Prospects for the Primakoff measurement of the pion polarizability at COMPASS

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Using high rate capability in conjunction with high precision, COMPASS can significantly contribute to the physics studied at very low momentum transfers as in Primakoff reactions, that is, the scattering of hadrons off the quasi-real photons forming the Coulomb field of nuclei. Most importantly, it has the unique chance to clarify the question of the pion polarisability, where an unprecedented level of precision is in reach.

6th International Workshop on Chiral Dynamics
July 6-10 2009
Bern, Switzerland

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†work supported by the DFG cluster of excellence “Origin and Structure of the Universe” (www.universe-cluster.de)
1. Pion polarisability

The electric and magnetic dipole polarisabilities of the charged pion, $\alpha_\pi$ and $\beta_\pi$, describe the interaction of the pion with external electromagnetic fields in the low-field quasi-static limit. They are fundamental parameters of pion physics, and the comparison of theoretically predicted and directly measured values provides a stringent test for various theoretical approaches like dispersion or quantum chromodynamics (QCD) sum rules and quark confinement models. These theoretical predictions disagree with each other and lie in the range $(2 - 8) \times 10^{-4}$ fm$^3$ for the absolute values of $\alpha_\pi$ and $\beta_\pi$ [1, 2, 3].

In the systematic QCD low-energy expansion of chiral perturbation theory ($\chi$PT), the pion is interpreted as the Goldstone boson of the underlying chiral symmetry, and its experimentally determined properties test this systematic approach. $\chi$PT has established a firm prediction of the pion polarisabilities, including higher-order effects and an error estimate (see [4, 5]). $\alpha_\pi - \beta_\pi = (5.7 \pm 1.0) \times 10^{-4}$ fm$^3$. The sum of the pion polarisabilities is small, taking a non-zero value only starting from a 2-loop $\chi$PT calculation, $\alpha_\pi + \beta_\pi = 0.16 \times 10^{-4}$ fm$^3$.

The actual dispute on the compatibility of $\chi$PT with the dispersion relation approach for the pion polarisability (see e.g. these proceedings [6, 7]) demonstrates the urgent need for experimental clarification.

The method of radiative $\pi^+$ photoproduction off the proton, most recently used at MAMI [8], has confirmed the earlier finding of the Serpukhov experiment [9], employing the Primakoff method (cf. Sec.2). In the MAMI data, as in the Serpukhov, the pion polarisability is found about twice as large as predicted by $\chi$PT.

2. Primakoff measurement of pion Compton scattering

A high-energetic pion beam allows to study scattering reactions within the pion lifetime. Scattering off nuclei at small momentum transfer $Q^2$ to the nucleus, in the range $\leq 0.001$ GeV$^2$/c$^2$ dominates the electromagnetic interaction, as the small momentum transfer corresponds to large impact parameters compared to the extension of the nucleus. So effectively, in this regime the

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**Figure 1**: Pion Compton reaction (right graph) embedded in the Primakoff reaction (left graph) on a nucleus of charge $Z$. Kinematical quantities in the laboratory and the CM scattering angle are indicated.
pions scatter off photons of the Coulomb field of the nucleus, which is referred to as Primakov reaction [10], and in the process
\[ \pi^- Z \rightarrow \pi^- Z \gamma \] (2.1)
the pion Compton scattering reaction is embedded, as depicted in Fig. 1. The cross section for this reaction, treating the nuclear vertex in the equivalent photon approximation, is given by
\[ \frac{d\sigma}{ds dt dQ^2} = \frac{\alpha}{\pi(s-m^2_\pi)} \cdot F_2^Z(Q^2) \cdot \frac{Q^2 - Q^2_{\min}}{Q^4} \cdot \frac{d\sigma_{\pi\gamma}}{dt} \] (2.2)
where \( Q_{\min} = (s-m^2_\pi)/2E_{\text{beam}} \), \( s \) and \( t \) are the Mandelstam variables in the \( \pi\gamma \) system, and the pion polarisabilities enter via
\[ \frac{d\sigma_{\pi\gamma}}{d\Omega_{\text{cm}}} = \frac{\alpha^2(z_+^2 + m^2_\pi z_-^2)}{s(s z_+ + m^2_\pi z_-)^2} \cdot \frac{\alpha m^3_\pi(s-m^2_\pi)^2 [z_-(\alpha_\pi - \beta_\pi) + \frac{s}{m^2_\pi} z_+^2 (\alpha_\pi + \beta_\pi)]}{4s^3(s z_+ + m^2_\pi z_-)} \] (2.3)
with \( z_\pm = 1 \pm \cos \theta \) and \( \theta \) the scattering angle in the CM system of the outgoing \( \pi\gamma \) pair.

The effect of the difference of electric and magnetic polarisability \( \alpha_\pi - \beta_\pi \) is strongest under backward angles (for this reason, this quantity is also referred to as backward polarisability), while the forward polarisability \( \alpha_\pi + \beta_\pi \) influences the cross section at large \( \cos \theta \). While the latter forward polarisability is expected to be small values (cf. Sec. 1), it is enhanced in the cross section by the \( s^2/m_\pi^4 \) factor. Consequently, measuring the energy and angular dependence of the cross section allows an extraction of the two polarisabilities separately.
The polarisability effect as given by Eq. 2.3 is depicted in Fig. 2. For the case of COMPASS kinematics with a 190 GeV incoming pion beam, Fig. 3 shows the kinematical relation with the laboratory quantities of the produced photon. The physically interesting region includes photons with energies in the range from 20 to 180 GeV at angles from 0 to about 5 mrad with respect to the incoming beam pion direction, referring to the physically interesting region $-1 < \cos_{\text{CM}} < 0.6$ and $1.5 < \sqrt{s} < 4$.

3. Primakoff measurements at COMPASS

The COMPASS experiment at CERN is a 2-stage magnetic spectrometer equipped with modern detector and data acquisition technology for large-acceptance measurements with high intensity beams and high interaction rates. The setup is described in [11]. For measuring Primakoff reactions as process 2.1, two features of COMPASS play a key role: Firstly, the excellent tracking capability for the incoming and outgoing pions, which allows the determination of the scattering angle with a precision better than 50 $\mu$rad, and secondly the electromagnetic calorimetry for the determination of the energy and direction of the produced photons. Furthermore, the elaborated muon identification system permits the separation of muon-induced reactions similar to 2.1. The possibility to switch to muon beam can be used in order to study systematic effects, since the cross section for the analogous process for the point-like muons is fully determined by QED.

The study of Primakoff reactions in COMPASS was started in a short pilot run with hadron beams in 2004 using 190 GeV $\pi^-$ and $\mu^-$ beams impinging on a longitudinally segmented Pb target. Additional samples with Cu and C targets were also collected. The total amount of Primakoff events with pion beam from the lead target was about 60,000 for photon energies above 40 GeV.
Instabilities in the amplification of many cells of the electromagnetic calorimeter connected with saturation effects, and some inefficiencies in the scattered pion triggering system, turned out to induce significant systematic uncertainties in the measurement and at the end prevented the extraction of a reliable value for the pion polarisabilities from the 2004 data. However, the measurement allowed to address the full experimental procedure and established the feasibility of the measurement.

The most important achievements of the present analysis are, the selection of Primakoff reactions by the request of exclusive $\pi\gamma$ events (Fig. 4) and the identification of the Primakoff peak in the $Q^2$-distribution (Fig. 5). By normalizing on the integrated luminosities collected with the different targets, we also found that the strength of the Primakoff peak follows the theoretically expected $Z^2$-dependence. On the other hand, we determined the important parameters of our setup such as resolutions and Monte Carlo control of detector efficiencies and identified the main sources of background, both, non-separable physics processes (the ratio of Primakoff signal to diffractive background for different targets as presented in Fig. 5), and backgrounds stemming from beam impurities for which a set of procedures for background reduction has been developed.

Corrections to the pure tree-level Primakoff cross section come from the Compton vertex, multiple photon exchange, vacuum polarization and nuclear charge screening by atomic electrons and have also been calculated. It was found that the multiple photon exchange introduces a large correction (see [12, 13]) for the lead target, estimated to be about 5%, making it favorable to measure on lighter nuclei like Nickel where this correction lies below 1%. The transition region to higher $Q^2$ was investigated within the Glauber model in the work of [14, 15], in which the influence of the strong interaction on the $Q^2$ spectrum is addressed.

4. Prospects for new measurements

In November 2009, a second data taking period for Primakoff measurements is ongoing. The readout electronics of the electromagnetic calorimeter has been refurbished, and was used in the 2009 data taking of diffractive reactions aiming at meson spectroscopy, where it has proven a much
better performance as compared to the 2004 data as presented in Sec. 3. An additionally installed laser system permits the control of the amplifications of the individual cells during the beam time.

A new component is the digital calorimeter trigger, it delivers a trigger signal as a function of the energy sum of the relevant cells of the calorimeter, which makes it an ideal tool for the intended Primakoff measurement.

The planned luminosity exceeds the statistics of the previous COMPASS data taken in 2004, which turned out to be comparable to the Sepukhov statistics, by about a factor of 10. This will allow the determination of the polarisability difference $\alpha_{\pi} - \beta_{\pi}$ to a precision comparable to the theoretical uncertainty as outlined in Sec. 1, assuming a negligible contribution from the sum of polarisabilities and so, introducing the constraint $\alpha_{\pi} + \beta_{\pi} = 0$ in the analysis. This, effectively, means that it is sufficient to observe the deviation of the cross section from the pointlike expectation with increasing energy of the produced photon only, integrating over the angular dependence.

It will be more ambitious to disentangle the magnetic and electric contribution separately, since the cross section behaviour must then be studied in both its dependence on the energy and angles of the outgoing particles, as explained in Sec. 2.

In order to reach a comparable statistical error on the two polarisabilities independently, a beam time of about 4 weeks at COMPASS is to be envisaged. During such a new beam time, it will be possible to obtain also first data on Compton scattering of the charged kaon, using also the kaon component of the incoming beam. In analogy to the described method for the pion, the kaon polarisability could be determined for the first time.

References

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