3 \pm 2.3) \cdot 10^{-3} & \text{SMC} \end{cases}$$

Diff.  $\implies$   $0.0050 \pm 0.0025$

$g_1^d \stackrel{\text{QPM}}{\approx} \frac{1}{9} (\Delta \Sigma + \frac{1}{4} \Delta g_8)$

$\int \Delta g_8$  fixed

$\implies$  Expect change in  $\Delta \Sigma$  w/ w/o COMPASS ( $\approx 0.045$ )



Fit results ( $Q^2 = 3 \text{ GeV}^2$ )

①

\*  $\Delta \Sigma (\overline{MS}) = 0.25 \pm 0.02$  (stat.)

(all  $g_1$  data, including  $g_1^d$  from COMPASS)

\*  $\Delta \Sigma (\overline{MS}) = 0.22 \pm 0.03$  (stat.)

(all  $g_1$  data, except COMPASS)

COMPASS data:  
- increase  $\Delta \Sigma$  (as expected) from  $g_1^d$   
- slight reduction of stat. error

- Statistical errors: Errors on parameters in present fit (15)

- Not quoted: systematic effects due to change in parametrisation, ref.  $Q^2$ , Nr. parameters...

- General assumption:

Parametrisations valid over the range of the data remain valid over the full range of x

⇒ **MOMENTS**



②  $\Delta G$  at  $Q^2 = 3 \text{ GeV}^2$  from NLO fit in  $\overline{\text{MS}}$  scheme

$\Delta G = 0.4 \pm 0.2$  (stat.)  $\pm ?$  (syst.)

- Statistical error = 15 from present fit  
(3 param. in  $\Delta G(x)$ )

- Systematic error (under study)

- parametrisation, ref  $\propto Q^2$
- different fitting programs (moments,  $(x, Q^2)$ )
- $\overline{\text{MS}}$  vs. other schemes
- ⋮

Validity of parametrisation outside range of data?

Another approach: direct measurement from high-pt events

NEXT TALK

(by Yann Beolfor)

COMPASS hi-pt

$\Delta G / G = 0.024 \pm \underline{0.089}$  (stat.)  $\pm 0.057$  (syst.)

$(0.065 \leq x_g \leq 0.175, Q^2 \approx 3 \text{ GeV}^2)$



$(G \approx 12-13)$

2 Complementary approaches to  $\Delta G$

<u>QCD fits</u>	<u>High-pt events</u>
<u>World data on <math>g_1</math></u> (200 points, 12 from COMPASS)	<u>COMPASS</u> Hadron events
DIS	$Q^2 < 1 \text{ GeV}^2$
Needs <u>input</u> param <sup>s</sup> of Polarised pdf's	Large contribution of <u>resolvable <math>\gamma</math>'s</u>
<u>Indirect</u> access to $\Delta G$ through $Q^2$ evolution of $g_1$	<u>Direct</u> access to $\Delta G$ in PGF events
NLO analysis	LO analysis
More sensitive to <u><math>\int \Delta G</math></u> than to detailed shape	Access to $\Delta G$ in <u>limited range of <math>x</math></u>
Needs control of <u>systematics</u>	Needs <u>precision</u>



2 results on  
 $\Delta G (0.095, Q^2 \approx 3)$

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Very good agreement