# First high $p_{T}$ asymmetry for $\frac{\Delta G}{G}$ at COMPASS 

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CEA/Saclay

- Measurement of the gluon polarization $\frac{\Delta G}{G}$
- Helicity asymmetry of the photon-gluon fusion $\rightarrow \frac{\Delta G}{G}$
- High $p_{T}$ tagging $\rightarrow$ background reduction
- $\operatorname{High} p_{T}$ analysis
- Measurement of $A_{\|} / D$
- Selection of the high $p_{T}$ data sample
- False asymmetries $\rightarrow$ systematic error on $A_{\|} / D$
- Results


## Measurement of $\frac{\Delta G}{G}$ : PGF

Photon-Gluon Fusion (PGF)


Cross-section helicity asymmetry :

$$
A_{p g f}^{\mu N} \equiv \frac{\Delta \sigma_{p g f}^{\mu N}}{\sigma_{p g f}^{\mu N}} \equiv \frac{\sigma_{p g}^{\mu \uparrow N \downarrow}-\sigma_{p g f}^{\mu \uparrow N \uparrow}}{\sigma_{p g f}^{\mu \uparrow N \downarrow}+\sigma_{p g f}^{\mu \uparrow \downarrow}}
$$

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$$

Phase space element ( $\xi, \hat{s}, \ldots$ ) :

$$
\begin{aligned}
d \Delta \sigma_{p g f}^{\mu N} & =d \Delta \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots) \Delta G(\xi, \hat{s}), \\
d \sigma_{p g f}^{\mu N} & =d \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots) G(\xi, \hat{s}) .
\end{aligned}
$$

- $\Delta G(\xi, \hat{s}), G(\xi, \hat{s})$ gluon distribution functions.
- $d \Delta \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots), d \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots)$ differential cross-sections for the $\mu g$ interaction


## Measurement of $\frac{\Delta G}{G}$ : PGF

Photon-Gluon Fusion (PGF)


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$$

Phase space element ( $\xi, \hat{s}, \ldots$ ) :

$$
\begin{aligned}
\Delta \sigma_{p g f}^{\mu N} & =\int d \Delta \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots) \Delta G(\xi, \hat{s}) \\
\sigma_{p g f}^{\mu N} & =\int d \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots) G(\xi, \hat{s})
\end{aligned}
$$

- $\Delta G(\xi, \hat{s}), G(\xi, \hat{s})$ gluon distribution functions.
- $d \Delta \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots), d \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots)$ differential cross-sections of the hard process.


## Measurement of $\frac{\Delta G}{G}$ : PGF

Photon-Gluon Fusion (PGF)


Cross-section helicity asymmetry :

$$
A_{p g f}^{\mu N}=\frac{\int d \Delta \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots) \Delta G(\xi, \hat{s})}{\int d \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots) G(\xi, \hat{s})}
$$

- Analysing power :

$$
\hat{a}_{L L}^{p g f}(\xi, \hat{s}, \ldots)=\frac{d \Delta \sigma_{p g f}^{\mu g}}{d \sigma_{p g f}^{\mu g}} .
$$

$$
\begin{aligned}
A_{p g f}^{\mu N} & =\frac{\int d \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots) \hat{a}_{L L}^{p g f} G(\xi, \hat{s}) \frac{\Delta G(\xi, \hat{s})}{G(\xi, s)}}{\int d \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots) G(\xi, \hat{s})} \\
& =\frac{\int d \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots) G(\xi, \hat{s}) \hat{a}_{L L}^{p g f}}{\int d \sigma_{p g f}^{\mu g}(\xi, \hat{s}, \ldots) G(\xi, \hat{s})} \times \frac{\Delta G}{G} \\
& =\left\langle\hat{a}_{L L}^{p g f}\right\rangle \frac{\Delta G}{G}
\end{aligned}
$$

## Measurement of $\frac{\Delta G}{G}$ : High $p_{T}$ cut


$\sigma_{l o d i s} \propto \alpha$
$+$

$\sigma_{q c d c} \propto \alpha \alpha_{s}$
$+$

$\sigma_{p g f} \propto \alpha \alpha_{s}$
C.Bernet - High $p_{T}$ events for $\frac{\Delta G}{G}$ at COMPASS (28/01/2004) - p.4/2

## Measurement of $\frac{\Delta G}{G}$ : High $p_{T}$ cut


C.Bernet - High $p_{T}$ events for $\frac{\Delta G}{G}$ at COMPASS (28/01/2004) - p.5/2

## Measurement of $\frac{\Delta G}{G}:$ High $p_{T}$ cut

The measured helicity of the total cross-section contains :

- the PGF asymmetry,
- a background asymmetry (lodis $+q c d c+\ldots$ )

$$
A_{\|}^{\mu d \rightarrow h h}=\frac{S}{N}\left\langle\hat{a}_{L L}^{p g f}\right\rangle \frac{\Delta G}{G}+\left(1-\frac{S}{N}\right) A_{B G}^{\mu N}
$$

- $\frac{S}{N}$ fraction of PGF events,
- $\left\langle\hat{a}_{L L}^{p g f}\right\rangle$ average analysing power,
- $A_{B G}^{\mu N}$ background asymmetry.
calculated in a Monte-Carlo simulation


## Asymmetry measurement



Raw counting rate asymmetry :

$$
\begin{aligned}
A_{\text {raw }} & =\frac{N^{\uparrow \downarrow}-N^{\uparrow \uparrow}}{N^{\uparrow \downarrow}+N^{\uparrow \uparrow}}=-\frac{N_{u}-N_{d}}{N_{u}+N_{d}} \\
& =\left\langle P_{t} P_{b} f D\right\rangle \frac{A_{\|}^{\mu d \rightarrow h h}}{D}
\end{aligned}
$$

$P_{t} \quad$ target polarization
$P_{b}$ beam polarization
$f$ dilution factor of the target
$D$ depolarization factor of the photon

## Asymmetry measurement



Raw counting rate asymmetry :

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& =\left\langle P_{t} P_{b} f D\right\rangle \frac{A_{\|}^{\mu d \rightarrow h h}}{D}
\end{aligned}
$$

Acceptance asymmetry $\Rightarrow$ bias.

## Asymmetry measurement



- 8 hours of data taking


## Asymmetry measurement



- 8 hours of data taking
- field rotation
- adiabatic
- $\sim 20$ minutes


## Asymmetry measurement



- 8 hours of data taking
- field rotation
- adiabatic
- $\sim 20$ minutes
- 8 hours of data taking


## Asymmetry measurement



$$
\begin{aligned}
A_{\text {raw }} & =-\frac{1}{2}\left(\frac{N_{u}-N_{d}}{N_{u}+N_{d}}\right. \\
& =\left\langle P_{t} P_{b} f D\right\rangle \frac{A_{\|}^{\mu d \rightarrow h h}}{D}
\end{aligned}
$$

$$
\left.-\quad \frac{N_{u}^{\prime}-N_{d}^{\prime}}{N_{u}^{\prime}+N_{d}^{\prime}}\right)
$$

This equation

- averages $\frac{A_{\|}}{D}$
- cancels the acceptance asymmetry.


## Asymmetry measurement


C.Bernet - High $p_{T}$ events for $\frac{\Delta G}{G}$ at COMPASS (28/01/2004) - p.9/2

## Event Selection



The primary vertex contains

- $\mu, \mu^{\prime}$ (identified by hits behind the absorber),
- at least 2 hadron candidates.

It is located in one of the target cells.

## Event Selection - hadron ID


muons are removed by requiring $E_{\text {cal }} / p>0.3$.

## Event Selection - hadrons cuts



- High $p_{T}$ cut
- $p_{T 1}, p_{T 2}>0.7 \mathrm{GeV} / \mathrm{c}$
- $p_{T 1}^{2}+p_{T 2}^{2}>2.5 \mathrm{GeV}^{2} / \mathrm{c}^{2}$
- Vector mesons are removed
- $m\left(h_{1} h_{2}\right)>1.5 \mathrm{GeV} / \mathrm{c}^{2}$
- Products of the target fragmentation are removed
- $x_{F}>0.1$
- $z>0.1$


## Event Selection - inclusive cuts




- Factorisation ensured by the high $p_{T}$ cut
- no $Q^{2}$ cut.
- Low $D$ events removed
- $y>0.4$
- Events strongly affected by radiative effects removed
- $y<0.9$


## Event Selection - target cuts


muons are required to cross both target cells

$$
\Rightarrow \phi_{u}=\phi_{d}
$$

## False asymmetries - definition

$$
\frac{A_{\|}}{D}=-\frac{1}{2\left\langle P_{t} P_{b} f D\right\rangle}\left(\frac{N_{u}-N_{d}}{N_{u}+N_{d}}-\frac{N_{u}^{\prime}-N_{d}^{\prime}}{N_{u}^{\prime}+N_{d}^{\prime}}\right)
$$

- The acceptance asymmetry cancels only if :

$$
\left(\frac{a_{u} \mathcal{L}_{u}}{a_{d} \mathcal{L}_{d}}\right)=\left(\frac{a_{u} \mathcal{L}_{u}}{a_{d} \mathcal{L}_{d}}\right)^{\prime},
$$

- $\mathcal{L}=\phi n$
- $\mu$ crosses both target cells $\Rightarrow \phi_{u}=\phi_{d}$.

$$
\left(\frac{a_{u} n_{u}}{a_{d} n_{d}}\right)=\left(\frac{a_{u} n_{u}}{a_{d} n_{d}}\right)^{\prime} .
$$

- If $a_{u} / a_{d}$ or $n_{u} / n_{d}$ varies during the field rotation : false asymmetries
- "correlated" $\Rightarrow$ bias.
- "random" $\Rightarrow$ increase of statistical error.
- any variation = "correlated" + "random"


## False asymmetries - correlated

$$
A_{+}=-\frac{1}{2\left\langle P_{t} P_{b} f D\right\rangle}\left(\frac{N_{u}-N_{d}}{N_{u}+N_{d}}-\frac{N_{u}^{\prime}-N_{d}^{\prime}}{N_{u}^{\prime}+N_{d}^{\prime}}\right)=\left(\frac{A_{\|}}{D}\right)^{\mu d \rightarrow h h}+A_{c o r}
$$



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$$
A_{+}=-\frac{1}{2\left\langle P_{t} P_{b} f D\right\rangle}\left(\frac{N_{u}-N_{d}}{N_{u}+N_{d}}-\frac{N_{u}^{\prime}-N_{d}^{\prime}}{N_{u}^{\prime}+N_{d}^{\prime}}\right)=\left(\frac{A_{\|}}{D}\right)^{\mu d \rightarrow h h}+A_{c o r}
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$$



$$
A_{-}=+\frac{1}{2\left\langle P_{t} P_{b} f D\right\rangle}\left(\frac{N_{u}-N_{d}}{N_{u}+N_{d}}-\frac{N_{u}^{\prime}-N_{d}^{\prime}}{N_{u}^{\prime}+N_{d}^{\prime}}\right)=\left(\frac{A_{\|}}{D}\right)^{\mu d \rightarrow h h}-A_{c o r}
$$

## False asymmetries - correlated

$$
\begin{array}{ccc}
\text { Periods } & \text { Microwave setup } & \text { Measured asymmetry } \\
P 2 D, P 2 E, P 2 F, P 2 G+ & + & A_{+}=\frac{A_{\|}}{D_{\|}}+A_{\text {cor }} \\
P 2 A 2, P 2 G- & - & A_{-}=\frac{A_{\|}}{D}-A_{\text {cor }}
\end{array}
$$

- If we measure $A_{+}$and $A_{-}$:

$$
\begin{aligned}
\frac{A_{\|}}{D} & =\frac{1}{2}\left(A_{+}+A_{-}\right), \\
A_{\text {cor }} & =\frac{1}{2}\left(A_{+}-A_{-}\right) .
\end{aligned}
$$

- $A_{c o r}$ cancels in the arithmetic average of $A_{+}$and $A_{-}$. but we do a weighted average $\Rightarrow A_{\text {cor }}$ cancels partially.
- $A_{\text {cor }}$ must be measured.
remaining fraction $\rightarrow$ systematic error on $\frac{A_{\|}}{D}$.


## False asymmetries - Iow $p_{T}$ sample

- high $p_{T}$ sample $\rightarrow$ no $A_{\text {cor }}$ observed.
$\Rightarrow A_{\text {cor }}$ is smaller than the statistical error. This does not mean that it is negligible.
- definition of the low $p_{T}$ sample :
- $p_{T}^{2}<0.5(\mathrm{GeV} / \mathrm{c})^{2}$,
- no cut on $m\left(h_{1} h_{2}\right)$.
- $Q^{2}<0.5(\mathrm{GeV} / \mathrm{c})^{2}$,
- no cut on $x_{F}$, nor $z$.
- all other cuts as in the high $p_{T}$ sample.
$\rightarrow 250$ times more events.


## False asymmetries - low $p_{T}$ sample


wide

optimal


## False asymmetries - low $p_{T}$ sample

wide target cuts

Low $\mathrm{p}_{\mathrm{T}}$ asymmetry


## False asymmetries - low $p_{T}$ sample

optimal target cuts


## False asymmetries - low $p_{T}$ sample

tight target cuts


## False asymmetries - low $p_{T}$ sample

Field


$$
\frac{n_{u}}{n_{d}}=1
$$

## False asymmetries - IOW $p_{T}$ sample



$$
\frac{n_{u}}{n_{d}}>1
$$

- The target moves when the field is reversed
$\leftarrow$ the field of the target solenoide tends to align on the fringe field of the spectrometer dipole.


## False asymmetries - low $p_{T}$ sample



$$
\frac{n_{u}}{n_{d}}=1
$$

- The target moves when the field is reversed
$\leftarrow$ the field of the target solenoide tends to align on the fringe field of the spectrometer dipole.
- Tighter target cuts remove this effect.


## False asymmetries - low $p_{T}$ sample



$$
\frac{n_{u}}{n_{d}}=1
$$

A $300 \mu \mathrm{~m}$ target movement has been measured.

- Enough to explain the false asymmetry observed with the wide cuts.
- Explains why :
- optimal cuts are enough to remove this false asymmetry
- tight cuts have no effect.


## False asymmetries - low $p_{T}$ sample

- remaining correlated false asymmetry with the optimal target cuts :

$$
A_{\text {cor }}=\frac{1}{2}\left(A_{+}-A_{-}\right)=0.0043 \pm 0.0023 .
$$

- remaining correlated false asymmetry after weighted average :

$$
A_{\text {cor }}=0.0018 \pm 0.0010
$$

## False asymmetries - low $p_{T}$ sample



- optimal target cuts


## False asymmetries - low $p_{T}$ sample



- $+\mu$ wave : $\frac{A_{\|}}{D}=A_{+}-A_{\text {cor }}$
- $-\mu$ wave : $\frac{A_{\|}}{D}=A_{-}+A_{\text {cor }}$
- $\frac{A_{\|}}{D}$ does not depend on the $\mu$ wave setup (by definition)
- the fluctuations of $\frac{A_{\|}}{D}$ are due to :
- statistics
- the uncorrelated false asymmetry $A_{\text {uncor }}$


## False asymmetries - low $p_{T}$ sample



- The 6 points are compatible
- $\chi^{2} / n d f=2.35 / 6$
- $\chi^{2}$ probability : $88 \%$
$\rightarrow A_{\text {uncor }}$ is smaller than the statistical error.
- if we assume $A_{\text {uncor }}<0.01$ for each period:

$$
A_{\text {uncor }}<0.004 \text {. }
$$

## False asymmetries - conclusion

- We obtained, with the low $p_{T}$ sample :

$$
\begin{aligned}
A_{\text {cor }} & =0.0018 \pm 0.0010 . \\
A_{\text {uncor }} & <0.004 .
\end{aligned}
$$

- Studies show that these results also hold for the hight $p_{T}$ sample.
- Other approaches have been followed to test false asymmetries, at high and low $p_{T}$.
- asymmetry calculated for upper, lower Jura, Saleve part of the spectrometer.
- asymmetry calculated between the 2 halves of a single target cell
$\rightarrow$ no problem.
We thus chose, conservatively :

$$
\delta\left(\frac{A_{\|}}{D}\right)^{\mu d \rightarrow h h}(\text { syst. })=0.01
$$

## Conclusion

For 2002 data, the preliminary asymmetry of the total cross-section for the production of 2 high $p_{T}$ hadrons is :

$$
\left.\left(\frac{A_{\|}}{D}\right)^{\mu d \rightarrow h h}=-0.065 \pm 0.036(\text { stat. }) \pm 0.01 \text { (syst. }\right)
$$

- radiative effects are not taken into account. (should be small for semi-inclusive DIS).
- the systematic error contains only the contribution of false asymmetries.
(other sources should be $\propto\left(\frac{A_{\|}}{D}\right)^{\mu d \rightarrow h h}$, hence small)
- projected statistical error (including 2003 and 2004) : 0.018
- A monte-carlo simulation is under way to extract $\frac{\Delta G}{G}$ from this result.

